CORE Skills

Delivering Data Science
In Resources & Energy

Data Analysis II: Simple Predictions - Regression and statistical model building

DAY 5

15-Day Data Science Springboard

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Data Mettle

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Data Mettle

Program partners

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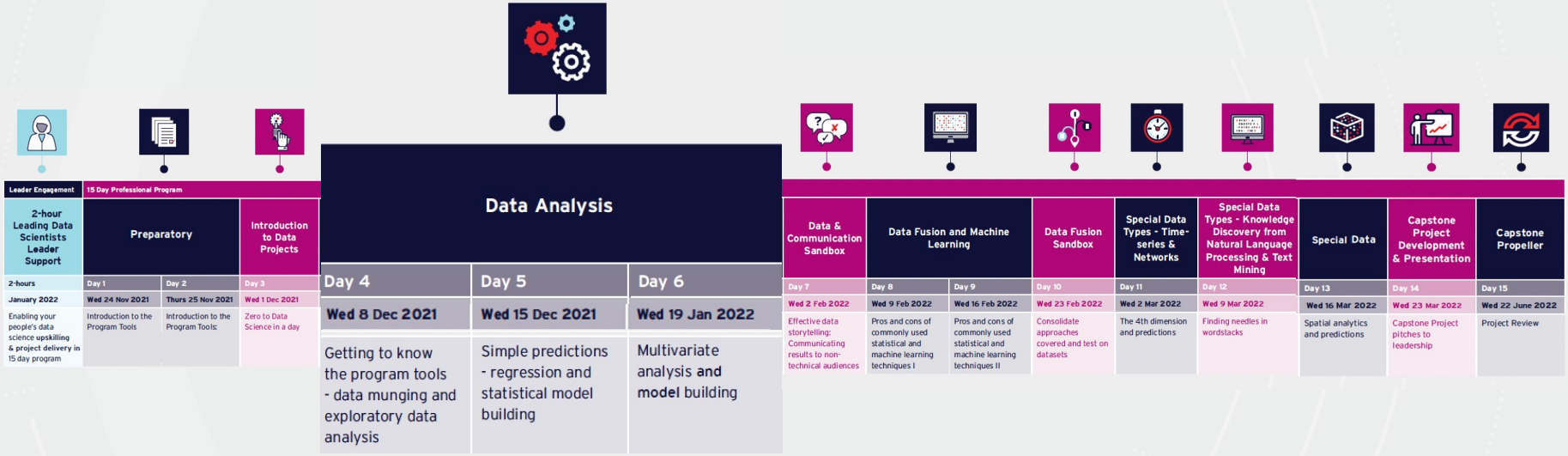
The University of Western Australia

Curtin University

A CORE partnership

Program Timeline

DAY 4, 5 & 6: Data Analysis



Q&A, Issues & Announcements

Before we Get Started

- Resources & Tasks on Github.

- We'll start talking about **projects** a bit this afternoon, and help you start setting up yours

- Make notes about any ideas, perspectives or issues you encounter throughout the day.
- If you have aspects you'd like to go over throughout the day, feel free to post them to the general channel and we'll try to address the straightforward ones as we break.
- We'll come together to discuss before we close out this afternoon.

Schedule

DAY 5

AWST	AEST	Agenda	Educator
07:30	**09:30**	**Q&A, Issues & Announcements**	
07:45	09:45	**Models & Regression**	Jeremy
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17:00	17:00	**Close**	

