2020 NCAA Tournament Prediction

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Executive Summary

Sadly, the 2020 NCAA Men's Basketball tournament could not be held this year due to the coronavirus. I found data on the past four years and thought it would be interesting to see if I could accurately represent what could have been. Based on several variables in this dataset found in Appendix 1 and 2.1, is it possible to predict the teams that will make the tournament? Also, based on this information, can we give an estimate of the round this team will make it to? These are great questions to be answered using a variety of different classification type models.

First, we should examine the data (Appendix 2.1). There are several variables that could have a potentially high correlation. The variance inflation factors in Appendix 3.1 with extremely high correlation are effective field goal percentage of shots taken and allowed. This is nearly a direct calculation of other variables presented in the dataset. Another variable with a high inflation factor is the power rating. This rating is more or less a summary of a team based on several factors presented in the data already. The last two factors of potential concern are offensive and defensive efficiency. Model selection should be able to take care of this multicollinearity. We can check our final models with diagnostic plots. The last step is to view the correlation of our potential responses and regressors with a correlation matrix. My main variable of interest is post season wins. It seems there is high correlation between several variables and the response, Appendix 3.2. We can plot some of the variables with the highest correlation. The scatter plot in Appendix 3.3 shows the relationships between post season wins and the regressors. There does appear to be significant multicollinearity as we found before.

Before we begin setting up models, it is necessary to check if the regressors need transformations. The Box-Cox method provides significant evidence for transformations, Appendix 3.4. Testing the case with no transformations gives a p-value of less than 0.0001 so transformations are clearly needed, but even after testing the recommended transformations, the p-value was still below 0.0001. It seems another factor is at play such as the multicollinearity noted previously. We can again proceed with caution. Model selection and diagnostic checks should give us a better look at what is going on later. Besides, the recommended transformations hurt the interpretability of our results quite substantially. Since we want models that perform classification, we are unable to test the transformation of our response.

First, we build a model using all potentially useful variables, Appendix 4. We can check for outliers before we begin model selection. The halfnorm plot in Appendix 4.1 suggests observation 1329 is an outlier. Upon further inspection, this team made the tournament with a terrible record among other poor variables. We will continue the analysis with this team since removing this team is unjustified. By reviewing the summary of our first model, we see several variables are insignificant. We will test removing the variable with the highest p-value in the summary of the model recursively until the ANOVA test provides evidence to accept the full model. The method is not exact, but it gives us a good idea of the variables and models that are most significant. The variables to be kept in the model were power rating, turnover rate, and wins above the bubble to name a few. Even the random effects were not significant with this final model (Appendix 4.2). Next, diagnostic checks were completed once more (Appendix 4.3). Observation 1329 was still an outlier, but the jump in trend is relatively insignificant. There is still some pretty high VIF results, but they are much lower than before. It seems this model does not drastically break any assumptions. Last, we can test the model's predictive ability. By looking at a ROC curve (Appendix 4.4), we find the best threshold for acceptance to balance the sensitivity and specificity appears to be 0.22. With this, our training error rate was 0.125. The testing error was 0.127 for 2019. Now, we can estimate the round at which a team will go out.

In this multinomial model, I will show a model that tries to predict all rounds (Appendix 5). Model selection was simple and chose a model with similar variables to the previous model except two point shooting percentage is now included in the final model. This model also allows for easy interpretation of variables. For example, power rating is still a big indictator for success in the tournament, but as a team progresses, other variables become more important. A look at the training error shows this model does better than the previous in predicting teams to make the tournament and even does a fair job in predicting the round a team will make it to. Another nice feature about this model is the ability to view important factors associated with each round of the tournament. The error is around 75%, but each team has 9 options to land

on (Appendix 5.2). This model did predict the champion and second place winner all four years (Appendix 5.1), but that could indicate the model is over fit on the training set. This model performed much better than the binomial model at predicting a team to make it to the tournament, but it may be useful to look at a model trained on the teams already known to make it to the tournament and see where they are predicted to make it in the tournament.

By setting up a model given a team has already made it into the tournament (Appendix 6), a summary of the most significant model shows power rating (both previous models biggest determining factor) is no longer included. The current model shows the highest magnitude predictor is now turnover rate which is somewhat interesting since it did not have a huge effect in the previous models and one does not typically view turnover rate as the statistic that wins games. Now, we see the error in the training set is still high (Appendix 6.2), but it is drastically reduced from the previous approach. The test set error reiterates this point. The model was actually even able to predict the correct champion in the test set. The next step would be to try out this line of thinking with a random forest.

This research question seems like it would be best fit for a categorical tree. We lose the quantitative inference capability about specific regressors the last models gave, but the main point of this analysis is prediction. We will compare the performance of a bagging and a random forest approach (Appendix 7). The bagging approach produced lower out of bag error as well as lower testing error per round. The bagging approach even correctly predicted the champion. From looking at importance we see both models put strong emphasis on wins above the bubble. This is the first model to do so. We will continue using the bagging model and try out a model trained on teams already in the tournament like before.

We fit a model in the same manner as the second multinomial model. The testing error is worse than the multinomial model (Appendix 8). We see the importance of wins above the bubble dropped as power rating became important once more. It will not be necessary to combine models on making the tournament versus round performance for the final prediction of the 2020 season. The multinomial model that considered all teams at once performed the best overall. This is nice since the model leaves interpretability of regressors intact. The table in Appendix 9 gives a comparison of error among the models created.

Each model has it own strengths. The binomial model was by far the least useful model in terms of error. Every other model was able to predict teams making the tournament much better. It appears the bag model performs the best on test data. It was also great at predicting teams to make the tournament. The multinomial model came in at a close second, but test error plays a big role when prediction is desired. We can try predicting the NCAA tournament for 2020 using both models as a comparison.

The final prediction of the tournament in 2020, which never happened due to the coronavirus, is given in Appendix 10. In this prediction, we will put more weight in the bag model's predictions due to the performance seen in the error table (Appendix 9). The summary of the predictions (Appendix 10) shows the bag model predicted 303 teams not making the tournament and 2 teams making it past the round of 32 and the multinomial model predicted 309 teams not making the tournament and 3 teams making it past the round of 32. We can view the teams the bag model predicted to make it to the Elite 8 which were Kansas and Gonzaga. The multinomial model also had Kansas and Gonzaga in the Elite 8 with Dayton coming out of nowhere and being the runner up in the tournament. The bag model predicted Dayton to go out in the round of 32. Last, but not least, we can see the comparison of teams in the Big Ten and their predicted round at which they lost in (Appendix 10.2). Indiana was predicted to go out in the first round in both models while, our rival, Purdue did not even make the tournament in either model.

Due to the error seen in the training and testing sets with these models, we cannot put much weight in their predictions, but the teams projected to make the tournament can almost be guaranteed. Every year sees drastic variability with the presence of "bracket busting" teams. It is difficult to identify winning teams without being able to compare specific matchups. This analysis gives a good measure of minimum performance based on overall team statistics alone. The main take away is the various impactful predictors an above average team possesses in order to make it late into the tournament such as power rating and wins above the bubble. The final prediction ability is less than desired, but this has been an interesting look on what could have been.

Methods and Results

Appendix 1. Variable Definitions

Team Information

YEAR: Season

TEAM: The Division I college basketball school

CONF: The Athletic Conference in which the school participates in

A10 = Atlantic 10

ACC = Atlantic Coast Conference

AE = America East

Amer = American

ASun = ASUN

B10 = Big Ten

B12 = Big 12

BE = Big East

BSky = Big Sky

BSth = Big South

BW = Big West

CAA = Colonial Athletic Association

CUSA = Conference USA

Horz = Horizon League

IND = Independent schools

Ivy = Ivy League

MAAC = Metro Atlantic Athletic Conference

MAC = Mid-American Conference

MEAC = Mid-Eastern Athletic Conference

MVC = Missouri Valley Conference

MWC = Mountain West

NEC = Northeast Conference

OVC = Ohio Valley Conference

P12 = Pac-12

Pat = Patriot League

SB = Sun Belt

SC = Southern Conference

SEC = South Eastern Conference

Slnd = Southland Conference

Sum = Summit League

SWAC = Southwestern Athletic Conference

WAC = Western Athletic Conference

WCC = West Coast Conference

Tournament Information

SEED: Seed in the NCAA March Madness Tournament

TRNMT: Made tournament, yes or no

PS_WINS: Post season wins in NCAA tournament

POSTSEASON: Round where the given team was eliminated or where their season ended

R68 = First Four

R64 = Round of 64

R32 = Round of 32

S16 = Sweet Sixteen

E8 = Elite Eight

F4 = Final Four

2ND = Runner-up

Champions = Winner of the NCAA March Madness Tournament for that given year

Team Statistics

G: Number of games played in total

W: Number of games won in total

BARTHAG: Power Rating (Chance of beating an average Division I team)

WAB: Wins Above Bubble (The bubble refers to the cut off between making the NCAA March Madness Tournament and not making it)

Offensive Statistics

ADJOE: Adjusted Offensive Efficiency (An estimate of the offensive efficiency (points scored per 100 possessions) a team would have against the average Division I defense)

EFG_O: Effective Field Goal Percentage Shot

TOR: Turnover Percentage Allowed (Turnover Rate)

ORB: Offensive Rebound Percentage

FTR: Free Throw Rate (How often the given team shoots Free Throws)

TWO_P_O: Two-Point Shooting Percentage

THREE_P_O: Three-Point Shooting Percentage

ADJ_T: Adjusted Tempo (An estimate of the tempo (possessions per 40 minutes) a team would have against the team that wants to play at an average Division I tempo)

Defensive Statistics

ADJDE: Adjusted Defensive Efficiency (An estimate of the defensive efficiency (points allowed per 100 possessions) a team would have against the average Division I offense)

EFG_D: Effective Field Goal Percentage Allowed

TORD: Turnover Percentage Committed (Steal Rate)

