

# Forecasting Major Cryptocurrency Prices with SARIMAX

Yuxin (Corinna) Ma

April 2025

## 1 Introduction

Cryptocurrencies have emerged over the last decade as a highly dynamic—and notoriously volatile—asset class. Bitcoin, Ethereum, Solana and their peers can swing by tens of percent in a single trading day, driven by shifts in investor sentiment, technological developments, regulatory news, and broader macroeconomic forces. For traders, portfolio managers, and risk analysts, accurately forecasting short-term price movements in these digital assets remains an open and urgent challenge.

In this study, we tackle two key obstacles in cryptocurrency forecasting. First, we apply spectral filtering (notch-filtered Fourier transforms) to separate high-frequency noise from the underlying trend in each coin’s percentage-change series. Second, we enrich our predictive model by incorporating returns on the Standard & Poor’s 500 Composite Stock Price Index—as a proxy for traditional market sentiment—as an exogenous regressor in a SARIMAX framework. By marrying signal-processing techniques with modern time-series methods, we aim to capture both the idiosyncratic oscillations of each cryptocurrency and their broader market co-movements.

The expected value of this analysis is threefold:

1. **Improved Short-Horizon Forecasts:** Demonstrate that combining FFT-based detrending with a SARIMAX model—augmented by S & P 500 returns—yields more accurate 10–100 day price forecasts than naïve benchmarks.
2. **Practical Toolkit:** Provide a reproducible, end-to-end pipeline—from data cleaning and interpolation, through spectral filtering, to exogenous time-series modeling—that practitioners can adapt for risk management, algorithmic trading, or portfolio optimization in the crypto space.

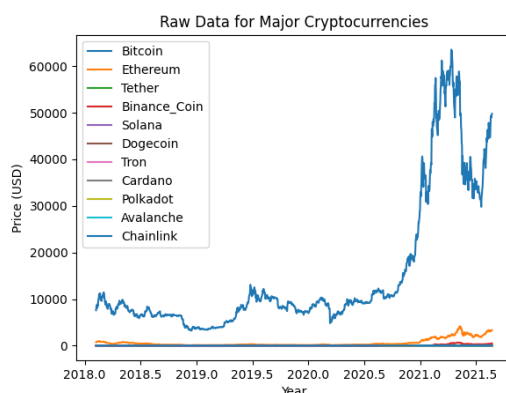
## 2 Method & Data Processing

Our forecasting pipeline combines signal-processing techniques with classical time-series modeling and exogenous regression. Below we describe each component, the rationale for its use, and briefly note alternative approaches we considered.

### 2.1 Data Preprocessing & Interpolation

#### 2.1.1 Loading and Data Parsing

We began by loading daily cryptocurrency prices (2018–2021) and S&P 500 historical data.



(a) Raw Price Data for Major Cryptocurrencies from 2018 to 2021

### 2.1.2 Filtering to Common Time Window

Since some coins began trading later than others, we restricted every series to dates  $\geq$  February 2018 in terms of decimal years—where all cryptocurrencies of our interest had active data—and computed a corresponding decimal-year index for easy plotting.

### 2.1.3 Percent-Change Calculation

For each coin, we took the first observed 2018-period price as a reference and computed

$$\text{Percent\_Change}_t = \frac{P_t - P_{ref}}{P_{ref}} \times 100\%$$

turning raw USD price into a normalized return series. This step makes different coins—whose price levels span orders of magnitude—directly comparable by expressing all moves on a common percentage scale (top-right 5).

### 2.1.4 Log-Transformation of Prices

We also created a `LogPrice` column via

$$\text{LogPrice}_t = \ln(P_t)$$

Taking the natural logarithm stabilizes variance (so that large absolute jumps at high prices don't dominate the model) and turns multiplicative price moves into additive ones (bottom-right 5). In practice, this makes ARIMA-style differencing and forecasting more numerically stable and interpretable: one unit of difference in log-price corresponds approximately to a  $100\% \times \Delta\%$  change. As we expect the price in cryptocurrencies follows an exponential increase/decrease manner, reverting into log-space ensures the data fits the additive properties of ARIMA model.

### 2.1.5 Handling Missing and Non-Trading Days

Because the financial markets close on weekends and holidays, the raw S&P 500 series contained gaps; we re-indexed it to a continuous calendar-daily and used a linear interpolation to fill missing Open, High, Low, Close, and derived MeanPrice values. A uniform daily index ensures that our exogenous and endogenous series align perfectly for model fitting and forecasting.

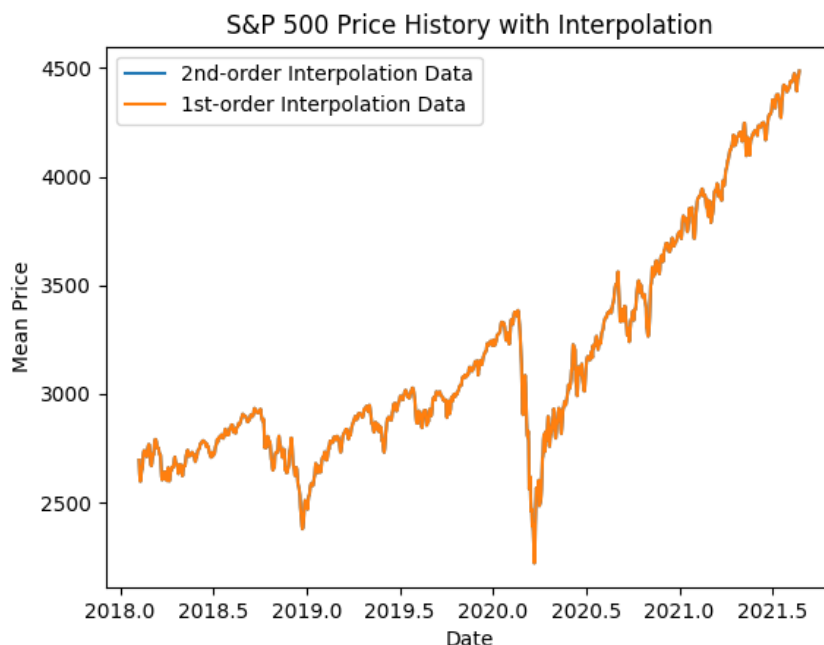


Figure 2: S&P Historical Price with Different Interpolation Methods

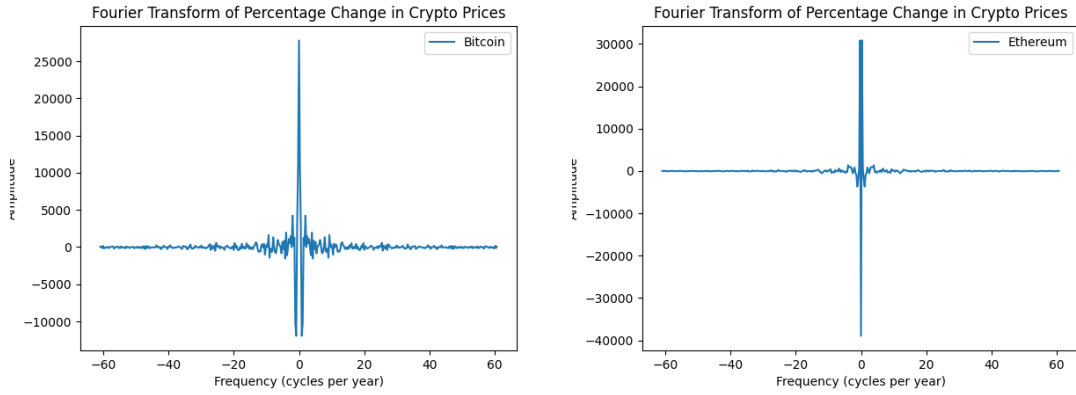
### 2.1.6 Alternative

A more complex forward-fill interpolation was tested, but 2nd-order polynomial interpolation produced approximately the same intermediate values.

## 2.2 Spectral Detrending & Noise Filtering

### 2.2.1 Windowed Fourier Transform

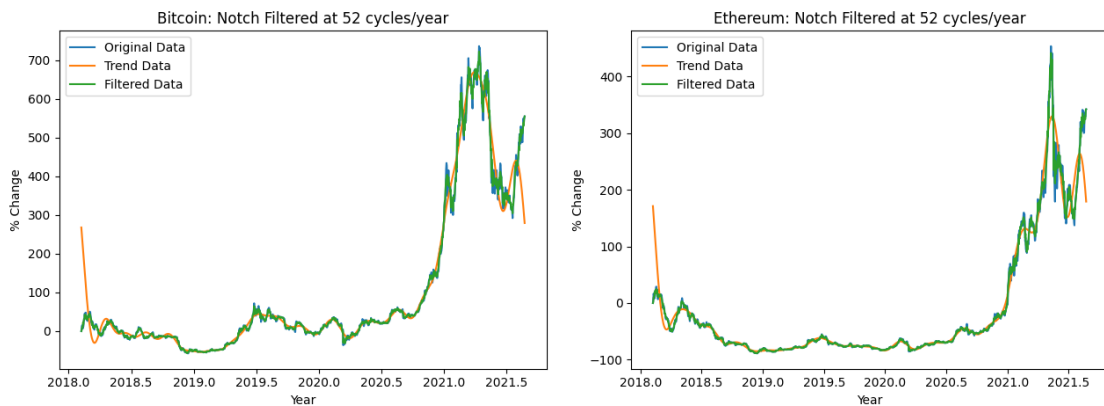
To isolate the underlying trend from high-frequency oscillations in each coin's percentage-change series, we applied a Hamming window from `scipy.signal` library, followed by a discrete Fourier transform. Two sample Fourier Transform is shown below, the rest of the transforms graph can be seen in the appendix.



(a) Fourier Transform of Percentage Change in Bitcoin Prices (b) Fourier Transform of Percentage Change in Ethereum Prices

### 2.2.2 Notch Filter

Figure 4 shows the magnitude spectrum of Bitcoin's percent-change series after applying a Hamming window. We zeroed out frequencies above 52 cycles/year to remove intra-weekly noise, then reconstructed the trend via inverse FFT and de-windowing. Here we just show the filtering result for Bitcoin and Ethereum, other cryptocurrency coin's data can be seen in the appendix.



(a) Notch Filtered Bitcoin Price at 52 cycles/year (b) Notch Filtered Ethereum Price at 52 cycles/year

Figure 4: Notch Filtered Results

### 2.2.3 Alternatives Rejected

- Polynomial Detrending: Too rigid, risks overfitting low-frequency drift. Non-uniform, cannot choose one degree that fits all cryptocurrencies.

## 2.3 Exogenous Variable Construction & Forecasting

### 2.3.1 S&P 500 Returns as Exogenous Input

We computed daily returns on the interpolated S&P 500 MeanPrice series to capture traditional market sentiment,

$$\text{MeanPrice}_t = \frac{1}{4}(\text{Open}_t + \text{High}_t + \text{Low}_t + \text{Close}_t)$$

Averaging across the day's highs and lows produces a smoother intradate aggregate than any single price alone.

From the interpolated `sp500['MeanPrice']` series, we calculate the return

$$\text{Return}_t = \frac{\text{MeanPrice}_t - \text{MeanPrice}_{t-1}}{\text{MeanPrice}_{t-1}}$$

The very first day in our window has no prior day, so we substitute a zero return to avoid missing data.

### 2.3.2 Forecasting Exogenous Series

Rather than using a constant mean, we built a separate SARIMAX(1,1,1) model on the S&P 500 returns to generate a forecast of future returns. Using `.get_forecast(steps=N)`, we produce an N-day ahead forecast of S&P 500 return. Because this forecast object carries its own date index, we can directly feed those predicted future returns as the exogenous inputs for our cryptocurrency models.

### 2.3.3 Alternative

1. In further research, we could employ more exogenous data series like trading volume & liquidity metrics. This would capture investor activity and can lead price moves, which could potentially lead to a more accurate prediction.
2. Alternatively, we could apply other forecasting techniques to the exogenous series—for example, we use the lagged predictions (e.g. take the opening value for the S&P 500 as the representing index for the day), or even machine learning regressors.
3. Because shifts in the S&P 500 and cryptocurrency markets may not occur simultaneously, we can compute lagged cross-correlations to identify lead-lag relationships and quantify how far one series tends to lead or lag the other.

## 2.4 SARIMAX Modeling and Grid Search

### 2.4.1 Model Specification

For each cryptocurrency, we fitted a seasonal ARIMAX model on the log-price series with the S&P 500 returns as an exogenous regressor.

$$y_t = \underbrace{\phi_1 y_{t-1} + \dots + \phi_p y_{t-p}}_{\text{AR}(p)} + \underbrace{\theta_1 \varepsilon_{t-1} + \dots + \theta_q \varepsilon_{t-q}}_{\text{MA}(q)} + \underbrace{X_t^\top \beta}_{\text{Exogenous S\&P 500 Return}} + \underbrace{s\text{-seasonal terms}}_{\text{Seasonality}} + \varepsilon_t$$

## 2.5 Grid Search over (p,d,q) & (P,D,Q,s)

Rather than manually chose orders, we performed a Bitcoin based grid search, where  $(p, d, q)$  each in  $\{0, 1, 2\}$  with seasonal period  $s = 12$ .

For each candidate, we fit `SARIMAX(y,exog,order=(p,d,q), seasonal_order=(P,D,Q,12))`. Record the model’s Bayesian Information Criterion.

