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*DECK DLSODE
  SUBROUTINE DLSODE (F, NEQ, Y, T, TOUT, ITOL, RTOL, ATOL, ITASK,
1      ISTATE, IOPT, RWORK, LRW, IWORK, LIW, JAC, MF)
  EXTERNAL F, JAC
  INTEGER NEQ, ITOL, ITASK, ISTATE, IOPT, LRW, IWORK, LIW, MF
  DOUBLE PRECISION Y, T, TOUT, RTOL, ATOL, RWORK
  DIMENSION NEQ(*), Y(*), RTOL(*), ATOL(*), RWORK(LRW), IWORK(LIW)
C***BEGIN PROLOGUE  DLSODE
C***PURPOSE  Livermore Solver for Ordinary Differential Equations.
C      DLSODE solves the initial-value problem for stiff or
C      nonstiff systems of first-order ODE's,
C       $dy/dt = f(t,y)$ , or, in component form,
C       $dy(i)/dt = f(i) = f(i,t,y(1),y(2),...,y(N))$ ,  $i=1,...,N$ .
C***CATEGORY  I1a
C***TYPE      DOUBLE PRECISION (SLSODE-S, DLSODE-D)
C***KEYWORDS  ORDINARY DIFFERENTIAL EQUATIONS, INITIAL VALUE PROBLEM,
C      STIFF, NONSTIFF
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C***DESCRIPTION
C
C      NOTE: The "Usage" and "Arguments" sections treat only a subset of
C      available options, in condensed fashion. The options
C      covered and the information supplied will support most
C      standard uses of DLSODE.
C
C      For more sophisticated uses, full details on all options are
C      given in the concluding section, headed "Long Description."
C      A synopsis of the DLSODE Long Description is provided at the
C      beginning of that section; general topics covered are:
C      - Elements of the call sequence; optional input and output
C      - Optional supplemental routines in the DLSODE package
C      - internal COMMON block
C
C *Usage:
C      Communication between the user and the DLSODE package, for normal
C      situations, is summarized here. This summary describes a subset
C      of the available options. See "Long Description" for complete
C      details, including optional communication, nonstandard options,
C      and instructions for special situations.
C
C      A sample program is given in the "Examples" section.
C
C      Refer to the argument descriptions for the definitions of the
C      quantities that appear in the following sample declarations.
C
C      For MF = 10,
C          PARAMETER (LRW = 20 + 16*NEQ,          LIW = 20)
C      For MF = 21 or 22,
C          PARAMETER (LRW = 22 + 9*NEQ + NEQ**2,  LIW = 20 + NEQ)
C      For MF = 24 or 25,
C          PARAMETER (LRW = 22 + 10*NEQ + (2*ML+MU)*NEQ,
C      *              LIW = 20 + NEQ)
C
C      EXTERNAL F, JAC
C      INTEGER NEQ, ITOL, ITASK, ISTATE, IOPT, LRW, IWORK(LIW),
C      *      LIW, MF
C      DOUBLE PRECISION Y(NEQ), T, TOUT, RTOL, ATOL(NTOL), RWORK(LRW)
C
C      CALL DLSODE (F, NEQ, Y, T, TOUT, ITOL, RTOL, ATOL, ITASK,
C      *      ISTATE, IOPT, RWORK, LRW, IWORK, LIW, JAC, MF)
C
C *Arguments:
C      F      :EXT  Name of subroutine for right-hand-side vector f.
C                  This name must be declared EXTERNAL in calling
C                  program. The form of F must be:
C
C                  SUBROUTINE F (NEQ, T, Y, YDOT)
C                  INTEGER NEQ
C                  DOUBLE PRECISION T, Y(*), YDOT(*)

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C           The inputs are NEQ, T, Y. F is to set
C
C           YDOT(i) = f(i,T,Y(1),Y(2),...,Y(NEQ)),
C                               i = 1, ..., NEQ .
C
C   NEQ   :IN      Number of first-order ODE's.
C
C   Y     :INOUT   Array of values of the y(t) vector, of length NEQ.
C                   Input: For the first call, Y should contain the
C                   values of y(t) at t = T. (Y is an input
C                   variable only if ISTATE = 1.)
C                   Output: On return, Y will contain the values at the
C                   new t-value.
C
C   T     :INOUT   Value of the independent variable. On return it
C                   will be the current value of t (normally TOUT).
C
C   TOUT  :IN      Next point where output is desired (.NE. T).
C
C   ITOL  :IN      1 or 2 according as ATOL (below) is a scalar or
C                   an array.
C
C   RTOL  :IN      Relative tolerance parameter (scalar).
C
C   ATOL  :IN      Absolute tolerance parameter (scalar or array).
C                   If ITOL = 1, ATOL need not be dimensioned.
C                   If ITOL = 2, ATOL must be dimensioned at least NEQ.
C
C           The estimated local error in Y(i) will be controlled
C           so as to be roughly less (in magnitude) than
C
C           EWT(i) = RTOL*ABS(Y(i)) + ATOL      if ITOL = 1, or
C           EWT(i) = RTOL*ABS(Y(i)) + ATOL(i)   if ITOL = 2.
C
C           Thus the local error test passes if, in each
C           component, either the absolute error is less than
C           ATOL (or ATOL(i)), or the relative error is less
C           than RTOL.
C
C           Use RTOL = 0.0 for pure absolute error control, and
C           use ATOL = 0.0 (or ATOL(i) = 0.0) for pure relative
C           error control. Caution: Actual (global) errors may
C           exceed these local tolerances, so choose them
C           conservatively.
C
C   ITASK :IN      Flag indicating the task DLSODE is to perform.
C                   Use ITASK = 1 for normal computation of output
C                   values of y at t = TOUT.
C
C   ISTATE:INOUT   Index used for input and output to specify the state
C                   of the calculation.
C                   Input:
C                   1 This is the first call for a problem.
C                   2 This is a subsequent call.
C                   Output:
C                   1 Nothing was done, because TOUT was equal to T.
C                   2 DLSODE was successful (otherwise, negative).
C                   Note that ISTATE need not be modified after a
C                   successful return.
C                   -1 Excess work done on this call (perhaps wrong
C                   MF).
C                   -2 Excess accuracy requested (tolerances too
C                   small).
C                   -3 Illegal input detected (see printed message).
C                   -4 Repeated error test failures (check all
C                   inputs).
C                   -5 Repeated convergence failures (perhaps bad
C                   Jacobian supplied or wrong choice of MF or
C                   tolerances).
C                   -6 Error weight became zero during problem
C                   (solution component i vanished, and ATOL or
C                   ATOL(i) = 0.).
C

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C      IOPT  :IN      Flag indicating whether optional inputs are used:
C                    0   No.
C                    1   Yes. (See "Optional inputs" under "Long
C                        Description," Part 1.)
C
C      RWORK :WORK    Real work array of length at least:
C                    20 + 16*NEQ          for MF = 10,
C                    22 + 9*NEQ + NEQ**2   for MF = 21 or 22,
C                    22 + 10*NEQ + (2*ML + MU)*NEQ for MF = 24 or 25.
C
C      LRW   :IN      Declared length of RWORK (in user's DIMENSION
C                    statement).
C
C      IWORK :WORK    Integer work array of length at least:
C                    20          for MF = 10,
C                    20 + NEQ    for MF = 21, 22, 24, or 25.
C
C                    If MF = 24 or 25, input in IWORK(1),IWORK(2) the
C                    lower and upper Jacobian half-bandwidths ML,MU.
C
C                    On return, IWORK contains information that may be
C                    of interest to the user:
C
C                    Name  Location  Meaning
C                    -----
C                    NST   IWORK(11) Number of steps taken for the problem so
C                               far.
C                    NFE   IWORK(12) Number of f evaluations for the problem
C                               so far.
C                    NJE   IWORK(13) Number of Jacobian evaluations (and of
C                               matrix LU decompositions) for the problem
C                               so far.
C                    NQU   IWORK(14) Method order last used (successfully).
C                    LENRW IWORK(17) Length of RWORK actually required. This
C                               is defined on normal returns and on an
C                               illegal input return for insufficient
C                               storage.
C                    LENIW IWORK(18) Length of IWORK actually required. This
C                               is defined on normal returns and on an
C                               illegal input return for insufficient
C                               storage.
C
C      LIW   :IN      Declared length of IWORK (in user's DIMENSION
C                    statement).
C
C      JAC   :EXT      Name of subroutine for Jacobian matrix (MF =
C                    21 or 24). If used, this name must be declared
C                    EXTERNAL in calling program. If not used, pass a
C                    dummy name. The form of JAC must be:
C
C                    SUBROUTINE JAC (NEQ, T, Y, ML, MU, PD, NROWPD)
C                    INTEGER NEQ, ML, MU, NROWPD
C                    DOUBLE PRECISION T, Y(*), PD(NROWPD,*)
C
C                    See item c, under "Description" below for more
C                    information about JAC.
C
C      MF    :IN      Method flag. Standard values are:
C                    10 Nonstiff (Adams) method, no Jacobian used.
C                    21 Stiff (BDF) method, user-supplied full Jacobian.
C                    22 Stiff method, internally generated full
C                        Jacobian.
C                    24 Stiff method, user-supplied banded Jacobian.
C                    25 Stiff method, internally generated banded
C                        Jacobian.
C
C *Description:
C   DLSODE solves the initial value problem for stiff or nonstiff
C   systems of first-order ODE's,
C
C       dy/dt = f(t,y) ,
C
C   or, in component form,

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C
C      dy(i)/dt = f(i) = f(i,t,y(1),y(2),...,y(NEQ))
C                                     (i = 1, ..., NEQ) .
C
C DLSODE is a package based on the GEAR and GEARB packages, and on
C the October 23, 1978, version of the tentative ODEPACK user
C interface standard, with minor modifications.
C
C The steps in solving such a problem are as follows.
C
C a. First write a subroutine of the form
C
C      SUBROUTINE F (NEQ, T, Y, YDOT)
C      INTEGER NEQ
C      DOUBLE PRECISION T, Y(*), YDOT(*)
C
C      which supplies the vector function f by loading YDOT(i) with
C      f(i).
C
C b. Next determine (or guess) whether or not the problem is stiff.
C      Stiffness occurs when the Jacobian matrix df/dy has an
C      eigenvalue whose real part is negative and large in magnitude
C      compared to the reciprocal of the t span of interest. If the
C      problem is nonstiff, use method flag MF = 10. If it is stiff,
C      there are four standard choices for MF, and DLSODE requires the
C      Jacobian matrix in some form. This matrix is regarded either
C      as full (MF = 21 or 22), or banded (MF = 24 or 25). In the
C      banded case, DLSODE requires two half-bandwidth parameters ML
C      and MU. These are, respectively, the widths of the lower and
C      upper parts of the band, excluding the main diagonal. Thus the
C      band consists of the locations (i,j) with
C
C      i - ML <= j <= i + MU ,
C
C      and the full bandwidth is ML + MU + 1 .
C
C c. If the problem is stiff, you are encouraged to supply the
C      Jacobian directly (MF = 21 or 24), but if this is not feasible,
C      DLSODE will compute it internally by difference quotients (MF =
C      22 or 25). If you are supplying the Jacobian, write a
C      subroutine of the form
C
C      SUBROUTINE JAC (NEQ, T, Y, ML, MU, PD, NROWPD)
C      INTEGER NEQ, ML, MU, NROWPD
C      DOUBLE PRECISION T, Y(*), PD(NROWPD,*)
C
C      which provides df/dy by loading PD as follows:
C      - For a full Jacobian (MF = 21), load PD(i,j) with df(i)/dy(j),
C        the partial derivative of f(i) with respect to y(j). (Ignore
C        the ML and MU arguments in this case.)
C      - For a banded Jacobian (MF = 24), load PD(i-j+MU+1,j) with
C        df(i)/dy(j); i.e., load the diagonal lines of df/dy into the
C        rows of PD from the top down.
C      - In either case, only nonzero elements need be loaded.
C
C d. Write a main program that calls subroutine DLSODE once for each
C      point at which answers are desired. This should also provide
C      for possible use of logical unit 6 for output of error messages
C      by DLSODE.
C
C      Before the first call to DLSODE, set ISTATE = 1, set Y and T to
C      the initial values, and set TOUT to the first output point. To
C      continue the integration after a successful return, simply
C      reset TOUT and call DLSODE again. No other parameters need be
C      reset.
C
C *Examples:
C
C      The following is a simple example problem, with the coding needed
C      for its solution by DLSODE. The problem is from chemical kinetics,
C      and consists of the following three rate equations:
C
C      dy1/dt = -.04*y1 + 1.E4*y2*y3
C      dy2/dt = .04*y1 - 1.E4*y2*y3 - 3.E7*y2**2