Aims & Learning Outcomes

DAY 5

Aims

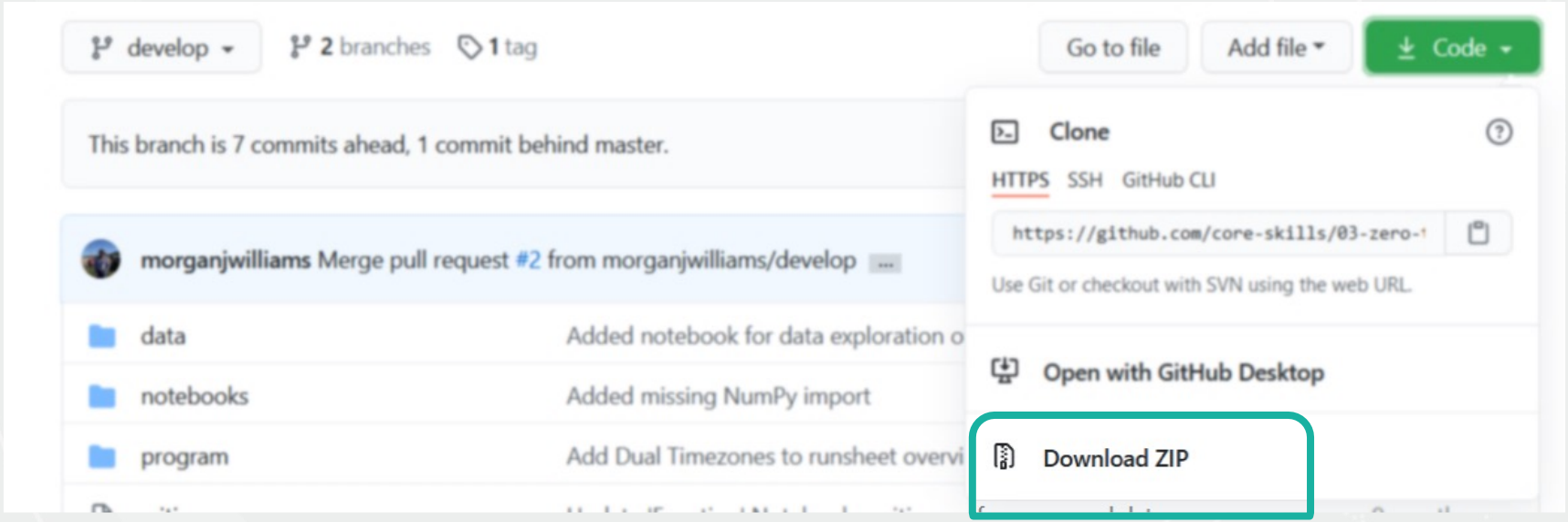
- Perform statistical model building.
- Conduct regression.
- Generate simple predictions - regression.

Learning Outcomes

- Understand regression as the basis for prediction.
- Understand how outliers and noisy data affect results.
- Understand the impact of missing data and recall practical solutions to work with incomplete data sets.
- Understand how to choose between basic statistical models and evaluate their effectiveness (e.g. linear vs polynomial).
- Have an understanding of hierarchical models as a means of modelling connections between datasets or processes.

GitHub Content for Today

[github.com / core-skills / 05-simple-predictions]



GitHub – Program Notes

[github.com / core-skills / 05-simple-predictions / program / 00_overview.md]

Overview

Overview | Data Culture | From Here to There | Data Projects | Data Exploration | Closeout

Aim

Provide an overview of a 'typical' data science workflow.

Learning Outcomes

1. To appreciate what data science is
2. To appreciate the fields data science spans
3. Understand the stages of a data science project and define a mental model of it
4. Analyse the opportunity and potential value of data science in your organisation

Schedule

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07:30 - 07:45	09:30 - 09:45	Q&A, Issues & Announcements
07:45 - 09:15	09:45 - 11:15	**Creating a Data Culture**
09:15 - 09:30	11:15 - 11:30	*Morning Tea*
09:30 - 11:00	11:30 - 13:00	**Getting From Here to There**

Environment

- Open an Anaconda Prompt
- Navigate to where you have the unzipped repository material

