## **Circle Modeling**

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## **Background: Geometric Models**

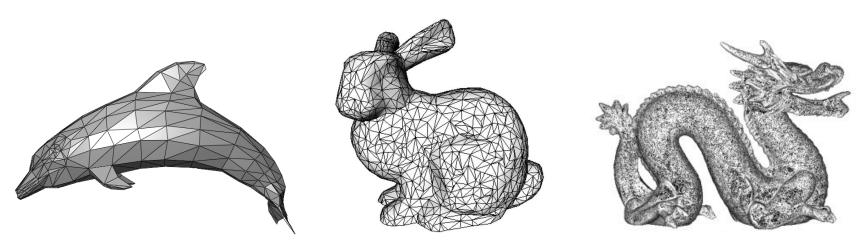
### **Models**

#### Models:

Mathematical abstraction of the real world or virtual worlds.

#### Geometric Models:

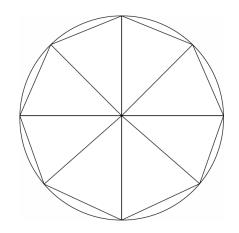
- In CG, we model our worlds with geometric objects.
- Building blocks: a set of simple 3D primitives (points, lines, triangles, ...)
- *Triangular meshes* are common, which comprises a set of triangles connected by their common edges or corners.

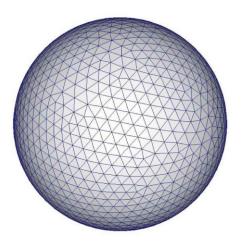


### **3D Primitives**

### 3D objects that fit well with graphics HW and SW:

- described by their 2D surfaces and can be thought of as being hollow.
  - c.f., objects with 3D surfaces are called the volumetric objects (e.g., CT).
- can be specified through a set of vertices.
- either are composed of or can be approximated by flat, convex polygons.
  - e.g., a circle/sphere approximated by flat triangles.





### **3D Primitives**

### Why we set these conditions?

- Modern graphics systems are optimized for rendering triangles or meshes of triangles (e.g., more than 100 M triangles / sec.).
  - Points and lines are also supported well.
- Vertices can be processed with the pipeline architecture, independently.

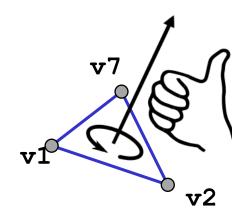
### Why are triangles fundamental primitives?

- The triangles are always flat.
- General polygons might not lie in the same plane, and then, there is no simple way to define interior of the object.
- Also, general polygons can be decomposed into a set of triangles:
  - then, we can apply the same pipeline on the triangles.

# **More on State Setup**

## **Vertex Ordering for a Triangle**

- In general, triangles are not double-sided.
  - Hence, we need to set the direction of a triangle face.
  - In OpenGL, we use the order of vertices to distinguish front-facing vs. back-facing triangles.
    - Counter-clockwise encirclement of outward-pointing normal.



 The order {v1, v2, v7} and {v2, v7, v1} (front-facing) define the same polygon with the same face direction, but the order {v1, v7, v2} (back-facing) is different.

## **Back-Face Culling**

- By default, OpenGL will render back-facing triangles as well as front-facing triangles.
  - You need to explicitly command not to render back-facing triangles.

- This mechanism is called the back-face culling.
- You can query the current state of the face culling as follows.

```
glIsEnabled( GL_CULL_FACE );
```

## Wireframe mode rendering

### Wireframe mode (desktop only):

- To see how triangles are organized, we can turn on the wireframe mode.
- Set glPolygonMode as GL\_LINE for wireframe mode or GL\_FILL for solid mode.
- You can change the line width using glLineWidth().

```
void keyboard( GLFWwindow* window, int key, int scancode, int action, int mods )
{
    ...
    else if(key==GLFW_KEY_W)
    {
        bWireframe = !bWireframe;
        glPolygonMode( GL_FRONT_AND_BACK, bWireframe ? GL_LINE:GL_FILL );
        printf( "> using %s mode\n", bWireframe ? "wireframe" : "solid" );
    }
    ...
}
```

