

Package ‘drimmR’

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Type Package

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Description This package introduces the drifting Markov models (DMMs) which are non-homogeneous Markov models designed for modeling the heterogeneities of sequences in a more flexible way than homogeneous Markov chains or even hidden Markov models. In this context, we developed an R package dedicated to the estimation, simulation and the exact computation of associated reliability of drifting Markov models. The implemented methods are described in Vergne, N. (2008), <doi:10.2202/1544-6115.1326> and Barbu, V.S., Vergne, N. (2019) <doi:10.1007/s11009-018-9682-8> .

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Biostrings,
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```

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drimmR-package

drimmR-package

Description

This package performs the estimation, simulation and the exact computation of associated reliability measures of drifting Markov models (DMMs). These are particular non-homogeneous Markov chains for which the Markov transition matrix is a linear (polynomial) function of two (several) Markov transition matrices. Several statistical frameworks are taken into account (one or several samples, complete or incomplete samples, models of the same length). Computation of probabilities of appearance of a word along a sequence under a given model are also considered.

aic	<i>Akaike Information Criterion (AIC)</i>
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Description

Generic function computing the Akaike Information Criterion of the model x, with the list of sequences sequences.

Usage

```
aic(x, sequences)
```

Arguments

x	An object for which the log-likelihood of the DMM can be computed.
sequences	A vector of characters or a list of vector of characters representing the sequences for which the AIC will be computed based on x.

Value

A list of AIC (numeric)

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

aic.dmm	<i>Evaluate the AIC of a drifting Markov Model</i>
---------	--

Description

Computation of the Akaike Information Criterion.

Usage

```
## S3 method for class 'dmm'
aic(x, sequences)
```

Arguments

x	An object of class dmm
sequences	A character vector or a list of character vector representing the sequences for which the AIC will be computed based on x.

Value

A list of AIC (numeric)

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [loglik](#), [aic](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
sequence <- c("a","g","g","t","c","g","a","t","a","a","a")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
aic(dmm,sequence)

## End(Not run)
```

availability

Availability function

Description

The pointwise (or instantaneous) availability of a system S_{system} at time $k \in N$ is the probability that the system is operational at time k (independently of the fact that the system has failed or not in $[0; k)$).

Usage

```
availability(x, k1 = 0L, k2, upstates, output_file = NULL, plot = FALSE)
```

Arguments

x	An object of class dmm
k1	Start position (default value=0): a positive integer giving the start position along the sequence from which the availabilities of the DMM should be computed, such that $k1 < k2$
k2	End position : a positive integer giving the end position along the sequence until which the availabilities of the DMM should be computed, such that $k2 > k1$
upstates	Character vector giving the subset of operational states U.
output_file	(Optional) A file containing matrix of availability probabilities (e.g. "C:/.../AVAL.txt")
plot	FALSE (default); TRUE (display a figure plot of availability probabilities by position)

Details

Consider a system (or a component) System whose possible states during its evolution in time are $E = \{1 \dots s\}$. Denote by $U = \{1 \dots s_1\}$ the subset of operational states of the system (the upstates) and by $D = \{s_1 + 1 \dots s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset, U \neq \emptyset, D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

Value

A vector of length $k+1$ giving the values of the availability for the period $[0 \dots k]$

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [reliability](#), [maintainability](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq",
  fit.method="sum", plot=TRUE)
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
getA <- availability(dmm,k1,k2,upstates,plot=TRUE)

## End(Not run)
```

bic	<i>Bayesian Information Criterion (BIC)</i>
-----	---

Description

Generic function computing the Bayesian Information Criterion of the model x, with the list of sequences sequences.

Usage

```
bic(x, sequences)
```

Arguments

x	An object for which the log-likelihood of the DMM can be computed.
sequences	A list of vectors representing the sequences for which the BIC will be computed based on x.

Value

A list of BIC (numeric)

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

bic.dmm	<i>Evaluate the BIC of a drifting Markov Model</i>
---------	--

Description

Computation of the Bayesian Information Criterion.

