# Applicative Functors Hidden in plain view...

Jim Powers

NYC Functional Programming Meetup
25 October 2011

```
buildName :: String \rightarrow Maybe String \rightarrow String buildName f m l = f ++ " " ++ (maybe "" id m) ++ " " ++ 1
```

```
buildName :: String -> Maybe String -> String -> String buildName f m l = f ++ " " ++ (maybe "" id m) ++ " " ++ 1
```

### Won't compile:

```
desired :: Maybe String -> Maybe String -> Maybe String desired f m 1 = buildName <$> f <$> (Just m) <$> 1
```

```
buildName :: String -> Maybe String -> String -> String buildName f m l = f ++ " " ++ (maybe "" id m) ++ " " ++ l
```

### Won't compile:

```
desired :: Maybe String -> Maybe String -> Maybe String desired f m 1 = buildName <$> f <$> (Just m) <$> 1
```

#### Not bad:

```
nice :: Maybe String -> Maybe String -> Maybe String
nice f m 1 = do
    fn <- f
    ln <- 1
    return $ buildName fn m ln</pre>
```

#### FUNCTIONAL PEARL

### Applicative programming with effects

CONOR MCBRIDE University of Nottingham

 $\begin{array}{c} {\rm ROSS~PATERSON} \\ {\rm City~University,~London} \end{array}$ 

#### Abstract

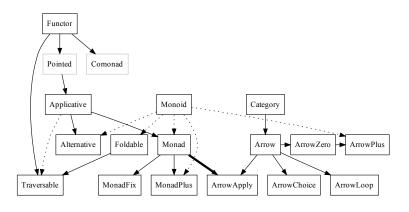
In this paper, we introduce Applicative functors—an abstract characterisation of an applicative style of effectful programming, weaker than Monads and hence more widespread. Indeed, it is the ubiquity of this programming pattern that drew us to the abstraction. We retrace our steps in this paper, introducing the applicative pattern by diverse examples, then abstracting it to define the Applicative type class and introducing a bracket notation which interprets the normal application syntax in the idiom of an Applicative functor. Further, we develop the properties of applicative functors and the generic operations they support. We close by identifying the categorical structure of applicative functors and examining their relationship both with Monads and with Arrows.

Applicative?

- Applicative?
- ► Functors?

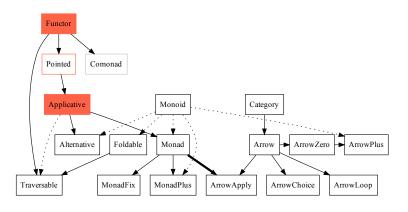
- Applicative?
- ► Functors?
- ▶ Effects?

# Family Tree



Typeclassopedia, Brent Yorgey, TMR-issue13

# Family Tree



Typeclassopedia, Brent Yorgey, TMR-issue13

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b

(<$>) = fmap
```

**Functors** enable performing a computation within a context. The function does not know anything about the context it is running in.

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b

(<$>) = fmap
```

#### Functor Laws

```
fmap id = id
fmap (g . h) = fmap g . fmap h
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

```
instance Functor Maybe where
  fmap _ Nothing = Nothing
  fmap f (Just x) = Just (f x)
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b

(<$>) = fmap
```

#### Common Functor Instances

```
instance Functor Maybe where
  fmap _ Nothing = Nothing
  fmap f (Just x) = Just (f x)
```

```
mFunc :: (Show a, Show b) => (a -> b) -> Maybe a -> Maybe b mFunc f x = f <$> x
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

```
instance Functor [] where
fmap = map
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

#### Common Functor Instances

```
instance Functor [] where
fmap = map
```

```
lFunc :: (Show a, Show b) => (a \rightarrow b) \rightarrow [a] \rightarrow [b]
lFunc f x = f <$> x
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

```
instance Functor (Either b) where
fmap f (Left 1) = Left 1
fmap f (Right r) = Right (f r)
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b

(<$>) = fmap
```

#### Common Functor Instances

```
instance Functor (Either b) where
fmap f (Left 1) = Left 1
fmap f (Right r) = Right (f r)
```

```
eFunc :: (Show a, Show c) => (a -> c) -> (Either [String] a) -> (Either [String] c) eFunc f x = f <$> x
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

```
instance Functor ((->) t) where
fmap f g = f . g
```

```
class Functor f where
  fmap :: (a -> b) -> f a -> f b

(<$>) :: Functor f => (a -> b) -> f a -> f b
(<$>) = fmap
```

#### Common Functor Instances