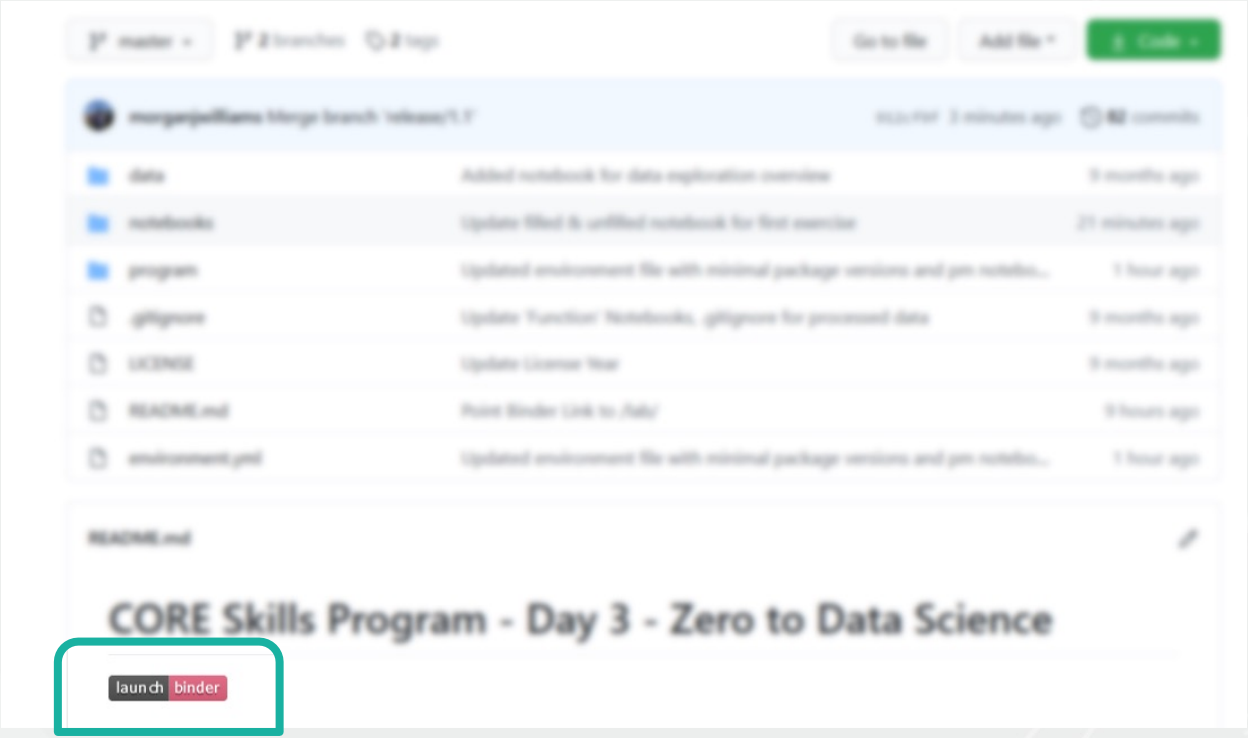
```
conda env create -f environment.yml # make new env

conda activate core05 # activate this env (Windows)

# make this available to Jupyter as a "kernel"
python -m ipykernel install --user --name=core05

jupyter lab # launch Jupyter lab
```

Binder Backup



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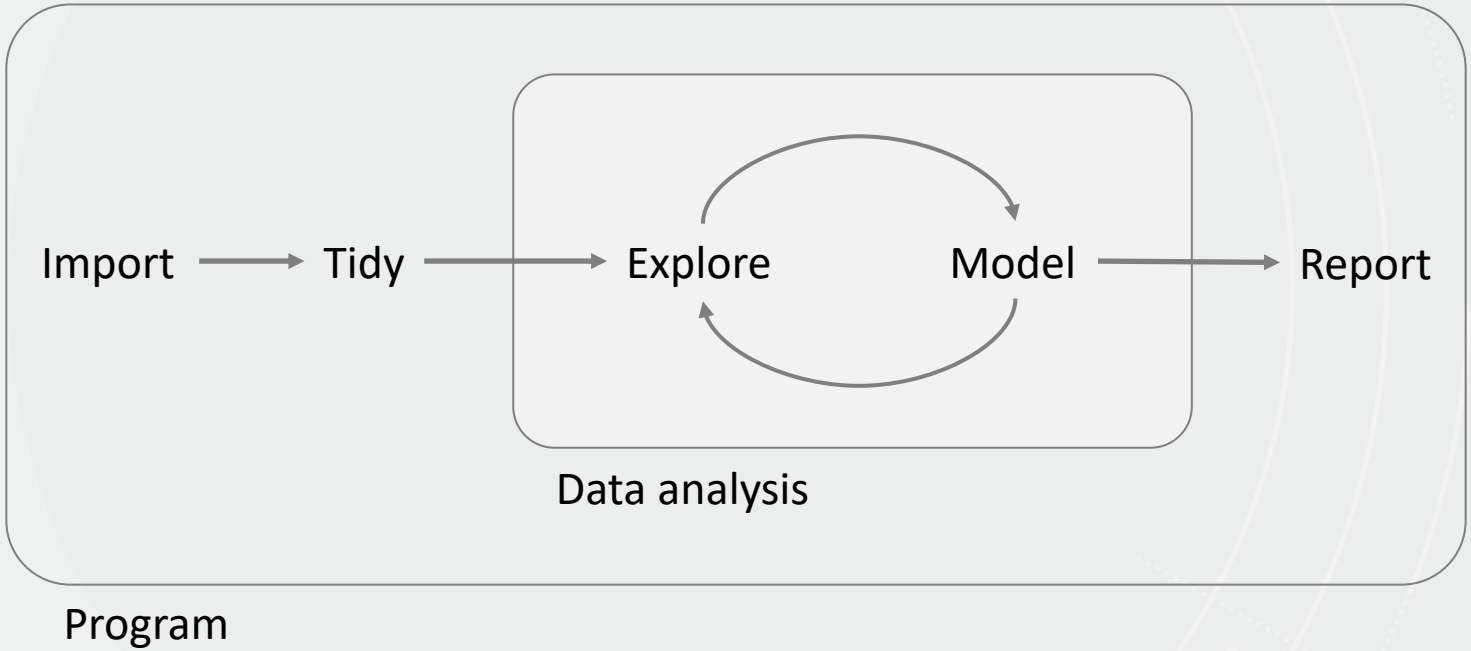
Models & Regression

What are the main steps of the data analysis workflow?