Usage

```
## S3 method for class 'dmm'
bic(x, sequences)
```

Arguments

x	An object of class dmm
sequences	A character vector or a list of character vector representing the sequences for which the BIC will be computed based on x.

Value

A list of BIC (numeric).

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [loglik](#), [bic](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
sequence <- c("a","g","g","t","c","g","a","t","a","a","a")
dmm<- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
bic(dmm,sequence)

## End(Not run)
```

distributions

Distributions for a range of positions between <start> and <end>

Description

Distributions for a range of positions between <start> and <end>

Usage

```
distributions(
  x,
  start = 1,
  end = NULL,
  step = NULL,
  output_file = NULL,
  plot = FALSE
)
```

Arguments

x	An object of class dmm
start	Start position : a positive integer giving the start position along the sequence from which the distributions of the DMM should be computed
end	End position : a positive integer giving the end position along the sequence until which the distributions of the DMM should be computed
step	A step (integer)
output_file	(Optional) A file containing matrix of distributions (e.g, "C:/.../DIST.txt")
plot	FALSE (default); TRUE (display a figure plot of distribution probabilities by position)

Value

A matrix with positions and distributions of states

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getDistribution](#), [getStationaryLaw](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
distributions(dmm,start=1,end=1000,step=100, plot=TRUE)

## End(Not run)
```

failureRate	<i>Failure rates function</i>
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Description

Computation of two different definition of the failure rate : the BMP-failure rate and RG-failure rate.

As for BMP-failure rate, consider a system S starting to work at time $k = 0$. The BMP-failure rate at time $k \in N$ is the conditional probability that the failure of the system occurs at time k , given that the system has worked until time $k - 1$. The BMP-failure rate denoted by $\lambda(k)$, $k \in N$ is usually considered for continuous time systems.

The RG-failure rate is a discrete-time adapted failure-rate proposed by D. Roy and R. Gupta. Classification of discrete lives. *Microelectronics Reliability*, 32(10):1459–1473, 1992. The RG-failure rate is denoted by $r(k)$, $k \in N$.

Usage

```
failureRate(
  x,
  k1 = 0L,
  k2,
  upstates,
  failure.rate = c("BMP", "RG"),
  output_file = NULL,
  plot = FALSE
)
```

Arguments

<code>x</code>	An object of class <code>dmm</code>
<code>k1</code>	Start position (default value=0) : a positive integer giving the start position along the sequence from which the failure rates of the DMM should be computed, such that $k1 < k2$
<code>k2</code>	End position : a positive integer giving the end position along the sequence until which the failure rates of the DMM should be computed, such that $k2 > k1$
<code>upstates</code>	Character vector of the subspace working states among the state space vector such that $upstates < s$
<code>failure.rate</code>	Default="BMP", then BMP-failure-rate is the method used to compute the failure rate. If <code>failure.rate="RG"</code> , then RG-failure rate is the method used to compute the failure rate.
<code>output_file</code>	(Optional) A file containing matrix of failure rates at each position (e.g, "C:/.../ER.txt")
<code>plot</code>	FALSE (default); TRUE (display a figure plot of failure rates by position)

Details

Consider a system (or a component) System whose possible states during its evolution in time are $E = \{1 \dots s\}$. Denote by $U = \{1 \dots s_1\}$ the subset of operational states of the system (the upstates) and by $D = \{s_1 + 1 \dots s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset$, $U \neq \emptyset$, $D \neq \emptyset$). One can think of the states of U as

different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

Value

A vector of length $k + 1$ giving the values of the BMP (or RG) -failure rate for the period $[0 \dots k]$

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Roy D, Gupta R (1992). “Classification of discrete lives. Microelectronics Reliability.” *Microelectronics Reliability*, 1459–1473. doi: [10.1016/00262714\(92\)90015D](https://doi.org/10.1016/00262714(92)90015D), [https://doi.org/10.1016/0026-2714\(92\)90015-D](https://doi.org/10.1016/0026-2714(92)90015-D).

