

# Package ‘drimmR’

February 24, 2021

**Type** Package

**Title** Estimation, Simulation and Reliability of drifting Markov Models

**Version** 1.0.0

**Author** Vlad Stefan Barbu,  
Geoffray Brelurut,  
Annthomy Gilles,  
Arnaud Lefebvre,  
Victor Mataigne,  
Alexandre Seiller,  
Nicolas Vergne

**Maintainer** Nicolas Vergne <Nicolas.Vergne@univ-rouen.fr>

**Description** This package introduces the drifting Markov models (DMMs) which are non-homogeneous Markov models designed for modeling the heterogeneities of sequences in a more flexible way than homogeneous Markov chains or even hidden Markov models. In this context, we developed an R package dedicated to the estimation, simulation and the exact computation of associated reliability of drifting Markov models. The implemented methods are described in Vergne, N. (2008), <doi:10.2202/1544-6115.1326> and Barbu, V.S., Vergne, N. (2019) <doi:10.1007/s11009-018-9682-8> .

**License** GPL

**Encoding** UTF-8

**LazyData** true

**Suggests** utils,  
knitr,  
rmarkdown

**Imports** seqinr,  
Biostrings,  
testthat,  
stats,  
ggplot2,  
parallel,  
foreach,  
future,  
doParallel,  
doSNOW,  
tidyverse,  
dplyr,

reshape2,  
Rdpack  
**RdMacros** Rdpack  
**RoxygenNote** 7.1.1  
**VignetteBuilder** knitr  
**Depends** R (>= 2.10)

**R topics documented:**

aic . . . . .	2
aic.dmm . . . . .	3
availability . . . . .	4
bic . . . . .	5
bic.dmm . . . . .	6
distributions . . . . .	7
failureRate . . . . .	8
fitdmm . . . . .	9
getDistribution . . . . .	11
getDistribution.dmm . . . . .	12
getStationaryLaw . . . . .	13
getStationaryLaw.dmm . . . . .	14
getTransitionMatrix . . . . .	15
getTransitionMatrix.dmm . . . . .	16
lambda . . . . .	17
lengthWord_probabilities . . . . .	17
loglik . . . . .	18
loglik.dmm . . . . .	19
maintainability . . . . .	20
reliability . . . . .	21
simulate . . . . .	22
simulate.dmm . . . . .	23
stationary_distributions . . . . .	24
words_probabilities . . . . .	25
word_probabilities . . . . .	26
word_probability . . . . .	27
<b>Index</b>	<b>28</b>

---

aic	<i>Akaike Information Criterion (AIC)</i>
-----	---

---

**Description**

Generic function computing the Akaike Information Criterion of the model x, with the list of sequences sequences.

**Usage**

aic(x, sequences)

**Arguments**

x	An object for which AIC of the DMM can be computed.
sequences	A vector of character or a list of vector of character representing the sequences for which the AIC criterion must be computed.

**Value**

A list of AIC (numeric)

**Author(s)**

Victor Mataigne, Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

---

aic.dmm

---

*Evaluate AIC*


---

**Description**

Evaluate AIC

**Usage**

```
## S3 method for class 'dmm'
aic(x, sequences)
```

**Arguments**

x	An object of class dmm
sequences	A character vector or a list of character vector representing the sequence

**Value**

A list of AIC (numeric)

**Author(s)**

Victor Mataigne, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#), [getTransitionMatrix](#), [loglik](#), [aic](#)

## Examples

```
data(lambda, package = "drimmR")
sequence <- c("a","g","g","t","c","g","a","t","a","a","a")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
aic(dmm,sequence)
```

---

availability

*Availability function*

---

## Description

Pointwise (or instantaneous) availability of a system at time  $l \in N$

## Usage

```
availability(x, k1, k2, upstates, output_file = NULL, plot = FALSE)
```

## Arguments

x	An object of class dmm
k1	Start position : a positive integer giving the start position along the sequence from which the availabilities of the DMM should be computed
k2	End position : a positive integer giving the end position along the sequence until which the availabilities of the DMM should be computed
upstates	Character vector of the subspace working states among the state space vector such that <code>upstates &lt; s</code>
output_file	(Optional) A file containing matrix of availability probabilities (e.g. "C:/.../AVAL.txt")
plot	FALSE (no figure plot of availability by position); TRUE (figure plot)

