

Latent Variable Machine Learning Algorithms: Applications in a Nuclear Physics Experiment

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Outline

1. Introducing the Active Target Time Projection Chamber (AT-TPC)
2. Challenges with traditional analysis of AT-TPC data - and the evangelization of Machine Learning
 - (i) Recap of central literature
 - (ii) Introducing thesis problem statements
3. An introduction to central Machine Learning concepts
4. The Auto-Encoder neural network
5. Results
6. Summary, Conclusion and Outlook

AT-TPC

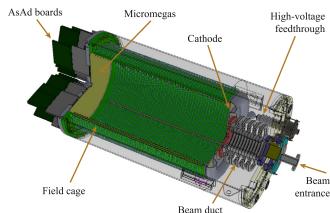


Figure: Diagram of the AT-TPC¹

The AT-TPC is an experiment set up at the rare isotopes facility on the Michigan State University campus. The AT-TPC is commissioned to capture reactions with exotic nuclei.

¹J. Bradt et al. "Commissioning of the Active-Target Time Projection Chamber". In: *Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment* 875 (2017), p. 65. DOI: 10.1016/J.NIMA.2017.09.013. URL: <https://www.sciencedirect.com/science/article/pii/S0168900217309683>

AT-TPC

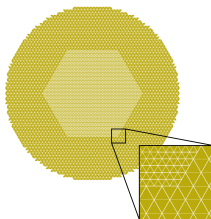


Figure: Detector pad plane of the AT-TPC²

Each triangle represents spatial discrete regions of the detector surface. The pad-plane consists of some 10^4 sensor pads on a circle with $r = 29cm$

²Bradt et al., "Commissioning of the Active-Target Time Projection Chamber".

AT-TPC Data

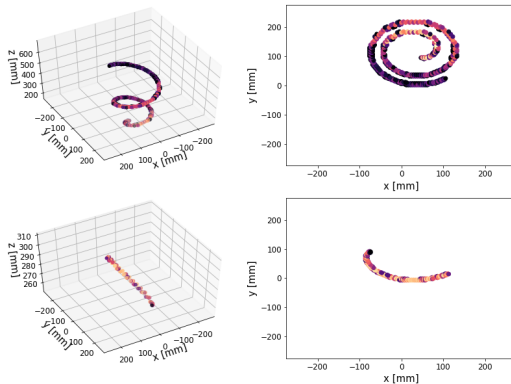
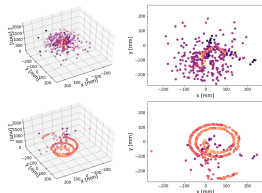
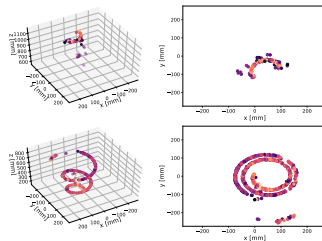


Figure: Simulated AT-TPC data in an experiment with ^{46}Ar

AT-TPC Data



(a) Unfiltered events from the ^{46}Ar experiment



(b) Noise-filtered events from the ^{46}Ar experiment

Significant noise levels in the experiment, from unknown sources.
Some 60% of the recorded events are from unidentified reactions.

Challenges with the AT-TPC

- I Expensive integration - for each event a fit is computed.
- II Assumptions of the integration technique:
 - (i) Each event is fit against parameters of the event of interest,
 - (ii) The integration is sensitive to Noise and Breaks in the tracks.
- III In some experiments researchers are unable to identify samples of the positive class of events.

The amount of data is also significant: the experiment generates on the order of 10^5 events per hour running.

Idea

Solve the problem by training deep neural networks.

Previous Work

- ▶ Work on applying ML to this data started with a supervised learning project by Kuchera et al.³.
- ▶ The authors explored a *supervised classification* problem of identifying reactions when ground-truth labels available.
- ▶ By fine tuning pre-trained networks the authors achieve very impressive performance.

One of the open questions is then, can we segment the events based on reactions without the ground truth labels?

³Michelle. P. Kuchera et al. "Machine learning methods for track classification in the AT-TPC". In: *Nuclear Instruments and Methods in Physics Research, Section A: Accelerators, Spectrometers, Detectors and Associated Equipment* 940 (2019), p. 156. DOI: 10.1016/j.nima.2019.05.097. URL: <https://linkinghub.elsevier.com/retrieve/pii/S0168900219308046>.