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C      dy3/dt = 3.E7*y2**2
C
C      on the interval from t = 0.0 to t = 4.E10, with initial conditions
C      y1 = 1.0, y2 = y3 = 0. The problem is stiff.
C
C      The following coding solves this problem with DLSODE, using
C      MF = 21 and printing results at t = .4, 4., ..., 4.E10. It uses
C      ITOL = 2 and ATOL much smaller for y2 than for y1 or y3 because y2
C      has much smaller values. At the end of the run, statistical
C      quantities of interest are printed.
C
C      EXTERNAL FEX, JEX
C      INTEGER IOPT, IOUT, ISTATE, ITASK, ITOL, IWORK(23), LIW, LRW,
C      *      MF, NEQ
C      DOUBLE PRECISION ATOL(3), RTOL, RWORK(58), T, TOUT, Y(3)
C      NEQ = 3
C      Y(1) = 1.D0
C      Y(2) = 0.D0
C      Y(3) = 0.D0
C      T = 0.D0
C      TOUT = .4D0
C      ITOL = 2
C      RTOL = 1.D-4
C      ATOL(1) = 1.D-6
C      ATOL(2) = 1.D-10
C      ATOL(3) = 1.D-6
C      ITASK = 1
C      ISTATE = 1
C      IOPT = 0
C      LRW = 58
C      LIW = 23
C      MF = 21
C      DO 40 IOUT = 1,12
C      CALL DLSODE (FEX, NEQ, Y, T, TOUT, ITOL, RTOL, ATOL, ITASK,
C      *      ISTATE, IOPT, RWORK, LRW, IWORK, LIW, JEX, MF)
C      WRITE(6,20) T, Y(1), Y(2), Y(3)
C      20  FORMAT(' At t =',D12.4,' y =',3D14.6)
C      IF (ISTATE .LT. 0) GO TO 80
C      40  TOUT = TOUT*10.D0
C      WRITE(6,60) IWORK(11), IWORK(12), IWORK(13)
C      60  FORMAT('/' No. steps =',i4,', No. f-s =',i4,', No. J-s =',i4)
C      STOP
C      80  WRITE(6,90) ISTATE
C      90  FORMAT('Error halt.. ISTATE =',i3)
C      STOP
C      END
C
C      SUBROUTINE FEX (NEQ, T, Y, YDOT)
C      INTEGER NEQ
C      DOUBLE PRECISION T, Y(3), YDOT(3)
C      YDOT(1) = -.04D0*Y(1) + 1.D4*Y(2)*Y(3)
C      YDOT(3) = 3.D7*Y(2)*Y(2)
C      YDOT(2) = -YDOT(1) - YDOT(3)
C      RETURN
C      END
C
C      SUBROUTINE JEX (NEQ, T, Y, ML, MU, PD, NRPD)
C      INTEGER NEQ, ML, MU, NRPD
C      DOUBLE PRECISION T, Y(3), PD(NRPD,3)
C      PD(1,1) = -.04D0
C      PD(1,2) = 1.D4*Y(3)
C      PD(1,3) = 1.D4*Y(2)
C      PD(2,1) = .04D0
C      PD(2,3) = -PD(1,3)
C      PD(3,2) = 6.D7*Y(2)
C      PD(2,2) = -PD(1,2) - PD(3,2)
C      RETURN
C      END
C
C      The output from this program (on a Cray-1 in single precision)
C      is as follows.
C
C      At t = 4.0000e-01 y = 9.851726e-01 3.386406e-05 1.479357e-02

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Y, T, ISTATE.

The work arrays RWORK and IWORK are also used for conditional and optional inputs and optional outputs. (The term output here refers to the return from subroutine DLSODE to the user's calling program.)

The legality of input parameters will be thoroughly checked on the initial call for the problem, but not checked thereafter unless a change in input parameters is flagged by ISTATE = 3 on input.

The descriptions of the call arguments are as follows.

F The name of the user-supplied subroutine defining the ODE system. The system must be put in the first-order form $dy/dt = f(t,y)$, where f is a vector-valued function of the scalar t and the vector y . Subroutine F is to compute the function f . It is to have the form

```
SUBROUTINE F (NEQ, T, Y, YDOT)
  DOUBLE PRECISION T, Y(*), YDOT(*)
```

where NEQ, T, and Y are input, and the array YDOT = $f(T,Y)$ is output. Y and YDOT are arrays of length NEQ. Subroutine F should not alter $Y(1), \dots, Y(NEQ)$. F must be declared EXTERNAL in the calling program.

Subroutine F may access user-defined quantities in $NEQ(2), \dots$ and/or in $Y(NEQ(1)+1), \dots$, if NEQ is an array (dimensioned in F) and/or Y has length exceeding $NEQ(1)$. See the descriptions of NEQ and Y below.

If quantities computed in the F routine are needed externally to DLSODE, an extra call to F should be made for this purpose, for consistent and accurate results. If only the derivative dy/dt is needed, use DINTDY instead.

NEQ The size of the ODE system (number of first-order ordinary differential equations). Used only for input. NEQ may be decreased, but not increased, during the problem. If NEQ is decreased (with ISTATE = 3 on input), the remaining components of Y should be left undisturbed, if these are to be accessed in F and/or JAC.

Normally, NEQ is a scalar, and it is generally referred to as a scalar in this user interface description. However, NEQ may be an array, with $NEQ(1)$ set to the system size. (The DLSODE package accesses only $NEQ(1)$.) In either case, this parameter is passed as the NEQ argument in all calls to F and JAC. Hence, if it is an array, locations $NEQ(2), \dots$ may be used to store other integer data and pass it to F and/or JAC. Subroutines F and/or JAC must include NEQ in a DIMENSION statement in that case.

Y A real array for the vector of dependent variables, of length NEQ or more. Used for both input and output on the first call (ISTATE = 1), and only for output on other calls. On the first call, Y must contain the vector of initial values. On output, Y contains the computed solution vector, evaluated at T. If desired, the Y array may be used for other purposes between calls to the solver.

This array is passed as the Y argument in all calls to F and JAC. Hence its length may exceed NEQ, and locations $Y(NEQ+1), \dots$ may be used to store other real data and pass it to F and/or JAC. (The DLSODE package accesses only $Y(1), \dots, Y(NEQ)$.)

T The independent variable. On input, T is used only on

the first call, as the initial point of the integration. On output, after each call, T is the value at which a computed solution Y is evaluated (usually the same as TOUT). On an error return, T is the farthest point reached.

TOUT The next value of T at which a computed solution is desired. Used only for input.

When starting the problem (ISTATE = 1), TOUT may be equal to T for one call, then should not equal T for the next call. For the initial T, an input value of TOUT .NE. T is used in order to determine the direction of the integration (i.e., the algebraic sign of the step sizes) and the rough scale of the problem. Integration in either direction (forward or backward in T) is permitted.

If ITASK = 2 or 5 (one-step modes), TOUT is ignored after the first call (i.e., the first call with TOUT .NE. T). Otherwise, TOUT is required on every call.

If ITASK = 1, 3, or 4, the values of TOUT need not be monotone, but a value of TOUT which backs up is limited to the current internal T interval, whose endpoints are TCUR - HU and TCUR. (See "Optional Outputs" below for TCUR and HU.)

ITOL An indicator for the type of error control. See description below under ATOL. Used only for input.

RTOL A relative error tolerance parameter, either a scalar or an array of length NEQ. See description below under ATOL. Input only.

ATOL An absolute error tolerance parameter, either a scalar or an array of length NEQ. Input only.

The input parameters ITOL, RTOL, and ATOL determine the error control performed by the solver. The solver will control the vector $e = (e(i))$ of estimated local errors in Y, according to an inequality of the form

$$\text{rms-norm of } (e(i)/\text{EWT}(i)) \leq 1,$$

where

$$\text{EWT}(i) = \text{RTOL}(i) * \text{ABS}(Y(i)) + \text{ATOL}(i),$$

and the rms-norm (root-mean-square norm) here is

$$\text{rms-norm}(v) = \sqrt{\text{sum } v(i)^2 / \text{NEQ}}.$$

Here EWT = (EWT(i)) is a vector of weights which must always be positive, and the values of RTOL and ATOL should all be nonnegative. The following table gives the types (scalar/array) of RTOL and ATOL, and the corresponding form of EWT(i).

ITOL	RTOL	ATOL	EWT(i)
1	scalar	scalar	$\text{RTOL} * \text{ABS}(Y(i)) + \text{ATOL}$
2	scalar	array	$\text{RTOL} * \text{ABS}(Y(i)) + \text{ATOL}(i)$
3	array	scalar	$\text{RTOL}(i) * \text{ABS}(Y(i)) + \text{ATOL}$
4	array	array	$\text{RTOL}(i) * \text{ABS}(Y(i)) + \text{ATOL}(i)$

When either of these parameters is a scalar, it need not be dimensioned in the user's calling program.

If none of the above choices (with ITOL, RTOL, and ATOL fixed throughout the problem) is suitable, more general error controls can be obtained by substituting user-supplied routines for the setting of EWT and/or for

the norm calculation. See Part 4 below.

If global errors are to be estimated by making a repeated run on the same problem with smaller tolerances, then all components of RTOL and ATOL (i.e., of EWT) should be scaled down uniformly.

ITASK An index specifying the task to be performed. Input only. ITASK has the following values and meanings:

- 1 Normal computation of output values of $y(t)$ at $t = TOUT$ (by overshooting and interpolating).
- 2 Take one step only and return.
- 3 Stop at the first internal mesh point at or beyond $t = TOUT$ and return.
- 4 Normal computation of output values of $y(t)$ at $t = TOUT$ but without overshooting $t = TCRIT$. $TCRIT$ must be input as $RWORK(1)$. $TCRIT$ may be equal to or beyond $TOUT$, but not behind it in the direction of integration. This option is useful if the problem has a singularity at or beyond $t = TCRIT$.
- 5 Take one step, without passing $TCRIT$, and return. $TCRIT$ must be input as $RWORK(1)$.

Note: If $ITASK = 4$ or 5 and the solver reaches $TCRIT$ (within roundoff), it will return $T = TCRIT$ (exactly) to indicate this (unless $ITASK = 4$ and $TOUT$ comes before $TCRIT$, in which case answers at $T = TOUT$ are returned first).

ISTATE An index used for input and output to specify the state of the calculation.

On input, the values of ISTATE are as follows:

- 1 This is the first call for the problem (initializations will be done). See "Note" below.
- 2 This is not the first call, and the calculation is to continue normally, with no change in any input parameters except possibly $TOUT$ and $ITASK$. (If $ITOL$, $RTOL$, and/or $ATOL$ are changed between calls with $ISTATE = 2$, the new values will be used but not tested for legality.)
- 3 This is not the first call, and the calculation is to continue normally, but with a change in input parameters other than $TOUT$ and $ITASK$. Changes are allowed in NEQ , $ITOL$, $RTOL$, $ATOL$, $IOPT$, LRW , LIW , MF , ML , MU , and any of the optional inputs except $H0$. (See $IWORK$ description for ML and MU .)

Note: A preliminary call with $TOUT = T$ is not counted as a first call here, as no initialization or checking of input is done. (Such a call is sometimes useful for the purpose of outputting the initial conditions.) Thus the first call for which $TOUT \neq T$ requires $ISTATE = 1$ on input.

On output, ISTATE has the following values and meanings:

- 1 Nothing was done, as $TOUT$ was equal to T with $ISTATE = 1$ on input.
- 2 The integration was performed successfully.
- 1 An excessive amount of work (more than $MXSTEP$ steps) was done on this call, before completing the requested task, but the integration was otherwise successful as far as T . ($MXSTEP$ is an optional input and is normally 500.) To continue, the user may simply reset $ISTATE$ to a value >1 and call again (the excess work step counter will be reset to 0). In addition, the user may increase $MXSTEP$ to avoid this error return; see "Optional Inputs" below.
- 2 Too much accuracy was requested for the precision of the machine being used. This was detected before completing the requested task, but the integration was successful as far as T . To continue, the tolerance parameters must be reset, and $ISTATE$ must

be set to 3. The optional output TOLSF may be used for this purpose. (Note: If this condition is detected before taking any steps, then an illegal input return (ISTATE = -3) occurs instead.)

- 3 Illegal input was detected, before taking any integration steps. See written message for details. (Note: If the solver detects an infinite loop of calls to the solver with illegal input, it will cause the run to stop.)
- 4 There were repeated error-test failures on one attempted step, before completing the requested task, but the integration was successful as far as T. The problem may have a singularity, or the input may be inappropriate.
- 5 There were repeated convergence-test failures on one attempted step, before completing the requested task, but the integration was successful as far as T. This may be caused by an inaccurate Jacobian matrix, if one is being used.
- 6 EWT(i) became zero for some i during the integration. Pure relative error control (ATOL(i)=0.0) was requested on a variable which has now vanished. The integration was successful as far as T.

Note: Since the normal output value of ISTATE is 2, it does not need to be reset for normal continuation. Also, since a negative input value of ISTATE will be regarded as illegal, a negative output value requires the user to change it, and possibly other inputs, before calling the solver again.

IOPT An integer flag to specify whether any optional inputs are being used on this call. Input only. The optional inputs are listed under a separate heading below.

- 0 No optional inputs are being used. Default values will be used in all cases.
- 1 One or more optional inputs are being used.

RWORK A real working array (double precision). The length of RWORK must be at least

$$20 + NYH*(MAXORD + 1) + 3*NEQ + LWM$$

where

NYH = the initial value of NEQ,
 MAXORD = 12 (if METH = 1) or 5 (if METH = 2) (unless a smaller value is given as an optional input),
 LWM = 0 if MITER = 0,
 LWM = NEQ**2 + 2 if MITER = 1 or 2,
 LWM = NEQ + 2 if MITER = 3, and
 LWM = (2*ML + MU + 1)*NEQ + 2
 if MITER = 4 or 5.

(See the MF description below for METH and MITER.)

Thus if MAXORD has its default value and NEQ is constant, this length is:

20 + 16*NEQ	for MF = 10,
22 + 16*NEQ + NEQ**2	for MF = 11 or 12,
22 + 17*NEQ	for MF = 13,
22 + 17*NEQ + (2*ML + MU)*NEQ	for MF = 14 or 15,
20 + 9*NEQ	for MF = 20,
22 + 9*NEQ + NEQ**2	for MF = 21 or 22,
22 + 10*NEQ	for MF = 23,
22 + 10*NEQ + (2*ML + MU)*NEQ	for MF = 24 or 25.