## Details

The pointwise (or instantaneous) availability is the probability that the system is in a working state at time  $l$ , independently of the fact that the system worked or not during the time interval  $[0; l)$

## Value

A matrix with positions and availability probabilities of states (and figure plot)

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [reliability](#), [maintainability](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
availability(dmm,k1,k2,upstates,plot=TRUE)
```

---

bic

*Bayesian Information Criterion (BIC)*

---

**Description**

Generic function computing the Bayesian Information Criterion of the model *x*, with the list of sequences *sequences*.

**Usage**

```
bic(x, sequences)
```

**Arguments**

<i>x</i>	An object for which BIC of the DMM can be computed.
<i>sequences</i>	A vector or a list of vector of character representing the sequences for which the BIC criterion must be computed.

**Value**

A list of BIC (numeric)

**Author(s)**

Victor Mataigne, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

---

bic.dmm

*Evaluate BIC*

---

## Description

Evaluate BIC

## Usage

```
## S3 method for class 'dmm'
bic(x, sequences)
```

## Arguments

x	An object of class dmm
sequences	A character vector or a list of character vector representing the sequence

## Value

A list of BIC (numeric)

## Author(s)

Victor Mataigne, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#), [getTransitionMatrix](#), [loglik](#), [bic](#)

## Examples

```
data(lambda, package = "drimmR")
sequence <- c("a","g","g","t","c","g","a","t","a","a","a")
dmm<- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
bic(dmm,sequence)
```

---

distributions	<i>Plot distributions for a range of positions between &lt;start&gt; and &lt;end&gt;</i>
---------------	--

---

## Description

Plot distributions for a range of positions between <start> and <end>

## Usage

```
distributions(  
  x,  
  start = 1,  
  end = NULL,  
  step = NULL,  
  output_file = NULL,  
  plot = FALSE  
)
```

## Arguments

x	An object of class dmm
start	Start position : a positive integer giving the start position along the sequence from which the distributions of the DMM should be computed
end	End position : a positive integer giving the end position along the sequence until which the distributions of the DMM should be computed
step	A step (integer)
output_file	(Optional) A file containing matrix of distributions (e.g, "C:/.../DIST.txt")
plot	FALSE (no figure plot of dist evolution); TRUE (figure plot)

## Value

A matrix with positions and distributions of states (and figure plot)

## Author(s)

Alexandre Seiller

## References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#), [getDistribution](#), [getStationaryLaw](#)

## Examples

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
distributions(dmm,start=1,end=1000,step=100, plot=TRUE)
```

---

failureRate	<i>Failure rates function</i>
-------------	-------------------------------

---

## Description

Estimation of two different definition of the failure rate : the BMP-failure rate and RG-failure rate.

As for BMP-failure rate, consider a system  $S$  starting to work at time  $l = 0$ . The BMP-failure rate at time  $l \in N$  is the conditional probability that the failure of the system occurs at time  $l$ , given that the system has worked until time  $l - 1$ .

The RG-failure rate is a discrete-time adapted failure-rate proposed by D. Roy and R. Gupta. Classification of discrete lives. *Microelectronics Reliability*, 32(10):1459–1473, 1992.

