

# {ordr}: Toward Tidy Principles for Matrix-Decomposed Data

## New Developments in Graphing Multivariate Data

Section on Statistical Graphics • Joint Statistical Meetings 2022

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# Acknowledgments

## Development

Emily Paul (UPenn)

## Discussion

Joyce Robbins (Columbia)

## Applications

Tom Agresta (UConn)

Ritchie Vaughan (UVA)

Martinna Bertolini (UFRJ)

Carol Mathews (UF)

## Land

Potano tribe ⊂ Timucua people

## Resources



## Slideshow

remark.js (Ole Petter Bang) + xaringan (Yihui Xie)

Catlab.jl (Evan Patterson &al)

Flaticon.com

# Prerequisites

# Singular value decomposition

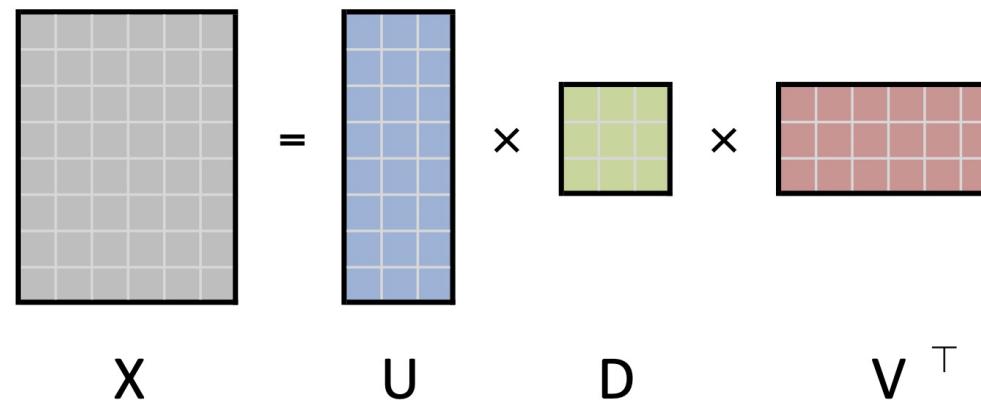
1. Data matrix  $X_{n \times p} \in \mathbb{R}^{n \times p}$

2. SVD into **inertia** and rotation matrices of left and right **singular vectors**:

$$X = U_{n \times k} D_{k \times k} V_{p \times k}^\top$$

3. Low-dimensional approximation via first  $r$  ordinates:

$$X \approx U_r D_r V_r^\top$$


$$X = U \times D \times V^\top$$

# Biplots

**Principal coordinates**  $F = UD$  or  $G = VD$  approximate the geometry of the rows or columns of  $X$ :

- Distances  $\|f_{j\bullet} - f_{i\bullet}\|$  approximate distances  $\sqrt{(x_{j1} - x_{i1})^2 + \dots + (x_{jp} - x_{ip})^2}$
- Inner products  $\frac{1}{n} g_{i\bullet} \cdot g_{j\bullet}$  approximate covariances  $\text{cov}(x_{\bullet i}, x_{\bullet j})$ 
  - Cosines  $\cos(\arg(g_{i\bullet}, g_{j\bullet}))$  approximate correlations  $\text{cor}(x_{\bullet i}, x_{\bullet j})$

**Standard coordinates**  $U$  or  $V$  pair with principal coordinates to recover the values of  $X$ :

- Inner products  $f_{i\bullet} \cdot v_{j\bullet}$  and  $u_{i\bullet} \cdot g_{j\bullet}$  approximate entries  $x_{ij}$

**Biplots** superimpose row and column coordinates with shares  $(a, b)$  of inertia:

$$\begin{bmatrix} U & D^a \\ V & D^b \end{bmatrix} \in \mathbb{R}^{(n+p) \times r}$$

# Biplots

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**Biplots** superimpose row and column coordinates with shares  $(a, b)$  of inertia:

$$\begin{bmatrix} U & D^a \\ V & D^b \end{bmatrix} \in \mathbb{R}^{(n+p) \times r}$$

Pick (at most) **two out of three**:

1. Approximate row geometry
2. Approximate column geometry
3. Approximate measured values

# Pitch: Principal components analysis

# PCA of Anderson's iris data

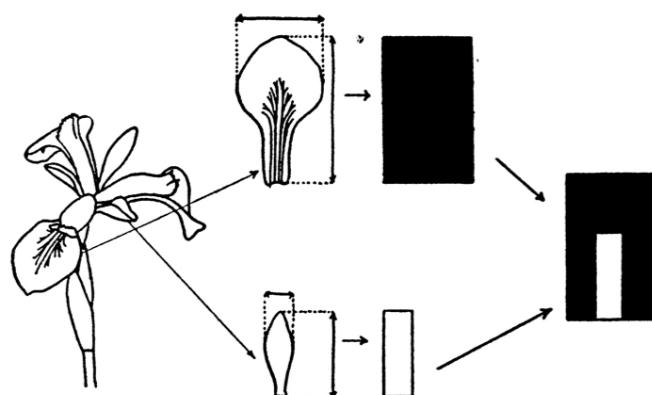
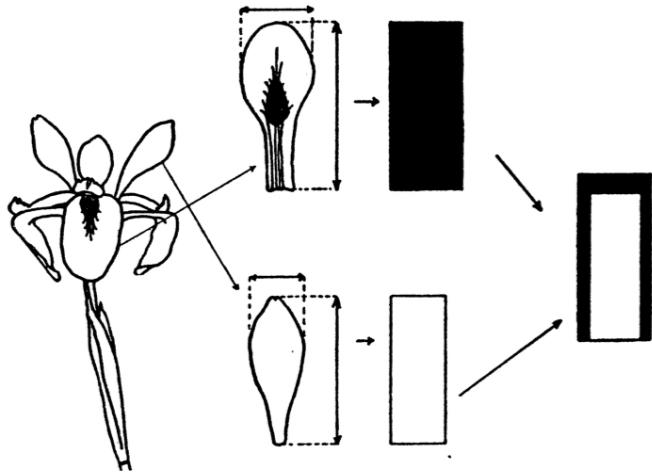


Fig. 8. Diagram illustrating how petal length and width, and sepal length and width are combined to form an ideograph. Above, *Iris virginica*; below, *I. versicolor*.

```
head(iris)
```

```
##   Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1      5.1       3.5       1.4       0.2  setosa
## 2      4.9       3.0       1.4       0.2  setosa
## 3      4.7       3.2       1.3       0.2  setosa
## 4      4.6       3.1       1.5       0.2  setosa
## 5      5.0       3.6       1.4       0.2  setosa
## 6      5.4       3.9       1.7       0.4  setosa
```

```
summary(iris)
```

```
##   Sepal.Length     Sepal.Width     Petal.Length     Petal.Width
## Min.   :4.300   Min.   :2.000   Min.   :1.000   Min.   :0.100
## 1st Qu.:5.100  1st Qu.:2.800  1st Qu.:1.600  1st Qu.:0.300
## Median :5.800  Median :3.000  Median :4.350  Median :1.300
## Mean    :5.843  Mean    :3.057  Mean    :3.758  Mean    :1.199
## 3rd Qu.:6.400  3rd Qu.:3.300  3rd Qu.:5.100  3rd Qu.:1.800
## Max.    :7.900  Max.    :4.400  Max.    :6.900  Max.    :2.500
## 
##   Species
##   setosa   :50
##   versicolor:50
##   virginica:50
## 
## 
```