DRB: Defensive Rebound Percentage

FTRD: Free Throw Rate Allowed

TWO_P_D: Two-Point Shooting Percentage Allowed

THREE_P_D: Three-Point Shooting Percentage Allowed

Appendix 2. Data Manipulation

```
# Read Data into an Object
# https://www.kaggle.com/andrewsundberg/college-basketball-dataset/data
raw_data_15_19 = fread("cbb.csv")
raw_data_20 = fread("cbb20.csv")
# Combining Dataframes
raw_data_20 <- raw_data_20[,-c("RK")] #shows rank which isn't included in other years
raw_data_20 <- raw_data_20 %>%
                  mutate(POSTSEASON="No Tournament", #including arbitrary values so dataframes match co
                         SEED=99,
                         YEAR=2020)
raw_data <- bind_rows(raw_data_15_19, raw_data_20)</pre>
# Remove unneeded dataframes
rm(raw_data_15_19)
rm(raw_data_20)
# View Data
summary(raw_data) #notice NAs
```

```
##
        TEAM
                            CONF
                                                                  : 0.00
##
   Length:2110
                        Length:2110
                                           Min.
                                                   :24.0
                                                           Min.
    Class : character
                        Class : character
                                            1st Qu.:30.0
                                                           1st Qu.:12.00
   Mode :character
                       Mode :character
                                           Median:31.0
                                                           Median :16.00
##
                                           Mean
                                                   :31.3
                                                           Mean
                                                                  :16.48
##
                                            3rd Qu.:33.0
                                                           3rd Qu.:21.00
##
                                           Max.
                                                   :40.0
                                                           Max.
                                                                  :38.00
##
##
        ADJOE
                         ADJDE
                                        BARTHAG
                                                           EFG O
##
    Min.
          : 76.7
                    Min.
                           : 84.0
                                            :0.0077
                                                              :39.30
    1st Qu.: 98.4
                    1st Qu.: 98.6
                                     1st Qu.:0.2833
                                                       1st Qu.:48.00
   Median :103.0
##
                    Median :103.3
                                     Median :0.4746
                                                       Median :49.90
## Mean
          :103.3
                    Mean :103.3
                                     Mean
                                            :0.4941
                                                       Mean
                                                              :50.03
    3rd Qu.:107.9
                    3rd Qu.:107.8
                                     3rd Qu.:0.7111
                                                       3rd Qu.:52.00
##
  Max.
           :129.1
                    Max.
                            :124.0
                                     Max.
                                            :0.9842
                                                       Max.
                                                              :59.80
##
                         TOR
##
        EFG_D
                                          TORD
                                                           ORB
   \mathtt{Min}.
           :39.60
                    Min.
                            :12.40
                                     Min.
                                             :10.20
                                                      Min.
                                                             :14.20
   1st Qu.:48.30
                    1st Qu.:17.30
                                     1st Qu.:17.10
                                                      1st Qu.:26.30
##
   Median :50.10
                    Median :18.60
                                     Median :18.50
                                                      Median :29.10
##
##
    Mean
           :50.19
                    Mean
                            :18.65
                                     Mean
                                            :18.58
                                                      Mean
                                                             :29.04
    3rd Qu.:52.10
                    3rd Qu.:19.90
                                     3rd Qu.:20.00
                                                      3rd Qu.:31.80
##
    Max.
           :59.50
                    Max.
                            :26.60
                                     Max.
                                            :28.00
                                                      Max.
                                                             :42.10
##
##
         DRB
                          FTR
                                          FTRD
                                                           2P 0
##
                                                             :37.70
  \mathtt{Min}.
           :18.40
                    Min.
                            :21.60
                                     Min.
                                            :19.70
                                                      Min.
   1st Qu.:27.10
                    1st Qu.:31.30
                                     1st Qu.:30.60
                                                      1st Qu.:46.90
## Median :29.20
                    Median :34.60
                                     Median :34.30
                                                      Median :49.10
## Mean
          :29.22
                    Mean
                          :34.69
                                     Mean
                                           :34.94
                                                      Mean
                                                           :49.19
## 3rd Qu.:31.30
                    3rd Qu.:38.00
                                     3rd Qu.:38.80
                                                      3rd Qu.:51.40
```

```
Max.
          :40.40 Max.
                          :51.00
                                   Max.
                                          :58.50 Max.
                                                         :62.60
##
##
##
        2P D
                        3P 0
                                        3P D
                                                     ADJ T
          :37.70
                          :24.80
                                         :27.1
##
  Min.
                  Min.
                                   Min.
                                                 Min.
                                                        :57.2
##
   1st Qu.:47.20
                   1st Qu.:32.40
                                   1st Qu.:32.9
                                                 1st Qu.:66.4
  Median: 49.30 Median: 34.30
                                   Median:34.5
##
                                                 Median:68.5
  Mean :49.32 Mean :34.33
                                   Mean :34.5 Mean :68.4
## 3rd Qu.:51.60 3rd Qu.:36.20
                                   3rd Qu.:36.1
                                                 3rd Qu.:70.3
## Max.
         :61.20 Max.
                          :44.10
                                   Max. :43.1
                                                 Max.
                                                        :83.4
##
##
        WAB
                     POSTSEASON
                                             SEED
                                                            YEAR
         :-25.200 Length:2110
                                              : 1.00 Min.
## Min.
                                       Min.
                                                              :2015
  1st Qu.:-13.000
                    Class :character
                                       1st Qu.: 9.00
                                                       1st Qu.:2016
                   Mode :character
## Median : -8.300
                                       Median:99.00
                                                      Median:2018
## Mean
         : -7.814
                                        Mean
                                             :54.74
                                                       Mean
                                                              :2018
## 3rd Qu.: -3.100
                                        3rd Qu.:99.00
                                                       3rd Qu.:2019
## Max. : 13.100
                                        Max.
                                               :99.00 Max. :2020
##
                                        NA's
                                               :1417
# Data Cleaning
raw_data$POSTSEASON[is.na(raw_data$POSTSEASON)] = "No Tournament" # removing NAs
raw_data$SEED[is.na(raw_data$SEED)] = 99
raw_data <- raw_data %>%
               mutate(TWO_P_O = `2P_O`, # Not a good naming format for R
                      TWO_P_D = `2P_D`,
                      THREE_P_O = 3P_0,
                      THREE_P_D = `3P_D`,
                      TRNMT = ifelse(POSTSEASON=="No Tournament", "No", "Yes")) %>%
               select(everything(), -c(`2P_O`, `2P_D`, `3P_O`, `3P_D`))
raw_data$POSTSEASON <- factor(raw_data$POSTSEASON, order = TRUE, levels = c('No Tournament', 'R68', 'R6
                                                                          'R32', 'S16', 'E8', 'F4', '
                                                                          'Champions'))
raw_data$PS_WINS = ifelse(as.numeric(raw_data$POSTSEASON) - 3 < 0, 0, as.numeric(raw_data$POSTSEASON) -
# Changing Data Types
raw_data$CONF <- as.factor(raw_data$CONF)</pre>
raw_data$TRNMT <- as.factor(raw_data$TRNMT)</pre>
raw_data$YEAR <- as.factor(raw_data$YEAR)</pre>
                                               # make year start at zero
# Data Cleaning Done
clean_data <- raw_data</pre>
```

Appendix 2.1. View Data

```
# View Data Attributes
head(clean_data)

## TEAM CONF G W ADJOE ADJDE BARTHAG EFG_0 EFG_D TOR TORD ORB
## 1 North Carolina ACC 40 33 123.3 94.9 0.9531 52.6 48.1 15.4 18.2 40.7

## 2 Wisconsin B10 40 36 129.1 93.6 0.9758 54.8 47.7 12.4 15.8 32.1

## 3 Michigan B10 40 33 114.4 90.4 0.9375 53.9 47.7 14.0 19.5 25.5
```

```
## 4
        Texas Tech B12 38 31 115.2 85.2 0.9696 53.5 43.0 17.7 22.8 27.4
## 5
           Gonzaga WCC 39 37 117.8 86.3 0.9728 56.6 41.1 16.2 17.1 30.0
## 6
              Duke ACC 39 35 125.2 90.6 0.9764 56.6 46.5 16.3 18.6 35.8
##
     DRB FTR FTRD ADJ_T WAB POSTSEASON SEED YEAR TWO_P_O TWO_P_D THREE_P_O
## 1 30.0 32.3 30.4 71.7 8.6
                                     2ND
                                            1 2016
                                                      53.9
                                                              44.6
                                                                       32.7
## 2 23.7 36.2 22.4 59.3 11.3
                                     2ND
                                            1 2015
                                                      54.8
                                                              44.7
                                                                       36.5
## 3 24.9 30.7 30.0 65.9 6.9
                                     2ND
                                            3 2018
                                                      54.7
                                                             46.8
                                                                       35.2
## 4 28.7 32.9 36.6 67.5 7.0
                                     2ND
                                            3 2019
                                                      52.8
                                                             41.9
                                                                       36.5
## 5 26.2 39.0 26.9 71.5 7.7
                                     2ND
                                            1 2017
                                                      56.3
                                                              40.0
                                                                       38.2
## 6 30.2 39.8 23.9 66.4 10.7 Champions
                                            1 2015
                                                      55.9
                                                              46.3
                                                                       38.7
    THREE_P_D TRNMT PS_WINS
## 1
         36.2
                Yes
                          5
## 2
         37.5
                Yes
                          5
## 3
         33.2
                          5
                Yes
## 4
         29.7
                Yes
                          5
## 5
         29.0
                Yes
                          5
## 6
         31.4
                Yes
                          6
```

summary(clean_data)

##	TEA	ΔM	CONF				G		W	
##	Length:	2110	ACC	:	90	Min.	:24.0	Min	. : 0.00	
##	_	characte		:	84	1st (Qu.:30.0	1st	Qu.:12.00	
##	Mode :	characte	B10	:	84		an :31.0		ian :16.00	
##			CUSA	:	84	Mean	:31.3	Mea:	n :16.48	
##			SEC	:	84	3rd (Qu.:33.0	3rd	Qu.:21.00	
##			Slnd	:	78	Max.	:40.0	Max	. :38.00	
##	(Other):1606									
##	ADJOE		ADJDE			BARTHAG			EFG_O	
##	Min.	: 76.7	Min.	: 84.	0	Min.	:0.0077	Min	. :39.30	
##	1st Qu.	: 98.4	1st Qu.	: 98.	6	1st Qu	.:0.2833	lst	Qu.:48.00	
##	Median	:103.0	Median	:103.	3	Median	:0.4746	Med	ian :49.90	
##	Mean	:103.3	Mean	:103.	3	Mean	:0.4941	Mea	n :50.03	
##	3rd Qu.	:107.9	3rd Qu.	:107.	8	3rd Qu	.:0.7111	. 3rd	Qu.:52.00	
##	Max.	:129.1	Max.	:124.	0	Max.	:0.9842	Max	. :59.80	
##										
##	EFG	<u>-</u> D	TOR			TORD			ORB	
##	Min.	:39.60	Min.	:12.4	0	Min.	:10.20	Min.	:14.20	
##	1st Qu.	:48.30	1st Qu.	:17.3	0	1st Qu	.:17.10	1st	Qu.:26.30	
##	Median	:50.10	Median	:18.6	0	${\tt Median}$:18.50	Medi	an :29.10	
##	Mean	:50.19	Mean	:18.6	5	Mean	:18.58	Mean	:29.04	
##	3rd Qu.	:52.10	$3rd\ Qu.$:19.9	0	3rd Qu	.:20.00	3rd	Qu.:31.80	
##	Max.	:59.50	Max.	:26.6	0	Max.	:28.00	${\tt Max.}$:42.10	
##										
##	DRB		FTR		FTRD			ADJ_T		
##	Min.	:18.40	Min.	:21.6	0	Min.	:19.70		:57.2	
##	1st Qu.		1st Qu.	:31.3	0	1st Qu	.:30.60	1st	Qu.:66.4	
##	Median		Median			Median	:34.30	Medi	an :68.5	
##	Mean		Mean		-		:34.94		:68.4	
##	3rd Qu.		3rd Qu.			-	.:38.80		Qu.:70.3	
##	Max.	:40.40	Max.	:51.0	0	Max.	:58.50	${\tt Max.}$:83.4	
##										
##						EASON SEE			YEAR	
##	Min.	:-25.200	No To	urnam	ent	: 1770	Min.	: 1.00	2015:35	

```
: 80
## Median : -8.300 R32
                                       Median :99.00
                                                     2017:351
## Mean : -7.814
                   S16
                               : 40
                                       Mean :84.46
                                                     2018:351
                               : 20
## 3rd Qu.: -3.100
                   R68
                                       3rd Qu.:99.00
                                                     2019:353
                               : 20
## Max. : 13.100
                   E8
                                      Max. :99.00
                                                     2020:353
                               : 20
##
                   (Other)
##
      TWO P O
                   TWO_P_D
                                THREE P O
                                                 THREE P D
## Min. :37.70 Min. :37.70 Min. :24.80
                                               Min. :27.1
                                                            No :1770
## 1st Qu.:46.90 1st Qu.:47.20
                               1st Qu.:32.40
                                               1st Qu.:32.9
                                                            Yes: 340
## Median :49.10 Median :49.30
                                Median :34.30
                                               Median:34.5
## Mean :49.19 Mean :49.32 Mean :34.33
                                               Mean :34.5
## 3rd Qu.:51.40 3rd Qu.:51.60
                                3rd Qu.:36.20
                                               3rd Qu.:36.1
## Max. :62.60 Max. :61.20
                                Max. :44.10 Max. :43.1
##
##
      PS_WINS
## Min. :0.0000
## 1st Qu.:0.0000
## Median :0.0000
## Mean :0.1493
## 3rd Qu.:0.0000
## Max. :6.0000
##
# Separate data for train and test sets
train_data <- clean_data[which(clean_data$YEAR==2015|clean_data$YEAR==2016|clean_data$YEAR==2017|clean_
test_data_19 <- clean_data[which(clean_data$YEAR==2019), ]</pre>
test_data_20 <- clean_data[which(clean_data$YEAR==2020), ]</pre>
rm(raw_data, clean_data)
```

1st Qu.:99.00

2016:351

: 160

R64

1st Qu.:-13.000

Appendix 3. Check Assumptions

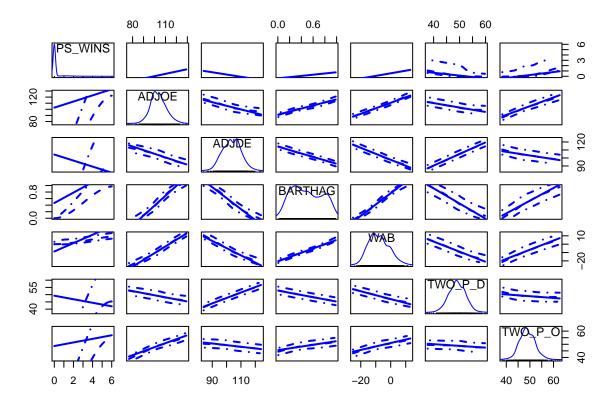
Appendix 3.1. Variance Inflation Factor

```
# Check multicollinearity
sort(faraway::vif(train_data[,-c(1:4, 18:20, 25:26)]))
                                                              # removing factors and potential respons
##
                                                     ORB
                                                               TORD
       ADJ_T
                    FTR
                              FTRD
                                          DRB
##
    1.236197
               1.299749
                          1.740173
                                     2.191951
                                                2.946805
                                                           3.098201
##
         TOR
                    WAB
                             ADJDE
                                        ADJOE THREE_P_O
                                                            BARTHAG
##
    3.105086 13.243053 22.690760 28.540690 33.348308 36.511312
## THREE_P_D
                TWO_P_O
                           TWO_P_D
                                        EFG_O
                                                   EFG_D
## 43.064142 69.770015 121.052453 152.321249 224.862661
```

Appendix 3.2. Correlation Matrix

```
# correlation matrix
round(cor(train_data[,-c(1:4, 18:20, 25)])[,c(18)], 4)
                                                                     TORD
##
       ADJOE
                 ADJDE
                         BARTHAG
                                     EFG_O
                                               EFG_D
                                                            TOR
##
      0.4683
               -0.4000
                          0.4270
                                    0.2836
                                             -0.2782
                                                        -0.2472
                                                                   0.0534
##
         ORB
                   DRB
                             FTR
                                      FTRD
                                               ADJ_T
                                                                  TWO_P_O
                                                            WAB
     0.1817
               -0.0908
                          0.0108
                                   -0.2017
                                             -0.0362
##
                                                         0.4950
                                                                   0.2764
    TWO_P_D THREE_P_O THREE_P_D
                                   PS_WINS
##
##
     -0.2553
                0.1983
                         -0.1937
                                    1.0000
```

