

Brief Article

The Author

Variable 1 (U) $U : Type$.

Definition 1 (Ensemble) $Ensemble := U \Rightarrow Prop$.

Definition 2 (In) $In(A : Ensemble)(x : U) := Ax$.

Notation 1 ("x") $"x \in A" := (In Ax)(at level 10)$.

Definition 3 (Included) $Included(BC : Ensemble) : Prop := \forall x : U, x \in B \Rightarrow x \in C$.

Notation 2 ("A") $"A \subseteq B" := (Included AB)(at level 10)$.

Definition 4 (Union) $Union(BC : Ensemble) : Ensemble := fun x : U => (x \in B) \vee (x \in C)$.

Notation 3 ("A") $"A \cup B" := (Union AB)(at level 8)$.

Definition 5 (Intersection) $Intersection(BC : Ensemble) : Ensemble := fun x : U => (x \in B) \wedge (x \in C)$.

Notation 4 ("A") $"A \cap B" := (Intersection AB)(at level 10)$.

Variable 2 (Beings:Set.) $Beings : Set$.

Variables 1 (Babies) $Babies Illogical ManageCroc Despised : Beings \Rightarrow Prop$.

Notation 5 ("x") $"x'is'a'Baby'" := (Babies x)(at level 10)$.

Notation 6 ("x") $"x'is'illogical'" := (Illogical x)(at level 10)$.

Notation 7 ("x") $"x'is'despised'" := (Despised x)(at level 10)$.

Notation 8 ("x) "*x'can''manage''crocodiles''*" := (*ManageCroc x*) (at level 10).

Axiom 1 (BI:) $BI : \forall x, x \text{ is a Baby} \Rightarrow x \text{ is illogical}.$

Axiom 2 (MND) $MND : \forall x, x \text{ can manage crocodiles} \Rightarrow \text{not}(x \text{ is despised}).$

Axiom 3 (ID:) $ID : \forall x, x \text{ is illogical} \Rightarrow x \text{ is despised}.$

Lemma 1 (LcBabies) $LcBabies : \forall x, x \text{ is a Baby} \Rightarrow \text{not}(x \text{ can manage crocodiles}).$

Proof: In order to show $\forall x : Beings, (x \text{ is a Baby}) \Rightarrow (\text{not}(x \text{ can manage crocodiles}))$ we pick an arbitrary

$$x$$

and show

$$(x \text{ is a Baby}) \Rightarrow (\text{not}(x \text{ can manage crocodiles})).$$

We will assume

$$Hyp : x \text{ is a Baby}$$

and show

$$\text{not}(x \text{ can manage crocodiles}).$$

Using the definition not, our conclusion becomes

$$(x \text{ can manage crocodiles}) \Rightarrow \text{False}.$$

We will assume

$$Hyp0 : x \text{ can manage crocodiles}$$

and show

$$\text{False}.$$

Claim

$$x \text{ is illogical}.$$

Let us prove that.

By *BI*, in order to prove *x is illogical* it suffices to prove

$$x \text{ is a Baby}.$$

x is a Baby follows trivially from the assumptions.

and therefore we have proved *x is illogical*. *H* and (*IDx*) imply

$$H0 : x \text{ is despised}.$$

$Hyp0$ and $(MNDx)$ imply

$$H1 : not(xisdespised).$$

By $H1$, in order to prove $False$ it suffices to prove

$$xisdespised.$$

$xisdespised$ follows trivially from the assumptions.

We have showed that if

$$Hyp0 : xcanmanagecrocodiles$$

then

$$False$$

a proof of $(xcanmanagecrocodiles) \Rightarrow False$.

Therefore we have showed

$$(xcanmanagecrocodiles) \Rightarrow False$$

and so $not(xcanmanagecrocodiles)$.

We have showed that if

$$Hyp : xisaBaby$$

then

$$not(xcanmanagecrocodiles)$$

a proof of $(xisaBaby) \Rightarrow (not(xcanmanagecrocodiles))$.

Since

$$x$$

was arbitrary this shows $\forall x : Beings, (xisaBaby) \Rightarrow (not(xcanmanagecrocodiles))$. This is done