# PCA of Anderson's iris data

```
(pca <- prcomp(iris[, 1:4]))
```

```
## Standard deviations (1, ..., p=4):  
## [1] 2.0562689 0.4926162 0.2796596 0.1543862  
##  
## Rotation (n x k) = (4 x 4):  
##          PC1       PC2       PC3       PC4  
## Sepal.Length 0.36138659 -0.65658877  0.58202985  0.3154872  
## Sepal.Width -0.08452251 -0.73016143 -0.59791083 -0.3197231  
## Petal.Length 0.85667061  0.17337266 -0.07623608 -0.4798390  
## Petal.Width  0.35828920  0.07548102 -0.54583143  0.7536574
```

```
(pca_ord <- ordinate(iris, prcomp, cols = 1:4))
```

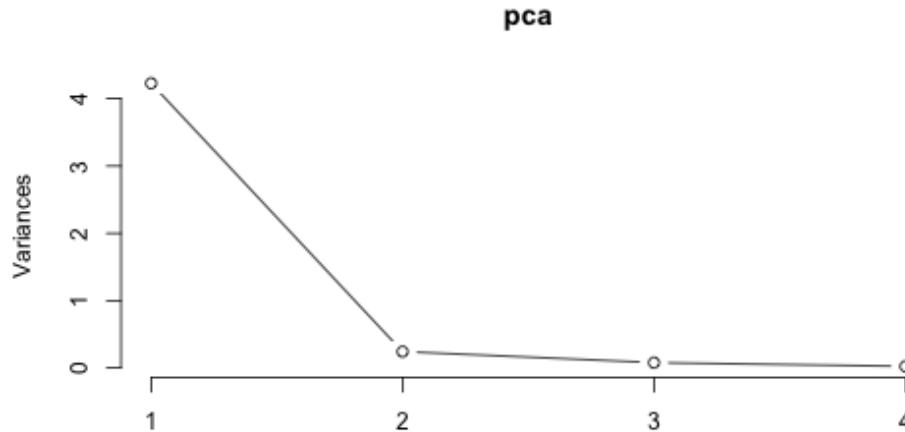
```
## # A tbl_ord of class 'prcomp': (150 x 4) x (4 x 4)'  
## # 4 coordinates: PC1, PC2, ..., PC4  
## #  
## # Rows (principal): [ 150 x 4 | 1 ]  
##   PC1     PC2     PC3 ... | Species  
##                           | <fct>  
## 1 -2.68 -0.319  0.0279 | 1 setosa  
## 2 -2.71  0.177  0.210  ... | 2 setosa  
## 3 -2.89  0.145 -0.0179 | 3 setosa  
## 4 -2.75  0.318 -0.0316 | 4 setosa  
## 5 -2.73 -0.327 -0.0901 | 5 setosa  
## # ... with 145 more rows  
## # i Use `print(n = ...)` to see more rows  
## #  
## # Columns (standard): [ 4 x 4 | 2 ]  
##   PC1     PC2     PC3 ... | .name      .center  
##                           | <chr>      <dbl>  
## 1  0.361  -0.657   0.582      | 1 Sepal.Length  5.84  
## 2 -0.0845 -0.730  -0.598  ... | 2 Sepal.Width  3.06  
## 3  0.857   0.173  -0.0762    | 3 Petal.Length 3.76  
## 4  0.358   0.0755 -0.546     | 4 Petal.Width  1.20
```

# PCA of Anderson's iris data

```
summary(pca)
```

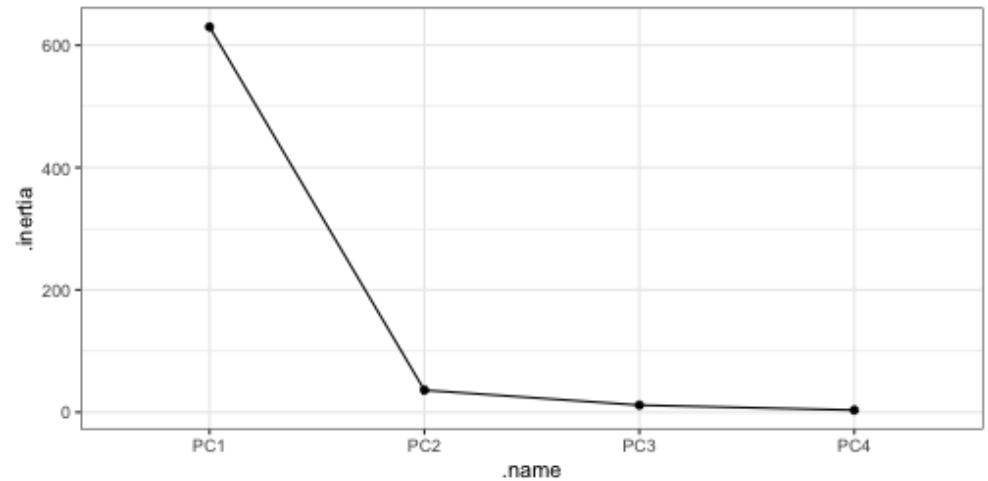
```
## Importance of components:  
##          PC1     PC2     PC3     PC4  
## Standard deviation 2.0563 0.49262 0.2797 0.15439  
## Proportion of Variance 0.9246 0.05307 0.0171 0.00521  
## Cumulative Proportion 0.9246 0.97769 0.9948 1.00000
```

```
screeplot(pca, type = "lines")
```



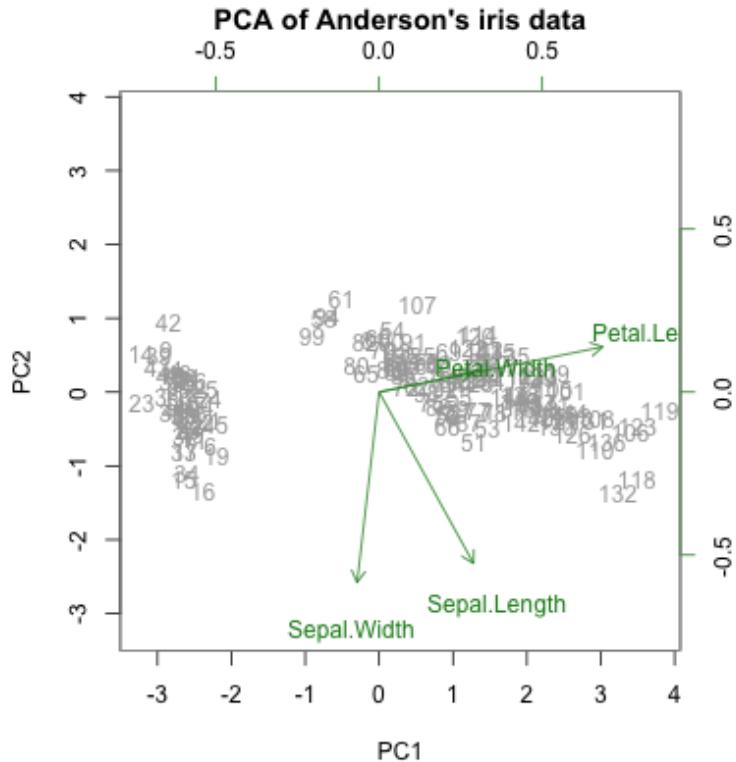
```
tidy(pca_ord) %>% print() %>%  
  ggplot(aes(x = .name, y = .inertia, group = 1)) +  
  geom_line() + geom_point()
```

```
## # A tibble: 4 × 4  
##   .name  .sdev  .inertia  .prop_var  
##   <fct>  <dbl>    <dbl>      <dbl>  
## 1 PC1    2.06    630.       0.925  
## 2 PC2    0.493   36.2       0.0531  
## 3 PC3    0.280   11.7       0.0171  
## 4 PC4    0.154    3.55      0.00521
```

