



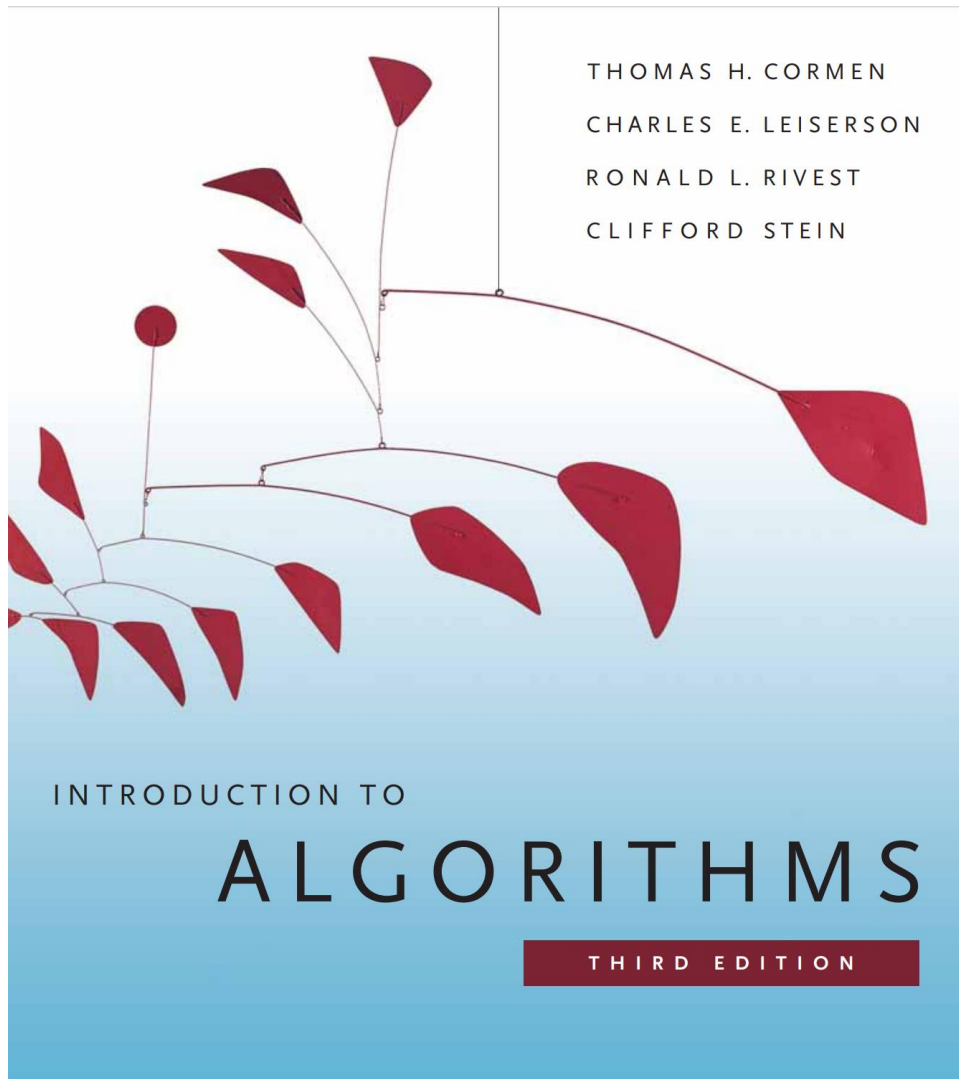
طراحی الگوریتم‌ها – جلسه اول

Introduction to Algorithm

مهدی جوانمردی

۱۴۰۱/۶/۲۷

کتاب مرجع درس طراحی الگوریتم

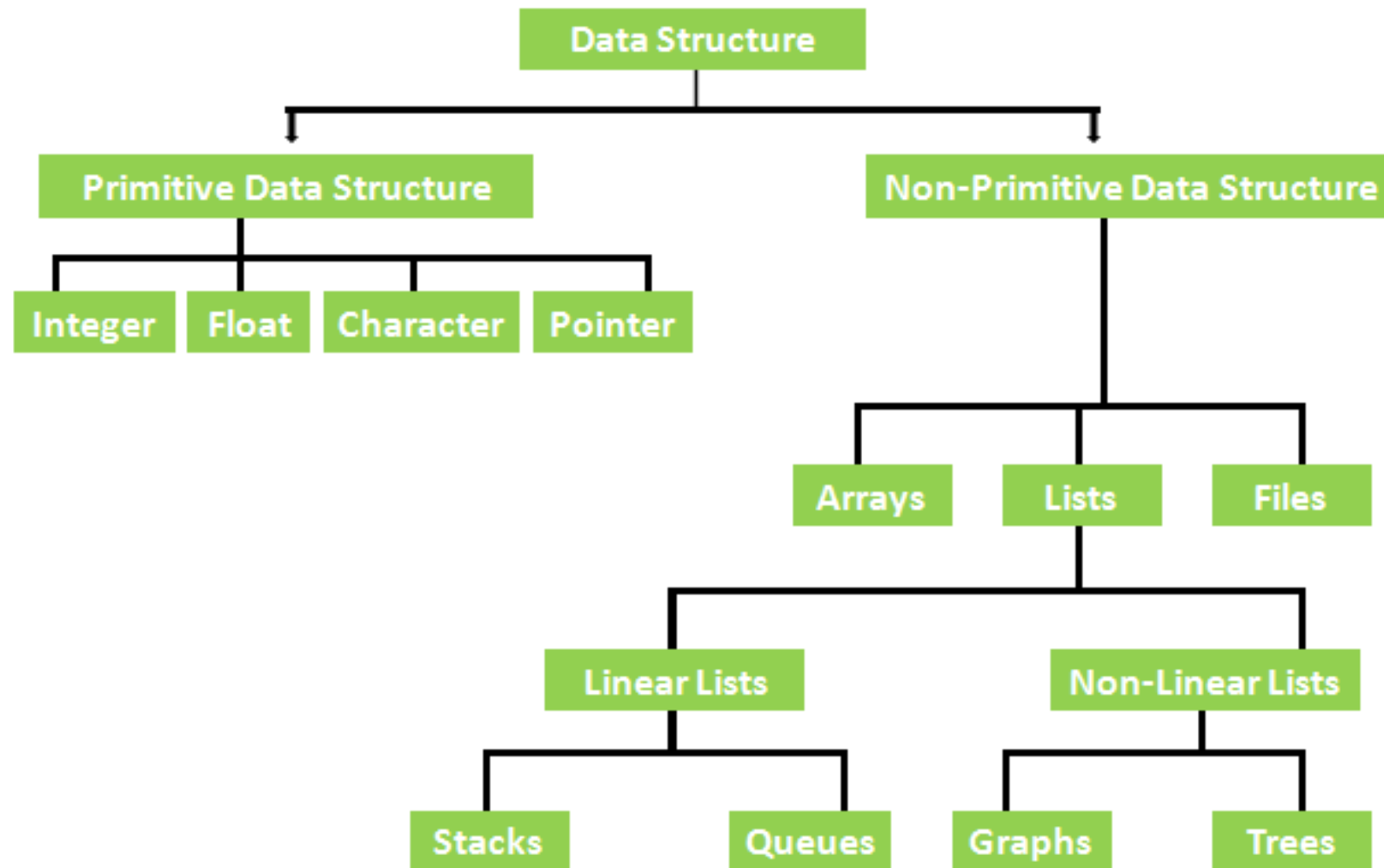


• کتاب Introduction to Algorithm معروف به CLRS

• ویرایش سوم کتاب

• لینک دانلود در سامانه قرار داده خواهد شد

انواع داده – ساختمان داده