Appendix 3.3. Scatter Plot Matrix



Appendix 3.4. Transformations

The scatter plot in Appendix 3.3 shows the relationships between post season wins and the regressors. There does appear to be pretty significant multicollinearity as we found before.

```
## bcPower Transformations to Multinormality
##
             Est Power Rounded Pwr Wald Lwr Bnd Wald Upr Bnd
## ADJOE
                -0.9338
                               -1.00
                                           -1.1530
                                                        -0.7146
## ADJDE
                 1.6317
                                1.63
                                            1.3267
                                                          1.9367
## BARTHAG
                 0.7129
                                0.71
                                            0.6719
                                                         0.7539
## EFG_0
                 0.2583
                                0.33
                                            0.0695
                                                          0.4471
## EFG_D
                 0.8536
                                1.00
                                            0.6600
                                                          1.0472
## TOR
                 0.8215
                                1.00
                                            0.5086
                                                          1.1344
## TORD
                 0.5926
                                0.50
                                            0.3252
                                                          0.8601
## ORB
                 1.3590
                                                          1.5927
                                1.36
                                            1.1254
## DRB
                 1.0166
                                1.00
                                            0.6691
                                                          1.3641
## FTR
                 0.5851
                                0.50
                                           0.2638
                                                         0.9065
## FTRD
                 0.1689
                                0.00
                                           -0.0738
                                                          0.4116
                                1.00
                                           0.0218
## ADJ_T
                 0.7688
                                                          1.5158
```

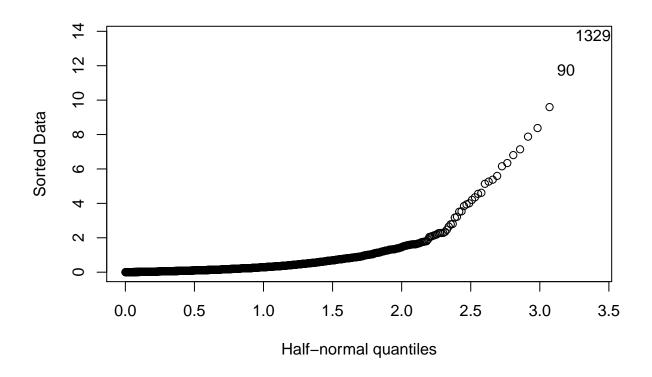
```
## TWO_P_O
                                    -0.3323
                                                 0.0675
             -0.1324
                           0.00
                                                 0.8876
## TWO_P_D
              0.6877
                           0.50
                                     0.4879
## THREE P O
              0.9606
                           1.00
                                     0.7557
                                                 1.1654
## THREE_P_D
              1.0242
                           1.00
                                     0.8111
                                                 1.2374
## Likelihood ratio test that transformation parameters are equal to 0
## (all log transformations)
                                                      LRT df
## LR test, lambda = (0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 2724.65 16 < 2.22e-16
## Likelihood ratio test that no transformations are needed
                                                       LRT df
testTransform(bc_x, c(-1, 1.63, 0.71, 0.33, 1, 1, 0.5, 1.36, 1, 0.50, 0, 1, 0, 0.5, 1, 1))
##
                                                                        LRT
## LR test, lambda = (-1 1.63 0.71 0.33 1 1 0.5 1.36 1 0.5 0 1 0 0.5 1 1) 51.98504
## LR test, lambda = (-1 1.63 0.71 0.33 1 1 0.5 1.36 1 0.5 0 1 0 0.5 1 1) 16
                                                                         pval
## LR test, lambda = (-1 1.63 0.71 0.33 1 1 0.5 1.36 1 0.5 0 1 0 0.5 1 1) 1.1015e-05
```

Appendix 4. Model 1: Logistic Model with Random Effects

boundary (singular) fit: see ?isSingular

Appendix 4.1. Diagnostic Check

```
halfnorm(resid(model_binom, type="pearson"))
```



```
train_data[1329,]
```

```
## TEAM CONF G W ADJOE ADJDE BARTHAG EFG_0 EFG_D TOR TORD ORB
## 1662 Holy Cross Pat 35 15 96.7 106.9 0.2398 47.9 53.2 16.8 19.6 23.1
## DRB FTR FTRD ADJ_T WAB POSTSEASON SEED YEAR TWO_P_0 TWO_P_D
## 1662 29.6 36.1 33.4 64.6 -14.5 R64 16 2016 47.2 52.8
## THREE_P_0 THREE_P_D TRNMT PS_WINS
## 1662 32.6 35.7 Yes 0
```

```
## Generalized linear mixed model fit by maximum likelihood (Adaptive
     Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
   Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
       ORB + DRB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_O +
##
##
       THREE_P_D + WAB + (1 | CONF)
##
     Data: train_data
##
                       logLik deviance df.resid
##
       AIC
                BIC
##
      613.1
              712.8
                      -287.5
                                575.1
                                           1385
##
## Scaled residuals:
##
       Min
                     Median
                                            Max
                 1Q
                                    3Q
## -11.7565 -0.2281 -0.0917 -0.0114 13.7424
## Random effects:
## Groups Name
                       Variance Std.Dev.
## CONF
           (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
                Estimate Std. Error z value Pr(>|z|)
                           7.078322
                                      2.634 0.00845 **
## (Intercept) 18.641462
## ADJOE
                0.524289
                            0.131323
                                      3.992 6.54e-05 ***
                           0.147173 -4.375 1.22e-05 ***
## ADJDE
               -0.643822
## BARTHAG
                           5.566700 -5.612 2.00e-08 ***
              -31.242596
## EFG O
                0.459814
                           0.405906
                                      1.133 0.25729
## EFG D
               -0.910582
                           0.612137 -1.488 0.13687
## TOR
               -0.178962
                           0.105983 -1.689 0.09130
## TORD
                0.149197
                           0.096552
                                      1.545 0.12229
## ORB
                0.035003
                           0.046874
                                      0.747 0.45521
## DRB
                0.009714
                           0.054970
                                      0.177
                                             0.85973
## FTR
                0.059434
                           0.027141
                                      2.190 0.02853 *
## FTRD
               -0.023435
                           0.024953 -0.939
                                             0.34766
## ADJ_T
                0.027996
                            0.036494
                                      0.767
                                              0.44300
## TWO_P_O
               -0.145603
                            0.253550
                                     -0.574 0.56579
## TWO P D
                0.535918
                            0.391769
                                      1.368 0.17133
## THREE_P_O
                            0.221848
                                     -0.533 0.59371
               -0.118350
## THREE_P_D
                0.404400
                            0.319731
                                      1.265 0.20594
## WAB
                0.554127
                            0.067668
                                      8.189 2.64e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation matrix not shown by default, as p = 18 > 12.
## Use print(x, correlation=TRUE) or
       vcov(x)
##
                     if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
```

Appendix 4.2. Model Selection

```
# Fixed Effects Test
model_binom1 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                                   # remove DRB
                      TOR + TORD + ORB + FTR + FTRD + ADJ_T +
                      TWO P O + TWO P D + THREE P O + THREE P D +
                      WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom, model_binom1)
                                                                                   # p-value: 0.8595
## Data: train_data
## Models:
## model_binom1: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model_binom1:
                    ORB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_O +
## model_binom1:
                    THREE_P_D + WAB + (1 | CONF)
## model_binom: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model_binom:
                   ORB + DRB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_O +
## model_binom:
                   THREE_P_D + WAB + (1 | CONF)
               Df
                     AIC
                           BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## model_binom1 18 611.09 705.53 -287.54
                                         575.09
## model binom 19 613.06 712.75 -287.53
                                         575.06 0.0313
                                                                   0.8595
summary(model binom1)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
    Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
  Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
      ORB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_O +
      THREE_P_D + WAB + (1 | CONF)
##
##
     Data: train_data
##
##
       AIC
                BIC
                      logLik deviance df.resid
##
                      -287.5
                                575.1
                                          1386
     611.1
              705.5
##
## Scaled residuals:
       Min 1Q Median
                                   3Q
                                           Max
## -11.6255 -0.2299 -0.0912 -0.0113 13.7483
##
## Random effects:
## Groups Name
                      Variance Std.Dev.
          (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 18.34933 6.87232 2.670 0.00758 **
## ADJOE
               0.53131
                           0.12562 4.229 2.34e-05 ***
```

ADJDE

```
## BARTHAG
              -31.27090
                           5.57122 -5.613 1.99e-08 ***
                                   1.122 0.26201
## EFG O
                           0.40445
                0.45365
## EFG D
               -0.93198
                           0.59894 -1.556 0.11970
## TOR
                           0.09768 -1.758 0.07869
               -0.17176
## TORD
                0.16007
                          0.07432
                                   2.154 0.03124 *
## ORB
                                   0.736 0.46158
               0.03182 0.04323
## FTR
               0.05903 0.02705
                                   2.182 0.02909 *
               -0.02460
                          0.02406 -1.022 0.30665
## FTRD
                                   0.756 0.44969
## ADJ_T
               0.02752
                          0.03641
## TWO_P_O
               -0.14786
                          0.25327 -0.584 0.55936
## TWO_P_D
               0.54361
                          0.38887
                                   1.398 0.16213
## THREE_P_O
                           0.22149 -0.546 0.58538
               -0.12083
## THREE_P_D
                0.41092
                          0.31715
                                   1.296 0.19509
## WAB
                0.55395
                          0.06763 8.191 2.59e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation matrix not shown by default, as p = 17 > 12.
## Use print(x, correlation=TRUE) or
##
      vcov(x)
                     if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom2 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                                 # remove THREE_P_O
                      TOR + TORD + ORB + FTR + FTRD + ADJ_T +
                      TWO_P_O + TWO_P_D + THREE_P_D +
                      WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom1, model_binom2)
                                                                                  # p-value: 0.5832
## Data: train_data
## Models:
## model_binom2: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model_binom2:
                   ORB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_D +
## model binom2:
                    WAB + (1 | CONF)
## model_binom1: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
                    ORB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_O +
## model binom1:
## model_binom1:
                    THREE_P_D + WAB + (1 | CONF)
               Df
                     AIC
                            BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## model_binom2 17 609.39 698.59 -287.69
                                         575.39
## model_binom1 18 611.09 705.53 -287.54 575.09 0.3011
                                                          1
                                                                  0.5832
summary(model_binom2)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
   Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
## Family: binomial (logit)
```

```
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
##
       ORB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_D +
##
      WAB + (1 \mid CONF)
     Data: train_data
##
##
##
       AIC
                 BIC
                       logLik deviance df.resid
      609.4
               698.6
                       -287.7
                                 575.4
##
                                           1387
##
## Scaled residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
  -11.5355 -0.2297 -0.0907 -0.0112 13.8210
##
## Random effects:
                       Variance Std.Dev.
## Groups Name
## CONF
           (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 18.21711
                            6.86923
                                    2.652 0.0080 **
## ADJOE
                0.53349
                           0.12579
                                     4.241 2.22e-05 ***
## ADJDE
                -0.63791
                            0.14232 -4.482 7.39e-06 ***
## BARTHAG
              -31.29282
                            5.58123 -5.607 2.06e-08 ***
## EFG O
                0.24236
                                     2.105
                                              0.0353 *
                            0.11515
## EFG D
               -0.93488
                            0.59985 - 1.559
                                              0.1191
                           0.09759 -1.742
## TOR
               -0.17005
                                              0.0814
## TORD
                0.16104
                            0.07416
                                     2.171
                                              0.0299 *
## ORB
                                     0.681
                0.02927
                            0.04298
                                              0.4958
## FTR
                0.05893
                            0.02702
                                    2.180
                                              0.0292 *
## FTRD
               -0.02491
                            0.02403 -1.037
                                              0.2999
## ADJ_T
                0.02777
                            0.03633
                                     0.764
                                              0.4446
## TWO_P_O
                -0.01579
                            0.07354 -0.215
                                              0.8299
## TWO_P_D
                0.54526
                            0.38953
                                    1.400
                                              0.1616
## THREE_P_D
                 0.41070
                                    1.293
                                              0.1960
                            0.31764
## WAB
                 0.55209
                            0.06744
                                    8.186 2.69e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation matrix not shown by default, as p = 16 > 12.
## Use print(x, correlation=TRUE) or
##
       vcov(x)
                     if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom3 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                                    # remove TWO_P_O
                       TOR + TORD + ORB + FTR + FTRD + ADJ_T +
                       TWO_P_D + THREE_P_D +
                       WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
```