## 2.6 Forecast Generation and Evaluation

### 2.6.1 Producing the Forecast

Using the fitted SARIMAX models and the forecasted S&P 500 exogenous inputs, we generated 100 day ahead price forecasts. Since our model is built on  $\ln(\text{Price})$ , we back-transforms and exponentiate:

$$\hat{P}_t = \exp(\ln \hat{P}_t), \quad CI_{\pm}(P)_t = \exp(CI_{\pm}(\ln P)_t).$$

## 3 Data

Our analysis draws on three primary time-series datasets:

### 1. Cryptocurrency Historical Data ("All.combined.csv")

**Content:** Daily Open, High, Low, Close, Volume and percent-change for 100+ cryptocurrencies.

**Period:** January 2018 – August 2021 (we subset to February 2018 onward so each “major” coin has data).

**Source & Access:** Sudalai Rajkumar (2019). *Cryptocurrency Price History* [CSV]. Kaggle. <https://www.kaggle.com/datasets/sudalairajkumar/cryptocurrencypricehistory>

### 2. Bitcoin Daily Close (NASDAQ)

**Content:** Ten-year history of Bitcoin’s daily closing prices, used to cross-validate and back-fill gaps in the Kaggle dataset.

**Source & Access:** Nasdaq (2025). *Bitcoin (BTC) Historical Data*. Retrieved April 2025 from [https://www.nasdaq.com/market-activity/cryptocurrency/btc/historical?page=11\&rows\\\_per\\\_page=100\&timeline=y10](https://www.nasdaq.com/market-activity/cryptocurrency/btc/historical?page=11\&rows\_per\_page=100\&timeline=y10)

### 3. S&P 500 Index Content:

Daily Open, High, Low, Close for the S&P 500 index, used to compute a smooth “MeanPrice” and derive daily returns as an exogenous regressor.

**Period:** February 2018 – August 2021 (matched to the crypto window)

**Source & Access:** Yahoo Finance (2025). *S&P 500 (GSPC) Historical Prices*. Retrieved April 2025 from <https://finance.yahoo.com/quote/\%5EGSPC/history>

## 4 Results and Analysis

### 4.1 Data Processing Results

After transforming the cryptocurrency prices as described in the method section, we get a relatively stationary result as shown below.

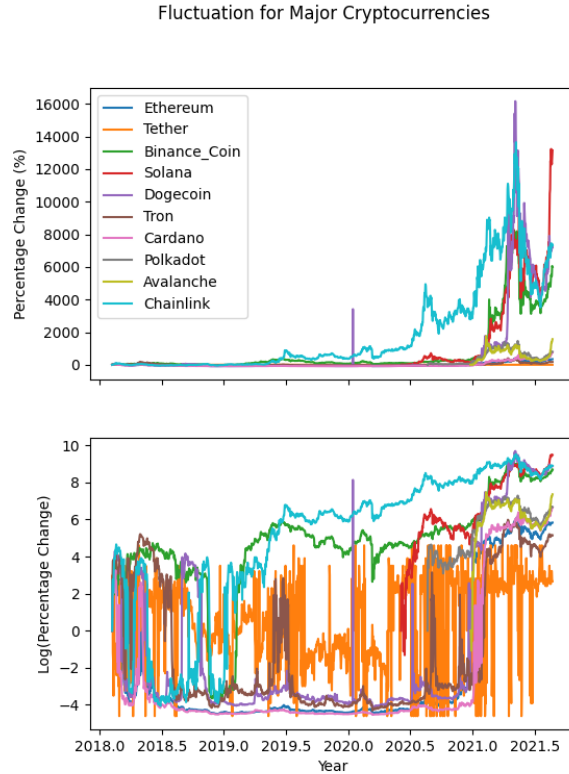


Figure 5: Percentage & Logarithmic Percentage Change for Prices of Major Cryptocurrencies

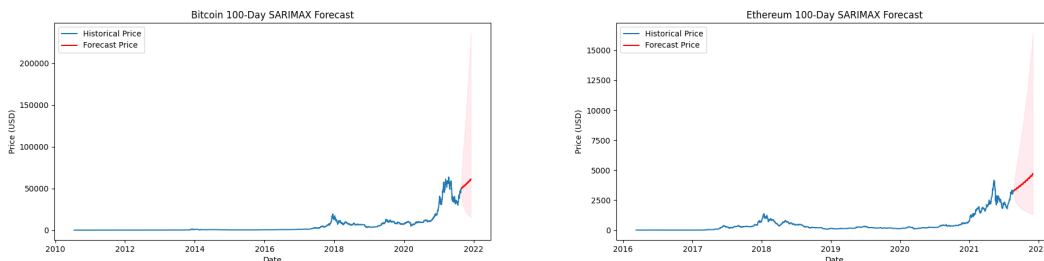
## 4.2 Spectral Analysis & Detrending

Fourier-based filtering allows precise attenuation of known periodic noise without arbitrarily choosing polynomial degrees or moving-average window length. Figure 4 compares the original percent-change (blue) to our filtered trend (orange). Small “ringing” at the endpoints remains, a known edge effect of finite-length Fourier approximation. Note that even though we applied a Hamming window to taper the series and reduce spectral leakage, we’ll still see oscillations at the very beginning and end of the reconstructed trend. This is due to the rounding errors of the computer, as it is not good dealing with small numbers. And when we try to reconstruct the waves and de-windowing it, the oscillation might be emphasized through this process.

## 4.3 SARIMAX Fit & Diagnostics

We collect all combinations of  $(p, d, q, P, D, Q)$  with their BIC values and sort by ascending BIC, and pick the top entry, which is  $(0, 1, 0)$  and  $(0, 2, 2, 12)$ . This is the combination with the lowest BIC, which indicates a better trade-off between goodness-of-fit and model complexity. 6.3 summarizes all the permutations and the estimated coefficient.

And we get the following forecast results for Bitcoin and Ethereum,



(a) Future Forecast Results for Bitcoin with Confidence Interval (b) Future Forecast Results for Ethereum with Confidence Interval

## 4.4 Forecast Accuracy

Since all cryptocurrencies has strong correlation in terms of tendencies, we’ll only discuss the Bitcoin results.

The graph above shows a comparison between historical Bitcoin price (blue), model forecast (red), the actual price (yellow), and the 95% confidence interval (red shading).

The SARIMAX mean forecast picks up Bitcoin’s prevailing upward drift in mid-2021, projecting a gradual rise from roughly \$35 k to around \$60 k over 100 days. This aligns with the broad market direction during that period. However, the red shaded band widens rapidly as the horizon extends, reflecting growing

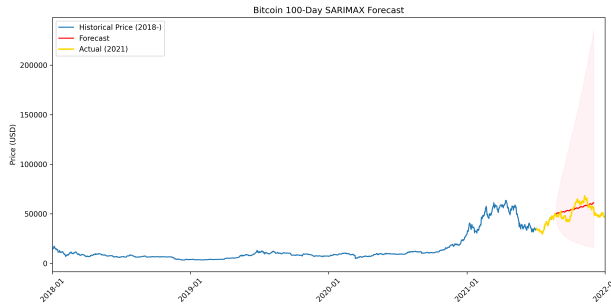


Figure 7: Comparison between Actual and SARIMAX Prediction Prices

uncertainty. Importantly, most of the yellow actual path remain inside the 95% interval, indicating that its uncertainty bounds are sufficiently wide to cover the realized outcomes.

## 5 Discussion & Conclusion

The spectral-filter + SARIMAX approach achieved three important goals:

### 5.0.1 Trend Extraction & Noise Reduction

By applying a windowed Fourier-notch filter, we effectively separated persistent price trends from short-term volatility. This preprocessing simplified the downstream time-series modeling and made the SARIMAX residuals more nearly white, improving forecast stability.

### 5.0.2 Incorporation of Market Sentiment

Introducing the S&P 500 returns as an exogenous regressor allowed the models to "listen" to broader equity-market moves. Across all coins, this extra signal reduced forecast error compared to purely auto-regressive approaches.

### 5.0.3 Quantified Uncertainty

The SARIMAX framework provide a 95% confidence bands that expanded widely over time. In future studies, more exogenous variables can be involved for a smaller band and reduce uncertainty interval.

## 5.1 Limitations & Future Directions

**Single Exogenous Input:** Relying solely on equity returns may miss crypto-specific drivers like on-chain metrics or sentiment.

**Static Parameter:** The fixed model orders and coefficients assume stationarity of relationships that may evolve over time.

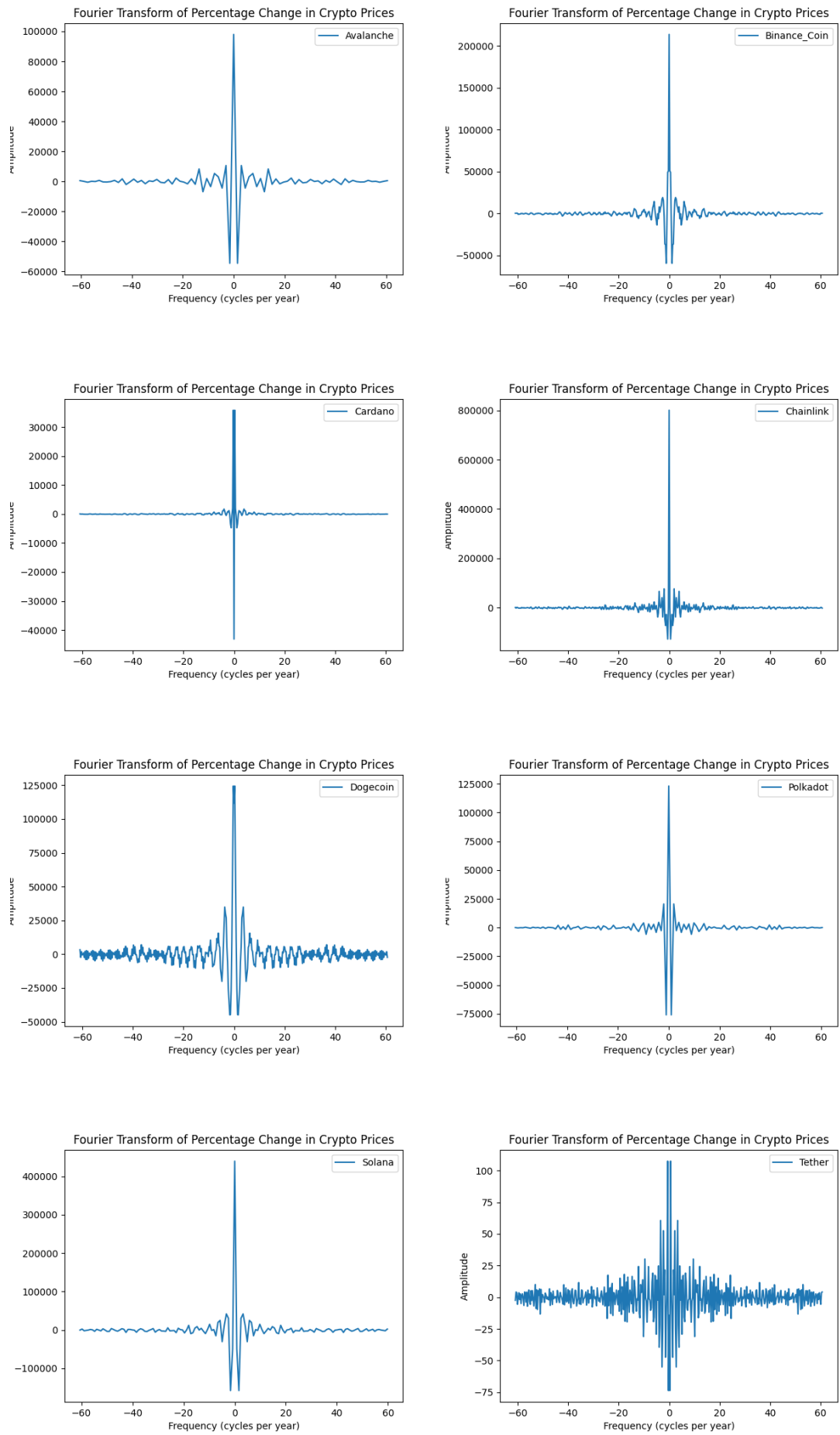
In the future, we could introduce additional exogenous signals like trading volume and implement volatility components into the analysis.

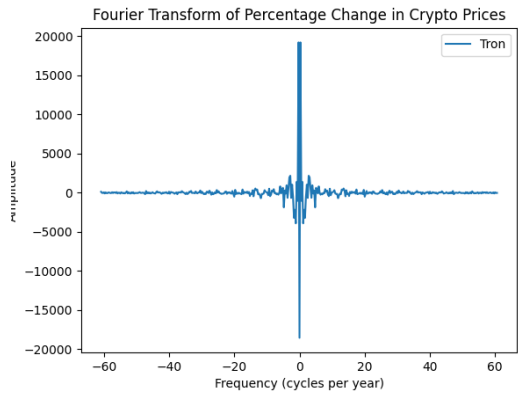
## 5.2 Practical Implication

For risk management or conservative scenario planning, the confidence band provides actionable ranges. However, for precise trading signals, the model's inability to capture abrupt spikes and crashes would need to be addressed—perhaps via a volatility model or by adding more sentiment indicators and exogenous variables.

