Spatial Regression Modeling Example - TAMU RDC

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This empirical example illustrates the use of R for extracting data from the American Community Survey, and using these data in a spatial regression model.

See what variables are in the ACS Demographic Profile Tables

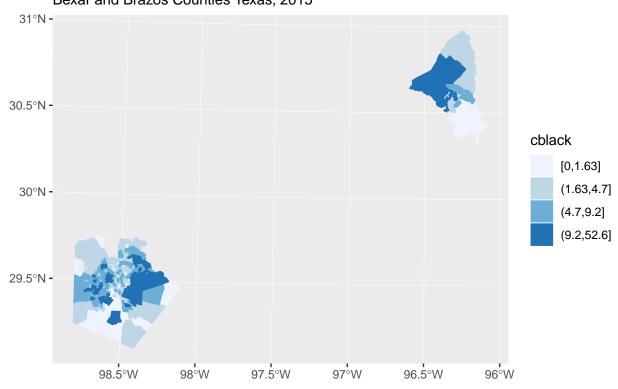
```
library(tidycensus); library(tidyverse)
## -- Attaching packages ------
## v ggplot2 2.2.1.9000
                    v purrr 0.2.4
## v tibble 1.4.2
                    v dplyr 0.7.4
## v tidyr
         0.8.0
                    v stringr 1.3.0
                    v forcats 0.3.0
## v readr
         1.1.1
## -- Conflicts ----- tidyverse_conflic
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                masks stats::lag()
## x dplyr::vars() masks ggplot2::vars()
v15 <- load_variables(2015 , "acs5/profile", cache = TRUE)
#View(v15)
```

Extract from ACS summary file from 2015

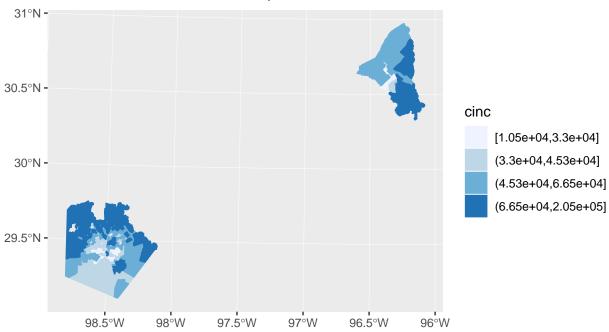
```
sa_acs<-get_acs(geography = "tract", state="TX", county = c("Bexar", "Brazos"), year = 2015,</pre>
                variables=c("DP05_0001E", "DP03_0009P", "DP03_0062E", "DP03_0119PE",
                             "DP05_0001E", "DP02_0009PE", "DP02_0008PE", "DP02_0040E", "DP02_0038E",
                             "DP02_0066PE", "DP02_0067PE", "DP02_0080PE", "DP02_0092PE",
                             "DP03_0005PE", "DP03_0028PE", "DP03_0062E", "DP03_0099PE", "DP03_0101PE",
                             "DP03_0119PE", "DP04_0046PE", "DP04_0078PE", "DP05_0072PE", "DP05_0073PE",
                             "DP05_0066PE", "DP05_0072PE", "DP02_0113PE"),
                geometry = T, output = "wide")
## Getting data from the 2011-2015 5-year ACS
## Downloading feature geometry from the Census website. To cache shapefiles for use in future session
## Using the ACS Data Profile
## Using the ACS Data Profile
sa_acs$county<-substr(sa_acs$GEOID, 1, 5)</pre>
sa_acs2<-sa_acs%>%
  mutate(totpop= DP05_0001E, fertrate = DP02_0040E,pwhite=DP05_0072PE,
         pblack=DP05_0073PE , phisp=DP05_0066PE, pfemhh=DP02_0008PE,
         phsormore=DP02_0066PE,punemp=DP03_0009PE, medhhinc=DP03_0062E,
         ppov=DP03_0119PE, pforn=DP02_0092PE,plep=DP02_0113PE) %>%
  na.omit()
```