5 min

Short introduction to data analytics and machine learning



Exercise: Explore a dataset using pandas and seaborn

Open **am1-models-and-regression.ipynb**

and go through exercise 1

Categories of machine learning

scikit-learn.org/stable/tutorial/machine_learning_map/index.html

Scikit-learn basics and API

- Dataset in tidy format

- Basic API:
  - model = LinearRegression()
  - model.fit(x_train, y_train)
  - y_pred = model.predict(x_pred)

Linear Regression Model

- The linear regression model is one of the most basic statistical models used in predictive analysis
- The model proceeds by fitting a linear equation to observed paired data to attempt to model the relationship between the two variables
- One variable is commonly referred as to the explanatory variable while the other is considered the dependent variable

Linear Regression Model

- The equation of a line is

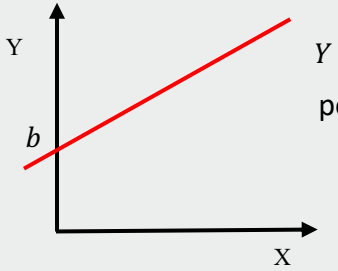
$$Y = aX + b$$

Dependent variable

Explanatory variable

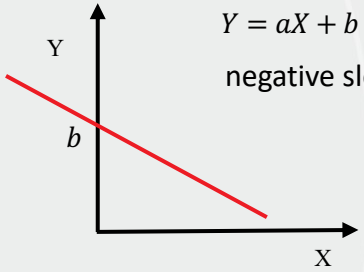
- a corresponds to the slope of the line and b to the intercept
- Parameters a and b need to be determined
- Different mathematical approaches can be used to determine the slope and the intercept. This leads to different types of regression

