

# QEA Night 10

## Exercise

In[1]:=

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eq1 =  $\theta[s] == e_{rr2}[s] G_p[s] G_{MC}[s] G_{VC}[s];$ 
eq2 =  $V_d[s] == e_{rr1}[s] G_{PI}[s];$ 
eq3 =  $e_{rr1}[s] == \theta_d[s] - \theta[s] + G_{DC}[s] V[s];$ 
eq4 =  $V[s] == e_{rr2}[s] G_p[s] G_{MC}[s];$ 
eq5 =  $e_{rr2}[s] == V_d[s] - V[s];$ 
sol = Solve[{eq1, eq2, eq3, eq4, eq5}, { $\theta[s]$ ,  $V_d[s]$ ,  $e_{rr1}[s]$ ,  $V[s]$ ,  $e_{rr2}[s]$ }][[1]];
{G_TOTSYSTEM[s]  $\rightarrow \frac{\theta[s]}{\theta_d[s]}$  /. sol} (* this is a rule to replace G_TOTSYSTEM,
you can just extract the value by using the righthand side of the rule *)
trans =  $\frac{\theta[s]}{\theta_d[s]}$  /. sol /. {G_PI[s]  $\rightarrow K_p + (J_i/s)$ , G_VC[s]  $\rightarrow -s/(L s^2 - g)$ ,
G_MC[s]  $\rightarrow (a b)/(s + a)$ , G_P[s]  $\rightarrow J_p + (J_i/s)$ , G_DC[s]  $\rightarrow K_t/s$ }
tsumsub = Factor[trans /. {b  $\rightarrow 1/400$ , a  $\rightarrow 14$ , L  $\rightarrow .1$ , g  $\rightarrow 9.8$ }]
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$$\text{Out[7]} = \left\{ G_{\text{TOTSYSTEM}}[s] \rightarrow \frac{G_{MC}[s] G_P[s] G_{PI}[s] G_{VC}[s]}{1 + G_{MC}[s] G_P[s] - G_{DC}[s] G_{MC}[s] G_P[s] G_{PI}[s] + G_{MC}[s] G_P[s] G_{PI}[s] G_{VC}[s]} \right\}$$

$$\text{Out[8]} = - \frac{a b s \left( \frac{J_i}{s} + J_p \right) \left( \frac{K_i}{s} + K_p \right)}{(a + s) (-g + L s^2) \left( 1 + \frac{a b \left( \frac{J_i}{s} + J_p \right)}{a + s} - \frac{a b s \left( \frac{J_i}{s} + J_p \right) \left( \frac{K_i}{s} + K_p \right)}{(a + s) (-g + L s^2)} - \frac{a b \left( \frac{J_i}{s} + J_p \right) \left( \frac{K_i}{s} + K_p \right) K_t}{s (a + s)} \right)}$$

$$\text{Out[9]} = - \left( \left( 0.35 s^2 \left( 1. J_i K_i + 1. s J_p K_i + 1. s J_i K_p + 1. s^2 J_p K_p \right) \right) / \right. \\ \left. \left( -1372. s^3 - 98. s^4 + 14. s^5 + 1. s^6 - 3.43 s^2 J_i + 0.035 s^4 J_i - 3.43 s^3 J_p + \right. \right. \\ \left. 0.035 s^5 J_p - 0.35 s^2 J_i K_i - 0.35 s^3 J_p K_i - 0.35 s^3 J_i K_p - 0.35 s^4 J_p K_p + \right. \\ \left. 3.43 J_i K_i K_t - 0.035 s^2 J_i K_i K_t + 3.43 s J_p K_i K_t - 0.035 s^3 J_p K_i K_t + \right. \\ \left. 3.43 s J_i K_p K_t - 0.035 s^3 J_i K_p K_t + 3.43 s^2 J_p K_p K_t - 0.035 s^4 J_p K_p K_t \right) \right)$$

