

# **Solitons**

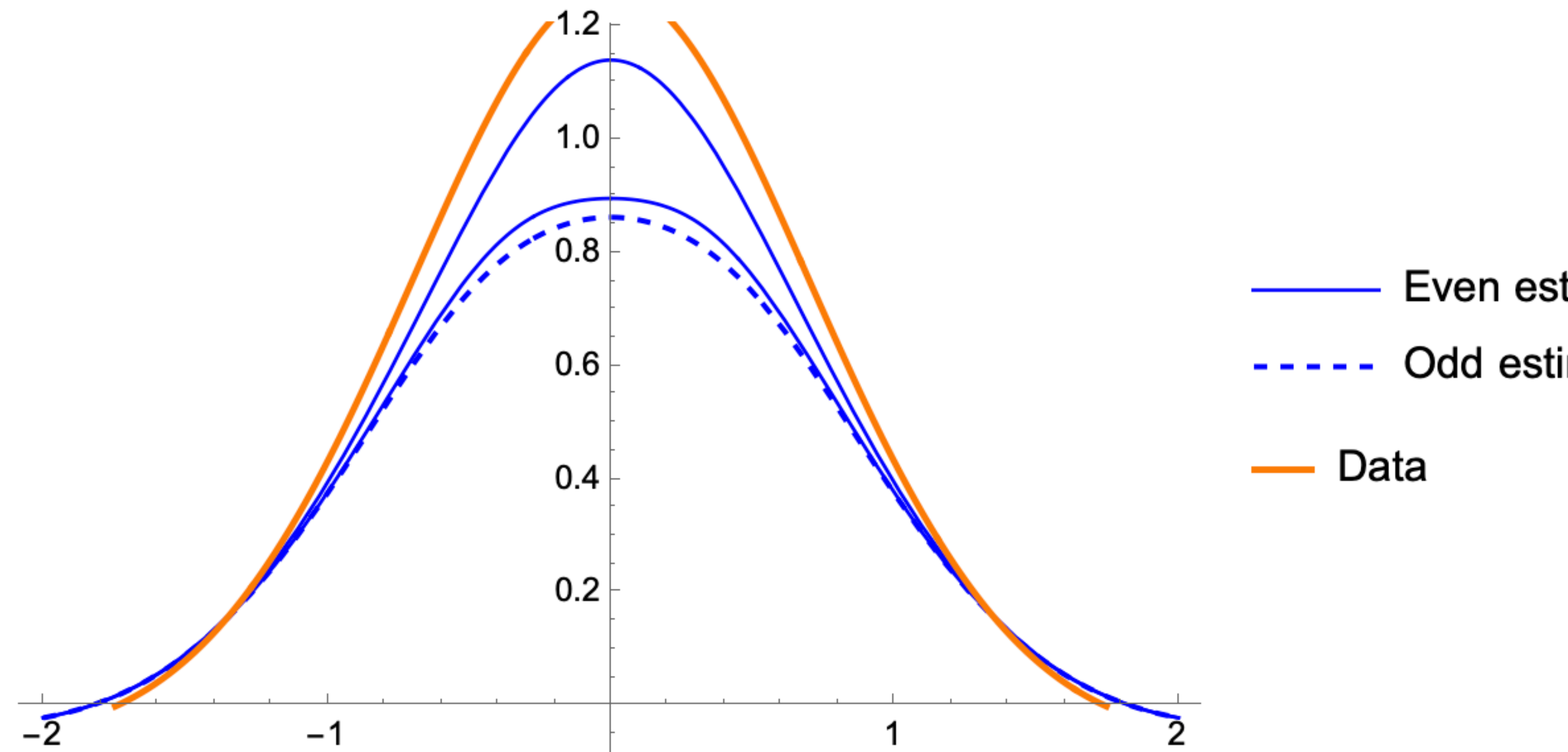
**Meeting 2022-01-31 1pm**

# Progress

- Analytic:
  - Experimented with Taylor expansions of the differential equation
- Numeric:
  - Considered how the output coupling affects the evolution of the soliton at each trip

# Analytic

- Process
  - 1. Substitute  $u_0 + u_1$  into the DE
  - 2. Taylor expand the result about 0, to the order  $x^2$
  - 3. Equate the coefficients of  $x^0$  and  $x^2$  to 0 to solve for A, B
- Result:
  - $\{A \rightarrow 0.242423, B \rightarrow 0.898534\}$
  - (Our current estimates are  $A \rightarrow 0.445408, B \rightarrow 1.02817$ )



