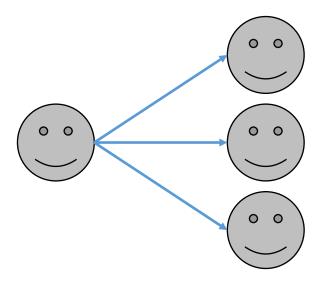
# R<sub>o</sub> or R<sub>e</sub> or Doubling-Time: Which to Follow?

CA-ANG/SG

25 March 2020

R = reproduction number

= average number cases arising from one case



$$R = 3$$

R = reproduction number

= average number cases arising from one case

This number changes as the epidemic progresses

As people recover, more of the population is immune to the virus. The virus has a harder time spreading. R decreases.

# $R_{C}$

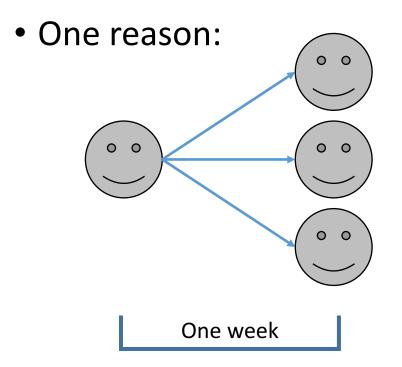
= initial reproduction number(at beginning of epidemic)

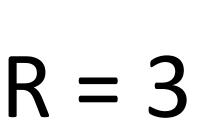
 $R_e$ 

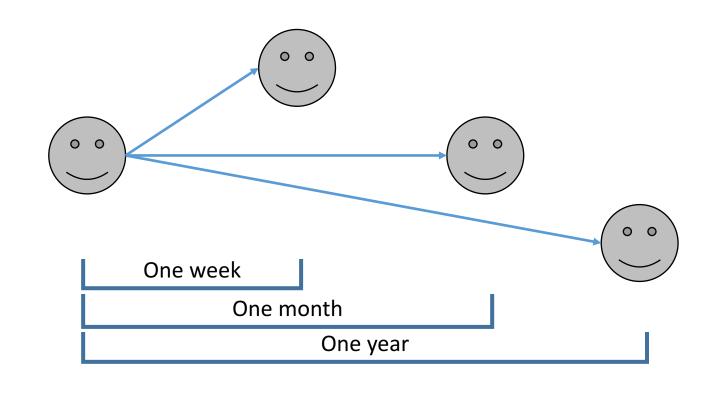
= effective reproduction number (at later times in the epidemic)

- Generally  $R_0 > R_e$
- Generally R<sub>e</sub> falls as epidemic progresses
- $\bullet$  Epidemic ends when  $R_e < 1$ : spread is no longer exponential

## R<sub>0</sub> & R<sub>e</sub>: Hard to Measure, Sometimes Misleading







$$R = 3$$

### Yes, R<sub>0</sub> and two more quantities define epidemic

And it should be obvious that:

$$I_{total} = \int_{t=0}^{t=\infty} \left[ \frac{R_0}{(1+d)^t} \right]^t dt$$

$$I_{total} = \frac{\exp\left(\frac{\ln(R_o)^2}{4\ln(1+d)}\right)\sqrt{\frac{\pi}{\ln(1+d)}}}{2} \bullet \left[erf(x-\mu)\sqrt{\ln(1+d)} - erf(-\mu)\sqrt{\ln(1+d)}\right]$$