Some basic mapping of variables

Proportion African American Bexar and Brazos Counties Texas, 2015



Median HH Income Bexar and Brazos Counties Texas, 2015



Spatial Representation of the data

library(spdep)

```
## Loading required package: sp
## Loading required package: Matrix
## Attaching package: 'Matrix'
## The following object is masked from 'package:tidyr':
##
##
       expand
## Loading required package: spData
## To access larger datasets in this package, install the spDataLarge
## package with: `install.packages('spDataLarge',
## repos='https://nowosad.github.io/drat/', type='source'))`
sapoly<-as(sa_acs2, "Spatial")</pre>
nbs<-poly2nb(sapoly, queen = T)</pre>
wts<-nb2listw(nbs, style="W")</pre>
plot(sapoly,main="Queen Contiguity Spatial Neighbors" )
plot(nbs, coords=coordinates(sapoly), col=2, add=T, cex=.2 )
```

Queen Contiguity Spatial Neighbors

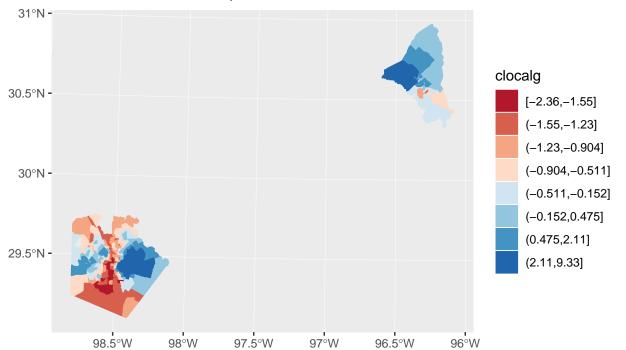




Basic spatial clustering of data

```
moran.mc(x=sapoly$medhhinc, listw = wts, nsim = 999, na.action = na.omit)
##
  Monte-Carlo simulation of Moran I
##
## data: sapoly$medhhinc
## weights: wts
## number of simulations + 1: 1000
## statistic = 0.63437, observed rank = 1000, p-value = 0.001
## alternative hypothesis: greater
moran.mc(x=sapoly$pblack, listw = wts, nsim = 999, na.action = na.omit)
##
## Monte-Carlo simulation of Moran I
##
## data: sapoly$pblack
## weights: wts
## number of simulations + 1: 1000
##
## statistic = 0.64936, observed rank = 1000, p-value = 0.001
## alternative hypothesis: greater
sa_acs2$local_g<- localG(sapoly$pblack, listw = wts)</pre>
```

Local Geary G Proportion Black Bexar and Brazos Counties, Texas

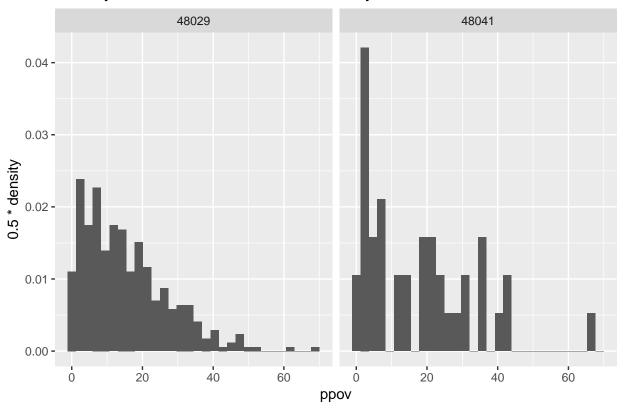


Descriptive analysis

```
sa_acs2%>%
ggplot()+geom_histogram(aes(x =ppov , y=0.5*..density..))+
facet_wrap(~county)+
ggtitle(label = "Poverty Rate in Bexar and Brazos County")
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Poverty Rate in Bexar and Brazos County



OLS regression models

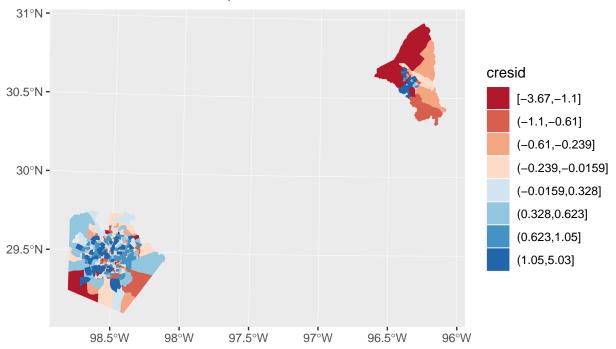
fit.1<-lm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county, data=sa_acs2)
summary(fit.1)</pre>