## Usage

```
failureRate(
  x,
  k1,
  k2,
  upstates,
  failure.rate = c("BMP", "RG"),
  output_file = NULL,
  plot = FALSE
)
```

## Arguments

<code>x</code>	An object of class <code>dmm</code>
<code>k1</code>	Start position : a positive integer giving the start position along the sequence from which the failure rates of the DMM should be computed
<code>k2</code>	End position : a positive integer giving the end position along the sequence until which the failure rates of the DMM should be computed
<code>upstates</code>	Character vector of the subspace working states among the state space vector such that <code>upstates &lt; s</code>
<code>output_file</code>	(Optional) A file containing matrix of failure rates at each position (e.g, "C:/.../ER.txt")
<code>plot</code>	FALSE (no figure plot of failure rates by position); TRUE (figure plot)
<code>failure.rate</code>	Default="BMP", then BMP-failure-rate is the method used to estimate the failure rate. If <code>failure.rate= "RG"</code> , then RG-failure rate is the method used to estimate the failure rate.

## Details

The BMP-failure rate denoted by  $\lambda(l), l \in N$  is usually considered for continuous time systems.

The RG-failure rate denoted by  $r(l), l \in N$  is adapted to work in discrete time systems.



**Value**

A matrix with positions and failure rate scores of states (and figure plot)

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Roy D, Gupta R (1992). “Classification of discrete lives. Microelectronics Reliability.” *Microelectronics Reliability*, 1459–1473. doi: [10.1016/00262714\(92\)90015D](https://doi.org/10.1016/00262714(92)90015D), [https://doi.org/10.1016/0026-2714\(92\)90015-D](https://doi.org/10.1016/0026-2714(92)90015-D).

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [reliability](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
failureRate(dmm,k1,k2,upstates,failure.rate="BMP",plot=TRUE)
```

---

fitdmm

---

*Point by point estimates of a k-th order drifting Markov Model*


---

**Description**

Estimation of  $d+1$  points of support transition matrices and  $|E|^k$  initial law of a  $k$ -th order drifting Markov Model starting from one or several sequences.

**Usage**

