



Electric Current & DC Circuits

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Progressive Science Initiative

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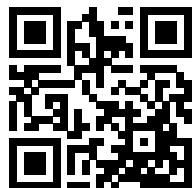
How to Use this File

- Each topic is composed of brief direct instruction
- There are formative assessment questions after every topic denoted by black text and a number in the upper left.
 - > Students work in groups to solve these problems but use student responders to enter their own answers.
 - > Designed for SMART Response PE student response systems.
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Electric Current & DC Circuits

Click on the topic to go to that section

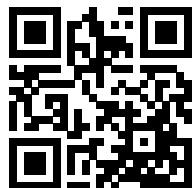
- Circuits
- Conductors
- Resistivity and Resistance
- Circuit Diagrams
- Measurement



<http://njc.tl/n3>

Circuits

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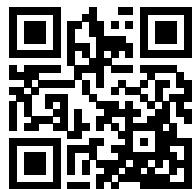
Circuits

So do positive or negative charges flow through the circuit?

Historically, positive charges were identified as the ones that flowed in the circuit. It was not until a later time that we understood that it was the negative charge (electrons) which were free to move.

In reality, electrons flow from the negative terminal of the battery, through a conductor, to the positive terminal.

This is the actual current.



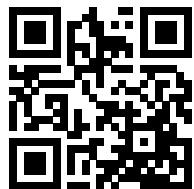
<http://njc.tl/n3>

Current

While actual current is the flow of electrons from the negative terminal to the positive terminal, we use conventional current to model electric circuits.

Conventional current is the flow of positive charges flowing from the positive to the negative terminal.

Going forward, we will use conventional current to discuss electric circuits. Both conventional current and actual current lead to the same predictions but flow in opposite directions.



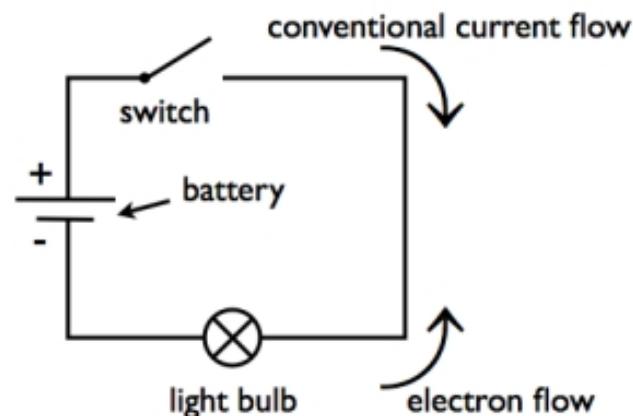
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Circuits

An electric circuit is an external path that charges can follow between two terminals using a conducting material.

For charge to flow, the path must be complete and unbroken.

An example of a conductor used to form a circuit is copper wire. You can think of a wire as a pipe for charge to move through.



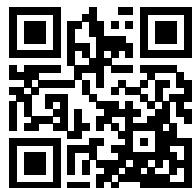
<http://njc.tl/n3>

Current

The letter "I" is the symbol for current. It is defined as the amount of charge that flows past a location in a conductor per unit time.

$$I = \frac{\Delta Q}{\Delta t}$$

ΔQ is the amount of charge, and Δt is the time it flowed past the location.



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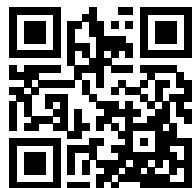
Current

The current, $I = \frac{\Delta Q}{\Delta t}$ has the units Coulombs per second.

The units can be rewritten as Amperes (A).

$$1 \text{ A} = 1 \text{ C/s}$$

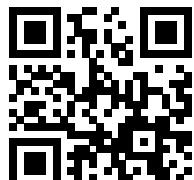
Amperes are often called "amps".



<http://njc.tl/n3>

- 1 12 C of charge passes a location in a circuit in 10 seconds. What is the current flowing past the point?

Answer

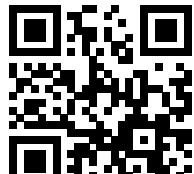


<http://njc.tl/n4>

- 1 12 C of charge passes a location in a circuit in 10 seconds. What is the current flowing past the point?

Answer

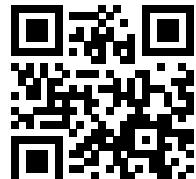
$$I = \frac{\Delta Q}{\Delta t} = \frac{12C}{10s} = 1.2A$$



<http://njc.tl/n4>

2 20 C of charge passes a location in a circuit in 30 seconds. What is the current flowing past the point?

Answer



<http://njc.tl/n5>

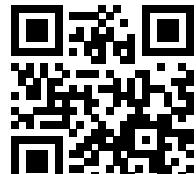
2 20 C of charge passes a location in a circuit in 30 seconds. What is the current flowing past the point?

Answer

$$I = \Delta Q / \Delta t$$

$$I = 20C / 30s$$

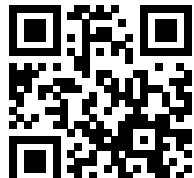
$$I = .66C / s = .66A$$



<http://njc.tl/n5>

3 A circuit has 3 A of current. How long does it take 45 C of charge to travel through the circuit?

Answer



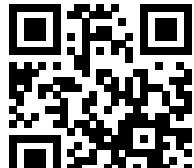
<http://njc.tl/n6>

3 A circuit has 3 A of current. How long does it take 45 C of charge to travel through the circuit?

Answer

$$I = \frac{\Delta Q}{\Delta t}$$

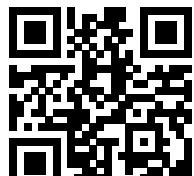
$$t = \frac{\Delta Q}{I} = \frac{45C}{3A} = 15s$$



<http://njc.tl/n6>

4 A circuit has 10 A of current. How long does it take 20 C of charge to travel through the circuit?

Answer



<http://njc.tl/n7>

4 A circuit has 10 A of current. How long does it take 20 C of charge to travel through the circuit?

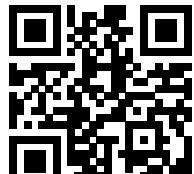
Answer

$$I = \Delta Q / \Delta t$$

$$\Delta t = \Delta Q / I$$

$$\Delta t = \frac{20C}{10C/s}$$

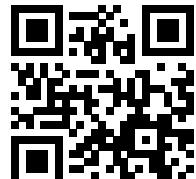
$$\Delta t = 2s$$



<http://njc.tl/n7>

5 A circuit has 10 A of current. How much charge travels through the circuit after 20s?

Answer



<http://njc.tl/n5>

5 A circuit has 10 A of current. How much charge travels through the circuit after 20s?

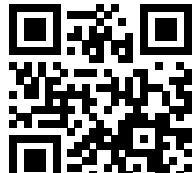
Answer

$$I = \frac{\Delta Q}{\Delta t}$$

$$\Delta Q = I \Delta t$$

$$\Delta Q = 10A(20s)$$

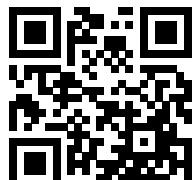
$$\Delta Q = 200C$$



<http://njc.tl/n5>

6 A circuit has 2.5 A of current. How much charge travels through the circuit after 4s?

Answer



<http://njc.tl/n8>

6 A circuit has 2.5 A of current. How much charge travels through the circuit after 4s?

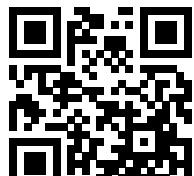
Answer

$$I = \frac{\Delta Q}{\Delta t}$$

$$\Delta Q = I \Delta t$$

$$\Delta Q = 2.5A(4s)$$

$$\Delta Q = 10C$$



<http://njc.tl/n8>

Batteries

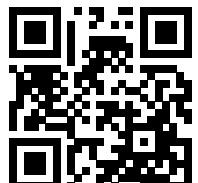
Each battery has two terminals which are conductors. The terminals are used to connect an external circuit allowing the movement of charge.

Batteries convert chemical energy to electrical energy which maintains the potential difference.

The chemical reaction acts like an escalator, carrying charge up to a higher voltage.



Click here for a Battery Voltage Simulation from PhET



<http://njc.tl/n9>

Reviewing Basic Circuits

The circuit cannot have gaps.

The bulb had to be between the wire and the terminal.

A voltage difference is needed to make the bulb light.

The bulb still lights regardless of which side of the battery you place it on.

*As you watch the video, observations and
the answers to the questions below.*

What is going on in the circuit?

What is the role of the battery?

How are the circuits similar? different?

Click here for
video using the
circuit simulator
from PhET



<http://njc.tl/n9>

Batteries and Current

The battery pushes current through the circuit. A battery acts like a pump, pushing charge through the circuit. It is the circuit's energy source.

Charges do not experience an electrical force unless there is a difference in electrical potential (voltage). Therefore, batteries have a potential difference between their terminals. The positive terminal is at a higher voltage than the negative terminal.

click here for a video from
Veritasium's Derek on current

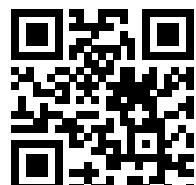
How will voltage affect current?



<http://njc.tl/n9>

Conductors

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<http://njc.tl/na>

Conductors

Some conductors "conduct" better or worse than others. Reminder: conducting means a material allows for the free flow of electrons.

The flow of electrons is just another name for current. Another way to look at it is that some conductors resist current to a greater or lesser extent.

We call this resistance, R. Resistance is measured in ohms which is noted by the Greek symbol omega (Ω)

How will resistance affect current?



<http://njc.tl/na>

Click here to run another
PhET simulation

Current vs Resistance & Voltage

Raising resistance reduces current.

Raising voltage increases current.

We can combine these relationships in what we call
"Ohm's Law".

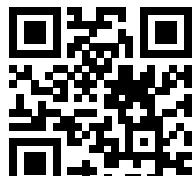
$$I = \frac{V}{R}$$

Another way to write this is that:

$$R = \frac{V}{I} \quad \text{OR} \quad V = IR$$

You can see that one $\Omega = \frac{V}{A}$

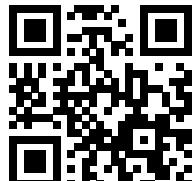
click here for a Veritasium
music video on electricity



<http://njc.tl/na>

- 7 A flashlight has a resistance of 25Ω and is connected by a wire to a 120 V source of voltage. What is the current in the flashlight?

Answer

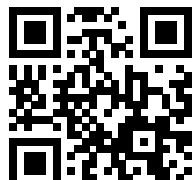


<http://njc.tl/nb>

- 7 A flashlight has a resistance of 25Ω and is connected by a wire to a 120 V source of voltage. What is the current in the flashlight?

Answer

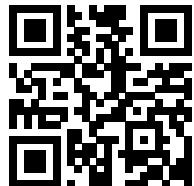
$$I = \frac{V}{R} = \frac{120V}{25\Omega} = 4.8A$$



<http://njc.tl/nb>

- 8 A flashlight has a resistance of 30Ω and is connected by a wire to a 90 V source of voltage. What is the current in the flashlight?

Answer



<http://njc.tl/nc>

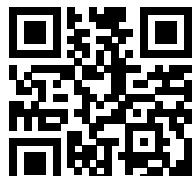
- 8 A flashlight has a resistance of 30Ω and is connected by a wire to a 90 V source of voltage. What is the current in the flashlight?

Answer

$$I = V / R$$

$$I = 90V / 30\Omega$$

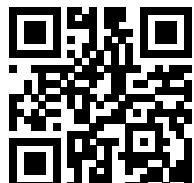
$$I = 3Amps$$



<http://njc.tl/nc>

9 What is the current in a wire whose resistance is 3Ω if $1.5 V$ is applied to it?

Answer

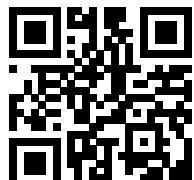


<http://njc.tl/nd>

9 What is the current in a wire whose resistance is 3Ω if $1.5 V$ is applied to it?

Answer

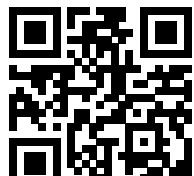
$$I = \frac{V}{R} = \frac{1.5V}{3\Omega} = .5A$$



<http://njc.tl/nd>

10 How much voltage is needed in order to produce a 0.70 A current through a $490\ \Omega$ resistor?

Answer



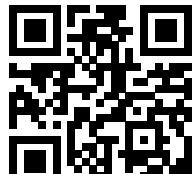
<http://njc.tl/ne>

10 How much voltage is needed in order to produce a 0.70 A current through a $490\ \Omega$ resistor?

Answer

$$I = \frac{V}{R}$$

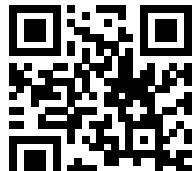
$$V = IR = (.7A)(490\Omega) = 343V$$



<http://njc.tl/ne>

11 How much voltage is needed in order to produce a 0.5 A current through a 150Ω resistor?

Answer



<http://njc.tl/nf>

11 How much voltage is needed in order to produce a 0.5 A current through a $150\ \Omega$ resistor?

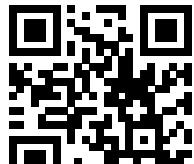
Answer

$$I = V / R$$

$$V = IR$$

$$V = (.5A)150\Omega$$

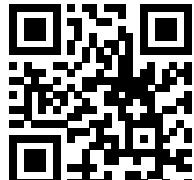
$$V = 75V$$



<http://njc.tl/nf>

12 What is the resistance of arheostat coil, if 0.05 A of current flows through it when 6 V is applied across it?

Answer



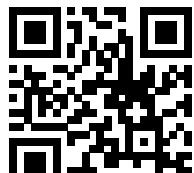
<http://njc.tl/ng>

12 What is the resistance of arheostat coil, if 0.05 A of current flows through it when 6 V is applied across it?

Answer

$$I = \frac{V}{R}$$

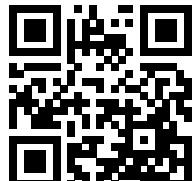
$$R = \frac{V}{I} = \frac{6V}{.05A} = 120\Omega$$



<http://njc.tl/ng>

13 What is the resistance of arheostat coil, if 20 A of current flows through it when 1000 V is applied across it?

Answer



<http://njc.tl/nh>

13 What is the resistance of arheostat coil, if 20 A of current flows through it when 1000 V is applied across it?

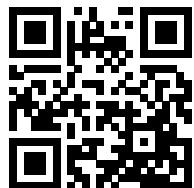
Answer

$$I = V / R$$

$$R = V / I$$

$$R = 1000V / 20A$$

$$R = 50\Omega$$



<http://njc.tl/nh>

Electrical Power

Power is defined as work per unit time

$$P = \frac{W}{t}$$

if $W = QV$ then substitute:

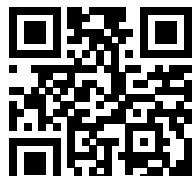
$$P = \frac{QV}{t}$$

if $I = \frac{Q}{t}$ then substitute:

$$P = IV$$

What happens if the current is increased?

What happens if the voltage is decreased?



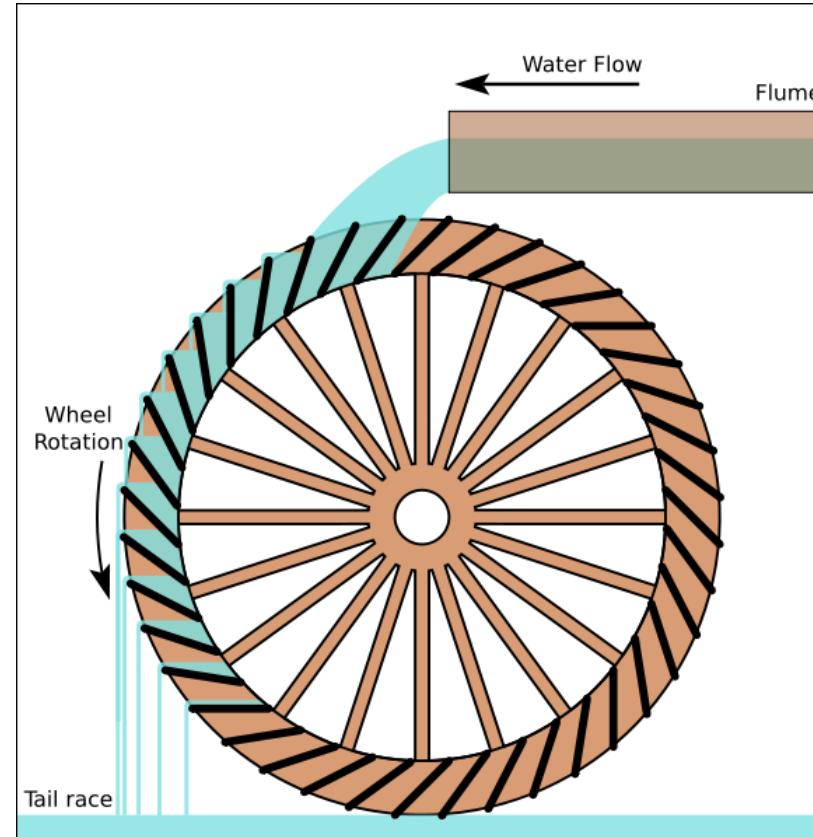
<http://njc.tl/ni>

Electrical Power

Let's think about this another way...

The water at the top has GPE & KE.

As the water falls, it loses GPE and the wheel gets turned, doing work. When the water falls to the bottom it is now slower, having done work.