# Analytic

If we consider another example,

$$h(x) = 3 \cos x + 1$$

which solves the DE

$$h'' - h + (1 + 6 \cos x) = 0$$

and we use the ansatz

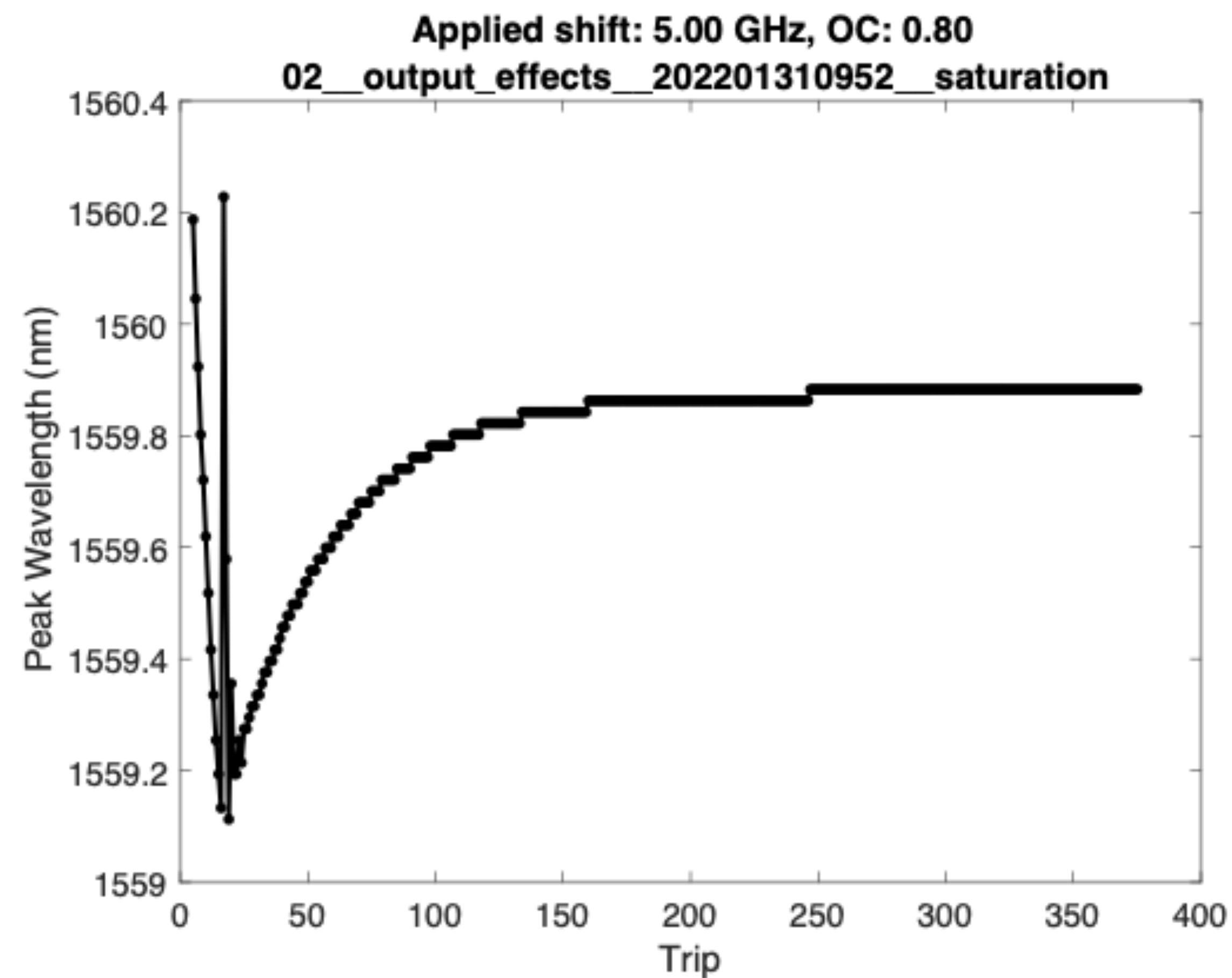
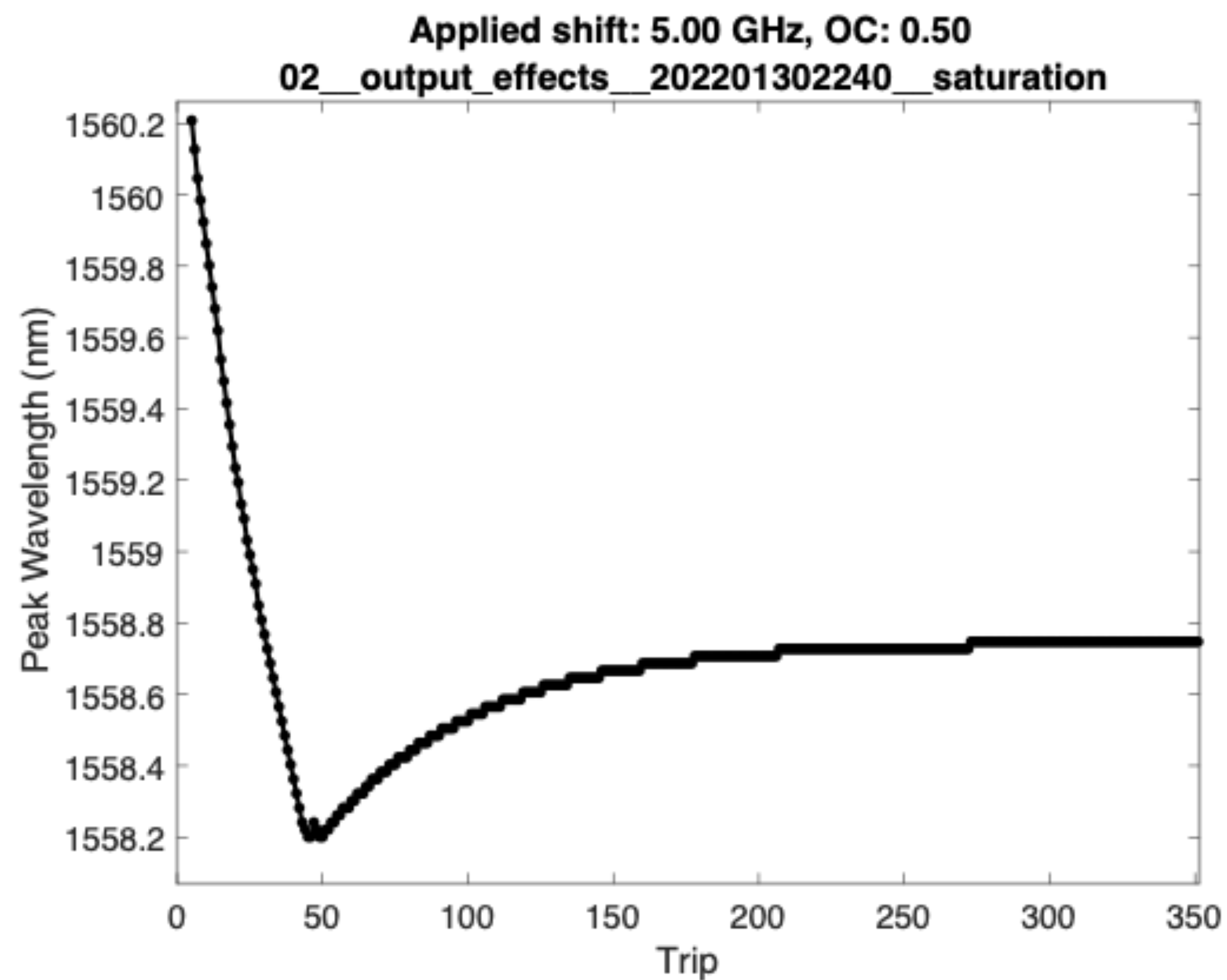
$$g(x) = A \cos x$$

Substituting it into the DE and expanding about  $x = 0$  gives

$$(7 - 2A) + (A - 3)x^2 + \mathcal{O}(x^3)$$

Solving this to the 0<sup>th</sup> order gives  $A \mapsto \frac{7}{2}$ , so  $h(0) \neq g(0)$  even though the DE is satisfied to this order.

# Numeric



# Numeric