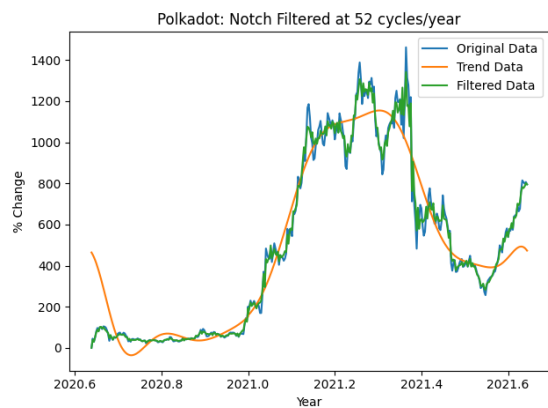
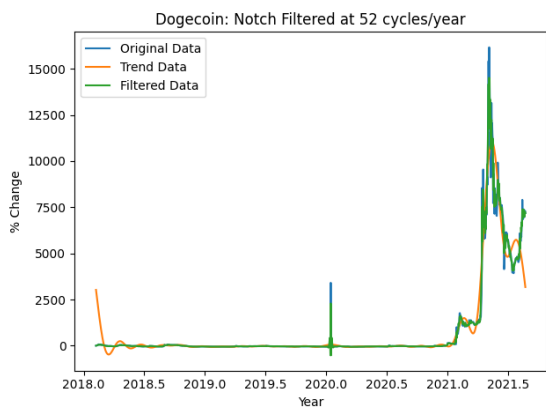
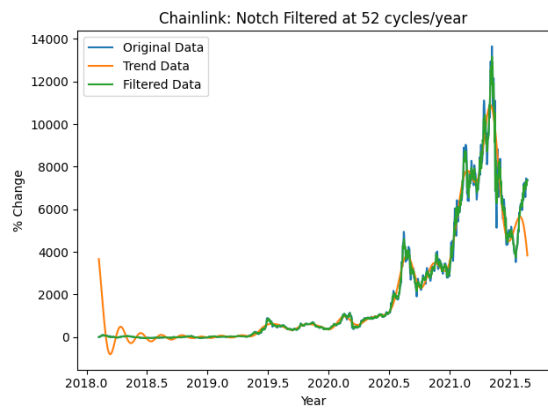
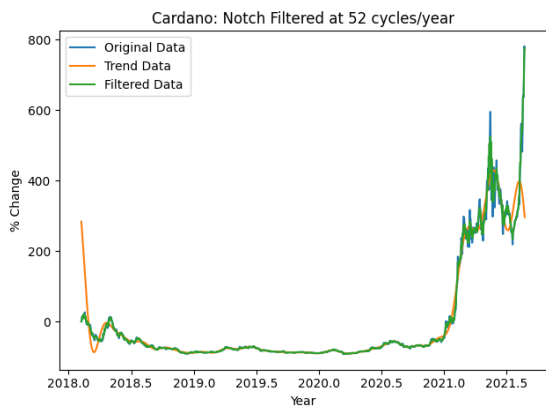
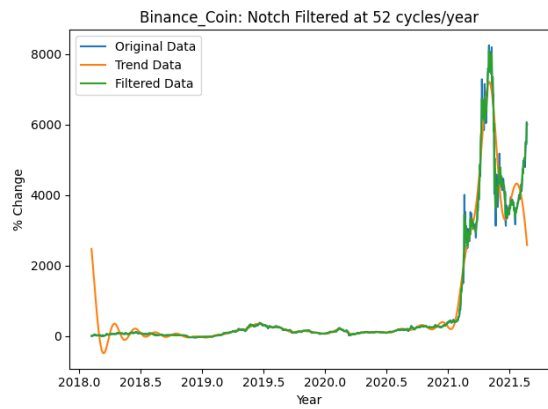
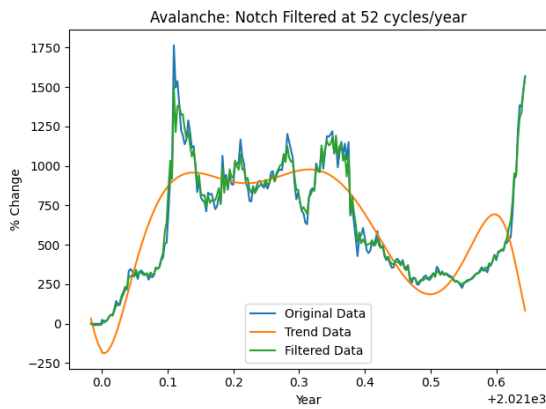
# 6 Appendix

## 6.1 Fourier Transform

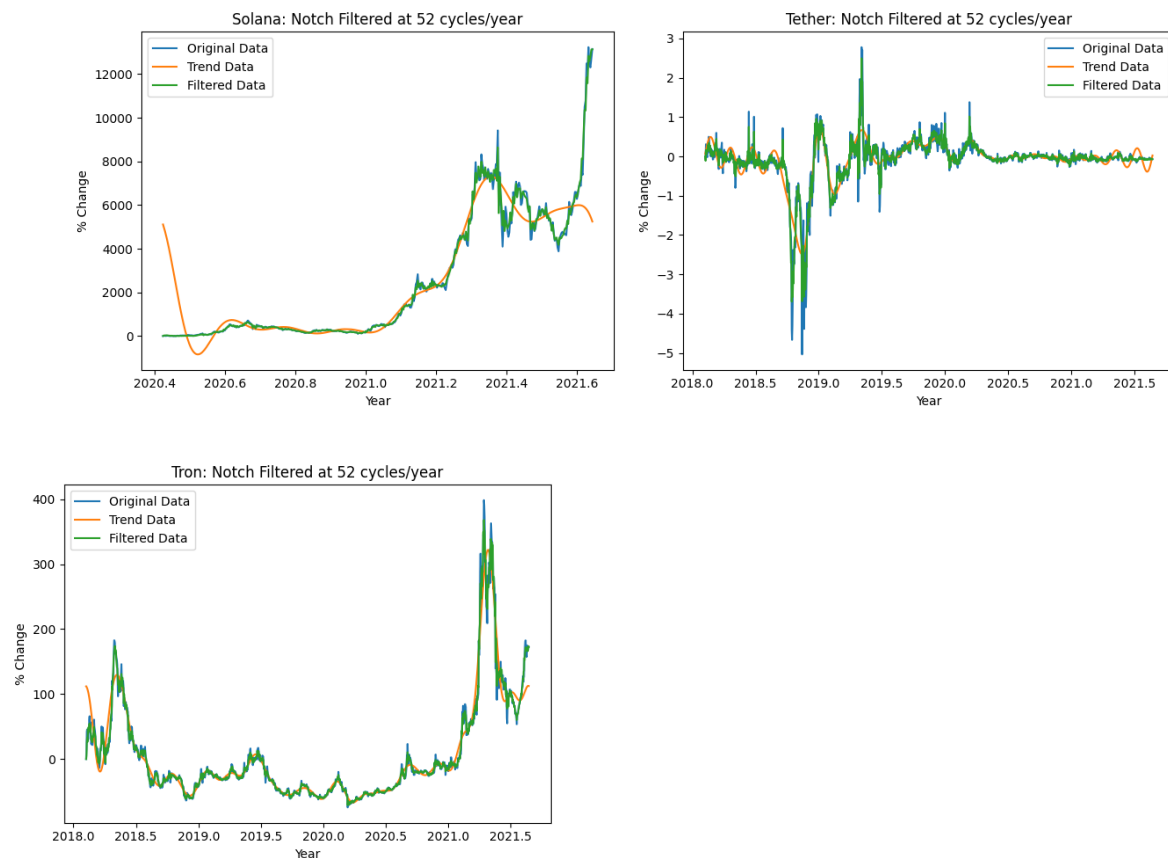




## 6.2 Notch Filtered Results







### 6.3 BIC Table

SARIMAX (0, 0, 0) x (0, 0, 0, 12): BIC =32029.319320243692  
 SARIMAX (0, 0, 0) x (0, 0, 1, 12): BIC =23706.15619129918  
 SARIMAX (0, 0, 0) x (0, 0, 2, 12): BIC =23822.031732326464  
 SARIMAX (0, 0, 0) x (0, 1, 0, 12): BIC =21310.390965175142  
 SARIMAX (0, 0, 0) x (0, 1, 1, 12): BIC =21316.309797407015  
 SARIMAX (0, 0, 0) x (0, 1, 2, 12): BIC =21311.694377216165  
 SARIMAX (0, 0, 0) x (0, 2, 0, 12): BIC =28797.611364156583  
 SARIMAX (0, 0, 0) x (0, 2, 1, 12): BIC =21016.512306602963  
 SARIMAX (0, 0, 0) x (0, 2, 2, 12): BIC =21214.34441257611  
 SARIMAX (0, 0, 0) x (1, 0, 0, 12): BIC =21587.317110742126  
 SARIMAX (0, 0, 0) x (1, 0, 1, 12): BIC =21593.440381792818  
 SARIMAX (0, 0, 0) x (1, 0, 2, 12): BIC =21590.605922590938  
 SARIMAX (0, 0, 0) x (1, 1, 0, 12): BIC =21316.072139904736  
 SARIMAX (0, 0, 0) x (1, 1, 1, 12): BIC =21322.722253891585  
 SARIMAX (0, 0, 0) x (1, 1, 2, 12): BIC =21079.867456565727  
 SARIMAX (0, 0, 0) x (1, 2, 0, 12): BIC =21496.83895953416  
 SARIMAX (0, 0, 0) x (1, 2, 1, 12): BIC =21053.44983412878  
 SARIMAX (0, 0, 0) x (1, 2, 2, 12): BIC =20987.781683381712  
 SARIMAX (0, 0, 0) x (2, 0, 0, 12): BIC =21595.090370918166  
 SARIMAX (0, 0, 0) x (2, 0, 1, 12): BIC =21561.09891257681  
 SARIMAX (0, 0, 0) x (2, 0, 2, 12): BIC =21560.44385125395  
 SARIMAX (0, 0, 0) x (2, 1, 0, 12): BIC =21315.502515910117  
 SARIMAX (0, 0, 0) x (2, 1, 1, 12): BIC =21186.89887873448  
 SARIMAX (0, 0, 0) x (2, 1, 2, 12): BIC =21232.12562457235  
 SARIMAX (0, 0, 0) x (2, 2, 0, 12): BIC =21049.68965159697  
 SARIMAX (0, 0, 0) x (2, 2, 1, 12): BIC =20845.246122955294  
 SARIMAX (0, 0, 0) x (2, 2, 2, 12): BIC =20843.933409839705  
 SARIMAX (0, 0, 1) x (0, 0, 0, 12): BIC =23830.46504556923  
 SARIMAX (0, 0, 1) x (0, 0, 1, 12): BIC =22864.148342035864  
 SARIMAX (0, 0, 1) x (0, 0, 2, 12): BIC =23782.928151345608  
 SARIMAX (0, 0, 1) x (0, 1, 0, 12): BIC =20254.812618234308  
 SARIMAX (0, 0, 1) x (0, 1, 1, 12): BIC =20523.295886729364  
 SARIMAX (0, 0, 1) x (0, 1, 2, 12): BIC =20527.704538191105  
 SARIMAX (0, 0, 1) x (0, 2, 0, 12): BIC =20903.56333919173  
 SARIMAX (0, 0, 1) x (0, 2, 1, 12): BIC =20057.75830464319  
 SARIMAX (0, 0, 1) x (0, 2, 2, 12): BIC =20790.83396110705  
 SARIMAX (0, 0, 1) x (1, 0, 0, 12): BIC =23525.761169553705  
 SARIMAX (0, 0, 1) x (1, 0, 1, 12): BIC =23682.462332039686  
 SARIMAX (0, 0, 1) x (1, 0, 2, 12): BIC =23877.44598612887  
 SARIMAX (0, 0, 1) x (1, 1, 0, 12): BIC =20461.302237491658  
 SARIMAX (0, 0, 1) x (1, 1, 1, 12): BIC =20530.50991320569