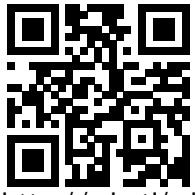
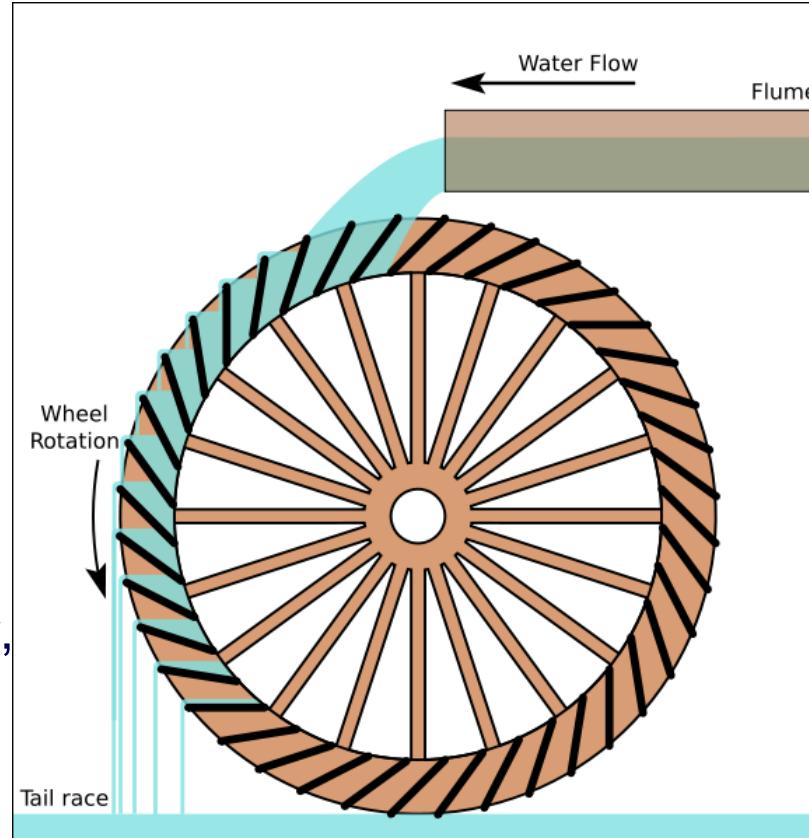
<http://njc.tl/ni>

Electrical Power

Electric circuits are similar.

A charge falls from high voltage to low voltage.

In the process of falling energy may be used (light bulb, run a motor, etc).



<http://njc.tl/ni>

What is the unit of Power?

Electrical Power

How can we re-write electrical power by using Ohm's Law?

(electrical power)

$$P = IV$$

(Ohm's Law)

$$I = \frac{V}{R}$$

$$P = \frac{VI}{R}$$

$$P = \frac{V^2}{R}$$



<http://njc.tl/ni>

Electrical Power

Is there yet another way to rewrite this?

$$I = \frac{V}{R} \text{ can be rewritten as } V = IR.$$

(electrical power)
 $P = IV$

(Ohm's Law)
 $V = IR$

We can substitute this into Power

$$P = I(IR)$$

$$P = I^2R$$



<http://njc.tl/ni>

Batteries



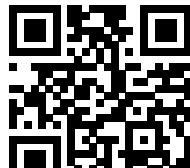
D C AAA AA

9 V

1.5 V

D, C, AA, & AAA have the same voltage, however they differ in the amount of power they deliver.

For instance, D batteries can deliver more current and therefore more power.



<http://njc.tl/ni>

- 14 A toy car's electric motor has a resistance of 17Ω ; find the power delivered to it by a 6-V battery.

Answer



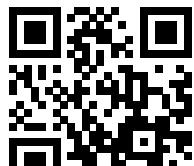
<http://njc.tl/nj>

- 14 A toy car's electric motor has a resistance of $17\ \Omega$; find the power delivered to it by a 6-V battery.

Answer

$$P = IV = \frac{V}{R}V = \frac{V^2}{R}$$

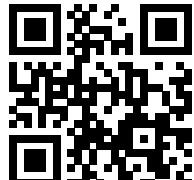
$$P = \frac{(6V)^2}{17\Omega} = 2.118W$$



<http://njc.tl/nj>

- 15 A toy car's electric motor has a resistance of $6\ \Omega$; find the power delivered to it by a 7-V battery.

Answer



<http://njc.tl/nk>

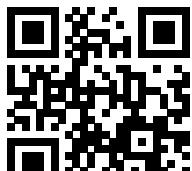
- 15 A toy car's electric motor has a resistance of $6\ \Omega$; find the power delivered to it by a 7-V battery.

Answer

$$P = IV = \frac{V}{R}V = \frac{V^2}{R}$$

$$P = \frac{(7V)^2}{6\Omega}$$

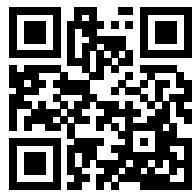
$$P = 8.16W$$



<http://njc.tl/nk>

16 What is the power consumption of a flash light bulb that draws a current of 0.28 A when connected to a 6 V battery?

Answer

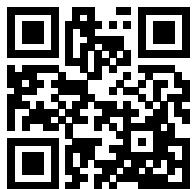


<http://njc.tl/nl>

- 16 What is the power consumption of a flash light bulb that draws a current of 0.28 A when connected to a 6 V battery?

Answer

$$P = IV = (.28A)(6V) = 1.68W$$



<http://njc.tl/nl>

17 What is the power consumption of a flash light bulb that draws a current of 0.33 A when connected to a 100 V battery?

Answer



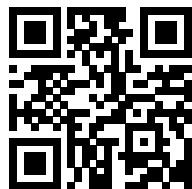
<http://njc.tl/nm>

- 17 What is the power consumption of a flash light bulb that draws a current of 0.33 A when connected to a 100 V battery?

Answer

$$P = IV = (.33A)100V$$

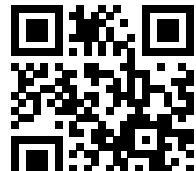
$$P = 33W$$



<http://njc.tl/nm>

18 A 30Ω toaster consumes 560 W of power: how much current is flowing through the toaster?

Answer



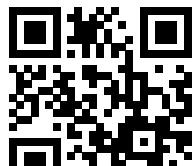
<http://njc.tl/nn>

- 18 A 30Ω toaster consumes 560 W of power: how much current is flowing through the toaster?

Answer

$$P = IV = I(IR) = I^2R$$

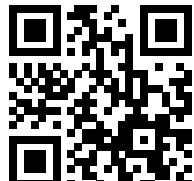
$$I = \sqrt{\frac{P}{R}} = \sqrt{\frac{560W}{30\Omega}} = 4.32A$$



<http://njc.tl/n>

19 A 50Ω toaster consumes 200 W of power: how much current is flowing through the toaster?

Answer



<http://njc.tl/no>

- 19 A 50Ω toaster consumes 200 W of power: how much current is flowing through the toaster?

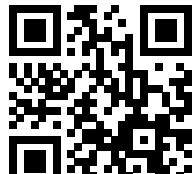
Answer

$$P = IV = I(IR) = I^2R$$

$$I = \sqrt{P/R}$$

$$I = \sqrt{200W / 50\Omega}$$

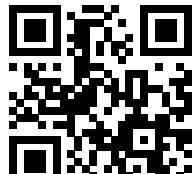
$$I = 2A$$



<http://njc.tl/no>

20 When 30 V is applied across a resistor it generates 600 W of heat: what is the magnitude of its resistance?

Answer



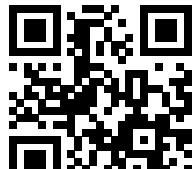
<http://njc.tl/np>

20 When 30 V is applied across a resistor it generates 600 W of heat: what is the magnitude of its resistance?

Answer

$$P = IV = \frac{V}{R}V = \frac{V^2}{R}$$

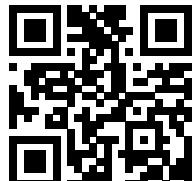
$$R = \frac{V^2}{P} = \frac{(30V)^2}{600W} = 1.5\Omega$$



<http://njc.tl/np>

21 When 100 V is applied across a resistor it generates 200 W of heat: what is the magnitude of its resistance?

Answer



<http://njc.tl/nq>

21 When 100 V is applied across a resistor it generates 200 W of heat: what is the magnitude of its resistance?

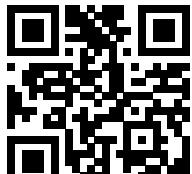
Answer

$$P = IV = \frac{V}{R}V = \frac{V^2}{R}$$

$$R = V^2 / P$$

$$R = (100V)^2 / 200W$$

$$R = 50\Omega$$



<http://njc.tl/nq>

"Pipe" size

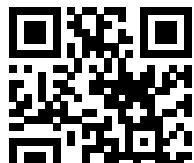
How could the wire in the circuit affect the current?

If wire is like a pipe, and current is like water that flows through the pipe...

if there were pipes with water in them, what could we do to the pipes to change the speed of the water (the current)?



Answer



<http://njc.tl/nr>

"Pipe" size

How could the wire in the circuit affect the current?

If wire is like a pipe, and current is like water that flows through the pipe...

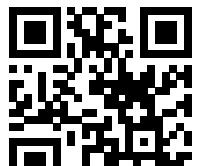
if there were pipes with them, what could we do to pipes to change the speed of water (the current)?

change the cross-sectional area of the pipe

making it bigger will allow more water to flow

change the length of the pipe

increasing the length will increase the time it takes for the water to get to the end of its trip

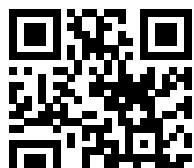


<http://njc.tl/nr>

Answer



Resistivity and Resistance



<http://njc.tl/nr>

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Resistivity & Resistance

Every conductor "conducts" electric charge to a greater or lesser extent.

The last example also applies to conductors like copper wire. Decreasing the length (L) or increasing the cross-sectional area (A) would increase conductivity.

Also, the measure of a conductor's resistance to conduct is called its resistivity. Each material has a different resistivity.

Resistivity is abbreviated using the Greek letter rho (ρ).

Combining what we know about A , L , and ρ , we can find a conductor's total resistance.



<http://njc.tl/nr>

$$R = \frac{\rho L}{A}$$

Resistivity & Resistance

$$R = \frac{\rho L}{A}$$

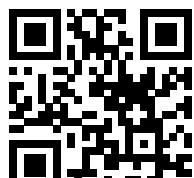
Resistance, R, is measured in Ohms (Ω). Ω is the Greek letter Omega.

Cross-sectional area, A, is measured in m^2

Length, L, is measured in m

Resistivity, ρ , is measured in Ωm

How can we define A for a wire?



<http://njc.tl/nr>

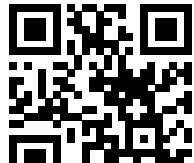
Resistance

$$\rho = \frac{RA}{L}$$

What is the resistance of a good conductor?

Low; low resistance means that electric charges are free to move in a conductor.

Click here for a PhET simulation about Resistance



<http://njc.tl/nr>

Resistivities of Common Conductors

Material	Resistivity ($10^{-8} \Omega\text{m}$)
Silver	1.59
Copper	1.68
Gold	2.44
Aluminum	2.65
Tungsten	5.60
Iron	9.71
Platinum	10.6
Mercury	98
Nichrome	100

22 Rank the following materials in order of best conductor to worst conductor.

- A Iron, Copper, Platinum
- B Platinum, Iron, Copper
- C Copper, Iron, Platinum

Material	Resistivity ($10^{-8} \Omega\text{m}$)
Silver	1.59
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Answer



<http://njc.tl/nr>

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Material	Resistivity ($10^{-8} \Omega\text{m}$)

Answer

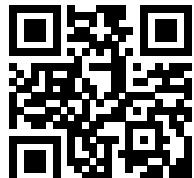
C



<http://njc.tl/nr>

23 What is the resistance of a 2 m long copper wire whose cross-sectional area of 0.2 mm^2 ?

Answer

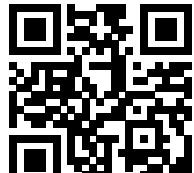


<http://njc.tl/ns>

23 What is the resistance of a 2 m long copper wire whose cross-sectional area of 0.2 mm²?

Answer

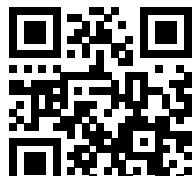
$$R = \frac{\rho L}{A} = \frac{(1.68 \times 10^{-8} \Omega m)(2m)}{.2 \text{mm}^2} = \frac{3.36 \times 10^{-8} \Omega m^2}{.2 \times 10^{-6} m^2} = .168 \Omega$$



<http://njc.tl/ns>

24 An aluminum wire with a length of 900 m and cross-sectional area of 10 mm^2 has a resistance of 2.5Ω . What is the resistivity of the wire?

Answer

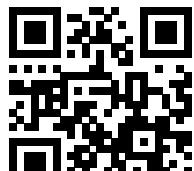


<http://njc.tl/nt>

24 An aluminum wire with a length of 900 m and cross-sectional area of 10 mm² has a resistance of 2.5 Ω. What is the resistivity of the wire?

Answer

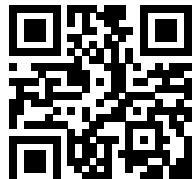
$$\rho = \frac{RA}{L} = \frac{(2.5\Omega)(10\text{mm}^2)}{900\text{m}} =$$
$$\frac{2.5 \times 10^{-5} \Omega\text{m}^2}{900\text{m}} = 2.78 \times 10^{-8} \Omega\text{m}$$



<http://njc.tl/nt>

25 What diameter of 100 m long copper wire would have a resistance of 0.10Ω ?

Answer



<http://njc.tl/nu>

25 What diameter of 100 m long copper wire would have a resistance of 0.10 Ω ?

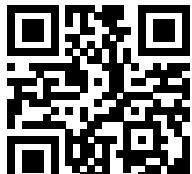
Answer

$$A = \pi r^2 \quad r = \frac{d}{2} \quad A = \frac{\pi d^2}{4}$$

$$R = \frac{\rho L}{A} = \frac{4\rho L}{\pi d^2}$$

$$d = \frac{\rho L}{A} = \sqrt{\frac{4\rho L}{\pi R}}$$

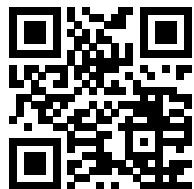
$$d = \sqrt{\frac{4(1.68 \times 10^{-8})(100m)}{\pi(.1\Omega)}} = 4.625mm$$



<http://njc.tl/nu>

26 What is the cross-sectional area of a 10Ω copper wire of length is 10000 meters ?

Answer



<http://njc.tl/nv>

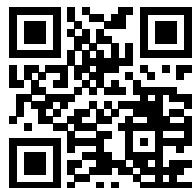
26 What is the cross-sectional area of a 10Ω copper wire of length is 10000 meters ?

Answer

$$R = \frac{\rho L}{A}$$

$$A = \frac{\rho L}{R} = \frac{(1.68 \times 10^{-8})(10000m)}{10\Omega}$$

$$A = 1.68 \times 10^{-5} m^2$$



<http://njc.tl/nv>

27 What is the length of a 10Ω copper wire whose diameter is 3.2 mm?

Answer



27 What is the length of a 10Ω copper wire whose diameter is 3.2 mm?

Answer

$$A = \pi r^2 \quad r = \frac{d}{2} \quad A = \frac{\pi d^2}{4}$$

$$R = \frac{\rho L}{A} = \frac{4\rho L}{\pi d^2}$$

$$L = \frac{\pi R d^2}{4\rho}$$

$$L = \frac{\pi (10\Omega)(3.2 \times 10^{-3} m)}{4(1.68 \times 10^{-8})} = 4787.2 m$$



Circuit Diagrams

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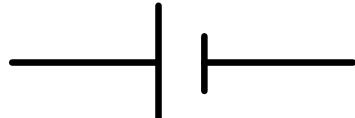
Circuit Diagrams

Drawing realistic pictures of circuits can be very difficult.

For this reason, we have common symbols to represent each piece.



Resistor



Battery



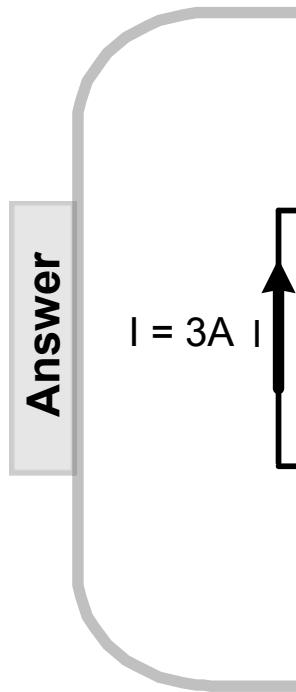
Wire



*Note: Circuit diagrams do not show where each part is physically located.

Circuit Diagrams

Draw a simple circuit that has a 9 V battery with a $3\ \Omega$ resistor across its terminals. What is the magnitude and direction of the current?



Answer

$$I = 3A$$



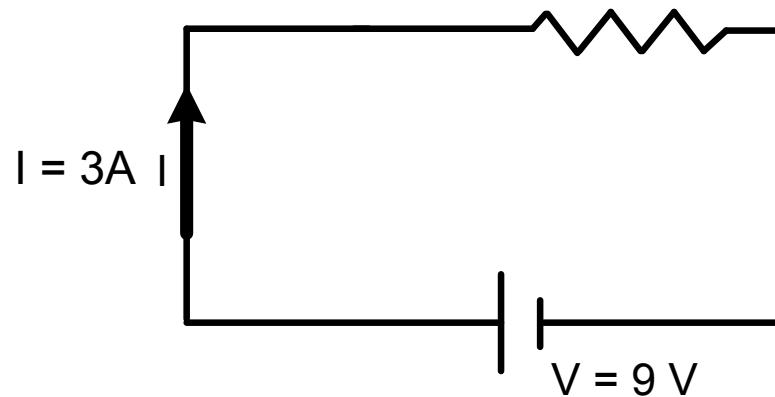
Conventional current flows from the positive terminal to the negative terminal.

Circuit Diagrams

Draw a simple circuit that has a 9 V battery with a $3\ \Omega$ resistor across its terminals. What is the magnitude and direction of the current?

Answer

$$R = 3\Omega$$



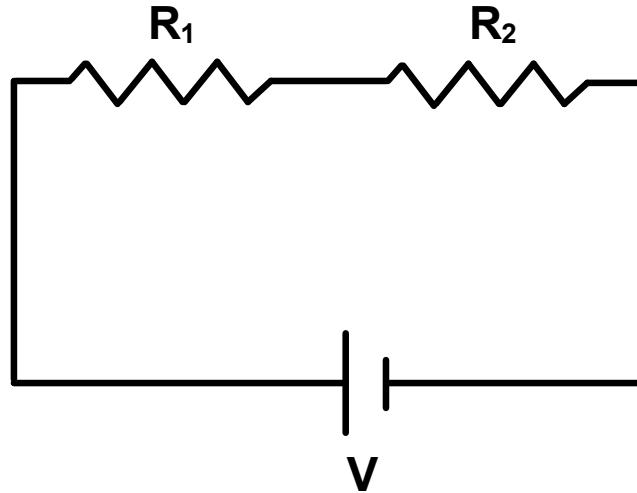
Conventional current flows from the positive terminal to the negative terminal.