## **Definition of Geometry**

## Where you make a geometry

### It actually does not matter.

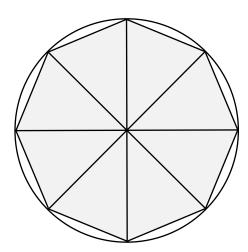
- as long as OpenGL stuffs are initialized.
- However, it is clean and easy to do it in user\_init().
- This is because we usually create geometric objects only once.

```
// usually called after basic GL stuffs are initialized
void user_init()
{
    ... // create objects here ...
}
```

### **Circle Definition**

### Polygonal approximation of a circle

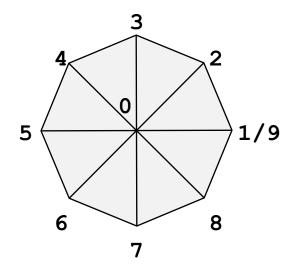
- Modern OpenGL supports only triangles as polygonal primitives.
  - Implicit curves, such as a circle, are not supported.
  - That is, we cannot use  $x^2 + y^2 = r^2$  for drawing.
- We thus need to approximate a circle using a finite set of triangles.
- As we increase the number of triangles, the shape becomes close to circle.



An octagonal approximation of a circle

### **Circle Definition**

#### Definition of vertex indices of vertices



#### Polar coordinates of vertices

 k-th boundary vertex of N-gon of a radius one has the following polar coordinates:

$$(x,y) = (\cos\frac{2\pi}{N} \times k, \sin\frac{2\pi}{N} \times k)$$

### **Circle Definition**

### Define arrays for vertices

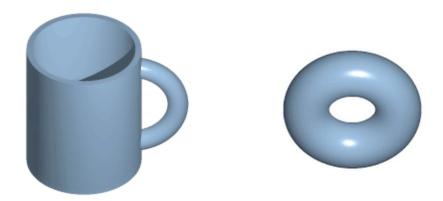
- Be sure that the positions here are defined in LHS form of the canonical view volume; z-axis goes farther from the eye.
  - This 2D circle is actually defined in 3D (z=0)
  - When you model 3D objects, pay more attention to the z axis.

```
std::vector<vertex> create_circle_vertices( uint N )
   std::vector<vertex> v = \{\{ vec3(0), vec3(0,0,-1.0f), vec2(0.5f) \}\}; // origin
   for( uint k=0; k <= N; k++ )
      float t = PI*2.0f*k/float(N), c=cos(t), s=sin(t);
      v.push_back
      ({
          vec3(c,s,0),
                        // vertex position
         vec3(0,0,-1.0f), // normal vector facing your eye vec2(c,s)*0.5f+0.5f // texture coordinate in ([0,1], [0,1])
      });
   return v;
```

# **Object Specification**

## **Geometry vs. Topology**

- Generally, it is a good idea to look for data structures that separate the geometry from the topology
  - Geometry: locations of the vertices
  - Topology: structural organization of the vertices and edges
    - Connectedness is preserved under continuous deformation
    - Topology holds even if geometry changes

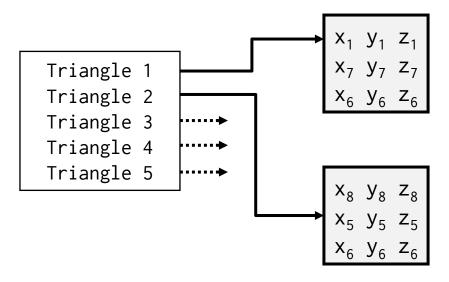


The cup and torus share the same topology.

