

Tutorial for Beam-forming

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[1] Application

Horizontal slowness (ray parameter) of some phase and back-azimuth of events can be constrained using beam-forming if the geometry of seismic array we use is perfect. Here we say delta-shaped, cross-shaped, circle-shaped and so on.

[2] Basic Principles

Before our journey of executing beam-forming, you need to master its basic principles. To know more details, please reference to the review paper: *ARRAY SEISMOLOGY: METHOD AND APPLICATIONS* by Sebastian Rost and Christine Thomas, 2002.

[3] Data preparation

SAC format files should be prepared and the latitudes (header variation “stla” saved in SAC format file) and longitudes (header variation “stlo” saved in SAC format file) are valid.

[4] Dependencies

- a. Linux or Mac OS platform;
- b. SAC (Seismic Analysis Code) with version 101.6a, here, to execute band-pass filter;
- c. GMT (the Generic Mapping Tools) with major version 5, here 5.3.1, to virtualize the outputting results.

[5] Executing Beam-forming

Execute command “make” to compile executable command “beamforming” in current directory. Usage is showed as below,

```
beamforming <sacfile.lst> <t1> <t2> <fre_low> <fre_high> <slow_low>  
<slow_high> <slow_step> <baz_step> <output_file>
```

<sacfile.lst> File containing names of SAC format files;

<t1> Beginning time of cutting SAC files;

<t2> Ending time of cutting SAC files;

<fre_low> Low limitation frequency of band-pass filtering (Hz);

<fre_high> High limitation frequency of band-pass filtering (Hz);

<slow_low> Low limitation of horizontal slowness scanning (second/degree);

<slow_high> High limitation of horizontal slowness scanning (second/degree);

<slow_step> Step length of scanning horizontal slowness; (second/degree)

<baz_step> Step length of back-azimuth scanning (degree);

<output_file> File name of outputting results containing 3 columns:

col1: back-azimuth col2: slowness col3: cross-coefficient.

[6] Executing Example

a. Seismic stations used are showed in Figure 1.

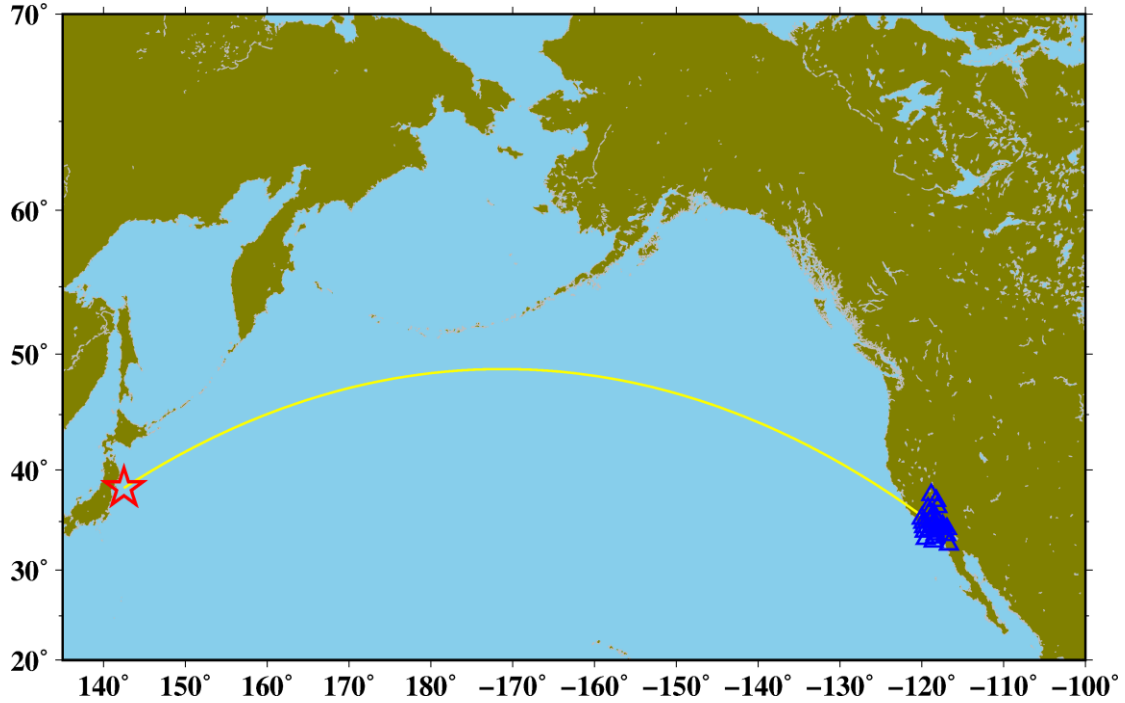


Figure 1. Seismic stations (indicated by blue triangles), array center (denoted with magenta solid circle) and hypocenter (indicated by red solid star).

b. SAC format files are plotted with varying distances in Figure 2.