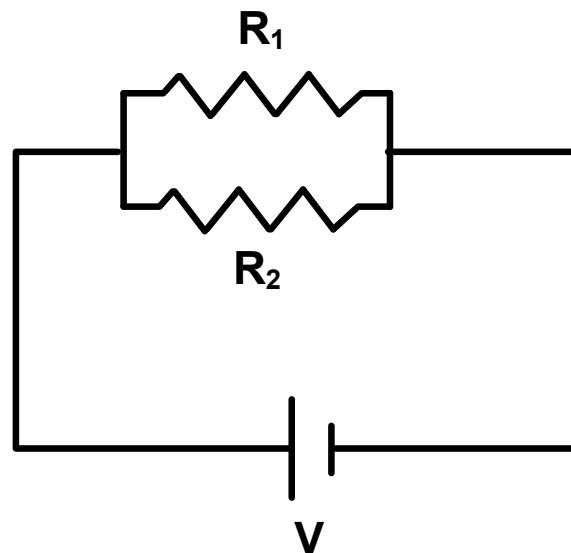
Circuit Diagrams

There are two ways to add a second resistor to the circuit.

Series



Parallel



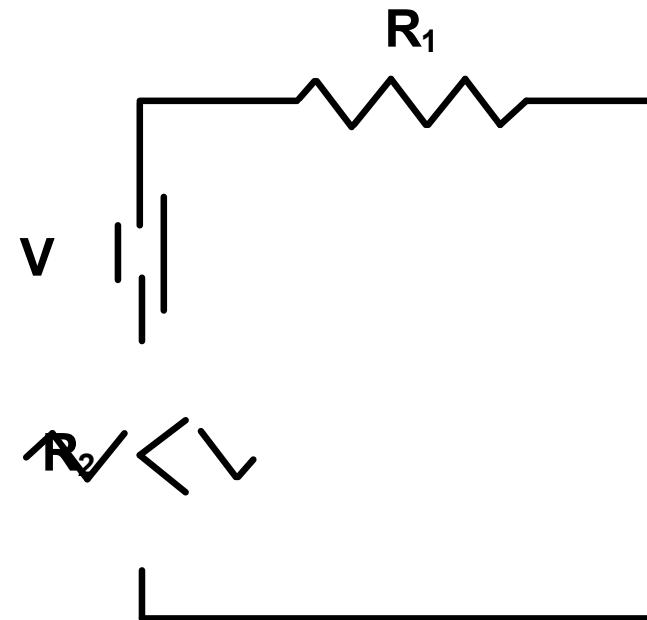
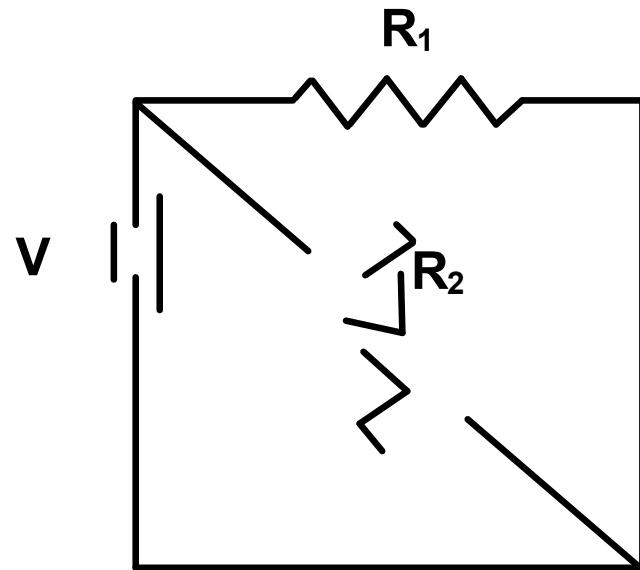
All charges must move through both resistors to get to the negative terminal.



Charges pass through either R_1 or R_2 but not both.

Circuit Diagrams

Are the following sets of resistors in series or parallel?



Answer



Answer

Circuit Diagrams

Parallel

Series

The "test" is to trace the shortest route around the circuit. The resistors found on the same route are in series; those not found on the same route are in parallel to those that were.

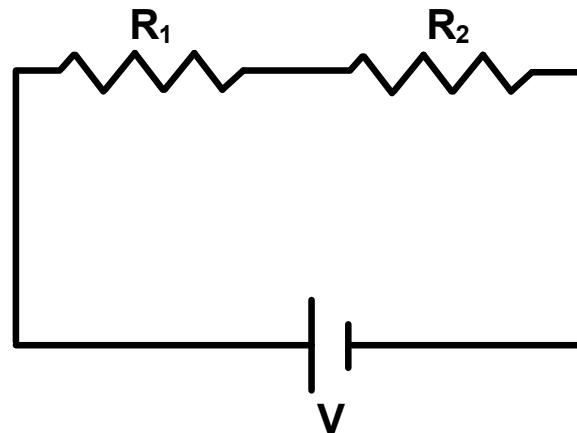


Equivalent Resistance

Resistors and voltage from batteries determine the current.

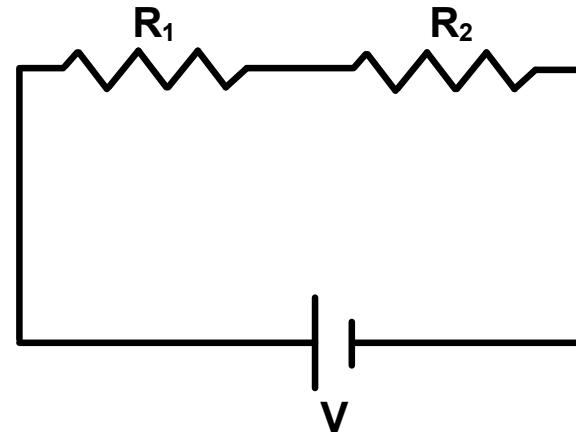
Circuits can be redrawn as if there were only a single resistor and battery. By reducing the circuit this way, the circuit becomes easier to study.

The process of reducing the resistors in a circuit is called finding the equivalent resistance (R_{eq}).



Series Circuits: Equivalent Resistance

What happens to the current in the circuit to the right?



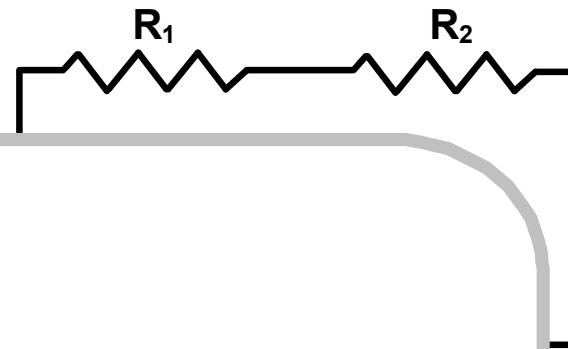
Answer



Series Circuits: Equivalent Resistance

What happens to the current in the circuit to the right?

Answer

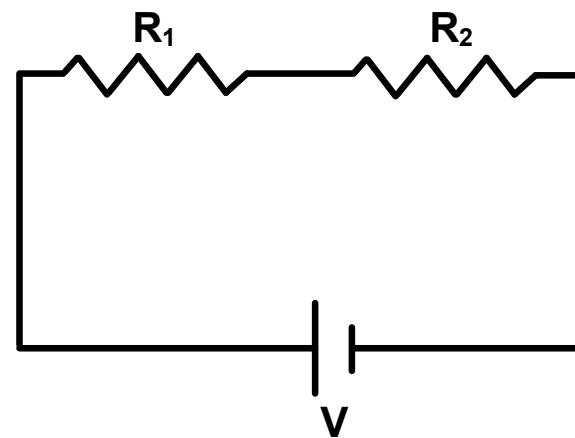


The current passing through all parts of a series circuit is the same. For example: $I = I_1 = I_2$



Series Circuits: Equivalent Resistance

What happens to the voltage as it moves around the circuit?



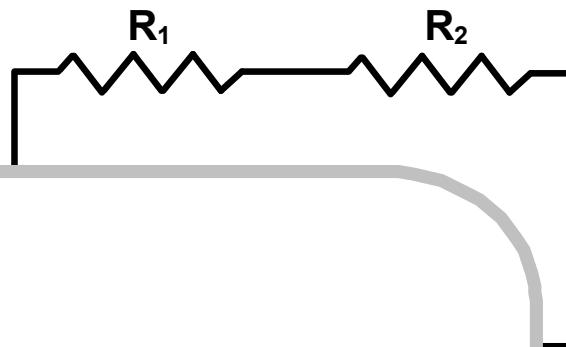
Answer



Series Circuits: Equivalent Resistance

What happens to the voltage as it moves around the circuit?

Answer



The sum of the voltage drops across each of the resistors in a series circuit equals the voltage of the battery.

For example: $V = V_1 + V_2$



Series Circuits: Equivalent Resistance

If $V = V_1 + V_2 + V_3 + \dots$

substitute Ohm's Law solved for V is: $V = IR$

$$IR = I_1R_1 + I_2R_2 + I_3R_3$$

but since current (I) is the same everywhere in a series circuit,

$$IR = IR_1 + IR_2 + IR_3$$

$$I = I_1 = I_2 = I_3$$

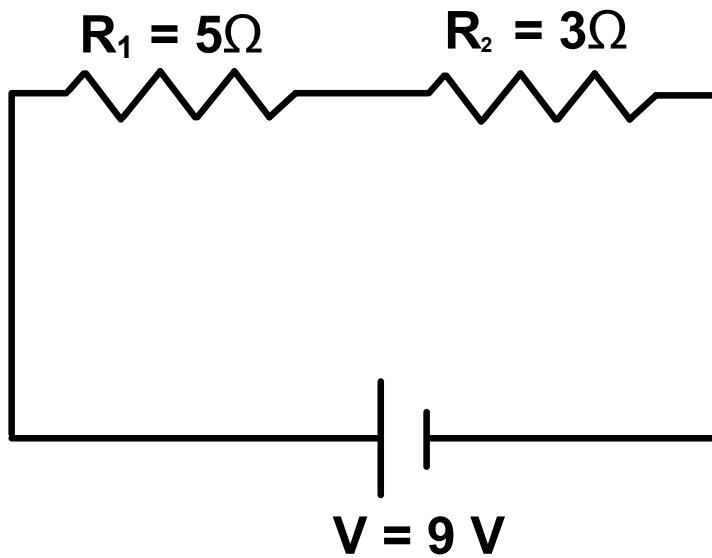
$$R_{eq} = R_1 + R_2 + R_3 + \dots$$

Now divide by I

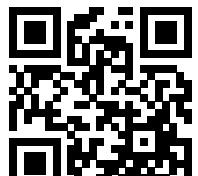


- find the equivalent resistance (R_{eq}) of a series circuit,
- add the resistance of all the resistors. If you add more resistors to a series circuit, what happens to the resistance?

28 What is the equivalent resistance in this circuit?

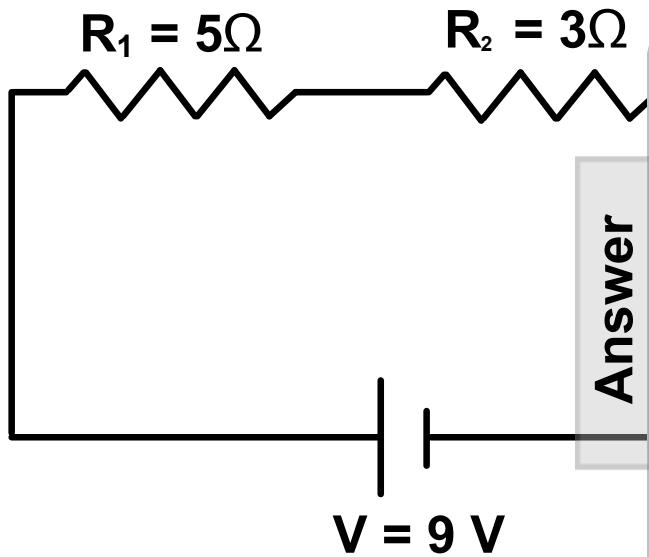


Answer



<http://njc.tl/nw>

28 What is the equivalent resistance in this circuit?



Answer

Resistors in series:

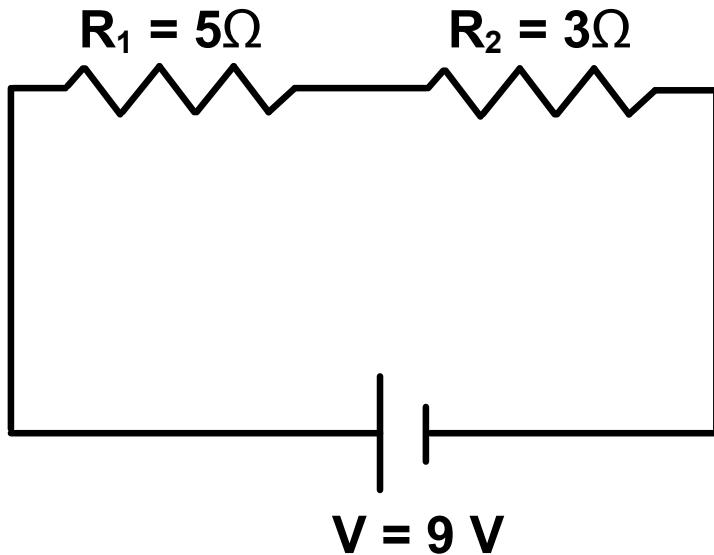
$$R_{net} = R_1 + R_2 = 5\Omega + 3\Omega$$

$$R_{net} = 8\Omega$$

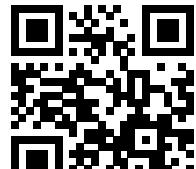


<http://njc.tl/nw>

29 What is the total current at any spot in the circuit?

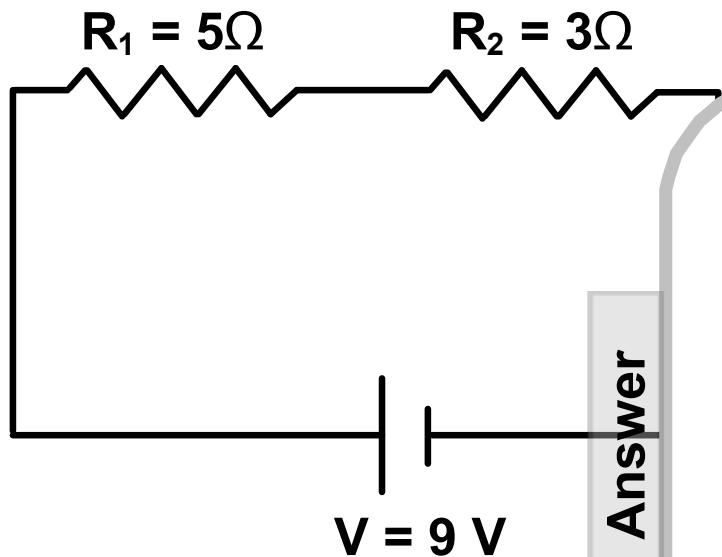


Answer



<http://njc.tl/nx>

29 What is the total current at any spot in the circuit?



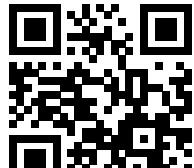
Answer

Resistors in series:

$$R_{net} = R_1 + R_2 = 5\Omega + 3\Omega$$

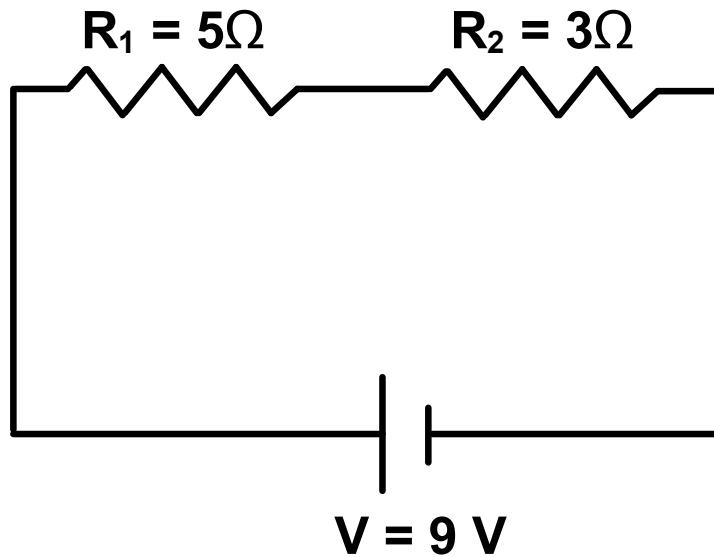
$$R_{net} = 8\Omega$$

$$I = \frac{V}{R} = \frac{9V}{8\Omega} = 1.125A$$



<http://njc.tl/nx>

30 What is the voltage drop across R_1 ?

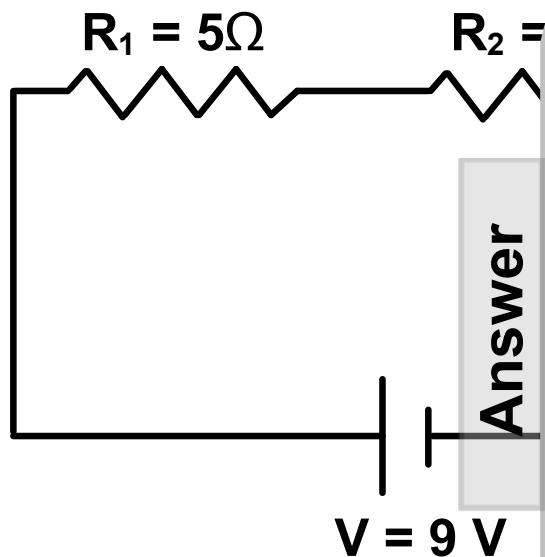


Answer



<http://njc.tl/ny>

30 What is the voltage drop across R_1 ?



Resistors in series:

$$R_{net} = R_1 + R_2 = 5\Omega + 3\Omega$$

$$R_{net} = 8\Omega$$

Net Current/equal everywhere:

$$I = \frac{V}{R} = \frac{9V}{8\Omega} = 1.125A$$

Voltage Drop across R_1 :

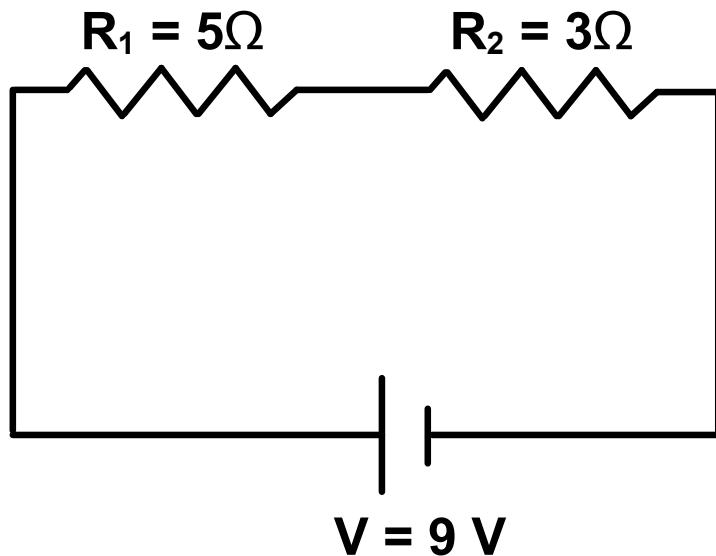
$$V_1 = IR_1 = (1.125A)(5\Omega)$$

$$V_1 = 5.625V$$



<http://njc.tl/ny>

31 What is the voltage drop across R_2 ?



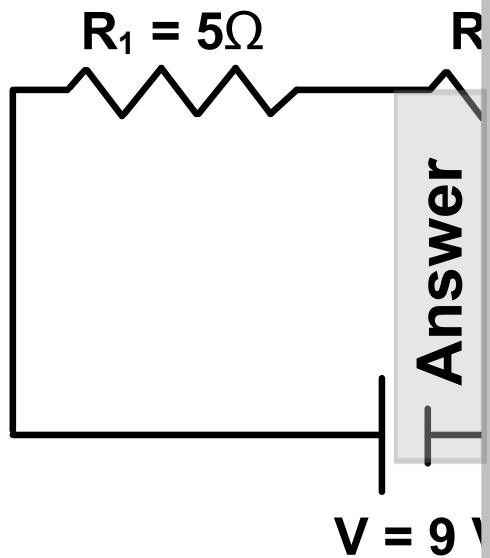
Answer

hint: A good way to check your work is to see if the voltage drop across all resistors equals the total voltage in the circuit.