boundary (singular) fit: see ?isSingular

```
## Data: train_data
## Models:
## model binom3: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG O + EFG D + TOR + TORD +
                    ORB + FTR + FTRD + ADJ_T + TWO_P_D + THREE_P_D + WAB + (1 |
## model_binom3:
## model_binom3:
                    CONF)
## model_binom2: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
                    ORB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D + THREE_P_D +
## model_binom2:
## model binom2:
                    WAB + (1 \mid CONF)
                            BIC logLik deviance Chisq Chi Df Pr(>Chisq)
               Df
                     AIC
## model binom3 16 607.43 691.39 -287.72
                                          575.43
## model binom2 17 609.39 698.59 -287.69 575.39 0.0462
                                                                   0.8298
summary(model_binom3)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
     Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
   Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
       ORB + FTR + FTRD + ADJ_T + TWO_P_D + THREE_P_D + WAB + (1 |
##
                                                                       CONF)
##
      Data: train_data
##
##
       AIC
                BIC
                      logLik deviance df.resid
##
      607.4
               691.4
                      -287.7
                                575.4
                                           1388
##
## Scaled residuals:
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -11.6171 -0.2299 -0.0913 -0.0113 13.7168
##
## Random effects:
                      Variance Std.Dev.
## Groups Name
           (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 18.30302
                           6.86100 2.668 0.00764 **
## ADJOE
                0.53646
                           0.12506
                                    4.290 1.79e-05 ***
## ADJDE
               -0.63877
                           0.14235 -4.487 7.21e-06 ***
## BARTHAG
              -31.37965
                           5.57055
                                   -5.633 1.77e-08 ***
## EFG O
                0.22495
                           0.08174
                                    2.752 0.00592 **
## EFG D
               -0.92798
                           0.59860 -1.550 0.12108
## TOR
               -0.17034
                           0.09759 - 1.745
                                            0.08091
## TORD
                0.15949
                           0.07378
                                    2.162 0.03065 *
## ORB
                0.02819
                           0.04266
                                    0.661 0.50866
## FTR
                0.05841
                           0.02691
                                    2.170 0.02998
## FTRD
                -0.02439
                           0.02391 -1.020 0.30783
## ADJ_T
                0.02634
                           0.03569
                                    0.738 0.46052
## TWO_P_D
                0.54016
                           0.38852
                                    1.390 0.16443
                           0.31728
                                    1.286 0.19834
## THREE_P_D
                0.40812
## WAB
                0.55267
                           0.06740 8.199 2.42e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation matrix not shown by default, as p = 15 > 12.
## Use print(x, correlation=TRUE) or
       vcov(x)
##
                     if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom4 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +</pre>
                                                                                   # remove ORB
                       TOR + TORD + FTR + FTRD + ADJ_T +
                       TWO_P_D + THREE_P_D +
                      WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom3, model_binom4)
                                                                                     # p-value: 0.5077
## Data: train_data
## Models:
## model binom4: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG O + EFG D + TOR + TORD +
## model binom4:
                  FTR + FTRD + ADJ T + TWO P D + THREE P D + WAB + (1 | CONF)
## model_binom3: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
                    ORB + FTR + FTRD + ADJ_T + TWO_P_D + THREE_P_D + WAB + (1 |
## model_binom3:
## model binom3:
                    CONF)
                     AIC
                            BIC logLik deviance Chisq Chi Df Pr(>Chisq)
               Df
## model binom4 15 605.87 684.58 -287.94 575.87
## model_binom3 16 607.43 691.39 -287.72 575.43 0.4387
                                                                   0.5077
summary(model binom4)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
   Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
## Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
##
      FTR + FTRD + ADJ_T + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
##
     Data: train_data
##
##
       AIC
                BIC logLik deviance df.resid
##
      605.9
              684.6 -287.9
                                575.9
                                          1389
##
## Scaled residuals:
                     Median
       Min
                 1Q
                                   3Q
                                           Max
## -10.6103 -0.2327 -0.0904 -0.0114 13.6077
##
## Random effects:
## Groups Name
                      Variance Std.Dev.
## CONF
          (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
```

```
##
## Fixed effects:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 17.75005 6.77933 2.618 0.00884 **
                                 4.484 7.34e-06 ***
## ADJOE
               0.55128
                        0.12296
## ADJDE
              ## BARTHAG
             -31.29170 5.55028 -5.638 1.72e-08 ***
              0.19019
                                 3.059 0.00222 **
## EFG O
                         0.06218
              -0.95654
## EFG D
                         0.59667 -1.603 0.10890
## TOR
              -0.13285 0.07933 -1.675 0.09400
## TORD
              0.17140
                         0.07141 2.400 0.01639 *
                                 2.092 0.03648 *
## FTR
               0.05566
                         0.02661
              -0.02430 0.02389 -1.017 0.30895
## FTRD
## ADJ_T
               ## TWO_P_D
                         0.38808
                                 1.408 0.15899
               0.54660
## THREE_P_D
               0.41365
                          0.31679
                                  1.306 0.19164
               0.56268
                          0.06577 8.555 < 2e-16 ***
## WAB
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation matrix not shown by default, as p = 14 > 12.
## Use print(x, correlation=TRUE) or
##
      vcov(x)
                    if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom5 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                              # remove ADJ_T
                     TOR + TORD + FTR + FTRD +
                     TWO_P_D + THREE_P_D +
                     WAB + (1 | CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom4, model_binom5)
                                                                               # p-value: 0.4698
## Data: train_data
## Models:
## model binom5: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG O + EFG D + TOR + TORD +
                   FTR + FTRD + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
## model binom5:
## model_binom4: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model_binom4:
                   FTR + FTRD + ADJ_T + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
                          BIC logLik deviance Chisq Chi Df Pr(>Chisq)
              Df
                    AIC
                                        576.40
## model_binom5 14 604.40 677.85 -288.20
## model binom4 15 605.87 684.58 -287.94
                                        575.87 0.5223
                                                               0.4698
summary(model_binom5)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
   Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
```

```
##
## Scaled residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
  -10.3533 -0.2309 -0.0920 -0.0118 12.9150
##
## Random effects:
## Groups Name
                       Variance Std.Dev.
## CONF
           (Intercept) 1.401e-17 3.743e-09
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 18.42403
                           6.72560
                                    2.739 0.00616 **
## ADJOE
                0.54672
                           0.12239
                                    4.467 7.93e-06 ***
## ADJDE
               -0.61378
                           0.13836 -4.436 9.16e-06 ***
## BARTHAG
              -31.03592
                           5.52133 -5.621 1.90e-08 ***
## EFG O
                0.19197
                           0.06204
                                     3.094 0.00197 **
## EFG D
               -0.92037
                           0.59287 -1.552 0.12057
## TOR
               -0.13512
                           0.07908 -1.709 0.08750
## TORD
                0.16674
                           0.07091
                                     2.351 0.01871 *
## FTR
                                    2.186 0.02884 *
                0.05776
                           0.02643
## FTRD
               -0.02206
                           0.02364 -0.933 0.35092
## TWO_P_D
                0.53090
                           0.38631
                                    1.374 0.16936
## THREE_P_D
                0.39836
                           0.31527
                                     1.264 0.20639
## WAB
                0.56444
                           0.06571
                                     8.590 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation matrix not shown by default, as p = 13 > 12.
## Use print(x, correlation=TRUE)
##
      vcov(x)
                     if you need it
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom6 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                                   # remove FTRD
                       TOR + TORD + FTR +
                      TWO_P_D + THREE_P_D +
                       WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom5, model_binom6)
                                                                                    # p-value: 0.3498
```

Family: binomial (logit)

677.9

Data: train_data

AIC 604.4

##

##

##

##

Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +

576.4

1390

FTR + FTRD + TWO_P_D + THREE_P_D + WAB + (1 | CONF)

BIC logLik deviance df.resid

-288.2

```
## Data: train_data
## Models:
## model binom6: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG O + EFG D + TOR + TORD +
                  FTR + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
## model binom6:
## model_binom5: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model binom5:
                    FTR + FTRD + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
                            BIC logLik deviance Chisq Chi Df Pr(>Chisq)
                     AIC
## model binom6 13 603.27 671.48 -288.63
                                         577.27
## model binom5 14 604.40 677.85 -288.20
                                          576.40 0.8743
                                                                  0.3498
summary(model_binom6)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
    Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
##
  Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
##
      FTR + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
##
     Data: train_data
##
##
       AIC
                BIC
                      logLik deviance df.resid
     603.3
                      -288.6
                                577.3
##
              671.5
                                          1391
##
## Scaled residuals:
       Min
                 1Q
                     Median
                                   3Q
## -11.0055 -0.2310 -0.0925 -0.0118 13.3267
##
## Random effects:
## Groups Name
                      Variance Std.Dev.
## CONF
          (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 18.86651
                          6.70974
                                   2.812 0.004926 **
## ADJOE
                           0.12262
                                   4.401 1.08e-05 ***
                0.53968
## ADJDE
               -0.62169
                           0.13858 -4.486 7.25e-06 ***
## BARTHAG
              -31.02780
                          5.53379 -5.607 2.06e-08 ***
## EFG O
                0.20306
                          0.06071
                                   3.345 0.000823 ***
## EFG D
                           0.58760 -1.449 0.147414
               -0.85127
## TOR
               -0.14438
                          0.07861 -1.837 0.066283
## TORD
                0.13618
                          0.06284
                                   2.167 0.030230 *
## FTR
                0.05514
                           0.02624
                                   2.102 0.035568 *
                0.49529
                           0.38412 1.289 0.197254
## TWO_P_D
## THREE_P_D
                0.36740
                           0.31325 1.173 0.240838
## WAB
                0.57073
                           0.06531 8.739 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
            (Intr) ADJOE ADJDE BARTHA EFG_O EFG_D TOR
                                                            TORD
##
                                                                   FTR
## ADJOE
             0.422
## ADJDE
            -0.701 -0.877
## BARTHAG -0.620 -0.938 0.942
```