```
##
## Call:
## lm(formula = phsormore ~ pforn + pblack + ppov + plep + punemp +
      ppov + log(medhhinc) + county, data = sa_acs2)
##
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   ЗQ
                                           Max
## -19.9340 -3.4460 -0.0902
                               3.5301
                                       27.0007
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                55.82949
                          12.53796
                                      4.453 1.11e-05 ***
                            0.06916 10.320 < 2e-16 ***
## pforn
                 0.71372
## pblack
                 0.03095
                            0.03624
                                      0.854 0.393632
## ppov
                -0.22986
                            0.04454 -5.161 3.91e-07 ***
                -1.46550
                            0.06981 -20.992 < 2e-16 ***
## plep
## punemp
                -0.22391
                            0.08658 -2.586 0.010059 *
## log(medhhinc) 3.75401
                            1.09724
                                      3.421 0.000688 ***
## county48041
                 0.84048
                            1.01322
                                      0.830 0.407315
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 5.706 on 394 degrees of freedom
## Multiple R-squared: 0.844, Adjusted R-squared: 0.8412
## F-statistic: 304.4 on 7 and 394 DF, p-value: < 2.2e-16
library(car)
## Loading required package: carData
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
       recode
## The following object is masked from 'package:purrr':
##
       some
library(lmtest)
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
#variance inflation factor for beta's
vif(fit.1)
##
           pforn
                        pblack
                                                      plep
                                                                   punemp
                                        ppov
##
        2.482648
                      1.142759
                                    3.716357
                                                  4.026892
                                                                 1.776046
## log(medhhinc)
                        county
##
        3.665739
                      1.135699
\#Breush-Pagan\ test\ for\ constant\ variance
bptest(fit.1)
##
   studentized Breusch-Pagan test
##
##
## data: fit.1
## BP = 44.769, df = 7, p-value = 1.516e-07
#looks like we have heteroskedasticity
Anova(fit.1, white.adjust=T)
## Coefficient covariances computed by hccm()
## Analysis of Deviance Table (Type II tests)
##
## Response: phsormore
                            F
                                 Pr(>F)
                  1 70.4181 8.695e-16 ***
## pforn
                  1 0.4424 0.5063440
## pblack
                  1 13.8192 0.0002304 ***
## ppov
                  1 247.5227 < 2.2e-16 ***
## plep
```

```
1 5.5576 0.0188888 *
## punemp
## log(medhhinc)
                  1 8.1796 0.0044619 **
## county
                      0.5522 0.4578764
                  1
## Residuals
                394
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Map of model residuals
#extract studentized residuals from the fit, and examine them
sa_acs2$residfit1<-rstudent(fit.1)</pre>
sa_acs2 %>%
 mutate(cresid=cut(residfit1,breaks = quantile(residfit1,p=seq(0,1,length.out = 9)),
                   include.lowest = T))%>%
  ggplot(aes(fill = cresid, color = cresid)) +
  geom_sf() +
  ggtitle("OLS model residuals", subtitle = "Bexar and Brazos Counties, Texas")+
  coord_sf(crs = 102009) +
  scale_fill_brewer(palette = "RdBu") +
  scale_color_brewer(palette = "RdBu")
```

OLS model residuals Bexar and Brazos Counties, Texas



Analysis of residual clustering

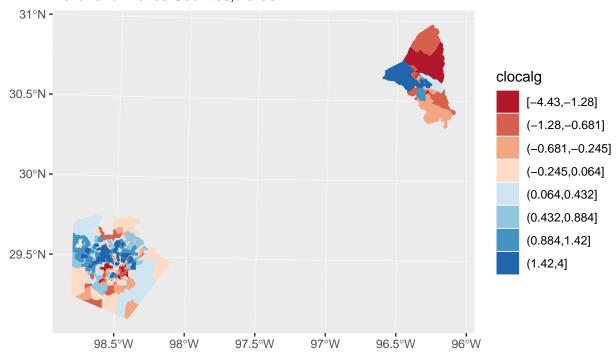
```
#test for residual autocorrelation
lm.morantest(fit.1, listw=wts)
```

##
Global Moran I for regression residuals

