Tutorial for Beam-forming

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[1] Application

Horizontal slowness (ray parameter) of some phase and back-azimuth of events can be constrained using beam-forming if the geometry of seismic array we use is perfect. Here we say delta-shaped, cross-shaped, circle-shaped and so on.

[2] Basic Principles

Before our journey of executing beam-forming, you need to master its basic principles. To know more details, please reference to the review paper: *ARRAY SEISMOLOGY: METHOD AND APPLICATIONS* by Sebastian Rost and Christine Thomas, 2002.

[3] Data preparation

SAC format files should be prepared and the latitudes (header variation "stla" saved in SAC format file) and longitudes (header variation "stlo" saved in SAC format file) are valid.

[4] Dependencies

- a. Linux or Mac OS platform;
- b. SAC (Seismic Analysis Code) with version 101.6a, here, to execute band-pass filter;
- c. GMT (the Generic Mapping Tools) with marjor version 5, here 5.3.1, to virtualize the outputting results.

[5] Executing Beam-forming

Execute command "make" to compile executable command "beamforming" in current directory. Usage is showed as below,

```
beamforming <sacfile.lst> <t1> <t2> <fre low> <fre high> <slow low>
<slow high> <slow step> <baz step> <output file>
<sacfile.lst>
              File containing names of SAC format files;
<t1>
               Beginning time of cutting SAC files;
<t2>
                Ending time of cutting SAC files;
<fre low>
                Low limitation frequency of band-pass filtering (Hz);
               High limitation frequency of band-pass filtering (Hz);
<fre high>
<slow low>
                Low limitation of horizontal slowness scanning (second/degree);
<slow high>
                High limitation of horizontal slowness scanning (second/degree);
               Step length of scanning horizontal slowness; (second/degree)
<slow step>
<br/>
<br/>
daz step>
               Step length of back-azimuth scanning (degree);
               File name of outputting results containing 3 columns:
<output file>
                col1: back-azimuth col2: slowness col3: cross-coefficient.
```

[6] Executing Example

a. Seismic stations used are showed in Figure 1.

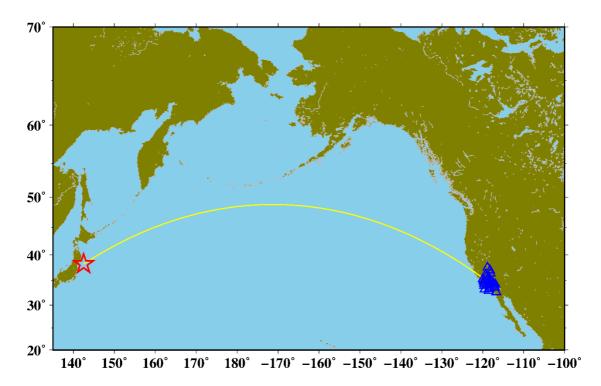


Figure 1. Seismic stations (indicated by blue triangles), array center (denoted with magenta solid circle) and hypocenter (indicated by red solid star).

b. SAC format files are plotted with varying distances in Figure 2.

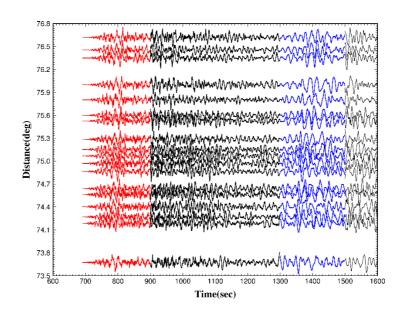


Figure 2. Two time segments (indicated by red and blue solid curves, respectively) are used to execute beam-forming.

c. Theoretical travel times and ray parameters is computed with iasp91 1-D model (Figure 3).

odel: iasp91								
Distance	Depth	Phase	Travel	Ray Param	Takeoff	Incident	Purist	Puri
(deg)	(km)	Name	Time (s)	p (s/deg)	(deg)	(deg)	Distance	Name
74.98	19.7	Р	699.89	5.777	17.59	17.54	74.98	= P
74.98	19.7	PcP	713.37	4.303	13.01	12.97	74.98	= PcP
74.98	19.7	PKiKP	1050.25	1.478	4.44	4.42	74.98	= PKiK
74.98	19.7	S	1277.15	11.127	19.71	19.65	74.98	= S
74.98	19.7	SKS	1307.03	7.341	12.86	12.82	74.98	= SKS
74.98	19.7	ScS	1310.81	8.032	14.09	14.05	74.98	= ScS
74.98	19.7	SKiKS	1477.86	1.593	2.77	2.76	74.98	= SKiK

Figure 3. Theoretical travel times and ray parameters of corresponding seismic phases computed under1-D iasp91 model.

d. Executing results of different time segments (Figure 4).

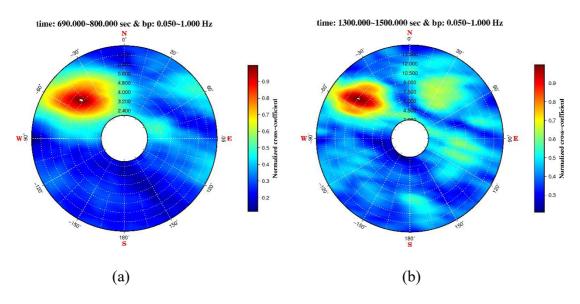


Figure 4. Beam-forming results. (a) Result with a time window of 690-800 seconds and a band-pass of 0.05-1 Hz. (b) Result with a time window of 1300-1500 seconds and a band-pass of 0.05-1 Hz.