0.215 0.047 -0.313 -0.201

EFG O

```
## EFG D
             0.123 0.029 -0.073 -0.048 0.013
## TOR
            -0.487 -0.064 0.248 0.165 -0.328 -0.054
## TORD
            -0.406 0.119 0.114 -0.007 -0.050 -0.189 0.052
## FTR
             0.056  0.132  -0.232  -0.155  0.302  0.120  -0.361  -0.087
## TWO P D
           -0.108 -0.049 0.056 0.055 -0.014 -0.990 0.057 0.130 -0.103
## THREE P D -0.125 -0.060 0.066 0.060 0.001 -0.981 0.048 0.151 -0.114
             0.105 -0.094 0.063 -0.122 -0.093 -0.025 0.184 -0.042 -0.163
## WAB
##
            TWO_P_ THREE_
## ADJOE
## ADJDE
## BARTHAG
## EFG_O
## EFG_D
## TOR
## TORD
## FTR
## TWO_P_D
## THREE_P_D 0.976
## WAB
             0.040 0.050
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom7 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                                    # remove THREE P D
                       TOR + TORD + FTR +
                       TWO_P_D +
                       WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom6, model_binom7)
                                                                                     # p-value: 0.2336
## Data: train_data
## Models:
## model_binom7: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model_binom7:
                    FTR + TWO_P_D + WAB + (1 | CONF)
## model_binom6: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model_binom6:
                    FTR + TWO_P_D + THREE_P_D + WAB + (1 | CONF)
                            BIC logLik deviance Chisq Chi Df Pr(>Chisq)
               Df
                     AIC
## model binom7 12 602.69 665.65 -289.34
## model_binom6 13 603.27 671.48 -288.63
                                           577.27 1.4189
                                                                    0.2336
summary(model_binom7)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
     Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
  Family: binomial (logit)
##
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
      FTR + TWO_P_D + WAB + (1 | CONF)
##
##
     Data: train_data
##
##
       AIC
                BIC
                      logLik deviance df.resid
##
     602.7
              665.7 -289.3
                                578.7
                                           1392
```

```
##
## Scaled residuals:
                     Median
       Min
                 1Q
## -11.1463 -0.2323 -0.0930 -0.0119 12.7045
## Random effects:
                      Variance Std.Dev.
## Groups Name
## CONF
          (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 19.91828
                           6.64579
                                   2.997 0.002725 **
## ADJOE
                                   4.475 7.63e-06 ***
                0.54984
                           0.12286
## ADJDE
                           0.13858 -4.576 4.73e-06 ***
               -0.63418
## BARTHAG
              -31.50604
                           5.54004 -5.687 1.29e-08 ***
## EFG_O
                           0.06060
                                   3.360 0.000779 ***
                0.20360
## EFG D
               -0.17737
                           0.11311 -1.568 0.116839
## TOR
                           0.07833 -1.904 0.056949
               -0.14911
## TORD
                0.12484
                           0.06171
                                   2.023 0.043084 *
## FTR
                0.05872
                          0.02608
                                   2.251 0.024373 *
## TWO P D
                0.05760
                           0.08315
                                   0.693 0.488483
                0.56843
                           0.06538
                                   8.694 < 2e-16 ***
## WAB
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
          (Intr) ADJOE ADJDE BARTHA EFG_O EFG_D TOR
                                                          TORD
                                                                 FTR
## ADJOE
           0.418
## ADJDE
          -0.699 -0.877
## BARTHAG -0.617 -0.938 0.942
## EFG_0
           0.216 0.049 -0.315 -0.202
## EFG_D
           0.005 -0.157 -0.045 0.059 0.074
## TOR
          -0.486 -0.063 0.246 0.163 -0.327 -0.039
## TORD
          -0.391 0.135 0.100 -0.022 -0.051 -0.218 0.048
## FTR
           0.040 0.127 -0.225 -0.148 0.305 0.045 -0.359 -0.067
## TWO P D 0.061 0.047 -0.038 -0.019 -0.071 -0.760 0.049 -0.075 0.032
## WAB
           0.115 -0.089 0.059 -0.127 -0.091 0.122 0.181 -0.052 -0.162
##
          TWO_P_
## ADJOE
## ADJDE
## BARTHAG
## EFG O
## EFG_D
## TOR
## TORD
## FTR
## TWO_P_D
## WAB
          -0.042
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom8 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D +
                                                                                  # remove TWO P D
                TOR + TORD + FTR +
```

```
WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom7, model_binom8)
                                                                                    # p-value: 0.488
## Data: train_data
## Models:
## model_binom8: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model binom8:
                    FTR + WAB + (1 | CONF)
## model_binom7: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model binom7:
                    FTR + TWO P D + WAB + (1 | CONF)
                            BIC logLik deviance Chisq Chi Df Pr(>Chisq)
##
               Df
                     AIC
## model_binom8 11 601.17 658.89 -289.58
                                          579.17
## model binom7 12 602.69 665.65 -289.34
                                          578.69 0.4809
                                                                    0.488
summary(model_binom8)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
    Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
## Family: binomial ( logit )
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
##
      FTR + WAB + (1 | CONF)
##
     Data: train_data
##
##
                BIC
       AIC
                     logLik deviance df.resid
     601.2
              658.9
                     -289.6
                                579.2
##
                                          1393
##
## Scaled residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -11.3517 -0.2339 -0.0917 -0.0122 12.8717
##
## Random effects:
## Groups Name
                      Variance Std.Dev.
## CONF
          (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 19.66107
                           6.62576
                                   2.967 0.00300 **
## ADJOE
                           0.12276
                                    4.452 8.49e-06 ***
                0.54657
## ADJDE
               -0.63132
                           0.13839 -4.562 5.07e-06 ***
## BARTHAG
              -31.46860
                           5.53863 -5.682 1.33e-08 ***
## EFG O
                0.20675
                           0.06041
                                     3.423 0.00062 ***
## EFG_D
               -0.11798
                           0.07350 -1.605 0.10849
## TOR
               -0.15195
                           0.07826 -1.942 0.05220
## TORD
                0.12805
                           0.06147
                                    2.083 0.03723 *
## FTR
                0.05821
                           0.02604
                                     2.235 0.02542 *
## WAB
                0.57075
                           0.06525
                                     8.747 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Correlation of Fixed Effects:
          (Intr) ADJOE ADJDE BARTHA EFG_O EFG_D TOR
## ADJOE
          0.416
## ADJDE
          -0.697 -0.877
## BARTHAG -0.616 -0.939 0.942
## EFG O
          0.220 0.050 -0.316 -0.202
          0.076 -0.187 -0.113 0.069 0.033
## EFG D
## TOR
          -0.490 -0.062 0.245 0.161 -0.324 -0.001
## TORD
         -0.386   0.142   0.094   -0.027   -0.057   -0.424   0.053
## FTR
          ## WAB
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom9 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O +</pre>
                                                                                # remove EFG_D
                     TOR + TORD + FTR +
                     WAB + (1 | CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom8, model_binom9)
                                                                                # p-value: 0.108
## Data: train_data
## Models:
## model_binom9: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + TORD + FTR +
## model binom9:
                   WAB + (1 \mid CONF)
## model_binom8: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR + TORD +
## model binom8:
                   FTR + WAB + (1 | CONF)
                           BIC logLik deviance Chisq Chi Df Pr(>Chisq)
##
               Df
                    AIC
## model_binom9 10 601.75 654.22 -290.88
                                        581.75
## model_binom8 11 601.17 658.89 -289.58 579.17 2.5831
                                                         1
                                                                 0.108
summary(model binom9)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
    Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
## Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + TORD + FTR +
##
     WAB + (1 | CONF)
##
     Data: train_data
##
##
       AIC
               BIC
                     logLik deviance df.resid
##
     601.8
                     -290.9
                              581.8
              654.2
                                        1394
##
## Scaled residuals:
                    Median
                1Q
## -10.1205 -0.2348 -0.0951 -0.0122 11.4464
##
## Random effects:
## Groups Name
                     Variance Std.Dev.
## CONF
          (Intercept) 0
```

```
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 20.55090
                          6.54723
                                 3.139 0.001696 **
                                 4.277 1.89e-05 ***
## ADJOE
               0.51194
                          0.11968
## ADJDE
                         0.13594 -4.850 1.23e-06 ***
              -0.65937
## BARTHAG
                         5.47869 -5.656 1.55e-08 ***
             -30.98621
                                  3.508 0.000451 ***
## EFG O
               0.21105
                         0.06016
## TOR
              -0.15231
                         0.07781 -1.957 0.050299 .
## TORD
               0.08614
                         0.05538 1.555 0.119845
                                 2.436 0.014846 *
## FTR
               0.06296
                          0.02584
## WAB
               0.58789
                          0.06464 9.095 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
          (Intr) ADJOE ADJDE BARTHA EFG_O TOR
                                                 TORD
                                                      FTR
          0.430
## ADJOE
## ADJDE
          -0.689 -0.919
## BARTHAG -0.618 -0.944 0.957
## EFG O
          0.212 0.050 -0.309 -0.196
          -0.487 -0.053 0.237 0.151 -0.320
## TOR
## TORD
          -0.391 0.075 0.049 0.001 -0.053 0.056
## FTR
          ## WAB
          ## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom10 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_0 +
                                                                                # remove TORD
                     TOR + FTR +
                     WAB + (1 | CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom9, model_binom10)
                                                                                # p-value: 0.1183
## Data: train_data
## Models:
## model_binom10: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + FTR + WAB + (1 |
## model binom10:
                    CONF)
## model_binom9: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + TORD + FTR +
## model_binom9:
                   WAB + (1 | CONF)
               Df
                     AIC
                           BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## model_binom10 9 602.19 649.42 -292.10
                                        584.19
## model binom9 10 601.75 654.22 -290.88
                                        581.75 2.4394
                                                                0.1183
summary(model_binom10)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
   Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
## Family: binomial (logit)
```

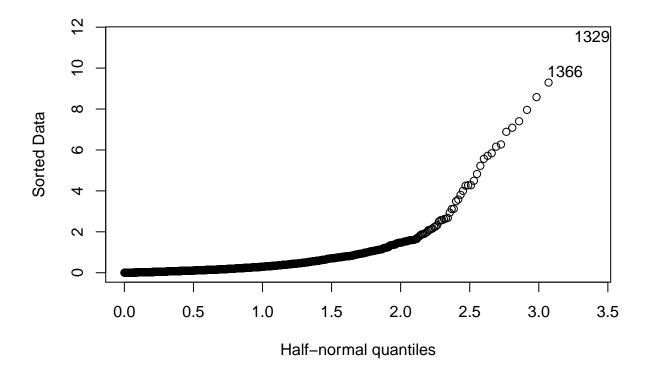
```
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + FTR + WAB + (1 |
##
      CONF)
##
      Data: train_data
##
##
       AIC
                BIC
                      logLik deviance df.resid
                      -292.1
                                584.2
##
      602.2
              649.4
                                           1395
##
## Scaled residuals:
##
      Min
               1Q Median
                               3Q
## -9.2942 -0.2370 -0.0964 -0.0121 11.5546
## Random effects:
## Groups Name
                       Variance Std.Dev.
## CONF
           (Intercept) 0
## Number of obs: 1404, groups: CONF, 33
##
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
                           5.99824
                                    4.107 4.01e-05 ***
## (Intercept) 24.63257
## ADJOE
                0.50122
                           0.11901
                                     4.212 2.54e-05 ***
## ADJDE
               -0.67338
                           0.13582 -4.958 7.12e-07 ***
## BARTHAG
              -31.15990
                           5.46624 -5.700 1.20e-08 ***
                                    3.611 0.000305 ***
## EFG_0
                0.21664
                           0.06000
               -0.15942
                           0.07783 -2.048 0.040528 *
## TOR
## FTR
                0.06424
                           0.02585 2.485 0.012963 *
## WAB
                0.59009
                           0.06424
                                    9.186 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Correlation of Fixed Effects:
##
           (Intr) ADJOE ADJDE BARTHA EFG_O TOR
## ADJOE
           0.502
## ADJDE
          -0.731 -0.926
## BARTHAG -0.672 -0.947 0.958
## EFG O
           0.224 0.063 -0.319 -0.208
## TOR
          -0.503 -0.055 0.234 0.148 -0.324
## FTR
           0.025  0.150  -0.215  -0.154  0.308  -0.364
## WAB
           0.115 -0.060 0.074 -0.142 -0.104 0.192 -0.186
## convergence code: 0
## boundary (singular) fit: see ?isSingular
model_binom11 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_0 + FTR +
                                                                                     # remove TOR
                      WAB + (1 CONF), nAGQ = 25, family = "binomial", train_data)
## boundary (singular) fit: see ?isSingular
anova(model_binom10, model_binom11)
                                                                                      # p-value: 0.038
## Data: train_data
## Models:
## model_binom11: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + FTR + WAB + (1 | CONF)
## model_binom10: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + FTR + WAB + (1 |
## model_binom10:
                     CONF)
```

```
AIC
                             BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## model_binom11 8 604.46 646.44 -294.23
                                          588.46
                                          584.19 4.2679
                                                                  0.03884 *
## model binom10 9 602.19 649.42 -292.10
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
summary(model_binom11)
## Generalized linear mixed model fit by maximum likelihood (Adaptive
    Gauss-Hermite Quadrature, nAGQ = 25) [glmerMod]
  Family: binomial (logit)
## Formula: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + FTR + WAB + (1 | CONF)
##
     Data: train_data
##
##
       AIC
                BIC
                      logLik deviance df.resid
##
     604.5
              646.4
                      -294.2
                                588.5
##
## Scaled residuals:
               1Q Median
      Min
                               3Q
## -8.6476 -0.2347 -0.0981 -0.0134 14.6925
##
## Random effects:
## Groups Name
                      Variance Std.Dev.
## CONF
           (Intercept) 0
                               0
## Number of obs: 1404, groups: CONF, 33
## Fixed effects:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 18.63127 5.13393 3.629 0.000284 ***
## ADJOE
                0.49358
                           0.11701 4.218 2.46e-05 ***
## ADJDE
                           0.12965 -4.744 2.10e-06 ***
               -0.61506
## BARTHAG
              -29.79642
                           5.32158 -5.599 2.15e-08 ***
## EFG_0
                0.17765
                          0.05667
                                   3.135 0.001720 **
                0.04517
                           0.02392
                                   1.888 0.058973 .
## FTR
## WAB
                0.61936
                           0.06310
                                   9.815 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##
          (Intr) ADJOE ADJDE BARTHA EFG_O FTR
## ADJOE
           0.538
          -0.724 -0.939
## ADJDE
## BARTHAG -0.692 -0.949 0.960
## EFG_O
           0.068 0.040 -0.260 -0.164
## FTR
           -0.210 0.136 -0.137 -0.104 0.215
           0.259 -0.047 0.026 -0.182 -0.049 -0.125
## WAB
## convergence code: 0
## boundary (singular) fit: see ?isSingular
# Random Effects
model_binom12 <- glmer(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O +</pre>
                                                                                    \# REML = F
                      TOR + FTR +
                      WAB + (1 CONF), REML = FALSE, family = "binomial", train_data)
```

```
## Warning: extra argument(s) 'REML' disregarded
## boundary (singular) fit: see ?isSingular
model_binom13 <- glm(TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O +
                                                                                      # remove CONF
                       TOR + FTR +
                       WAB, family = "binomial", train_data)
anova(model_binom12, model_binom13)
                                                                                      # p-value: 1
## Data: train_data
## Models:
## model_binom13: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + FTR + WAB
## model_binom12: TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR + FTR + WAB + (1 |
## model_binom12:
                     CONF)
##
                 Df
                       AIC
                              BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## model_binom13 8 600.19 642.17 -292.1
                                           584.19
## model_binom12 9 602.19 649.42 -292.1
                                           584.19
                                                             1
summary(model binom13)
##
## Call:
## glm(formula = TRNMT ~ ADJOE + ADJDE + BARTHAG + EFG_O + TOR +
      FTR + WAB, family = "binomial", data = train_data)
##
##
## Deviance Residuals:
       Min
##
                   1Q
                        Median
                                       3Q
                                                Max
## -2.99008 -0.33058 -0.13608 -0.01713
                                            3.13102
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) 24.63257
                           5.95394
                                    4.137 3.52e-05 ***
## ADJOE
                0.50122
                            0.11747
                                     4.267 1.98e-05 ***
## ADJDE
               -0.67338
                           0.13383 -5.032 4.86e-07 ***
                           5.39211 -5.779 7.52e-09 ***
## BARTHAG
              -31.15990
## EFG_0
                0.21664
                           0.05992
                                    3.616
                                              0.0003 ***
## TOR
               -0.15942
                            0.07778 - 2.050
                                              0.0404 *
                0.06424
                            0.02584
                                    2.486
                                             0.0129 *
## FTR
## WAB
                 0.59009
                            0.06423
                                    9.187 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1380.38 on 1403 degrees of freedom
## Residual deviance: 584.19 on 1396 degrees of freedom
## AIC: 600.19
## Number of Fisher Scoring iterations: 7
```

Appendix 4.3. Post Diagnostic Checks

```
# Check Diagnostics
halfnorm(resid(model_binom13, type="pearson"))
```



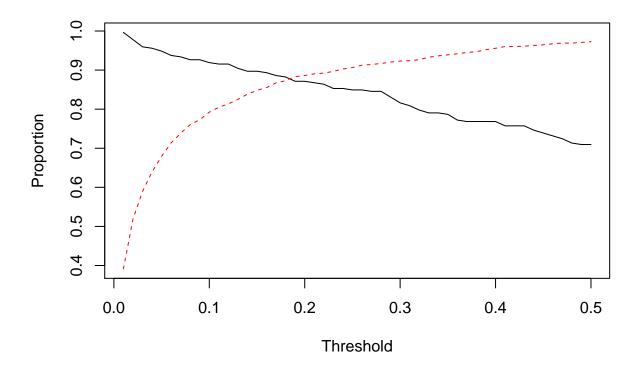
```
sort(faraway::vif(train_data[,c(5:8, 10, 14, 17)]))
### FTR TOR EFG_0 WAB ADJDE ADJOE BARTHAG
## 1.174302 1.849976 2.771205 11.270400 14.118669 19.035144 36.023259
```