SARIMAX (0, 0, 1) x (1, 1, 2, 12): BIC =20533.0371268043  
SARIMAX (0, 0, 1) x (1, 2, 0, 12): BIC =20948.254450423734  
SARIMAX (0, 0, 1) x (1, 2, 1, 12): BIC =20801.28646009879  
SARIMAX (0, 0, 1) x (1, 2, 2, 12): BIC =20836.591096101856  
SARIMAX (0, 0, 1) x (2, 0, 0, 12): BIC =23866.412754569083  
SARIMAX (0, 0, 1) x (2, 0, 1, 12): BIC =23877.39437666303  
SARIMAX (0, 0, 1) x (2, 0, 2, 12): BIC =23884.441775016796  
SARIMAX (0, 0, 1) x (2, 1, 0, 12): BIC =20530.20932428893  
SARIMAX (0, 0, 1) x (2, 1, 1, 12): BIC =20529.79167635271  
SARIMAX (0, 0, 1) x (2, 1, 2, 12): BIC =20528.349666744434  
SARIMAX (0, 0, 1) x (2, 2, 0, 12): BIC =20847.35248179039  
SARIMAX (0, 0, 1) x (2, 2, 1, 12): BIC =20793.37032344457  
SARIMAX (0, 0, 1) x (2, 2, 2, 12): BIC =20795.04825491164  
SARIMAX (0, 0, 2) x (0, 0, 0, 12): BIC =23911.33634097961  
SARIMAX (0, 0, 2) x (0, 0, 1, 12): BIC =23878.240713881416  
SARIMAX (0, 0, 2) x (0, 0, 2, 12): BIC =23872.54133374041  
SARIMAX (0, 0, 2) x (0, 1, 0, 12): BIC =20284.290816388126  
SARIMAX (0, 0, 2) x (0, 1, 1, 12): BIC =20277.795263053013  
SARIMAX (0, 0, 2) x (0, 1, 2, 12): BIC =20283.346573255665  
SARIMAX (0, 0, 2) x (0, 2, 0, 12): BIC =20900.06322077692  
SARIMAX (0, 0, 2) x (0, 2, 1, 12): BIC =20633.829559934304  
SARIMAX (0, 0, 2) x (0, 2, 2, 12): BIC =20601.93644758001  
SARIMAX (0, 0, 2) x (1, 0, 0, 12): BIC =23855.927208705292  
SARIMAX (0, 0, 2) x (1, 0, 1, 12): BIC =23861.886655423034  
SARIMAX (0, 0, 2) x (1, 0, 2, 12): BIC =23868.987983038987  
SARIMAX (0, 0, 2) x (1, 1, 0, 12): BIC =20276.899431174417  
SARIMAX (0, 0, 2) x (1, 1, 1, 12): BIC =20284.884298607452  
SARIMAX (0, 0, 2) x (1, 1, 2, 12): BIC =20293.072080517366  
SARIMAX (0, 0, 2) x (1, 2, 0, 12): BIC =20747.155057812408  
SARIMAX (0, 0, 2) x (1, 2, 1, 12): BIC =20620.87377342299  
SARIMAX (0, 0, 2) x (1, 2, 2, 12): BIC =20609.48295592861  
SARIMAX (0, 0, 2) x (2, 0, 0, 12): BIC =23862.040654134493  
SARIMAX (0, 0, 2) x (2, 0, 1, 12): BIC =23869.140631311904  
SARIMAX (0, 0, 2) x (2, 0, 2, 12): BIC =23876.050326968474  
SARIMAX (0, 0, 2) x (2, 1, 0, 12): BIC =20284.00316855052  
SARIMAX (0, 0, 2) x (2, 1, 1, 12): BIC =20288.769506525052  
SARIMAX (0, 0, 2) x (2, 1, 2, 12): BIC =20295.212097132  
SARIMAX (0, 0, 2) x (2, 2, 0, 12): BIC =20655.95687348093  
SARIMAX (0, 0, 2) x (2, 2, 1, 12): BIC =20608.18364134932  
SARIMAX (0, 0, 2) x (2, 2, 2, 12): BIC =20610.01660824089  
SARIMAX (0, 1, 0) x (0, 0, 0, 12): BIC =18514.791571458114  
SARIMAX (0, 1, 0) x (0, 0, 1, 12): BIC =18521.889133642322  
SARIMAX (0, 1, 0) x (0, 0, 2, 12): BIC =18520.09195884056  
SARIMAX (0, 1, 0) x (0, 1, 0, 12): BIC =19087.65445618315  
SARIMAX (0, 1, 0) x (0, 1, 1, 12): BIC =18373.50433847866  
SARIMAX (0, 1, 0) x (0, 1, 2, 12): BIC =18427.610040682706  
SARIMAX (0, 1, 0) x (0, 2, 0, 12): BIC =20068.615170918376  
SARIMAX (0, 1, 0) x (0, 2, 1, 12): BIC =18950.446780077764  
SARIMAX (0, 1, 0) x (0, 2, 2, 12): BIC =18294.907593028332  
SARIMAX (0, 1, 0) x (1, 0, 0, 12): BIC =18521.82856752411  
SARIMAX (0, 1, 0) x (1, 0, 1, 12): BIC =18524.414479431634  
SARIMAX (0, 1, 0) x (1, 0, 2, 12): BIC =18526.388359664405  
SARIMAX (0, 1, 0) x (1, 1, 0, 12): BIC =18841.17050860133  
SARIMAX (0, 1, 0) x (1, 1, 1, 12): BIC =18389.248688674772  
SARIMAX (0, 1, 0) x (1, 1, 2, 12): BIC =18409.707031896553  
SARIMAX (0, 1, 0) x (1, 2, 0, 12): BIC =19538.20444710906  
SARIMAX (0, 1, 0) x (1, 2, 1, 12): BIC =18714.153578851037  
SARIMAX (0, 1, 0) x (1, 2, 2, 12): BIC =18556.472269631842  
SARIMAX (0, 1, 0) x (2, 0, 0, 12): BIC =18518.964112407997  
SARIMAX (0, 1, 0) x (2, 0, 1, 12): BIC =18524.985232470382  
SARIMAX (0, 1, 0) x (2, 0, 2, 12): BIC =18531.515958671698  
SARIMAX (0, 1, 0) x (2, 1, 0, 12): BIC =18649.1224557098  
SARIMAX (0, 1, 0) x (2, 1, 1, 12): BIC =18403.775703712443  
SARIMAX (0, 1, 0) x (2, 1, 2, 12): BIC =18399.008586195305  
SARIMAX (0, 1, 0) x (2, 2, 0, 12): BIC =19181.979724489396  
SARIMAX (0, 1, 0) x (2, 2, 1, 12): BIC =18545.669662218228  
SARIMAX (0, 1, 0) x (2, 2, 2, 12): BIC =18465.213200646616  
SARIMAX (0, 1, 1) x (0, 0, 0, 12): BIC =18521.317379753316  
SARIMAX (0, 1, 1) x (0, 0, 1, 12): BIC =18528.350814704852  
SARIMAX (0, 1, 1) x (0, 0, 2, 12): BIC =18526.010849725255  
SARIMAX (0, 1, 1) x (0, 1, 0, 12): BIC =19094.595921624197  
SARIMAX (0, 1, 1) x (0, 1, 1, 12): BIC =18379.904566374964

SARIMAX (0, 1, 1) x (0, 1, 2, 12): BIC =18580.979150965817  
 SARIMAX (0, 1, 1) x (0, 2, 0, 12): BIC =20075.44916120445  
 SARIMAX (0, 1, 1) x (0, 2, 1, 12): BIC =19365.644169701518  
 SARIMAX (0, 1, 1) x (0, 2, 2, 12): BIC =19227.57123411756  
 SARIMAX (0, 1, 1) x (1, 0, 0, 12): BIC =18528.3556097222  
 SARIMAX (0, 1, 1) x (1, 0, 1, 12): BIC =18530.63259536323  
 SARIMAX (0, 1, 1) x (1, 0, 2, 12): BIC =18532.212171974294  
 SARIMAX (0, 1, 1) x (1, 1, 0, 12): BIC =18872.54494129301  
 SARIMAX (0, 1, 1) x (1, 1, 1, 12): BIC =18559.694135280075  
 SARIMAX (0, 1, 1) x (1, 1, 2, 12): BIC =18586.81869287088  
 SARIMAX (0, 1, 1) x (1, 2, 0, 12): BIC =19643.789395009768  
 SARIMAX (0, 1, 1) x (1, 2, 1, 12): BIC =19309.22641717099  
 SARIMAX (0, 1, 1) x (1, 2, 2, 12): BIC =19240.31435494454  
 SARIMAX (0, 1, 1) x (2, 0, 0, 12): BIC =18525.710475703436  
 SARIMAX (0, 1, 1) x (2, 0, 1, 12): BIC =18531.66488784874  
 SARIMAX (0, 1, 1) x (2, 0, 2, 12): BIC =18537.596610063494  
 SARIMAX (0, 1, 1) x (2, 1, 0, 12): BIC =18716.881447458305  
 SARIMAX (0, 1, 1) x (2, 1, 1, 12): BIC =18578.76010813984  
 SARIMAX (0, 1, 1) x (2, 1, 2, 12): BIC =18586.068461198425  
 SARIMAX (0, 1, 1) x (2, 2, 0, 12): BIC =19457.71987789332  
 SARIMAX (0, 1, 1) x (2, 2, 1, 12): BIC =19271.346037447645  
 SARIMAX (0, 1, 1) x (2, 2, 2, 12): BIC =19243.585138686136  
 SARIMAX (0, 1, 2) x (0, 0, 0, 12): BIC =18526.381065812526  
 SARIMAX (0, 1, 2) x (0, 0, 1, 12): BIC =18533.44927036163  
 SARIMAX (0, 1, 2) x (0, 0, 2, 12): BIC =18530.598904134702  
 SARIMAX (0, 1, 2) x (0, 1, 0, 12): BIC =19101.641893947486  
 SARIMAX (0, 1, 2) x (0, 1, 1, 12): BIC =18390.429531940383  
 SARIMAX (0, 1, 2) x (0, 1, 2, 12): BIC =18586.84817430062  
 SARIMAX (0, 1, 2) x (0, 2, 0, 12): BIC =20082.486370252078  
 SARIMAX (0, 1, 2) x (0, 2, 1, 12): BIC =19169.676617834644  
 SARIMAX (0, 1, 2) x (0, 2, 2, 12): BIC =19239.377122496826  
 SARIMAX (0, 1, 2) x (1, 0, 0, 12): BIC =18533.43845213394  
 SARIMAX (0, 1, 2) x (1, 0, 1, 12): BIC =18535.942294899258  
 SARIMAX (0, 1, 2) x (1, 0, 2, 12): BIC =18537.019897441918  
 SARIMAX (0, 1, 2) x (1, 1, 0, 12): BIC =18880.49640779953  
 SARIMAX (0, 1, 2) x (1, 1, 1, 12): BIC =18589.66417474654  
 SARIMAX (0, 1, 2) x (1, 1, 2, 12): BIC =18594.440166719727  
 SARIMAX (0, 1, 2) x (1, 2, 0, 12): BIC =19661.929719279753  
 SARIMAX (0, 1, 2) x (1, 2, 1, 12): BIC =19321.414452343815  
 SARIMAX (0, 1, 2) x (1, 2, 2, 12): BIC =19248.14853699159  
 SARIMAX (0, 1, 2) x (2, 0, 0, 12): BIC =18530.323376977885  
 SARIMAX (0, 1, 2) x (2, 0, 1, 12): BIC =18536.553562040146  
 SARIMAX (0, 1, 2) x (2, 0, 2, 12): BIC =18542.833819114963  
 SARIMAX (0, 1, 2) x (2, 1, 0, 12): BIC =18739.662404074035  
 SARIMAX (0, 1, 2) x (2, 1, 1, 12): BIC =18586.709064526436  
 SARIMAX (0, 1, 2) x (2, 1, 2, 12): BIC =18594.086184917098  
 SARIMAX (0, 1, 2) x (2, 2, 0, 12): BIC =19469.020437553572  
 SARIMAX (0, 1, 2) x (2, 2, 1, 12): BIC =19280.344089477883  
 SARIMAX (0, 1, 2) x (2, 2, 2, 12): BIC =19252.619964485595  
 SARIMAX (0, 2, 0) x (0, 0, 0, 12): BIC =19322.190884346397  
 SARIMAX (0, 2, 0) x (0, 0, 1, 12): BIC =19329.095554374424  
 SARIMAX (0, 2, 0) x (0, 0, 2, 12): BIC =19323.86622641448  
 SARIMAX (0, 2, 0) x (0, 1, 0, 12): BIC =19870.246232597157  
 SARIMAX (0, 2, 0) x (0, 1, 1, 12): BIC =19173.26841032062  
 SARIMAX (0, 2, 0) x (0, 1, 2, 12): BIC =19267.155979523013  
 SARIMAX (0, 2, 0) x (0, 2, 0, 12): BIC =20820.12573705995  
 SARIMAX (0, 2, 0) x (0, 2, 1, 12): BIC =19721.925100313605  
 SARIMAX (0, 2, 0) x (0, 2, 2, 12): BIC =19479.54701786935  
 SARIMAX (0, 2, 0) x (1, 0, 0, 12): BIC =19329.067589202074  
 SARIMAX (0, 2, 0) x (1, 0, 1, 12): BIC =19333.30682897211  
 SARIMAX (0, 2, 0) x (1, 0, 2, 12): BIC =19330.91524946667  
 SARIMAX (0, 2, 0) x (1, 1, 0, 12): BIC =19650.663006090377  
 SARIMAX (0, 2, 0) x (1, 1, 1, 12): BIC =19258.082269363433  
 SARIMAX (0, 2, 0) x (1, 1, 2, 12): BIC =19243.68699897133  
 SARIMAX (0, 2, 0) x (1, 2, 0, 12): BIC =20318.599647564002  
 SARIMAX (0, 2, 0) x (1, 2, 1, 12): BIC =19689.762467578614  
 SARIMAX (0, 2, 0) x (1, 2, 2, 12): BIC =19480.488113632877  
 SARIMAX (0, 2, 0) x (2, 0, 0, 12): BIC =19320.30153571223  
 SARIMAX (0, 2, 0) x (2, 0, 1, 12): BIC =19327.34374887706  
 SARIMAX (0, 2, 0) x (2, 0, 2, 12): BIC =19324.61768577241  
 SARIMAX (0, 2, 0) x (2, 1, 0, 12): BIC =19463.363478969783  
 SARIMAX (0, 2, 0) x (2, 1, 1, 12): BIC =19206.36560547592