<http://njc.tl/nz>

31 What is the voltage drop across R_2 ?



Net Current/equal everywhere:
Resistors in series:

$$R_{net} = R_1 + R_2 = 5\Omega + 3\Omega$$

$$R_{net} = 8\Omega$$

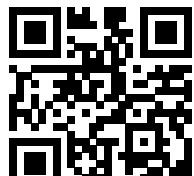
$$I = \frac{V}{R} = \frac{9V}{8\Omega} = 1.125A$$

Voltage Drop across R_2 :

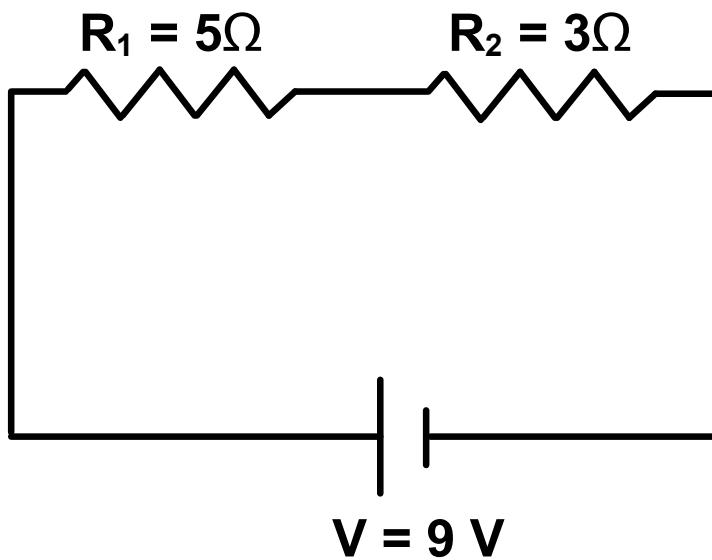
$$V_2 = IR_2 = (1.125A)(3\Omega)$$

$$V_2 = 3.375V$$

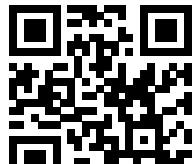
hint: A good way to find the voltage drop across all resistors is to multiply current times resistance.



32 How much power is used by R_1 ?

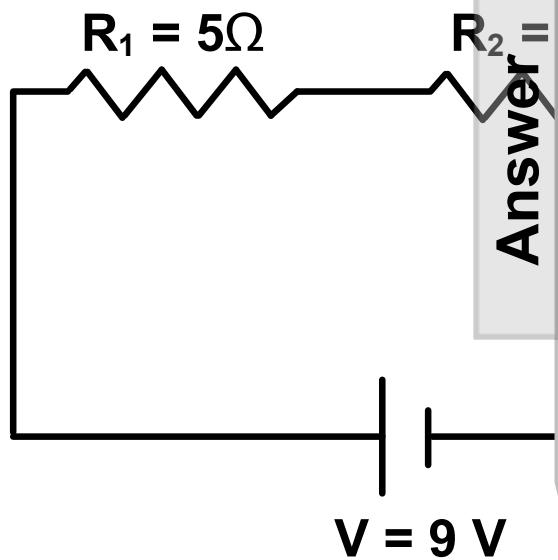


Answer



<http://njc.tl/o0>

32 How much power is used by R_1 ?



Net Current/equal everywhere:

$$I = \frac{V}{R} = \frac{9V}{8\Omega} = 1.125A$$

Voltage Drop across R_1 :

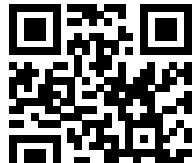
$$V_1 = IR_1 = (1.125A)(5\Omega)$$

$$V_1 = 5.625V$$

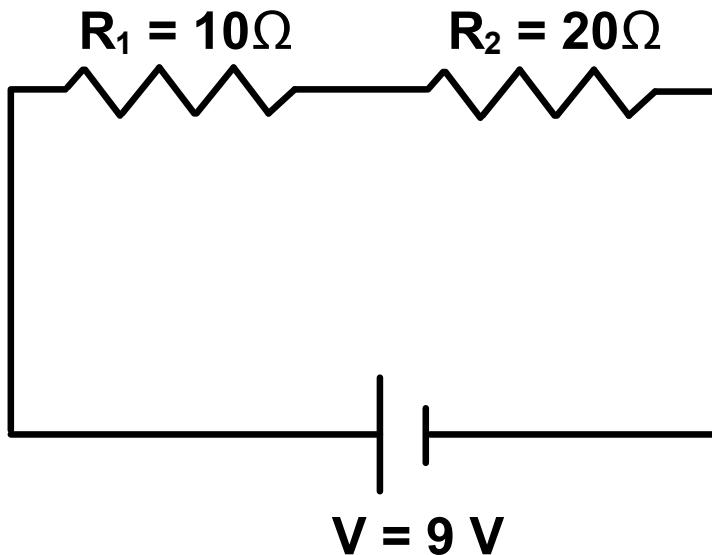
Power used by R_1 :

$$P = IV = (1.125A)(5.625V)$$

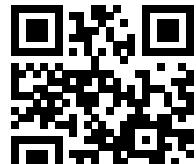
$$P = 6.33W$$



33 What is the equivalent resistance in this circuit?

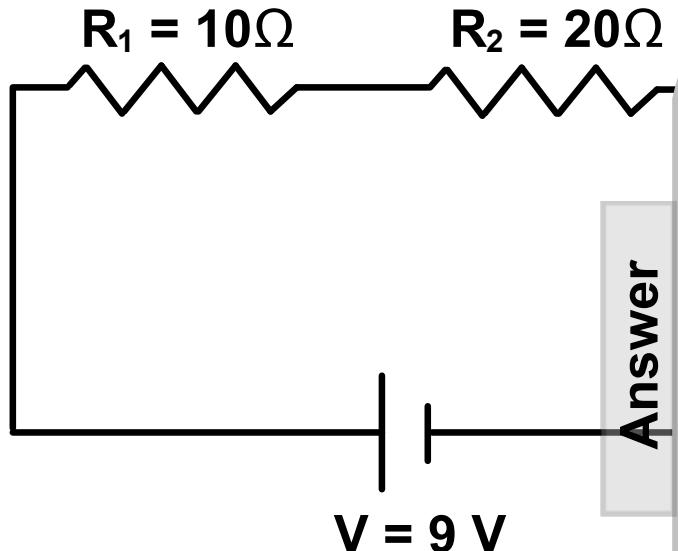


Answer



<http://njc.tl/o1>

33 What is the equivalent resistance in this circuit?



Answer

Resistors in series:

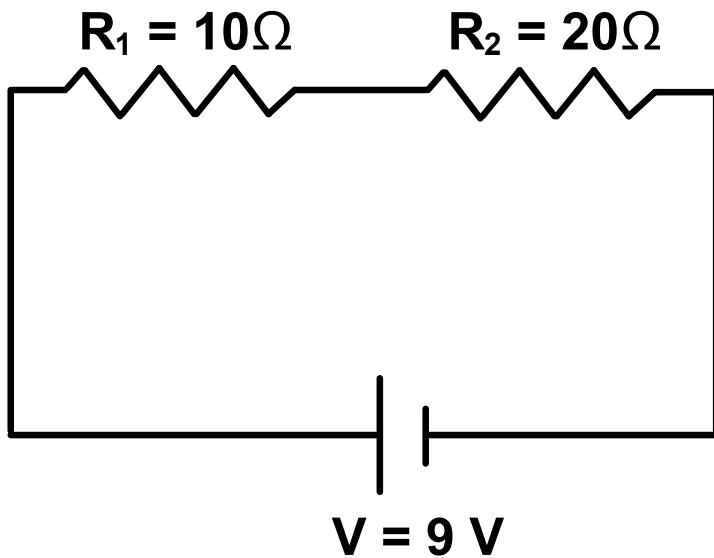
$$R_{net} = R_1 + R_2 = 10\Omega + 20\Omega$$

$$R_{net} = 30\Omega$$

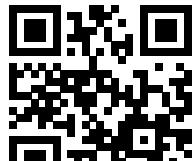


<http://njc.tl/o1>

34 What is the total current at any spot in the circuit?

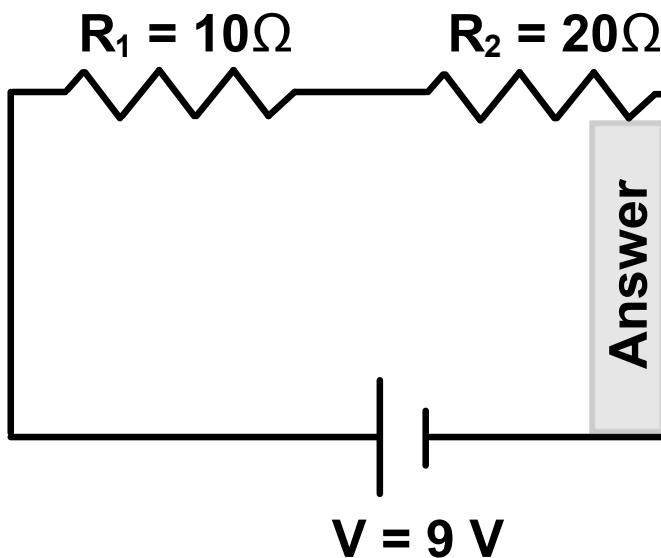


Answer



<http://njc.tl/o1>

34 What is the total current at any spot in the circuit?



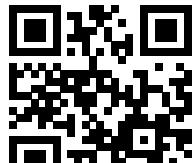
Answer

Resistors in series:

$$R_{net} = R_1 + R_2 = 10\Omega + 20\Omega$$

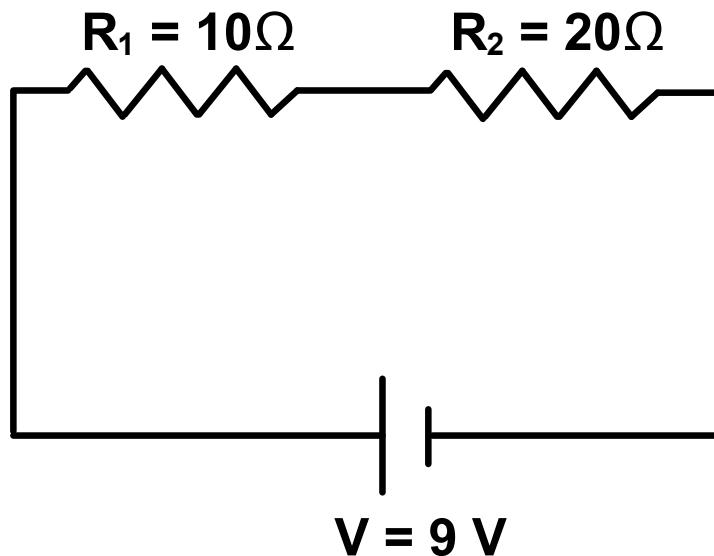
$$R_{net} = 30\Omega$$

$$I = \frac{V}{R} = \frac{9V}{30\Omega} = .3A$$

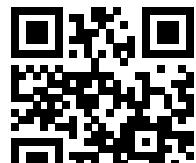


<http://njc.tl/o1>

35 What is the voltage drop across R_1 ?

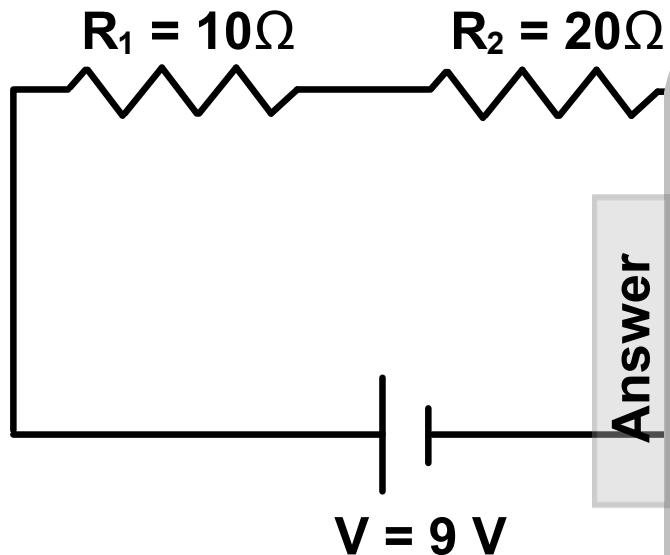


Answer



<http://njc.tl/o1>

35 What is the voltage drop across R_1 ?



Resistors in series:

$$R_{net} = R_1 + R_2 = 10\Omega + 20\Omega$$

$$R_{net} = 30\Omega$$

Net Current/equal everywhere:

$$I = \frac{V}{R} = \frac{9V}{30\Omega} = .3A$$

Voltage Drop across R_1 :

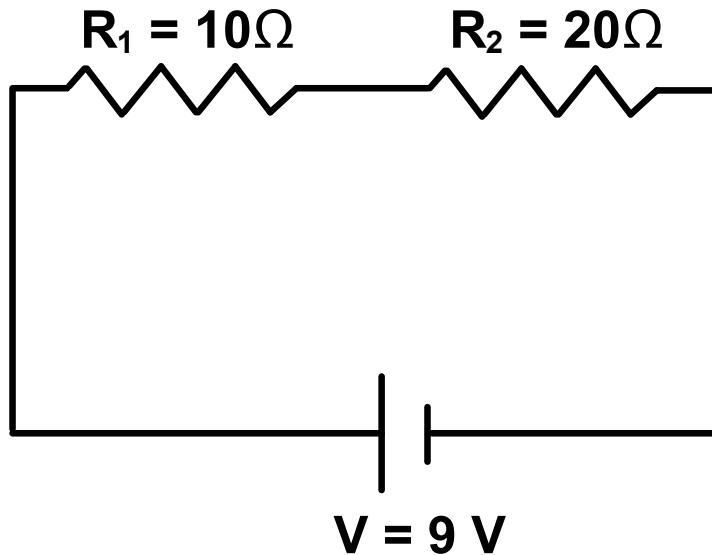
$$V_1 = IR_1 = (.3A)(10\Omega)$$

$$V_1 = 3V$$

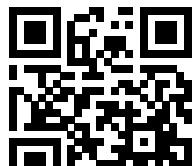


<http://njc.tl/o1>

36 What is the voltage drop across R_2 ?

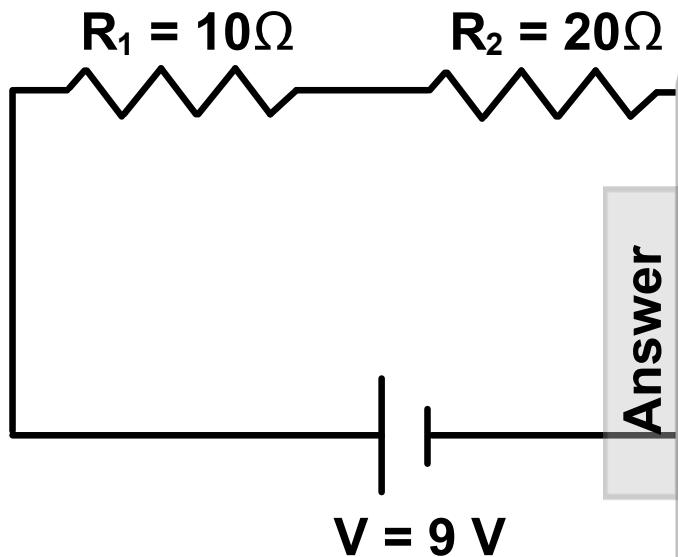


Answer



<http://njc.tl/o2>

36 What is the voltage drop across R_2 ?



Answer

Resistors in series:

$$R_{net} = R_1 + R_2 = 10\Omega + 20\Omega$$

$$R_{net} = 30\Omega$$

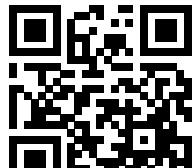
Net Current/equal everywhere:

$$I = \frac{V}{R} = \frac{9V}{30\Omega} = .3A$$

Voltage Drop across R_2 :