See Also

[fitdmm](#), [getTransitionMatrix](#), [reliability](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq",
  fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
failureRate(dmm,k1,k2,upstates,failure.rate="BMP",plot=TRUE)

## End(Not run)
```

fitdmm

Point by point estimates of a k-th order drifting Markov Model

Description

Estimation of $d+1$ points of support transition matrices and $|E|^k$ initial law of a k -th order drifting Markov Model starting from one or several sequences.

Usage

```
fitdmm(
  sequences,
  order,
  degree,
  states,
  init.estim = c("mle", "freq", "prod", "stationary", "unif"),
  fit.method = c("sum")
)
```

Arguments

sequences	A list of character vector(s) representing one (several) sequence(s)
order	Order of the Markov chain
degree	Degree of the polynomials (e.g., linear drifting if degree=1, etc.)
states	Vector of states space of length $s > 1$
init.estim	Default="mle". Method used to estimate the initial law. If <code>init.estim = "mle"</code> , then the classical Maximum Likelihood Estimator is used, if <code>init.estim = "freq"</code> , then, the initial distribution <code>init.estim</code> is estimated by taking the frequencies of the words of length k for all sequences. If <code>init.estim = "prod"</code> , then, <code>init.estim</code> is estimated by using the product of the frequencies of each letter (for all the sequences) in the word of length k . If <code>init.estim = "stationary"</code> , then <code>init.estim</code> is estimated by using the stationary law of the point of support transition matrices of each letter. If <code>init.estim = "unif"</code> , then, <code>init.estim</code> of each letter is estimated by using $\frac{1}{s}$. Or 'init.estim' = customisable vector of length $ E ^k$. See Details for the formulas.
fit.method	If sequences is a list of several character vectors of the same length, the usual LSE over the sample paths is proposed when <code>fit.method="sum"</code> (a list of a single character vector is its special case).

Details

The `fitdmm` function creates a drifting Markov model object `dmm`.

Let $E = 1, \dots, s$, $s < \infty$ be random system with finite state space, with a time evolution governed by discrete-time stochastic process of values in E . A sequence X_0, X_1, \dots, X_n with state space $E = 1, 2, \dots, s$ is said to be a linear drifting Markov chain (of order 1) of length n between the Markov transition matrices Π_0 and Π_1 if the distribution of X_t , $t = 1, \dots, n$, is defined by $P(X_t = v \mid X_{t-1} = u, X_{t-2}, \dots) = \Pi_{\frac{t}{n}}(u, v)$, $u, v \in E$, where $\Pi_{\frac{t}{n}}(u, v) = (1 - \frac{t}{n})\Pi_0(u, v) + \frac{t}{n}\Pi_1(u, v)$, $u, v \in E$. The linear drifting Markov model of order 1 can be generalized to polynomial drifting Markov model of order k and degree d . Let $\Pi_{\frac{i}{d}} = (\Pi_{\frac{i}{d}}(u_1, \dots, u_k, v))_{u_1, \dots, u_k, v \in E}$ be d Markov transition matrices (of order k) over a state space E .

The estimation of DMMs is carried out for 4 different types of data :

One can observe one sample path : It is denoted by $H(m, n) := (X_0, X_1, \dots, X_m)$, where m denotes the length of the sample path and n the length of the drifting Markov chain. Two cases can be considered:

1. $m=n$ (a complete sample path),
2. $m < n$ (an incomplete sample path).

One can also observe H i.i.d. sample paths : It is denoted by $H_i(m_i, n_i)$, $i = 1, \dots, H$. Two cases cases are considered :

1. $m_i = n_i = n \forall i = 1, \dots, H$ (complete sample paths of drifting Markov chains of the same length),
2. $n_i = n \forall i = 1, \dots, H$ (incomplete sample paths of drifting Markov chains of the same length). In this case, an usual LSE over the sample paths is used.

The initial distribution of a k -th order drifting Markov Model is defined as $\mu_i = P(X_1 = i)$. The initial distribution of the k first letters is freely customisable by the user, but five methods are proposed for the estimation of the latter :

Estimation based on the Maximum Likelihood Estimator: The Maximum Likelihood Estimator for the initial distribution. The formula is: $\hat{\mu}_i = \frac{N_{start_i}}{L}$, where N_{start_i} is the number of occurrences of the word i (of length k) at the beginning of each sequence and L is the number of sequences. This estimator is reliable when the number of sequences L is high.

Estimation based on the frequency: The initial distribution is estimated by taking the frequencies of the words of length k for all sequences. The formula is $\hat{\mu}_i = \frac{N_i}{N}$, where N_i is the number of occurrences of the word i (of length k) in the sequences and N is the sum of the lengths of the sequences.

Estimation based on the product of the frequencies of each state: The initial distribution is estimated by using the product of the frequencies of each state (for all the sequences) in the word of length k .

Estimation based on the stationary law of point of support transition matrix for a word of length k :
The initial distribution is estimated using $\mu(\Pi_{\frac{k-1}{n}})$

Estimation based on the uniform law : $\frac{1}{s}$

Value

An object of class dmm

Author(s)

Geoffray Brelurut, Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

Examples