```
instance Functor ((->) t) where
fmap f g = f . g
```

```
fFunc :: (Show a, Show b, Show c) => (b -> c) -> (a -> b) -> (a -> c) fFunc f x = f <$> x
```

# Pointed

class Functor f => Pointed f where
 pure :: a -> f a

# **Pointed**

```
class Functor f => Pointed f where
  pure :: a -> f a
```

The **Pointed** typeclass is not represented in the Haskell standard library by itself. Conceptually, **Pointed** presents the ability to **lift** an ordinary value into a context, thus creating a **point** in that context.

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

The **Applicative** combines that ability to create a **point** within a context, as well as the ability to apply a **lifted** function within that context.

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

The **Applicative** combines that ability to create a **point** within a context, as well as the ability to apply a **lifted** function within that context.

Each context expresses how to apply the lifted function in its own particular way. Also known as its **idiom**.

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

#### Applicative Laws

```
fmap g x = pure g <*> x
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

```
instance Applicative Maybe where
  pure = return
  (<*>) = ap
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

#### Common Functor Instances

```
instance Applicative Maybe where
  pure = return
  (<*>) = ap
```

```
mAplic :: (a \rightarrow b) \rightarrow Maybe a \rightarrow Maybe b mAplic f x = pure f <*> x
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

```
instance Applicative [] where
  pure = return
  (<*>) = ap
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

#### Common Functor Instances

```
instance Applicative [] where
  pure = return
  (<*>) = ap
```

```
lAplic :: (Show a, Show b) => (a -> b) -> [a] -> [b] lAplic f x = pure f <*> x
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

#### Common Functor Instances

```
eAplic :: (Show a, Show c) => (a -> c) -> (Either [String] a) -> (Either [String] c) eAplic f x = pure f <*> x
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

```
instance Applicative ((->) a) where
  pure = const
  (<*>) f g x = f x (g x)
```

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

#### Common Functor Instances

```
instance Applicative ((->) a) where
  pure = const
  (<*>) f g x = f x (g x)
```

```
fAplic :: (Show a, Show b, Show c) => (b -> c) -> (a -> b) -> (a -> c) fAplic f x = pure f <*> x
```

```
buildName :: String -> Maybe String -> String -> String buildName f m l = f ++ " " ++ (maybe "" id m) ++ " " ++ l
```

### Won't compile:

```
desired :: Maybe String -> Maybe String -> Maybe String desired f m 1 = buildName <$> f <$> (Just m) <$> 1
```

#### Not bad:

```
nice :: Maybe String -> Maybe String -> Maybe String
nice f m 1 = do
    fn <- f
    ln <- 1
    return $ buildName fn m ln</pre>
```

### Inspiration

```
buildName :: String -> Maybe String -> String -> String buildName f m l = f ++ " " ++ (maybe "" id m) ++ " " ++ l
```

#### Won't compile:

```
desired :: Maybe String -> Maybe String -> Maybe String desired f m 1 = buildName <$> f <$> (Just m) <$> 1
```

#### Not bad:

```
nice :: Maybe String -> Maybe String -> Maybe String
nice f m 1 = do
    fn <- f
    ln <- 1
    return $ buildName fn m ln</pre>
```

#### Sweet:

```
sweet :: Maybe String -> Maybe String -> Maybe String sweet f m 1 = buildName <f (pure m) <f 1
```

#### **Applicative**

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

**Applicatives** can be used as a tool to remove boilerplate!

#### **Applicative**

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

**Applicatives** can be used as a tool to remove boilerplate!

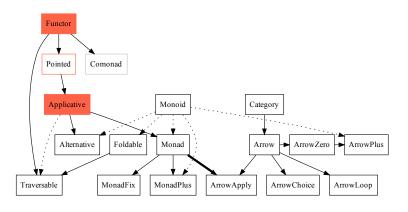
Orly? How?

### **Applicative**

```
class Functor f => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

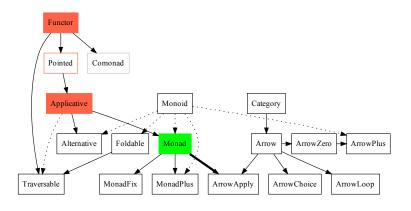
Predictable web example!

