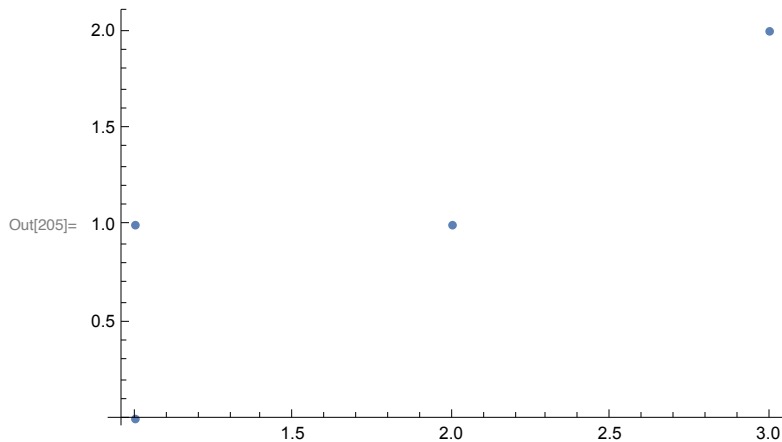


ListPlot examples

To plot a function, you use Plot. To plot a collection of points, you use ListPlot.

```
In[204]:= list = {{1, 0}, {1, 1}, {2, 1}, {3, 2}};  
ListPlot[list]
```

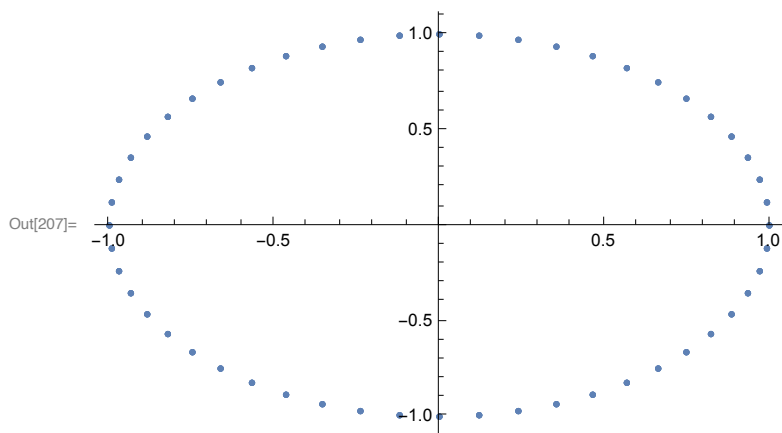


Here are examples of plotting all of the points given by $(A^k)X$, where A is a 2×2 matrix, and X is an initial point in the xy plane. We will let “mat” be our matrix, and we will obtain a list of points by using the Table command. By plugging this into the ListPlot command, we can get a graph of the points of the form $A^k X$.

(Note that in order to switch back and forth between row/column matrices, I am using the Transpose command, along with the fact that $(AB)^T = B^T A^T$.)

```
In[206]:= mat = N[ $\begin{bmatrix} \text{Cos}[2 \text{ Pi} * (1 / 52)] & -\text{Sin}[2 \text{ Pi} (1 / 52)] \\ \text{Sin}[2 \text{ Pi} (1 / 52)] & \text{Cos}[2 \text{ Pi} (1 / 52)] \end{bmatrix}$ ];
```

```
ListPlot[Table[{0, 1}.Transpose[MatrixPower[mat, k]], {k, 0, 200}]]
```



By combining the above with the Manipulate command, we can get a nice picture showing us how a

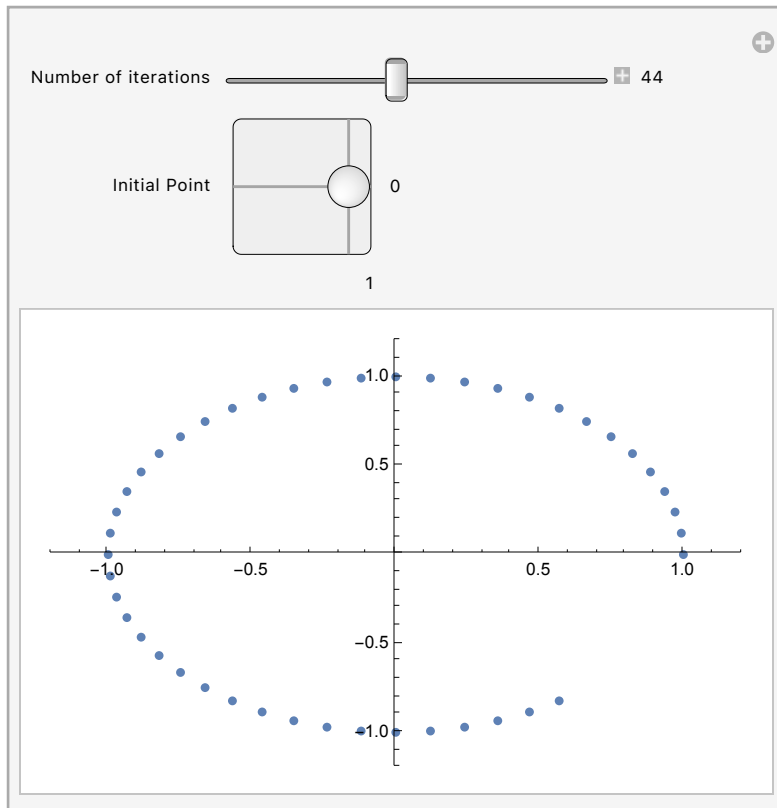
point evolves along progressive iterations along with how things change as the initial point changes.

```
In[208]:= mat1 = N[
$$\begin{pmatrix} \cos[2 \pi (1/52)] & -\sin[2 \pi (1/52)] \\ \sin[2 \pi (1/52)] & \cos[2 \pi (1/52)] \end{pmatrix}];$$