Linear Regression Model



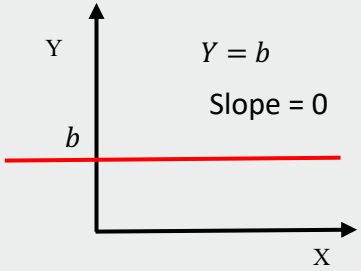
$Y = aX + b$

positive slope



$Y = aX + b$

negative slope

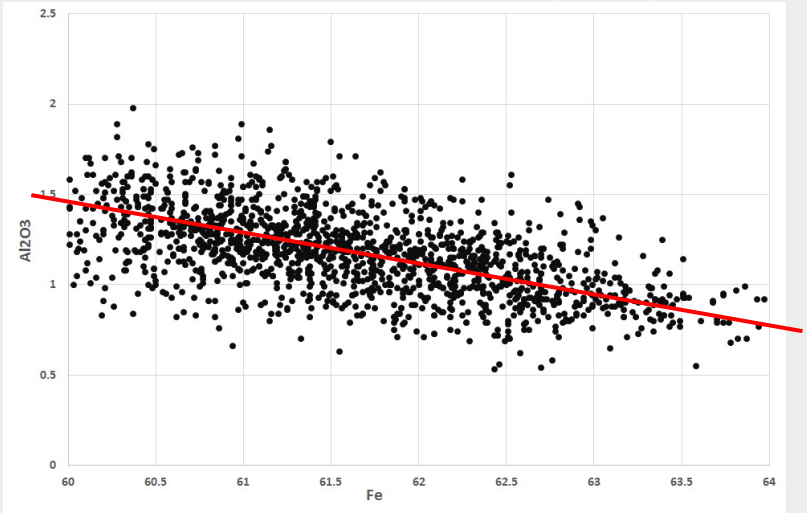


$Y = b$

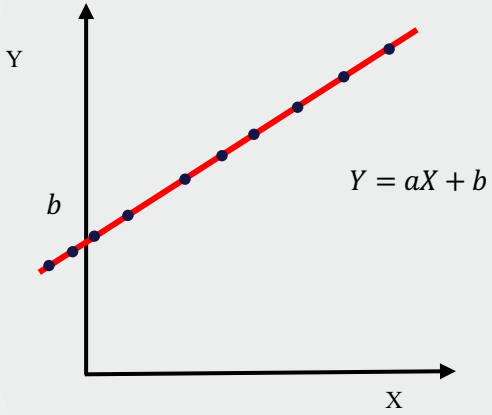
Slope = 0

Linear Regression Model

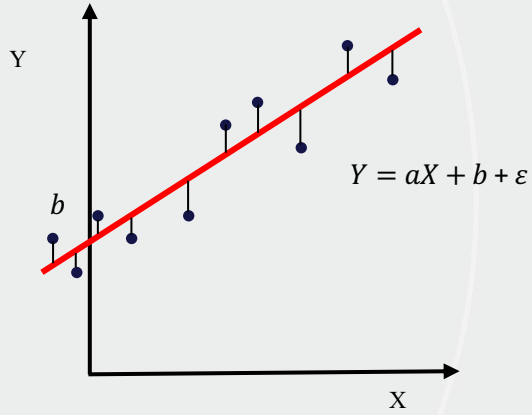
- Why do we want to fit a line?
- The scatterplot shows the paired data is scattered around a trend line
- The line is indicative of the average value of the dependent variable given the explanatory variable



Linear Regression Model



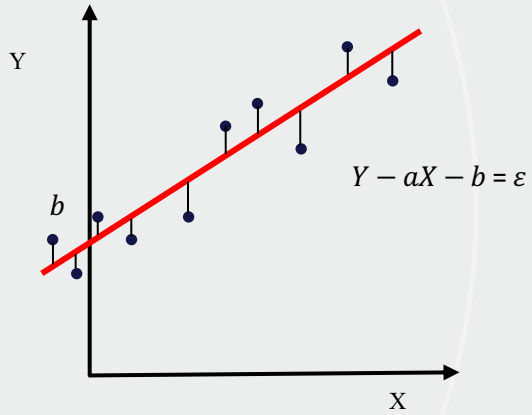
Values of X and Y are perfectly related



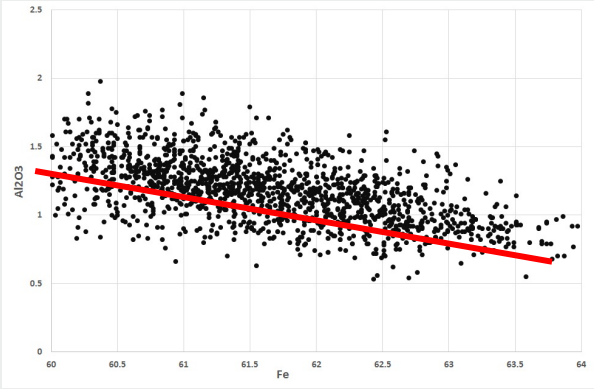
Values of X are known and it is assumed that $Y = aX + b$ plus a random term ε

Statistical assumptions

- A number of assumptions are made on the random error term ε
- First assumption is that on average the error is equal to zero
- This ensures the model has no bias