```
##
## data:
## model: lm(formula = phsormore ~ pforn + pblack + ppov + plep +
## punemp + ppov + log(medhhinc) + county, data = sa_acs2)
## weights: wts
##
## Moran I statistic standard deviate = 6.1087, p-value = 5.022e-10
## alternative hypothesis: greater
## sample estimates:
## Observed Moran I
                         Expectation
                                             Variance
##
       0.1600961814
                       -0.0104723871
                                         0.0007796511
#looks like we have significant autocorrelation in our residuals
#Let's look at the local autocorrelation in our residuals
#qet the values of I
sa_acs2$local_G<-as.numeric(localG(sa_acs2$residfit1, wts))</pre>
sa_acs2 %>%
  mutate(clocalg=cut(local_G, breaks = quantile(local_G, probs = seq(0,1, length.out = 9)),
                     include.lowest = T))%>%
  ggplot(aes(fill = clocalg, color = clocalg)) +
  geom_sf() +
  ggtitle("Local Geary G of OLS model residuals", subtitle = "Bexar and Brazos Counties, Texas")+
  coord_sf(crs = 102009) +
  scale_fill_brewer(palette = "RdBu") +
  scale_color_brewer(palette = "RdBu")
```

Local Geary G of OLS model residuals

Bexar and Brazos Counties, Texas



Picking a spatial regression model

```
#perform a model specification test
lm.LMtests(fit.1, listw=wts, test="all")

##
## Lagrange multiplier diagnostics for spatial dependence
##
```

```
## data:
## model: lm(formula = phsormore ~ pforn + pblack + ppov + plep +
## punemp + ppov + log(medhhinc) + county, data = sa_acs2)
## weights: wts
##
## LMerr = 31.091, df = 1, p-value = 2.462e-08
##
##
##
   Lagrange multiplier diagnostics for spatial dependence
##
## data:
## model: lm(formula = phsormore ~ pforn + pblack + ppov + plep +
## punemp + ppov + log(medhhinc) + county, data = sa_acs2)
## weights: wts
##
## LMlag = 112.29, df = 1, p-value < 2.2e-16
##
##
## Lagrange multiplier diagnostics for spatial dependence
```

```
## data:
## model: lm(formula = phsormore ~ pforn + pblack + ppov + plep +
## punemp + ppov + log(medhhinc) + county, data = sa_acs2)
## weights: wts
##
## RLMerr = 0.034807, df = 1, p-value = 0.852
##
##
  Lagrange multiplier diagnostics for spatial dependence
##
##
## data:
## model: lm(formula = phsormore ~ pforn + pblack + ppov + plep +
## punemp + ppov + log(medhhinc) + county, data = sa_acs2)
## weights: wts
##
## RLMlag = 81.238, df = 1, p-value < 2.2e-16
##
##
## Lagrange multiplier diagnostics for spatial dependence
##
## data:
## model: lm(formula = phsormore ~ pforn + pblack + ppov + plep +
## punemp + ppov + log(medhhinc) + county, data = sa_acs2)
## weights: wts
## SARMA = 112.33, df = 2, p-value < 2.2e-16
#Now we fit the spatial lag model
#The lag mode is fit with lagsarlm() in the spdep library
#we basically specify the same model as in the lm() fit above
#But we need to specify the spatial weight matrix and the type
#of lag model to fit
Fit the spatial regression models
#Spatial Error model
fit.err<-errorsarlm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county,
                  data=sa acs2, listw=wts)
#summary(fit.err, Nagelkerke=T)
#Spatial Lag Model
fit.lag<-lagsarlm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county,
                  data=sa_acs2, listw=wts, type="lag")
#summary(fit.lag, Nagelkerke=T)
#Spatial Durbin Lag Model
fit.lag2<-lagsarlm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county,
                   data=sa_acs2, listw=wts, type="mixed")
#summary(fit.lag2, Nagelkerke=T)
#Spatial Durbin Error Model
fit.errdurb<-errorsarlm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county,
                   data=sa_acs2, listw=wts, etype="emixed", method="spam")
```

##

