

$$R^*(s_1, s), i = \text{null}, u, v \neq \text{null}, \underline{i_1 \leq_1 u \leq_1 v} \Rightarrow v \leq u$$

from frame prop  $R \leq$  (extended)

$$Ax_0, R(s_0, s_1), \underline{i_1 \leq_0 u \leq_0 v} \Rightarrow \underline{i_1 \leq_1 u \leq_1 v}$$

general prop of TC (probably needs proof too)

$$\underline{i_0 \leq_0 u', u = n_0(u')} \Rightarrow \underline{n_0(i_0) \leq_0 u}$$

follows from def of  $R$

$$R(s_0, s_1) \Rightarrow \underline{i_1 = n_0(i_0)}$$

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$$R(s_0, s_1), R^*(s_1, s), i = \text{null}, u, v \neq \text{null}, \underline{i_0 \leq_0 u'}, \underline{u \leq_0 v} \Rightarrow v \leq u$$