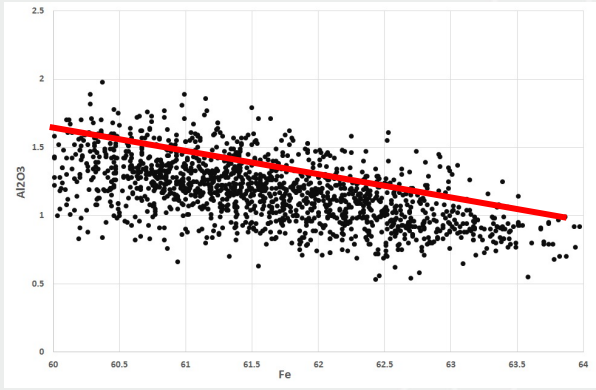


Statistical assumptions



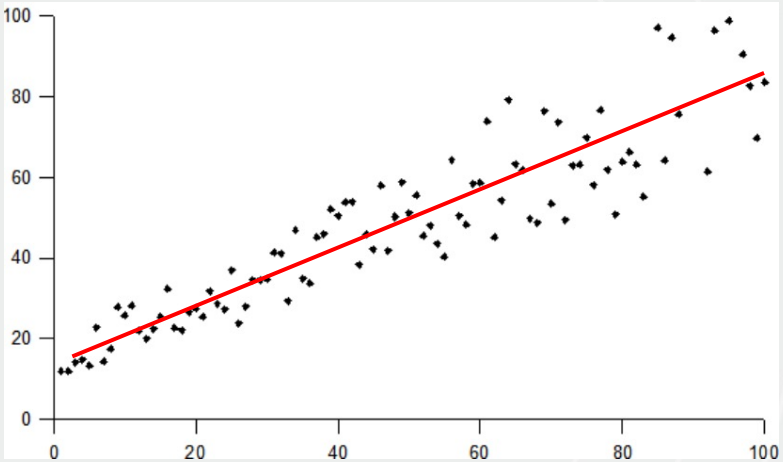
Positive bias

Negative bias



Statistical assumptions

- Second assumption is that the variance of the random error term is constant
- This is know in statistics as homoscedasticity asummption
- Heteroscedasticity refers to the violation of this assumption

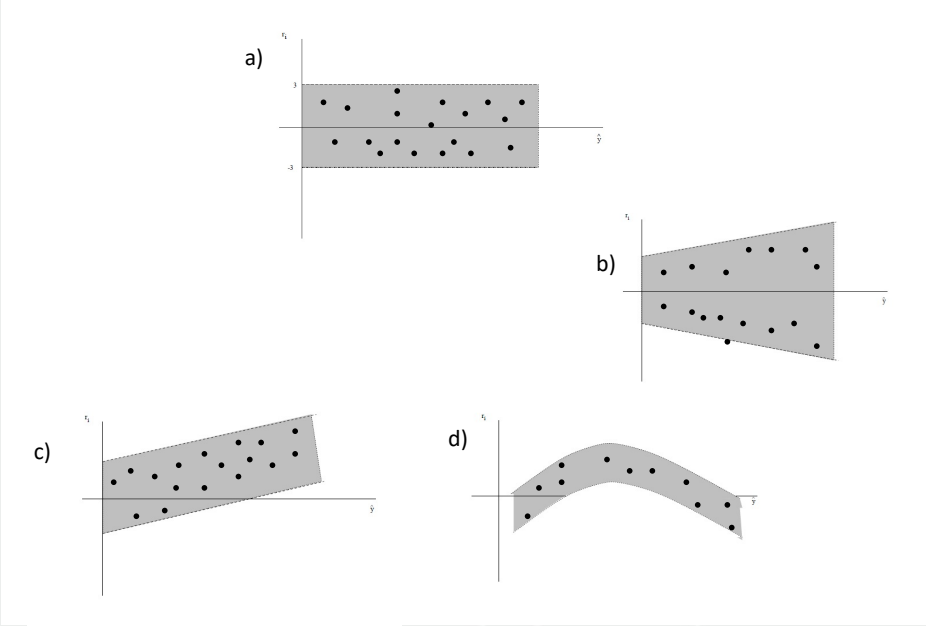


Statistical assumptions

- Third assumption is that random error term is independent of both the explanatory and dependent variable
- Extremely important assumption and provides a way to assess the goodness of the linear model
- Scatterplot of the error with either the explanatory or the dependent variable should not show any clear pattern

Statistical assumptions

- a) Appropriate
- b) homoscedasticity violated
- c) and d) are indicative that the linear regression model is not adequate



Statistical assumptions

- Fourth assumption corresponds to the statistical distribution of the error component
- It is assumed that the distribution of the random error is Gaussian with mean equal to zero and variance σ^2

$$\varepsilon \sim N(0, \sigma^2)$$

- The Gaussian assumption allows to derive all the theoretical properties of the linear regression model

Statistical assumptions

Some of the theoretical properties are:

- The dependent variable has Gaussian distribution

  This allows to construct confidence intervals for the estimated values

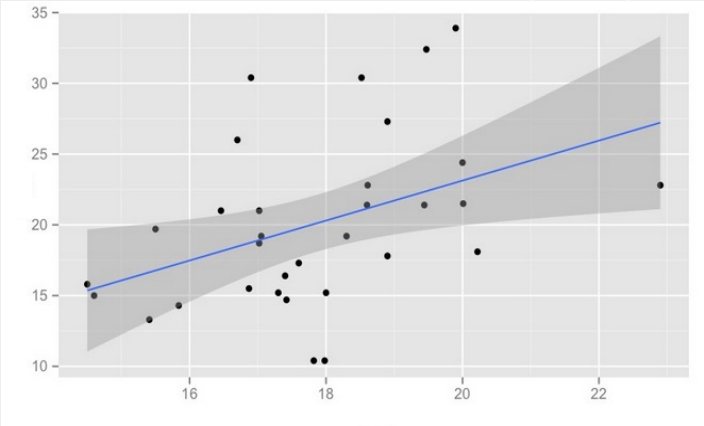
- The slope a has Gaussian distribution

  This allows to use statistical tests to assess the "importance" of the explanatory variable

Statistical tests on the parameters are more important in multivariate problems

Statistical assumptions

- Example of a linear regression model with confidence intervals
- Can you anticipate the behaviour of the residuals?
- Would you say the linear model is reasonable?