The first 20 words of RWORK are reserved for conditional and optional inputs and optional outputs.

The following word in RWORK is a conditional input:

RWORK(1) = TCRIT, the critical value of t which the solver is not to overshoot. Required if ITASK is 4 or 5, and ignored otherwise. See ITASK.

```

C      LRW      The length of the array RWORK, as declared by the user.
C                (This will be checked by the solver.)
C
C      IWORK    An integer work array.  Its length must be at least
C                20      if MITER = 0 or 3 (MF = 10, 13, 20, 23), or
C                20 + NEQ otherwise (MF = 11, 12, 14, 15, 21, 22, 24, 25).
C                (See the MF description below for MITER.)  The first few
C                words of IWORK are used for conditional and optional
C                inputs and optional outputs.
C
C                The following two words in IWORK are conditional inputs:
C                IWORK(1) = ML   These are the lower and upper half-
C                IWORK(2) = MU   bandwidths, respectively, of the banded
C                                Jacobian, excluding the main diagonal.
C                                The band is defined by the matrix locations
C                                (i,j) with i - ML <= j <= i + MU. ML and MU
C                                must satisfy 0 <= ML,MU <= NEQ - 1. These are
C                                required if MITER is 4 or 5, and ignored
C                                otherwise. ML and MU may in fact be the band
C                                parameters for a matrix to which df/dy is only
C                                approximately equal.
C
C      LIW      The length of the array IWORK, as declared by the user.
C                (This will be checked by the solver.)
C
C      Note: The work arrays must not be altered between calls to DLSODE
C      for the same problem, except possibly for the conditional and
C      optional inputs, and except for the last 3*NEQ words of RWORK.
C      The latter space is used for internal scratch space, and so is
C      available for use by the user outside DLSODE between calls, if
C      desired (but not for use by F or JAC).
C
C      JAC      The name of the user-supplied routine (MITER = 1 or 4) to
C                compute the Jacobian matrix, df/dy, as a function of the
C                scalar t and the vector y.  (See the MF description below
C                for MITER.)  It is to have the form
C
C                SUBROUTINE JAC (NEQ, T, Y, ML, MU, PD, NROWPD)
C                DOUBLE PRECISION T, Y(*), PD(NROWPD,*)
C
C                where NEQ, T, Y, ML, MU, and NROWPD are input and the
C                array PD is to be loaded with partial derivatives
C                (elements of the Jacobian matrix) on output.  PD must be
C                given a first dimension of NROWPD.  T and Y have the same
C                meaning as in subroutine F.
C
C                In the full matrix case (MITER = 1), ML and MU are
C                ignored, and the Jacobian is to be loaded into PD in
C                columnwise manner, with df(i)/dy(j) loaded into PD(i,j).
C
C                In the band matrix case (MITER = 4), the elements within
C                the band are to be loaded into PD in columnwise manner,
C                with diagonal lines of df/dy loaded into the rows of PD.
C                Thus df(i)/dy(j) is to be loaded into PD(i-j+MU+1,j). ML
C                and MU are the half-bandwidth parameters (see IWORK).
C                The locations in PD in the two triangular areas which
C                correspond to nonexistent matrix elements can be ignored
C                or loaded arbitrarily, as they are overwritten by DLSODE.
C
C                JAC need not provide df/dy exactly. A crude approximation
C                (possibly with a smaller bandwidth) will do.
C
C                In either case, PD is preset to zero by the solver, so
C                that only the nonzero elements need be loaded by JAC.
C                Each call to JAC is preceded by a call to F with the same
C                arguments NEQ, T, and Y. Thus to gain some efficiency,
C                intermediate quantities shared by both calculations may
C                be saved in a user COMMON block by F and not recomputed
C                by JAC, if desired. Also, JAC may alter the Y array, if
C                desired. JAC must be declared EXTERNAL in the calling
C                program.
C
C      Subroutine JAC may access user-defined quantities in

```

NEQ(2),... and/or in Y(NEQ(1)+1),... if NEQ is an array (dimensioned in JAC) and/or Y has length exceeding NEQ(1). See the descriptions of NEQ and Y above.

MF The method flag. Used only for input. The legal values of MF are 10, 11, 12, 13, 14, 15, 20, 21, 22, 23, 24, and 25. MF has decimal digits METH and MITER:

$$MF = 10 \cdot METH + MITER$$

METH indicates the basic linear multistep method:

- 1 Implicit Adams method.
- 2 Method based on backward differentiation formulas (BDF's).

MITER indicates the corrector iteration method:

- 0 Functional iteration (no Jacobian matrix is involved).
- 1 Chord iteration with a user-supplied full (NEQ by NEQ) Jacobian.
- 2 Chord iteration with an internally generated (difference quotient) full Jacobian (using NEQ extra calls to F per df/dy value).
- 3 Chord iteration with an internally generated diagonal Jacobian approximation (using one extra call to F per df/dy evaluation).
- 4 Chord iteration with a user-supplied banded Jacobian.
- 5 Chord iteration with an internally generated banded Jacobian (using ML + MU + 1 extra calls to F per df/dy evaluation).

If MITER = 1 or 4, the user must supply a subroutine JAC (the name is arbitrary) as described above under JAC. For other values of MITER, a dummy argument can be used.

Optional Inputs

The following is a list of the optional inputs provided for in the call sequence. (See also Part 2.) For each such input variable, this table lists its name as used in this documentation, its location in the call sequence, its meaning, and the default value. The use of any of these inputs requires IOPT = 1, and in that case all of these inputs are examined. A value of zero for any of these optional inputs will cause the default value to be used. Thus to use a subset of the optional inputs, simply preload locations 5 to 10 in RWORK and IWORK to 0.0 and 0 respectively, and then set those of interest to nonzero values.

Name	Location	Meaning and default value
H0	RWORK(5)	Step size to be attempted on the first step. The default value is determined by the solver.
HMAX	RWORK(6)	Maximum absolute step size allowed. The default value is infinite.
HMIN	RWORK(7)	Minimum absolute step size allowed. The default value is 0. (This lower bound is not enforced on the final step before reaching TCRIT when ITASK = 4 or 5.)
MAXORD	IWORK(5)	Maximum order to be allowed. The default value is 12 if METH = 1, and 5 if METH = 2. (See the MF description above for METH.) If MAXORD exceeds the default value, it will be reduced to the default value. If MAXORD is changed during the problem, it may cause the current order to be reduced.
MXSTEP	IWORK(6)	Maximum number of (internally defined) steps allowed during one call to the solver. The default value is 500.
MXHNIL	IWORK(7)	Maximum number of messages printed (per problem) warning that $T + H = T$ on a step (H = step size). This must be positive to result in a nondefault value. The default value is 10.

Optional Outputs

As optional additional output from DLSODE, the variables listed below are quantities related to the performance of DLSODE which are available to the user. These are communicated by way of the work arrays, but also have internal mnemonic names as shown. Except where stated otherwise, all of these outputs are defined on any successful return from DLSODE, and on any return with ISTATE = -1, -2, -4, -5, or -6. On an illegal input return (ISTATE = -3), they will be unchanged from their existing values (if any), except possibly for TOLSF, LENRW, and LENIW. On any error return, outputs relevant to the error will be defined, as noted below.

Name	Location	Meaning
-----	-----	-----
HU	RWORK(11)	Step size in t last used (successfully).
HCUR	RWORK(12)	Step size to be attempted on the next step.
TCUR	RWORK(13)	Current value of the independent variable which the solver has actually reached, i.e., the current internal mesh point in t. On output, TCUR will always be at least as far as the argument T, but may be farther (if interpolation was done).
TOLSF	RWORK(14)	Tolerance scale factor, greater than 1.0, computed when a request for too much accuracy was detected (ISTATE = -3 if detected at the start of the problem, ISTATE = -2 otherwise). If ITOL is left unaltered but RTOL and ATOL are uniformly scaled up by a factor of TOLSF for the next call, then the solver is deemed likely to succeed. (The user may also ignore TOLSF and alter the tolerance parameters in any other way appropriate.)
NST	IWORK(11)	Number of steps taken for the problem so far.
NFE	IWORK(12)	Number of F evaluations for the problem so far.
NJE	IWORK(13)	Number of Jacobian evaluations (and of matrix LU decompositions) for the problem so far.
NQU	IWORK(14)	Method order last used (successfully).
NQCUR	IWORK(15)	Order to be attempted on the next step.
IMXER	IWORK(16)	Index of the component of largest magnitude in the weighted local error vector ($e(i)/EWT(i)$), on an error return with ISTATE = -4 or -5.
LENRW	IWORK(17)	Length of RWORK actually required. This is defined on normal returns and on an illegal input return for insufficient storage.
LENIW	IWORK(18)	Length of IWORK actually required. This is defined on normal returns and on an illegal input return for insufficient storage.

The following two arrays are segments of the RWORK array which may also be of interest to the user as optional outputs. For each array, the table below gives its internal name, its base address in RWORK, and its description.

Name	Base address	Description
----	-----	-----
YH	21	The Nordsieck history array, of size NYH by (NQCUR + 1), where NYH is the initial value of NEQ. For $j = 0, 1, \dots, NQCUR$, column $j + 1$ of YH contains $HCUR**j/factorial(j)$ times the j th derivative of the interpolating polynomial currently representing the solution, evaluated at $t = TCUR$.
ACOR	LENRW-NEQ+1	Array of size NEQ used for the accumulated corrections on each step, scaled on output to represent the estimated local error in Y on the last step. This is the vector e in the description of the error control. It is defined only on successful return from DLSODE.

The following are optional calls which the user may make to gain additional capabilities in conjunction with DLSODE.

Form of call	Function
CALL XSETUN(LUN)	Set the logical unit number, LUN, for output of messages from DLSODE, if the default is not desired. The default value of LUN is 6. This call may be made at any time and will take effect immediately.
CALL XSETF(MFLAG)	Set a flag to control the printing of messages by DLSODE. MFLAG = 0 means do not print. (Danger: this risks losing valuable information.) MFLAG = 1 means print (the default). This call may be made at any time and will take effect immediately.
CALL DSRCOM(RSAV,ISAV,JOB)	Saves and restores the contents of the internal COMMON blocks used by DLSODE (see Part 3 below). RSAV must be a real array of length 218 or more, and ISAV must be an integer array of length 37 or more. JOB = 1 means save COMMON into RSAV/ISAV. JOB = 2 means restore COMMON from same. DSRCOM is useful if one is interrupting a run and restarting later, or alternating between two or more problems solved with DLSODE.
CALL DINTDY(,,,,,) (see below)	Provide derivatives of y, of various orders, at a specified point t, if desired. It may be called only after a successful return from DLSODE. Detailed instructions follow.

Detailed instructions for using DINTDY

The form of the CALL is:

```
CALL DINTDY (T, K, RWORK(21), NYH, DKY, IFLAG)
```

The input parameters are:

T Value of independent variable where answers are desired (normally the same as the T last returned by DLSODE). For valid results, T must lie between TCUR - HU and TCUR. (See "Optional Outputs" above for TCUR and HU.)

K Integer order of the derivative desired. K must satisfy $0 \leq K \leq NQCUR$, where NQCUR is the current order (see "Optional Outputs"). The capability corresponding to $K = 0$, i.e., computing $y(t)$, is already provided by DLSODE directly. Since $NQCUR \geq 1$, the first derivative dy/dt is always available with DINTDY.

RWORK(21) The base address of the history array YH.

NYH Column length of YH, equal to the initial value of NEQ.

The output parameters are:

DKY Real array of length NEQ containing the computed value of the Kth derivative of $y(t)$.

IFLAG Integer flag, returned as 0 if K and T were legal, -1 if K was illegal, and -2 if T was illegal. On an error return, a message is also written.

Part 3. Common Blocks

If DLSODE is to be used in an overlay situation, the user must declare, in the primary overlay, the variables in:

- (1) the call sequence to DLSODE,
- (2) the internal COMMON block /DLS001/, of length 255
(218 double precision words followed by 37 integer words).

If DLSODE is used on a system in which the contents of internal COMMON blocks are not preserved between calls, the user should declare the above COMMON block in his main program to insure that its contents are preserved.

If the solution of a given problem by DLSODE is to be interrupted and then later continued, as when restarting an interrupted run or alternating between two or more problems, the user should save, following the return from the last DLSODE call prior to the interruption, the contents of the call sequence variables and the internal COMMON block, and later restore these values before the next DLSODE call for that problem. In addition, if XSETUN and/or XSETF was called for non-default handling of error messages, then these calls must be repeated. To save and restore the COMMON block, use subroutine DSRCOM (see Part 2 above).

Part 4. Optionally Replaceable Solver Routines

Below are descriptions of two routines in the DLSODE package which relate to the measurement of errors. Either routine can be replaced by a user-supplied version, if desired. However, since such a replacement may have a major impact on performance, it should be done only when absolutely necessary, and only with great caution. (Note: The means by which the package version of a routine is superseded by the user's version may be system-dependent.)

DEWSET

The following subroutine is called just before each internal integration step, and sets the array of error weights, EWT, as described under ITOL/RTOL/ATOL above:

```
SUBROUTINE DEWSET (NEQ, ITOL, RTOL, ATOL, YCUR, EWT)
```

where NEQ, ITOL, RTOL, and ATOL are as in the DLSODE call sequence, YCUR contains the current dependent variable vector, and EWT is the array of weights set by DEWSET.

If the user supplies this subroutine, it must return in EWT(i) ($i = 1, \dots, \text{NEQ}$) a positive quantity suitable for comparing errors in $Y(i)$ to. The EWT array returned by DEWSET is passed to the DVNORM routine (see below), and also used by DLSODE in the computation of the optional output IMXER, the diagonal Jacobian approximation, and the increments for difference quotient Jacobians.