```
## `validspamobject()` is deprecated. Use `validate_spam()` directly
#summary(fit.errdurb, Nagelkerke=T)
#SAC Model
fit.sac<-sacsarlm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county,
                   data=sa_acs2, listw=wts, type="sac", method="MC")
## Warning in sqrt(diag(fdHess)[-c(1, 2)]): NaNs produced
#summary(fit.sac, Nagelkerke=T)
#SMA Model
fit.sma<-spautolm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc)+county,
                   data=sa_acs2, listw=wts, family="SMA")
#summary(fit.sma)
#which says we still have significant autocorrelation in the residuals, even after
#accounting for autocorrelation in the outcome
bptest.sarlm(fit.lag)
##
##
   studentized Breusch-Pagan test
## data:
## BP = 31.395, df = 7, p-value = 5.257e-05
bptest.sarlm(fit.lag2)
##
## studentized Breusch-Pagan test
##
## data:
## BP = 44.621, df = 13, p-value = 2.42e-05
AIC(fit.lag)
## [1] 2430.949
AIC(fit.lag2)
## [1] 2418.411
AIC(fit.errdurb)
## [1] 2418.929
AIC(fit.sac)
## [1] 2433.421
AIC(fit.sma)
## [1] 2513.918
```

Table 1: Spatially autoregressive models

	Dependent variable:			
	phsormore			
	spatial		spatial	
	error Error Model	autore Lag Model	egressive Durbin Lag Model	
	(1)	(2)	(3)	
pforn	0.308*** (0.163, 0.452)	0.381*** (0.260, 0.502)	0.273*** (0.134, 0.413)	
pblack	$0.045 \\ (-0.055, 0.144)$	$ \begin{array}{c} -0.009 \\ (-0.069, 0.051) \end{array} $	$0.061 \\ (-0.045, 0.168)$	
ppov	$-0.135^{***} \\ (-0.209, -0.061)$	$-0.180^{***} \\ (-0.253, -0.107)$	$-0.176^{***} \\ (-0.248, -0.103)$	
plep	$-0.949^{***} \\ (-1.101, -0.798)$	$-0.941^{***} \\ (-1.077, -0.804)$	$-0.847^{***} \\ (-0.998, -0.697)$	
punemp	$-0.172^{**} \\ (-0.318, -0.026)$	$-0.188^{***} \\ (-0.330, -0.046)$	$-0.166^{**} \\ (-0.308, -0.024)$	
$\log(\text{medhhinc})$	4.524*** (2.298, 6.751)	$ \begin{array}{c} 1.044 \\ (-0.844, 2.933) \end{array} $	2.855** (0.671, 5.038)	
county48041	3.603 (-2.368, 9.575)	$0.091 \\ (-1.583, 1.764)$	$ \begin{array}{c} -0.984 \\ (-2.778, 0.811) \end{array} $	
lag.pforn			0.399*** (0.162, 0.636)	
lag.pblack			$ \begin{array}{c} -0.100 \\ (-0.240, 0.040) \end{array} $	
lag.ppov			$-0.251^{***} (-0.426, -0.076)$	
lag.plep			$-0.336^{**} \\ (-0.653, -0.018)$	
lag.punemp			$ \begin{array}{c} -0.042 \\ (-0.365, 0.280) \end{array} $	
${\rm lag.log(medhhinc)}$			$-7.389^{***} (-11.214, -3.563)$	
Constant	43.998*** (18.729, 69.268)	46.216*** (25.675, 66.758)	115.959*** (74.365, 157.553)	
Observations Log Likelihood σ^2 Akaike Inf. Crit. Wald Test (df = 1) LR Test (df = 1)	402 -1,235.543 24.352 2,491.085 272.941*** 61.860***	$ \begin{array}{r} 402 \\ -1,205.475 \\ 22.750 \\ 2,430.949 \\ 154.313^{***} \\ 121.996^{***} \end{array} $	402 -1,193.205 21.656 2,418.411 28.550*** 23.967***	

Note: *p<0.1; **p<0.05; ***p<0.01

Spatial Impacts in lag models