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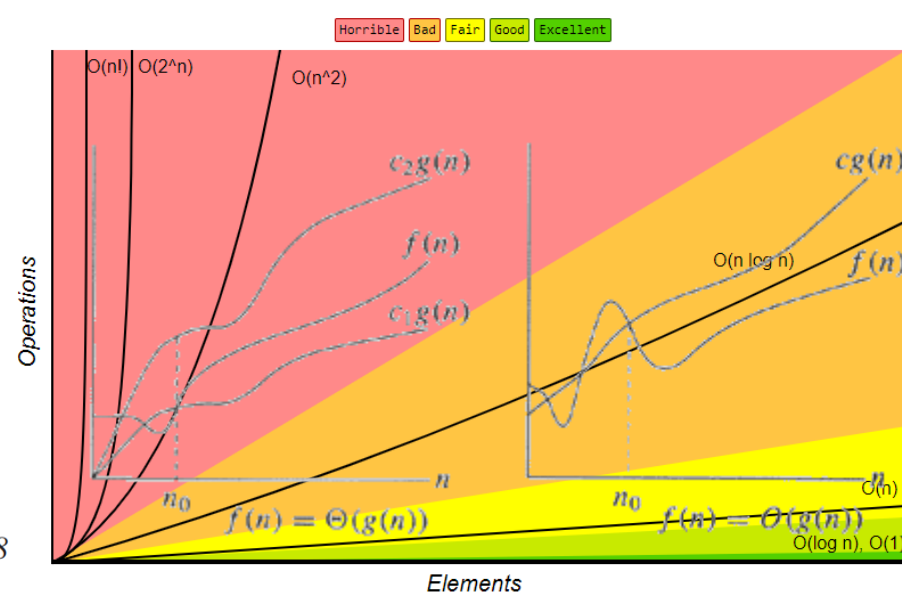
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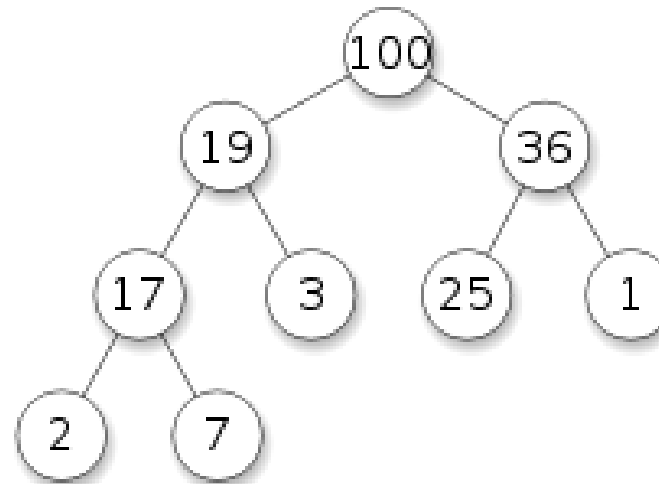
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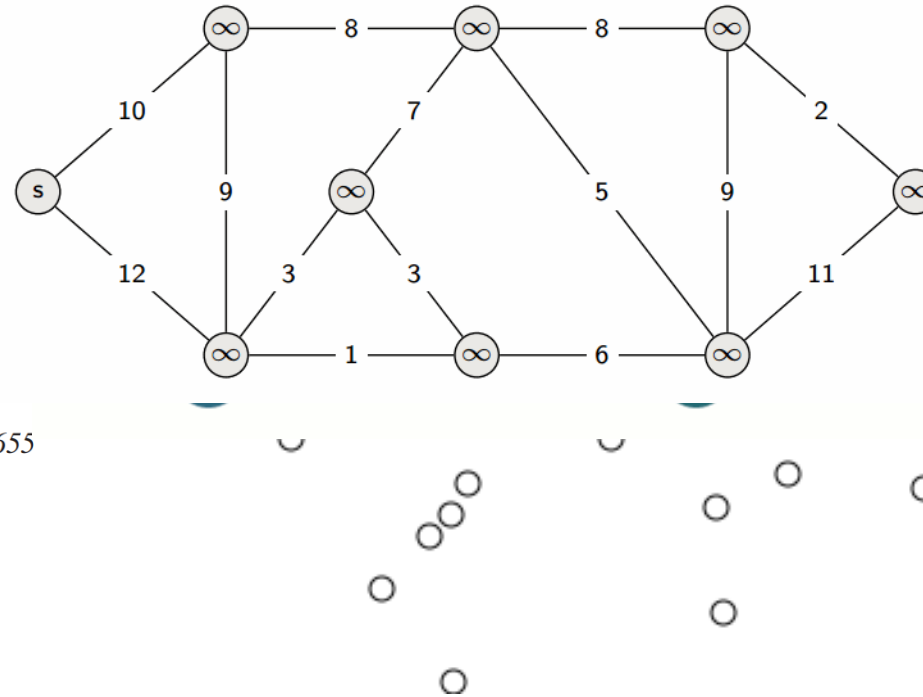
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- میان‌ترم ۷ نمره ----- فصل‌های ۱، ۲، ۳، ۴، ۶ و ۷، ۸، ۹، ۱۵ و ۱۶ کتاب
- پایان ترم ۷ نمره ----- تا فصل ۲۶ کتاب

حل تمرین و اطلاع رسانی

- حل تمرین تا هفته آینده تعیین خواهد شد
- کلاس حل تمرین جداگانه برگزار میشود

سوالات ضروری: mjavan@aut.ac.ir

کانال تلگرام برای اطلاع رسانی‌ها: t.me/aut_ce_algorithm

Instructor



Mahdi Javanmardi

email: mjavan@aut.ac.ir | office: 4th floor CE department

Courses:

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