# Family Tree



Typeclassopedia, Brent Yorgey, TMR-issue13

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Typeclassopedia, Brent Yorgey, TMR-issue13

# Mo'nads!



http://twitpic.com/5j3x2t

```
import Data.List (lookup)
import Web.MaybeResult

type Request = [(String,String)]

required :: Request -> String -> MaybeResult String
required r k = maybe (failure $ "Required value for:"++k++" missing")
success (lookup k r)

opt :: Request -> String -> MaybeResult (Maybe String)
opt r k = success (lookup k r)
```

```
data ResponseValue = Value String
| Stream [String]
| deriving (Show)
```

type Response = MaybeResult ResponseValue

#### Reader Monad

```
newtype Reader r a = Reader {
 runReader :: r -> a
instance Monad (Reader r) where
 return a = Reader $ \ -> a
 m >>= k = Reader \$ \ r -> runReader (k (runReader m r)) r
myRequired :: String -> Reader Request (MaybeResult String)
myRequired k =
 asks (doRead k) >>= return
 where
   doRead k r = required r k
myOptional :: String -> Reader Request (MaybeResult (Maybe String))
myOptional k =
 asks (doRead k) >>= return
 where
   doRead k r = opt r k
```

```
goodRequest = [("first", "James"),("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

```
goodRequest = [("first", "James"), ("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

▶ => "Page rendered STRING: James Powers"

```
goodRequest = [("first", "James"),("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

- ▶ => "Page rendered STRING: James Powers"
- ► => "BZZT! Invalid request: [Required value for:last missing]"

```
goodRequest = [("first", "James"),("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

- ► => "Page rendered STRING: James Powers"
- ▶ => "BZZT! Invalid request: [Required value for:last missing]"
- ▶ => "BZZT! Invalid request: [Required value for:first missing]"

```
goodRequest = [("first", "James"),("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

- ▶ => "Page rendered STRING: James Powers"
- ► => "BZZT! Invalid request: [Required value for:last missing]"
- ► => "BZZT! Invalid request: [Required value for:first missing]"
- ▶ => Hrm...

```
data MaybeResult a = Failure [String]
                   I Success a
 deriving (Eq. Ord, Show, Data, Typeable)
instance Functor MaybeResult where
 fmap _ (Failure s) = Failure s
 fmap f (Success x) = Success (f x)
instance Applicative MaybeResult where
 pure = Success
 Failure e1 <*> Failure e2 = Failure (e1 ++ e2)
 Failure e1 <*> Success _ = Failure e1
 Success <*> Failure e2 = Failure e2
 Success f <*> Success a = Success (f a)
failure :: forall a. String -> MaybeResult a
failure s = Failure [s]
success :: forall a. a -> MaybeResult a
success s = Success s
```

```
handler :: Reader Request Response
handler = do
    name <- asks buildNamehandler
    return (fmap Value name)

buildNamehandler :: Request -> MaybeResult String
buildNamehandler r = buildName <$> (required r "first") <*> (opt r
"middle") <*> (required r "last")
```

```
goodRequest = [("first", "James"), ("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

▶ => "Page rendered STRING: James Powers"

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   putStrLn $ show $ browser goodRequest
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   putStrLn $ show $ browser badRequest
```

- ▶ => "Page rendered STRING: James Powers"
- ► => "BZZT! Invalid request: [Required value for:last missing]"

```
goodRequest = [("first", "James"),("last", "Powers")]
badRequest = [("first", "James")]
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main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

- ▶ => "Page rendered STRING: James Powers"
- ► => "BZZT! Invalid request: [Required value for:last missing]"
- ► => "BZZT! Invalid request: [Required value for:first missing,Required value for:last missing]"

```
goodRequest = [("first", "James"),("last", "Powers")]
badRequest = [("first", "James")]
badRequest1 = [("middle", "Matthew")]
main = do
   putStrLn $ show $ browser goodRequest
   putStrLn $ show $ browser badRequest
   putStrLn $ show $ browser badRequest
```

- ► => "Page rendered STRING: James Powers"
- ► => "BZZT! Invalid request: [Required value for:last missing]"
- ► => "BZZT! Invalid request: [Required value for:first missing,Required value for:last missing]"
- => Whoa! Now dats powah!

# Applicatives vs. Monads

Monads enable conditional (short-circuited) computation.