SARIMAX (0, 2, 0) x (2, 1, 2, 12): BIC =19208.592954842134  
 SARIMAX (0, 2, 0) x (2, 2, 0, 12): BIC =20019.532870253166  
 SARIMAX (0, 2, 0) x (2, 2, 1, 12): BIC =19511.252439768115  
 SARIMAX (0, 2, 0) x (2, 2, 2, 12): BIC =19350.2870637642  
 SARIMAX (0, 2, 1) x (0, 0, 0, 12): BIC =18499.152193601138  
 SARIMAX (0, 2, 1) x (0, 0, 1, 12): BIC =18514.166456736293  
 SARIMAX (0, 2, 1) x (0, 0, 2, 12): BIC =18530.071681469137  
 SARIMAX (0, 2, 1) x (0, 1, 0, 12): BIC =19086.580761554913  
 SARIMAX (0, 2, 1) x (0, 1, 1, 12): BIC =18373.867457637516  
 SARIMAX (0, 2, 1) x (0, 1, 2, 12): BIC =18532.131264623615  
 SARIMAX (0, 2, 1) x (0, 2, 0, 12): BIC =20065.902547044094  
 SARIMAX (0, 2, 1) x (0, 2, 1, 12): BIC =18954.432060236875  
 SARIMAX (0, 2, 1) x (0, 2, 2, 12): BIC =18400.13977319973  
 SARIMAX (0, 2, 1) x (1, 0, 0, 12): BIC =18530.84454730537  
 SARIMAX (0, 2, 1) x (1, 0, 1, 12): BIC =18521.995834166122  
 SARIMAX (0, 2, 1) x (1, 0, 2, 12): BIC =18537.041437246837  
 SARIMAX (0, 2, 1) x (1, 1, 0, 12): BIC =18839.767293273322  
 SARIMAX (0, 2, 1) x (1, 1, 1, 12): BIC =18564.10723590746  
 SARIMAX (0, 2, 1) x (1, 1, 2, 12): BIC =18714.999787713845  
 SARIMAX (0, 2, 1) x (1, 2, 0, 12): BIC =19535.91327370122  
 SARIMAX (0, 2, 1) x (1, 2, 1, 12): BIC =18718.205088248455  
 SARIMAX (0, 2, 1) x (1, 2, 2, 12): BIC =19432.055216721623  
 SARIMAX (0, 2, 1) x (2, 0, 0, 12): BIC =18528.46525400582  
 SARIMAX (0, 2, 1) x (2, 0, 1, 12): BIC =18536.931931376166  
 SARIMAX (0, 2, 1) x (2, 0, 2, 12): BIC =18543.82378824961  
 SARIMAX (0, 2, 1) x (2, 1, 0, 12): BIC =18831.977598131263  
 SARIMAX (0, 2, 1) x (2, 1, 1, 12): BIC =18709.91269347764  
 SARIMAX (0, 2, 1) x (2, 1, 2, 12): BIC =18719.937409412232  
 SARIMAX (0, 2, 1) x (2, 2, 0, 12): BIC =19181.78468727112  
 SARIMAX (0, 2, 1) x (2, 2, 1, 12): BIC =19451.753912348096  
 SARIMAX (0, 2, 1) x (2, 2, 2, 12): BIC =19439.19778193821  
 SARIMAX (0, 2, 2) x (0, 0, 0, 12): BIC =18515.79139444276  
 SARIMAX (0, 2, 2) x (0, 0, 1, 12): BIC =18525.492167134536  
 SARIMAX (0, 2, 2) x (0, 0, 2, 12): BIC =18518.352979197047  
 SARIMAX (0, 2, 2) x (0, 1, 0, 12): BIC =19093.622026371566  
 SARIMAX (0, 2, 2) x (0, 1, 1, 12): BIC =18399.22855029098  
 SARIMAX (0, 2, 2) x (0, 1, 2, 12): BIC =18679.85358735675  
 SARIMAX (0, 2, 2) x (0, 2, 0, 12): BIC =20082.26934159594  
 SARIMAX (0, 2, 2) x (0, 2, 1, 12): BIC =19493.638087029794  
 SARIMAX (0, 2, 2) x (0, 2, 2, 12): BIC =19327.389072661987  
 SARIMAX (0, 2, 2) x (1, 0, 0, 12): BIC =18525.563220388038  
 SARIMAX (0, 2, 2) x (1, 0, 1, 12): BIC =18528.551429195362  
 SARIMAX (0, 2, 2) x (1, 0, 2, 12): BIC =18527.802541302342  
 SARIMAX (0, 2, 2) x (1, 1, 0, 12): BIC =18857.787265569234  
 SARIMAX (0, 2, 2) x (1, 1, 1, 12): BIC =18686.281144925735  
 SARIMAX (0, 2, 2) x (1, 1, 2, 12): BIC =18684.840918623348  
 SARIMAX (0, 2, 2) x (1, 2, 0, 12): BIC =19730.477650687775  
 SARIMAX (0, 2, 2) x (1, 2, 1, 12): BIC =19448.634826253936  
 SARIMAX (0, 2, 2) x (1, 2, 2, 12): BIC =19390.137162342853  
 SARIMAX (0, 2, 2) x (2, 0, 0, 12): BIC =18520.565130696825  
 SARIMAX (0, 2, 2) x (2, 0, 1, 12): BIC =18527.71940898488  
 SARIMAX (0, 2, 2) x (2, 0, 2, 12): BIC =18534.50446757634  
 SARIMAX (0, 2, 2) x (2, 1, 0, 12): BIC =18739.97299496672  
 SARIMAX (0, 2, 2) x (2, 1, 1, 12): BIC =18682.91218919616  
 SARIMAX (0, 2, 2) x (2, 1, 2, 12): BIC =18693.755001307392  
 SARIMAX (0, 2, 2) x (2, 2, 0, 12): BIC =19570.57070855349  
 SARIMAX (0, 2, 2) x (2, 2, 1, 12): BIC =19415.15979215337  
 SARIMAX (0, 2, 2) x (2, 2, 2, 12): BIC =19395.68571877193  
 SARIMAX (1, 0, 0) x (0, 0, 0, 12): BIC =18547.83500002325  
 SARIMAX (1, 0, 0) x (0, 0, 1, 12): BIC =18556.650355235084  
 SARIMAX (1, 0, 0) x (0, 0, 2, 12): BIC =18554.66148350053  
 SARIMAX (1, 0, 0) x (0, 1, 0, 12): BIC =19076.856339848873  
 SARIMAX (1, 0, 0) x (0, 1, 1, 12): BIC =18404.928279697528  
 SARIMAX (1, 0, 0) x (0, 1, 2, 12): BIC =18572.651273942574  
 SARIMAX (1, 0, 0) x (0, 2, 0, 12): BIC =20040.19269325897  
 SARIMAX (1, 0, 0) x (0, 2, 1, 12): BIC =18934.912781350347  
 SARIMAX (1, 0, 0) x (0, 2, 2, 12): BIC =18325.336103337817  
 SARIMAX (1, 0, 0) x (1, 0, 0, 12): BIC =18553.881762692243  
 SARIMAX (1, 0, 0) x (1, 0, 1, 12): BIC =18561.394624967048  
 SARIMAX (1, 0, 0) x (1, 0, 2, 12): BIC =18573.808232984553  
 SARIMAX (1, 0, 0) x (1, 1, 0, 12): BIC =18843.053219955644  
 SARIMAX (1, 0, 0) x (1, 1, 1, 12): BIC =18578.837570936426

SARIMAX (1, 0, 0) x (1, 1, 2, 12): BIC =18454.085639483834  
 SARIMAX (1, 0, 0) x (1, 2, 0, 12): BIC =19607.02747824478  
 SARIMAX (1, 0, 0) x (1, 2, 1, 12): BIC =18827.374676812193  
 SARIMAX (1, 0, 0) x (1, 2, 2, 12): BIC =19197.02277243212  
 SARIMAX (1, 0, 0) x (2, 0, 0, 12): BIC =18557.67988696546  
 SARIMAX (1, 0, 0) x (2, 0, 1, 12): BIC =18572.839463899316  
 SARIMAX (1, 0, 0) x (2, 0, 2, 12): BIC =18569.838562106106  
 SARIMAX (1, 0, 0) x (2, 1, 0, 12): BIC =18729.83122496861  
 SARIMAX (1, 0, 0) x (2, 1, 1, 12): BIC =18581.495291467865  
 SARIMAX (1, 0, 0) x (2, 1, 2, 12): BIC =18590.00410044773  
 SARIMAX (1, 0, 0) x (2, 2, 0, 12): BIC =19428.450202743836  
 SARIMAX (1, 0, 0) x (2, 2, 1, 12): BIC =19240.33430470534  
 SARIMAX (1, 0, 0) x (2, 2, 2, 12): BIC =19211.41229216782  
 SARIMAX (1, 0, 1) x (0, 0, 0, 12): BIC =18555.120762191178  
 SARIMAX (1, 0, 1) x (0, 0, 1, 12): BIC =18564.56509015524  
 SARIMAX (1, 0, 1) x (0, 0, 2, 12): BIC =18561.770517147204  
 SARIMAX (1, 0, 1) x (0, 1, 0, 12): BIC =19083.14723522928  
 SARIMAX (1, 0, 1) x (0, 1, 1, 12): BIC =18551.54924524611  
 SARIMAX (1, 0, 1) x (0, 1, 2, 12): BIC =18581.6648991453  
 SARIMAX (1, 0, 1) x (0, 2, 0, 12): BIC =20042.792420294405  
 SARIMAX (1, 0, 1) x (0, 2, 1, 12): BIC =18943.713392406404  
 SARIMAX (1, 0, 1) x (0, 2, 2, 12): BIC =19205.262376335904  
 SARIMAX (1, 0, 1) x (1, 0, 0, 12): BIC =18566.178065803222  
 SARIMAX (1, 0, 1) x (1, 0, 1, 12): BIC =18567.583096001395  
 SARIMAX (1, 0, 1) x (1, 0, 2, 12): BIC =18579.13965954472  
 SARIMAX (1, 0, 1) x (1, 1, 0, 12): BIC =18870.930616227055  
 SARIMAX (1, 0, 1) x (1, 1, 1, 12): BIC =18588.298016792654  
 SARIMAX (1, 0, 1) x (1, 1, 2, 12): BIC =18594.800613812957  
 SARIMAX (1, 0, 1) x (1, 2, 0, 12): BIC =19623.392705350547  
 SARIMAX (1, 0, 1) x (1, 2, 1, 12): BIC =19284.10326198705  
 SARIMAX (1, 0, 1) x (1, 2, 2, 12): BIC =19215.034159281488  
 SARIMAX (1, 0, 1) x (2, 0, 0, 12): BIC =18573.409543859278  
 SARIMAX (1, 0, 1) x (2, 0, 1, 12): BIC =18582.340296220613  
 SARIMAX (1, 0, 1) x (2, 0, 2, 12): BIC =18579.324104234565  
 SARIMAX (1, 0, 1) x (2, 1, 0, 12): BIC =18736.41089912199  
 SARIMAX (1, 0, 1) x (2, 1, 1, 12): BIC =18591.795634506285  
 SARIMAX (1, 0, 1) x (2, 1, 2, 12): BIC =18597.1973767431  
 SARIMAX (1, 0, 1) x (2, 2, 0, 12): BIC =19433.561276330747  
 SARIMAX (1, 0, 1) x (2, 2, 1, 12): BIC =19244.972956271413  
 SARIMAX (1, 0, 1) x (2, 2, 2, 12): BIC =19217.24021569053  
 SARIMAX (1, 0, 2) x (0, 0, 0, 12): BIC =18560.93987551355  
 SARIMAX (1, 0, 2) x (0, 0, 1, 12): BIC =18569.00250604654  
 SARIMAX (1, 0, 2) x (0, 0, 2, 12): BIC =18566.817337160897  
 SARIMAX (1, 0, 2) x (0, 1, 0, 12): BIC =19088.54878474725  
 SARIMAX (1, 0, 2) x (0, 1, 1, 12): BIC =18591.89465578594  
 SARIMAX (1, 0, 2) x (0, 1, 2, 12): BIC =18603.19776532813  
 SARIMAX (1, 0, 2) x (0, 2, 0, 12): BIC =20048.146901263797  
 SARIMAX (1, 0, 2) x (0, 2, 1, 12): BIC =19362.923852119085  
 SARIMAX (1, 0, 2) x (0, 2, 2, 12): BIC =19216.125290922482  
 SARIMAX (1, 0, 2) x (1, 0, 0, 12): BIC =18571.472940479765  
 SARIMAX (1, 0, 2) x (1, 0, 1, 12): BIC =18576.715436829854  
 SARIMAX (1, 0, 2) x (1, 0, 2, 12): BIC =18585.290526909655  
 SARIMAX (1, 0, 2) x (1, 1, 0, 12): BIC =18877.135840488758  
 SARIMAX (1, 0, 2) x (1, 1, 1, 12): BIC =18598.338380375695  
 SARIMAX (1, 0, 2) x (1, 1, 2, 12): BIC =18605.102056073007  
 SARIMAX (1, 0, 2) x (1, 2, 0, 12): BIC =19629.06630536935  
 SARIMAX (1, 0, 2) x (1, 2, 1, 12): BIC =19296.219912736586  
 SARIMAX (1, 0, 2) x (1, 2, 2, 12): BIC =19224.256932560387  
 SARIMAX (1, 0, 2) x (2, 0, 0, 12): BIC =18576.513298645805  
 SARIMAX (1, 0, 2) x (2, 0, 1, 12): BIC =18585.692159190996  
 SARIMAX (1, 0, 2) x (2, 0, 2, 12): BIC =18584.84244992873  
 SARIMAX (1, 0, 2) x (2, 1, 0, 12): BIC =18744.568877454432  
 SARIMAX (1, 0, 2) x (2, 1, 1, 12): BIC =18597.52972806926  
 SARIMAX (1, 0, 2) x (2, 1, 2, 12): BIC =18605.93587616274  
 SARIMAX (1, 0, 2) x (2, 2, 0, 12): BIC =19442.115050071323  
 SARIMAX (1, 0, 2) x (2, 2, 1, 12): BIC =19255.835689302745  
 SARIMAX (1, 0, 2) x (2, 2, 2, 12): BIC =19227.503051339747  
 SARIMAX (1, 1, 0) x (0, 0, 0, 12): BIC =18521.27709770321  
 SARIMAX (1, 1, 0) x (0, 0, 1, 12): BIC =18528.311041014535  
 SARIMAX (1, 1, 0) x (0, 0, 2, 12): BIC =18525.969143662533  
 SARIMAX (1, 1, 0) x (0, 1, 0, 12): BIC =19094.595796364483  
 SARIMAX (1, 1, 0) x (0, 1, 1, 12): BIC =18379.875421948138