In the user-supplied version of DEWSET, it may be desirable to use the current values of derivatives of y . Derivatives up to order NQ are available from the history array YH, described above under optional outputs. In DEWSET, YH is identical to the YCUR array, extended to $NQ + 1$ columns with a column length of NYH and scale factors of $H^{**j}/\text{factorial}(j)$. On the first call for the problem, given by $\text{NST} = 0$, NQ is 1 and H is temporarily set to 1.0. NYH is the initial value of NEQ. The quantities NQ , H , and NST can be obtained by including in SEWSET the statements:

```
DOUBLE PRECISION RLS
COMMON /DLS001/ RLS(218), ILS(37)
NQ = ILS(33)
NST = ILS(34)
H = RLS(212)
```

Thus, for example, the current value of dy/dt can be obtained as $\text{YCUR}(\text{NYH}+i)/H$ ($i=1, \dots, \text{NEQ}$) (and the division by H is unnecessary when $\text{NST} = 0$).

DVNORM

```

C      DVNORM is a real function routine which computes the weighted
C      root-mean-square norm of a vector v:
C
C      d = DVNORM (n, v, w)
C
C      where:
C      n = the length of the vector,
C      v = real array of length n containing the vector,
C      w = real array of length n containing weights,
C      d = SQRT( (1/n) * sum(v(i)*w(i))**2 ).
C
C      DVNORM is called with n = NEQ and with w(i) = 1.0/EWT(i), where
C      EWT is as set by subroutine DEWSET.
C
C      If the user supplies this function, it should return a nonnegative
C      value of DVNORM suitable for use in the error control in DLSODE.
C      None of the arguments should be altered by DVNORM. For example, a
C      user-supplied DVNORM routine might:
C      - Substitute a max-norm of (v(i)*w(i)) for the rms-norm, or
C      - Ignore some components of v in the norm, with the effect of
C      suppressing the error control on those components of Y.
C      -----
C***ROUTINES CALLED  DEWSET, DINTDY, DUMACH, DSTODE, DVNORM, XERRWD
C***COMMON BLOCKS   DLS001
C***REVISION HISTORY (YYYYMMDD)
C 19791129  DATE WRITTEN
C 19791213  Minor changes to declarations; DELP init. in STODE.
C 19800118  Treat NEQ as array; integer declarations added throughout;
C           minor changes to prologue.
C 19800306  Corrected TESCO(1,NQP1) setting in CFODE.
C 19800519  Corrected access of YH on forced order reduction;
C           numerous corrections to prologues and other comments.
C 19800617  In main driver, added loading of SQRT(UROUND) in RWORK;
C           minor corrections to main prologue.
C 19800923  Added zero initialization of HU and NQU.
C 19801218  Revised XERRWD routine; minor corrections to main prologue.
C 19810401  Minor changes to comments and an error message.
C 19810814  Numerous revisions: replaced EWT by 1/EWT; used flags
C           JCUR, ICF, IERPJ, IERSL between STODE and subordinates;
C           added tuning parameters CCMAX, MAXCOR, MSBP, MXNCF;
C           reorganized returns from STODE; reorganized type decls.;
C           fixed message length in XERRWD; changed default LUNIT to 6;
C           changed Common lengths; changed comments throughout.
C 19870330  Major update by ACH: corrected comments throughout;
C           removed TRET from Common; rewrote EWSET with 4 loops;
C           fixed t test in INTDY; added Cray directives in STODE;
C           in STODE, fixed DELP init. and logic around PJAC call;
C           combined routines to save/restore Common;
C           passed LEVEL = 0 in error message calls (except run abort).
C 19890426  Modified prologue to SLATEC/LDOC format. (FNF)
C 19890501  Many improvements to prologue. (FNF)
C 19890503  A few final corrections to prologue. (FNF)
C 19890504  Minor cosmetic changes. (FNF)
C 19890510  Corrected description of Y in Arguments section. (FNF)
C 19890517  Minor corrections to prologue. (FNF)
C 19920514  Updated with prologue edited 891025 by G. Shaw for manual.
C 19920515  Converted source lines to upper case. (FNF)
C 19920603  Revised XERRWD calls using mixed upper-lower case. (ACH)
C 19920616  Revised prologue comment regarding CFT. (ACH)
C 19921116  Revised prologue comments regarding Common. (ACH).
C 19930326  Added comment about non-reentrancy. (FNF)
C 19930723  Changed DLMACH to DUMACH. (FNF)
C 19930801  Removed ILLIN and NTREP from Common (affects driver logic);
C           minor changes to prologue and internal comments;
C           changed Hollerith strings to quoted strings;
C           changed internal comments to mixed case;
C           replaced XERRWD with new version using character type;
C           changed dummy dimensions from 1 to *. (ACH)
C 19930809  Changed to generic intrinsic names; changed names of
C           subprograms and Common blocks to DLSODE etc. (ACH)
C 19930929  Eliminated use of REAL intrinsic; other minor changes. (ACH)
C 20010412  Removed all 'own' variables from Common block /DLS001/
C           (affects declarations in 6 routines). (ACH)

```



```

C 20010509 Minor corrections to prologue. (ACH)
C 20031105 Restored 'own' variables to Common block /DLS001/, to
C          enable interrupt/restart feature. (ACH)
C 20031112 Added SAVE statements for data-loaded constants.
C
C***END PROLOGUE  DLSODE
C
C*Internal Notes:
C
C Other Routines in the DLSODE Package.
C
C In addition to Subroutine DLSODE, the DLSODE package includes the
C following subroutines and function routines:
C DINTDY  computes an interpolated value of the y vector at t = TOUT.
C DSTODE  is the core integrator, which does one step of the
C          integration and the associated error control.
C DCFODE  sets all method coefficients and test constants.
C DPREPJ  computes and preprocesses the Jacobian matrix  $J = df/dy$ 
C          and the Newton iteration matrix  $P = I - h*10*J$ .
C DSOLSY  manages solution of linear system in chord iteration.
C DEWSET  sets the error weight vector EWT before each step.
C DVNORM  computes the weighted R.M.S. norm of a vector.
C DSRCOM  is a user-callable routine to save and restore
C          the contents of the internal Common block.
C DGEFA and DGESL are routines from LINPACK for solving full
C          systems of linear algebraic equations.
C DGBFA and DGBSL are routines from LINPACK for solving banded
C          linear systems.
C DUMACH  computes the unit roundoff in a machine-independent manner.
C XERRWD, XSETUN, XSETF, IXSAV, IUMACH handle the printing of all
C          error messages and warnings. XERRWD is machine-dependent.
C Note: DVNORM, DUMACH, IXSAV, and IUMACH are function routines.
C All the others are subroutines.
C
C**End
C
C Declare externals.
C      EXTERNAL DPREPJ, DSOLSY
C      DOUBLE PRECISION DUMACH, DVNORM
C
C Declare all other variables.
C      INTEGER INIT, MXSTEP, MXHNIL, NHNIL, NSLAST, NYH, IOWNS,
C      1 ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
C      2 LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
C      3 MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
C      INTEGER I, I1, I2, IFLAG, IMXER, KGO, LF0,
C      1 LENIW, LENRW, LENWM, ML, MORD, MU, MXHNL0, MXSTP0
C      DOUBLE PRECISION ROWNS,
C      1 CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
C      DOUBLE PRECISION ATOLI, AYI, BIG, EWTI, H0, HMAX, HMX, RH, RTOLI,
C      1 TCRIT, TDIST, TNEXT, TOL, TOLSF, TP, SIZE, SUM, W0
C      DIMENSION MORD(2)
C      LOGICAL IHIT
C      CHARACTER*80 MSG
C      SAVE MORD, MXSTP0, MXHNL0
C-----
C The following internal Common block contains
C (a) variables which are local to any subroutine but whose values must
C     be preserved between calls to the routine ("own" variables), and
C (b) variables which are communicated between subroutines.
C The block DLS001 is declared in subroutines DLSODE, DINTDY, DSTODE,
C DPREPJ, and DSOLSY.
C Groups of variables are replaced by dummy arrays in the Common
C declarations in routines where those variables are not used.
C-----
C      COMMON /DLS001/ ROWNS(209),
C      1 CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
C      2 INIT, MXSTEP, MXHNIL, NHNIL, NSLAST, NYH, IOWNS(6),
C      3 ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
C      4 LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
C      5 MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
C
C      DATA MORD(1),MORD(2)/12,5/, MXSTP0/500/, MXHNL0/10/

```

```

C-----
C Block A.
C This code block is executed on every call.
C It tests ISTATE and ITASK for legality and branches appropriately.
C If ISTATE .GT. 1 but the flag INIT shows that initialization has
C not yet been done, an error return occurs.
C If ISTATE = 1 and TOUT = T, return immediately.
C-----
C
C***FIRST EXECUTABLE STATEMENT  DLSODE
      IF (ISTATE .LT. 1 .OR. ISTATE .GT. 3) GO TO 601
      IF (ITASK .LT. 1 .OR. ITASK .GT. 5) GO TO 602
      IF (ISTATE .EQ. 1) GO TO 10
      IF (INIT .EQ. 0) GO TO 603
      IF (ISTATE .EQ. 2) GO TO 200
      GO TO 20
10    INIT = 0
      IF (TOUT .EQ. T) RETURN
C-----
C Block B.
C The next code block is executed for the initial call (ISTATE = 1),
C or for a continuation call with parameter changes (ISTATE = 3).
C It contains checking of all inputs and various initializations.
C
C First check legality of the non-optional inputs NEQ, ITOL, IOPT,
C MF, ML, and MU.
C-----
20    IF (NEQ(1) .LE. 0) GO TO 604
      IF (ISTATE .EQ. 1) GO TO 25
      IF (NEQ(1) .GT. N) GO TO 605
25    N = NEQ(1)
      IF (ITOL .LT. 1 .OR. ITOL .GT. 4) GO TO 606
      IF (IOPT .LT. 0 .OR. IOPT .GT. 1) GO TO 607
      METH = MF/10
      MITER = MF - 10*METH
      IF (METH .LT. 1 .OR. METH .GT. 2) GO TO 608
      IF (MITER .LT. 0 .OR. MITER .GT. 5) GO TO 608
      IF (MITER .LE. 3) GO TO 30
      ML = IWORK(1)
      MU = IWORK(2)
      IF (ML .LT. 0 .OR. ML .GE. N) GO TO 609
      IF (MU .LT. 0 .OR. MU .GE. N) GO TO 610
30    CONTINUE
C Next process and check the optional inputs. -----
      IF (IOPT .EQ. 1) GO TO 40
      MAXORD = MORD(METH)
      MXSTEP = MXSTP0
      MXHNIL = MXHNLO
      IF (ISTATE .EQ. 1) H0 = 0.0D0
      HMXI = 0.0D0
      HMIN = 0.0D0
      GO TO 60
40    MAXORD = IWORK(5)
      IF (MAXORD .LT. 0) GO TO 611
      IF (MAXORD .EQ. 0) MAXORD = 100
      MAXORD = MIN(MAXORD,MORD(METH))
      MXSTEP = IWORK(6)
      IF (MXSTEP .LT. 0) GO TO 612
      IF (MXSTEP .EQ. 0) MXSTEP = MXSTP0
      MXHNIL = IWORK(7)
      IF (MXHNIL .LT. 0) GO TO 613
      IF (MXHNIL .EQ. 0) MXHNIL = MXHNLO
      IF (ISTATE .NE. 1) GO TO 50
      H0 = RWORK(5)
      IF ((TOUT - T)*H0 .LT. 0.0D0) GO TO 614
50    HMAX = RWORK(6)
      IF (HMAX .LT. 0.0D0) GO TO 615
      HMXI = 0.0D0
      IF (HMAX .GT. 0.0D0) HMXI = 1.0D0/HMAX
      HMIN = RWORK(7)
      IF (HMIN .LT. 0.0D0) GO TO 616
C-----
C Set work array pointers and check lengths LRW and LIW.

