

A Quick User Guide on  
**Peking University**  
**Analog Resistive Random Access Memory (RRAM)**  
**SPICE Model**

**Version: 3.1**

Patent Pending.

*Copyright Peking University 2021*

All rights reserved.

January 12, 2021

Contributors:

Ms. Lixia Han, Ms. Linlin Cai,  
Prof. Jinfeng Kang, Prof. Xiaoyan Liu, Dr. Peng Huang

## *Terms of Use*

Peking University and the authors provide these model files to you subject to the Terms of Use, which may be updated by us from time to time without notice to you.

**By using the Peking University Analog RRAM SPICE Model (“Model”), you acknowledge that you have read the most up-to-date Terms of Use and agree to abide by the Terms of Use (“Terms”).**

These Terms include, but are not limited to, the following:

### License Agreement

**Peking University grants you a non-transferable license to use this Model on a single computer for a single user (You).** This license may not be sub-leased, sub-licensed, sold or otherwise transferred to another individual, company, or third party. Peking University reserves the right to revoke this license at any time, at which point you must stop using the Model and delete all Model files.

### Acceptable Usage

**This Model shall be used solely for non-commercial academic and industrial research by the individual to whom this Model, and its license, is granted.**

The Model and its files may not be used, in part or in whole, by another individual, institution, or a third party other than the original individual to whom this Model, and its license, is granted without prior written approval from Peking University. The Model and its files may not be copied, redistributed, or otherwise transferred, in part or in whole, to a third party without prior written approval from Peking University.

You agree not to disclose the ideas and inventions inherent in this Model to other individuals, institutions, or third parties. You further agree not to decompile or otherwise reverse-engineer this Model, in part or in whole, not to decompose the Model and its files, and not to misrepresent the Models and its files through modifications and add-ons.

### Additional Terms

**You agree to appropriately acknowledge and reference the Model work by Peking University in all publications, presentations, and/or other works derived from the use, in part or in whole, of this Model and/or its variants.** (See Section 5. References and additional references on the Website.)

### Disclaimer and Limitation of Liability

This Model is provided to you “As Is,” without warranty of any kind, either expressed or implied. By using this Model, you agree that you and your representing institution or company will not hold Peking University, the Model inventors, the Model authors, as well as all other contributing members to the Model and its official distribution, liable for damage of any kind resulting from the download or use of the Model and its files and documents.

#### Legal Notice

This Model, including the files, documents, and inherent ideas, are protected by Chinese Copyright Law and Chinese Patent Law. Peking University and authors reserve all rights. Unauthorized reproduction of the files and/or the documents included in the Model package is unlawful.

## 1. Model Files

This documentation pertains to the model files in the PKU Analog RRAM SPICE Model v3.1 package. A brief summary and description of the model files included in the package are shown in Table 1.

Table 1. Summary of Model Files

File Name	Description
RRAM_v_3_1.va	Analog RRAM SPICE Model File

Additional Files

File Name	Description
<i>User Guide</i>	
Analog_RRAM_Model_v3.1_Quick_User_Guide.pdf	This User Guide in PDF format.
<i>References/Publications</i>	[1]-[6]
<i>Sample Decks</i>	
AC_analog_SET.sp	Example HSPICE decks: AC SET pulse
AC_analog_RESET.sp	Example HSPICE decks: AC RESET pulse

The package should include all the sample decks, plus this User Guide document. A summary of the model scope is in 2. *The scope of the Model*; details regarding model usage and instantiation can be found in 3. *Model Usage*; and 4. *Sample results* describe the sample results using our model and discussion concerned.

## 2. The scope of the Model

Table 2 below summarizes the scope of the model.

Table 2. Summary of the Scope of the RRAM Model

Device Types	
Metal-Oxide Bipolar RRAM with Intermediate Modulation Layer (IML)	
Physics Aspects	
Filament Growth	Microscopic changes of oxygen vacancies and oxygen ions
Electronic Conduction	Combined: Ohmic & Fowler-Nordheim tunnelling mechanism
Analog switching characterize	Electrical and thermal properties of IML layer
Temperature and Heat Conduction	Joule heating

Different from the previously published RRAM\_v\_2\_1, RRAM\_v\_3\_1 is designed for fast and accurate simulation of analog metal-oxide based RRAM devices with intermediate modulation layer [1]. The underlying influences of electrical and thermal properties of IML on the analog switching behavior is dominant in improving the linearity [2] [3]. The model captures the pulse conductance update of analog RRAM devices with microscopic physical descriptions including the changes of oxygen vacancies ( $V_o$ ) and oxygen ions ( $O^{2-}$ ).