SARIMAX (1, 1, 0) x (0, 1, 2, 12): BIC =18581.448902197004  
 SARIMAX (1, 1, 0) x (0, 2, 0, 12): BIC =20075.44905334532  
 SARIMAX (1, 1, 0) x (0, 2, 1, 12): BIC =19378.30756299557  
 SARIMAX (1, 1, 0) x (0, 2, 2, 12): BIC =19136.568053834082  
 SARIMAX (1, 1, 0) x (1, 0, 0, 12): BIC =18528.315724713626  
 SARIMAX (1, 1, 0) x (1, 0, 1, 12): BIC =18530.562429760826  
 SARIMAX (1, 1, 0) x (1, 0, 2, 12): BIC =18532.162841899706  
 SARIMAX (1, 1, 0) x (1, 1, 0, 12): BIC =18861.221992287024  
 SARIMAX (1, 1, 0) x (1, 1, 1, 12): BIC =18386.637132511314  
 SARIMAX (1, 1, 0) x (1, 1, 2, 12): BIC =18583.923877308167  
 SARIMAX (1, 1, 0) x (1, 2, 0, 12): BIC =19645.92507770219  
 SARIMAX (1, 1, 0) x (1, 2, 1, 12): BIC =19311.61944827238  
 SARIMAX (1, 1, 0) x (1, 2, 2, 12): BIC =19238.95932298747  
 SARIMAX (1, 1, 0) x (2, 0, 0, 12): BIC =18525.672843131015  
 SARIMAX (1, 1, 0) x (2, 0, 1, 12): BIC =18531.62041175574  
 SARIMAX (1, 1, 0) x (2, 0, 2, 12): BIC =18537.56524770429  
 SARIMAX (1, 1, 0) x (2, 1, 0, 12): BIC =18730.741345547463  
 SARIMAX (1, 1, 0) x (2, 1, 1, 12): BIC =18577.106221199112  
 SARIMAX (1, 1, 0) x (2, 1, 2, 12): BIC =18585.709189068806  
 SARIMAX (1, 1, 0) x (2, 2, 0, 12): BIC =19412.62239944481  
 SARIMAX (1, 1, 0) x (2, 2, 1, 12): BIC =19271.285084689694  
 SARIMAX (1, 1, 0) x (2, 2, 2, 12): BIC =19243.39501509281  
 SARIMAX (1, 1, 1) x (0, 0, 0, 12): BIC =18519.878438355117  
 SARIMAX (1, 1, 1) x (0, 0, 1, 12): BIC =18526.768693203492  
 SARIMAX (1, 1, 1) x (0, 0, 2, 12): BIC =18521.997423063665  
 SARIMAX (1, 1, 1) x (0, 1, 0, 12): BIC =19101.64738604784  
 SARIMAX (1, 1, 1) x (0, 1, 1, 12): BIC =18385.64265572922  
 SARIMAX (1, 1, 1) x (0, 1, 2, 12): BIC =18585.954309205026  
 SARIMAX (1, 1, 1) x (0, 2, 0, 12): BIC =20082.490287689576  
 SARIMAX (1, 1, 1) x (0, 2, 1, 12): BIC =19211.083806232935  
 SARIMAX (1, 1, 1) x (0, 2, 2, 12): BIC =19234.923029974874  
 SARIMAX (1, 1, 1) x (1, 0, 0, 12): BIC =18526.804225529457  
 SARIMAX (1, 1, 1) x (1, 0, 1, 12): BIC =18530.540224384262  
 SARIMAX (1, 1, 1) x (1, 0, 2, 12): BIC =18529.467011107692  
 SARIMAX (1, 1, 1) x (1, 1, 0, 12): BIC =18874.133054857753  
 SARIMAX (1, 1, 1) x (1, 1, 1, 12): BIC =18502.584373423582  
 SARIMAX (1, 1, 1) x (1, 1, 2, 12): BIC =18593.57748844076  
 SARIMAX (1, 1, 1) x (1, 2, 0, 12): BIC =19640.573599978496  
 SARIMAX (1, 1, 1) x (1, 2, 1, 12): BIC =19317.360860056524  
 SARIMAX (1, 1, 1) x (1, 2, 2, 12): BIC =19245.600847498576  
 SARIMAX (1, 1, 1) x (2, 0, 0, 12): BIC =18521.520388545898  
 SARIMAX (1, 1, 1) x (2, 0, 1, 12): BIC =18529.130578453183  
 SARIMAX (1, 1, 1) x (2, 0, 2, 12): BIC =18535.81817675132  
 SARIMAX (1, 1, 1) x (2, 1, 0, 12): BIC =18731.88381938191  
 SARIMAX (1, 1, 1) x (2, 1, 1, 12): BIC =18584.53677797793  
 SARIMAX (1, 1, 1) x (2, 1, 2, 12): BIC =18591.895522675124  
 SARIMAX (1, 1, 1) x (2, 2, 0, 12): BIC =19469.621487559063  
 SARIMAX (1, 1, 1) x (2, 2, 1, 12): BIC =19270.872857289487  
 SARIMAX (1, 1, 1) x (2, 2, 2, 12): BIC =19247.45876351015  
 SARIMAX (1, 1, 2) x (0, 0, 0, 12): BIC =18531.380497983428  
 SARIMAX (1, 1, 2) x (0, 0, 1, 12): BIC =18538.437272935877  
 SARIMAX (1, 1, 2) x (0, 0, 2, 12): BIC =18534.62360298232  
 SARIMAX (1, 1, 2) x (0, 1, 0, 12): BIC =19064.377228044737  
 SARIMAX (1, 1, 2) x (0, 1, 1, 12): BIC =18433.17235159575  
 SARIMAX (1, 1, 2) x (0, 1, 2, 12): BIC =18596.672071170888  
 SARIMAX (1, 1, 2) x (0, 2, 0, 12): BIC =20006.246037355937  
 SARIMAX (1, 1, 2) x (0, 2, 1, 12): BIC =19384.36291768391  
 SARIMAX (1, 1, 2) x (0, 2, 2, 12): BIC =19245.450131577953  
 SARIMAX (1, 1, 2) x (1, 0, 0, 12): BIC =18538.436950591975  
 SARIMAX (1, 1, 2) x (1, 0, 1, 12): BIC =18541.304070584618  
 SARIMAX (1, 1, 2) x (1, 0, 2, 12): BIC =18541.329614021466  
 SARIMAX (1, 1, 2) x (1, 1, 0, 12): BIC =18867.068356908872  
 SARIMAX (1, 1, 2) x (1, 1, 1, 12): BIC =18589.604524414204  
 SARIMAX (1, 1, 2) x (1, 1, 2, 12): BIC =18596.139517461663  
 SARIMAX (1, 1, 2) x (1, 2, 0, 12): BIC =19643.445808125467  
 SARIMAX (1, 1, 2) x (1, 2, 1, 12): BIC =19322.165216768317  
 SARIMAX (1, 1, 2) x (1, 2, 2, 12): BIC =19253.49376672465  
 SARIMAX (1, 1, 2) x (2, 0, 0, 12): BIC =18534.385623347764  
 SARIMAX (1, 1, 2) x (2, 0, 1, 12): BIC =18540.871662299163  
 SARIMAX (1, 1, 2) x (2, 0, 2, 12): BIC =18547.32109503398  
 SARIMAX (1, 1, 2) x (2, 1, 0, 12): BIC =18739.926519548615  
 SARIMAX (1, 1, 2) x (2, 1, 1, 12): BIC =18589.718119983052

SARIMAX (1, 1, 2) x (2, 1, 2, 12): BIC =18596.871040702892  
SARIMAX (1, 1, 2) x (2, 2, 0, 12): BIC =19475.75823481145  
SARIMAX (1, 1, 2) x (2, 2, 1, 12): BIC =19283.82098306445  
SARIMAX (1, 1, 2) x (2, 2, 2, 12): BIC =19256.6933424078  
SARIMAX (1, 2, 0) x (0, 0, 0, 12): BIC =18953.205955583344  
SARIMAX (1, 2, 0) x (0, 0, 1, 12): BIC =18959.746675658305  
SARIMAX (1, 2, 0) x (0, 0, 2, 12): BIC =18948.532679302327  
SARIMAX (1, 2, 0) x (0, 1, 0, 12): BIC =19546.96806739077  
SARIMAX (1, 2, 0) x (0, 1, 1, 12): BIC =18864.908932905608  
SARIMAX (1, 2, 0) x (0, 1, 2, 12): BIC =19025.94943167921  
SARIMAX (1, 2, 0) x (0, 2, 0, 12): BIC =20512.13314779995  
SARIMAX (1, 2, 0) x (0, 2, 1, 12): BIC =19693.02371066181  
SARIMAX (1, 2, 0) x (0, 2, 2, 12): BIC =19292.95504241559  
SARIMAX (1, 2, 0) x (1, 0, 0, 12): BIC =18959.87648971524  
SARIMAX (1, 2, 0) x (1, 0, 1, 12): BIC =18956.05661881757  
SARIMAX (1, 2, 0) x (1, 0, 2, 12): BIC =18954.275944345296  
SARIMAX (1, 2, 0) x (1, 1, 0, 12): BIC =19307.894584571484  
SARIMAX (1, 2, 0) x (1, 1, 1, 12): BIC =19028.766308273407  
SARIMAX (1, 2, 0) x (1, 1, 2, 12): BIC =19024.168272182284  
SARIMAX (1, 2, 0) x (1, 2, 0, 12): BIC =20086.035599972514  
SARIMAX (1, 2, 0) x (1, 2, 1, 12): BIC =19414.366555038665  
SARIMAX (1, 2, 0) x (1, 2, 2, 12): BIC =19679.11727012613  
SARIMAX (1, 2, 0) x (2, 0, 0, 12): BIC =18948.91799279198  
SARIMAX (1, 2, 0) x (2, 0, 1, 12): BIC =18954.869325263116  
SARIMAX (1, 2, 0) x (2, 0, 2, 12): BIC =18961.487229807215  
SARIMAX (1, 2, 0) x (2, 1, 0, 12): BIC =19197.451429836186  
SARIMAX (1, 2, 0) x (2, 1, 1, 12): BIC =19025.265024376247  
SARIMAX (1, 2, 0) x (2, 1, 2, 12): BIC =19032.54611761705  
SARIMAX (1, 2, 0) x (2, 2, 0, 12): BIC =19915.37390996378  
SARIMAX (1, 2, 0) x (2, 2, 1, 12): BIC =19716.564269037688  
SARIMAX (1, 2, 0) x (2, 2, 2, 12): BIC =19684.737895759004  
SARIMAX (1, 2, 1) x (0, 0, 0, 12): BIC =18513.520567259333  
SARIMAX (1, 2, 1) x (0, 0, 1, 12): BIC =18538.413421265755  
SARIMAX (1, 2, 1) x (0, 0, 2, 12): BIC =18534.493423118052  
SARIMAX (1, 2, 1) x (0, 1, 0, 12): BIC =19093.595402556588  
SARIMAX (1, 2, 1) x (0, 1, 1, 12): BIC =18465.57390722239  
SARIMAX (1, 2, 1) x (0, 1, 2, 12): BIC =18720.73084206198  
SARIMAX (1, 2, 1) x (0, 2, 0, 12): BIC =20097.089586759004  
SARIMAX (1, 2, 1) x (0, 2, 1, 12): BIC =19368.604047891724  
SARIMAX (1, 2, 1) x (0, 2, 2, 12): BIC =19426.429727887105  
SARIMAX (1, 2, 1) x (1, 0, 0, 12): BIC =18538.564388884242  
SARIMAX (1, 2, 1) x (1, 0, 1, 12): BIC =18541.95467900633  
SARIMAX (1, 2, 1) x (1, 0, 2, 12): BIC =18541.4311481299  
SARIMAX (1, 2, 1) x (1, 1, 0, 12): BIC =18845.814651439985  
SARIMAX (1, 2, 1) x (1, 1, 1, 12): BIC =18721.069927488945  
SARIMAX (1, 2, 1) x (1, 1, 2, 12): BIC =18719.463703487705  
SARIMAX (1, 2, 1) x (1, 2, 0, 12): BIC =19562.573208851034  
SARIMAX (1, 2, 1) x (1, 2, 1, 12): BIC =19491.27501481007  
SARIMAX (1, 2, 1) x (1, 2, 2, 12): BIC =19439.811316203082  
SARIMAX (1, 2, 1) x (2, 0, 0, 12): BIC =18534.334550547737  
SARIMAX (1, 2, 1) x (2, 0, 1, 12): BIC =18541.21170377235  
SARIMAX (1, 2, 1) x (2, 0, 2, 12): BIC =18549.114092052183  
SARIMAX (1, 2, 1) x (2, 1, 0, 12): BIC =18814.6065913138  
SARIMAX (1, 2, 1) x (2, 1, 1, 12): BIC =18722.094384603668  
SARIMAX (1, 2, 1) x (2, 1, 2, 12): BIC =18728.0108522124  
SARIMAX (1, 2, 1) x (2, 2, 0, 12): BIC =19604.867560197472  
SARIMAX (1, 2, 1) x (2, 2, 1, 12): BIC =19463.553469252107  
SARIMAX (1, 2, 1) x (2, 2, 2, 12): BIC =19445.697650029117  
SARIMAX (1, 2, 2) x (0, 0, 0, 12): BIC =18520.65842342449  
SARIMAX (1, 2, 2) x (0, 0, 1, 12): BIC =18528.235352453838  
SARIMAX (1, 2, 2) x (0, 0, 2, 12): BIC =18523.440227408762  
SARIMAX (1, 2, 2) x (0, 1, 0, 12): BIC =19065.137154525073  
SARIMAX (1, 2, 2) x (0, 1, 1, 12): BIC =18396.193511768786  
SARIMAX (1, 2, 2) x (0, 1, 2, 12): BIC =18663.66395830096  
SARIMAX (1, 2, 2) x (0, 2, 0, 12): BIC =19994.812728889545  
SARIMAX (1, 2, 2) x (0, 2, 1, 12): BIC =18969.11530652989  
SARIMAX (1, 2, 2) x (0, 2, 2, 12): BIC =19346.042330863893  
SARIMAX (1, 2, 2) x (1, 0, 0, 12): BIC =18528.17014868882  
SARIMAX (1, 2, 2) x (1, 0, 1, 12): BIC =18531.636702687952  
SARIMAX (1, 2, 2) x (1, 0, 2, 12): BIC =18532.64336775437  
SARIMAX (1, 2, 2) x (1, 1, 0, 12): BIC =18898.553388365766  
SARIMAX (1, 2, 2) x (1, 1, 1, 12): BIC =18663.81418251074