```
## Not run:
data(lambda, package = "drimmR")
states <- c("a", "c", "g", "t")
order <- 1
degree <- 1
fitdmm(lambda, order, degree, states, init.estim = "freq", fit.method = "sum")

## End(Not run)
```

getDistribution

Distributions of the drifting Markov Model

Description

Generic function evaluating the distribution of a model x at a given position pos or at every position $all.pos$

Usage

```
getDistribution(x, pos, all.pos = FALSE, internal = FALSE)
```

Arguments

x	An object for which the distributions of the DMM can be computed.
pos	A positive integer giving the position along the sequence on which the distribution of the DMM should be computed
all.pos	'FALSE' (evaluation at position index) ; 'TRUE' (evaluation for all position indices)
internal	'FALSE' (default) ; 'TRUE' (for internal use of the distributions function)

Details

Distribution at position l is evaluated by $\mu_l = \mu_0 \prod_{t=k}^l \pi_{\frac{t}{n}}, \forall l \geq k, k \in N^*$ order of the DMM

Value

A vector or matrix of distribution probabilities

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

getDistribution.dmm	<i>Get the distributions of the DMM</i>
---------------------	---

Description

Evaluate the distribution of the DMM at a given position or at every position

Usage

```
## S3 method for class 'dmm'
getDistribution(x, pos, all.pos = FALSE, internal = FALSE)
```

Arguments

x	An object of class dmm
pos	A positive integer giving the position along the sequence on which the distribution of the DMM should be computed
all.pos	'FALSE' (default, evaluation at position index) ; 'TRUE' (evaluation for all position indices)
internal	'FALSE' (default) ; 'TRUE' (for internal use of distributions function)

Details

Distribution at position l is evaluated by $\mu_l = \mu_0 \prod_{t=k}^l \pi_{\frac{t}{n}}, \forall l \geq k, k \in N^*$ order of the DMM

Value

A vector or matrix of distribution probabilities

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [distributions](#), [getStationaryLaw](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
t <- 10
getDistribution(dmm,pos=t)

## End(Not run)
```

getStationaryLaw	<i>Stationary laws of the drifting Markov Model</i>
------------------	---

Description

Generic function evaluating the stationary law of a model `x` at a given position `pos` or at every position `all.pos`

Usage

```
getStationaryLaw(x, pos, all.pos = FALSE, internal = FALSE)
```

Arguments

<code>x</code>	An object for which the stationary laws of the DMM can be computed.
<code>pos</code>	A positive integer giving the position along the sequence on which the stationary law of the DMM should be computed
<code>all.pos</code>	'FALSE' (default, evaluation at position index) ; 'TRUE' (evaluation for all position indices)
<code>internal</code>	'FALSE' (default) ; 'TRUE' (for internal use of the initial law computation)