Fig. 1 shows the proposed physical model of filamentary RRAM including the resistive switching (RS) model and conduction model. The RS behavior involves the processes of oxygen vacancy ( $V_o$ ) generation and recombination, oxygen ions ( $O^{2-}$ ) absorption and release from IML. The conductive filament (CF) consists of one RS region and one  $V_o$  rich (VR) region. The electrical properties of the filament are determined by the dimension of the filament [4] [5]. For SET process, the increased percentage of  $V_o$  ( $\Delta C_V^+$ ) in RS regions is attributed to the  $V_o$  generation, where  $C_V$  is the  $V_o$  percentage denoting the number of  $V_o$  divided by the total number of lattice oxygen. For RESET process, the release of  $O^{2-}$  from IML and the recombination of  $V_o$  and  $O^{2-}$  lead to the decrease of  $C_V$  ( $\Delta C_V^-$ ). The changes of  $C_V$  are directly associated with the conductance of CF, especially associated with the conductance of RS region. Parameter extraction method can be referred to [6].

In VR region, the conductivity is assumed as metallic-like conduction.

In RS region, the effective conductivity is deduced by adopting the Maxwell-Garnett model [7] based on effective medium theory (EMT), which depends on three parameters, namely, the conductivity of intrinsic  $HfO_2$ , the conductivity of VR region, and  $V_o$  percentage ( $C_V$ ). Here the CF region is regarded as the intrinsic RS material with the changeable  $V_o$ . The main conduction mechanism of the intrinsic RS material without traps involved is assumed as Fowler-Nordheim tunnelling [8] and the conductivity is a function of electric field.

In IML region, The conductivity of IML is calculated by considering the  $O^{2-}$  percentage of IML according to EMT.

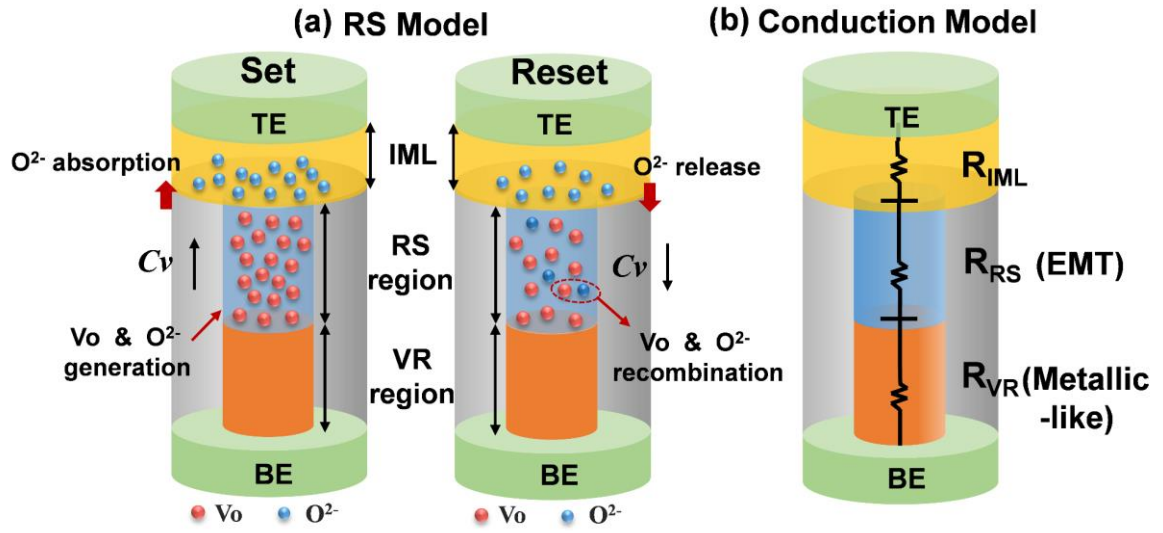


Fig. 1 Physical model of analog RRAM(a) RS model. The CF formation and rupture are determined by the changes of  $C_V$ . (b) Conduction model using effective medium theory (EMT) in RS region and metallic-like conduction in VR region.

### 3. Model Usage

The model is developed in Verilog-AMS, and it can be instantiated in HSPICE or other SPICE tools (with the appropriate Verilog-AMS support). **Here we recommend that user adopt Linux system as a simulation environment. We use Hspice-2016\_linux as our simulation tool.** This section illustrates how to instantiate the model in HSPICE.