SARIMAX (1, 2, 2) x (1, 1, 2, 12): BIC =18663.087401194836  
 SARIMAX (1, 2, 2) x (1, 2, 0, 12): BIC =19688.034923539606  
 SARIMAX (1, 2, 2) x (1, 2, 1, 12): BIC =19300.9585683983  
 SARIMAX (1, 2, 2) x (1, 2, 2, 12): BIC =19361.076260849186  
 SARIMAX (1, 2, 2) x (2, 0, 0, 12): BIC =18524.344434854946  
 SARIMAX (1, 2, 2) x (2, 0, 1, 12): BIC =18532.789342931093  
 SARIMAX (1, 2, 2) x (2, 0, 2, 12): BIC =18539.76574638735  
 SARIMAX (1, 2, 2) x (2, 1, 0, 12): BIC =18791.123007998067  
 SARIMAX (1, 2, 2) x (2, 1, 1, 12): BIC =18661.41549695926  
 SARIMAX (1, 2, 2) x (2, 1, 2, 12): BIC =18669.183019065575  
 SARIMAX (1, 2, 2) x (2, 2, 0, 12): BIC =19539.677515836094  
 SARIMAX (1, 2, 2) x (2, 2, 1, 12): BIC =19386.666176635088  
 SARIMAX (1, 2, 2) x (2, 2, 2, 12): BIC =19367.50131378798  
 SARIMAX (2, 0, 0) x (0, 0, 0, 12): BIC =18557.166011459583  
 SARIMAX (2, 0, 0) x (0, 0, 1, 12): BIC =18565.532419525727  
 SARIMAX (2, 0, 0) x (0, 0, 2, 12): BIC =18562.86661580995  
 SARIMAX (2, 0, 0) x (0, 1, 0, 12): BIC =19083.081322582493  
 SARIMAX (2, 0, 0) x (0, 1, 1, 12): BIC =18578.139208465545  
 SARIMAX (2, 0, 0) x (0, 1, 2, 12): BIC =18581.03136130843  
 SARIMAX (2, 0, 0) x (0, 2, 0, 12): BIC =20042.284234828872  
 SARIMAX (2, 0, 0) x (0, 2, 1, 12): BIC =19327.872835063336  
 SARIMAX (2, 0, 0) x (0, 2, 2, 12): BIC =19199.324742756053  
 SARIMAX (2, 0, 0) x (1, 0, 0, 12): BIC =18565.0259107411  
 SARIMAX (2, 0, 0) x (1, 0, 1, 12): BIC =18568.573279882963  
 SARIMAX (2, 0, 0) x (1, 0, 2, 12): BIC =18583.967269900833  
 SARIMAX (2, 0, 0) x (1, 1, 0, 12): BIC =18870.660439538784  
 SARIMAX (2, 0, 0) x (1, 1, 1, 12): BIC =18584.018221874496  
 SARIMAX (2, 0, 0) x (1, 1, 2, 12): BIC =18587.21910696633  
 SARIMAX (2, 0, 0) x (1, 2, 0, 12): BIC =19621.948427492647  
 SARIMAX (2, 0, 0) x (1, 2, 1, 12): BIC =19284.054992010973  
 SARIMAX (2, 0, 0) x (1, 2, 2, 12): BIC =19211.440176578075  
 SARIMAX (2, 0, 0) x (2, 0, 0, 12): BIC =18577.46877103056  
 SARIMAX (2, 0, 0) x (2, 0, 1, 12): BIC =18579.072212602514  
 SARIMAX (2, 0, 0) x (2, 0, 2, 12): BIC =18580.38562936004  
 SARIMAX (2, 0, 0) x (2, 1, 0, 12): BIC =18736.234772086413  
 SARIMAX (2, 0, 0) x (2, 1, 1, 12): BIC =18589.0075235071  
 SARIMAX (2, 0, 0) x (2, 1, 2, 12): BIC =18596.22391245864  
 SARIMAX (2, 0, 0) x (2, 2, 0, 12): BIC =19432.87769389369  
 SARIMAX (2, 0, 0) x (2, 2, 1, 12): BIC =19244.03000482958  
 SARIMAX (2, 0, 0) x (2, 2, 2, 12): BIC =19215.58935591644  
 SARIMAX (2, 0, 1) x (0, 0, 0, 12): BIC =18554.569044864802  
 SARIMAX (2, 0, 1) x (0, 0, 1, 12): BIC =18561.90115167353  
 SARIMAX (2, 0, 1) x (0, 0, 2, 12): BIC =18556.943876929723  
 SARIMAX (2, 0, 1) x (0, 1, 0, 12): BIC =19048.280673772264  
 SARIMAX (2, 0, 1) x (0, 1, 1, 12): BIC =18475.82532279902  
 SARIMAX (2, 0, 1) x (0, 1, 2, 12): BIC =18593.86371254886  
 SARIMAX (2, 0, 1) x (0, 2, 0, 12): BIC =19897.42007422542  
 SARIMAX (2, 0, 1) x (0, 2, 1, 12): BIC =19009.473705672226  
 SARIMAX (2, 0, 1) x (0, 2, 2, 12): BIC =19208.68444748363  
 SARIMAX (2, 0, 1) x (1, 0, 0, 12): BIC =18562.097352572942  
 SARIMAX (2, 0, 1) x (1, 0, 1, 12): BIC =18566.62163573937  
 SARIMAX (2, 0, 1) x (1, 0, 2, 12): BIC =18563.54704156988  
 SARIMAX (2, 0, 1) x (1, 1, 0, 12): BIC =18877.12048846786  
 SARIMAX (2, 0, 1) x (1, 1, 1, 12): BIC =18593.94021668683  
 SARIMAX (2, 0, 1) x (1, 1, 2, 12): BIC =18598.257196277922  
 SARIMAX (2, 0, 1) x (1, 2, 0, 12): BIC =19568.967910412826  
 SARIMAX (2, 0, 1) x (1, 2, 1, 12): BIC =18836.495740881746  
 SARIMAX (2, 0, 1) x (1, 2, 2, 12): BIC =19217.65635009182  
 SARIMAX (2, 0, 1) x (2, 0, 0, 12): BIC =18555.79526397292  
 SARIMAX (2, 0, 1) x (2, 0, 1, 12): BIC =18564.1211283127  
 SARIMAX (2, 0, 1) x (2, 0, 2, 12): BIC =18578.45691437732  
 SARIMAX (2, 0, 1) x (2, 1, 0, 12): BIC =18747.703881803547  
 SARIMAX (2, 0, 1) x (2, 1, 1, 12): BIC =18590.127325145342  
 SARIMAX (2, 0, 1) x (2, 1, 2, 12): BIC =18605.798083251855  
 SARIMAX (2, 0, 1) x (2, 2, 0, 12): BIC =19418.81713126018  
 SARIMAX (2, 0, 1) x (2, 2, 1, 12): BIC =19248.598168937915  
 SARIMAX (2, 0, 1) x (2, 2, 2, 12): BIC =19223.95380429447  
 SARIMAX (2, 0, 2) x (0, 0, 0, 12): BIC =18561.91875210275  
 SARIMAX (2, 0, 2) x (0, 0, 1, 12): BIC =18568.900234377084  
 SARIMAX (2, 0, 2) x (0, 0, 2, 12): BIC =18569.26222345265  
 SARIMAX (2, 0, 2) x (0, 1, 0, 12): BIC =19063.24130470544  
 SARIMAX (2, 0, 2) x (0, 1, 1, 12): BIC =18593.634447219472



SARIMAX (2, 0, 2) x (0, 1, 2, 12): BIC =18604.116845155575  
SARIMAX (2, 0, 2) x (0, 2, 0, 12): BIC =19898.06541264086  
SARIMAX (2, 0, 2) x (0, 2, 1, 12): BIC =19343.255367799942  
SARIMAX (2, 0, 2) x (0, 2, 2, 12): BIC =19208.326178973788  
SARIMAX (2, 0, 2) x (1, 0, 0, 12): BIC =18569.20562116669  
SARIMAX (2, 0, 2) x (1, 0, 1, 12): BIC =18574.02867343672  
SARIMAX (2, 0, 2) x (1, 0, 2, 12): BIC =18571.999440832304  
SARIMAX (2, 0, 2) x (1, 1, 0, 12): BIC =18883.373831447185  
SARIMAX (2, 0, 2) x (1, 1, 1, 12): BIC =18608.745500568664  
SARIMAX (2, 0, 2) x (1, 1, 2, 12): BIC =18607.305841909514  
SARIMAX (2, 0, 2) x (1, 2, 0, 12): BIC =19568.103550232616  
SARIMAX (2, 0, 2) x (1, 2, 1, 12): BIC =19287.575336678805  
SARIMAX (2, 0, 2) x (1, 2, 2, 12): BIC =19218.03359230143  
SARIMAX (2, 0, 2) x (2, 0, 0, 12): BIC =18563.591715709783  
SARIMAX (2, 0, 2) x (2, 0, 1, 12): BIC =18570.182681718034  
SARIMAX (2, 0, 2) x (2, 0, 2, 12): BIC =18585.893941146496  
SARIMAX (2, 0, 2) x (2, 1, 0, 12): BIC =18752.380063881395  
SARIMAX (2, 0, 2) x (2, 1, 1, 12): BIC =18596.55385079806  
SARIMAX (2, 0, 2) x (2, 1, 2, 12): BIC =18609.38182265908  
SARIMAX (2, 0, 2) x (2, 2, 0, 12): BIC =19417.408013901048  
SARIMAX (2, 0, 2) x (2, 2, 1, 12): BIC =19248.863141953043  
SARIMAX (2, 0, 2) x (2, 2, 2, 12): BIC =19219.387636715885  
SARIMAX (2, 1, 0) x (0, 0, 0, 12): BIC =18526.82552219505  
SARIMAX (2, 1, 0) x (0, 0, 1, 12): BIC =18533.881079136674  
SARIMAX (2, 1, 0) x (0, 0, 2, 12): BIC =18530.994428201604  
SARIMAX (2, 1, 0) x (0, 1, 0, 12): BIC =19101.645264917905  
SARIMAX (2, 1, 0) x (0, 1, 1, 12): BIC =18422.22175341525  
SARIMAX (2, 1, 0) x (0, 1, 2, 12): BIC =18587.55585793272  
SARIMAX (2, 1, 0) x (0, 2, 0, 12): BIC =20082.482845372513  
SARIMAX (2, 1, 0) x (0, 2, 1, 12): BIC =19382.41446126037  
SARIMAX (2, 1, 0) x (0, 2, 2, 12): BIC =19237.277582056464  
SARIMAX (2, 1, 0) x (1, 0, 0, 12): BIC =18533.889240374145  
SARIMAX (2, 1, 0) x (1, 0, 1, 12): BIC =18536.359459968535  
SARIMAX (2, 1, 0) x (1, 0, 2, 12): BIC =18537.40799138459  
SARIMAX (2, 1, 0) x (1, 1, 0, 12): BIC =18879.878747536866  
SARIMAX (2, 1, 0) x (1, 1, 1, 12): BIC =18588.272212901073  
SARIMAX (2, 1, 0) x (1, 1, 2, 12): BIC =18594.159570713982  
SARIMAX (2, 1, 0) x (1, 2, 0, 12): BIC =19658.311315514737  
SARIMAX (2, 1, 0) x (1, 2, 1, 12): BIC =19319.21526220429  
SARIMAX (2, 1, 0) x (1, 2, 2, 12): BIC =19245.83806483477  
SARIMAX (2, 1, 0) x (2, 0, 0, 12): BIC =18530.698063392672  
SARIMAX (2, 1, 0) x (2, 0, 1, 12): BIC =18536.910459300198  
SARIMAX (2, 1, 0) x (2, 0, 2, 12): BIC =18543.12591853057  
SARIMAX (2, 1, 0) x (2, 1, 0, 12): BIC =18738.770827041713  
SARIMAX (2, 1, 0) x (2, 1, 1, 12): BIC =18585.252255304  
SARIMAX (2, 1, 0) x (2, 1, 2, 12): BIC =18592.270423553182  
SARIMAX (2, 1, 0) x (2, 2, 0, 12): BIC =19466.546484768583  
SARIMAX (2, 1, 0) x (2, 2, 1, 12): BIC =19275.66352979381  
SARIMAX (2, 1, 0) x (2, 2, 2, 12): BIC =19250.043882107446  
SARIMAX (2, 1, 1) x (0, 0, 0, 12): BIC =18531.781794727725  
SARIMAX (2, 1, 1) x (0, 0, 1, 12): BIC =18538.842766955946  
SARIMAX (2, 1, 1) x (0, 0, 2, 12): BIC =18535.04268964091  
SARIMAX (2, 1, 1) x (0, 1, 0, 12): BIC =19108.82802172192  
SARIMAX (2, 1, 1) x (0, 1, 1, 12): BIC =18491.596353722714  
SARIMAX (2, 1, 1) x (0, 1, 2, 12): BIC =18590.557718994434  
SARIMAX (2, 1, 1) x (0, 2, 0, 12): BIC =20083.96052282967  
SARIMAX (2, 1, 1) x (0, 2, 1, 12): BIC =19378.202179938296  
SARIMAX (2, 1, 1) x (0, 2, 2, 12): BIC =19221.799967457864  
SARIMAX (2, 1, 1) x (1, 0, 0, 12): BIC =18538.84619586847  
SARIMAX (2, 1, 1) x (1, 0, 1, 12): BIC =18541.725726353685  
SARIMAX (2, 1, 1) x (1, 0, 2, 12): BIC =18541.71911355756  
SARIMAX (2, 1, 1) x (1, 1, 0, 12): BIC =18883.681367230958  
SARIMAX (2, 1, 1) x (1, 1, 1, 12): BIC =18587.318728236045  
SARIMAX (2, 1, 1) x (1, 1, 2, 12): BIC =18593.44220449029  
SARIMAX (2, 1, 1) x (1, 2, 0, 12): BIC =19655.809047655282  
SARIMAX (2, 1, 1) x (1, 2, 1, 12): BIC =19305.70586183955  
SARIMAX (2, 1, 1) x (1, 2, 2, 12): BIC =19231.863311547146  
SARIMAX (2, 1, 1) x (2, 0, 0, 12): BIC =18534.78927908915  
SARIMAX (2, 1, 1) x (2, 0, 1, 12): BIC =18541.259869906717  
SARIMAX (2, 1, 1) x (2, 0, 2, 12): BIC =18547.68118667028  
SARIMAX (2, 1, 1) x (2, 1, 0, 12): BIC =18738.85868781077  
SARIMAX (2, 1, 1) x (2, 1, 1, 12): BIC =18584.3722326821

