Another application of the multivariable minimizer is to convexify a function. Suppose we have a function.

$$f(x) = x^4 - x^2/2 + x/3 \tag{1}$$

2

3

The following function is the convexified version of it

0

-2

0

x

1

$$F(x) = \inf_{x_1 < x < x_2} \left[f(x_1) + \frac{f(x_2) - f(x_1)}{x_2 - x_1} (x - x_1) \right]$$

$$40$$

$$20$$

$$50$$

$$20$$

-50

-2

-1

0

 \boldsymbol{x}

2

1

3