

Introduction to Statistics

Probability and Inference Quiz

Instructions:

- Answer all questions.
- For Questions 1–5, choose the best option.
- For Questions 6–8, mark True or False.
- For Questions 9–10, write detailed answers with calculations where appropriate.

1. If $P(A) = 0.3$ and $P(B) = 0.4$, and A and B are independent events, what is $P(A \cap B)$?
 - (A) 0.70
 - (B) 0.12
 - (C) 0.10
 - (D) 0.58
2. The Central Limit Theorem states that:
 - (A) All populations are normally distributed
 - (B) Sample means approach a normal distribution as sample size increases
 - (C) Larger samples always have smaller means
 - (D) The median equals the mean in all distributions
3. A Type I error occurs when:
 - (A) Failing to reject a false null hypothesis
 - (B) Rejecting a true null hypothesis
 - (C) The sample size is too small
 - (D) The p-value is greater than alpha
4. Which measure of central tendency is most resistant to outliers?
 - (A) Mean
 - (B) Median
 - (C) Mode
 - (D) Range

- 5.** A 95% confidence interval means:
- (A) 95% of the data falls within the interval
 - (B) There is a 95% probability the true parameter is in this specific interval
 - (C) 95% of similarly constructed intervals would contain the true parameter
 - (D) The sample mean is 95% accurate
- 6.** The standard deviation of a sampling distribution is called the standard error. (True/False)
- 7.** A p-value of 0.03 means there is a 3% chance the null hypothesis is true. (True/False)
- 8.** Correlation implies causation between two variables. (True/False)
- 9.** Explain the difference between descriptive and inferential statistics. Provide examples of when each would be appropriate and discuss the role of sampling in making inferences about populations.
- 10.** Describe the process of hypothesis testing, including the null and alternative hypotheses, significance level, p-value, and decision rules. Use an example to illustrate each step.