```
#impacts for lag models
im.sdm<-impacts(fit.lag,listw=wts, R=100)</pre>
summary( im.sdm, zstats=TRUE)
## Impact measures (lag, exact):
##
                     Direct
                                Indirect
                                              Total
## pforn
               0.395573976 0.280072981 0.67564696
## pblack
               -0.009442059 -0.006685135 -0.01612719
               -0.186845084 -0.132289440 -0.31913452
## ppov
## plep
               -0.976673509 -0.691501154 -1.66817466
## punemp
               -0.195121755 -0.138149461 -0.33327122
## log(medhhinc) 1.084438999 0.767800921 1.85223992
                ## county48041
## Simulation results (asymptotic variance matrix):
## Direct:
##
## Iterations = 1:100
## Thinning interval = 1
## Number of chains = 1
## Sample size per chain = 100
##
## 1. Empirical mean and standard deviation for each variable,
     plus standard error of the mean:
##
##
                            SD Naive SE Time-series SE
                  Mean
## pforn
                0.4002 0.05703 0.005703
                                        0.005703
## pblack
               -0.0111 0.02749 0.002749
                                             0.002749
## ppov
               -0.1856 0.03422 0.003422
                                             0.003422
               -0.9861 0.06699 0.006699
## plep
                                             0.006699
               -0.1899 0.07068 0.007068
## punemp
                                             0.007068
## log(medhhinc) 1.0848 0.99701 0.099701
                                             0.099701
## county48041
                0.1378 0.83228 0.083228
                                             0.083228
##
## 2. Quantiles for each variable:
##
##
                   2.5%
                             25%
                                     50%
                                               75%
                                                      97.5%
## pforn
                0.30041 0.36043 0.39398 0.435663 0.50450
## pblack
               -0.06344 -0.02981 -0.01081 0.007477 0.04022
## ppov
               -0.24351 -0.21066 -0.18706 -0.162260 -0.11512
## plep
               -1.12485 -1.02578 -0.97921 -0.940348 -0.87873
## punemp
               -0.33871 -0.23996 -0.17896 -0.140834 -0.07854
## log(medhhinc) -0.84441 0.44605 1.04241 1.795226 3.22203
## county48041 -1.58329 -0.30370 0.19115 0.713530 1.65400
##
## Indirect:
## Iterations = 1:100
## Thinning interval = 1
## Number of chains = 1
## Sample size per chain = 100
##
```

```
## 1. Empirical mean and standard deviation for each variable,
##
     plus standard error of the mean:
##
##
                               SD Naive SE Time-series SE
                     Mean
## pforn
                 0.282778 0.04364 0.004364
                                                0.004364
                -0.008279 0.01994 0.001994
                                                0.001994
## pblack
                -0.131284 0.02607 0.002607
                                                0.002607
## ppov
## plep
                -0.698105 0.07566 0.007566
                                                0.007566
                -0.134091 0.04986 0.004986
## punemp
                                                0.004986
## log(medhhinc) 0.763351 0.71015 0.071015
                                                0.071015
## county48041
                 0.095568 0.58733 0.058733
                                                0.058733
## 2. Quantiles for each variable:
##
##
                    2.5%
                             25%
                                       50%
                                                75%
                                                       97.5%
## pforn
                 0.20304 0.2497 0.278549 0.313521
                                                     0.37308
                -0.04566 -0.0202 -0.007184 0.005234 0.02684
## pblack
## ppov
                -0.17598 -0.1470 -0.130235 -0.118292 -0.07827
                -0.85070 -0.7432 -0.697626 -0.646432 -0.56322
## plep
## punemp
                -0.23082 -0.1696 -0.133535 -0.096227 -0.05575
## log(medhhinc) -0.59400 0.3129 0.740958 1.263147 2.29366
## county48041
                -1.09292 -0.2333 0.122693 0.503534 1.10233
##
## Total:
## Iterations = 1:100
## Thinning interval = 1
## Number of chains = 1
## Sample size per chain = 100
##
## 1. Empirical mean and standard deviation for each variable,
##
     plus standard error of the mean:
##
##
                              SD Naive SE Time-series SE
                 0.68298 0.09354 0.009354
                                                0.009354
## pforn
## pblack
                -0.01938 0.04735 0.004735
                                                0.004735
## ppov
                -0.31690 0.05758 0.005758
                                                0.005758
                -1.68421 0.11378 0.011378
                                                0.007872
## plep
                -0.32396 0.11891 0.011891
## punemp
                                                0.011891
## log(medhhinc) 1.84817 1.70296 0.170296
                                                0.170296
## county48041
                 0.23333 1.41753 0.141753
                                                0.141753
## 2. Quantiles for each variable:
##
                   2.5%
                                    50%
                                             75%
##
                            25%
                                                   97.5%
## pforn
                 0.5047 0.6111 0.6789 0.74952
                                                 0.86997
                -0.1090 -0.0488 -0.0183 0.01271
## pblack
                                                 0.06762
## ppov
                -0.4141 -0.3557 -0.3198 -0.28043 -0.19621
## plep
                -1.9223 -1.7478 -1.6708 -1.61157 -1.46506
                -0.5526 -0.4044 -0.3128 -0.23651 -0.13657
## punemp
## log(medhhinc) -1.4419 0.7591 1.7794 3.07390 5.51568
## county48041
                -2.6530 -0.5494 0.3090 1.21779 2.70795
```

##