## **Method 1: Simple Vertex Buffering**

### A single vertex buffer defines geometry and topology.

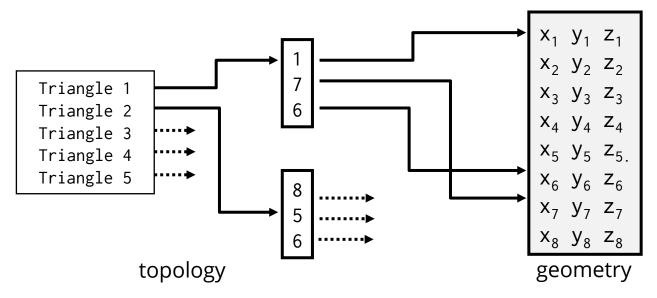
- Topology information is hard-coded in a vertex buffer.
- When a vertex moves to a new location, we must search and replace it for all the occurrences.
- Often inefficient and unstructured.



## **Method 2: Index Buffering**

### Using vertex buffer + index buffer together

- Topology is separated from geometry by indexing scheme.
- Use indices from the vertices into this array.



### Typically faster than simple vertex buffering

 Index buffering avoids redundant vertex shading, while the simple vertexonly buffering has duplicate vertices in its definition.

# **Simple Vertex-Only Buffering**

## **Simple Vertex Buffering**

- For an N-gon, we need N×3 vertices.
  - Pay attention to make out-facing triangles (counter-clockwise order)

```
void update_vertex_buffer( const std::vector<vertex>& vertices, uint N )
{
   std::vector<vertex> v; // triangle vertices
   for( uint k=0; k < N; k++)
      v.push_back(vertices.front()); // the origin
     v.push_back(vertices[k+1]);
      v.push_back(vertices[k+2]);
   // generation of vertex buffer: use triangle_vertices instead of vertex_list
   glGenBuffers( 1, &vertex_buffer );
   glBindBuffer( GL_ARRAY_BUFFER, vertex_buffer );
   glBufferData( GL_ARRAY_BUFFER, sizeof(vertex)*v.size(), &v[0], GL_STATIC_DRAW );
```

## **Simple Vertex Buffering**

### render()

Render N×3 vertices instead of 3 vertices in the hello example.

```
void render()
{
    ...

// render vertices: trigger shader programs to process vertex data
    glDrawArrays( GL_TRIANGLES, 0, NUM_TESS*3 ); // NUM_TESS = N
    ...
}
```

#### Index definition

- We only specify the topology for indices.
- Use the vertex buffer array (for geometry) as it is.
- We use N×3 indices unlike the simple vertex buffering.

```
void update_vertex_buffer( const std::vector<vertex>& vertices, uint N )
{
    ...
    indices.clear();
    for( uint k=0; k < N; k++ )
    {
        indices.push_back(0); // the origin
        indices.push_back(k+1);
        indices.push_back(k+2);
    }
}</pre>
```

### Vertex/index buffer definition

- We need two buffers, vertex buffer and index buffer, simultaneously.
- The index buffer uses **GL\_ELEMENT\_ARRAY\_BUFFER** as a buffer type.
- Vertex buffer will use the initial vertices directly (without connectivity).

```
void update_vertex_buffer( const std::vector<vertex>& vertices, uint N )
{
    ...

// generation of vertex buffer: use vertex_list as it is
    glGenBuffers( 1, &vertex_buffer );
    glBindBuffer( GL_ARRAY_BUFFER, vertex_buffer );
    glBufferData( GL_ARRAY_BUFFER, sizeof(vertex)*vertics.size(), &vertices[0], GL_STATIC_DRAW);

// geneation of index buffer
    glGenBuffers( 1, &index_buffer );
    glBindBuffer(GL_ELEMENT_ARRAY_BUFFER,index_buffer);
    glBindBuffer(GL_ELEMENT_ARRAY_BUFFER,sizeof(uint)*indices.size(),&indices[0],GL_STATIC_DRAW);
}
```