Appendix 4.4. Prediction

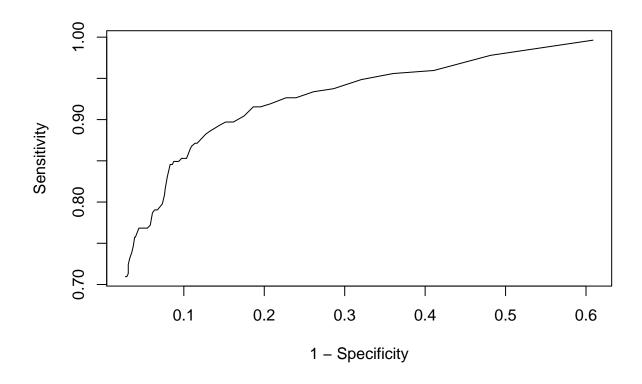
```
# Checking Performance
predprob=predict(model_binom13, train_data, type="response")

thresh <- seq(0.01,0.5,0.01)
Sensitivity <- numeric(length(thresh))
Specificity <- numeric(length(thresh))
for(j in seq(along=thresh)){
    pp <- ifelse(predprob < thresh[j],"No","Yes")
    xx <- xtabs( ~ train_data$TRNMT + pp)
    Specificity[j] <- xx[1,1]/(xx[1,1]+xx[1,2])</pre>
```

```
Sensitivity[j] <- xx[2,2]/(xx[2,1]+xx[2,2])
}
matplot(thresh,cbind(Sensitivity,Specificity),type="l",xlab="Threshold",ylab="Proportion",lty=1:2)</pre>
```



```
plot(1-Specificity, Sensitivity, type="l")
abline(0,1,lty=2)
```



```
# Classification: Sensitivity and Specificity (ROC)
predout=ifelse(predprob < 0.18, "No", "Yes")</pre>
xtabs( ~ train_data$TRNMT + predout)
##
                   predout
## train_data$TRNMT No Yes
                No 988 144
##
##
                Yes 32 240
# Training Error classification rate
1-(988+240)/(988+240+144+32)
## [1] 0.1253561
# Testing Error classification rate
predprob_test=predict(model_binom10, test_data_19, type="response")
predout_test=ifelse(predprob_test < 0.18, "No", "Yes")</pre>
xtabs( ~ test_data_19$TRNMT + predout_test)
##
                     predout_test
## test_data_19$TRNMT
                       No Yes
##
                      247 38
                  No
##
                        7 61
                  Yes
```

1-(247+61)/(247+61+7+38)

[1] 0.1274788

Appendix 5. Model 2: Multinomial Model - All possibilities

Appendix 5.1. Prediction

```
summary(mmod1)
## Call:
```

```
multinom(formula = POSTSEASON ~ ADJOE + ADJDE + BARTHAG + EFG_O +
       EFG_D + TOR + TWO_P_O + WAB, data = train_data, trace = FALSE)
##
##
## Coefficients:
##
             (Intercept)
                             ADJOE
                                        ADJDE
                                                BARTHAG
                                                               EFG O
## R68
               22.36917 0.6930545 -0.6387554 -35.55184
                                                         0.10514273
## R64
               20.05135 0.3591553 -0.4764981 -25.62416
                                                         0.18339258
## R32
                43.97908 0.4799637 -0.7631146 -29.61770
## S16
               -25.97634 0.2539697 -0.3535155 24.02096 -0.16766864
## E8
                25.74885 0.5936211 -0.9496349 -25.40841 -0.40395542
## F4
                31.32057 0.7035848 -1.1607442 -31.56321
                                                         0.51679491
## 2ND
                38.68386 1.5249836 -1.8073067 -14.92299 -4.01741403
## Champions
               -26.29208 4.2496101 -5.5472676 -91.10589 -3.70585699
##
                   EFG_D
                                 TOR
                                           TWO_P_0
             -0.36310116 -0.20504637
## R68
                                      0.0856522551
                                                    0.3284524
## R64
             -0.03428303 -0.04884582 -0.0006071909
                                                    0.6555698
## R32
            -0.08257088 -0.38844792 0.2031092296
                                                    0.7157722
## S16
              0.07755960 -0.14868146 0.3246490619
                                                    0.6036942
## E8
              0.17909511 -0.28493369 0.6690769352
                                                    0.8535485
## F4
              0.05044687
                         0.22295890 -0.1748514197
                                                   0.5565037
             -0.42421579 -3.52135155 4.7837766041 -0.0726802
## 2ND
  Champions 3.37708666 0.62909477 2.9240761169 -1.2029202
##
## Std. Errors:
##
                              ADJOE
                                         ADJDE
                                                  BARTHAG
             (Intercept)
## R68
              0.24180881 0.07939885 0.08769994 0.71626161 0.2176209
## R64
              1.74444597 0.07222554 0.05875595 2.26236503 0.0995162
              2.19415373\ 0.09344604\ 0.08559134\ 3.07789830\ 0.1635410
## R32
## S16
              1.09455542 0.09604182 0.12575847 1.02116845 0.2265747
## E8
              0.32485850 0.12335647 0.16585797 0.33350867 0.3171549
## F4
              0.10823782 0.15291949 0.21733239 0.12743699 0.3413094
              0.04078992 0.41198906 0.59784005 0.03145736 1.3029543
## 2ND
## Champions 0.04017241 0.92960089 1.48949074 0.04935019 1.3030123
##
                  EFG D
                               TOR
                                     TWO_P_O
## R68
             0.15506872 0.13954521 0.1670340 0.13315705
## R64
             0.07314185 0.06981779 0.0760650 0.06980336
             0.11333051 0.10913873 0.1265307 0.10697108
## R32
## S16
            0.14700707 0.13881999 0.1784446 0.13511803
```

```
## E8
              0.19966822 0.20043210 0.2589957 0.18736637
## F4
              0.23504649 \ 0.27781350 \ 0.2728535 \ 0.21217333
## 2ND
             0.64280916 1.07712118 1.4243489 0.45968890
## Champions 1.38532950 0.91461645 1.1864221 1.38636168
## Residual Deviance: 1142.137
## AIC: 1286.137
# Train Error
mmod1.pred <- predict(mmod1, train_data)</pre>
mmod1.table <- table(mmod1.pred, train_data[,"POSTSEASON"])</pre>
mmod1.error <- numeric(dim(mmod1.table)[1])</pre>
for(i in 1:dim(mmod1.table)[1]){
  mmod1.error[i] = round(((1-(mmod1.table[i,i]))/(sum(mmod1.table[,i])))*100), 4)
mmod1.error.table <- data.frame(names(mmod1.table[,1]), mmod1.error)</pre>
colnames(mmod1.error.table) <- c("Round", "% Error")</pre>
# Test Error
mmod1.pred.test <- predict(mmod1, test_data_19)</pre>
mmod1.table.test <- table(mmod1.pred.test, test_data_19[,"POSTSEASON"])</pre>
mmod1.error.test <- numeric(dim(mmod1.table.test)[1])</pre>
for(i in 1:dim(mmod1.table.test)[1]){
  mmod1.error.test[i] = round(((1-(mmod1.table.test[i,i])/(sum(mmod1.table.test[,i])))*100), 4)
mmod1.error.test.table <- data.frame(names(mmod1.table.test[,1]), mmod1.error.test)</pre>
colnames(mmod1.error.test.table) <- c("Round", "% Error")</pre>
```

Appendix 5.2. Error Tables (%)

```
knitr::kable(mmod1.error.table)
```

Round	% Error
No Tournament	1.5901
R68	100.0000
R64	65.6250
R32	54.6875
S16	78.1250
E8	68.7500
F4	100.0000
2ND	0.0000
Champions	0.0000

knitr::kable(mmod1.error.test.table)

Round	% Error
No Tournament	1.7544
R68	100.0000

Round	% Error
R64	75.0000
R32	75.0000
S16	75.0000
E8	75.0000
F4	100.0000
2ND	100.0000
Champions	100.0000

Appendix 6. Model 3: Multinomial Model - Round Selection Given Already in Tournament

Appendix 6.1. Prediction

```
summary(mmod3)
```

```
## Call:
## multinom(formula = POSTSEASON ~ ADJOE + ADJDE + TOR + ORB + DRB +
      TWO_P_O + THREE_P_D, data = train_given_trnmt, trace = FALSE)
##
## Coefficients:
                                     ADJDE
                                                TOR
                                                         ORB
                                                                    DRB
##
            (Intercept)
                            ADJOE
## Champions -236.056663 2.852387 2.555557 11.78722 -2.025824 -1.3480990
## E8
               8.900188 -2.173893 5.519055 19.74867 -2.692411
                                                              1.0909452
## F4
               3.967330 -1.924539 5.569355 20.86565 -3.114750
                                                              1.3208299
## R32
              15.016957 -2.274593 5.875645 19.84169 -2.725084
              -8.026639 -2.307673 6.205060 20.28381 -2.765259
## R64
                                                              0.7592421
## R68
             -25.960280 -2.152685 6.488939 20.72191 -2.997752
             -11.220968 -2.103083 5.802243 20.07609 -2.719376
## S16
              TWO P O THREE P D
## Champions -6.599466 -1.821630
            -7.732776 -2.242833
## F.8
## F4
            -8.075189 -2.994908
## R32
            -8.013475 -2.467972
## R64
            -8.209898 -2.358930
## R68
            -8.396799 -3.068424
            -8.022214 -2.227293
## S16
##
## Std. Errors:
##
            (Intercept)
                            ADJOE
                                      ADJDE
                                                  TOR
                                                           ORB
                                                                    DRB
## Champions 0.18694932 1.3967303 1.5390742 3.6535538 0.6854387 1.090490
             0.44581638 0.8797126 0.8448868 0.5426949 0.6486490 1.168592
## F.8
## F4
             ## R32
             3.50710706 0.8794955 0.8478554 0.5219588 0.6466125 1.170012
## R64
             4.00974955 0.8798437 0.8484075 0.5212229 0.6472330 1.170833
## R68
             0.74323733  0.8820179  0.8511628  0.5477912  0.6548939  1.176055
```

```
## S16
              0.25546310 0.8796789 0.8476393 0.5272317 0.6467417 1.170386
##
              TWO_P_O THREE_P_D
## Champions 1.141480 1.913517
             1.078119 1.338540
## E8
## F4
             1.085946 1.367293
## R32
             1.076049 1.340593
## R64
             1.076647 1.341498
             1.084958 1.356640
## R68
## S16
             1.077323 1.340915
##
## Residual Deviance: 538.46
## AIC: 650.46
# Train Error
mmod3.pred <- predict(mmod3, train_given_trnmt)</pre>
mmod3.table <- table(mmod3.pred, train_given_trnmt[,"POSTSEASON"])</pre>
mmod3.error <- numeric(dim(mmod3.table)[1])</pre>
for(i in 1:dim(mmod3.table)[1]){
 mmod3.error[i] = round(((1-(mmod3.table[i,i])/(sum(mmod3.table[,i])))*100), 4)
mmod3.error.table <- data.frame(names(mmod3.table[,1]), mmod3.error)</pre>
colnames(mmod3.error.table) <- c("Round", "% Error")</pre>
# Test Error
mmod3.pred.test <- predict(mmod3, test_given_trnmt_19)</pre>
mmod3.table.test <- table(mmod3.pred.test, test_given_trnmt_19[,"POSTSEASON"])
mmod3.error.test <- numeric(dim(mmod3.table.test)[1])</pre>
for(i in 1:dim(mmod3.table.test)[1]){
 mmod3.error.test[i] = round(((1-(mmod3.table.test[i,i])/(sum(mmod3.table.test[,i])))*100), 4)
}
mmod3.error.test.table <- data.frame(names(mmod3.table.test[,1]), mmod3.error.test)
colnames(mmod3.error.test.table) <- c("Round", "% Error")</pre>
```

Appendix 6.2. Error Tables (%)

knitr::kable(mmod3.error.table)

Round	% Error
2ND	0.0000
Champions	0.0000
E8	75.0000
F4	75.0000
R32	53.1250
R64	13.2812
R68	81.2500
S16	75.0000

```
knitr::kable(mmod3.error.test.table)
```

Round	% Error
2ND	100.0
Champions	0.0
E8	75.0
F4	100.0
R32	50.0
R64	25.0
R68	50.0
S16	62.5