Details

Stationary law at position t is evaluated by solving $\mu_t \pi_{\frac{t}{n}} = \mu$

Value

A vector or matrix of stationary law probabilities

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

getStationaryLaw.dmm *Get the stationary laws of the DMM*

Description

Evaluate the stationary law of the DMM at a given position or at every position

Usage

```
## S3 method for class 'dmm'
getStationaryLaw(x, pos, all.pos = FALSE, internal = FALSE)
```

Arguments

x	An object of class dmm
pos	A positive integer giving the position along the sequence on which the stationary law of the DMM should be computed
all.pos	'FALSE' (default, evaluation at position index) ; 'TRUE' (evaluation for all position indices)
internal	'FALSE' (default) ; 'TRUE' (for internal use of the initial law of fitdmm and word applications)

Details

Stationary law at position t is evaluated by solving $\mu_t \pi_{\frac{t}{n}} = \mu$

Value

A vector or matrix of stationary law probabilities

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [stationary_distributions](#), [getDistribution](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
t <- 10
getStationaryLaw(dmm,pos=t)

## End(Not run)
```

getTransitionMatrix	<i>Transition matrix of the drifting Markov Model</i>
---------------------	---

Description

Generic function evaluating the transition matrix of a model x at a given position pos

Usage

```
getTransitionMatrix(x, pos)
```

Arguments

x	An object for which the transition matrices of the DMM can be computed.
pos	A positive integer giving the position along the sequence on which the transition matrix of the DMM should be computed

Value

A transition matrix at a given position

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

`getTransitionMatrix.dmm`*Get transition matrix of the drifting Markov Model*

Description

Evaluate the transition matrix of the DMM at a given position

Usage

```
## S3 method for class 'dmm'  
getTransitionMatrix(x, pos)
```

Arguments

x	An object of class dmm
pos	A positive integer giving the position along the sequence on which the transition matrix of the DMM should be computed

Value

A transition matrix at a given position

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#)

Examples

```
## Not run:  
data(lambda, package = "drimmR")  
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'),init.estim = "freq", fit.method="sum")  
t <- 10  
getTransitionMatrix(dmm,pos=t)  
  
## End(Not run)
```

lambda

lambda genome

Description

Complete data from phage genome [WT71] of length 48502

Usage

```
data(lambda)
```

Format

A vector object of class "Rdata".

Examples

```
data(lambda)
```

lengthWord_probabilities

Probability of occurrence of the observed word of size m in a sequence at several positions

Description

Probability of occurrence of the observed word of size m in a sequence at several positions

Usage

```
lengthWord_probabilities(m, sequence, pos, x, output_file = NULL, plot = FALSE)
```

Arguments

m	An integer, the length word
sequence	A vector of characters
pos	A vector of integer positions
x	An object of class dmm
output_file	(Optional) A file containing the vector of probabilities (e.g, "C:/.../PROB.txt")
plot	FALSE (default); TRUE (display figure plots of probabilities of occurrence of the observed word of size m by position)

Value

A dataframe of probability by position

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [word_probability](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
m <- 2
lengthWordProbabilities(m, lambda, c(1,length(lambda)-m+1), dmm, plot=TRUE)

## End(Not run)
```

loglik

Log-likelihood of the drifting Markov Model

Description

Generic function computing the log-likelihood of the model x , with the list of sequences `sequences`.

Usage

```
loglik(x, sequences)
```

Arguments

<code>x</code>	An object for which the log-likelihood of the DMM can be computed.
<code>sequences</code>	A vector of character or list of vectors representing the sequences for which the log-likelihood of the model must be computed.