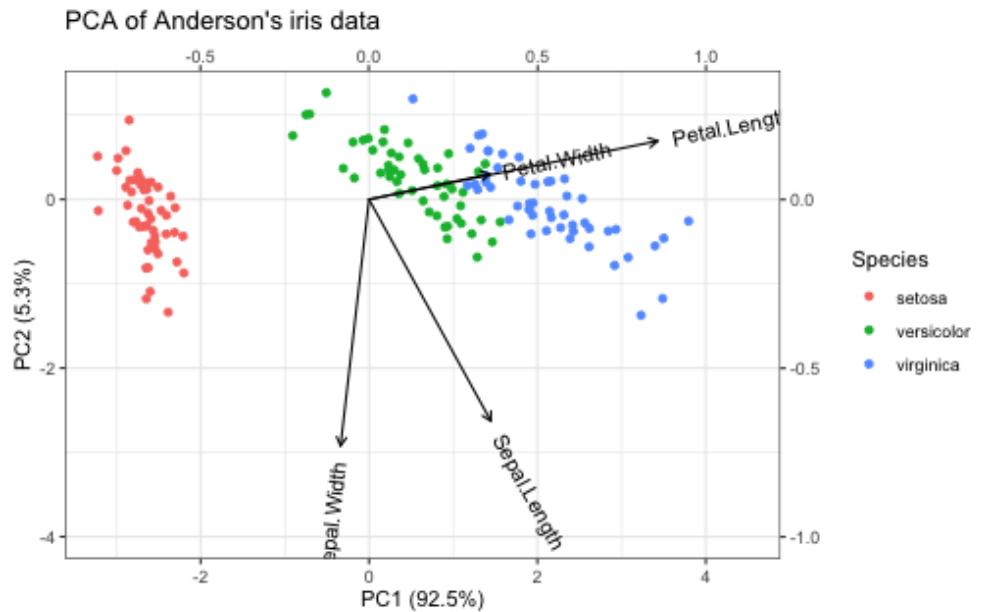


# PCA of Anderson's iris data

```
biplot(pca, scale = 0, col = c("darkgrey", "forestgreen")
       main = "PCA of Anderson's iris data")
```



```
pca_ord %>% confer_inertia("rows") %>%
  ggbioplot(aes(label = .name),
            sec.axes = "cols", scale.factor = 4) +
  geom_rows_point(aes(color = Species)) +
  geom_cols_vector() + geom_cols_text_radiate() +
  expand_limits(x = c(NA, 4.5), y = c(-4, NA)) +
  ggtitle("PCA of Anderson's iris data")
```

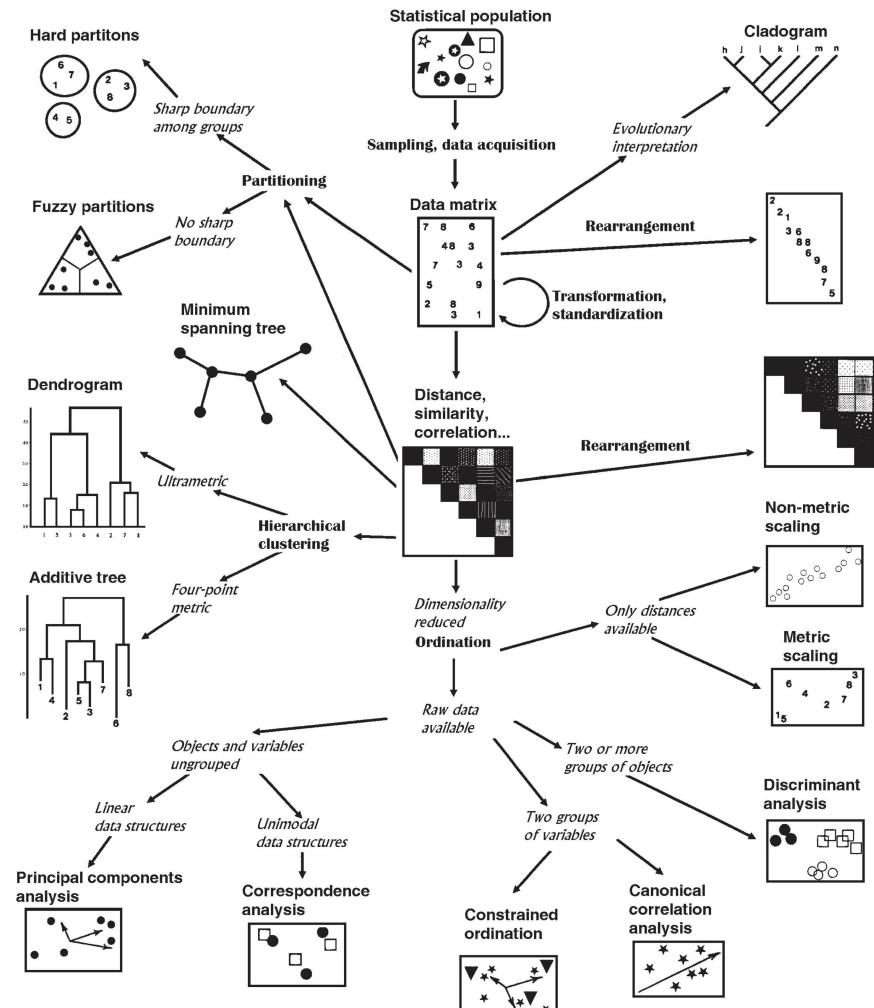


# Motivation

# Ordination

"[A]ny technique that extracts artificial variables in order to reduce the dimensionality of the data is referred to as **ordination**."<sup>1</sup>

		model	
		unsupervised	supervised
discrete	clustering	classification	
continuous	dimension reduction		regression



# Statement of need

R is replete with ordination methods!

## CRAN Task View: Multivariate Statistics

**Maintainer:** Paul Hewson

**Contact:** Paul.Hewson at plymouth.ac.uk

**Version:** 2014-09-19

## CRAN Task View: Analysis of Ecological and Environmental Data

**Maintainer:** Gavin Simpson

**Contact:** ucfagls at gmail.com

**Version:** 2014-05-31

... but they are

- **specialized:** unwieldy or unintuitive inspection
- **heterogeneous:** diverse, dissimilar conventions
- **standalone:** not designed to be interoperable

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- **specialized:** unwieldy or unintuitive inspection
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The tidyverse strives to be

- **human-centered:** supports data analysis conducted by humans
- **consistent:** ensures that learning transfers between packages
- **composable:** enables modular data exploration and study design
- **inclusive:** is developed and informed by a broad community of users



# Statement of purpose

*The {ordr} package leverages a **unifying framework** for matrix decomposition models and the **philosophy, conventions, and popularity** of the tidyverse in order to more **naturally** and **efficiently** integrate ordination analyses into **common** data science workflows.*

# Pitch: Correspondence analysis

# CA of Snee's hair and eye color data

The data in Table 3 are the observed frequencies of hair color (black, brunette, red, blond) and eye color (brown, blue, hazel, green) of 592 subjects. These data were collected, as part of a class project, by students in

TABLE 3  
HAIR COLOR - EYE COLOR DATA

Eye Color	Hair Color				Total
	Black	Brunette	Red	Blond	
Brown	68 .309*	119 .541	26 .118	7 .032	220 1.000
Blue	20 .093	84 .391	17 .079	94 .437	215 1.000
Hazel	15 .161	54 .581	14 .150	10 .108	93 1.000
Green	5 .078	29 .453	14 .219	16 .250	64 1.000