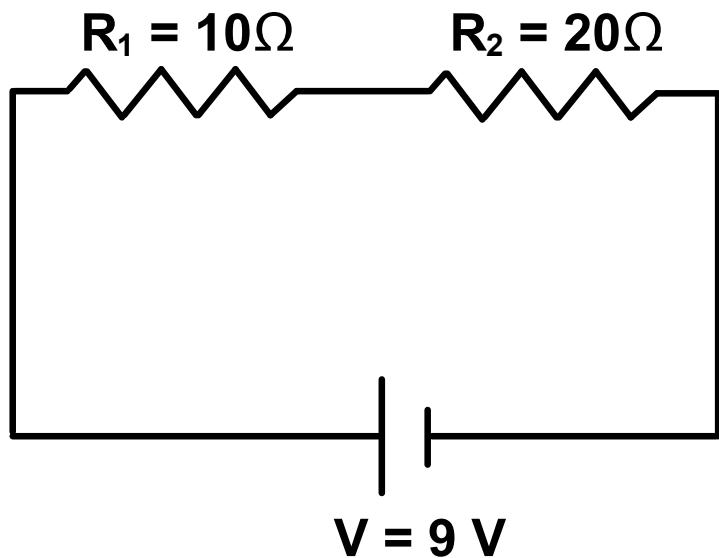
$$V_2 = IR_2 = (.3A)(20\Omega)$$

$$V_2 = 6V$$

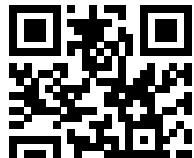


<http://njc.tl/o2>

37 How much power is used by R_1 ?

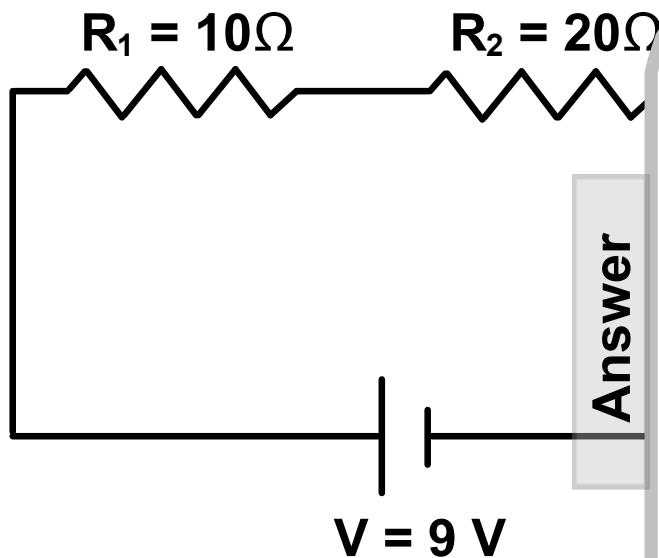


Answer



<http://njc.tl/o3>

37 How much power is used by R_1 ?



Net Current/equal everywhere:

$$I = \frac{V}{R} = \frac{9V}{30\Omega} = .3A$$

Voltage Drop across R_1 :

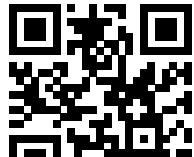
$$V_1 = IR_1 = (.3A)(10\Omega)$$

$$V_1 = 3V$$

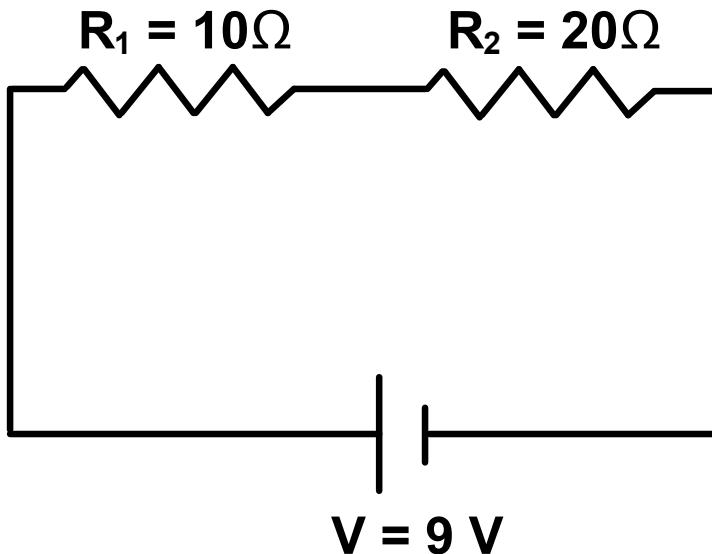
Power used by R_1 :

$$P = IV = (.3A)(3V)$$

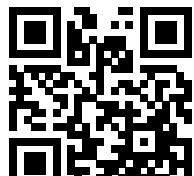
$$P = .9W$$



38 How much power is used by R_2 ?

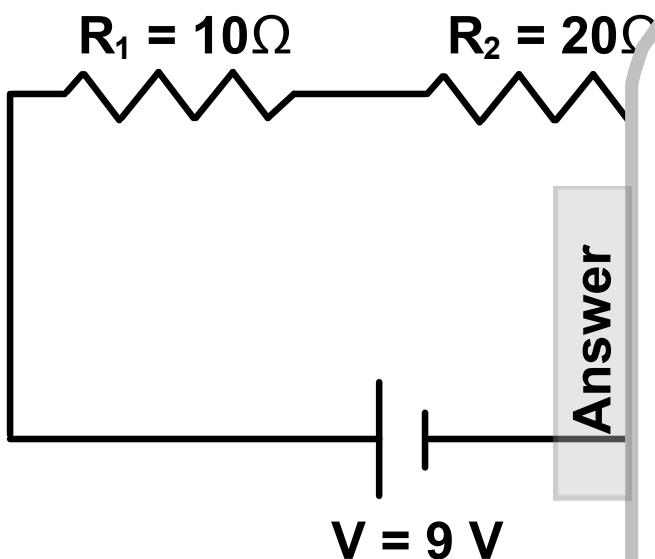


Answer



<http://njc.tl/o4>

38 How much power is used by R_2 ?



Net Current/equal everywhere:

$$I = \frac{V}{R} = \frac{9V}{30\Omega} = .3A$$

Voltage Drop across R_2 :

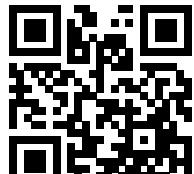
$$V_2 = IR_2 = (.3A)(20\Omega)$$

$$V_1 = 6V$$

Power used by R_2 :

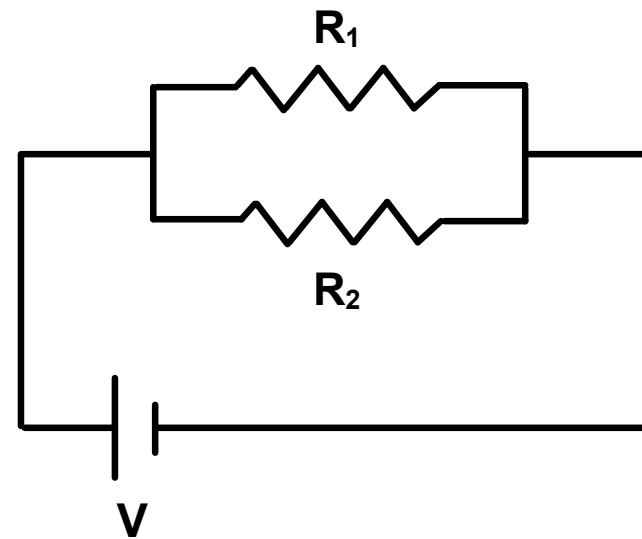
$$P = IV = (.3A)(6V)$$

$$P = 1.8W$$

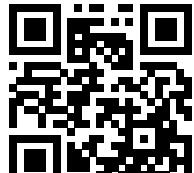


Parallel Circuits: Equivalent Resistance

What happens to the current in the circuit to the right?



Answer

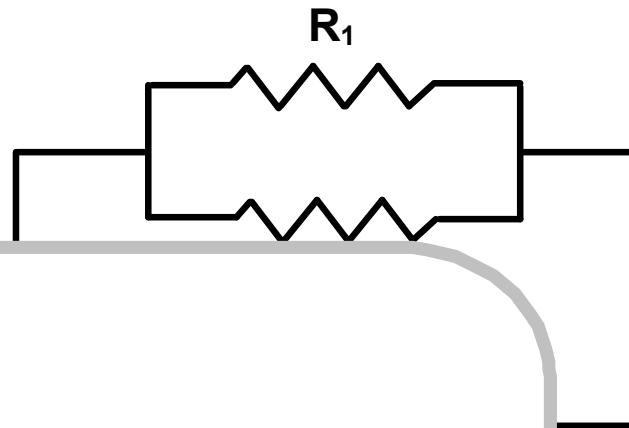


<http://njc.tl/o5>

Parallel Circuits: Equivalent Resistance

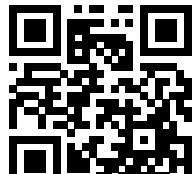
What happens to the current in the circuit to the right?

Answer



The sum of the currents through each of the resistors in a parallel circuit equals the current of the battery.

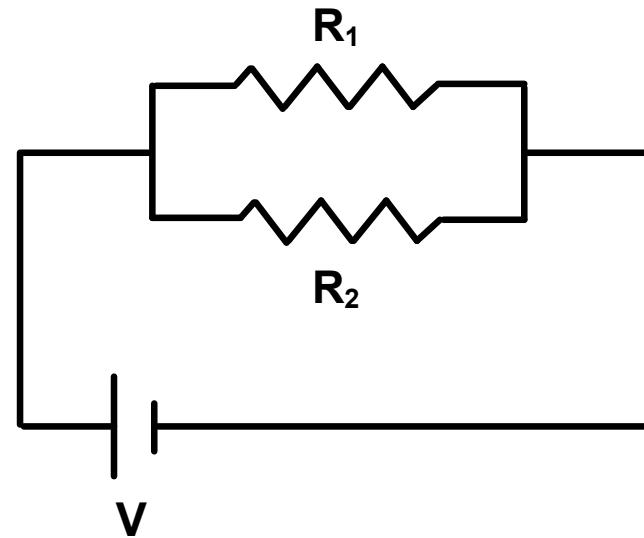
For example: $I = I_1 + I_2$



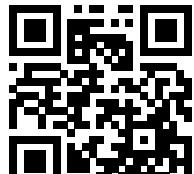
<http://njc.tl/o5>

Parallel Circuits: Equivalent Resistance

What happens to the voltage as it moves around the circuit?



Answer

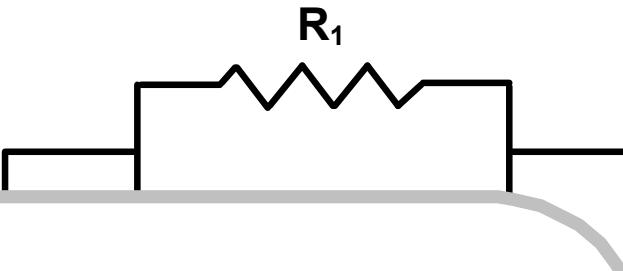


<http://njc.tl/o5>

Parallel Circuits: Equivalent Resistance

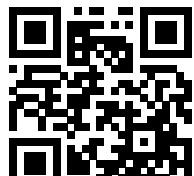
What happens to the voltage as it moves around the circuit?

Answer



The voltage across all the resistors in a parallel circuit is the same.

For example: $V = V_1 = V_2$



<http://njc.tl/o5>

Parallel Circuits: Equivalent Resistance

If $I = I_1 + I_2 + I_3$

$$\frac{V}{R} = \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3}$$

$$\frac{V}{R} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

$$\frac{V}{R} = V \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)$$



$$+ \frac{1}{R_2} + \frac{1}{R_3}$$

Rewrite Ohm's Law for I and substitute for each resistor

Also, since $V = V_1 = V_2 = V_3$ so we can substitute V for any other voltage

Voltage is a common factor, so factor it out!

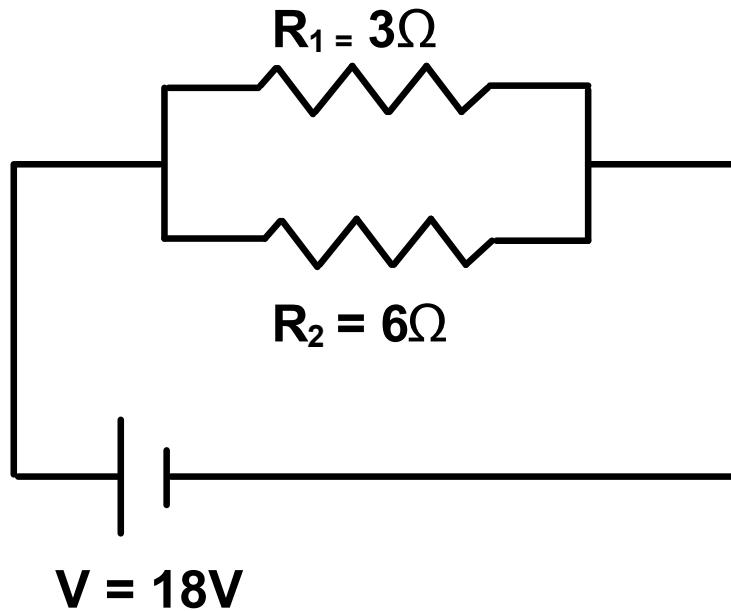
Divide by V to eliminate voltage from the equation.



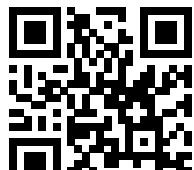
you add more resistors in parallel, what will happen to the resistance of the circuit?

<http://njc.tl/o5>

39 What is the equivalent resistance in the circuit?

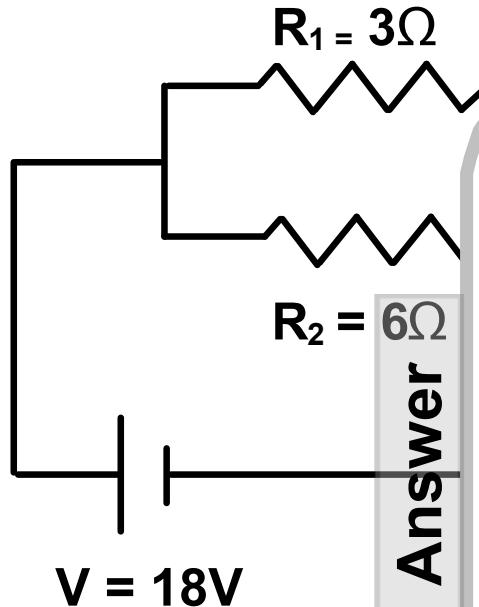


Answer



<http://njc.tl/o6>

39 What is the equivalent resistance in the circuit?



Answer

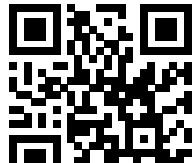
$$\frac{1}{R_{net}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\frac{1}{R_{net}} = \frac{1}{3\Omega} + \frac{1}{6\Omega}$$

$$\frac{1}{R_{net}} = \frac{2}{6\Omega} + \frac{1}{6\Omega}$$

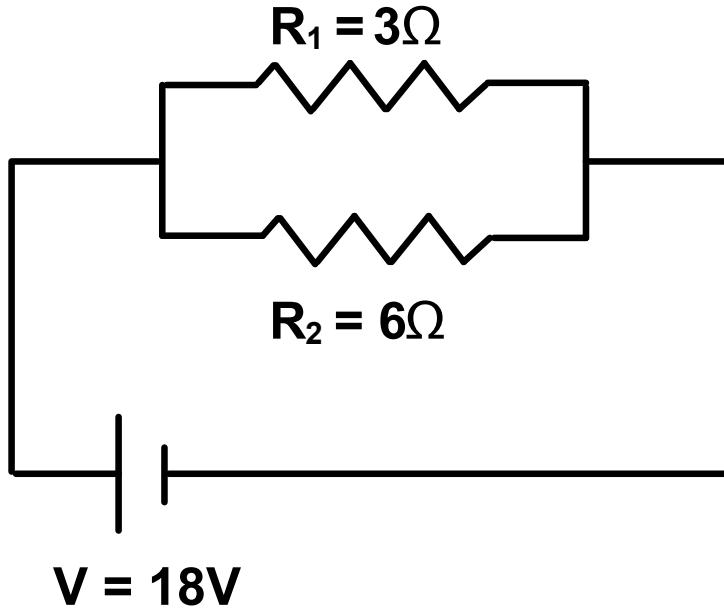
$$\frac{1}{R_{net}} = \frac{3}{6\Omega}$$