Value

A list of loglikelihood (numeric)

Author(s)

Annthomy Gilles, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

loglik.dmm

Evaluate the log-likelihood of a drifting Markov Model

Description

Evaluate the log-likelihood of a drifting Markov Model

Usage

```
## S3 method for class 'dmm'
loglik(x, sequences)
```

Arguments

x	An object of class dmm
sequences	A character vector or a list of character vectors representing the sequence

Value

A list of log-likelihood (numeric)

Author(s)

Annthomy Gilles, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
sequence <- c("a","g","g","t","c","g","a","t","a","a","a")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
loglik(dmm,sequence)

## End(Not run)
```

maintainability	<i>Maintainability function</i>
-----------------	---------------------------------

Description

Maintainability of a system at time $k \in N$ is the probability that the system is repaired up to time k , given that it has failed at time $k = 0$.

Usage

```
maintainability(x, k1 = 0L, k2, upstates, output_file = NULL, plot = FALSE)
```

Arguments

x	An object of class dmm
k1	Start position (default value=0) : a positive integer giving the start position along the sequence from which the maintainabilities of the DMM should be computed, such that $k1 < k2$
k2	End position : a positive integer giving the end position along the sequence until which the maintainabilities of the DMM should be computed, such that $k2 > k1$
upstates	Character vector of the subspace working states among the state space vector such that $upstates < s$
output_file	(Optional) A file containing matrix of maintainability probabilities (e.g, "C:/.../MAIN.txt")
plot	FALSE (default); TRUE (display a figure plot of maintainability probabilities by position)

Details

Consider a system (or a component) System whose possible states during its evolution in time are $E = \{1 \dots s\}$. Denote by $U = \{1 \dots s_1\}$ the subset of operational states of the system (the upstates) and by $D = \{s_1 + 1 \dots s\}$ the subset of failure states (the down states), with $0 < s_1 < s$ (obviously, $E = U \cup D$ and $U \cap D = \emptyset, U \neq \emptyset, D \neq \emptyset$). One can think of the states of U as different operating modes or performance levels of the system, whereas the states of D can be seen as failures of the systems with different modes.

Value

A vector of length $k + 1$ giving the values of the maintainability for the period $[0 \dots k]$

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>.

See Also

[fitdmm](#), [getTransitionMatrix](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'),
  init.estim = "freq", fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
maintainability(dmm,k1,k2,upstates,plot=TRUE)

## End(Not run)
```

reliability	<i>Reliability function</i>
-------------	-----------------------------

Description

Reliability or the survival function of a system at time $k \in N$

Usage

```
reliability(x, k1 = 0L, k2, upstates, output_file = NULL, plot = FALSE)
```

Arguments

x	An object of class dmm
k1	Start position (default value=0) : a positive integer giving the start position along the sequence from which the reliabilities of the DMM should be computed, such that $k1 < k2$
k2	End position : a positive integer giving the end position along the sequence until which the reliabilities of the DMM should be computed, such that $k2 > k1$
upstates	Character vector of the subspace working states among the state space vector such that $upstates < s$
output_file	(Optional) A file containing matrix of reliability probabilities (e.g, "C:/.../REL.txt")
plot	FALSE (default); TRUE (display a figure plot of reliability probabilities by position)

Details

The reliability at time $k \in N$ is the probability that the system has functioned without failure in the period $[0, k]$

Value

A vector of length $k + 1$ giving the values of the reliability for the period $[0 \dots k]$

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>.

See Also

[fitdmm](#), [getTransitionMatrix](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq",
  fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
reliability(dmm,k1,k2,upstates,plot=TRUE)

## End(Not run)
```

simulate

Simulate a sequence under a drifting Markov model

Description

Generic function simulating a sequence of length `model_size` under a model `x`

Usage

```
simulate(x, output_file, model_size = 1e+05)
```

Arguments

<code>x</code>	An object for which simulated sequences of the DMM can be computed.
<code>output_file</code>	(Optional) File containing the simulated sequence (e.g, "C:/.../SIM.txt")
<code>model_size</code>	Size of the model

Value

the vector of simulated sequence

Author(s)

Annthomy Gilles, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

simulate.dmm

Simulate a sequence under a drifting Markov model

Description

Simulate a sequence under a k-th order DMM.

Usage