```
fitdmm(
  sequences,
  order,
  degree,
  states,
  init.estim = c("mle", "freq", "prod", "stationary", "unif"),
  fit.method = c("sum")
)
```

### Arguments

sequences	A list of character vector(s) representing one (several) sequence(s)
order	Order of the Markov chain
degree	Degree of the polynomials (e.g., linear drifting if degree=1, etc.)
states	Vector of states space of length $s > 1$
init.estim	Default="mle". Method used to estimate the initial law. If <code>init.estim = "mle"</code> , then the classical Maximum Likelihood Estimator is used, if <code>init.estim = "freq"</code> , then, the initial distribution <code>init.estim</code> is estimated by taking the frequencies of the words of length $k$ for all sequences. If <code>init.estim = "prod"</code> , then, <code>init.estim</code> is estimated by using the product of the frequencies of each letter (for all the sequences) in the word of length $k$ . If <code>init.estim = "stationary"</code> , then <code>init.estim</code> is estimated by using the stationary law of the point of support transition matrices of each letter. If <code>init.estim = "unif"</code> , then, <code>init.estim</code> of each letter is estimated by using $\frac{1}{s}$ . Or 'init.estim' = customisable vector of length $ E ^k$ . See Details for the formulas.
fit.method	If sequences is a list of several character vectors of the same length, the usual LSE over the sample paths is proposed when <code>fit.method="sum"</code> (a list of a single character vector is its special case).

### Details

The `fitdmm` function creates a drifting Markov model object `dmm`.

Let  $E = 1, \dots, s$ ,  $s < \infty$  be random system with finite state space, with a time evolution governed by discrete-time stochastic process of values in  $E$ . A sequence  $X_0, X_1, \dots, X_n$  with state space  $E = 1, 2, \dots, s$  is said to be a linear drifting Markov chain (of order 1) of length  $n$  between the Markov transition matrices  $\Pi_0$  and  $\Pi_1$  if the distribution of  $X_t$ ,  $t = 1, \dots, n$ , is defined by  $P(X_t = v \mid X_{t-1} = u, X_{t-2}, \dots) = \Pi_{\frac{t}{n}}(u, v)$ ,  $u, v \in E$ , where  $\Pi_{\frac{t}{n}}(u, v) = (1 - \frac{t}{n})\Pi_0(u, v) + \frac{t}{n}\Pi_1(u, v)$ ,  $u, v \in E$ . The linear drifting Markov model of order 1 can be generalized to polynomial drifting Markov model of order  $k$  and degree  $d$ . Let  $\Pi_{\frac{i}{d}} = (\Pi_{\frac{i}{d}}(u_1, \dots, u_k, v))_{u_1, \dots, u_k, v \in E}$  be  $d$  Markov transition matrices (of order  $k$ ) over a state space  $E$ .

The estimation of DMMs is carried out for 4 different types of data :

**One can observe one sample path :** It is denoted by  $H(m, n) := (X_0, X_1, \dots, X_m)$ , where  $m$  denotes the length of the sample path and  $n$  the length of the drifting Markov chain. Two cases can be considered:

1.  $m=n$  (a complete sample path),
2.  $m < n$  (an incomplete sample path).

**One can also observe  $H$  i.i.d. sample paths :** It is denoted by  $H_i(m_i, n_i)$ ,  $i = 1, \dots, H$ . Two cases cases are considered :

1.  $m_i = n_i = n \forall i = 1, \dots, H$  (complete sample paths of drifting Markov chains of the same length),
2.  $n_i = n \forall i = 1, \dots, H$  (incomplete sample paths of drifting Markov chains of the same length). In this case, an usual LSE over the sample paths is used.

The initial distribution of a  $k$ -th order drifting Markov Model is defined as  $\mu_i = P(X_1 = i)$ . The initial distribution of the  $k$  first letters is freely customisable by the user, but five methods are proposed for the estimation of the latter :

**Estimation based on the Maximum Likelihood Estimator:** The Maximum Likelihood Estimator for the initial distribution. The formula is:  $\hat{\mu}_i = \frac{N_{start_i}}{L}$ , where  $N_{start_i}$  is the number of occurrences of the word  $i$  (of length  $k$ ) at the beginning of each sequence and  $L$  is the number of sequences. This estimator is reliable when the number of sequences  $L$  is high.

**Estimation based on the frequency:** The initial distribution is estimated by taking the frequencies of the words of length  $k$  for all sequences. The formula is  $\hat{\mu}_i = \frac{N_i}{N}$ , where  $N_i$  is the number of occurrences of the word  $i$  (of length  $k$ ) in the sequences and  $N$  is the sum of the lengths of the sequences.

**Estimation based on the product of the frequencies of each state:** The initial distribution is estimated by using the product of the frequencies of each state (for all the sequences) in the word of length  $k$ .

**Estimation based on the stationary law of point of support transition matrix for a word of length  $k$  :**  
The initial distribution is estimated using  $\mu(\prod_{n=1}^{k-1})$

**Estimation based on the uniform law :**  $\frac{1}{s}$

### Value

An object of class dmm

### Author(s)

Geoffray Brelurut, Alexandre Seiller

### References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

### Examples

```
data(lambda, package = "drimmR")
states <- c("a","c","g","t")
order <- 1
degree <- 1
fitdmm(lambda,order,degree,states, init.estim = "freq",fit.method="sum")
```

---

getDistribution

*Get the distributions of the DMM*


---

### Description

Generic function evaluating the distribution of a model  $x$  at a given position code or at every position `all.pos`

### Usage

```
getDistribution(x, pos, all.pos = FALSE, internal = FALSE)
```

**Arguments**

x	An object for which the distributions of the DMM can be computed.
pos	A positive integer giving the position along the sequence on which the distribution of the DMM should be computed
all.pos	'FALSE' (evaluation at position index) ; 'TRUE' (evaluation for all position indices)
internal	'FALSE' (default) ; 'TRUE' (for internal use of the <a href="#">distributions</a> function)

**Details**

Distribution at position  $l$  is evaluated by  $\mu_l = \mu_0 \prod_{t=k}^l \pi_{\frac{t}{n}}, \forall l \geq k, k \in N^*$  order of the DMM

**Value**

A vector or matrix of distribution probabilities

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

---

getDistribution.dmm      *Get the distributions of the DMM*

---

**Description**

Evaluate the distribution of the DMM at a given position or at every position

**Usage**