```

C Pointers to segments of RWORK and IWORK are named by prefixing L to
C the name of the segment. E.g., the segment YH starts at RWORK(LYH).
C Segments of RWORK (in order) are denoted YH, WM, EWT, SAVF, ACOR.

```

C-----
60  LYH = 21
    IF (ISTATE .EQ. 1) NYH = N
    LWM = LYH + (MAXORD + 1)*NYH
    IF (MITER .EQ. 0) LENWM = 0
    IF (MITER .EQ. 1 .OR. MITER .EQ. 2) LENWM = N*N + 2
    IF (MITER .EQ. 3) LENWM = N + 2
    IF (MITER .GE. 4) LENWM = (2*ML + MU + 1)*N + 2
    LEWT = LWM + LENWM
    LSAVF = LEWT + N
    LACOR = LSAVF + N
    LENRW = LACOR + N - 1
    IWORK(17) = LENRW
    LIWM = 1
    LENIW = 20 + N
    IF (MITER .EQ. 0 .OR. MITER .EQ. 3) LENIW = 20
    IWORK(18) = LENIW
    IF (LENRW .GT. LRW) GO TO 617
    IF (LENIW .GT. LIW) GO TO 618
C Check RTOL and ATOL for legality. -----
    RTOLI = RTOL(1)
    ATOLI = ATOL(1)
    DO 70 I = 1,N
        IF (ITOL .GE. 3) RTOLI = RTOL(I)
        IF (ITOL .EQ. 2 .OR. ITOL .EQ. 4) ATOLI = ATOL(I)
        IF (RTOLI .LT. 0.0D0) GO TO 619
        IF (ATOLI .LT. 0.0D0) GO TO 620
70  CONTINUE
    IF (ISTATE .EQ. 1) GO TO 100
C If ISTATE = 3, set flag to signal parameter changes to DSTODE. -----
    JSTART = -1
    IF (NQ .LE. MAXORD) GO TO 90
C MAXORD was reduced below NQ. Copy YH(*,MAXORD+2) into SAVF. -----
    DO 80 I = 1,N
60  RWORK(I+LSAVF-1) = RWORK(I+LWM-1)
C Reload WM(1) = RWORK(LWM), since LWM may have changed. -----
90  IF (MITER .GT. 0) RWORK(LWM) = SQRT(UROUND)
    IF (N .EQ. NYH) GO TO 200
C NEQ was reduced. Zero part of YH to avoid undefined references. -----
    I1 = LYH + L*NYH
    I2 = LYH + (MAXORD + 1)*NYH - 1
    IF (I1 .GT. I2) GO TO 200
    DO 95 I = I1,I2
95  RWORK(I) = 0.0D0
    GO TO 200
C-----

```

C Block C.
C The next block is for the initial call only (ISTATE = 1).
C It contains all remaining initializations, the initial call to F,
C and the calculation of the initial step size.
C The error weights in EWT are inverted after being loaded.

```

C-----
100 UROUND = DUMACH()
    TN = T
    IF (ITASK .NE. 4 .AND. ITASK .NE. 5) GO TO 110
    TCRIT = RWORK(1)
    IF ((TCRIT - TOUT)*(TOUT - T) .LT. 0.0D0) GO TO 625
    IF (H0 .NE. 0.0D0 .AND. (T + H0 - TCRIT)*H0 .GT. 0.0D0)
1  H0 = TCRIT - T
110 JSTART = 0
    IF (MITER .GT. 0) RWORK(LWM) = SQRT(UROUND)
    NHNIL = 0
    NST = 0
    NJE = 0
    NSLAST = 0
    HU = 0.0D0
    NQU = 0
    CCMAX = 0.3D0
    MAXCOR = 3
    MSBP = 20

```

```

      MXNCF = 10
C Initial call to F. (LF0 points to YH(*,2).) -----
      LF0 = LYH + NYH
      CALL F (NEQ, T, Y, RWORK(LF0))
      NFE = 1
C Load the initial value vector in YH. -----
      DO 115 I = 1,N
115      RWORK(I+LYH-1) = Y(I)
C Load and invert the EWT array. (H is temporarily set to 1.0.) -----
      NQ = 1
      H = 1.0D0
      CALL DEWSET (N, ITOL, RTOL, ATOL, RWORK(LYH), RWORK(LEWT))
      DO 120 I = 1,N
          IF (RWORK(I+LEWT-1) .LE. 0.0D0) GO TO 621
120      RWORK(I+LEWT-1) = 1.0D0/RWORK(I+LEWT-1)
C-----
C The coding below computes the step size, H0, to be attempted on the
C first step, unless the user has supplied a value for this.
C First check that TOUT - T differs significantly from zero.
C A scalar tolerance quantity TOL is computed, as MAX(RTOL(I))
C if this is positive, or MAX(ATOL(I)/ABS(Y(I))) otherwise, adjusted
C so as to be between 100*UROUND and 1.0E-3.
C Then the computed value H0 is given by..
C
C
C      H0**2 = TOL / ( w0**2 + (1/NEQ) * SUM ( f(i)/ywt(i) )**2 )
C
C
C where      w0      = MAX ( ABS(T), ABS(TOUT) ),
C            f(i)    = i-th component of initial value of f,
C            ywt(i)  = EWT(i)/TOL (a weight for y(i)).
C The sign of H0 is inferred from the initial values of TOUT and T.
C-----
      IF (H0 .NE. 0.0D0) GO TO 180
      TDIST = ABS(TOUT - T)
      W0 = MAX(ABS(T),ABS(TOUT))
      IF (TDIST .LT. 2.0D0*UROUND*W0) GO TO 622
      TOL = RTOL(1)
      IF (ITOL .LE. 2) GO TO 140
      DO 130 I = 1,N
130      TOL = MAX(TOL,RTOL(I))
140      IF (TOL .GT. 0.0D0) GO TO 160
      ATOLI = ATOL(1)
      DO 150 I = 1,N
          IF (ITOL .EQ. 2 .OR. ITOL .EQ. 4) ATOLI = ATOL(I)
          AYI = ABS(Y(I))
          IF (AYI .NE. 0.0D0) TOL = MAX(TOL,ATOLI/AYI)
150      CONTINUE
160      TOL = MAX(TOL,100.0D0*UROUND)
      TOL = MIN(TOL,0.001D0)
      SUM = DVNORM (N, RWORK(LF0), RWORK(LEWT))
      SUM = 1.0D0/(TOL*W0*W0) + TOL*SUM**2
      H0 = 1.0D0/SQRT(SUM)
      H0 = MIN(H0,TDIST)
      H0 = SIGN(H0,TOUT-T)
C Adjust H0 if necessary to meet HMAX bound. -----
180      RH = ABS(H0)*HMXI
      IF (RH .GT. 1.0D0) H0 = H0/RH
C Load H with H0 and scale YH(*,2) by H0. -----
      H = H0
      DO 190 I = 1,N
190      RWORK(I+LF0-1) = H0*RWORK(I+LF0-1)
      GO TO 270
C-----
C Block D.
C The next code block is for continuation calls only (ISTATE = 2 or 3)
C and is to check stop conditions before taking a step.
C-----
200      NSLAST = NST
      GO TO (210, 250, 220, 230, 240), ITASK
210      IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 250
      CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
      IF (IFLAG .NE. 0) GO TO 627
      T = TOUT
      GO TO 420

```

```

220 TP = TN - HU*(1.0D0 + 100.0D0*UROUND)
   IF ((TP - TOUT)*H .GT. 0.0D0) GO TO 623
   IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 250
   GO TO 400
230 TCRIT = RWORK(1)
   IF ((TN - TCRIT)*H .GT. 0.0D0) GO TO 624
   IF ((TCRIT - TOUT)*H .LT. 0.0D0) GO TO 625
   IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 245
   CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
   IF (IFLAG .NE. 0) GO TO 627
   T = TOUT
   GO TO 420
240 TCRIT = RWORK(1)
   IF ((TN - TCRIT)*H .GT. 0.0D0) GO TO 624
245 HMX = ABS(TN) + ABS(H)
   IHIT = ABS(TN - TCRIT) .LE. 100.0D0*UROUND*HMX
   IF (IHIT) GO TO 400
   TNEXT = TN + H*(1.0D0 + 4.0D0*UROUND)
   IF ((TNEXT - TCRIT)*H .LE. 0.0D0) GO TO 250
   H = (TCRIT - TN)*(1.0D0 - 4.0D0*UROUND)
   IF (ISTATE .EQ. 2) JSTART = -2
C-----
C Block E.
C The next block is normally executed for all calls and contains
C the call to the one-step core integrator DSTODE.
C
C This is a looping point for the integration steps.
C
C First check for too many steps being taken, update EWT (if not at
C start of problem), check for too much accuracy being requested, and
C check for H below the roundoff level in T.
C-----
250 CONTINUE
   IF ((NST-NSLAST) .GE. MXSTEP) GO TO 500
   CALL DEWSET (N, ITOL, RTOL, ATOL, RWORK(LYH), RWORK(LEWT))
   DO 260 I = 1,N
      IF (RWORK(I+LEWT-1) .LE. 0.0D0) GO TO 510
260   RWORK(I+LEWT-1) = 1.0D0/RWORK(I+LEWT-1)
270 TOLSF = UROUND*DVNORM (N, RWORK(LYH), RWORK(LEWT))
   IF (TOLSF .LE. 1.0D0) GO TO 280
   TOLSF = TOLSF*2.0D0
   IF (NST .EQ. 0) GO TO 626
   GO TO 520
280 IF ((TN + H) .NE. TN) GO TO 290
   NHNIL = NHNIL + 1
   IF (NHNIL .GT. MXHNIL) GO TO 290
   MSG = 'DLSODE- Warning..internal T (=R1) and H (=R2) are'
   CALL XERRWD (MSG, 50, 101, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
   MSG = '      such that in the machine, T + H = T on the next step '
   CALL XERRWD (MSG, 60, 101, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
   MSG = '      (H = step size). Solver will continue anyway'
   CALL XERRWD (MSG, 50, 101, 0, 0, 0, 0, 2, TN, H)
   IF (NHNIL .LT. MXHNIL) GO TO 290
   MSG = 'DLSODE- Above warning has been issued I1 times. '
   CALL XERRWD (MSG, 50, 102, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
   MSG = '      It will not be issued again for this problem'
   CALL XERRWD (MSG, 50, 102, 0, 1, MXHNIL, 0, 0, 0.0D0, 0.0D0)
290 CONTINUE
C-----
C CALL DSTODE(NEQ,Y,YH,NYH,YH,EWT,SAVF,ACOR,WM,IWM,F,JAC,DPREPJ,DSOLSY)
C-----
   CALL DSTODE (NEQ, Y, RWORK(LYH), NYH, RWORK(LYH), RWORK(LEWT),
1  RWORK(LSAVF), RWORK(LACOR), RWORK(LWM), IWORK(LIWM),
2  F, JAC, DPREPJ, DSOLSY)
   KGO = 1 - KFLAG
   GO TO (300, 530, 540), KGO
C-----
C Block F.
C The following block handles the case of a successful return from the
C core integrator (KFLAG = 0). Test for stop conditions.
C-----
300 INIT = 1
   GO TO (310, 400, 330, 340, 350), ITASK

```

```

C ITASK = 1.  If TOUT has been reached, interpolate. -----
310 IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 250
    CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
    T = TOUT
    GO TO 420
C ITASK = 3.  Jump to exit if TOUT was reached. -----
330 IF ((TN - TOUT)*H .GE. 0.0D0) GO TO 400
    GO TO 250
C ITASK = 4.  See if TOUT or TCRIT was reached.  Adjust H if necessary.
340 IF ((TN - TOUT)*H .LT. 0.0D0) GO TO 345
    CALL DINTDY (TOUT, 0, RWORK(LYH), NYH, Y, IFLAG)
    T = TOUT
    GO TO 420
345 HMX = ABS(TN) + ABS(H)
    IHIT = ABS(TN - TCRIT) .LE. 100.0D0*UROUND*HMX
    IF (IHIT) GO TO 400
    TNEXT = TN + H*(1.0D0 + 4.0D0*UROUND)
    IF ((TNEXT - TCRIT)*H .LE. 0.0D0) GO TO 250
    H = (TCRIT - TN)*(1.0D0 - 4.0D0*UROUND)
    JSTART = -2
    GO TO 250
C ITASK = 5.  See if TCRIT was reached and jump to exit. -----
350 HMX = ABS(TN) + ABS(H)
    IHIT = ABS(TN - TCRIT) .LE. 100.0D0*UROUND*HMX
C-----
C Block G.
C The following block handles all successful returns from DLSODE.
C If ITASK .NE. 1, Y is loaded from YH and T is set accordingly.
C ISTATE is set to 2, and the optional outputs are loaded into the
C work arrays before returning.
C-----
400 DO 410 I = 1,N
410   Y(I) = RWORK(I+LYH-1)
    T = TN
    IF (ITASK .NE. 4 .AND. ITASK .NE. 5) GO TO 420
    IF (IHIT) T = TCRIT
420  ISTATE = 2
    RWORK(11) = HU
    RWORK(12) = H
    RWORK(13) = TN
    IWORK(11) = NST
    IWORK(12) = NFE
    IWORK(13) = NJE
    IWORK(14) = NQU
    IWORK(15) = NQ
    RETURN
C-----
C Block H.
C The following block handles all unsuccessful returns other than
C those for illegal input.  First the error message routine is called.
C If there was an error test or convergence test failure, IMXER is set.
C Then Y is loaded from YH and T is set to TN.  The optional outputs
C are loaded into the work arrays before returning.
C-----
C The maximum number of steps was taken before reaching TOUT. -----
500 MSG = 'DLSODE- At current T (=R1), MXSTEP (=I1) steps  '
    CALL XERRWD (MSG, 50, 201, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
    MSG = '          taken on this call before reaching TOUT  '
    CALL XERRWD (MSG, 50, 201, 0, 1, MXSTEP, 0, 1, TN, 0.0D0)
    ISTATE = -1
    GO TO 580
C EWT(I) .LE. 0.0 for some I (not at start of problem). -----
510 EWTI = RWORK(LEWT+I-1)
    MSG = 'DLSODE- At T (=R1), EWT(I1) has become R2 .LE. 0.'
    CALL XERRWD (MSG, 50, 202, 0, 1, I, 0, 2, TN, EWTI)
    ISTATE = -6
    GO TO 580
C Too much accuracy requested for machine precision. -----
520 MSG = 'DLSODE- At T (=R1), too much accuracy requested  '
    CALL XERRWD (MSG, 50, 203, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
    MSG = '          for precision of machine.. see TOLSF (=R2) '
    CALL XERRWD (MSG, 50, 203, 0, 0, 0, 0, 2, TN, TOLSF)
    RWORK(14) = TOLSF

