

Breakpoint Billiards Rating System (BFRS)

The rating system is an **Elo-derived system** with several enhancements designed to provide fair and accurate player ratings.

Core Formula

1. Initial Rating

All players start at **500** (displayed as Breakpoint Level **5.0**)

2. Expected Win Probability (Elo Formula)

$$\text{Expected} = 1 / (1 + 10^{((\text{OpponentRating} - \text{PlayerRating}) / 400)})$$

3. K-Factor (Based on Experience Level)

The K-Factor determines how much a player's rating can change. Less experienced players have higher volatility:

Racks Played	K-Factor	Category
Under 100	28	Provisional
100–300	20	Established
Over 300	14	Stable

4. Base Rating Change

$$\text{BaseDelta} = K \times (\text{ActualOutcome} - \text{ExpectedWinProb})$$

Where `ActualOutcome` is **1** for a win, **0** for a loss

5. Opponent Strength Scaling

Players earn more for beating stronger opponents and less for beating weaker ones:

$$\text{Scale} = 1 + (\text{RatingDifference} / 1000)$$

- Clamped between **0.85** (beating weaker) and **1.15** (beating stronger)

6. Match Modifier (Margin of Victory)

Compares actual rack differential vs expected:

$$\text{Modifier} = 1 + ((\text{ActualRackDiff} - \text{ExpectedRackDiff}) / 20)$$

- Bonus/penalty of up to **±10%** based on performance vs expectations

7. Event Weighting

Event Type	Weight
League	1.0x

Playoffs	1.05x
Tournament	1.08x

Final Calculation

```
RatingChange = BaseDelta × OpponentScaling × MatchModifier × EventWeight
```

Display Conversion

The raw rating is converted to a "Breakpoint Level" for display:

```
BreakpointLevel = floor(rating / 10) / 10
```

A rating of **523** displays as **5.2**

Example: Rating 7.9 vs Rating 5.3

Players

- **Player A:** Breakpoint 7.9 (internal rating: **790**)
- **Player B:** Breakpoint 5.3 (internal rating: **530**)

Assumptions: League match, both players "Established" ($K = 20$)

Step 1: Expected Win Probability

$$\begin{aligned} \text{Expected_A} &= 1 / (1 + 10^{((530 - 790) / 400)}) \\ &= 1 / (1 + 10^{-0.65}) \\ &= 1 / (1 + 0.224) \\ &= 0.817 \text{ (81.7%)} \end{aligned}$$

$$\text{Expected_B} = 1 - 0.817 = 0.183 \text{ (18.3%)}$$

Player A is heavily favored with an 81.7% win expectation.

Step 2: Opponent Strength Scaling

$$\begin{aligned} \text{Scale_A} &= 1 + (530 - 790) / 1000 = 0.74 \rightarrow \text{capped at } 0.85 \\ \text{Scale_B} &= 1 + (790 - 530) / 1000 = 1.26 \rightarrow \text{capped at } 1.15 \end{aligned}$$

- Player A gets **lower scaling (0.85)** for beating a weaker opponent
- Player B gets **higher scaling (1.15)** for beating a stronger opponent

Scenario 1: Player A (7.9) Wins 7-4

Player A's Rating Change:

$$\text{BaseDelta_A} = 20 \times (1 - 0.817) = +3.66$$

$$\text{Scaled} = 3.66 \times 0.85 = +3.11$$

With match modifier = ~+3 points

Result: 790 → 793 (still 7.9)

Player B's Rating Change:

$$\text{BaseDelta}_B = 20 \times (0 - 0.183) = -3.66$$

$$\text{Scaled} = -3.66 \times 1.15 = -4.21$$

With match modifier = ~-4 points

Result: 530 → 526 (now 5.2)

Scenario 2: Player B (5.3) Upsets and Wins 7-5

Player B's Rating Change:

$$\text{BaseDelta}_B = 20 \times (1 - 0.183) = +16.34$$

$$\text{Scaled} = 16.34 \times 1.15 = +18.79$$

With match modifier = ~+21 points

Result: 530 → 551 (now 5.5!)

Player A's Rating Change:

$$\text{BaseDelta}_A = 20 \times (0 - 0.817) = -16.34$$

$$\text{Scaled} = -16.34 \times 0.85 = -13.89$$

With match modifier = ~-15 points

Result: 790 → 775 (now 7.7)

Summary Table

Outcome	Player A (7.9)	Player B (5.3)
A wins 7-4 (expected)	+3 pts → 7.9	-4 pts → 5.2
A wins 7-0 (dominant)	+5 pts → 7.9	-6 pts → 5.2
B wins 7-5 (upset!)	-15 pts → 7.7	+21 pts → 5.5
B wins 7-0 (blowout upset!)	-18 pts → 7.7	+25 pts → 5.7

Key Takeaways

1. **Beating weaker opponents = small gains** - Higher-rated players barely move for expected wins
2. **Upsets are rewarding** - Lower-rated players get massive points for beating higher-rated players
3. **Margin of victory matters** - Winning by more than expected adds up to 10% bonus
4. **The system protects higher-rated players** - Losses to strong upsets hurt less (0.85 scaling)
5. **Lower-rated players risk less** - Expected losses cost fewer points (they weren't favored anyway)