```
## S3 method for class 'dmm'
simulate(x, output_file = NULL, model_size = NULL)
```

Arguments

x	An object of class dmm
output_file	(Optional) File containing the simulated sequence (e.g. "C:/.../SIM.txt")
model_size	Size of the model

Value

the vector of simulated sequence

Author(s)

Annthomy Gilles, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [getStationaryLaw](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
simulate(dmm, model_size=100)

## End(Not run)
```

stationary_distributions

Stationary laws for a range of positions between <start> and <end>

Description

Stationary laws for a range of positions between <start> and <end>

Usage

```
stationary_distributions(
  x,
  start = 1,
  end = NULL,
  step = NULL,
  output_file = NULL,
  plot = FALSE
)
```

Arguments

x	An object of class dmm
start	Start position : a positive integer giving the start position along the sequence from which the stationary laws of the DMM should be computed
end	End position : a positive integer giving the end position along the sequence until which the stationary laws of the DMM should be computed
step	A step (integer)
output_file	(Optional) A file containing matrix of stationary laws (e.g, "C:/.../SL.txt")
plot	FALSE (default); TRUE (display a figure plot of stationary distribution probabilities by position)

Value

A matrix with positions and stationary laws of states

Author(s)

Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getStationaryLaw](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
stationary_distributions(dmm, start=1, end=1000, step=100, plot=TRUE)

## End(Not run)
```

words_probabilities	<i>Probability of appearance of several words at several positions of a DMM</i>
---------------------	---

Description

Probability of appearance of several words at several positions of a DMM

Usage

```
words_probabilities(words, pos, x, output_file = NULL, plot = FALSE)
```

Arguments

words	A vector of characters containing words
pos	A vector of integer positions
x	An object of class dmm
output_file	(Optional) A file containing the matrix of probabilities (e.g, "C:/.../PROB.txt")
plot	FALSE (default); TRUE (display figure plots of words' probabilities by position)

Value

A dataframe of word probabilities along the positions of the sequence

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [word_probability](#), [word_probabilities](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq",
  fit.method="sum")
words <- c("atcgattc", "taggct", "ggatcgg")
pos <- c(100,300)
words_probabilities(words=words,pos=pos,dmm,plot=TRUE)

## End(Not run)
```

word_probabilities	<i>Probabilities of a word at several positions of a DMM</i>
--------------------	--

Description

Probabilities of a word at several positions of a DMM

Usage

```
word_probabilities(word, pos, x, output_file = NULL, plot = FALSE)
```

Arguments

word	A subsequence (string of characters)
pos	A vector of integer positions
x	An object of class dmm
output_file	(Optional) A file containing the vector of probabilities (e.g, "C:/.../PROB.txt")
plot	FALSE (default); TRUE (display figure plot of word's probabilities by position)

Value

A numeric vector, probabilities of word

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [word_probability](#), [words_probabilities](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'),
  init.estim = "freq", fit.method="sum")
word_probabilities("aggctga",c(100,300),dmm, plot=TRUE)

## End(Not run)
```

word_probability	<i>Probability of a word at a position t of a DMM</i>
------------------	---

Description

Probability of a word at a position t of a DMM

Usage

```
word_probability(word, pos, x, output_file = NULL, internal = FALSE)
```

Arguments

word	A subsequence (string of characters)
pos	A position (numeric)
x	An object of class dmm
output_file	(Optional) A file containing the probability (e.g,"C:/.../PROB.txt")
internal	FALSE (default) ; TRUE (for internal use of word applications)

Value

A numeric, probability of word

Author(s)

Victor Mataigne, Alexandre Seiller

References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

See Also

[fitdmm](#), [getTransitionMatrix](#), [word_probabilities](#), [words_probabilities](#)

Examples

```
## Not run:
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
word_probability("aggctga",4,dmm)

## End(Not run)
```

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