```

```

        ISTATE = -2
        GO TO 580
C KFLAG = -1. Error test failed repeatedly or with ABS(H) = HMIN. -----
530 MSG = 'DLSODE- At T(=R1) and step size H(=R2), the error'
      CALL XERRWD (MSG, 50, 204, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      MSG = '          test failed repeatedly or with ABS(H) = HMIN'
      CALL XERRWD (MSG, 50, 204, 0, 0, 0, 0, 2, TN, H)
      ISTATE = -4
      GO TO 560
C KFLAG = -2. Convergence failed repeatedly or with ABS(H) = HMIN. ----
540 MSG = 'DLSODE- At T(=R1) and step size H(=R2), the '
      CALL XERRWD (MSG, 50, 205, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      MSG = '          corrector convergence failed repeatedly '
      CALL XERRWD (MSG, 50, 205, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      MSG = '          or with ABS(H) = HMIN '
      CALL XERRWD (MSG, 30, 205, 0, 0, 0, 0, 2, TN, H)
      ISTATE = -5
C Compute IMXER if relevant. -----
560 BIG = 0.0D0
      IMXER = 1
      DO 570 I = 1,N
        SIZE = ABS(RWORK(I+LACOR-1)*RWORK(I+LEWT-1))
        IF (BIG .GE. SIZE) GO TO 570
        BIG = SIZE
        IMXER = I
570   CONTINUE
      IWORK(16) = IMXER
C Set Y vector, T, and optional outputs. -----
580 DO 590 I = 1,N
590   Y(I) = RWORK(I+LYH-1)
      T = TN
      RWORK(11) = HU
      RWORK(12) = H
      RWORK(13) = TN
      IWORK(11) = NST
      IWORK(12) = NFE
      IWORK(13) = NJE
      IWORK(14) = NQU
      IWORK(15) = NQ
      RETURN
C-----
C Block I.
C The following block handles all error returns due to illegal input
C (ISTATE = -3), as detected before calling the core integrator.
C First the error message routine is called. If the illegal input
C is a negative ISTATE, the run is aborted (apparent infinite loop).
C-----
601 MSG = 'DLSODE- ISTATE(=I1) illegal '
      CALL XERRWD (MSG, 30, 1, 0, 1, ISTATE, 0, 0, 0.0D0, 0.0D0)
      IF (ISTATE .LT. 0) GO TO 800
      GO TO 700
602 MSG = 'DLSODE- ITASK(=I1) illegal '
      CALL XERRWD (MSG, 30, 2, 0, 1, ITASK, 0, 0, 0.0D0, 0.0D0)
      GO TO 700
603 MSG = 'DLSODE- ISTATE .GT. 1 but DLSODE not initialized '
      CALL XERRWD (MSG, 50, 3, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
      GO TO 700
604 MSG = 'DLSODE- NEQ(=I1) .LT. 1 '
      CALL XERRWD (MSG, 30, 4, 0, 1, NEQ(1), 0, 0, 0.0D0, 0.0D0)
      GO TO 700
605 MSG = 'DLSODE- ISTATE = 3 and NEQ increased (I1 to I2) '
      CALL XERRWD (MSG, 50, 5, 0, 2, N, NEQ(1), 0, 0.0D0, 0.0D0)
      GO TO 700
606 MSG = 'DLSODE- ITOL(=I1) illegal '
      CALL XERRWD (MSG, 30, 6, 0, 1, ITOL, 0, 0, 0.0D0, 0.0D0)
      GO TO 700
607 MSG = 'DLSODE- IOPT(=I1) illegal '
      CALL XERRWD (MSG, 30, 7, 0, 1, IOPT, 0, 0, 0.0D0, 0.0D0)
      GO TO 700
608 MSG = 'DLSODE- MF(=I1) illegal '
      CALL XERRWD (MSG, 30, 8, 0, 1, MF, 0, 0, 0.0D0, 0.0D0)
      GO TO 700
609 MSG = 'DLSODE- ML(=I1) illegal.. .LT.0 or .GE.NEQ(=I2)'

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        CALL XERRWD (MSG, 50, 9, 0, 2, ML, NEQ(1), 0, 0.0D0, 0.0D0)
        GO TO 700
610 MSG = 'DLSODE- MU (=I1) illegal.. .LT.0 or .GE.NEQ (=I2)'
        CALL XERRWD (MSG, 50, 10, 0, 2, MU, NEQ(1), 0, 0.0D0, 0.0D0)
        GO TO 700
611 MSG = 'DLSODE- MAXORD (=I1) .LT. 0 '
        CALL XERRWD (MSG, 30, 11, 0, 1, MAXORD, 0, 0, 0.0D0, 0.0D0)
        GO TO 700
612 MSG = 'DLSODE- MXSTEP (=I1) .LT. 0 '
        CALL XERRWD (MSG, 30, 12, 0, 1, MXSTEP, 0, 0, 0.0D0, 0.0D0)
        GO TO 700
613 MSG = 'DLSODE- MXHNIL (=I1) .LT. 0 '
        CALL XERRWD (MSG, 30, 13, 0, 1, MXHNIL, 0, 0, 0.0D0, 0.0D0)
        GO TO 700
614 MSG = 'DLSODE- TOUT (=R1) behind T (=R2) '
        CALL XERRWD (MSG, 40, 14, 0, 0, 0, 0, 2, TOUT, T)
        MSG = '      Integration direction is given by H0 (=R1) '
        CALL XERRWD (MSG, 50, 14, 0, 0, 0, 0, 1, H0, 0.0D0)
        GO TO 700
615 MSG = 'DLSODE- HMAX (=R1) .LT. 0.0 '
        CALL XERRWD (MSG, 30, 15, 0, 0, 0, 0, 1, HMAX, 0.0D0)
        GO TO 700
616 MSG = 'DLSODE- HMIN (=R1) .LT. 0.0 '
        CALL XERRWD (MSG, 30, 16, 0, 0, 0, 0, 1, HMIN, 0.0D0)
        GO TO 700
617 CONTINUE
        MSG='DLSODE- RWORK length needed, LENRW (=I1), exceeds LRW (=I2)'
        CALL XERRWD (MSG, 60, 17, 0, 2, LENRW, LRW, 0, 0.0D0, 0.0D0)
        GO TO 700
618 CONTINUE
        MSG='DLSODE- IWORK length needed, LENIW (=I1), exceeds LIW (=I2)'
        CALL XERRWD (MSG, 60, 18, 0, 2, LENIW, LIW, 0, 0.0D0, 0.0D0)
        GO TO 700
619 MSG = 'DLSODE- RTOL(I1) is R1 .LT. 0.0 '
        CALL XERRWD (MSG, 40, 19, 0, 1, I, 0, 1, RTOLI, 0.0D0)
        GO TO 700
620 MSG = 'DLSODE- ATOL(I1) is R1 .LT. 0.0 '
        CALL XERRWD (MSG, 40, 20, 0, 1, I, 0, 1, ATOLI, 0.0D0)
        GO TO 700
621 EWTI = RWORK(LEWT+I-1)
        MSG = 'DLSODE- EWT(I1) is R1 .LE. 0.0 '
        CALL XERRWD (MSG, 40, 21, 0, 1, I, 0, 1, EWTI, 0.0D0)
        GO TO 700
622 CONTINUE
        MSG='DLSODE- TOUT (=R1) too close to T(=R2) to start integration'
        CALL XERRWD (MSG, 60, 22, 0, 0, 0, 0, 2, TOUT, T)
        GO TO 700
623 CONTINUE
        MSG='DLSODE- ITASK = I1 and TOUT (=R1) behind TCUR - HU (= R2) '
        CALL XERRWD (MSG, 60, 23, 0, 1, ITASK, 0, 2, TOUT, TP)
        GO TO 700
624 CONTINUE
        MSG='DLSODE- ITASK = 4 OR 5 and TCRIT (=R1) behind TCUR (=R2) '
        CALL XERRWD (MSG, 60, 24, 0, 0, 0, 0, 2, TCRIT, TN)
        GO TO 700
625 CONTINUE
        MSG='DLSODE- ITASK = 4 or 5 and TCRIT (=R1) behind TOUT (=R2) '
        CALL XERRWD (MSG, 60, 25, 0, 0, 0, 0, 2, TCRIT, TOUT)
        GO TO 700
626 MSG = 'DLSODE- At start of problem, too much accuracy '
        CALL XERRWD (MSG, 50, 26, 0, 0, 0, 0, 0, 0.0D0, 0.0D0)
        MSG='      requested for precision of machine.. See TOLSF (=R1) '
        CALL XERRWD (MSG, 60, 26, 0, 0, 0, 0, 1, TOLSF, 0.0D0)
        RWORK(14) = TOLSF
        GO TO 700
627 MSG = 'DLSODE- Trouble in DINTDY. ITASK = I1, TOUT = R1'
        CALL XERRWD (MSG, 50, 27, 0, 1, ITASK, 0, 1, TOUT, 0.0D0)
C
700 ISTATE = -3
    RETURN
C
800 MSG = 'DLSODE- Run aborted.. apparent infinite loop '
        CALL XERRWD (MSG, 50, 303, 2, 0, 0, 0, 0, 0.0D0, 0.0D0)

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      RETURN
C----- END OF SUBROUTINE DLSODE -----
      END
*DECK DUMACH
      DOUBLE PRECISION FUNCTION DUMACH ()
C***BEGIN PROLOGUE  DUMACH
C***PURPOSE  Compute the unit roundoff of the machine.
C***CATEGORY  R1
C***TYPE      DOUBLE PRECISION (RUMACH-S, DUMACH-D)
C***KEYWORDS  MACHINE CONSTANTS
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C  *Usage:
C      DOUBLE PRECISION  A, DUMACH
C      A = DUMACH()
C
C  *Function Return Values:
C      A : the unit roundoff of the machine.
C
C  *Description:
C      The unit roundoff is defined as the smallest positive machine
C      number u such that 1.0 + u .ne. 1.0. This is computed by DUMACH
C      in a machine-independent manner.
C
C***REFERENCES  (NONE)
C***ROUTINES CALLED  DUMSUM
C***REVISION HISTORY  (YYYYMMDD)
C      19930216  DATE WRITTEN
C      19930818  Added SLATEC-format prologue.  (FNF)
C      20030707  Added DUMSUM to force normal storage of COMP.  (ACH)
C***END PROLOGUE  DUMACH
C
      DOUBLE PRECISION U, COMP
C***FIRST EXECUTABLE STATEMENT  DUMACH
      U = 1.0D0
10    U = U*0.5D0
      CALL DUMSUM(1.0D0, U, COMP)
      IF (COMP .NE. 1.0D0) GO TO 10
      DUMACH = U*2.0D0
      RETURN
C----- End of Function DUMACH -----
      END
      SUBROUTINE DUMSUM(A,B,C)
C      Routine to force normal storing of A + B, for DUMACH.
      DOUBLE PRECISION A, B, C
      C = A + B
      RETURN
      END
*DECK DCFODE
      SUBROUTINE DCFODE (METH, ELCO, TESCO)
C***BEGIN PROLOGUE  DCFODE
C***SUBSIDIARY
C***PURPOSE  Set ODE integrator coefficients.
C***TYPE      DOUBLE PRECISION (SCFODE-S, DCFODE-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C      DCFODE is called by the integrator routine to set coefficients
C      needed there. The coefficients for the current method, as
C      given by the value of METH, are set for all orders and saved.
C      The maximum order assumed here is 12 if METH = 1 and 5 if METH = 2.
C      (A smaller value of the maximum order is also allowed.)
C      DCFODE is called once at the beginning of the problem,
C      and is not called again unless and until METH is changed.
C
C      The ELCO array contains the basic method coefficients.
C      The coefficients el(i), 1 .le. i .le. nq+1, for the method of
C      order nq are stored in ELCO(i,nq). They are given by a generating
C      polynomial, i.e.,
C      
$$l(x) = el(1) + el(2)*x + \dots + el(nq+1)*x^{nq}.$$

C      For the implicit Adams methods, l(x) is given by
C      
$$dl/dx = (x+1)*(x+2)*\dots*(x+nq-1)/factorial(nq-1), \quad l(-1) = 0.$$

C      For the BDF methods, l(x) is given by

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C      1(x) = (x+1)*(x+2)* ... *(x+nq)/K,
C where      K = factorial(nq)*(1 + 1/2 + ... + 1/nq).
C
C The TESCO array contains test constants used for the
C local error test and the selection of step size and/or order.
C At order nq, TESCO(k,nq) is used for the selection of step
C size at order nq - 1 if k = 1, at order nq if k = 2, and at order
C nq + 1 if k = 3.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C  791129  DATE WRITTEN
C  890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C  890503  Minor cosmetic changes.  (FNF)
C  930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DCFODE
C**End
      INTEGER METH
      INTEGER I, IB, NQ, NQM1, NQP1
      DOUBLE PRECISION ELCO, TESCO
      DOUBLE PRECISION AGAMQ, FNQ, FNQM1, PC, PINT, RAGQ,
1    RQFAC, RQ1FAC, TSIGN, XPIN
      DIMENSION ELCO(13,12), TESCO(3,12)
      DIMENSION PC(12)

C
C***FIRST EXECUTABLE STATEMENT  DCFODE
      GO TO (100, 200), METH
C
100  ELCO(1,1) = 1.0D0
      ELCO(2,1) = 1.0D0
      TESCO(1,1) = 0.0D0
      TESCO(2,1) = 2.0D0
      TESCO(1,2) = 1.0D0
      TESCO(3,12) = 0.0D0
      PC(1) = 1.0D0
      RQFAC = 1.0D0
      DO 140 NQ = 2,12

C-----
C The PC array will contain the coefficients of the polynomial
C  $p(x) = (x+1)*(x+2)*...*(x+nq-1)$ .
C Initially,  $p(x) = 1$ .
C-----
      RQ1FAC = RQFAC
      RQFAC = RQFAC/NQ
      NQM1 = NQ - 1
      FNQM1 = NQM1
      NQP1 = NQ + 1
C Form coefficients of  $p(x)*(x+nq-1)$ . -----
      PC(NQ) = 0.0D0
      DO 110 IB = 1,NQM1
        I = NQP1 - IB
110    PC(I) = PC(I-1) + FNQM1*PC(I)
        PC(1) = FNQM1*PC(1)
C Compute integral, -1 to 0, of  $p(x)$  and  $x*p(x)$ . -----
      PINT = PC(1)
      XPIN = PC(1)/2.0D0
      TSIGN = 1.0D0
      DO 120 I = 2,NQ
        TSIGN = -TSIGN
        PINT = PINT + TSIGN*PC(I)/I
120    XPIN = XPIN + TSIGN*PC(I)/(I+1)
C Store coefficients in ELCO and TESCO. -----
      ELCO(1,NQ) = PINT*RQ1FAC
      ELCO(2,NQ) = 1.0D0
      DO 130 I = 2,NQ
130    ELCO(I+1,NQ) = RQ1FAC*PC(I)/I
        AGAMQ = RQFAC*XPIN
        RAGQ = 1.0D0/AGAMQ
        TESCO(2,NQ) = RAGQ
        IF (NQ .LT. 12) TESCO(1,NQP1) = RAGQ*RQFAC/NQP1
        TESCO(3,NQM1) = RAGQ
140  CONTINUE

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        RETURN
C
200  PC(1) = 1.0D0
    RQ1FAC = 1.0D0
    DO 230 NQ = 1,5
C-----
C The PC array will contain the coefficients of the polynomial
C    $p(x) = (x+1)*(x+2)*...*(x+nq)$ .
C Initially,  $p(x) = 1$ .
C-----
        FNQ = NQ
        NQP1 = NQ + 1
C Form coefficients of  $p(x)*(x+nq)$ . -----
        PC(NQP1) = 0.0D0
        DO 210 IB = 1,NQ
            I = NQ + 2 - IB
210     PC(I) = PC(I-1) + FNQ*PC(I)
        PC(1) = FNQ*PC(1)
C Store coefficients in ELCO and TESCO. -----
        DO 220 I = 1,NQP1
220     ELCO(I,NQ) = PC(I)/PC(2)
        ELCO(2,NQ) = 1.0D0
        TESCO(1,NQ) = RQ1FAC
        TESCO(2,NQ) = NQP1/ELCO(1,NQ)
        TESCO(3,NQ) = (NQ+2)/ELCO(1,NQ)
        RQ1FAC = RQ1FAC/FNQ
230     CONTINUE
        RETURN
C----- END OF SUBROUTINE DCFODE -----
        END
*DECK DINTDY
        SUBROUTINE DINTDY (T, K, YH, NYH, DKY, IFLAG)
C***BEGIN PROLOGUE  DINTDY
C***SUBSIDIARY
C***PURPOSE  Interpolate solution derivatives.
C***TYPE      DOUBLE PRECISION (SINTDY-S, DINTDY-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C   DINTDY computes interpolated values of the K-th derivative of the
C   dependent variable vector y, and stores it in DKY. This routine
C   is called within the package with K = 0 and T = TOUT, but may
C   also be called by the user for any K up to the current order.
C   (See detailed instructions in the usage documentation.)
C
C   The computed values in DKY are gotten by interpolation using the
C   Nordsieck history array YH. This array corresponds uniquely to a
C   vector-valued polynomial of degree NQCUR or less, and DKY is set
C   to the K-th derivative of this polynomial at T.
C   The formula for DKY is:
C
C       
$$DKY(i) = \sum_{j=K}^q c(j,K) * (T - tn)^{(j-K)} * h^{(-j)} * YH(i,j+1)$$

C   where  $c(j,K) = j*(j-1)*...*(j-K+1)$ ,  $q = NQCUR$ ,  $tn = TCUR$ ,  $h = HCUR$ .
C   The quantities  $nq = NQCUR$ ,  $l = nq+1$ ,  $N = NEQ$ ,  $tn$ , and  $h$  are
C   communicated by COMMON. The above sum is done in reverse order.
C   IFLAG is returned negative if either K or T is out of bounds.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  XERRWD
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format. (FNF)
C   890503  Minor cosmetic changes. (FNF)
C   930809  Renamed to allow single/double precision versions. (ACH)
C   010418  Reduced size of Common block /DLS001/. (ACH)