Appendix 7. Model 4: Classification Tree - All possibilities

```
# Bagging
bag.cbb <- randomForest(POSTSEASON ~ ADJOE + ADJDE + BARTHAG + EFG O + EFG D + TOR +
                   TORD + ORB + DRB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D +
                   THREE_P_O + THREE_P_D + WAB + CONF, train_data, mtry=18, importance=T)
bag.cbb
##
## Call:
    randomForest(formula = POSTSEASON ~ ADJOE + ADJDE + BARTHAG +
                                                                         EFG_O + EFG_D + TOR + TORD + ORB
##
                  Type of random forest: classification
##
                        Number of trees: 500
## No. of variables tried at each split: 18
           OOB estimate of error rate: 15.81%
##
## Confusion matrix:
                 No Tournament R68 R64 R32 S16 E8 F4 2ND Champions
## No Tournament
                                              0
                                                 0
                         1114
                                  0
                                     16
                                          2
                                                         0
                                                                   0
## R68
                             13
                                  0
                                      3
                                          0
                                              0
                                                 0
                                                         0
                                                                   0
                                  0
                                     45
                                              3
                                                 0
                                                        0
                                                                   0
## R64
                             68
                                         12
                                                    Λ
## R32
                             12
                                  0
                                     21
                                         17
                                             10
                                                 3
                                                    0
                                                        0
## S16
                                      5
                                         17
                                              4
                                                 3
                                                        0
                              3
                                  0
                                                    Ω
                                                                   0
## E8
                              0
                                  0
                                          5
                                              4
                                                 2
                                                        0
                                                                   0
                                          3
                                              2
                                                 0
                                                    0
                                                        0
## F4
                                  0
                                      1
                                                                   1
                              1
## 2ND
                                              0
                                                 2
                                                    0
                                                                   1
  Champions
                              0
                                  0
                                      0
                                          3
                                              0
                                                 1
                                                        0
                                                                   0
##
                 class.error
## No Tournament 0.01590106
## R68
                  1.00000000
## R64
                  0.64843750
## R32
                  0.73437500
## S16
                  0.87500000
## E8
                  0.87500000
## F4
                  1.00000000
## 2ND
                  1.00000000
## Champions
                  1.00000000
importance(bag.cbb)
##
             No Tournament
                                    R68
                                                 R64
                                                              R32
                                                                         S16
                                         -5.02668979
## ADJOE
               15.67835597 -0.93312258
                                                      1.74994572 1.9153305
## ADJDE
                6.62177339 -1.77410628
                                         -0.32637798
                                                      4.41255190 -2.7950529
## BARTHAG
               20.76796719 -0.62667335 -15.00950552
                                                     2.50311592 16.3233098
## EFG_O
                7.50099642
                            0.62936560
                                          3.13095180 -3.87104401 -0.4123208
## EFG_D
                                         -1.17847550 0.65810438 -4.2414247
               12.41735393 -1.95194898
## TOR
               13.68030969 0.86712456
                                         -4.95771879 9.75086054 -6.8194483
                2.34339108 2.15681669
## TORD
                                        -2.14922398 1.90159055 3.5940922
## ORB
                7.96752682
                           1.99407970
                                          1.52415853 -0.07218137 -3.1188850
## DRB
                4.65633047 2.44619065
                                          1.74733567 -0.40556357 -1.4609951
                                          1.39771949 -0.58548431 -3.2252597
## FTR
                9.67861176 1.34458587
```

FTRD

```
## ADJ T
             ## TWO P O
                                   2.82041888 -2.80555642 2.7055801
             12.72989310 -0.12847545
## TWO P D
             6.20676578 1.66986811 -0.20670393 2.23140896 -4.3055149
## THREE_P_O
             5.16366544 0.93853795
                                   4.23366027 -1.67706769 -2.6315510
## THREE P D
             ## WAB
## CONF
             18.45531021 -0.04121671
                                   5.29678822 0.46241115 -0.4153374
##
                   F.8
                              F4
                                        2ND
                                             Champions
## ADJOE
           -1.38123177 -0.09835262 0.09491665 4.42659843
## ADJDE
           -0.74821533 -0.42107688 0.63662149 1.32177554
## BARTHAG
          10.42552909 3.17357304 4.01277893 9.83209996
## EFG_O
           1.93531756 -1.15585603 0.41215169 1.12256457
## EFG D
            0.20771086 1.21446542 0.00000000 0.57226487
## TOR
           -0.07533205 -0.73280281 2.85994166 -0.06984337
## TORD
           0.31953933 -0.23250785 -0.57754282 0.10425834
## ORB
            0.59151758 1.19667218 -1.41705050 0.21321041
## DRB
           -2.18508589 1.73833842 1.29315150 -1.96874808
## FTR
           1.63320920 -0.63120036 -1.00100150 -1.61006779
## FTRD
           -1.33592151 0.87216244 -0.82255090 0.70892831
## ADJ T
           ## TWO_P_O
            4.24148103 -3.30867967 0.33337038 1.06185543
## TWO P D
          -1.40692092 -2.18721555 -1.00100150 -1.69640277
## THREE_P_O -0.50020436 1.76204510 -0.83262693 -1.28313261
## THREE P D -0.75966210 2.09465131 -1.88327385 0.00000000
## WAB
           17.23814775 3.48497671 3.64339626 9.07836966
## CONF
            1.79054694 1.29321837 0.21822828 0.55973710
##
           MeanDecreaseAccuracy MeanDecreaseGini
## ADJOE
                     15.191981
                                    13.583919
## ADJDE
                                    10.779949
                      6.612711
## BARTHAG
                     21.623182
                                    33.626511
## EFG O
                      7.323086
                                    10.002384
## EFG_D
                     11.909420
                                     9.436318
## TOR
                     12.977863
                                    15.972846
## TORD
                     2.459812
                                    15.275153
## ORB
                     7.233455
                                    17.196017
## DRB
                     4.235551
                                    14.382168
## FTR
                     8.232703
                                    18.120075
## FTRD
                                    16.901478
                     11.321849
## ADJ T
                     -1.394040
                                    14.341741
## TWO_P_O
                     12.962444
                                    13.288670
## TWO P D
                     5.454263
                                    10.819950
## THREE P O
                                    14.893252
                     5.051946
## THREE P D
                     13.011488
                                    16.129329
## WAB
                     98.339254
                                    184.488331
## CONF
                     18.509861
                                    46.594871
# Random Forest
rf.cbb <- randomForest(POSTSEASON ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR +
                 TORD + ORB + DRB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D +
                 THREE_P_O + THREE_P_D + WAB + CONF, train_data, importance=T)
rf.cbb
##
```

Call:

```
randomForest(formula = POSTSEASON ~ ADJOE + ADJDE + BARTHAG +
                                                                          EFG_O + EFG_D + TOR + TORD + ORB
##
                  Type of random forest: classification
##
                         Number of trees: 500
## No. of variables tried at each split: 4
##
##
           OOB estimate of error rate: 16.45%
## Confusion matrix:
##
                 No Tournament R68 R64 R32 S16 E8 F4 2ND Champions
## No Tournament
                           1116
                                  0
                                     13
                                           2
                                               1
                                                  0
                                                     0
                                                          0
                                       4
                                               0
                                                  0
                                                                    0
## R68
                             12
                                   0
                                           0
                                                     0
                                                          0
## R64
                             74
                                   0
                                      35
                                          16
                                                                    0
## R32
                                     19
                                          18
                                              10
                                                  2
                                                          0
                             14
                                   0
                                                     0
                                                                    1
## S16
                              2
                                   0
                                       9
                                          18
                                               2
                                                  1
                                                     0
                                                          0
                                                                    0
                              0
                                       4
                                           6
                                               4
                                                 2 0
## E8
                                  0
                                                          0
                                                                    0
## F4
                                           5
                                               1
                                                  0 0
                                                          0
                                                                    0
                              1
                                  0
                                       1
## 2ND
                              0
                                  0
                                       0
                                           2
                                               0
                                                  1
                                                     0
                                                          0
                                                                    1
                              0
                                       0
                                               0
                                                  2 0
                                                          0
## Champions
                  class.error
## No Tournament 0.01413428
## R68
                  1.00000000
## R64
                  0.72656250
## R32
                  0.71875000
## S16
                  0.93750000
## E8
                  0.87500000
## F4
                  1.00000000
## 2ND
                   1.00000000
                   1.0000000
## Champions
```

importance(rf.cbb)

```
##
                                  R68
                                                         R32
                                                                    S16
            No Tournament
                                             R64
## ADJOE
                17.516365 0.03712023 -4.09221832
                                                  2.27568860
                                                              8.3836460
## ADJDE
                16.580518 -2.60754808 -3.81142243
                                                  7.18086637
                                                              2.8849812
## BARTHAG
                22.890156 -1.43707535 -5.09296854 9.40071881 15.0781601
## EFG_0
                13.704443 -1.03310994 3.81633754 -2.78545688 0.8523017
## EFG D
                15.656768 -4.75616547 0.60533887
                                                  3.53555515 -3.2388041
## TOR
                 9.928228 0.58239392 -3.31992969 8.84716127 -3.4234049
## TORD
                 7.215060 - 1.53338164 - 0.96522612  0.02271085  2.3047714
## ORB
                 8.062355 -1.20516012 -0.88985411 -0.75024434 -2.5147046
## DRB
                 4.110359 -1.64087992 1.00294120 -3.74633436 -1.6365326
## FTR
                 2.281594 1.99661271 4.79745906 -2.09787117 -2.2904637
## FTRD
                 8.697927 -0.41623308 -0.05596516 -3.54647696 1.9577487
## ADJ T
                 1.310325
                          ## TWO_P_O
                12.082016  0.44642798  3.24267001  -3.27391669  3.3297598
## TWO_P_D
                13.321296 -3.16760248 -1.91964788
                                                 1.05950355 -0.6558216
## THREE_P_O
                 9.489062 -0.01097076 3.40521365 -0.73080363 -1.3177905
## THREE_P_D
                          0.31627742 -2.26346583
                                                 4.36052927 -3.2437657
                11.231062
                35.904206 -0.36663767 21.22823435 17.72189220 15.3222928
## WAB
## CONF
                 9.864365
                          0.43753432 1.79536055
                                                  0.63667494 -2.0388192
##
                      E8
                                 F4
                                              2ND
                                                  Champions
## ADJOE
             5.169928685
                          0.2839869 2.413971e+00
                                                  6.8418715
## ADJDE
             2.094628689
                          1.9796397 1.702664e+00
                                                  5.6774521
            10.090560461 1.6202907 2.356755e+00
## BARTHAG
                                                  8.9834834
## EFG O
             3.290323527   0.4257054   -9.548675e-01   2.7096372
```

```
## EFG D
            ## TOR
           -0.294682560 -2.4947759 2.977290e+00 3.5549915
            0.559092816 -2.0189680 -5.627221e-01 0.6745065
## TORD
## ORB
            ## DRB
           -0.123490419 -2.0321987 3.492577e-01 0.1428601
## FTR
           -0.509940335 0.7719138 -1.447010e+00 -0.7019921
## FTRD
           -1.267969236 0.8740944 1.001002e+00 0.7883281
## ADJ T
            0.798564735 -1.0359028 -1.417051e+00 -1.0950482
## TWO P O
            4.472930613 -3.3273379 1.116161e+00 3.1231336
## TWO_P_D
            ## THREE_P_O 0.002376116 1.1370170 -1.150272e+00 0.4790230
## THREE_P_D 0.050716978 1.9170528 -1.315053e+00 0.7530714
## WAB
           13.010322056 1.2794265 4.430478e+00 7.4431495
## CONF
            0.048194574 -0.2350161 -3.721557e-01 1.8774112
##
           MeanDecreaseAccuracy MeanDecreaseGini
## ADJOE
                     17.705543
                                     37.97875
## ADJDE
                                     31.15775
                     16.915173
## BARTHAG
                     24.114008
                                     57.22234
## EFG O
                     13.897414
                                     18.51597
## EFG D
                     15.474244
                                     19.25853
## TOR
                     9.511572
                                     19.29152
## TORD
                     5.919104
                                     16.07345
## ORB
                                     16.09836
                     5.852788
## DRB
                      2.133066
                                     14.52356
## FTR
                      3.354277
                                     17.60762
## FTRD
                     7.554887
                                     16.48044
## ADJ_T
                     1.211641
                                     15.51746
## TWO_P_O
                     12.037891
                                     18.25599
## TWO_P_D
                     12.858595
                                     16.62382
## THREE P O
                      9.534882
                                     17.03434
## THREE_P_D
                     10.188479
                                     16.65825
## WAB
                     40.759544
                                     89.99358
## CONF
                      8.983196
                                     34.24977
```

Appendix 7.1. Prediction

```
# Testing Error - Bagging
bag.pred_test <- predict(bag.cbb, test_data_19, type = "class")
bag.table <- table(bag.pred_test, test_data_19[,"POSTSEASON"])
bag.error <- numeric(dim(bag.table)[1])
for(i in 1:dim(bag.table)[1]){
   bag.error[i] = round(((1-(bag.table[i,i])/(sum(bag.table[,i])))*100), 4)
}
bag.error.table <- data.frame(names(bag.table[,1]), bag.error)
colnames(bag.error.table) <- c("Round", "% Error")

# Testing Error - Random Forest
rf.pred_test <- predict(rf.cbb, test_data_19, type = "class")
rf.table <- table(rf.pred_test, test_data_19[,"POSTSEASON"])
rf.error <- numeric(dim(rf.table)[1])
for(i in 1:dim(rf.table)[1]){
   rf.error[i] = round(((1-(rf.table[i,i])/(sum(rf.table[,i])))*100), 4)</pre>
```

```
}
rf.error.table <- data.frame(names(rf.table[,1]), rf.error)
colnames(rf.error.table) <- c("Round", "% Error")</pre>
```

Appendix 7.2. Error Tables (%)

knitr::kable(bag.error.table)

Round	% Error
No Tournament	1.4035
R68	100.0000
R64	68.7500
R32	81.2500
S16	87.5000
E8	50.0000
F4	100.0000
2ND	100.0000
Champions	0.0000

knitr::kable(rf.error.table)

Round	% Error
No Tournament	1.0526
R68	100.0000
R64	78.1250
R32	81.2500
S16	87.5000
E8	50.0000
F4	100.0000
2ND	100.0000
Champions	100.0000