Where

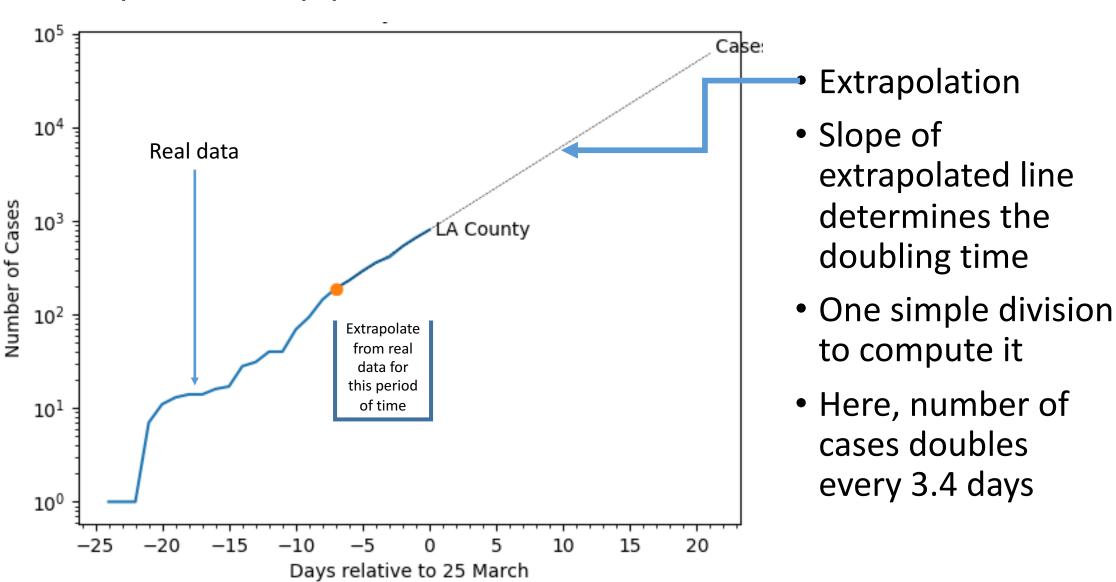
$$\mu = \frac{\ln(R_0)}{2\ln(1+d)}$$

#### "Doubling Time" is a simpler way

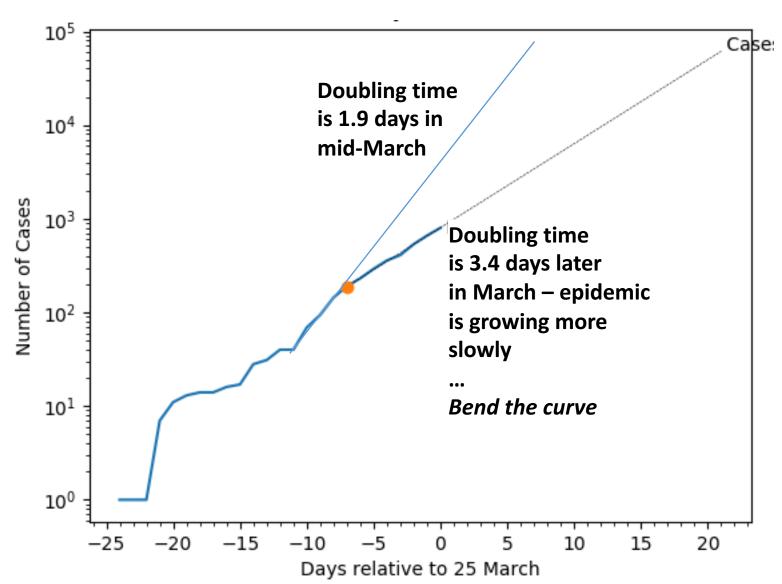
- Graph the number of total cases over the course of the epidemic
- Extrapolate from the last few days of the curve
- From this extrapolation, calculate how long it will take for the number of cases to double
  - This is the "doubling time"

#### Graphical approach

(note logarithmic y-axis)



#### Doubling Time changes during epidemic



#### Governor Cuomo uses doubling times



#### PLAN OF ACTION

Evidence suggests density control plan working:

- Sunday: hospitalizations doubling every 2 days
- Monday: hospitalizations doubling every 3.4 days
- Tuesday: hospitalizations doubling every 4.7 days

#### Summary

- R<sub>0</sub> is good for describing early stages of epidemic
- R<sub>e</sub> is hard to know

- Doubling time
  - Is easy to calculate
  - Has an easily understood meaning
  - Is well-suited to making decisions

#### References

- The monster equation
  - https://journals.plos.org/plosone/article?id=10.1371/journal.pone.0083622