\*Proportion of total

an elementary statistics course taught by the author at the University of Delaware. The chi-squared statistic for Table 3 is 138.29 (9 df,  $p < .01$ ), indicating a significant correlation between hair color and eye color. In this problem it is of interest to determine which of the eye colors are producing the nonhomogeneity. The eigenvalue-eigenvector analysis (Table 4) indicated that the first two eigenvalues accounted for approximately 97 percent of the variation. The coordinates of

```
(haireye <- as.data.frame(rowSums(HairEyeColor, dims = 2L)))
```

```
##          Brown Blue Hazel Green
## Black      68   20    15     5
## Brown     119   84    54    29
## Red        26   17    14    14
## Blond       7   94    10    16
```

```
summary(HairEyeColor)
```

```
## Number of cases in table: 592
## Number of factors: 3
## Test for independence of all factors:
##     Chisq = 164.92, df = 24, p-value = 5.321e-23
## Chi-squared approximation may be incorrect
```

# CA of Snee's hair and eye color data

```
(ca <- MASS::corresp(haireye, nf = 2L))
```

```
## First canonical correlation(s): 0.4569165 0.1490859
## 
## Row scores:
##          [,1]      [,2]
## Black -1.1042772  1.4409170
## Brown -0.3244635 -0.2191109
## Red   -0.2834725 -2.1440145
## Blond  1.8282287  0.4667063
## 
## Column scores:
##          [,1]      [,2]
## Brown -1.0771283  0.5924202
## Blue   1.1980612  0.5564193
## Hazel -0.4652862 -1.1227826
## Green  0.3540108 -2.2741218
```

```
(ca_ord <- ordinate(haireye,
                      model = MASS::corresp, nf = 2L))
```

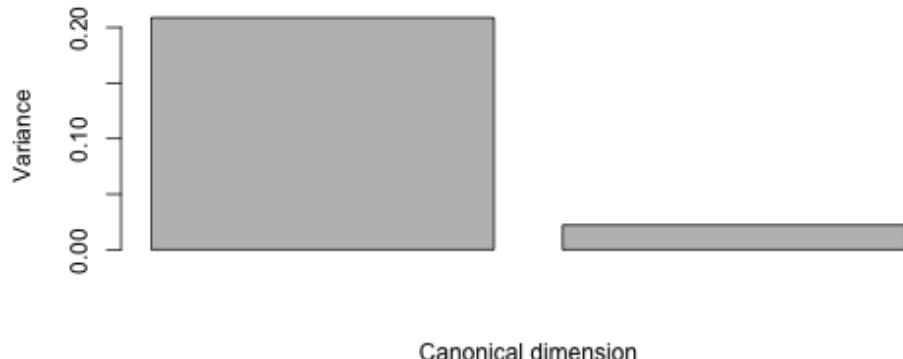
```
## # A tbl_ord of class 'correspondence': (4 x 2) x (4 x 2)'
## # 2 coordinates: Can1 and Can2
## #
## # Rows (standard): [ 4 x 2 | 1 ]
##     Can1   Can2 | .name
##             | <chr>
## 1 -1.10    1.44 | 1 Black
## 2 -0.324   -0.219 | 2 Brown
## 3 -0.283   -2.14 | 3 Red
## 4  1.83    0.467 | 4 Blond
## #
## # Columns (standard): [ 4 x 2 | 1 ]
##     Can1   Can2 | .name
##             | <chr>
## 1 -1.08    0.592 | 1 Brown
## 2  1.20    0.556 | 2 Blue
## 3 -0.465   -1.12 | 3 Hazel
## 4  0.354   -2.27 | 4 Green
```

# CA of Snee's hair and eye color data

```
summary(ca)
```

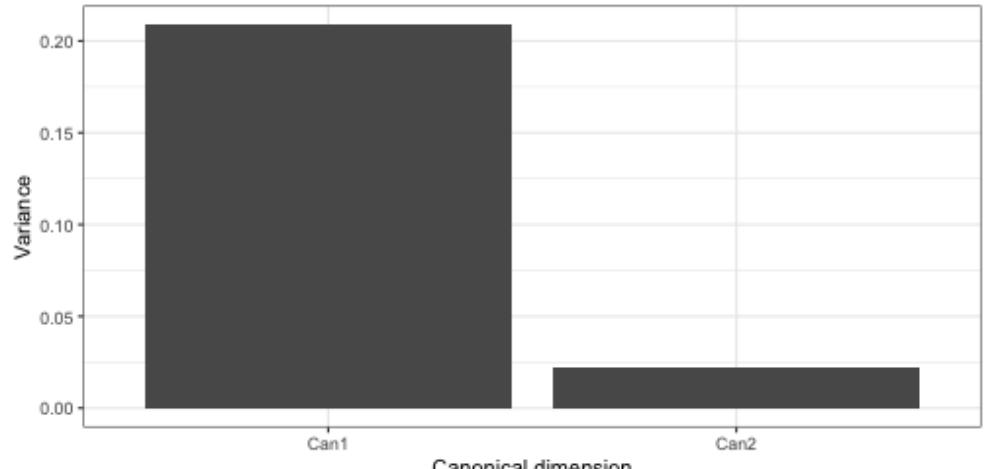
```
##          Length Class  Mode
## cor         2    -none- numeric
## rscore      8    -none- numeric
## cscore      8    -none- numeric
## Freq        16   -none- numeric
```

```
barplot(ca$cor^2,
        xlab = "Canonical dimension", ylab = "Variance")
```



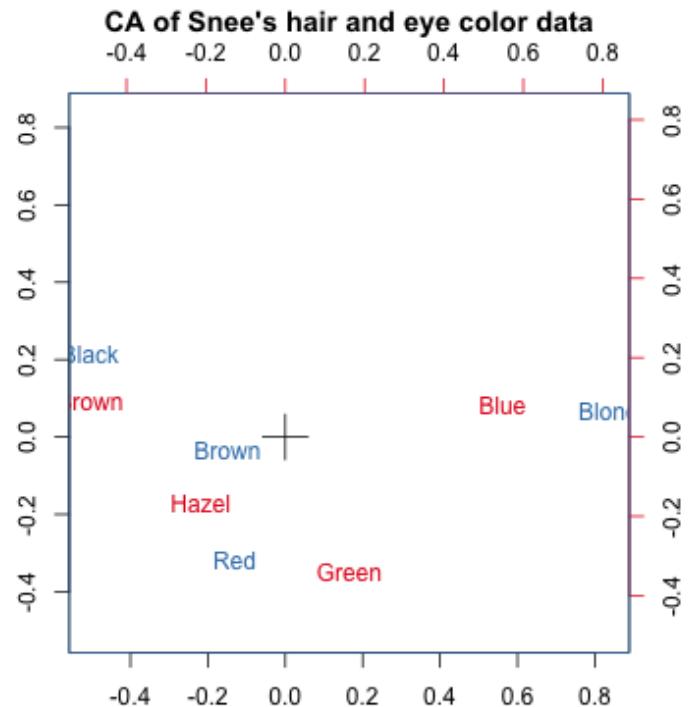
```
tidy(ca_ord) %>% print() %>%
  ggplot(aes(x = .name, y = .cor^2)) +
  geom_col() +
  labs(x = "Canonical dimension", y = "Variance")
```

```
## # A tibble: 2 × 4
##   .name   .cor .inertia .prop_var
##   <fct>  <dbl>    <dbl>     <dbl>
## 1 Can1   0.457    0.209     0.904
## 2 Can2   0.149    0.0222    0.0962
```