Exercise: Linear regression with scikit-learn

Return to **am1-models-and-regression.ipynb**

and go through exercise 2

Exercise: Perturbing perfect linear data

Return to **am1-models-and-regression.ipynb**

and go through exercise 3

A look at R^2

- R^2 is also known as coefficient of determination
- R^2 is used as a goodness of fit measure for linear regression models, i.e. to determine how well the regression model fits the data

$$R^2 = 1 - \frac{\sum \varepsilon_i^2}{\sum (y_i - \bar{y})^2}$$

- Proportion of the variance in the dependent variable that the explanatory variable explains

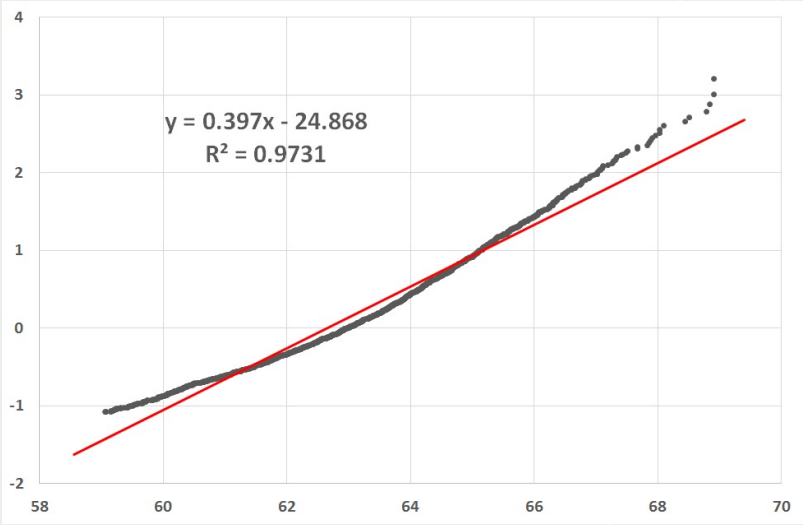
A look at R^2

- R^2 has limitations and therefore should not be the only criteria used to assess the goodness of the linear regression model

- Some of its limitations are:
  - Does not account for the number of paired data used
  - Does not indicate if the explanatory variable used is appropriate
  - Does not indicate if the regression used is appropriate
  - Does not indicate if the model is biased

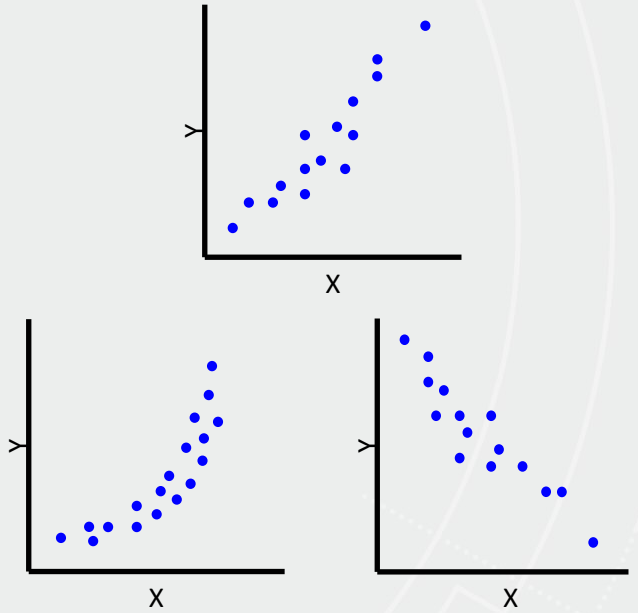
A look at R^2

A biased model can have a high R^2 value!



Correlation and Independence

- Traditional correlation is a measure of the linear relationship between two variables
- A correlation value equal to zero does not mean the variables are not related



Correlation and Independence

- The concept of statistical independence is given by the factorisation of the joint probability distribution as the product of the marginal distributions
- This means that knowing the value of one of the variables does not tell anything about the value of the other variable
- Independence implies no correlation but the reverse is not true

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Apply to your own Problem

If you don’t have a dataset

- UCI Machine Learning Repository:
  archive.ics.uci.edu/ml/index.php
- Kaggle datasets:
  www.kaggle.com/datasets

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Takeaways & Closeout

High-level Takeaways From Today

- Understand regression as the basis for prediction.
- Understand how outliers and noisy data affect results.
- Understand the impact of missing data and recall practical solutions to work with incomplete data sets.
- Understand how to choose between basic statistical models and evaluate their effectiveness (e.g. linear vs polynomial).
- Have an understanding of hierarchical models as a means of modelling connections between datasets or processes.