```

```
Manipulate[
  ListPlot[Table[x.Transpose[MatrixPower[mat1, k]], {k, 0, n}],
    PlotRange → {{-1.2, 1.2}, {-1.2, 1.2}},
    {{n, 0, "Number of iterations"}, 0, 100, 1, Appearance → "Labeled"},
    {{x, {1, 0}, "Initial Point"}, -1, 1,
      ControlType → Slider2D, Appearance → "Labeled"} ]
```

Out[209]=

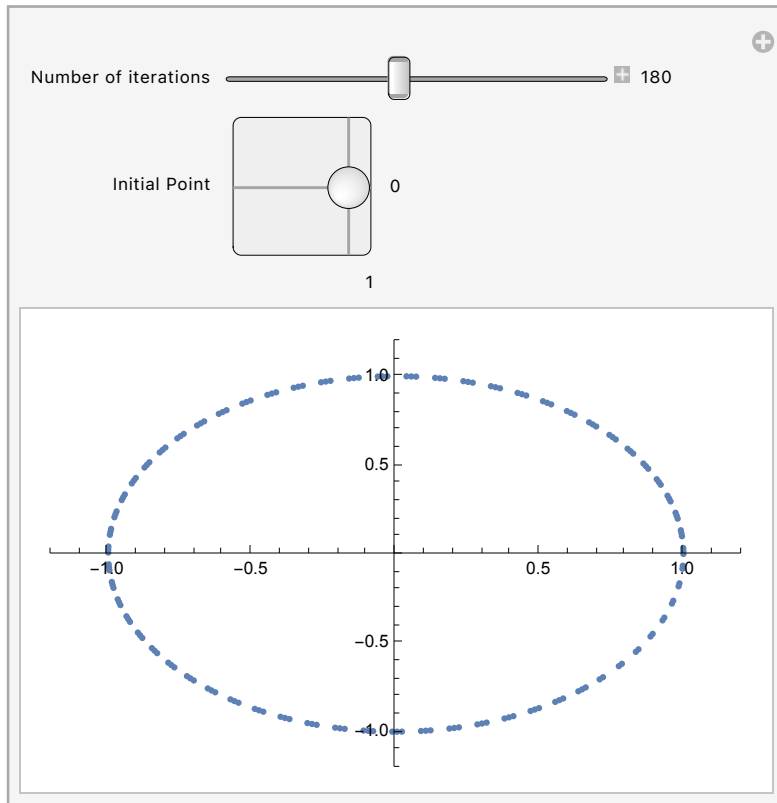


Here's another example, but the matrix has been changed slightly.

```
In[210]:= mat2 = N[ $\begin{pmatrix} \cos[.1] & -\sin[.1] \\ \sin[.1] & \cos[.1] \end{pmatrix}$ ];
```

```
Manipulate[
  ListPlot[Table[x.Transpose[MatrixPower[mat2, k]], {k, 0, n}],
    PlotRange → {{-1.2, 1.2}, {-1.2, 1.2}},
    {{n, 0, "Number of iterations"}, 0, 400, 1, Appearance → "Labeled"},
    {{x, {1, 0}, "Initial Point"}, -1, 1,
      ControlType → Slider2D, Appearance → "Labeled"} ]
```

Out[211]=



Here is a visualization of the example we did at the beginning of class, where the linear transformation satisfied

$T(2,1) = 2(2,1)$ and $T(0,1) = .5(0,1)$.

```
In[212]:= mat3 = N[ $\begin{pmatrix} 2 & 0 \\ 3/4 & 1/2 \end{pmatrix}$ ];
```

```
Manipulate[
  ListPlot[Table[x.Transpose[MatrixPower[mat3, k]], {k, 0, n}],
    PlotRange → {{-10, 10}, {-5, 5}},
    {{n, 0, "Number of iterations"}, 0, 20, 1, Appearance → "Labeled"},
    {{x, {0, 1}, "Initial Point"}, -1, 1,
      ControlType → Slider2D, Appearance → "Labeled"} ]
```

Out[213]=