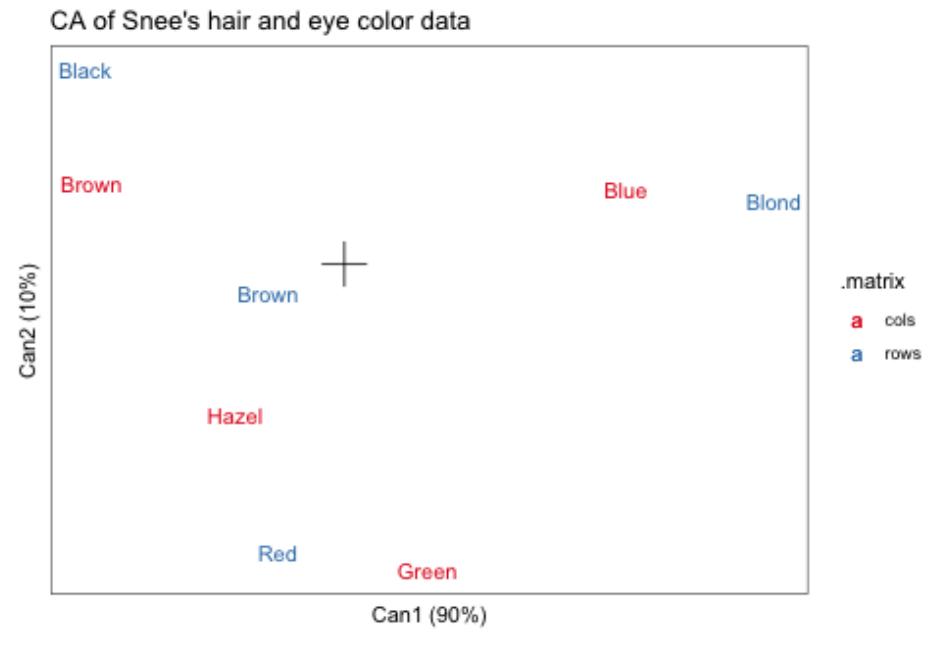


# CA of Snee's hair and eye color data

```
biplot(ca, type = "symmetric",
       col = c("#377eb8", "#e41a1c"),
       main = "CA of Snee's hair and eye color data")
```



```
ca_ord %>% confer_inertia("symmetric") %>%
  ggbioplot(aes(label = .name, color = .matrix)) +
  scale_color_brewer(type = "qual", palette = "Set1") +
  theme_biplot() + geom_origin() +
  geom_rows_text() + geom_cols_text() +
  ggtitle("CA of Snee's hair and eye color data")
```



# Design

# Principles

{ordr} strives for a coherent grammar<sup>2</sup> that is



## accessible

- easy to learn and straightforward to advance
- couples easily with other data science tools



## opinionated

- foregrounds the unity of supported techniques
- rewards good practice, relieves choice paralysis



## extensible

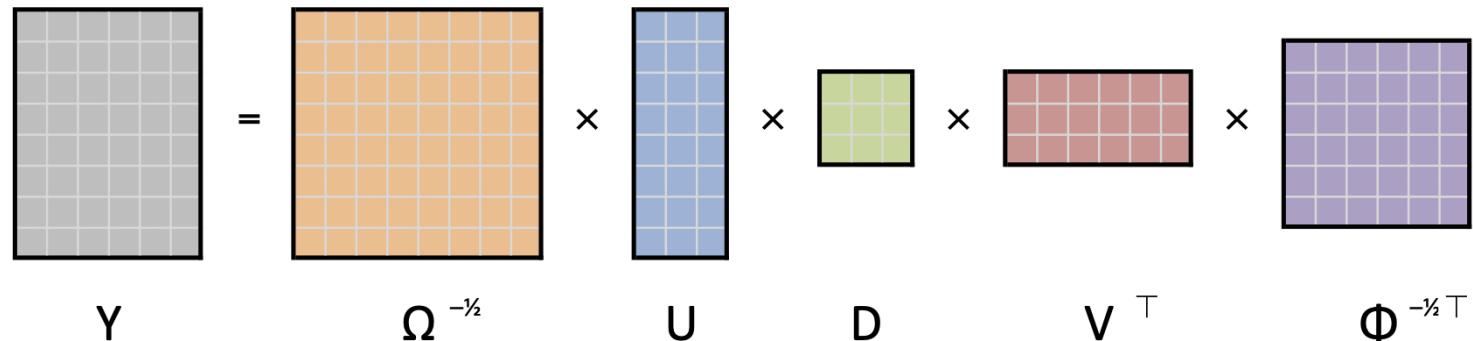
- relies on a small set of core generics
- borrows conventions from widely-used tools

# Inspiration

A general approach to ordination techniques:<sup>3</sup>

1. Preprocess data (centering; double-centering):  $X \rightsquigarrow Y$
2. Generalized SVD (weights; spherering):

$$Y = (\Omega^{-1/2} U) D (\Phi^{-1/2} V)^{\top}$$



3. Biplot, with  $a + b = 1$  (row-principal; column-principal; symmetric):

$$F = \Omega^{-1/2} U D^a, \quad G = \Phi^{-1/2} V D^b$$

# Core generics

## Engine

For each supported model class, **recover**:

- left & right matrix factors (singular vectors)

$$U, V$$

- inertia and its distribution unto the factors

$$D = \text{diag}(d_1, \dots, d_k), (a, b)$$

- supplementary elements

$$U D = X V, X' V, \text{ etc.}$$

- metadata about model components

# Core generics

## Engine

For each supported model class, **recover**:

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$$U D = X V, X' V, \text{ etc.}$$

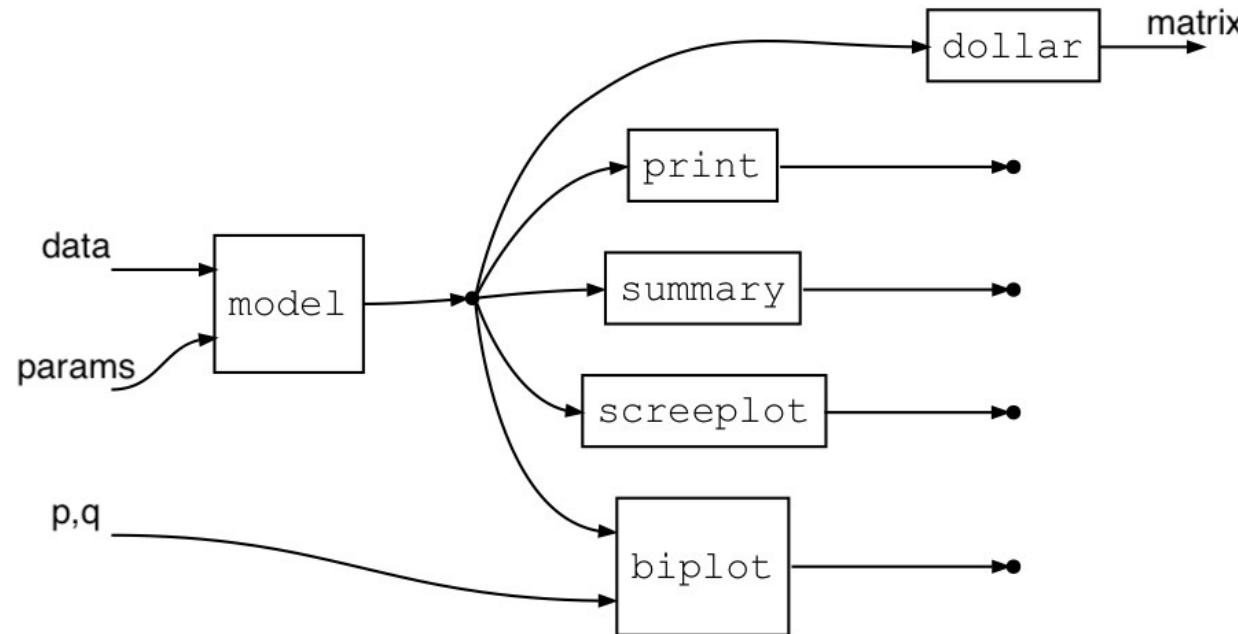
- metadata about model components

## Dashboard

Via the wrapper class `'tbl_ord'`, **enable**:<sup>4</sup>

- clear & consistent formatting via `{tibble}`
- re-distribution of inertia
- negations of axes
- annotation of components via `{dplyr}`
- summaries for further analysis via `{broom}`
- grammatical construction of biplots via `{ggplot2}`
- workflows via `{magrittr}` (or `|>` if one must)