SARIMAX (2, 1, 1) x (2, 1, 2, 12): BIC =18591.603053206407  
SARIMAX (2, 1, 1) x (2, 2, 0, 12): BIC =19463.013617341087  
SARIMAX (2, 1, 1) x (2, 2, 1, 12): BIC =19263.06011086457  
SARIMAX (2, 1, 1) x (2, 2, 2, 12): BIC =19233.842333391487  
SARIMAX (2, 1, 2) x (0, 0, 0, 12): BIC =18508.893069144186  
SARIMAX (2, 1, 2) x (0, 0, 1, 12): BIC =18523.22046444815  
SARIMAX (2, 1, 2) x (0, 0, 2, 12): BIC =18528.30104412841  
SARIMAX (2, 1, 2) x (0, 1, 0, 12): BIC =19071.425814194685  
SARIMAX (2, 1, 2) x (0, 1, 1, 12): BIC =18587.30836915535  
SARIMAX (2, 1, 2) x (0, 1, 2, 12): BIC =18603.734303744575  
SARIMAX (2, 1, 2) x (0, 2, 0, 12): BIC =19960.59212894137  
SARIMAX (2, 1, 2) x (0, 2, 1, 12): BIC =19367.429793716816  
SARIMAX (2, 1, 2) x (0, 2, 2, 12): BIC =19248.671789242908  
SARIMAX (2, 1, 2) x (1, 0, 0, 12): BIC =18520.657626383974  
SARIMAX (2, 1, 2) x (1, 0, 1, 12): BIC =18523.516906551267  
SARIMAX (2, 1, 2) x (1, 0, 2, 12): BIC =18532.369237309005  
SARIMAX (2, 1, 2) x (1, 1, 0, 12): BIC =18844.212961262994  
SARIMAX (2, 1, 2) x (1, 1, 1, 12): BIC =18596.54346859124  
SARIMAX (2, 1, 2) x (1, 1, 2, 12): BIC =18601.47214222178  
SARIMAX (2, 1, 2) x (1, 2, 0, 12): BIC =19625.12392649973  
SARIMAX (2, 1, 2) x (1, 2, 1, 12): BIC =19327.213496025804  
SARIMAX (2, 1, 2) x (1, 2, 2, 12): BIC =19254.70807906285  
SARIMAX (2, 1, 2) x (2, 0, 0, 12): BIC =18519.900765916114  
SARIMAX (2, 1, 2) x (2, 0, 1, 12): BIC =18538.695814042265  
SARIMAX (2, 1, 2) x (2, 0, 2, 12): BIC =18541.70495403264  
SARIMAX (2, 1, 2) x (2, 1, 0, 12): BIC =18739.70964302934  
SARIMAX (2, 1, 2) x (2, 1, 1, 12): BIC =18594.876753390996  
SARIMAX (2, 1, 2) x (2, 1, 2, 12): BIC =18599.988330118507  
SARIMAX (2, 1, 2) x (2, 2, 0, 12): BIC =19472.44700808779  
SARIMAX (2, 1, 2) x (2, 2, 1, 12): BIC =19288.058689588663  
SARIMAX (2, 1, 2) x (2, 2, 2, 12): BIC =19260.63804547856  
SARIMAX (2, 2, 0) x (0, 0, 0, 12): BIC =18788.815059132747  
SARIMAX (2, 2, 0) x (0, 0, 1, 12): BIC =18795.369066401097  
SARIMAX (2, 2, 0) x (0, 0, 2, 12): BIC =18786.946671333848  
SARIMAX (2, 2, 0) x (0, 1, 0, 12): BIC =19336.78452928554  
SARIMAX (2, 2, 0) x (0, 1, 1, 12): BIC =18836.082284679655  
SARIMAX (2, 2, 0) x (0, 1, 2, 12): BIC =18848.970231614323  
SARIMAX (2, 2, 0) x (0, 2, 0, 12): BIC =20277.702248035785  
SARIMAX (2, 2, 0) x (0, 2, 1, 12): BIC =19603.37254031362  
SARIMAX (2, 2, 0) x (0, 2, 2, 12): BIC =19454.025080682804  
SARIMAX (2, 2, 0) x (1, 0, 0, 12): BIC =18795.492311862807  
SARIMAX (2, 2, 0) x (1, 0, 1, 12): BIC =18798.87903558279  
SARIMAX (2, 2, 0) x (1, 0, 2, 12): BIC =18793.02524540705  
SARIMAX (2, 2, 0) x (1, 1, 0, 12): BIC =19144.636415090376  
SARIMAX (2, 2, 0) x (1, 1, 1, 12): BIC =18847.16424363538  
SARIMAX (2, 2, 0) x (1, 1, 2, 12): BIC =18850.75617625589  
SARIMAX (2, 2, 0) x (1, 2, 0, 12): BIC =19885.183243652817  
SARIMAX (2, 2, 0) x (1, 2, 1, 12): BIC =19540.76933854248  
SARIMAX (2, 2, 0) x (1, 2, 2, 12): BIC =19466.456014253323  
SARIMAX (2, 2, 0) x (2, 0, 0, 12): BIC =18785.84892605923  
SARIMAX (2, 2, 0) x (2, 0, 1, 12): BIC =18792.619507490315  
SARIMAX (2, 2, 0) x (2, 0, 2, 12): BIC =18799.46609167564  
SARIMAX (2, 2, 0) x (2, 1, 0, 12): BIC =19017.19025624109  
SARIMAX (2, 2, 0) x (2, 1, 1, 12): BIC =18850.06906952655  
SARIMAX (2, 2, 0) x (2, 1, 2, 12): BIC =18846.399797409566  
SARIMAX (2, 2, 0) x (2, 2, 0, 12): BIC =19718.64805528352  
SARIMAX (2, 2, 0) x (2, 2, 1, 12): BIC =19501.57175607166  
SARIMAX (2, 2, 0) x (2, 2, 2, 12): BIC =19465.816284306602  
SARIMAX (2, 2, 1) x (0, 0, 0, 12): BIC =18536.7833268373  
SARIMAX (2, 2, 1) x (0, 0, 1, 12): BIC =18543.577120189122  
SARIMAX (2, 2, 1) x (0, 0, 2, 12): BIC =18540.774031358604  
SARIMAX (2, 2, 1) x (0, 1, 0, 12): BIC =19121.505265065287  
SARIMAX (2, 2, 1) x (0, 1, 1, 12): BIC =18700.436422346476  
SARIMAX (2, 2, 1) x (0, 1, 2, 12): BIC =18709.71616485042  
SARIMAX (2, 2, 1) x (0, 2, 0, 12): BIC =20094.972432754417  
SARIMAX (2, 2, 1) x (0, 2, 1, 12): BIC =19518.996010201517  
SARIMAX (2, 2, 1) x (0, 2, 2, 12): BIC =19391.053707667448  
SARIMAX (2, 2, 1) x (1, 0, 0, 12): BIC =18544.110807261695  
SARIMAX (2, 2, 1) x (1, 0, 1, 12): BIC =18551.710296712212  
SARIMAX (2, 2, 1) x (1, 0, 2, 12): BIC =18547.89306569926  
SARIMAX (2, 2, 1) x (1, 1, 0, 12): BIC =18940.4297379643  
SARIMAX (2, 2, 1) x (1, 1, 1, 12): BIC =18705.522027331503

SARIMAX (2, 2, 1) x (1, 1, 2, 12): BIC =18710.783822262176  
 SARIMAX (2, 2, 1) x (1, 2, 0, 12): BIC =19738.742133586733  
 SARIMAX (2, 2, 1) x (1, 2, 1, 12): BIC =19457.4593393265  
 SARIMAX (2, 2, 1) x (1, 2, 2, 12): BIC =19400.12776380892  
 SARIMAX (2, 2, 1) x (2, 0, 0, 12): BIC =18539.42084116585  
 SARIMAX (2, 2, 1) x (2, 0, 1, 12): BIC =18547.347259861734  
 SARIMAX (2, 2, 1) x (2, 0, 2, 12): BIC =18553.63355512256  
 SARIMAX (2, 2, 1) x (2, 1, 0, 12): BIC =18827.32453148663  
 SARIMAX (2, 2, 1) x (2, 1, 1, 12): BIC =18706.03364044882  
 SARIMAX (2, 2, 1) x (2, 1, 2, 12): BIC =18715.513250824624  
 SARIMAX (2, 2, 1) x (2, 2, 0, 12): BIC =19580.62465859039  
 SARIMAX (2, 2, 1) x (2, 2, 1, 12): BIC =19424.023038999985  
 SARIMAX (2, 2, 1) x (2, 2, 2, 12): BIC =19404.65742069795  
 SARIMAX (2, 2, 2) x (0, 0, 0, 12): BIC =18528.295638455187  
 SARIMAX (2, 2, 2) x (0, 0, 1, 12): BIC =18537.179513727497  
 SARIMAX (2, 2, 2) x (0, 0, 2, 12): BIC =18530.894154715053  
 SARIMAX (2, 2, 2) x (0, 1, 0, 12): BIC =19075.052431286553  
 SARIMAX (2, 2, 2) x (0, 1, 1, 12): BIC =18392.949306524013  
 SARIMAX (2, 2, 2) x (0, 1, 2, 12): BIC =18660.61578950005  
 SARIMAX (2, 2, 2) x (0, 2, 0, 12): BIC =20013.316549359923  
 SARIMAX (2, 2, 2) x (0, 2, 1, 12): BIC =19461.50301369961  
 SARIMAX (2, 2, 2) x (0, 2, 2, 12): BIC =19335.300856050824  
 SARIMAX (2, 2, 2) x (1, 0, 0, 12): BIC =18537.3352928159  
 SARIMAX (2, 2, 2) x (1, 0, 1, 12): BIC =18539.40095300109  
 SARIMAX (2, 2, 2) x (1, 0, 2, 12): BIC =18538.131769572137  
 SARIMAX (2, 2, 2) x (1, 1, 0, 12): BIC =18901.647140157485  
 SARIMAX (2, 2, 2) x (1, 1, 1, 12): BIC =18659.93199260413  
 SARIMAX (2, 2, 2) x (1, 1, 2, 12): BIC =18667.614708787172  
 SARIMAX (2, 2, 2) x (1, 2, 0, 12): BIC =19680.837230849964  
 SARIMAX (2, 2, 2) x (1, 2, 1, 12): BIC =19379.5258540444  
 SARIMAX (2, 2, 2) x (1, 2, 2, 12): BIC =19347.02858160338  
 SARIMAX (2, 2, 2) x (2, 0, 0, 12): BIC =18530.773066116562  
 SARIMAX (2, 2, 2) x (2, 0, 1, 12): BIC =18538.35992701235  
 SARIMAX (2, 2, 2) x (2, 0, 2, 12): BIC =18545.52575251914  
 SARIMAX (2, 2, 2) x (2, 1, 0, 12): BIC =18788.625159827396  
 SARIMAX (2, 2, 2) x (2, 1, 1, 12): BIC =18658.4656191886  
 SARIMAX (2, 2, 2) x (2, 1, 2, 12): BIC =18667.41331327403  
 SARIMAX (2, 2, 2) x (2, 2, 0, 12): BIC =19529.76866152616  
 SARIMAX (2, 2, 2) x (2, 2, 1, 12): BIC =19369.929988156397  
 SARIMAX (2, 2, 2) x (2, 2, 2, 12): BIC =19351.284693490117