ML background

Machine Learning (ML) is an amorphous set of algorithms for pattern recognition and function approximation. Bred as a mix between computer science and statistical learning theory, it includes algorithms like:

- I Linear Regression

- II Logistic Regression

- III Random Forest Classifiers

- IV Genetic Algorithms

And many others...

Why machine learning

- I Builds on the work by Kuchera⁴.
- II Exploration of feasibility, modern computing resources has created a resurgence in ML with strong results from other fields.

⁴Kuchera et al., "Machine learning methods for track classification in the AT-TPC". 

Deep Learning

A special sub-branch of Machine Learning is the field of Deep Learning, or more broadly: Differentiable Programming

The premise of Deep Learning is to formulate an approximation to some unknown function $f(\mathbf{x})$ with a model, \hat{f} , that maintains some set of parameters $\{\theta\}$.

Some examples of the unknown function, $f(\mathbf{x})$, we would want to approximate are:

- (a) a Hamiltonian of a system
- (b) a function which determines the thermodynamic phase of a system
- (c) a function which identifies dog-species from a picture

Deep Learning: Neural Networks

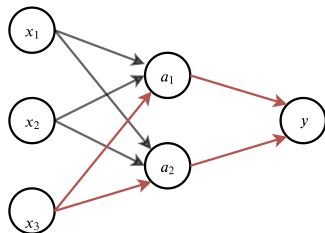
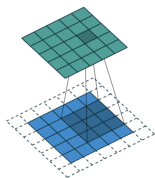


Figure: A neural network with three input nodes, two hidden nodes, and one output node

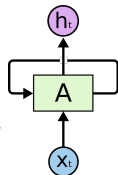
Each of the *activations* \mathbf{a} are computed as a matrix product fed through a nonlinear activation *activation function* g

$$\mathbf{a}^{[1]} = g(\mathbf{x}\boldsymbol{\theta}^{[1]})_D \quad (1)$$

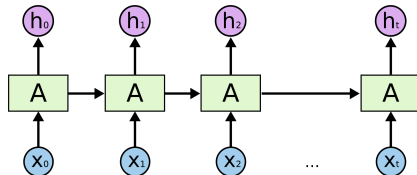
Deep Learning: Network Types



(a) Convolutional architecture capturing local structures⁵



=



(b) Recurrent architecture for serialized applications⁶

⁵Vincent Dumoulin and Francesco Visin. "A guide to convolution arithmetic for deep learning". In: (Mar. 2016). arXiv: 1603.07285. URL: <http://arxiv.org/abs/1603.07285>.

⁶Ma Jianqiang. *All of Recurrent Neural Networks - Jianqiang Ma - Medium*. URL: <https://medium.com/@jianqiangma/all-about-recurrent-neural-networks-9e5ae2936f6e> (visited on 11/13/2019).

Autoencoders

- ▶ Recall that we want to separate classes of reaction products
- ▶ Additionally - we assume that we have access to very little or no ground truth labelled data

Idea

Learn the distribution over the events through two nonlinear maps which compress and inflate a representation of the events.

Central Hypothesis

If we can create a compressed representation of an event from which we can reconstruct the even - the compression should be informative of the type of event that occurred.

Autoencoders

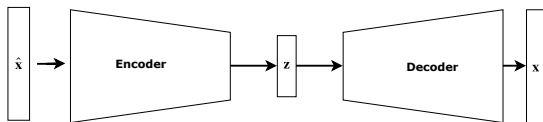


Figure: Autoencoder neural network schematic

An autoencoder is defined by an encoder/decoder pair of neural networks. We construct these such that

$$\dim(\hat{x}) \gg \dim(z), \quad (2)$$

and with the optimization objective

$$\mathcal{O} = \arg \min ||\hat{x} - \text{Decoder}(\text{Encoder}(\hat{x}))||_2^2. \quad (3)$$

Implementing details

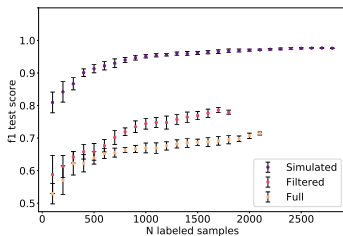
TBD

Experiment

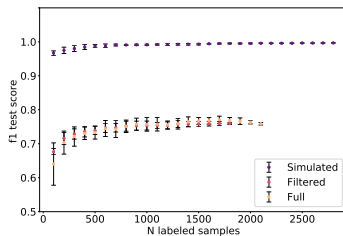
- ▶ We chose to represent the data as 2D projections, neglecting the z-axis.
- ▶ An autoencoder network is then fit to the events in an end to end manner.
- ▶ After training, we extract the compressed (or *latent*) expressions of the data.
- ▶ With varying amounts of labelled ground-truth data we fit a very simple classifier to the latent expressions

We wish to construct latent spaces that are as close to trivially separable, and so use a logistic regression classifier.