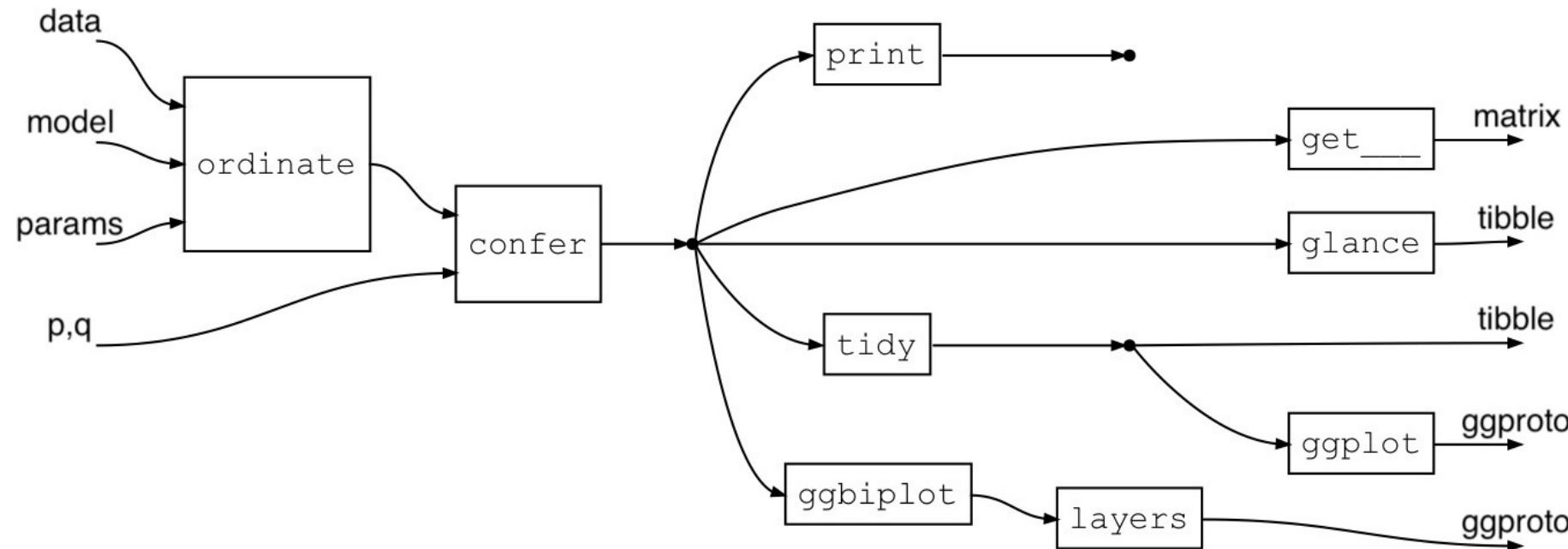
# Base R workflow



## Limitations

- idiosyncratic fit function and output class
- retrievable model components are nonstandard
- model summaries often have no class or methods
- (bi)plots offer limited customization and annotation

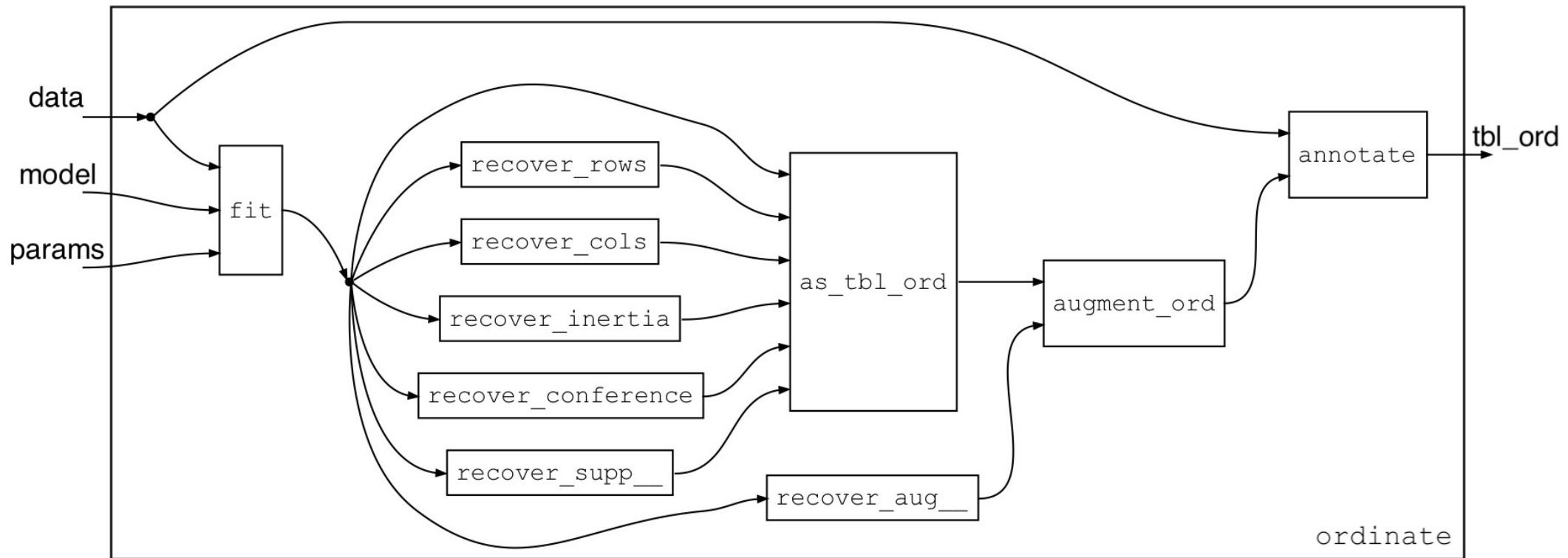
# {ordr} workflow: Dashboard



## Differences

- unified fit function and modifiable wrapper class
- retrieval methods for standard components
- model summaries are returned as data frames
- biplots can be layered