$$R_{net} = 2\Omega$$

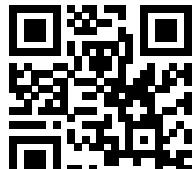


<http://njc.tl/o6>

40 What is the voltage at any spot in the circuit?

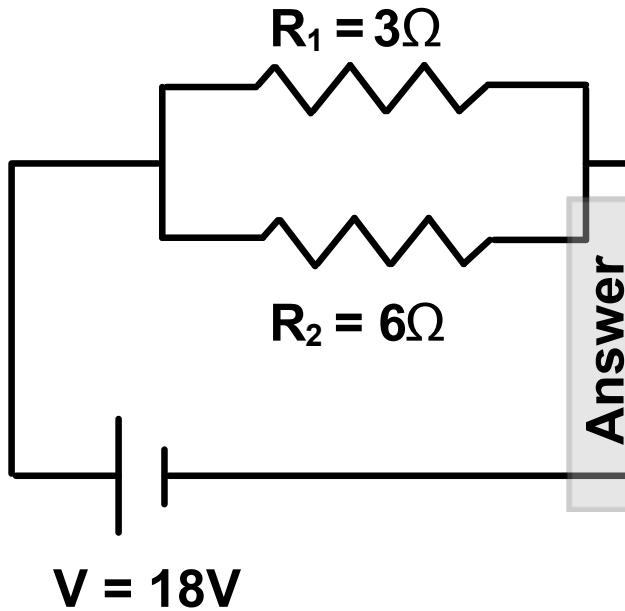


Answer



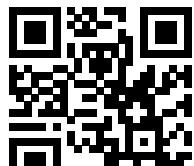
<http://njc.tl/o7>

40 What is the voltage at any spot in the circuit?



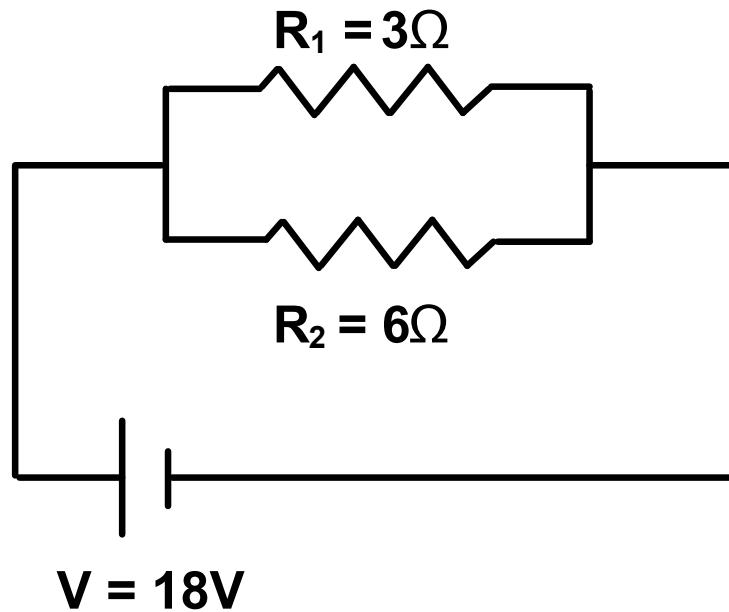
Answer

18 V



<http://njc.tl/o7>

41 What is the current through R_1 ?

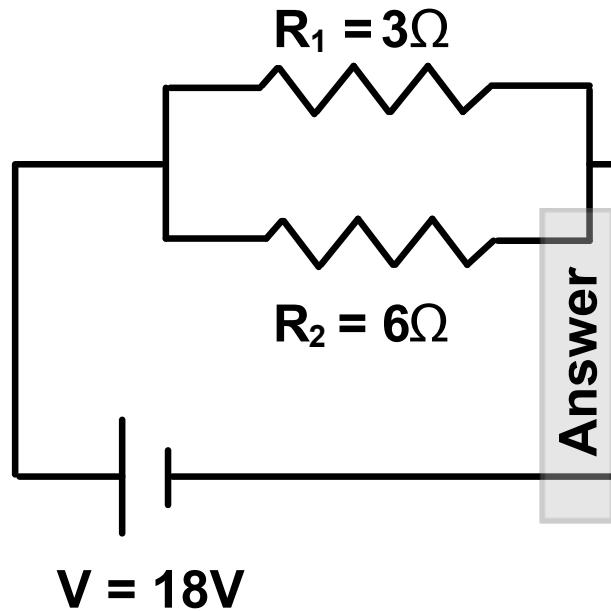


Answer



<http://njc.tl/o8>

41 What is the current through R_1 ?



Answer

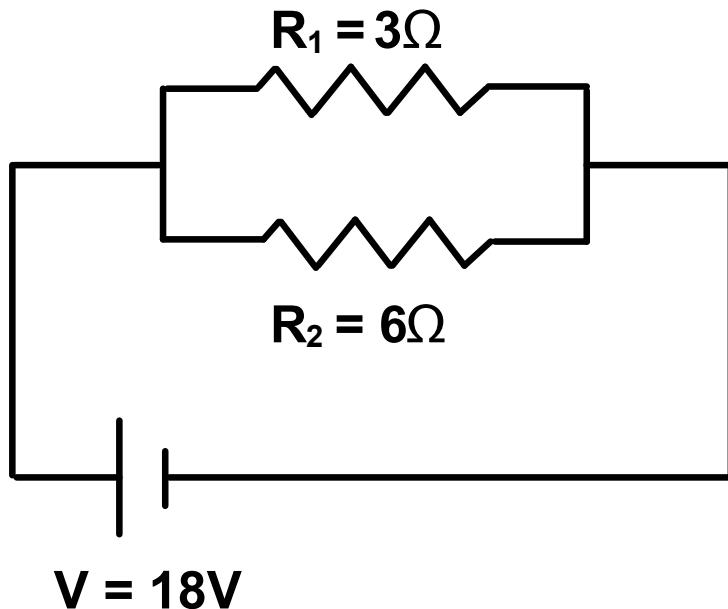
$$I_1 = \frac{V_1}{R_1} = \frac{18V}{3\Omega}$$

$$I_1 = 6A$$

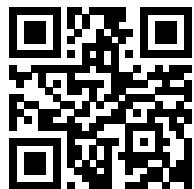


<http://njc.tl/o8>

42 What is the current through R_2 ?

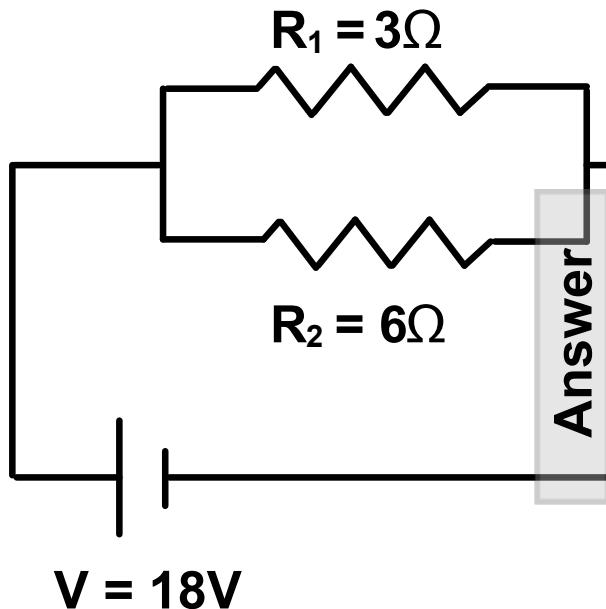


Answer



<http://njc.tl/o9>

42 What is the current through R_2 ?



Answer

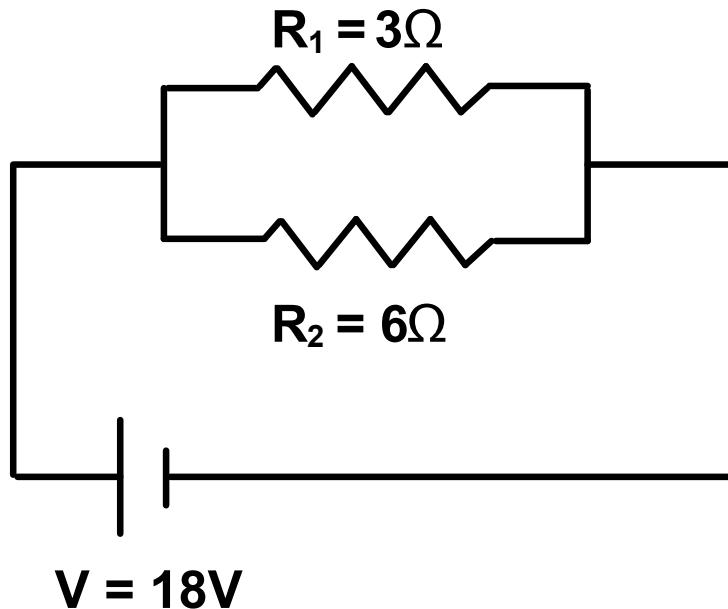
$$I_2 = \frac{V_2}{R_2} = \frac{18V}{6\Omega}$$

$$I_2 = 3A$$

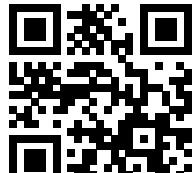


<http://njc.tl/o9>

43 What is the power used by R_1 ?

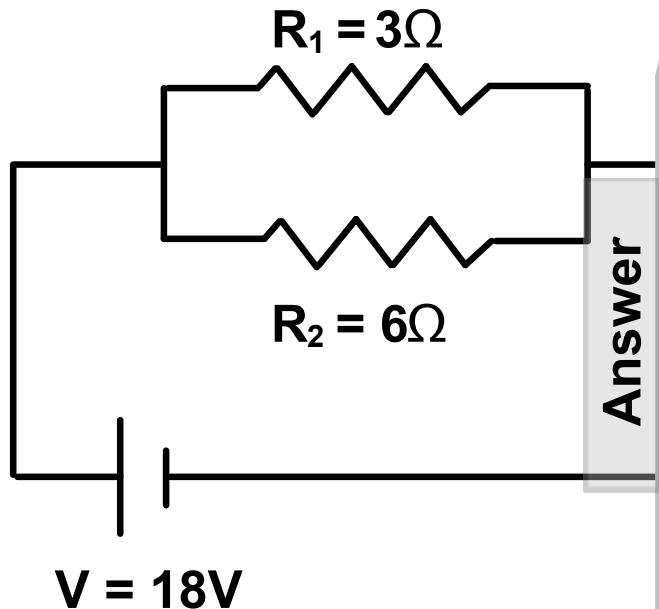


Answer



<http://njc.tl/oa>

43 What is the power used by R_1 ?



Answer

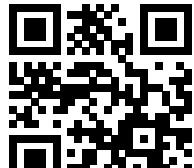
$$I_1 = \frac{V_1}{R_1} = \frac{18V}{3\Omega}$$

$$I_1 = 6A$$

Power used by R_1 :

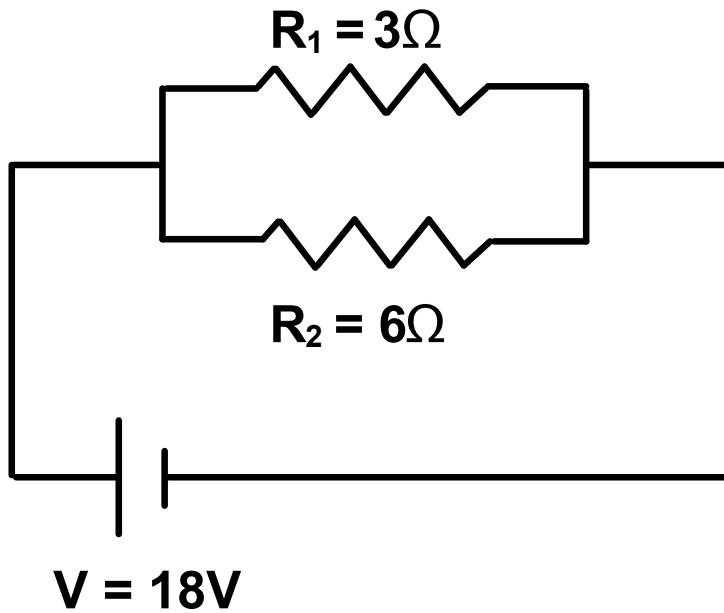
$$P_1 = I_1 V_1 = (6A)(18V)$$

$$P_1 = 108W$$

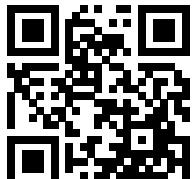


<http://njc.tl/oa>

44 What is the power used by R_2 ?

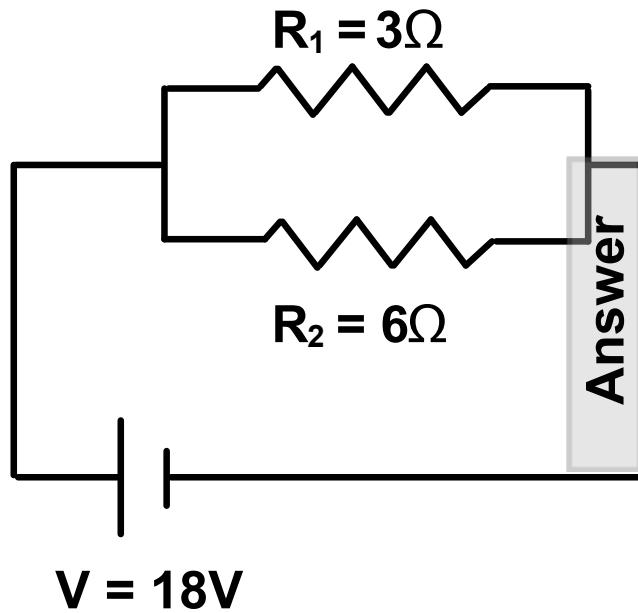


Answer



<http://njc.tl/ob>

44 What is the power used by R_2 ?



Answer

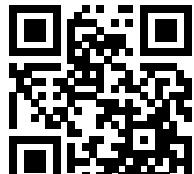
$$I_2 = \frac{V_2}{R_2} = \frac{18V}{6\Omega}$$

$$I_2 = 3A$$

Power used by R_2 :

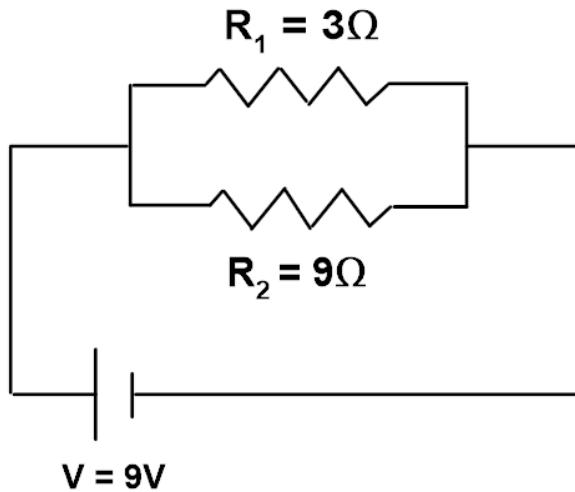
$$P_2 = I_2 V_2 = (3A)(18V)$$

$$P_2 = 54W$$

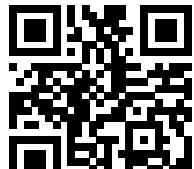


<http://njc.tl/ob>

45 What is the equivalent resistance in the circuit?

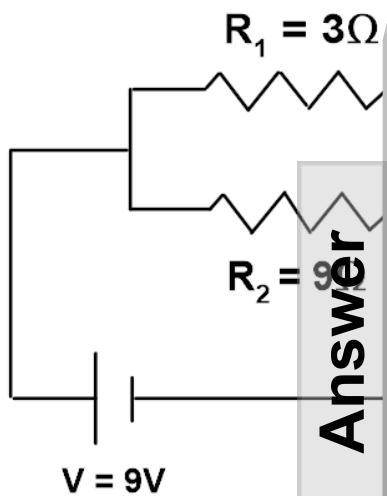


Answer



<http://njc.tl/oc>

45 What is the equivalent resistance in the circuit?



Answer

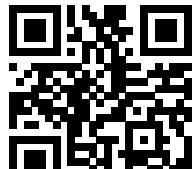
$$\frac{1}{R_{net}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\frac{1}{R_{net}} = \frac{1}{3\Omega} + \frac{1}{9\Omega}$$

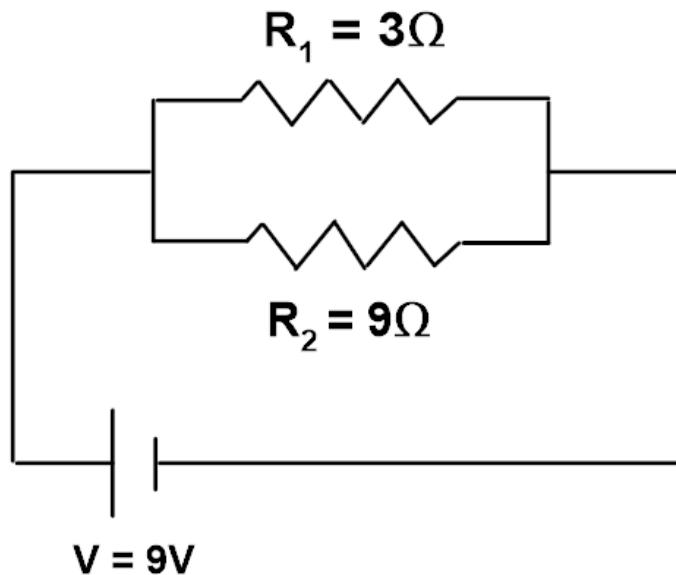
$$\frac{1}{R_{net}} = \frac{3}{9\Omega} + \frac{1}{9\Omega}$$

$$\frac{1}{R_{net}} = \frac{4}{9\Omega}$$

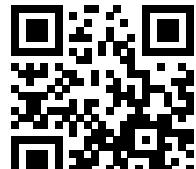
$$R_{net} = 2.25\Omega$$



46 What is the voltage at any spot in the circuit?

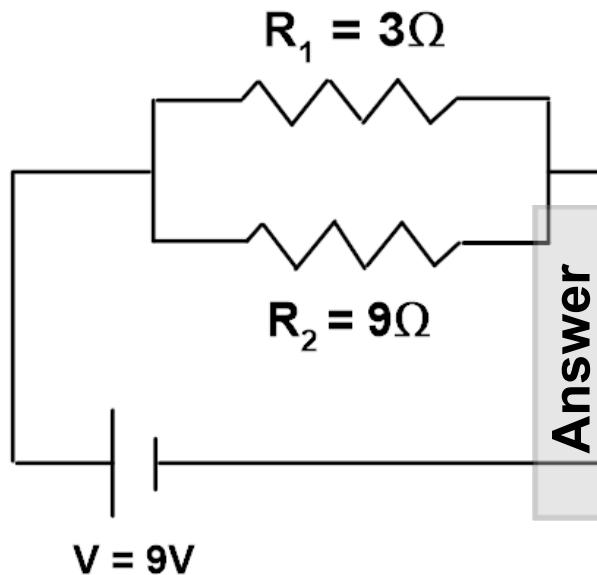


Answer



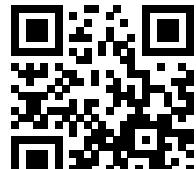
<http://njc.tl/od>

46 What is the voltage at any spot in the circuit?



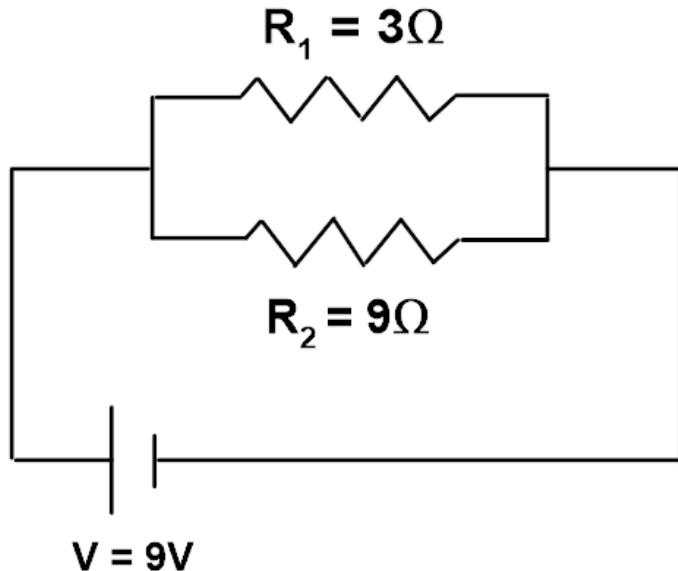
Answer

9V

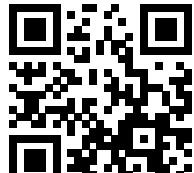


<http://njc.tl/od>

47 What is the current through R_1 ?

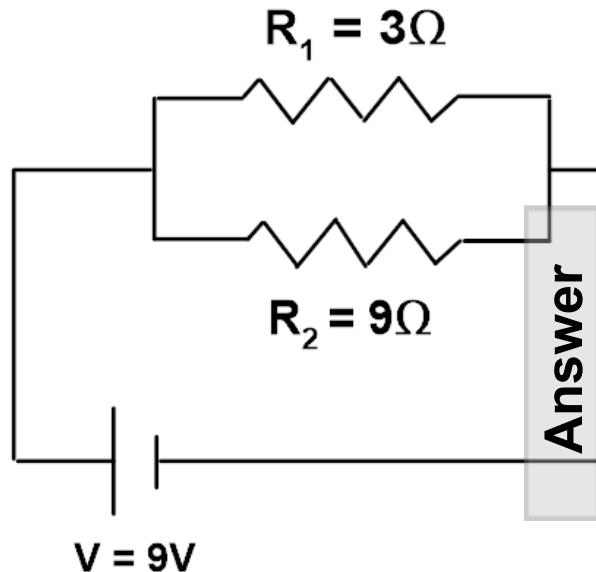


Answer



<http://njc.tl/od>

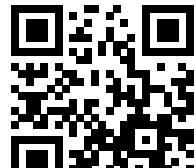
47 What is the current through R_1 ?