#### 3.1 Convergence and Settings

For improved accuracy and convergence, include the following commands at the beginning of the SPICE deck:

```
*****  
.option converge = 0  
.option RUNLVL = 6  
.option METHOD=GEAR  
*****
```

#### 3.2 Model Instantiation

To instantiate the devices in the model, the library (model file) must be included at the beginning of the SPICE deck. If the model file and your test file are located in the same folder, you can use the syntax below. Otherwise, you should specify the absolute address where your model file is saved.

```
.hdl RRAM_v_3_1.va
```

To instantiate an RRAM device, use the appropriate syntax below. The usage of this model is similar to that of the Si CMOS transistor model.

\* Analog RRAM Model

**X\_RRAM TE BE RRAM\_v\_3\_1 <Parameter\_Name = Parameter\_Value>**

The port definitions, *TE* and *BE*, for the top electrode and the bottom electrode of RRAM, respectively. The ports *TE* and *BE* are not interchangeable in this model due to the nature of the asymmetry of the RRAM programming mechanism and the details of the model implementation.

The device parameters indicated in the < ... > are optional and can be set differently for each device instance. If the device parameters are omitted, default or global values set in the parameter definition file are used. The syntax for setting a parameter is: *parameter\_name = value or parameter*

Table 3 below lists the definitions and default values of the device parameters.

Table 3. Model Parameter Descriptions and Default Values			
Parameters	Descriptions	Default Value	Suggested Range <sup>1</sup>
$a$	Lattice oxygen distance	0.5 nm	[0.3,1]
$f$	O <sup>2-</sup> vibration frequency	10 <sup>13</sup> Hz	[10 <sup>12</sup> , 10 <sup>14</sup> ]
$E_a$	Activation energy of O <sup>2-</sup>	1.0 eV	[0.8,1.5]
$E_r$	Recombination barrier between V <sub>O</sub> and O <sup>2-</sup>	1.25 eV	[0.8,1.5]
$E_o$	Kinetic barrier of O <sup>2-</sup> from IML to RS region	1.0 eV	[0.8,1.5]
$E_{AC}$	Activation energy of conductance in VR region	-0.001 eV	[-0.01,0]
$\Psi_1$	Energy barrier between RS layer and BE	1.55 V	[0.5,2]
$\Psi_2$	Energy barrier between IML and RS layer	0.85 V	[0.5,2]
$\alpha_1$	Field enhancement factor for SET	0.95	[0.5,1.5]
$\alpha_2$	Field enhancement factor for RESET	1.2	[0.5,1.5]
$Z \& e$	Charge number & unit charge	2 & e	2 & e
$R_{th}$	Effective thermal resistance	1.8×10 <sup>6</sup> K/W	[1×10 <sup>6</sup> ,5×10 <sup>6</sup> ]
$L_{IML}$	Intermediate modulation layer thickness	60 nm	[0,100]
$L_{VR}$	VR region height	5.5nm	[0,10]
$L_{RS}$	RS region height	2.5 nm	[0,10]
$W_{IML}$	Intermediate modulation layer width	30 nm	[0,100]
$w_0$	Conductance filament radius	2.5nm	[0,5]
$A$	(The coefficient associated with the relationship between conductance and electric field)	1.5×10 <sup>-6</sup>	1.5×10 <sup>-6</sup>
$B$		1×10 <sup>9</sup>	1×10 <sup>9</sup>
$C_{V0}$	The proportion of V <sub>O</sub> in lattice oxygen	0.9	[0,1]
$C_{O0}$	The proportion of O <sup>2-</sup> in lattice oxygen	0	[0,1]
$\sigma_{v0}$	Initial conductivity of VR region	3×10 <sup>4</sup> Ω <sup>-1</sup> m <sup>-1</sup>	~10 <sup>4</sup>
$\sigma_{IML}$	Initial conductivity of IML region	1.25×10 <sup>5</sup> Ω <sup>-1</sup> m <sup>-1</sup>	[10 <sup>3</sup> ,10 <sup>6</sup> ]

<sup>1</sup> The range listed represents reasonable values based on experimental observations and physical insights. The units should be the same as the default values.



#### 4. Sample Results

RRAM\_v\_3\_1 is validated by the experimental data [9]. When inserting an IML between the top electrode and RS layer, the analog behavior with continuous conductance accumulation is obtained under the identical pulse training, as shown in Fig. 2 and Fig. 3. By adjusting the resistivity of IML, the analytic model shows an excellent agreement with the measurements about the linearity improvement of conductance modulation whether SET or RESET.