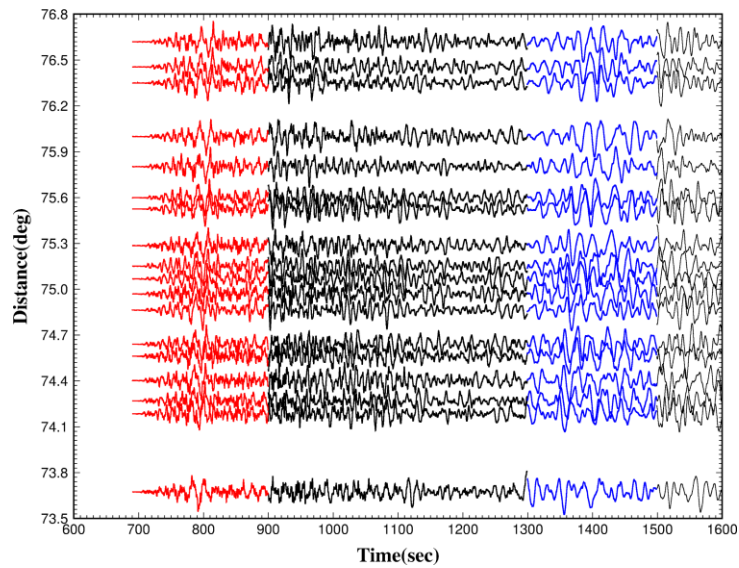


Figure 2. Two time segments (indicated by red and blue solid curves, respectively) are used to execute beam-forming.

c. Theoretical travel times and ray parameters is computed with iasp91 1-D model (Figure 3).

```
[$]taup_time -h 19.7 -mod prem -evt 38.29630 142.498 -sta 34.9454 -118.936
```

Model: prem									
Distance (deg)	Depth (km)	Phase Name	Travel Time (s)	Ray Param p (s/deg)	Takeoff (deg)	Incident (deg)	Purist Distance	Purist Name	
74.98	19.7	P	698.55	5.758	20.68	17.48	74.98	=	P
74.98	19.7	PcP	712.02	4.292	15.26	12.94	74.98	=	PcP
74.98	19.7	PKiKP	1048.00	1.482	5.22	4.43	74.98	=	PKiKP
74.98	19.7	S	1276.13	11.091	22.97	18.61	74.98	=	S
74.98	19.7	SKS	1305.78	7.256	14.79	12.05	74.98	=	SKS
74.98	19.7	ScS	1310.42	8.031	16.41	13.36	74.98	=	ScS
74.98	19.7	SKiKS	1476.53	1.597	3.22	2.63	74.98	=	SKiKS

Figure 3. Theoretical travel times and ray parameters of corresponding seismic phases computed with 1-D iasp91 model.

d. Executing results of different time segments (Figure 4).

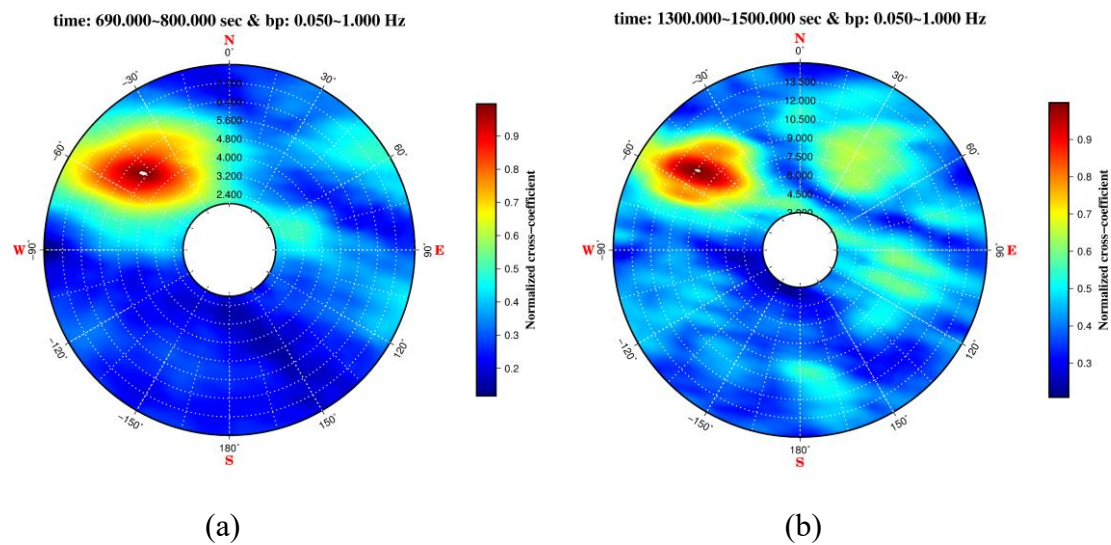


Figure 4. Beam-forming results. (a) Result with a time window of 690 – 800 seconds and a band-pass of 0.05 – 1 Hz. (b) Result with a time window of 1300 – 1500 seconds and a band-pass of 0.05 – 1 Hz.