Answer

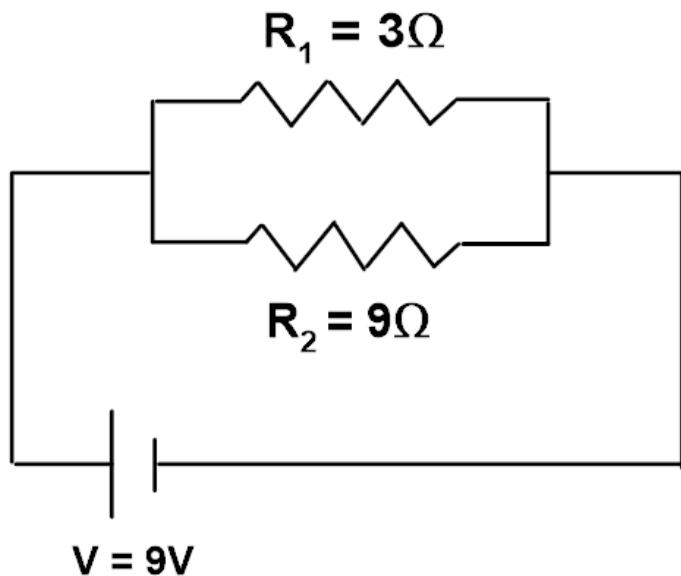
$$I_1 = \frac{V_1}{R_1} = \frac{9V}{3\Omega}$$

$$I_1 = 3A$$



<http://njc.tl/od>

48 What is the current through R_2 ?

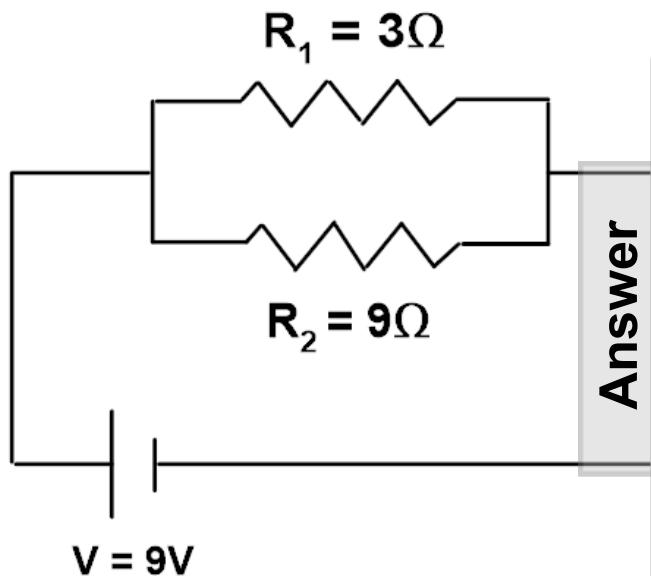


Answer



<http://njc.tl/oe>

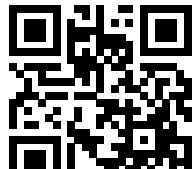
48 What is the current through R_2 ?



Answer

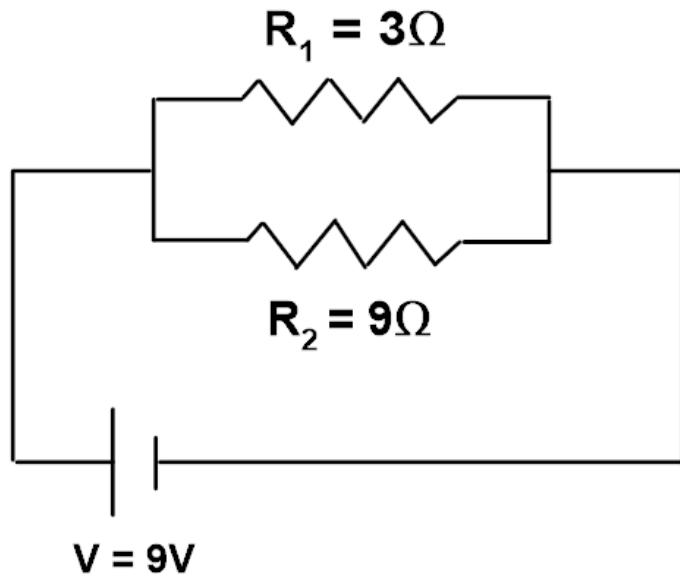
$$I_2 = \frac{V_2}{R_2} = \frac{9V}{9\Omega}$$

$$I_2 = 1A$$

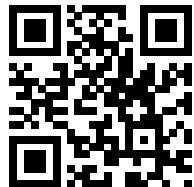


<http://njc.tl/oe>

49 What is the power used by R_1 ?

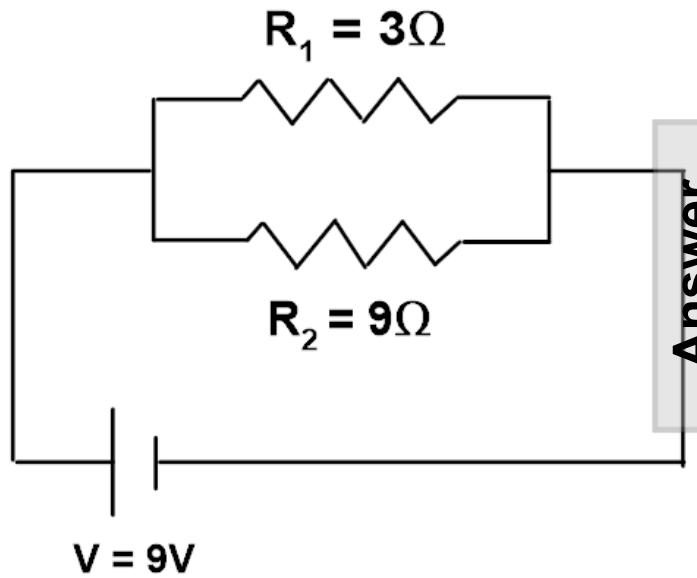


Answer



<http://njc.tl/of>

49 What is the power used by R_1 ?



Answer

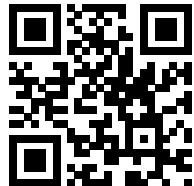
$$I_1 = \frac{V_1}{R_1} = \frac{9V}{3\Omega}$$

$$I_1 = 3A$$

Power used by R_1 :

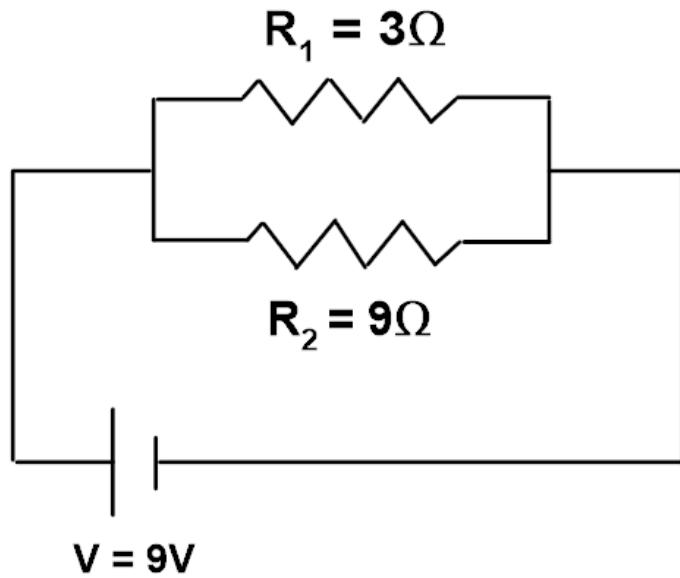
$$P_1 = I_1 V_1 = (3A)(9V)$$

$$P_1 = 27W$$

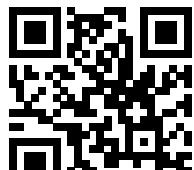


<http://njc.tl/of>

50 What is the power used by R_1 ?

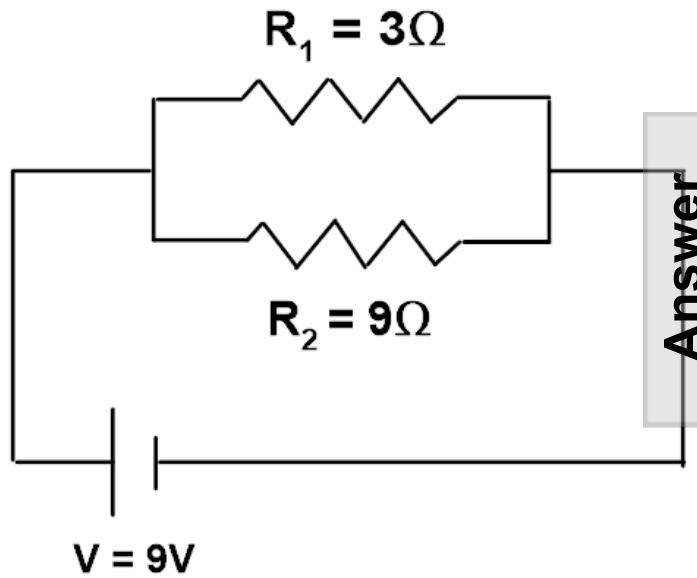


Answer



<http://njc.tl/og>

50 What is the power used by R_1 ?



Answer

$$I_1 = \frac{V_1}{R_1} = \frac{9V}{3\Omega}$$

$$I_1 = 3A$$

Power used by R_1 :

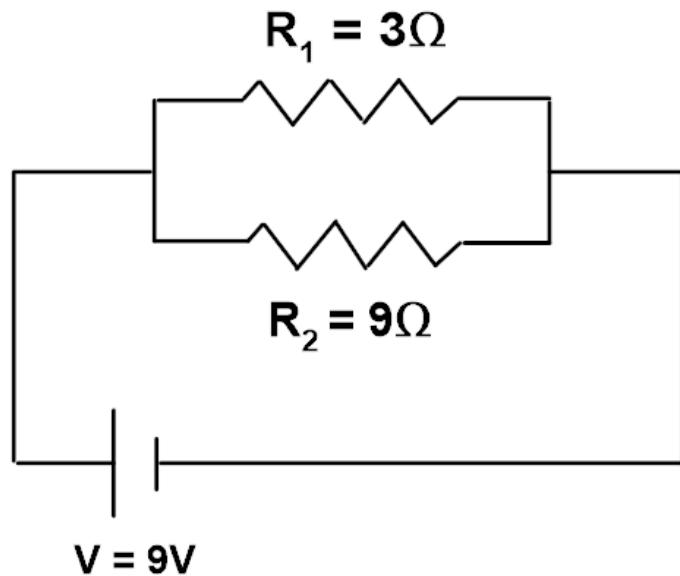
$$P_1 = I_1 V_1 = (3A)(9V)$$

$$P_1 = 27W$$



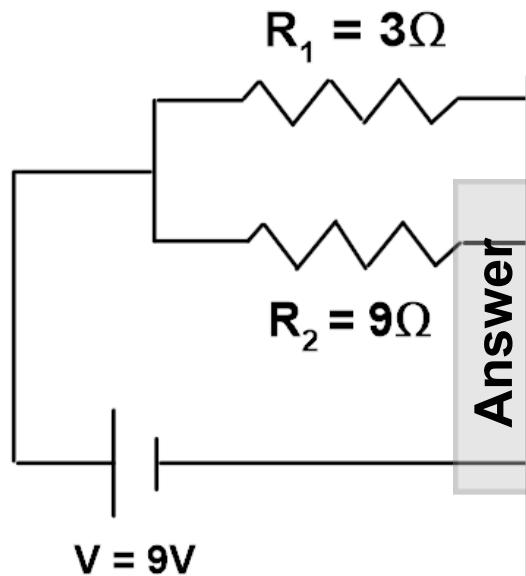
<http://njc.tl/og>

51 What is the power used by R_2 ?



Answer

51 What is the power used by R_2 ?



Answer

$$I_2 = \frac{V_2}{R_2} = \frac{9V}{9\Omega}$$

$$I_2 = 1A$$

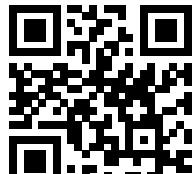
Power used by R_2 :

$$P_2 = I_2 V_2 = (9A)(9V)$$

$$P_2 = 81W$$

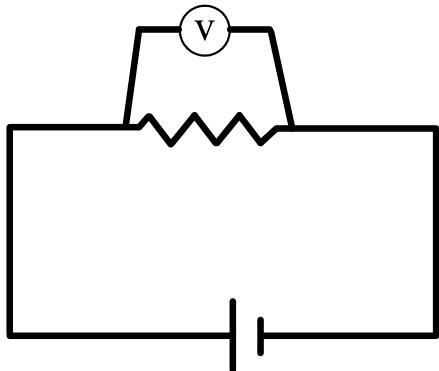
Measurement

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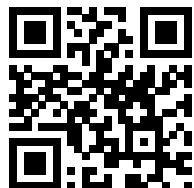
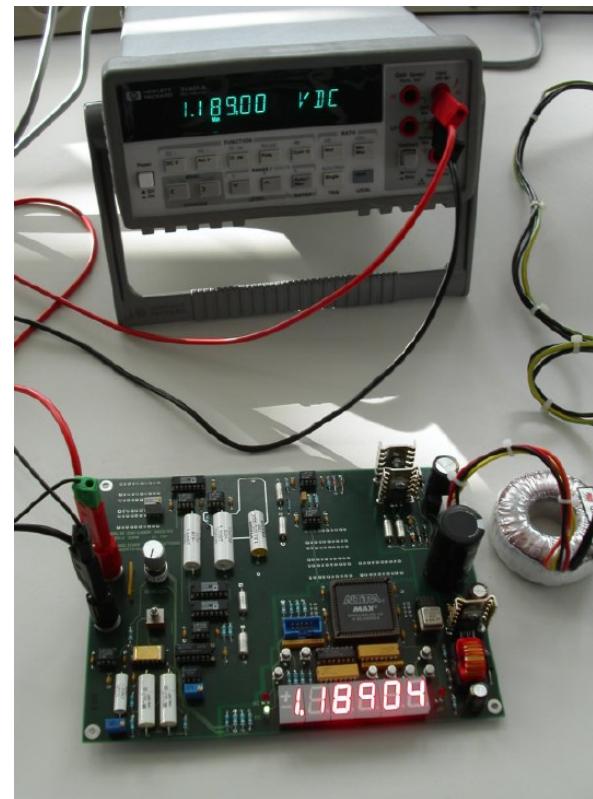
Voltmeter



Voltage is measured with a voltmeter. Voltmeters are connected in parallel and measure the difference in potential between two points.

Since circuits in parallel have the same voltage, and a voltmeter has very high resistance, very little current passes through it.

This means that it has little effect on the circuit.



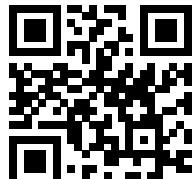
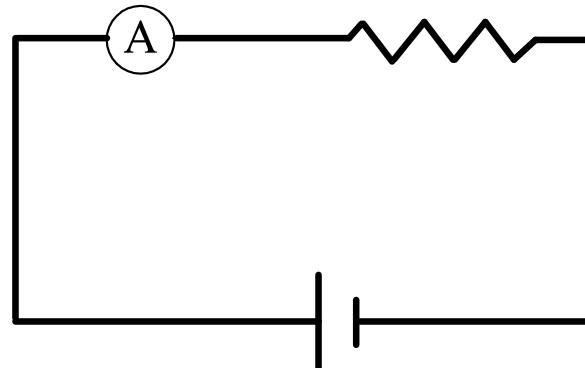
<http://njc.tl/oh>

Ammeter

Current is measured using an ammeter.



Ammeters are placed in series with a circuit. In order to not interfere with the current, the ammeter has a very low resistance.



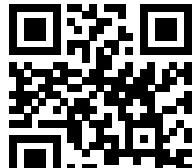
<http://njc.tl/oh>

Multimeter

Although there are separate items to measure current and voltage, there are devices that can measure both (one at a time).

These devices are called multimeters. Multimeters can also measure resistance.