```
## S3 method for class 'dmm'
getDistribution(x, pos, all.pos = FALSE, internal = FALSE)
```

**Arguments**

x	An object of class dmm
pos	A positive integer giving the position along the sequence on which the distribution of the DMM should be computed
all.pos	'FALSE' (default, evaluation at position index) ; 'TRUE' (evaluation for all position indices)
internal	'FALSE' (default) ; 'TRUE' (for internal use of <a href="#">distributions</a> function)

**Details**

Distribution at position  $l$  is evaluated by  $\mu_l = \mu_0 \prod_{t=k}^l \pi_{\frac{t}{n}}, \forall l \geq k, k \in N^*$  order of the DMM

**Value**

A vector or matrix of distribution probabilities

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [distributions](#), [getStationaryLaw](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
t <- 10
getDistribution(dmm,pos=t)
```

---

getStationaryLaw

*Get the stationary laws of the DMM*


---

**Description**

Generic function evaluating the stationary law of a model `x` at a given position `pos` or at every position `all.pos`

**Usage**

```
getStationaryLaw(x, pos, all.pos = FALSE, internal = FALSE)
```

**Arguments**

<code>x</code>	An object for which the stationary laws of the DMM can be computed.
<code>pos</code>	A positive integer giving the position along the sequence on which the stationary law of the DMM should be computed
<code>all.pos</code>	‘FALSE’ (default, evaluation at position index) ; ‘TRUE’ (evaluation for all position indices)
<code>internal</code>	‘FALSE’ (default) ; ‘TRUE’ (for internal use of the initial law computation)

**Details**

Stationary law at position  $t$  is evaluated by solving  $\mu_t \pi_{\frac{t}{n}} = \mu$

**Value**

A vector or matrix of stationary law probabilities

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

---

getStationaryLaw.dmm    *Get the stationary laws of the DMM*

---

**Description**

Evaluate the stationary law of the DMM at a given position or at every position

**Usage**

```
## S3 method for class 'dmm'
getStationaryLaw(x, pos, all.pos = FALSE, internal = FALSE)
```

**Arguments**

x	An object of class dmm
pos	A positive integer giving the position along the sequence on which the stationary law of the DMM should be computed
all.pos	‘FALSE’ (default, evaluation at position index) ; ‘TRUE’ (evaluation for all position indices)
internal	‘FALSE’ (default) ; ‘TRUE’ (for internal use of the initial law of <a href="#">fitdmm</a> and word applications)

**Details**

Stationary law at position  $t$  is evaluated by solving  $\mu_t \pi_{\frac{t}{n}} = \mu$

**Value**

A vector or matrix of stationary law probabilities

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

**See Also**
[fitdmm](#), [getTransitionMatrix](#), [stationary\\_distributions](#), [getDistribution](#)
**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
t <- 10
getStationaryLaw(dmm,pos=t)
```

---

getTransitionMatrix	<i>Get transition matrix of the drifting Markov Model</i>
---------------------	---

---

**Description**

Generic function evaluating the transition matrix of a model x at a given position pos

**Usage**

```
getTransitionMatrix(x, pos)
```

**Arguments**

x	An object for which the transition matrices of the DMM can be computed.
pos	A positive integer giving the position along the sequence on which the transition matrix of the DMM should be computed

**Value**

A transition matrix at a given position

**Author(s)**

Victor Mataigne, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

---

getTransitionMatrix.dmm

*Get transition matrix of the drifting Markov Model*

---

## Description

Evaluate the transition matrix of the DMM at a given position

## Usage

```
## S3 method for class 'dmm'
getTransitionMatrix(x, pos)
```

## Arguments

x	An object of class dmm
pos	A positive integer giving the position along the sequence on which the transition matrix of the DMM should be computed

## Value

A transition matrix at a given position

## Author(s)

Victor Mataigne, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#)



**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'),init.estim = "freq", fit.method="sum")
t <- 10
getTransitionMatrix(dmm,pos=t)
```

---

lambda	<i>lambda genome</i>
--------	----------------------

---

**Description**

Complete data from phage genome [WT71] of length 48502

**Usage**

```
data(lambda)
```

**Format**

A vector object of class "Rdata".