```
## Simulated z-values:
                                              Total
##
                     Direct Indirect
                 7.0172197 6.4797357 7.3012070
## pforn
                 -0.4038482 -0.4152134 -0.4093015
## pblack
## ppov
                 -5.4234289 -5.0348702 -5.5037453
## plep
                -14.7211399 -9.2269679 -14.8020886
                 -2.6862452 -2.6891085 -2.7244943
## punemp
## log(medhhinc) 1.0880675 1.0749208 1.0852698
## county48041
                 0.1655277 0.1627152 0.1646058
## Simulated p-values:
                            Indirect Total
                Direct
## pforn
                 2.2633e-12 9.1883e-11 2.8511e-13
## pblack
                0.686324
                           0.6779857 0.68232
## ppov
                5.8466e-08 4.7817e-07 3.7181e-08
## plep
                < 2.22e-16 < 2.22e-16 < 2.22e-16
## punemp
                 0.007226
                          0.0071643 0.00644
## log(medhhinc) 0.276565
                            0.2824102 0.27780
## county48041
                 0.868529
                           0.8707426 0.86925
Spatial Regimes, split data by unemployment rate
sa_acs2$unemp_cut<-cut(sa_acs2$punemp, breaks = quantile(sa_acs2$punemp,</pre>
                                                         p=c(0, .33, .66, 1)))
table(sa_acs2$unemp_cut)
(0,5.4] (5.4,8.6] (8.6,33.8] 134 131 136
fit.low<-lm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc),</pre>
            data=sa acs2, subset=unemp cut=="(0,5.4]")
fit.med<-lm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc),</pre>
            data=sa_acs2, subset=unemp_cut=="(5.4,8.6]")
fit.hi<-lm(phsormore~pforn+pblack+ppov+plep +punemp+ppov+log(medhhinc),
           data=sa_acs2, subset=unemp_cut=="(8.6,33.8]")
stargazer(fit.low, fit.med, fit.hi,header=FALSE, type='latex',
          ci = T,title = "Spatial regime models",
          column.labels = c("Low Unemployment", "Moderate Unemployment", "High Unemployment"))
```

Table 2: Spatial regime models

	10010 2 . 5P			
	Dependent variable:			
	Low Unemployment	phsormore Moderate Unemployment	High Unemployment	
	(1)	(2)	(3)	
pforn	0.401*** (0.213, 0.589)	0.580*** (0.376, 0.785)	0.977*** (0.724, 1.231)	
pblack	$ \begin{array}{c} -0.081 \\ (-0.224, 0.063) \end{array} $	$0.156^{**} \\ (0.026, 0.286)$	$ \begin{array}{c} -0.017 \\ (-0.123, 0.088) \end{array} $	
ppov	$-0.246^{***} \\ (-0.396, -0.097)$	$-0.264^{***} \\ (-0.410, -0.119)$	$ \begin{array}{c} -0.086 \\ (-0.241, 0.070) \end{array} $	
plep	-0.929^{***} (-1.153, -0.705)	$ \begin{array}{c} -1.710^{***} \\ (-1.911, -1.509) \end{array} $	$-1.664^{***} \\ (-1.900, -1.429)$	
punemp	$ \begin{array}{c} -0.052 \\ (-0.681, 0.576) \end{array} $	$ \begin{array}{c} -0.253 \\ (-1.232, 0.727) \end{array} $	$-0.353^* \\ (-0.722, 0.016)$	
$\log(\mathrm{medhhinc})$	4.518*** (1.645, 7.392)	$0.539 \\ (-2.656, 3.734)$	8.531*** (3.620, 13.442)	
Constant	46.225*** (12.770, 79.680)	95.580*** (57.760, 133.399)	$4.212 \\ (-50.485, 58.908)$	
Observations R^2 Adjusted R^2	134 0.758 0.746	131 0.874 0.868	136 0.805 0.795	
Residual Std. Error F Statistic	4.213 (df = 127) 66.208*** (df = 6; 127)	4.860 (df = 124) 143.524*** (df = 6; 124)	6.659 (df = 129) 88.520*** (df = 6; 129)	

Note: *p<0.1; **p<0.05; ***p<0.01

sessionInfo()