C   031105  Restored 'own' variables to Common block /DLS001/, to
C           enable interrupt/restart feature. (ACH)
C   050427  Corrected roundoff decrement in TP. (ACH)
C***END PROLOGUE  DINTDY
C**End
        INTEGER K, NYH, IFLAG

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      DOUBLE PRECISION T, YH, DKY
      DIMENSION YH(NYH,*), DKY(*)
      INTEGER IOWND, IOWNS,
1     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
2     LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
3     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      DOUBLE PRECISION ROWNS,
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
      COMMON /DLS001/ ROWNS(209),
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
2     IOWND(6), IOWNS(6),
3     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
4     LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
5     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      INTEGER I, IC, J, JB, JB2, JJ, JJ1, JP1
      DOUBLE PRECISION C, R, S, TP
      CHARACTER*80 MSG
C
C***FIRST EXECUTABLE STATEMENT  DINTDY
      IFLAG = 0
      IF (K .LT. 0 .OR. K .GT. NQ) GO TO 80
      TP = TN - HU - 100.0D0*UROUND*SIGN(ABS(TN) + ABS(HU), HU)
      IF ((T-TP)*(T-TN) .GT. 0.0D0) GO TO 90
C
      S = (T - TN)/H
      IC = 1
      IF (K .EQ. 0) GO TO 15
      JJ1 = L - K
      DO 10 JJ = JJ1,NQ
10      IC = IC*JJ
15      C = IC
      DO 20 I = 1,N
20      DKY(I) = C*YH(I,L)
      IF (K .EQ. NQ) GO TO 55
      JB2 = NQ - K
      DO 50 JB = 1,JB2
      J = NQ - JB
      JP1 = J + 1
      IC = 1
      IF (K .EQ. 0) GO TO 35
      JJ1 = JP1 - K
      DO 30 JJ = JJ1,J
30      IC = IC*JJ
35      C = IC
      DO 40 I = 1,N
40      DKY(I) = C*YH(I,JP1) + S*DKY(I)
50      CONTINUE
      IF (K .EQ. 0) RETURN
55      R = H*(-K)
      DO 60 I = 1,N
60      DKY(I) = R*DKY(I)
      RETURN
C
80      MSG = 'DINTDY- K (=I1) illegal          '
      CALL XERRWD (MSG, 30, 51, 0, 1, K, 0, 0, 0.0D0, 0.0D0)
      IFLAG = -1
      RETURN
90      MSG = 'DINTDY- T (=R1) illegal          '
      CALL XERRWD (MSG, 30, 52, 0, 0, 0, 0, 1, T, 0.0D0)
      MSG='          T not in interval TCUR - HU (= R1) to TCUR (=R2)          '
      CALL XERRWD (MSG, 60, 52, 0, 0, 0, 0, 2, TP, TN)
      IFLAG = -2
      RETURN
C----- END OF SUBROUTINE DINTDY -----
      END
*DECK DPREPJ
      SUBROUTINE DPREPJ (NEQ, Y, YH, NYH, EWT, FTEM, SAVF, WM, IWM,
1     F, JAC)
C***BEGIN PROLOGUE  DPREPJ
C***SUBSIDIARY
C***PURPOSE Compute and process Newton iteration matrix.
C***TYPE DOUBLE PRECISION (SPREPJ-S, DPREPJ-D)
C***AUTHOR Hindmarsh, Alan C., (LLNL)

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C***DESCRIPTION
C
C  DPREPJ is called by DSTODE to compute and process the matrix
C   $P = I - h*el(1)*J$ , where J is an approximation to the Jacobian.
C  Here J is computed by the user-supplied routine JAC if
C  MITER = 1 or 4, or by finite differencing if MITER = 2, 3, or 5.
C  If MITER = 3, a diagonal approximation to J is used.
C  J is stored in WM and replaced by P. If MITER .ne. 3, P is then
C  subjected to LU decomposition in preparation for later solution
C  of linear systems with P as coefficient matrix. This is done
C  by DGEFA if MITER = 1 or 2, and by DGBFA if MITER = 4 or 5.
C
C  In addition to variables described in DSTODE and DLSODE prologues,
C  communication with DPREPJ uses the following:
C  Y      = array containing predicted values on entry.
C  FTEM   = work array of length N (ACOR in DSTODE).
C  SAVF   = array containing f evaluated at predicted y.
C  WM     = real work space for matrices. On output it contains the
C           inverse diagonal matrix if MITER = 3 and the LU decomposition
C           of P if MITER is 1, 2, 4, or 5.
C           Storage of matrix elements starts at WM(3).
C           WM also contains the following matrix-related data:
C           WM(1) = SQRT(UROUND), used in numerical Jacobian increments.
C           WM(2) = H*EL0, saved for later use if MITER = 3.
C  IWM    = integer work space containing pivot information, starting at
C           IWM(21), if MITER is 1, 2, 4, or 5. IWM also contains band
C           parameters ML = IWM(1) and MU = IWM(2) if MITER is 4 or 5.
C  EL0    = EL(1) (input).
C  IERPJ  = output error flag, = 0 if no trouble, .gt. 0 if
C           P matrix found to be singular.
C  JCUR   = output flag = 1 to indicate that the Jacobian matrix
C           (or approximation) is now current.
C  This routine also uses the COMMON variables EL0, H, TN, UROUND,
C  MITER, N, NFE, and NJE.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  DGBFA, DGEFA, DVNORM
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YYMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890504  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions.  (ACH)
C   010418  Reduced size of Common block /DLS001/.  (ACH)
C   031105  Restored 'own' variables to Common block /DLS001/, to
C           enable interrupt/restart feature.  (ACH)
C***END PROLOGUE  DPREPJ
C**End
      EXTERNAL F, JAC
      INTEGER NEQ, NYH, IWM
      DOUBLE PRECISION Y, YH, EWT, FTEM, SAVF, WM
      DIMENSION NEQ(*), Y(*), YH(NYH,*), EWT(*), FTEM(*), SAVF(*),
1     WM(*), IWM(*)
      INTEGER IOWND, IOWNS,
1     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
2     LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
3     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      DOUBLE PRECISION ROWNS,
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
      COMMON /DLS001/ ROWNS(209),
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
2     IOWND(6), IOWNS(6),
3     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
4     LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
5     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      INTEGER I, I1, I2, IER, II, J, J1, JJ, LENP,
1     MBA, MBAND, MEB1, MEBAND, ML, ML3, MU, NP1
      DOUBLE PRECISION CON, DI, FAC, HL0, R, R0, SRUR, YI, YJ, YJJ,
1     DVNORM
C
C***FIRST EXECUTABLE STATEMENT  DPREPJ
      NJE = NJE + 1
      IERPJ = 0

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        JCUR = 1
        HL0 = H*EL0
        GO TO (100, 200, 300, 400, 500), MITER
C If MITER = 1, call JAC and multiply by scalar. -----
100  LENP = N*N
    DO 110 I = 1,LENP
110  WM(I+2) = 0.0D0
    CALL JAC (NEQ, TN, Y, 0, 0, WM(3), N)
    CON = -HL0
    DO 120 I = 1,LENP
120  WM(I+2) = WM(I+2)*CON
    GO TO 240
C If MITER = 2, make N calls to F to approximate J. -----
200  FAC = DVNORM (N, SAVF, EWT)
    R0 = 1000.0D0*ABS(H)*UROUND*N*FAC
    IF (R0 .EQ. 0.0D0) R0 = 1.0D0
    SRUR = WM(1)
    J1 = 2
    DO 230 J = 1,N
        YJ = Y(J)
        R = MAX(SRUR*ABS(YJ),R0/EWT(J))
        Y(J) = Y(J) + R
        FAC = -HL0/R
        CALL F (NEQ, TN, Y, FTEM)
        DO 220 I = 1,N
220  WM(I+J1) = (FTEM(I) - SAVF(I))*FAC
        Y(J) = YJ
        J1 = J1 + N
230  CONTINUE
    NFE = NFE + N
C Add identity matrix. -----
240  J = 3
    NP1 = N + 1
    DO 250 I = 1,N
        WM(J) = WM(J) + 1.0D0
250  J = J + NP1
C Do LU decomposition on P. -----
    CALL DGEFA (WM(3), N, N, IWM(21), IER)
    IF (IER .NE. 0) IERPJ = 1
    RETURN
C If MITER = 3, construct a diagonal approximation to J and P. -----
300  WM(2) = HL0
    R = EL0*0.1D0
    DO 310 I = 1,N
310  Y(I) = Y(I) + R*(H*SAVF(I) - YH(I,2))
    CALL F (NEQ, TN, Y, WM(3))
    NFE = NFE + 1
    DO 320 I = 1,N
        R0 = H*SAVF(I) - YH(I,2)
        DI = 0.1D0*R0 - H*(WM(I+2) - SAVF(I))
        WM(I+2) = 1.0D0
        IF (ABS(R0) .LT. UROUND/EWT(I)) GO TO 320
        IF (ABS(DI) .EQ. 0.0D0) GO TO 330
        WM(I+2) = 0.1D0*R0/DI
320  CONTINUE
    RETURN
330  IERPJ = 1
    RETURN
C If MITER = 4, call JAC and multiply by scalar. -----
400  ML = IWM(1)
    MU = IWM(2)
    ML3 = ML + 3
    MBAND = ML + MU + 1
    MEBAND = MBAND + ML
    LENP = MEBAND*N
    DO 410 I = 1,LENP
410  WM(I+2) = 0.0D0
    CALL JAC (NEQ, TN, Y, ML, MU, WM(ML3), MEBAND)
    CON = -HL0
    DO 420 I = 1,LENP
420  WM(I+2) = WM(I+2)*CON
    GO TO 570
C If MITER = 5, make MBAND calls to F to approximate J. -----

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500  ML = IWM(1)
      MU = IWM(2)
      MBAND = ML + MU + 1
      MBA = MIN(MBAND,N)
      MEBAND = MBAND + ML
      MEB1 = MEBAND - 1
      SRUR = WM(1)
      FAC = DVNORM (N, SAVF, EWT)
      R0 = 1000.0D0*ABS(H)*UROUND*N*FAC
      IF (R0 .EQ. 0.0D0) R0 = 1.0D0
      DO 560 J = 1,MBA
          DO 530 I = J,N,MBAND
              YI = Y(I)
              R = MAX(SRUR*ABS(YI),R0/EWT(I))
530    Y(I) = Y(I) + R
          CALL F (NEQ, TN, Y, FTEM)
          DO 550 JJ = J,N,MBAND
              Y(JJ) = YH(JJ,1)
              YJJ = Y(JJ)
              R = MAX(SRUR*ABS(YJJ),R0/EWT(JJ))
              FAC = -HL0/R
              I1 = MAX(JJ-MU,1)
              I2 = MIN(JJ+ML,N)
              II = JJ*MEB1 - ML + 2
              DO 540 I = I1,I2
540                WM(II+I) = (FTEM(I) - SAVF(I))*FAC
550          CONTINUE
560    CONTINUE
      NFE = NFE + MBA
C Add identity matrix. -----
570  II = MBAND + 2
      DO 580 I = 1,N
          WM(II) = WM(II) + 1.0D0
580  II = II + MEBAND
C Do LU decomposition of P. -----
      CALL DGBFA (WM(3), MEBAND, N, ML, MU, IWM(21), IER)
      IF (IER .NE. 0) IERPJ = 1
      RETURN
C----- END OF SUBROUTINE DPREPJ -----
      END
*DECK DSOLSY
      SUBROUTINE DSOLSY (WM, IWM, X, TEM)
C***BEGIN PROLOGUE  DSOLSY
C***SUBSIDIARY
C***PURPOSE  ODEPACK linear system solver.
C***TYPE      DOUBLE PRECISION (SSOLSY-S, DSOLSY-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  This routine manages the solution of the linear system arising from
C  a chord iteration.  It is called if MITER .ne. 0.
C  If MITER is 1 or 2, it calls DGESL to accomplish this.
C  If MITER = 3 it updates the coefficient h*EL0 in the diagonal
C  matrix, and then computes the solution.
C  If MITER is 4 or 5, it calls DGBSL.
C  Communication with DSOLSY uses the following variables:
C  WM      = real work space containing the inverse diagonal matrix if
C            MITER = 3 and the LU decomposition of the matrix otherwise.
C            Storage of matrix elements starts at WM(3).
C            WM also contains the following matrix-related data:
C            WM(1) = SQRT(UROUND) (not used here),
C            WM(2) = HL0, the previous value of h*EL0, used if MITER = 3.
C  IWM     = integer work space containing pivot information, starting at
C            IWM(21), if MITER is 1, 2, 4, or 5.  IWM also contains band
C            parameters ML = IWM(1) and MU = IWM(2) if MITER is 4 or 5.
C  X       = the right-hand side vector on input, and the solution vector
C            on output, of length N.
C  TEM     = vector of work space of length N, not used in this version.
C  IERSL   = output flag (in COMMON).  IERSL = 0 if no trouble occurred.
C            IERSL = 1 if a singular matrix arose with MITER = 3.
C  This routine also uses the COMMON variables EL0, H, MITER, and N.
C
C***SEE ALSO  DLSODE

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C***ROUTINES CALLED  DGBSL, DGESL
C***COMMON BLOCKS   DLS001
C***REVISION HISTORY (YYMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions. (ACH)
C   010418  Reduced size of Common block /DLS001/. (ACH)
C   031105  Restored 'own' variables to Common block /DLS001/, to
C           enable interrupt/restart feature. (ACH)
C***END PROLOGUE  DSOLSY
C**End
      INTEGER IWM
      DOUBLE PRECISION WM, X, TEM
      DIMENSION WM(*), IWM(*), X(*), TEM(*)
      INTEGER IOWND, IOWNS,
1     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
2     LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
3     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      DOUBLE PRECISION ROWNS,
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
      COMMON /DLS001/ ROWNS(209),
1     CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
2     IOWND(6), IOWNS(6),
3     ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
4     LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
5     MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
      INTEGER I, MEBAND, ML, MU
      DOUBLE PRECISION DI, HL0, PHL0, R
C
C***FIRST EXECUTABLE STATEMENT  DSOLSY
      IERSL = 0
      GO TO (100, 100, 300, 400, 400), MITER
100  CALL DGESL (WM(3), N, N, IWM(21), X, 0)
      RETURN
C
300  PHL0 = WM(2)
      HL0 = H*EL0
      WM(2) = HL0
      IF (HL0 .EQ. PHL0) GO TO 330
      R = HL0/PHL0
      DO 320 I = 1,N
          DI = 1.0D0 - R*(1.0D0 - 1.0D0/WM(I+2))
          IF (ABS(DI) .EQ. 0.0D0) GO TO 390
320  WM(I+2) = 1.0D0/DI
330  DO 340 I = 1,N
340  X(I) = WM(I+2)*X(I)
      RETURN
390  IERSL = 1
      RETURN
C
400  ML = IWM(1)
      MU = IWM(2)
      MEBAND = 2*ML + MU + 1
      CALL DGBSL (WM(3), MEBAND, N, ML, MU, IWM(21), X, 0)
      RETURN
C----- END OF SUBROUTINE DSOLSY -----
      END
*DECK DSRCOM
      SUBROUTINE DSRCOM (RSAV, ISAV, JOB)
C***BEGIN PROLOGUE  DSRCOM
C***SUBSIDIARY
C***PURPOSE  Save/restore ODEPACK COMMON blocks.
C***TYPE      DOUBLE PRECISION (SSRCOM-S, DSRCOM-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C   This routine saves or restores (depending on JOB) the contents of
C   the COMMON block DLS001, which is used internally
C   by one or more ODEPACK solvers.
C
C   RSAV = real array of length 218 or more.
C   ISAV = integer array of length 37 or more.