**Examples**

```
data(lambda)
```

---

lengthWord_probabilities	<i>Probability of occurrence of the observed word of size n in a sequence at several positions</i>
--------------------------	--

---

**Description**

Probability of occurrence of the observed word of size n in a sequence at several positions

**Usage**

```
lengthWord_probabilities(m, sequence, pos, x, output_file = NULL, plot = FALSE)
```

**Arguments**

m	An integer, the length word
sequence	A vector of characters
pos	A vector of integer positions
x	An object of class dmm
output_file	(Optional) A file containing the vector of probabilities (e.g,"C:/.../PROB.txt")
plot	FALSE (no figure plot of words probabilities); TRUE (figure plot)

**Value**

A dataframe of probability by position (and probability plots)

**Author(s)**

Victor Mataigne, Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). “Reliability and survival analysis for drifting Markov models: modelling and estimation.” *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). “Drifting Markov models with polynomial drift and applications to DNA sequences.” *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [word\\_probability](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq")
m <- 2
lengthWordProbabilities(m, lambda, c(1,length(lambda)-m+1), dmm,plot=TRUE, fit.method="sum")
```

---

loglik

*Log-likelihood*


---

**Description**

Generic function computing the log-likelihood of the model x, with the list of sequences sequences.

**Usage**

```
loglik(x, sequences)
```

**Arguments**

x	An object for which the log-likelihood of the DMM can be computed.
sequences	A vector of character or list of vectors representing the sequences for which the log-likelihood of the model must be computed.

**Value**

A list of loglikelihood (numeric)

**Author(s)**

Annthomy Gilles, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

loglik.dmm

*Evaluate Log-likelihood*

## Description

Evaluate Log-likelihood

## Usage

```
## S3 method for class 'dmm'
loglik(x, sequences)
```

## Arguments

x	An object of class dmm
sequences	A character vector or a list of character vectors representing the sequence

## Value

A list of log-likelihood (numeric)

## Author(s)

Annthomy Gilles, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#), [getTransitionMatrix](#)

## Examples

```
data(lambda, package = "drimmR")
sequence <- c("a","g","g","t","c","g","a","t","a","a","a")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
loglik(dmm,sequence)
```

---

maintainability	<i>Maintainability function</i>
-----------------	---------------------------------

---

### Description

Maintainability of a system at time  $k \in N$ .

### Usage

```
maintainability(x, k1, k2, upstates, output_file = NULL, plot = FALSE)
```

### Arguments

x	An object of class dmm
k1	Start position : a positive integer giving the start position along the sequence from which the maintainabilities of the DMM should be computed
k2	End position : a positive integer giving the end position along the sequence until which the maintainabilities of the DMM should be computed
upstates	Character vector of the subspace working states among the state space vector such that $upstates < s$
output_file	(Optional) A file containing matrix of maintainability probabilities (e.g. "C:/.../MAIN.txt")
plot	FALSE (no figure plot of maintainability by position); TRUE (figure plot)

### Details

The maintainability at time  $k \in N$  of a system is the probability that the system is repaired up to time  $l$ , given that it has failed at time  $l = 0$ .

### Value

A matrix with positions and maintainability probabilities of states (and figure plot)

### Author(s)

Alexandre Seiller

### References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>.

### See Also

[ftdmm](#), [getTransitionMatrix](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
maintainability(dmm,k1,k2,upstates,plot=TRUE)
```

---

reliability	<i>Reliability function</i>
-------------	-----------------------------