# {ordr} workflow: Engine



Wrapper `'tbl_ord'`

- connects underlying models to unified functions by way of recovery methods

Decorator `augment_ord()`

- annotates recovered model components with recovered metadata

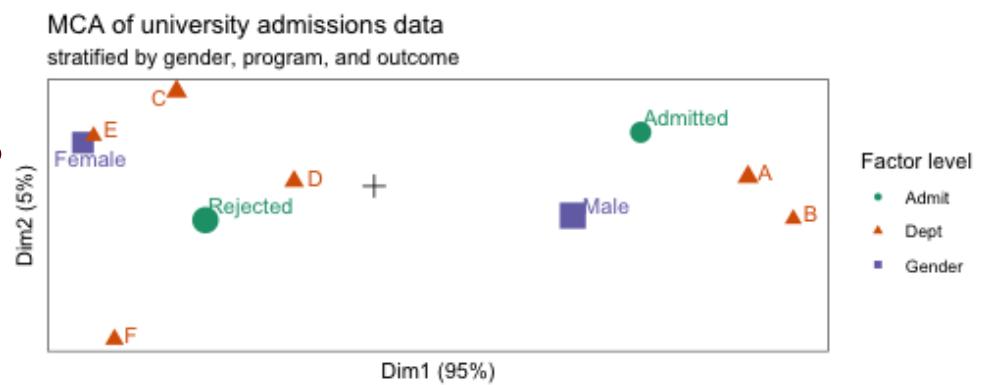
# Gallery

# Gallery: Multiple correspondence analysis of university admissions data

```
ca::mjca(UCBAmissions) %>%
  as_tbl_ord() %>% augment_ord() %>%
  print() -> admissions_mca

## # A tbl_ord of class 'mjca': (4526 x 2) x (10 x 2)
## # 2 coordinates: Dim1 and Dim2
## #
## # Rows (standard): [ 4526 x 2 | 4 ]
##   Dim1  Dim2 | .name   .mass   .dist
##             | <chr>   <dbl>   <dbl>
## 1  3.33  2.68 | 1 1    0.000221 0.00672
## 2  3.33  2.68 | 2 2    0.000221 0.00672
## 3  3.33  2.68 | 3 3    0.000221 0.00672
## 4  3.33  2.68 | 4 4    0.000221 0.00672
## 5  3.33  2.68 | 5 5    0.000221 0.00672
## # ... with 4,521 more rows, and
## #   1 more variable:
## #     .inertia <dbl>
## # i Use `print(n = ...)` to see more rows, and `colnames()` to
## #
## # Columns (standard): [ 10 x 2 | 6 ]
##   Dim1  Dim2 | .name .factor .level   .mass
##             | <chr> <chr>   <chr>   <dbl>
## 1  1.08  0.975 | 1 Admi... Admit  Admit... 0.129
## 2 -0.681 -0.617 | 2 Admi... Admit  Rejec... 0.204
## 3 -1.18  0.786 | 3 Gend... Gender  Female  0.135
## 4  0.802 -0.536 | 4 Gend... Gender  Male    0.198
```

```
admissions_mca %>%
  confer_inertia("colprincipal") %>%
  ggbiplot() + theme_biplot() + geom_origin() +
  geom_cols_point(aes(color = .factor, shape = .factor,
                       size = .mass)) +
  geom_cols_text_repel(aes(label = .level, color = .facto
                            show.legend = FALSE) +
  scale_color_brewer(palette = "Dark2") +
  scale_size_area(guide = "none") +
  labs(color = "Factor level", shape = "Factor level") +
  ggtitle("MCA of university admissions data",
          "stratified by gender, program, and outcome")
```



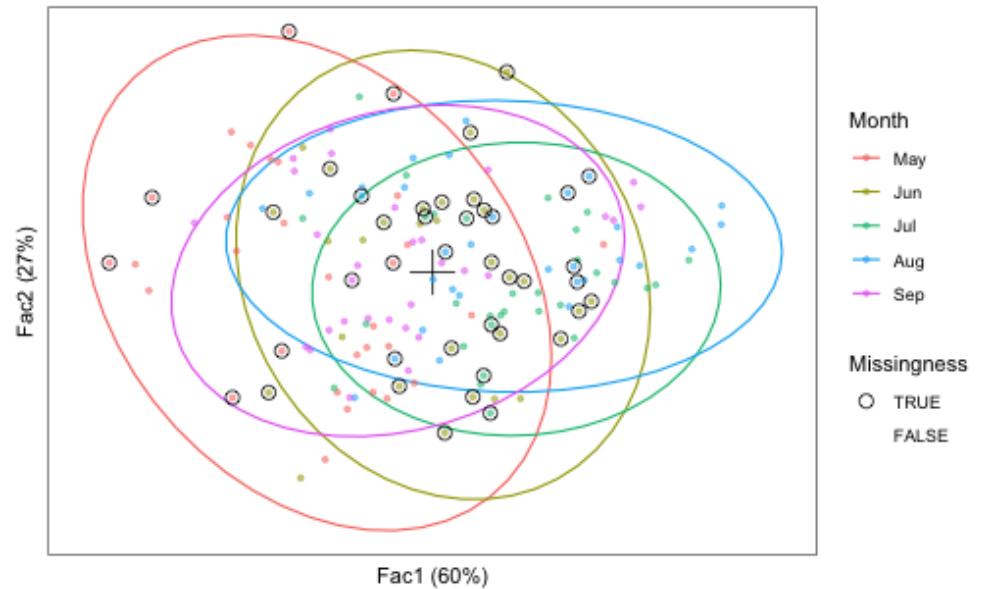
# Gallery: NIPALS of (incomplete) air quality data

```
ordinate(airquality, seq(4L), ade4::nipals, nf = 3L) %>%
  mutate_rows(
    Month = factor(month.abb[Month], levels = month.abb),
    Missingness = apply(is.na(airquality[, 1:4]), 1L, any)
  ) %>%
  print() -> airqual_nipals
```

```
## # A tbl_ord of class 'nipals': (153 x 3) x (4 x 3)'
## # 3 coordinates: Fac1, Fac2, Fac3
## #
## # Rows (principal): [ 153 x 3 | 4 ]
##   Fac1   Fac2   Fac3 | .name Month Day Missing...
##   <dbl> <dbl> <dbl> | <chr> <fct> <int> <lgl>
## 1 -0.305  0.334 -1.25 | 1 1     May    1 FALSE
## 2 -0.426  0.930 -0.501 | 2 2     May    2 FALSE
## 3 -1.27   -0.0592  0.279 | 3 3     May    3 FALSE
## 4 -1.16   -1.46   -1.44 | 4 4     May    4 FALSE
## 5 -3.41   0.906  -0.280 | 5 5     May    5 TRUE
## # ... with 148 more rows, and
## #   abbreviated variable name
## #   `Missingness'
## # i Use `print(n = ...)` to see more rows
## #
## # Columns (standard): [ 4 x 3 | 1 ]
##   Fac1   Fac2   Fac3 | .name
##   <dbl> <dbl> <dbl> | <chr>
## 1  0.582  0.0175  0.104 | 1 Ozone
```

```
airqual_nipals %>%
  ggbioplot() + theme_biplot() + geom_origin() +
  stat_rows_ellipse(aes(color = Month)) +
  geom_rows_point(aes(color = Month), size = 1, alpha = .5) +
  geom_rows_point(aes(shape = Missingness), size = 3) +
  scale_shape_manual(values = c(`TRUE` = 1L, `FALSE` = NA))
gtitle("PCA of 1973 air quality measurements")
```