Appendix 8. Model 5: Classification Tree - Round Selection Given Already in Tournament

```
# Bagging
bag.cbb_trmnt <- randomForest(POSTSEASON ~ ADJOE + ADJDE + BARTHAG + EFG_O + EFG_D + TOR +
                   TORD + ORB + DRB + FTR + FTRD + ADJ_T + TWO_P_O + TWO_P_D +
                   THREE_P_O + THREE_P_D + WAB + CONF, train_given_trnmt, mtry=18, importance=T)
bag.cbb_trmnt
##
## Call:
   randomForest(formula = POSTSEASON ~ ADJOE + ADJDE + BARTHAG +
                                                                       EFG O + EFG D + TOR + TORD + ORB
##
                  Type of random forest: classification
                        Number of trees: 500
##
## No. of variables tried at each split: 18
           OOB estimate of error rate: 47.79%
##
## Confusion matrix:
##
             2ND Champions E8 F4 R32 R64 R68 S16 class.error
## 2ND
              0
                         1
                            2
                              0
                                   1
                                       0
                                           0
                                                    1.000000
## Champions
               0
                         1
                            1
                              0
                                   2
                                       0
                                           0
                                               0
                                                    0.750000
## E8
               0
                         0
                            2 1
                                   6
                                       4
                                           0
                                               3
                                                    0.875000
## F4
               0
                         0
                           0 0
                                   3
                                       2
                                           0
                                               3
                                                    1.000000
## R32
               0
                         1
                            3 0
                                  24
                                      27
                                           0
                                               9
                                                    0.625000
## R64
               0
                         0
                            0
                               0
                                  13 110
                                           0
                                               5
                                                    0.140625
               0
                         0
                            0
                               0
                                      15
                                           0
                                               0
## R68
                                   1
                                                    1.000000
## S16
               0
                         0
                            3 0
                                           0
                                                    0.843750
importance(bag.cbb_trmnt)
##
                    2ND
                                                                     R32
                            Champions
                                               F.8
                                       0.06538190
## ADJOE
                                                   0.15144294 -2.7891609
             -1.8469846 5.342399e+00
## ADJDE
             -1.0010015 2.022215e+00
                                       0.09703627
                                                   1.09909616 3.6386826
## BARTHAG
              3.1940198 1.018070e+01 8.35282462
                                                   3.46821184 -3.2654904
## EFG O
             -0.2062930 -2.582161e-01 1.06309367 -1.48284067 -2.1858729
## EFG D
             -1.0010015 -4.473031e-01 -1.18092311 -2.06176847 -0.9498378
## TOR
             1.7105892 2.128188e+00 0.20803596 -0.24097979 3.4468345
## TORD
             -0.7849477 -1.624634e-01 -0.19697171
                                                  1.35363955 1.3800280
## ORB
             -2.5416040 1.009989e-16 2.56524556 1.38319778 -2.1528073
## DRB
              0.3780185 -1.344062e+00 0.20102971 -0.03886942 -1.6018445
## FTR
             -0.5424857 -2.049800e+00 2.02028175
                                                   0.32280512 -0.9895899
## FTRD
              0.9184367 2.437140e+00 -0.83396233 -0.24548971 -1.2866105
## ADJ_T
              0.6327087 -2.847705e-01 -3.34928744 -0.75118745 -0.6730142
## TWO_P_O
              1.8849590 1.610068e+00 2.87191858 -2.34759563 -3.4334246
              1.7372705 -2.210726e+00 1.06662915 -1.54650166 0.7281433
## TWO_P_D
## THREE P O -1.0010015 -2.554979e+00 0.02034866 -0.62883578 -0.7169213
## THREE_P_D 1.1948196 -5.489050e-01 1.25585646
                                                   2.14517572 3.9491805
## WAB
              1.8220696
                         4.592111e+00 7.60437668
                                                   0.84495448 -4.7800010
## CONF
              0.3333704
                         2.870732e+00 2.20579247 0.18551904 1.6552898
```

S16 MeanDecreaseAccuracy

4.4570488

##

ADJOE

R.64

R68

5.0588635 1.0763093 1.5548960

```
## ADJDE
            7.2126104 5.0591854 -2.1039096
                                                       8.2830164
## BARTHAG
            33.1270155 6.9511785 10.8458114
                                                      32.5141130
## EFG O
             2.3717475 1.7341707 1.3180398
                                                      1.4891280
## EFG D
             4.2595231 -2.4255351 -2.7119394
                                                       0.6870089
## TOR
             3.6657920 -0.1656119 -4.3784348
                                                       3.2024541
## TORD
             2.1939582 -0.9811254 2.9382190
                                                       3.3069571
## ORB
             0.7502062 0.3158865 -1.8694528
                                                      -1.3484595
## DRB
            -0.3453966 3.9348031 -3.1523622
                                                      -1.1640590
## FTR
             2.0269341 1.5291874 -2.0345251
                                                       0.3133915
## FTRD
            4.6478166 -0.9403420 1.1924899
                                                       3.0530572
## ADJ_T
            -0.8902485 1.8500909 -1.8511404
                                                      -1.9486951
## TWO_P_O
             1.8380679 1.0624924 1.1896894
                                                       0.7157788
## TWO_P_D
             1.3288280 0.5766336 -1.4787298
                                                       0.8103443
## THREE_P_O 5.9220827 1.0169490 -1.2450765
                                                       2.9454826
## THREE_P_D 5.0852191 3.8755252 -2.4240851
                                                       6.5279816
## WAB
            12.1952839 5.0416586 0.1527851
                                                      11.3413443
## CONF
             3.2081878 1.4087007 -2.8567038
                                                      3.1314758
##
            MeanDecreaseGini
                    6.799858
## ADJOE
## ADJDE
                    7.433371
## BARTHAG
                   39.271930
## EFG O
                    5.377488
## EFG_D
                    5.206575
## TOR
                    9.814789
## TORD
                   10.071716
## ORB
                    8.665016
## DRB
                    6.831251
## FTR
                    7.370977
## FTRD
                    9.596918
## ADJ T
                    6.509115
## TWO_P_O
                    7.994255
## TWO_P_D
                    5.549594
## THREE_P_O
                    7.921413
## THREE_P_D
                   11.420087
## WAB
                   12.671988
## CONF
                   21.517040
```

Appendix 8.1. Prediction

```
# Testing Error - Bagging
bag1.pred_test <- predict(bag.cbb_trmnt, test_given_trnmt_19, type = "class")
bag1.table <- table(bag1.pred_test, test_given_trnmt_19[,"POSTSEASON"])
bag1.error <- numeric(dim(bag1.table)[1])
for(i in 1:dim(bag1.table)[1]){
  bag1.error[i] = round(((1-(bag1.table[i,i])/(sum(bag1.table[,i])))*100), 4)
}
bag1.error.table <- data.frame(names(bag1.table[,1]), bag1.error)
colnames(bag1.error.table) <- c("Round", "% Error")</pre>
```

Appendix 8.2. Error Table (%)

knitr::kable(bag1.error.table)

Round	% Error
2ND	100.000
Champions	0.000
E8	75.000
F4	100.000
R32	81.250
R64	21.875
R68	75.000
S16	87.500

Appendix 9. Full Error Table (%)

```
# Model 1: Binomial
binom.table.error <- xtabs( ~ train_data$TRNMT + predout)</pre>
binom.error = round((1-(binom.table.error[1,1]+binom.table.error[2,2])/(sum(binom.table.error)))*100, 4
binom.error.full <- c(binom.error, rep(NA, 8))</pre>
# Testing Error classification rate
binom.table.error.test <- xtabs( ~ test_data_19$TRNMT + predout_test)</pre>
binom.error.test = round((1-(binom.table.error.test[1,1]+binom.table.error.test[2,2])/(sum(binom.table.
binom.error.test.full <- c(binom.error.test, rep(NA, 8))
# Model 2: Multi
# Model 3: Multi
mmod3.error.full <- c(NA, mmod3.error)</pre>
mmod3.error.test.full <- c(NA, mmod3.error.test)</pre>
# Model 4: RF
bag.error.train <- round(bag.cbb$confusion[,"class.error"]*100, 4)</pre>
rf.error.train <- round(rf.cbb$confusion[,"class.error"]*100, 4)
# Model 5: RF
bag1.error.train <- round(bag.cbb_trmnt$confusion[,"class.error"]*100, 4)</pre>
bag1.error.train.full <- c(NA, bag1.error.train)</pre>
bag1.error.full <- c(NA, bag1.error)</pre>
# Final Table
mini.error.table <- data.frame(mmod3.error.full, mmod3.error.test.full, bag1.error.train.full, bag1.err
mini.error.table <- mini.error.table[c(1, 8, 7, 6, 9, 4, 5, 2, 3),]
                                                                                       # correcting order to
full.error.table1 <- data.frame(binom.error.full, binom.error.test.full,</pre>
                                    mmod1.error, mmod1.error.test, bag.error.train,
                                    bag.error)
full.error.table2 <- data.frame(rf.error.train, rf.error, mini.error.table)</pre>
names(full.error.table1) <- c("Binom. Train", "Binom. Test", "Multi. Train", "Multi. Test",</pre>
                               "Bag Train", "Bag Test")
names(full.error.table2) <- c("RF Train", "RF Test", "Sp. Multi. Train",</pre>
                               "Sp. Multi. Test", "Sp. Bag Train", "Sp. Bag Test")
knitr::kable(full.error.table1)
```

	Binom. Train	Binom. Test	Multi. Train	Multi. Test	Bag Train	Bag Test
No Tournament	12.5356	12.7479	1.5901	1.7544	1.5901	1.4035
R68	NA	NA	100.0000	100.0000	100.0000	100.0000
R64	NA	NA	65.6250	75.0000	64.8438	68.7500
R32	NA	NA	54.6875	75.0000	73.4375	81.2500
S16	NA	NA	78.1250	75.0000	87.5000	87.5000
E8	NA	NA	68.7500	75.0000	87.5000	50.0000
F4	NA	NA	100.0000	100.0000	100.0000	100.0000
2ND	NA	NA	0.0000	100.0000	100.0000	100.0000
Champions	NA	NA	0.0000	100.0000	100.0000	0.0000

knitr::kable(full.error.table2)

	RF Train	RF Test	Sp. Multi. Train	Sp. Multi. Test	Sp. Bag Train	Sp. Bag Test
No Tournament	1.4134	1.0526	NA	NA	NA	NA
R68	100.0000	100.0000	81.2500	50.0	100.0000	75.000
R64	72.6562	78.1250	13.2812	25.0	14.0625	21.875
R32	71.8750	81.2500	53.1250	50.0	62.5000	81.250
S16	93.7500	87.5000	75.0000	62.5	84.3750	87.500
E8	87.5000	50.0000	75.0000	75.0	87.5000	75.000
F4	100.0000	100.0000	75.0000	100.0	100.0000	100.000
2ND	100.0000	100.0000	0.0000	100.0	100.0000	100.000
Champions	100.0000	100.0000	0.0000	0.0	75.0000	0.000

Appendix 10. 2020 March Madness Predictions

```
bag.pred test 20 <- predict(bag.cbb, test data 20, type = "class")</pre>
mmod.pred_test_20 <- predict(mmod1, test_data_20, type = "class")</pre>
final_20 <- data.frame(test_data_20, bag.pred_test_20, mmod.pred_test_20)
summary(final 20[,c("bag.pred test 20", "mmod.pred test 20")])
##
                             mmod.pred_test_20
        bag.pred_test_20
## No Tournament:302
                         No Tournament: 309
                : 25
                         R32
                                      : 26
## R32
## R64
                : 24
                       R64
                                      : 15
## E8
                : 2
                       E8
                                      : 2
                         2ND
## R68
                : 0
                : 0
                         R68
## S16
## (Other)
                         (Other)
                : 0
```

Appendix 10.1. Late Round Predictions

```
final 20[which(final 20$bag.pred test 20=="E8"), c("TEAM", "bag.pred test 20")]
##
           TEAM bag.pred_test_20
## 1758 Kansas
                              E8
## 1760 Gonzaga
                              F.8
final_20[which(final_20$mmod.pred_test_20=="E8"), c("TEAM", "mmod.pred_test_20")]
           TEAM mmod.pred test 20
##
## 1758 Kansas
                               E8
## 1760 Gonzaga
final_20[which(final_20$mmod.pred_test_20=="2ND"), c("TEAM", "mmod.pred_test_20")]
          TEAM mmod.pred_test_20
## 1761 Dayton
                             2ND
```

Appendix 10.2. Big Ten Predictions

```
final_20[which(final_20$CONF=="B10"), c("TEAM", "bag.pred_test_20", "mmod.pred_test_20")]
##
               TEAM bag.pred_test_20 mmod.pred_test_20
## 1762 Michigan St.
                                                   R32
                                 R32
## 1765
           Ohio St.
                                 R32
                                                   R64
## 1771
           Michigan
                                 R32
                                                   R32
## 1772
          Penn St.
                                 R32
                                                   R32
```

##	1776	Wisconsin	R32	R32
##	1780	Purdue	No Tournament N	o Tournament
##	1783	Maryland	R32	R32
##	1784	Minnesota	No Tournament N	o Tournament
##	1786	Illinois	R32	R32
##	1787	Rutgers	R32	R32
##	1788	Iowa	R64	R64
##	1793	Indiana	R64	R64
##	1873	${\tt Northwestern}$	No Tournament N	o Tournament
##	1916	Nebraska	No Tournament N	o Tournament

options(op)