---

**Description**

Reliability or the survival function of a system at time  $l \in N$

**Usage**

```
reliability(x, k1, k2, upstates, output_file = NULL, plot = FALSE)
```

**Arguments**

x	An object of class dmm
k1	Start position : a positive integer giving the start position along the sequence from which the reliabilities of the DMM should be computed
k2	End position : a positive integer giving the end position along the sequence until which the reliabilities of the DMM should be computed
upstates	Character vector of the subspace working states among the state space vector such that $upstates < s$
output_file	(Optional) A file containing matrix of reliability probabilities (e.g, "C:/.../REL.txt")
plot	FALSE (no figure plot of reliability by position); TRUE (figure plot)

**Details**

The reliability at time  $l \in N$  is the probability that the system has functioned without failure in the period  $[0, l]$

**Value**

A matrix with positions and reliability probabilities of states (and figure plot)

**Author(s)**

Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
k1 <- 1
k2 <- 200
upstates <- c("c","t") # vector of working states
reliability(dmm,k1,k2,upstates,plot=TRUE)
```

---

simulate	<i>Simulate a sequence under a drifting Markov model</i>
----------	--

---

**Description**

Generic function simulating a sequence of length `model_size` under a model `x`

**Usage**

```
simulate(x, output_file, model_size = 1e+05)
```

**Arguments**

<code>x</code>	An object for which simulated sequences of the DMM can be computed.
<code>output_file</code>	(Optional) File containing the simulated sequence (e.g, "C:/.../SIM.txt")
<code>model_size</code>	Size of the model

**Value**

the vector of simulated sequence

**Author(s)**

Annthomy Gilles, Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

simulate.dmm

*Simulate a sequence under a drifting Markov model***Description**

Simulate a sequence under a k-th order DMM.

**Usage**

```
## S3 method for class 'dmm'
simulate(x, output_file = NULL, model_size = NULL)
```

**Arguments**

x	An object of class dmm
output_file	(Optional) File containing the simulated sequence (e.g, "C:/.../SIM.txt")
model_size	Size of the model

**Value**

the vector of simulated sequence

**Author(s)**

Annthomy Gilles, Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [getStationaryLaw](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
simulate(dmm, model_size=100)
```

---

stationary\_distributions

*Plot stationary laws for a range of positions between <start> and <end>*


---

## Description

Plot stationary laws for a range of positions between <start> and <end>

## Usage

```
stationary_distributions(
  x,
  start = 1,
  end = NULL,
  step = NULL,
  output_file = NULL,
  plot = FALSE
)
```

## Arguments

x	An object of class dmm
start	Start position : a positive integer giving the start position along the sequence from which the stationary laws of the DMM should be computed
end	End position : a positive integer giving the end position along the sequence until which the stationary laws of the DMM should be computed
step	A step (integer)
output_file	(Optional) A file containing matrix of stationary laws (e.g, "C:/.../SL.txt")
plot	FALSE (no figure plot of SL evolution); TRUE (figure plot)

## Value

A matrix with positions and stationary laws of states (and figure plot)

## Author(s)

Alexandre Seiller

## References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s1100901896828](https://doi.org/10.1007/s1100901896828), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/15446115.1326](https://doi.org/10.2202/15446115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#), [getStationaryLaw](#)



**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
stationary_distributions(dmm,start=1,end=1000,step=100, plot=TRUE)
```

---

words_probabilities	<i>Probability of appearance of several words at several positions of a DMM</i>
---------------------	---

---

**Description**

Probability of appearance of several words at several positions of a DMM

**Usage**

```
words_probabilities(words, pos, x, output_file = NULL, plot = FALSE)
```

**Arguments**

words	A vector of characters containing words
pos	A vector of integer positions
x	An object of class dmm
output_file	(Optional) A file containing the matrix of probabilities (e.g,"C:/.../PROB.txt")
plot	FALSE (no figure plot of words probabilities); TRUE (figure plot)

**Value**

A dataframe of word probabilities along the positions of the sequence

**Author(s)**

Victor Mataigne, Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [word\\_probability](#), [word\\_probabilities](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
words_probabilities(c("atcgattc", "taggct", "ggatcgg"),c(100,300),dmm, plot=TRUE)
```