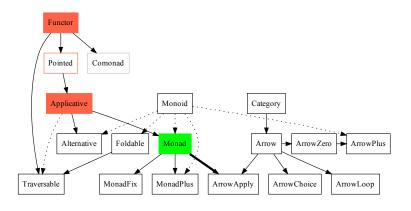
# Applicatives vs. Monads

- Monads enable conditional (short-circuited) computation.
- Monads can be stacked through monad transformers.

# Applicatives vs. Monads

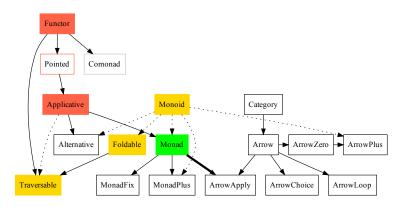
- Monads enable conditional (short-circuited) computation.
- Monads can be stacked through monad transformers.
- Monads are much more restrictive and hence less common.

# Family Tree



Typeclassopedia, Brent Yorgey, TMR-issue13

# Family Tree



Typeclassopedia, Brent Yorgey, TMR-issue13

#### Monoid

```
class Monoid a where
```

mempty :: a

mappend ::  $a \rightarrow a \rightarrow a$ 

#### **Foldable**

```
class Foldable t where
  fold :: Monoid m => t m -> m
  foldMap :: Monoid m => (a -> m) -> t a -> m
  foldr :: (a -> b -> b) -> b -> t a -> b
  foldl :: (a -> b -> a) -> a -> t b -> a
  foldr1 :: (a -> a -> a) -> t a -> a
  foldl1 :: (a -> a -> a) -> t a -> a
```

#### Must Read!

#### Functional Programming with Bananas, Lenses, Envelopes and Barbed Wire

Erik Meijer \* Maarten Fokkinga † Ross Paterson ‡

#### **Abstract**

We develop a calculus for lazy functional programming based on recursion operators associated with data type definitions. For these operators we derive various algebraic laws that are useful in deriving and manipulating programs. We shall show that all example functions in Bird and Wadler's "Introduction to Functional Programming" can be expressed using these operators.

Anamorphism

- Anamorphism
- Apomorphism

- Anamorphism
- Apomorphism
- Hylomorphism

- Anamorphism
- Apomorphism
- Hylomorphism
- Paramorphism

#### Must Read!

#### The Essence of the Iterator Pattern

Jeremy Gibbons and Bruno C. d. S. Oliveira Oxford University Computing Laboratory Wolfson Building, Parks Road, Oxford OX1 3QD, UK http://www.comlab.ox.ac.uk/jeremy.gibbons/ http://www.comlab.ox.ac.uk/bruno.oliveira/

#### Abstract

The ITERATOR pattern gives a clean interface for element-by-element access to a collection, independent of the collection's shape. Imperative iterations using the pattern have two simultaneous aspects: mapping and accumulating. Various existing functional models of iteration capture one or other of these aspects, but not both simultaneously. We argue that McBride and Paterson's applicative functors, and in particular the corresponding traverse operator, do exactly this, and therefore capture the essence of the ITERATOR pattern. Moreover, they do so in a way that nicely supports modular programming. We present some axioms for traversal, discuss modularity concerns, and illustrate with a simple example, the wordcount problem.

#### Traversable

```
class (Functor t, Foldable t) => Traversable t where
  traverse :: Applicative f => (a -> f b) -> t a -> f (t b)
  sequenceA :: Applicative f => t (f a) -> f (t a)
  mapM :: Monad m => (a -> m b) -> t a -> m (t b)
  sequence :: Monad m => t (m a) -> m (t a)
```

#### Traversable

```
class (Functor t, Foldable t) => Traversable t where traverse :: Applicative f => (a -> f b) -> t a -> f (t b) sequenceA :: Applicative f => t (f a) -> f (t a) mapM :: Monad m => (a -> m b) -> t a -> m (t b) sequence :: Monad m => t (m a) -> m (t a)
```

```
traverse id [Just 1, Just 2]
```

$$=>$$
 Just [1,2]

#### Traversable

```
class (Functor t, Foldable t) => Traversable t where
  traverse :: Applicative f => (a -> f b) -> t a -> f (t b)
  sequenceA :: Applicative f => t (f a) -> f (t a)
  mapM :: Monad m => (a -> m b) -> t a -> m (t b)
  sequence :: Monad m => t (m a) -> m (t a)
```

```
traverse id [Just 1, Just 2]
```

$$=>$$
 Just [1,2]

traverse id [Just 1, Nothing, Just 2]

=> Nothing