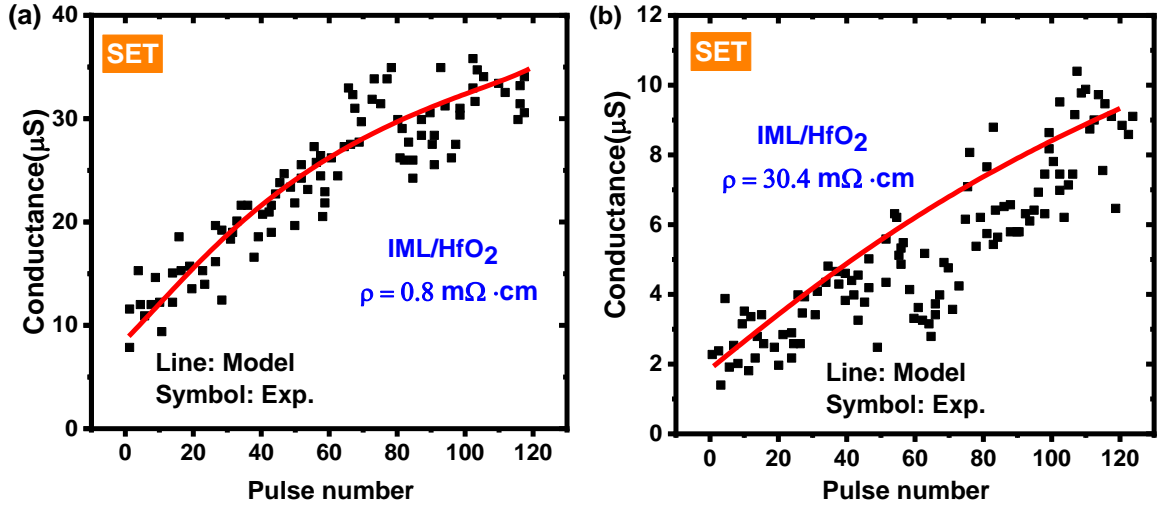


Fig. 2 Analog behavior of IML/HfO<sub>2</sub> RRAM with identical pulse in SET process. (a) the resistivity of IML is 0.8 mΩ·cm (b) the resistivity of IML is 30.4 mΩ·cm.

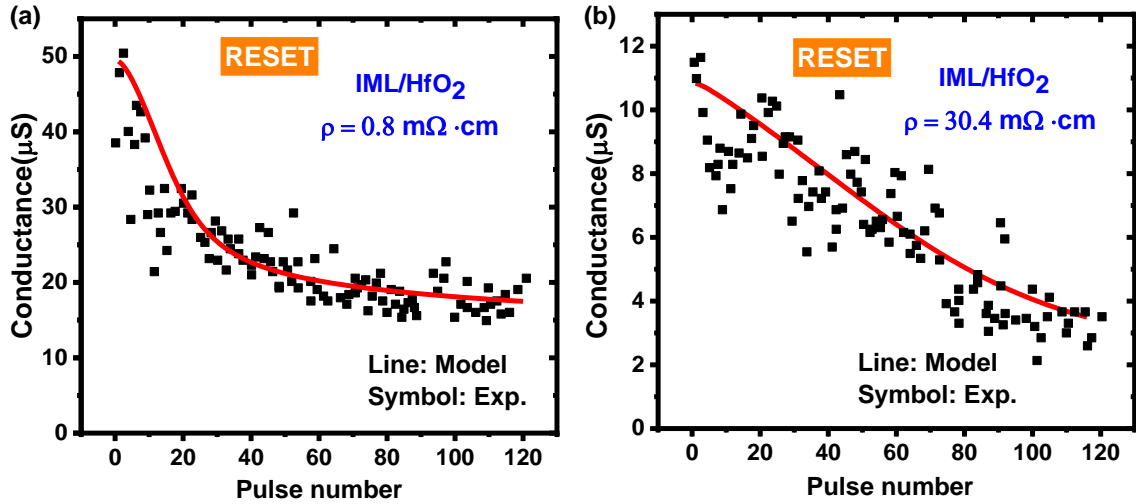


Fig. 3 Analog behavior of IML/HfO<sub>2</sub> RRAM with identical pulse in RESET process. (a) the resistivity of IML is 0.8 mΩ·cm (b) the resistivity of IML is 30.4 mΩ·cm.

Below is a short introduction of the key parameters that influence the resistive switching characteristics of RRAM. For further analysis purpose, users can print values of key variables in the model by calling system functions. As for the usage of system functions, please refer to the Verilog-AMS language documents.