---

word_probabilities	<i>Probabilities of a word at several positions of a DMM</i>
--------------------	--

---

## Description

Probabilities of a word at several positions of a DMM

## Usage

```
word_probabilities(word, pos, x, output_file = NULL, plot = FALSE)
```

## Arguments

word	A subsequence (string of characters)
pos	A vector of integer positions
x	An object of class dmm
output_file	(Optional) A file containing the vector of probabilities (e.g, "C:/.../PROB.txt")
plot	FALSE (no figure plot of word probabilities); TRUE (figure plot)

## Value

A numeric vector, probabilities of word

## Author(s)

Victor Mataigne, Alexandre Seiller

## References

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1) . doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

## See Also

[fitdmm](#), [getTransitionMatrix](#), [word\\_probability](#), [words\\_probabilities](#)

## Examples

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
word_probabilities("aggctga",c(100,300),dmm, plot=TRUE)
```

---

word_probability	<i>Probability of a word at a position t of a DMM</i>
------------------	---

---

**Description**

Probability of a word at a position t of a DMM

**Usage**

```
word_probability(word, pos, x, output_file = NULL, internal = FALSE)
```

**Arguments**

word	A subsequence (string of characters)
pos	A position (numeric)
x	An object of class dmm
output_file	(Optional) A file containing the probability (e.g, "C:/.../PROB.txt")
internal	FALSE (default) ; TRUE (for internal use of word applications)

**Value**

A numeric, probability of word

**Author(s)**

Victor Mataigne, Alexandre Seiller

**References**

Barbu VS, Vergne N (2018). "Reliability and survival analysis for drifting Markov models: modelling and estimation." *Methodology and Computing in Applied Probability*, 1–33. doi: [10.1007/s11009-018-9682-8](https://doi.org/10.1007/s11009-018-9682-8), <https://doi.org/10.1007/s11009-018-9682-8>. Vergne N (2008). "Drifting Markov models with polynomial drift and applications to DNA sequences." *Statistical Applications in Genetics Molecular Biology*, **7**(1). doi: [10.2202/1544-6115.1326](https://doi.org/10.2202/1544-6115.1326), <https://doi.org/10.2202/1544-6115.1326>.

**See Also**

[fitdmm](#), [getTransitionMatrix](#), [word\\_probabilities](#), [words\\_probabilities](#)

**Examples**

```
data(lambda, package = "drimmR")
dmm <- fitdmm(lambda, 1, 1, c('a','c','g','t'), init.estim = "freq", fit.method="sum")
word_probability("aggctga", 4, dmm)
```

# Index

## \* datasets

lambda, [17](#)

aic, [2](#), [4](#)

aic.dmm, [3](#)

availability, [4](#)

bic, [5](#), [6](#)

bic.dmm, [6](#)

distributions, [7](#), [12](#), [13](#)

failureRate, [8](#)

fitdmm, [4–7](#), [9](#), [9](#), [10](#), [13–16](#), [18–20](#), [22–27](#)

getDistribution, [7](#), [11](#), [15](#)

getDistribution.dmm, [12](#)

getStationaryLaw, [7](#), [13](#), [13](#), [23](#), [24](#)

getStationaryLaw.dmm, [14](#)

getTransitionMatrix, [4–6](#), [9](#), [13](#), [15](#), [15](#),  
[18–20](#), [22](#), [23](#), [25–27](#)

getTransitionMatrix.dmm, [16](#)

lambda, [17](#)

lengthWord\_probabilities, [17](#)

loglik, [4](#), [6](#), [18](#)

loglik.dmm, [19](#)

maintainability, [5](#), [20](#)

reliability, [5](#), [9](#), [21](#)

simulate, [22](#)

simulate.dmm, [23](#)

stationary\_distributions, [15](#), [24](#)

word\_probabilities, [25](#), [26](#), [27](#)

word\_probability, [18](#), [25](#), [26](#), [27](#)

words\_probabilities, [25](#), [26](#), [27](#)