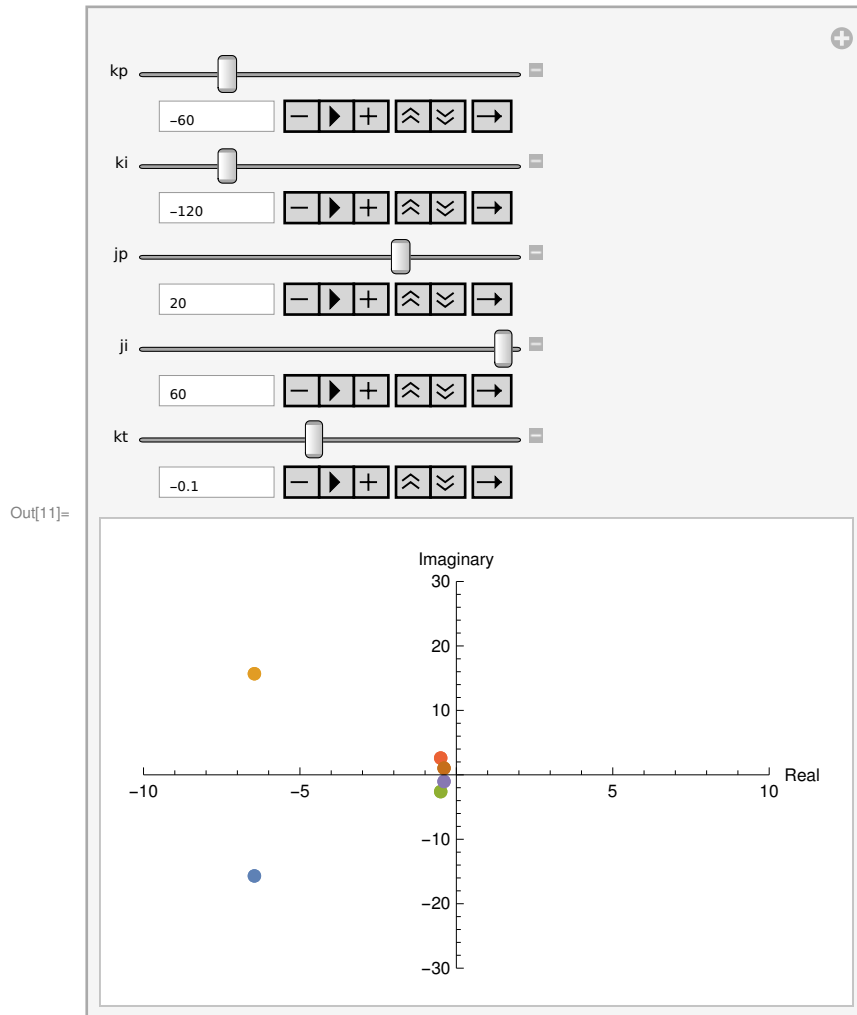
$$\text{Out[*]} = - \left( \left( 0.249 s^2 \left( 1. J_i K_i + 1. s J_p K_i + 1. s J_i K_p + 1. s^2 J_p K_p \right) \right) / \right. \\ \left. \left( -813.4 s^3 - 98. s^4 + 8.3 s^5 + 1. s^6 - 2.4402 s^2 J_i + 0.0249 s^4 J_i - 2.4402 s^3 J_p + \right. \right. \\ \left. 0.0249 s^5 J_p - 0.249 s^2 J_i K_i - 0.249 s^3 J_p K_i - 0.249 s^3 J_i K_p - 0.249 s^4 J_p K_p + \right. \\ \left. 2.4402 J_i K_i K_t - 0.0249 s^2 J_i K_i K_t + 2.4402 s J_p K_i K_t - 0.0249 s^3 J_p K_i K_t + \right. \\ \left. 2.4402 s J_i K_p K_t - 0.0249 s^3 J_i K_p K_t + 2.4402 s^2 J_p K_p K_t - 0.0249 s^4 J_p K_p K_t \right) \right)$$

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In[8]:= poles = ReIm[Values[Solve[Denominator[tsumsub] == 0, s]]];
ListPlot[poles /. {Kp → -88, Ki → -100, Jp → 10, Ji → 56, Kt → -0.1}];
```

**Solve:** Solve was unable to solve the system with inexact coefficients. The answer was obtained by solving a corresponding exact system and numericizing the result.

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In[10]:= (*Sweep values of kp and ki*)
f[Kp_, Ki_, Jp_, Ji_, Kt_] = ReIm[N[Values[Solve[
  Denominator[tsumsub /. {Kp → Kp, Ki → Ki, Jp → Jp, Ji → Ji, Kt → Kt}] == 0, s]]]];
(*returns list as s→[[values]]*)
Manipulate[
  ListPlot[f[Kp, Ki, Jp, Ji, Kt] /. {Kp → kp, Ki → ki, Jp → jp, Ji → ji, Kt → kt},
    AxesLabel → {"Real", "Imaginary"}, PlotStyle → PointSize[Large],
    PlotRange → {{-10, 10}, {-30, 30}}, {kp, -100, 100},
    {ki, -200, 200}, {jp, -50, 50}, {ji, -60, 60}, {kt, -1, 1}]
```

**Solve:** Solve was unable to solve the system with inexact coefficients. The answer was obtained by solving a corresponding exact system and numericizing the result.



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In[ ]:= ClearAll["Global`*"]
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