```
## R version 3.5.0 (2018-04-23)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 15063)
##
## Matrix products: default
##
## locale:
## [1] LC COLLATE=English United States.1252
## [2] LC_CTYPE=English_United States.1252
## [3] LC_MONETARY=English_United States.1252
## [4] LC_NUMERIC=C
## [5] LC_TIME=English_United States.1252
##
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                                datasets methods
                                                                    base
## other attached packages:
   [1] stargazer_5.2.1
                           lmtest_0.9-36
                                               zoo_1.8-1
   [4] car_3.0-0
                           carData_3.0-1
                                               spdep_0.7-7
##
  [7] spData_0.2.8.3
                           Matrix_1.2-14
                                               sp_1.2-7
## [10] bindrcpp_0.2.2
                           forcats_0.3.0
                                               stringr_1.3.0
## [13] dplyr_0.7.4
                           purrr_0.2.4
                                               readr_1.1.1
## [16] tidyr_0.8.0
                           tibble_1.4.2
                                               ggplot2_2.2.1.9000
## [19] tidyverse_1.2.1
                           tidycensus_0.4.6
##
## loaded via a namespace (and not attached):
## [1] nlme_3.1-137
                           sf 0.6-2
                                               lubridate 1.7.4
## [4] gmodels_2.16.2
                           RColorBrewer_1.1-2 httr_1.3.1
                                               backports_1.1.2
## [7] rprojroot_1.3-2
                           tools 3.5.0
## [10] rgdal_1.2-20
                           R6_2.2.2
                                               DBI_1.0.0
## [13] lazyeval_0.2.1
                           colorspace_1.3-2
                                               withr_2.1.2
## [16] mnormt_1.5-5
                           curl_3.2
                                               compiler_3.5.0
## [19] cli_1.0.0
                           rvest_0.3.2
                                               expm_0.999-2
## [22] xml2_1.2.0
                                               scales_0.5.0.9000
                           labeling_0.3
## [25] classInt_0.2-3
                           psych_1.8.4
                                               rappdirs_0.3.1
## [28] digest_0.6.15
                           foreign_0.8-70
                                               rmarkdown_1.9
## [31] rio_0.5.10
                                               htmltools_0.3.6
                           pkgconfig_2.0.1
## [34] rlang_0.2.0.9001
                           readxl_1.1.0
                                               rstudioapi_0.7
## [37] bindr_0.1.1
                           jsonlite_1.5
                                               gtools_3.5.0
## [40] magrittr_1.5
                           dotCall64_0.9-5.2
                                               Rcpp_0.12.16
## [43] munsell_0.4.3
                           RPostgreSQL_0.6-2
                                               abind_1.4-5
## [46] stringi 1.2.2
                           yaml 2.1.19
                                               MASS 7.3-50
## [49] plyr_1.8.4
                           grid_3.5.0
                                               maptools_0.9-2
## [52] parallel 3.5.0
                           gdata 2.18.0
                                               crayon 1.3.4
## [55] udunits2_0.13
                           deldir_0.1-15
                                               lattice_0.20-35
## [58] haven 1.1.1
                           splines_3.5.0
                                               hms 0.4.2
## [61] knitr_1.20
                           pillar_1.2.2
                                               uuid_0.1-2
## [64] boot_1.3-20
                           reshape2_1.4.3
                                               LearnBayes_2.15.1
## [67] glue_1.2.0
                           evaluate_0.10.1
                                               data.table_1.11.0
## [70] modelr_0.1.1
                           spam_2.1-4
                                               cellranger_1.1.0
## [73] gtable_0.2.0
                           assertthat_0.2.0
                                               openxlsx_4.0.17
```

[76] broom_0.4.4 e1071_1.6-8 coda_0.19-1 ## [79] class_7.3-14 tigris_0.7 units_0.5-1