

$$\cos(\phi) = x_p \text{ , } \sin(\phi) = y_p \text{ , } \tan(\phi) = \frac{y_p}{x_p}$$

$$\sin^2(x) + \cos^2(x) = 1 \text{ and } \cos^{-2}(x) = 1 + \tan^2(x).$$

$$\cos(a \pm b) = \cos(a) \cos(b) \mp \sin(a) \sin(b) \text{ , } \sin(a \pm b) = \sin(a) \cos(b) \pm \cos(a) \sin(b)$$

$$\tan(a \pm b) = \frac{\tan(a) \pm \tan(b)}{1 \mp \tan(a) \tan(b)}$$

$$\begin{aligned} \sin(p) + \sin(q) &= 2 \sin\left(\frac{1}{2}(p+q)\right) \cos\left(\frac{1}{2}(p-q)\right) \\ \sin(p) - \sin(q) &= 2 \cos\left(\frac{1}{2}(p+q)\right) \sin\left(\frac{1}{2}(p-q)\right) \\ \cos(p) + \cos(q) &= 2 \cos\left(\frac{1}{2}(p+q)\right) \cos\left(\frac{1}{2}(p-q)\right) \\ \cos(p) - \cos(q) &= -2 \sin\left(\frac{1}{2}(p+q)\right) \sin\left(\frac{1}{2}(p-q)\right) \end{aligned}$$

$$\begin{aligned} 2 \cos^2(x) &= 1 + \cos(2x) \text{ , } & 2 \sin^2(x) &= 1 - \cos(2x) \\ \sin(\pi - x) &= \sin(x) \text{ , } & \cos(\pi - x) &= -\cos(x) \\ \sin\left(\frac{1}{2}\pi - x\right) &= \cos(x) \text{ , } & \cos\left(\frac{1}{2}\pi - x\right) &= \sin(x) \end{aligned}$$

$$\begin{aligned} \underline{\sin(x) = \sin(a)} &\Rightarrow x = a \pm 2k\pi \text{ or } x = (\pi - a) \pm 2k\pi, \text{ } k \in \mathbb{Z} \\ \underline{\cos(x) = \cos(a)} &\Rightarrow x = a \pm 2k\pi \text{ or } x = -a \pm 2k\pi \\ \underline{\tan(x) = \tan(a)} &\Rightarrow x = a \pm k\pi \text{ and } x \neq \frac{\pi}{2} \pm k\pi \end{aligned}$$

$$\arctan(x) = \arcsin\left(\frac{x}{\sqrt{x^2+1}}\right) = \arccos\left(\frac{1}{\sqrt{x^2+1}}\right) \text{ , } \sin(\arccos(x)) = \sqrt{1-x^2}$$