### Vertex array definition with index buffering

- Unlike the simple vertex-only buffering, we also provide the index buffer as input cg\_create\_vertex\_array().
- When you bind the vertex array, the vertex and index buffers and their binding are bound at the same time.

```
void update_vertex_buffer( const std::vector<vertex>& vertices, uint N )
{
    ...
    // generate vertex array object, which is mandatory for OpenGL 3.3 and higher if(vertex_array) glDeleteVertexArrays(1,&vertex_array);
    vertex_array = cg_create_vertex_array( vertex_buffer, index_buffer );
}
```

### render()

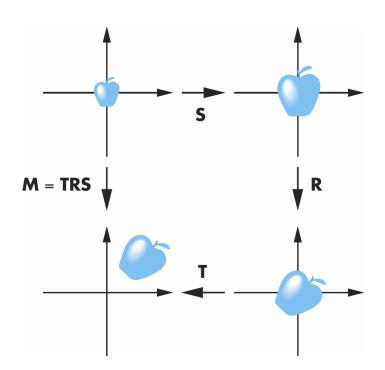
- Binding the vertex array handles the binding of index buffers as well.
- Render N×3 indices instead of N×3 vertices in the simple vertex buffering.
- Use glDrawElements() instead of glDrawArrays() to use the index buffering.

```
void render()
{
    ...
    glBindVertexArray( vertex_array );
    ...
    glDrawElements( GL_TRIANGLES, NUM_TESS*3, GL_UNSIGNED_INT, nullptr );
    ...
}
```

# **Instancing**

## **Instancing**

- In modeling, we often start with an object centered at the origin, oriented with the axis, and at a standard size.
  - We apply an *instance transformation* to its vertices to scale, orient, and locate somewhere.
  - This allows us to work with minimal geometric objects, while rendering many different objects.



## **Instancing**

- To realize the concept of instancing, we use a unit vertex buffer:
  - We create a single vertex buffer, which is unit-sized and located at the origin.
  - In render(), we use a loop to render multiple objects.
  - In the loop, we change the size and position for each circle, and pass them to their uniform variables residing in (vertex or fragment) shaders.
- Refer to the circle example in the following pages.

### First, define the structure of objects.

- Here, we define a circle structure.
- The attributes include the center position, radius, rotation angle, color, and modeling matrix.
- We also define an update() function for per-circle updates.

```
// in circle.h

struct circle_t
{
   vec2 center=vec2(0);  // 2D position for translation
   float radius=1.0f;  // radius
   float theta=0.0f;  // rotation angle
   vec4 color;  // RGBA color in [0,1]
   mat4 model_matrix;  // modeling transformation

   // public functions
   void update( float t );
};
```

- create\_circles() instantiates many circles.
  - Here, two circle objects are instantiated.

```
std::vector<circle_t> create_circles()
{
    std::vector<circle_t> circles;
    circle_t c;

    c = {vec2(-0.5f,0),1.0f,0.0f,vec4(1.0f,0.5f,0.5f,1.0f)};
    circles.emplace_back(c);

    c = {vec2(+0.5f,0),1.0f,0.0f,vec4(0.5f,1.0f,1.0f,1.0f)};
    circles.emplace_back(c);

    return circles;
}
```

### circle\_t::update() builds a transformation matrix.

- radius and theta are user-defined parameters for animation.
- The parameters are used to build a 2D transformation matrix.
- The details will be explained later in the transformation lecture.