Parameters which are critical to analog RRAM behavior during SET process include  $E_a$ ,  $\alpha_1$ , and  $C_{V0}$ .

1.  $E_a$  and  $\alpha_1$  control the rate of  $V_O$  generation during the SET process. In the model, decreasing  $E_a$  or increasing  $\alpha_1$  leads to worse nonlinearity.
2.  $C_{V0}$  determines the initial RRAM states and affects the linearity and resistance of RRAM with pulse numbers.

Parameters which are critical to analog RRAM behavior during RESET process include  $E_r$ ,  $E_o$ ,  $\alpha_2$ , and  $C_{V0}$ .

1.  $E_o$  and  $\alpha_2$  control the rate of  $O^{2-}$  released from IML, which is the first step of the RESET process. In the model, decreasing  $E_o$  or increasing  $\alpha_2$  can accelerate RESET process.
2.  $E_r$  is critical to the rate of the recombination between  $V_O$  and  $O^{2-}$ , which is the second stage during the RESET process. In the model, increasing  $E_r$  leads to the slower RESET process with the identical pulse.
3.  $C_{V0}$  determines the initial RRAM states and affects the linearity and resistance of RRAM with pulse numbers.

For more parameter descriptions, users can look up our model file.

## 5. References

- [1] Cai, Linlin, et al. "A Physics-Based Analytic Model of Analog Switching Resistive Random Access Memory." *IEEE Electron Device Letters* 41.2 (2019): 236-239.  
DOI: 10.1109/LED.2019.2961697
- [2] J. Woo, et al. "Improved Synaptic Behavior Under Identical Pulses Using AlOx /HfO2 Bilayer RRAM Array for Neuromorphic Systems," *IEEE Electron Device Lett.*, vol. 37, no. 8, pp. 994–997, Aug. 2016.  
DOI: 10.1109/LED.2016.2582859
- [3] W. Wu, et al. "A Methodology to Improve Linearity of Analog RRAM for Neuromorphic Computing," in *Proc. IEEE Symp. VLSI Technol.*, Jun. 2018, pp. 103–104.  
DOI: 10.1109/VLSIT.2018.8510690.
- [4] P. Huang, et al. "A Physical Based Analytic Model of RRAM Operation for CircuitSimulation," *IEEE International Electron Devices Meeting (IEDM)*, pp.605-608, 2012.  
DOI:10.1109/iedm.2012.6479110
- [5] P. Huang, et al. "A Physics Based Compact Model of Metal Oxide Based RRAM DCand AC Operation," *IEEE Trans. Electron Devices*, vol. 60, no.12, pp. 4090-4097, 2013.  
DOI: 10.1109/ted.2013.2287755
- [6] P. Huang, et al. "Parameters Extraction onHfOX based RRAM," *European Solid-State Device Research Conference (ESSDERC)*, pp.250-253,2014.  
DOI:10.1109/essderc.2014.6948807
- [7] J. C. M. Garnett, "Colours in Metal Glasses and in Metallic Films," *Philos. Trans. Roy. Soc. London A, Math., Phys. Eng. Sci.*, vol. 203, pp. 385–420, Jan. 1904.  
DOI: 10.1098/rsta.1904.0024.
- [8] A. G. Khairnar, et al. "Investigation of Current Conduction Mechanism in HfO2 Thin Film on Silicon Substrate," in *Physics of Semiconductor Devices*. Springer, 2014, pp. 25–27.  
DOI: 10.1007/978-3-319-03002-9\_7.
- [9] W. Wu, et al. "A Methodology to Improve Linearity of Analog RRAM for Neuromorphic Computing," in *Proc. IEEE Symp. VLSI Technol.*, Jun. 2018, pp. 103–104.  
DOI: 10.1109/VLSIT.2018.8510690.

## 6. Contacts

Please direct all inquiries and comments to:

Peng Huang, associate research fellow of Peking University

Email: [Phwang@pku.edu.cn](mailto:Phwang@pku.edu.cn)

Xiaoyan Liu, Professor of Peking University

Email: [xyliu@ime.pku.edu.cn](mailto:xyliu@ime.pku.edu.cn)

OR (for technical support):

Lixia Han, PhD candidate with Peking University

Email: [lixiahan@pku.edu.cn](mailto:lixiahan@pku.edu.cn)

Linlin Cai, PhD candidate with Peking University

Email: [linlinc@pku.edu.cn](mailto:linlinc@pku.edu.cn)

Please report any bugs to us. Suggestions and comments are also welcome.