High-level Takeaways From Today

Your thoughts?

Capstone Projects

Capstone Projects

Update

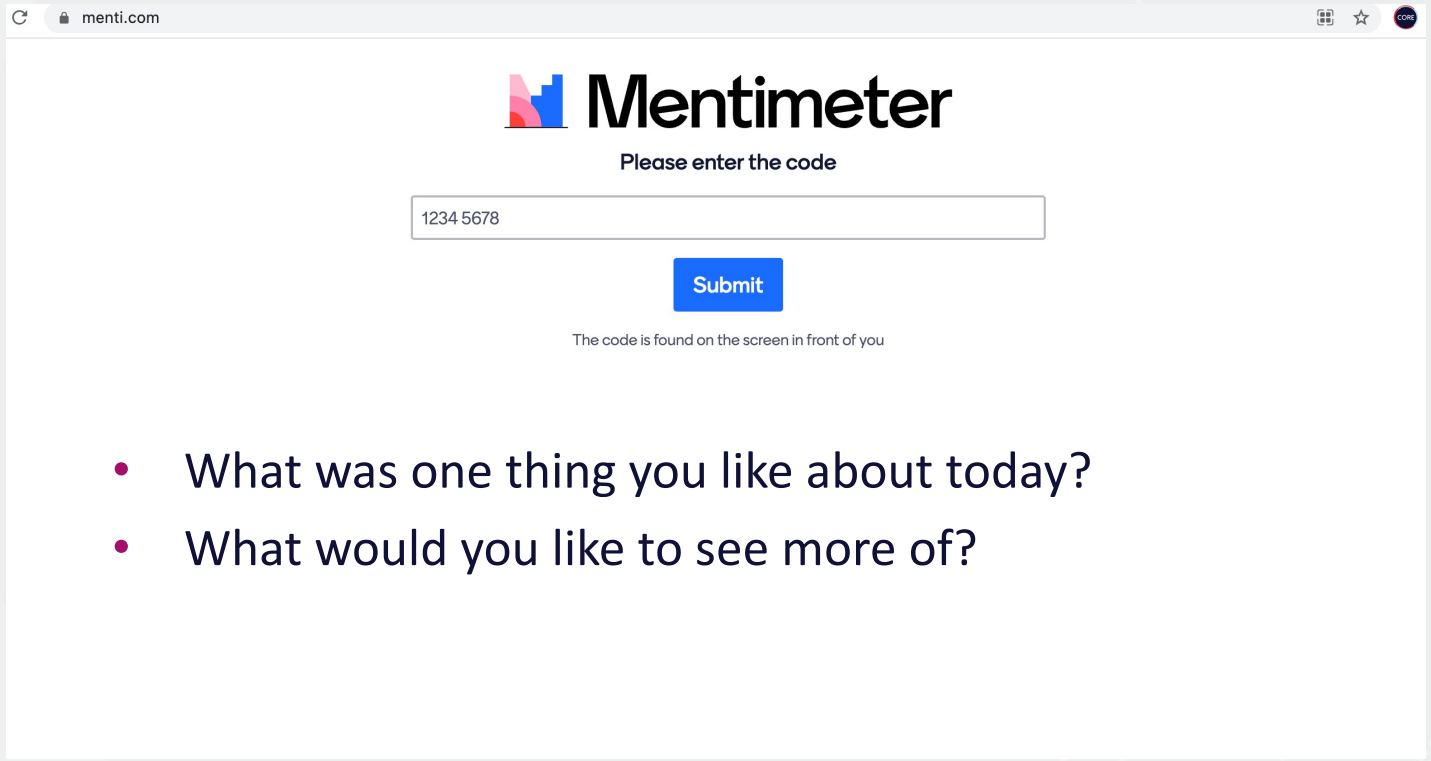
- How you are shaping up your Project

Action

- Milestone #1 → L0 in Momentum
- If not done already, update your Working Project Title & Short Project Statement (Problem/Solution/Plan) here.
- Update your Leader

Daily Feedback

Menti



- What was one thing you like about today?
- What would you like to see more of?

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