### In render(), update per-circle parameters and matrices.

- Here, we change the color and matrix for each circle.
- Then, we call glDrawElements for each circle, repeatedly.
- Your shader draws them differently, based on the different uniforms.

```
void render(){
  for( auto& c : circles )
      c.update(t); // per-circle update
      // update per-circle uniforms
     GLint uloc;
      uloc = glGetUniformLocation( program, "solid_color" );
      glUniform4fv( uloc, 1, c.color ); // pointer version
      uloc = glGetUniformLocation( program, "model_matrix" );
      glUniformMatrix4fv( uloc, 1, GL_TRUE, c.model_matrix );
      // per-circle draw calls
      glDrawElements( GL_TRIANGLES, NUM_TESS*3, GL_UNSIGNED_INT, nullptr );
```

## **Vertex and Fragment Shaders**

### Your vertex shader

- In the vertex shader, we locate the vertices based on its transformation and attributes.
  - Here, we apply scaling, rotation, and translation in a row.
  - We first scale the vertex with the circle radius, and rotate it.
  - Then, we add its offset, which is the center of the circle.

```
// uniform variables
uniform mat4  model_matrix;  // 4x4 transformation matrix
uniform mat4  aspect_matrix;  // tricky 4x4 aspect-correction matrix

void main()
{
   gl_Position = aspect_matrix * model_matrix * vec4(position,1);
   ...
}
```

### Your vertex shader

### One last stuff to do is the correction of the aspect ratio.

- Since we specify the vertex position in the default viewing volume, the resulting shape in the horizontally/vertically wider screen will be distorted.
- To handle this, using matrix is consistent in vertex shader.

## Your fragment shader

### Nearly the same as the hello example.

Additionally, we visualize texture coordinates as color output.

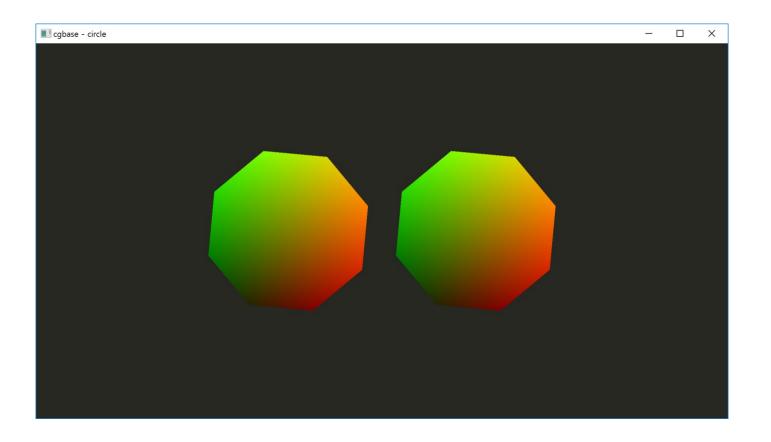
```
// inputs from vertex shader
in vec2 tc; // used for texture coordinate visualization
...

void main()
{
   fragColor = b_solid_color ? solid_color : vec4(tc.xy,0,1);
}
```

### **Results**

### Octagonal approximation

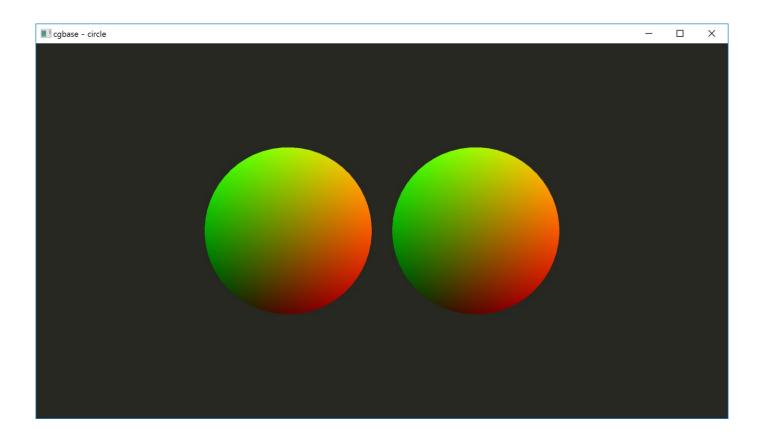
Color indicates the texture coordinates.



### **Results**

### • 64-gon approximation

Now, they looks almost like circles.



### **Results**

- Wireframe-mode rendering (not supported in OpenGL ES)
  - Now, you can see the triangular structure.