PCA of 1973 air quality measurements

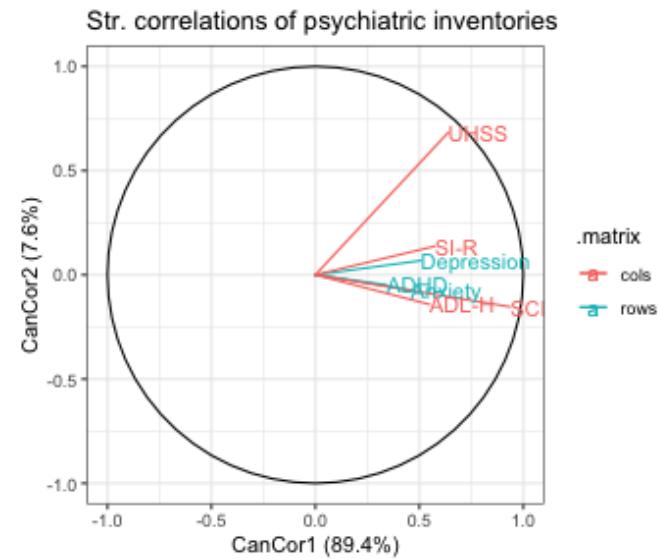


# Gallery: Canonical correlation analysis of psychiatric inventories

```
cca_ord <- cancor_ord(pred, resp, scores = TRUE)
(cca_ord <- augment_ord(as_tbl_ord(cca_ord)))

## # A tbl_ord of class 'cancor_ord': (322 x 3) x (324 x 3)'
## # 3 coordinates: CanCor1, CanCor2, CanCor3
## #
## # Rows (standard): [ 322 x 3 | 3 ]
##   CanCor1  CanCor2  CanCor3 | .name      .center .element
##                           | <chr>     <dbl> <chr>
## 1  0.00146 -0.00494 -0.00306 | 1 Anxiety      18.9 active
## 2  0.00264  0.00507 -0.000169 | 2 Depression    20.7 active
## 3  0.00143 -0.000979  0.00371 | 3 ADHD         38.0 active
## 4 -0.0307   0.00214  0.0151  | 4 <NA>          NA score
## 5  0.0263   0.148   -0.0476 | 5 <NA>          NA score
## # ... with 317 more rows
## # i Use `print(n = ...)` to see more rows
## #
## # Columns (standard): [ 324 x 3 | 3 ]
##   CanCor1  CanCor2  CanCor3 | .name .center .element
##                           | <chr>  <dbl> <chr>
## 1 -0.000433 -0.00240 -0.00560 | 1 SI-R      65.4 active
## 2  0.0208   -0.0303  -0.0176 | 2 ADL-H     2.13 active
## 3  0.00154  -0.000812  0.00120 | 3 SCI       100. active
## 4  0.00247   0.0136   0.00318 | 4 UHSS      30.0 active
## 5 -0.0510   -0.169   -0.0889 | 5 1          NA score
## # ... with 319 more rows
## # i Use `print(n = ...)` to see more rows
```

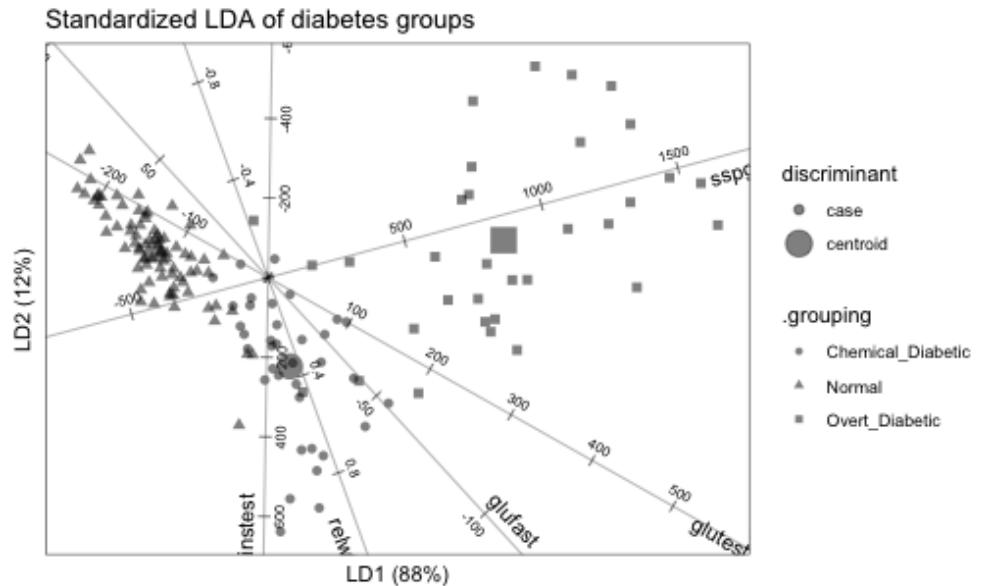
```
cca_ord %>% confer_inertia("rows") %>%
  ggbiplot(aes(label = .name, color = .matrix)) +
  geom_unit_circle() +
  geom_rows_vector(elements = "structure", arrow = NULL) +
  geom_cols_vector(elements = "structure", arrow = NULL) +
  geom_rows_text(elements = "structure", hjust = "outward") +
  geom_cols_text(elements = "structure", hjust = "outward") +
  expand_limits(x = c(-1, 1), y = c(-1, 1)) +
  ggtitle("Str. correlations of psychiatric inventories")
```



# Gallery: Linear discriminant analysis of diabetes data

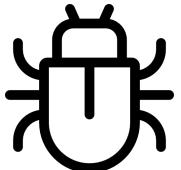
```
MASS::lda(group ~ ., heplots::Diabetes) %>%  
  as_tbl_ord() %>% augment_ord() %>%  
  mutate_rows(discriminant = ifelse(  
    .element == "active", "centroid", "case"  
) %>%  
  print() -> diabetes_lda  
  
## # A tbl_ord of class 'lda': (148 x 2) x (5 x 2)  
## # 2 coordinates: LD1 and LD2  
## #  
## # Rows (principal): [ 148 x 2 | 6 ]  
##   LD1     LD2 | .name .prior .counts .grou...  
##             | <chr> <dbl>   <int> <chr>  
## 1 -1.75  0.400 | 1 Norm...  0.524      76 Normal  
## 2  0.340 -1.38 | 2 Chem...  0.248      36 Chemic...  
## 3  3.66  0.580 | 3 Over...  0.228      33 Overt_...  
## 4 -1.72  0.663 | 4 1       NA        NA Normal  
## 5 -2.85  1.30  | 5 2       NA        NA Normal  
## # ... with 143 more rows, 2  
## #   more variables:  
## #   .element <chr>,  
## #   discriminant <chr>, and  
## #   abbreviated variable name  
## #   ^.grouping  
## # i Use `print(n = ...)` to see more rows, and `colnames()` to  
## #  
## # Columns (standard): [ 5 x 2 | 2 ]
```

```
diabetes_lda %>% confer_inertia(1) %>%  
  ggbioplot() + theme_bioplot() +  
  geom_rows_point(aes(shape = .grouping, size = discriminant,  
    alpha = .5)) +  
  geom_cols_axis(aes(label = .name),  
    color = "#888888", num = 8L,  
    text_size = 2.5, label_dodge = .02) +  
  ggtitle("Standardized LDA of diabetes groups")
```



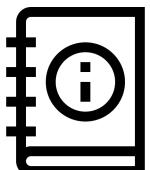
# Wrap

# Needs



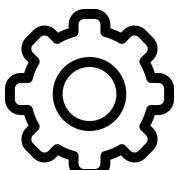
## Engagement

- bug & need reports
- use cases
- code contributions



## Documentation

- how to use {ordr} with **new model classes**
- how to use **new plot layers** with `ggbiplots()`



## Features

- quality measures
- predictive biplots<sup>5</sup>

# Welcome

Install `ordr`, and optionally methods for additional S3 classes:

```
remotes::install_github("corybrunson/ordr")
remotes::install_github("corybrunson/ordr.extra")
```

# Thank you!

- [1] Podani J • 2000 • *Introduction to the Exploration of Multivariate Biological Data* • <http://ramet.elte.hu/~podani/books.html>
- [2] Wilkinson L • 2005 • *The Grammar of Graphics* • <https://link.springer.com/book/10.1007/0-387-28695-0>
- [3] Greenacre M • 1984 • *Theory and applications of correspondence analysis* • <http://www.carme-n.org/>
- [4] Pedersen TL • 2022 • {tidygraph}: A Tidy API for Graph Manipulation • <https://CRAN.R-project.org/package=tidygraph>
- [5] Gower JC, Lubbe SG, le Roux NJ • 2011 • *Understanding Biplots* • <https://www.wiley.com/go/biplots>