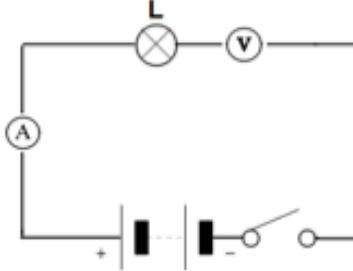
Click here for a PhET simulation on circuits



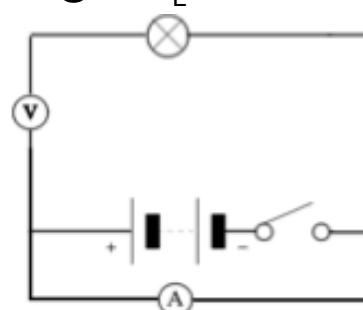
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52 A group of students prepare an experiment with electric circuits. Which of the following diagrams can be used to measure both current and voltage?

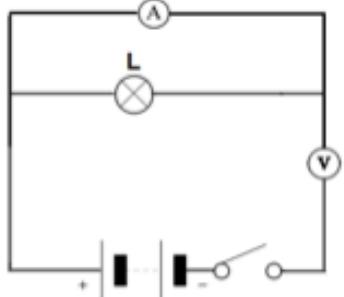
A



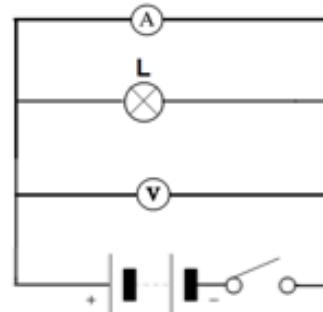
B



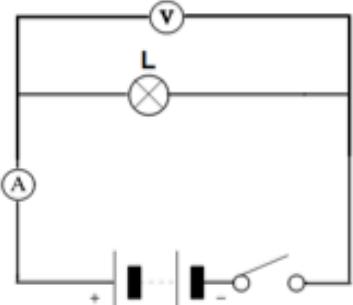
C



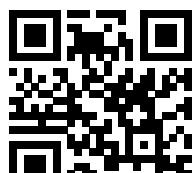
D



E



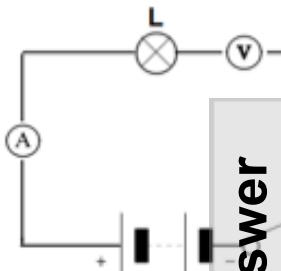
Answer



<http://njc.tl/oi>

52 A group of students prepare an experiment with electric circuits. Which of the following diagrams can be used to measure both current and voltage?

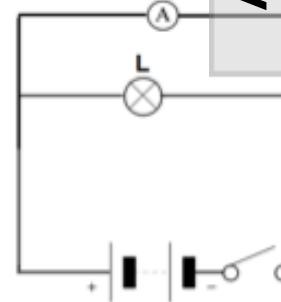
A



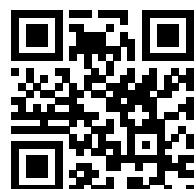
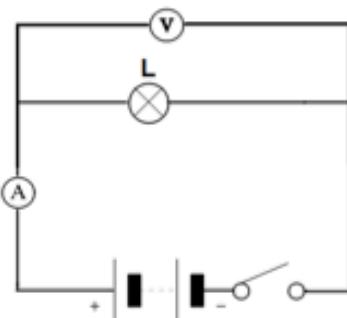
Answer

E

C

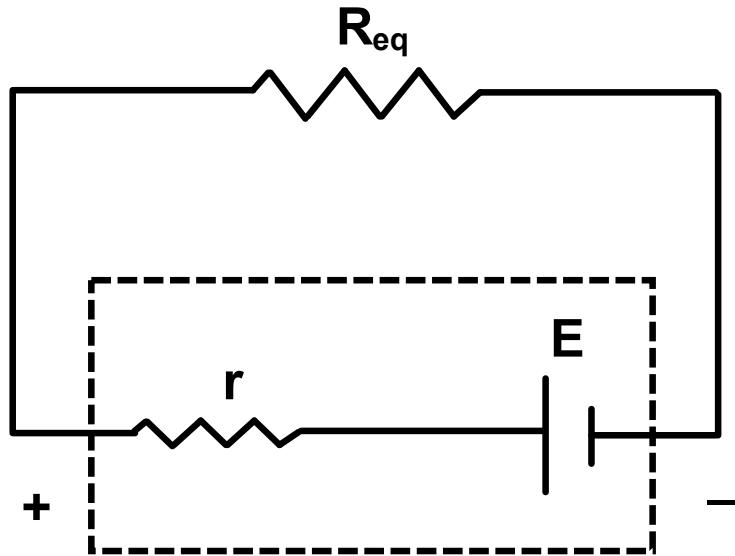


E



<http://njc.tl/oi>

Electromotive Force

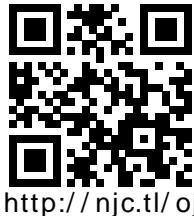


A battery is a source of voltage AND a resistor.

Each battery has a source of electromotive force and internal resistance.

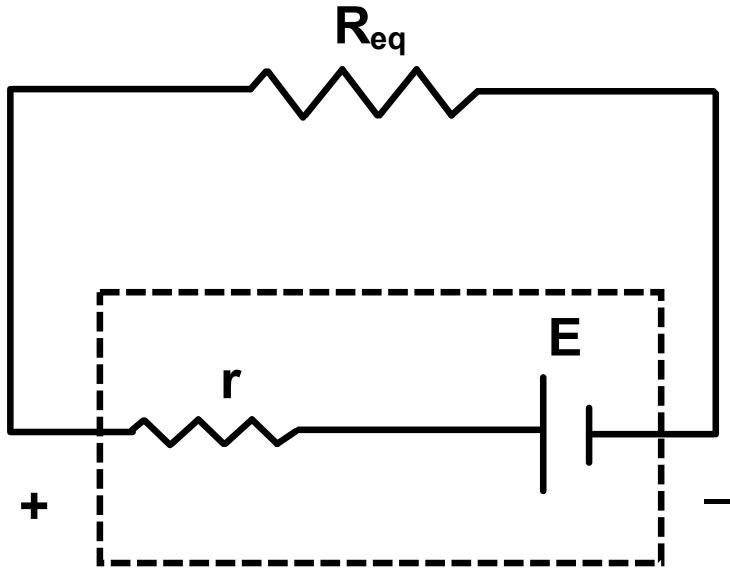
Electromotive force (EMF) is the process that carries charge from low to high voltage.

other way to think about it is that EMF is the voltage you measure when no resistance is connected to the circuit.



<http://njc.tl/oj>

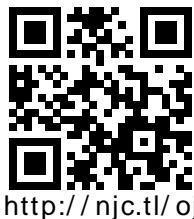
Electromotive Force



Terminal voltage (V_T) is the voltage measured when a voltmeter is across its terminals.

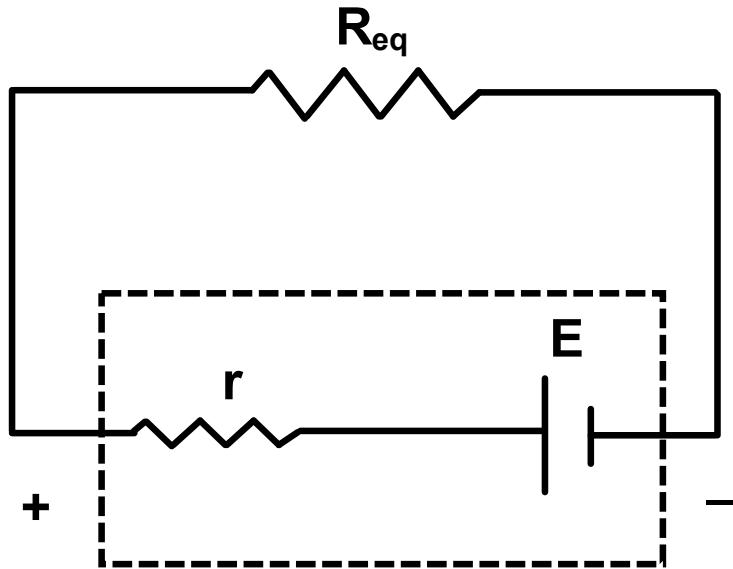
If there is no circuit attached, no current flows, and the measurement will equal the EMF.

If however a circuit is attached, the internal resistance will result in a voltage drop, and a smaller terminal voltage. $(E - Ir)$



<http://njc.tl/oj>

Terminal Voltage



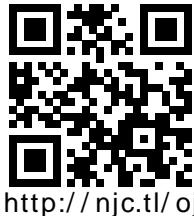
We say that the terminal voltage is:

$$V_T = E - Ir$$

Maximum current will occur when there is zero external current.

When solving for equivalent resistance in a circuit, the internal resistance of the battery is considered a series resistor.

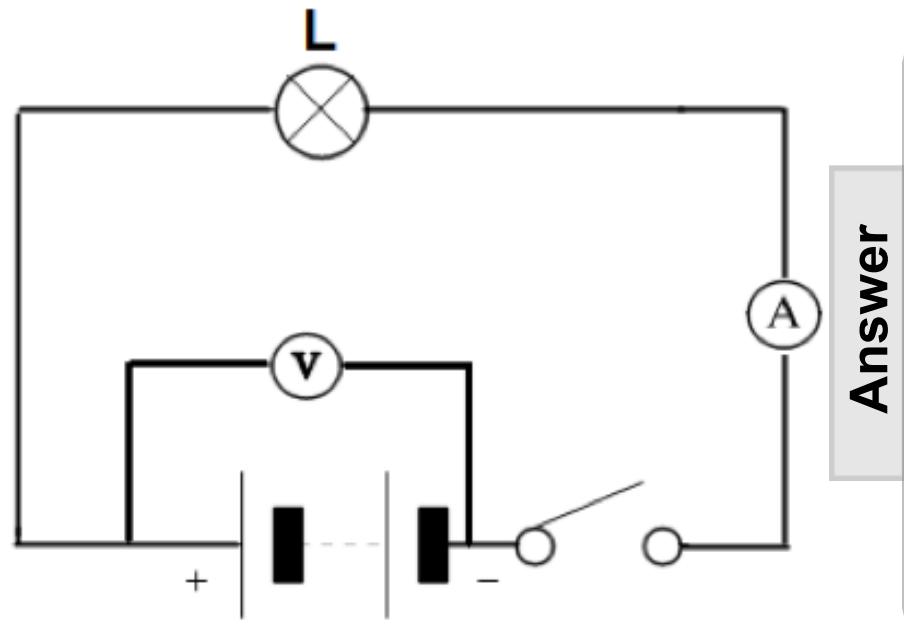
$$R_{\text{EQ}} = R_{\text{int}} + R_{\text{ext}}$$



<http://njc.tl/oj>

53 When the switch in the circuit below is open, the voltmeter reading is referred to as:

- A EMF
- B Current
- C Power
- D Terminal Voltage
- E Resistivity



Answer



<http://njc.tl/ok>

53 When the switch in the circuit below is open, the voltmeter reading is referred to as:

- A EMF
- B Current
- C Power
- D Terminal Voltage
- E Resistivity

Answer

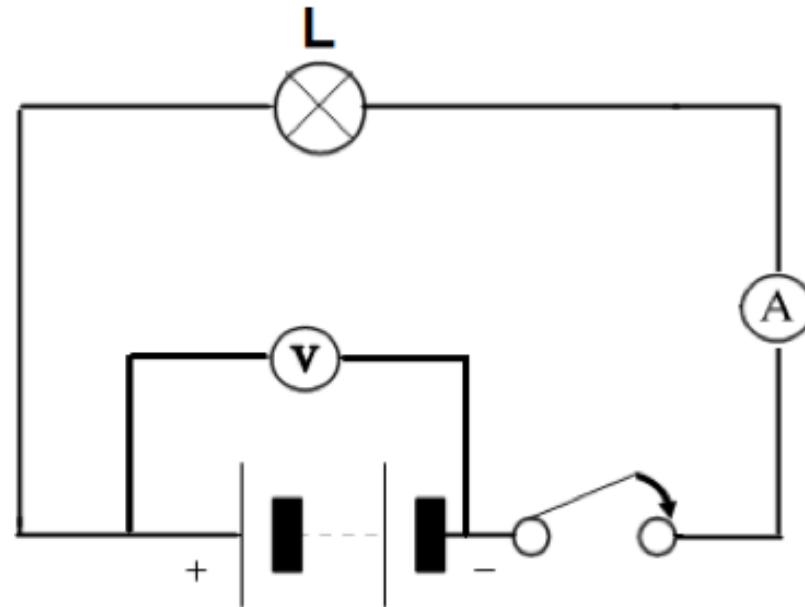
A



<http://njc.tl/ok>

54 When the switch in the circuit below is closed, the voltmeter reading is referred to as:

- A Terminal Voltage
- B EMF
- C Current
- D Resistance
- E Power



Answer

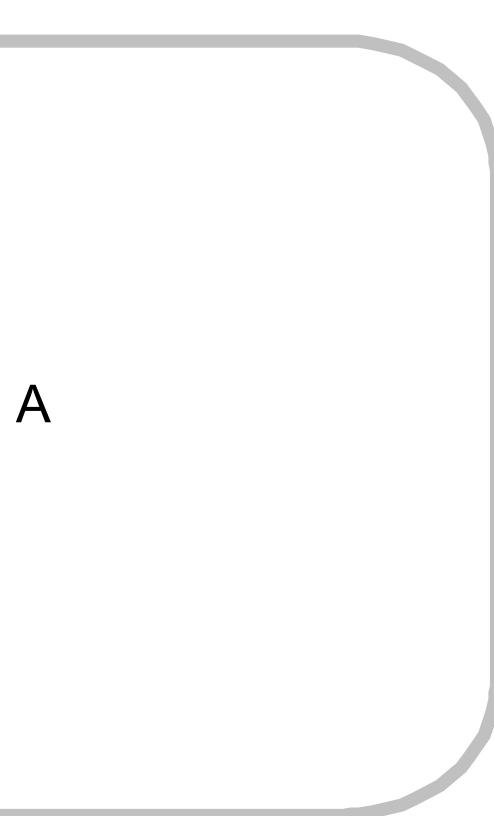


<http://njc.tl/oI>

54 When the switch in the circuit below is closed, the voltmeter reading is referred to as:

- A Terminal Voltage
- B EMF
- C Current
- D Resistance
- E Power

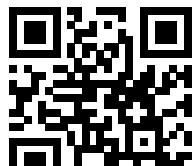
Answer



<http://njc.tl/oI>

55 A 6V battery, whose internal resistance 1.5Ω is connected in series to a light bulb with a resistance of 6.8Ω . What is the current in the circuit?

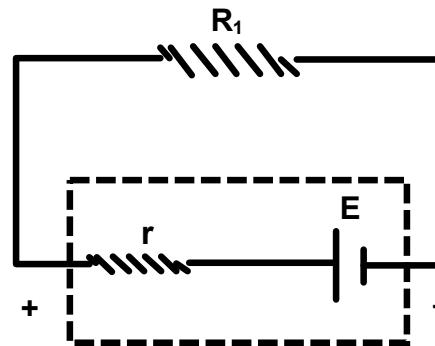
Answer



<http://njc.tl/om>

- 55 A 6V battery, whose internal resistance 1.5Ω is connected in series to a light bulb with a resistance of 6.8Ω . What is the current in the circuit?

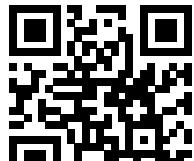
Answer



$$R_{net} = R_1 + R_2 = 1.5\Omega + 6.8\Omega$$

$$R_{net} = 8.3\Omega$$

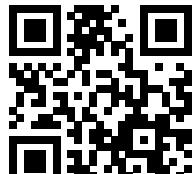
$$I = \frac{V}{R_{net}} = \frac{6V}{8.3\Omega} = .72A$$



<http://njc.tl/om>

- 56 A 6V battery, whose internal resistance 1.5Ω is connected in series to a light bulb with a resistance of 6.8Ω . What is the terminal voltage of the battery?

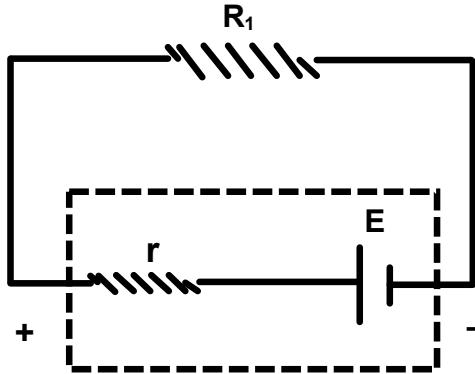
Answer



<http://njc.tl/on>

- 56 A 6V battery, whose internal resistance 1.5Ω is connected in series with a resistor R_1 of 6.8Ω

Answer



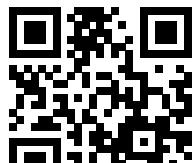
$$R_{net} = R_1 + R_2 = 1.5\Omega + 6.8\Omega$$

$$R_{net} = 8.3\Omega$$

$$I = \frac{V}{R_{net}} = \frac{6V}{8.3\Omega} = .72A$$

$$V_{ter\ min\ al} = IR_1 = (.72A)(6.8\Omega)$$

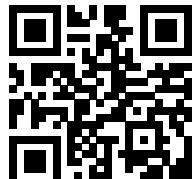
$$V_{ter\ min\ al} = 4.9V$$



<http://njc.tl/on>

57 A $25\ \Omega$ resistor is connected across the terminals of a battery whose internal resistance is $0.6\ \Omega$. What is the EMF of the battery if the current in the circuit is 0.75 A ?

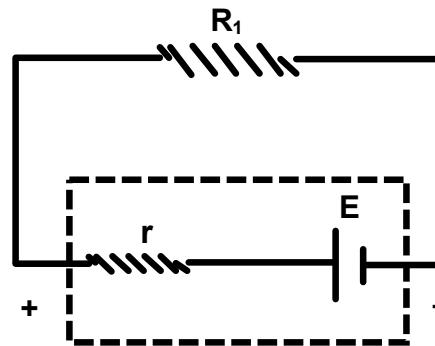
Answer



<http://njc.tl/oo>

57 A $25\ \Omega$ resistor is connected across the terminals of a battery whose internal resistance is $0.6\ \Omega$. What is the EMF of the battery if the current in the circuit is 0.75 A ?

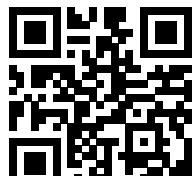
Answer



$$\varepsilon = V + Ir$$

$$\varepsilon = IR_l + Ir = I(R_l + r)$$

$$\varepsilon = (.75\text{ A})(25\Omega + .6\Omega) = 19.2V$$



<http://njc.tl/oo>