Results



(a) Performance for an autoencoder with a naive architecture



(b) Performance using a representation of the events as seen by a VGG16 network

$$\text{recall} = \frac{TP}{TP + FP}, \quad \text{precision} = \frac{TP}{TP + FN}. \quad (4)$$

The $f1$ score is defined as the harmonic mean of precision and recall for each class. Formally we define it as

$$f1 = 2 \frac{\text{precision} \cdot \text{recall}}{\text{precision} + \text{recall}}. \quad (5)$$

Clustering

- ▶ We demonstrated that we can construct high quality spaces that are linearly separable
- ▶ The next step then is a *clustering* task. Can we separate classes without knowing the ground truth labels?
- ▶ Clustering, while similar to classification have some principal differences.

We explored two autoencoder-based clustering algorithms, in addition to ordinary K-means clustering.

K-means clustering

- ▶ Ordinary K-means on the two-dimensional representations would obviously not be productive because of the dimensionality of the problem.
- ▶ Instead we try to cluster the representation of the events as seen by an image classifying algorithm: VGG16

With 8e3 output nodes the VGG16 representation is still very much high dimensional, but importantly it is sparse.

K-means results

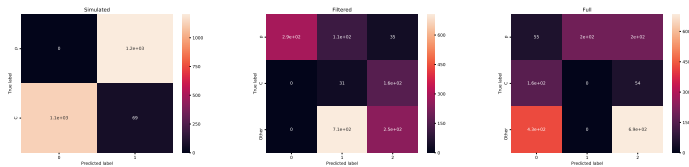
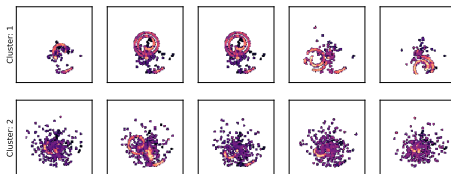


Figure: K-means clustering results using the VGG16 representation of the datasets

Cluster elements for clustering full data



Mixture of Autoencoders

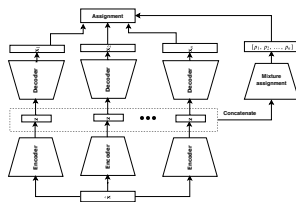
- ▶ One can also attempt clustering with Autoencoder based algorithms
- ▶ Niche field with only limited applications (MNIST, Reuters)

$$\mathcal{L}_x = \sum_j p_j^{(i)} \mathcal{C}(\mathbf{x}_j^{(i)}, \hat{\mathbf{x}}^{(i)})$$

$$S(\mathbf{p}^{(i)})_{\text{sample}} = - \sum_j p_j^{(i)} \log p_j^{(i)}$$

$$S(\{\mathbf{p}^{(i)}\}_i)_{\text{batch}} = \left(- \sum_j \bar{p}_j \log \bar{p}_j \right)^{-1},$$

$$\bar{\mathbf{p}} = \frac{1}{\beta} \sum_i^{\beta} \mathbf{p}^{(i)}$$



Deep Clustering Results

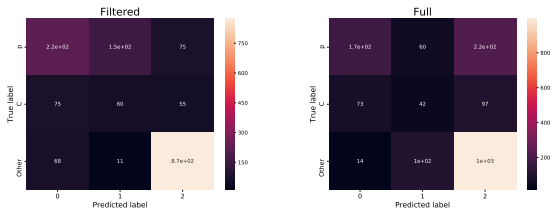
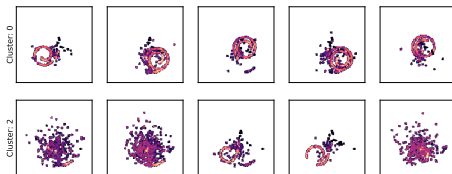


Figure: Top-performing mixae results for the real experimental data

Cluster elements for clustering of full data



Summary and Outlook

- ▶ We have shown that Autoencoder models are suitable for both semi-supervised and unsupervised applications.
- ▶ Autoencoder clustering has a fundamental challenge with issues of stability and convergence. We still need labelled samples to verify.
- ▶ Including physical parameters increases the quality of the latent space.

Neural network models clearly have a place in this analysis going forward: but connecting the analysis to the physical properties of the system remains a challenge to solve.