```



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C JOB = flag indicating to save or restore the COMMON blocks:
C   JOB = 1 if COMMON is to be saved (written to RSAV/ISAV)
C   JOB = 2 if COMMON is to be restored (read from RSAV/ISAV)
C   A call with JOB = 2 presumes a prior call with JOB = 1.
C
C***SEE ALSO DLSODE
C***ROUTINES CALLED (NONE)
C***COMMON BLOCKS DLS001
C***REVISION HISTORY (YYMMDD)
C 791129 DATE WRITTEN
C 890501 Modified prologue to SLATEC/LDOC format. (FNF)
C 890503 Minor cosmetic changes. (FNF)
C 921116 Deleted treatment of block /EH0001/. (ACH)
C 930801 Reduced Common block length by 2. (ACH)
C 930809 Renamed to allow single/double precision versions. (ACH)
C 010418 Reduced Common block length by 209+12. (ACH)
C 031105 Restored 'own' variables to Common block /DLS001/, to
C        enable interrupt/restart feature. (ACH)
C 031112 Added SAVE statement for data-loaded constants.
C***END PROLOGUE DSRCOM
C**End
      INTEGER ISAV, JOB
      INTEGER ILS
      INTEGER I, LENILS, LENRLS
      DOUBLE PRECISION RSAV, RLS
      DIMENSION RSAV(*), ISAV(*)
      SAVE LENRLS, LENILS
      COMMON /DLS001/ RLS(218), ILS(37)
      DATA LENRLS/218/, LENILS/37/

C
C***FIRST EXECUTABLE STATEMENT DSRCOM
      IF (JOB .EQ. 2) GO TO 100
C
      DO 10 I = 1,LENRLS
10      RSAV(I) = RLS(I)
      DO 20 I = 1,LENILS
20      ISAV(I) = ILS(I)
      RETURN

C
100 CONTINUE
      DO 110 I = 1,LENRLS
110      RLS(I) = RSAV(I)
      DO 120 I = 1,LENILS
120      ILS(I) = ISAV(I)
      RETURN

C----- END OF SUBROUTINE DSRCOM -----
      END
*DECK DSTODE
      SUBROUTINE DSTODE (NEQ, Y, YH, NYH, YH1, EWT, SAVF, ACOR,
1 WM, IWM, F, JAC, PJAC, SLVS)
C***BEGIN PROLOGUE DSTODE
C***SUBSIDIARY
C***PURPOSE Performs one step of an ODEPACK integration.
C***TYPE DOUBLE PRECISION (SSTODE-S, DSTODE-D)
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C DSTODE performs one step of the integration of an initial value
C problem for a system of ordinary differential equations.
C Note: DSTODE is independent of the value of the iteration method
C indicator MITER, when this is .ne. 0, and hence is independent
C of the type of chord method used, or the Jacobian structure.
C Communication with DSTODE is done with the following variables:
C
C NEQ = integer array containing problem size in NEQ(1), and
C      passed as the NEQ argument in all calls to F and JAC.
C Y = an array of length .ge. N used as the Y argument in
C     all calls to F and JAC.
C YH = an NYH by LMAX array containing the dependent variables
C      and their approximate scaled derivatives, where
C      LMAX = MAXORD + 1. YH(i,j+1) contains the approximate
C      j-th derivative of y(i), scale/d by h**j/factorial(j)
C      (j = 0,1,...,NQ). on entry for the first step, the first

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```

C      two columns of YH must be set from the initial values.
C NYH   = a constant integer .ge. N, the first dimension of YH.
C YH1   = a one-dimensional array occupying the same space as YH.
C EWT   = an array of length N containing multiplicative weights
C        for local error measurements. Local errors in Y(i) are
C        compared to 1.0/EWT(i) in various error tests.
C SAVF  = an array of working storage, of length N.
C        Also used for input of YH(*,MAXORD+2) when JSTART = -1
C        and MAXORD .lt. the current order NQ.
C ACOR   = a work array of length N, used for the accumulated
C        corrections. On a successful return, ACOR(i) contains
C        the estimated one-step local error in Y(i).
C WM,IWM = real and integer work arrays associated with matrix
C        operations in chord iteration (MITER .ne. 0).
C PJAC   = name of routine to evaluate and preprocess Jacobian matrix
C        and  $P = I - h \cdot e_{10} \cdot JAC$ , if a chord method is being used.
C SLVS   = name of routine to solve linear system in chord iteration.
C CCMAX  = maximum relative change in  $h \cdot e_{10}$  before PJAC is called.
C H      = the step size to be attempted on the next step.
C        H is altered by the error control algorithm during the
C        problem. H can be either positive or negative, but its
C        sign must remain constant throughout the problem.
C HMIN   = the minimum absolute value of the step size h to be used.
C HMXI   = inverse of the maximum absolute value of h to be used.
C        HMXI = 0.0 is allowed and corresponds to an infinite hmax.
C        HMIN and HMXI may be changed at any time, but will not
C        take effect until the next change of h is considered.
C TN     = the independent variable. TN is updated on each step taken.
C JSTART = an integer used for input only, with the following
C        values and meanings:
C          0   perform the first step.
C          .gt.0 take a new step continuing from the last.
C          -1   take the next step with a new value of H, MAXORD,
C               N, METH, MITER, and/or matrix parameters.
C          -2   take the next step with a new value of H,
C               but with other inputs unchanged.
C        On return, JSTART is set to 1 to facilitate continuation.
C KFLAG  = a completion code with the following meanings:
C          0   the step was succesful.
C          -1   the requested error could not be achieved.
C          -2   corrector convergence could not be achieved.
C          -3   fatal error in PJAC or SLVS.
C        A return with KFLAG = -1 or -2 means either
C         $abs(H) = HMIN$  or 10 consecutive failures occurred.
C        On a return with KFLAG negative, the values of TN and
C        the YH array are as of the beginning of the last
C        step, and H is the last step size attempted.
C MAXORD = the maximum order of integration method to be allowed.
C MAXCOR = the maximum number of corrector iterations allowed.
C MSBP   = maximum number of steps between PJAC calls (MITER .gt. 0).
C MXNCF  = maximum number of convergence failures allowed.
C METH/MITER = the method flags. See description in driver.
C N      = the number of first-order differential equations.
C The values of CCMAX, H, HMIN, HMXI, TN, JSTART, KFLAG, MAXORD,
C MAXCOR, MSBP, MXNCF, METH, MITER, and N are communicated via COMMON.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  DCFODE, DVNORM
C***COMMON BLOCKS  DLS001
C***REVISION HISTORY  (YYMMDD)
C  791129  DATE WRITTEN
C  890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C  890503  Minor cosmetic changes.  (FNF)
C  930809  Renamed to allow single/double precision versions.  (ACH)
C  010418  Reduced size of Common block /DLS001/.  (ACH)
C  031105  Restored 'own' variables to Common block /DLS001/, to
C          enable interrupt/restart feature.  (ACH)
C***END PROLOGUE  DSTODE
C**End
      EXTERNAL F, JAC, PJAC, SLVS
      INTEGER NEQ, NYH, IWM
      DOUBLE PRECISION Y, YH, YH1, EWT, SAVF, ACOR, WM
      DIMENSION NEQ(*), Y(*), YH(NYH,*), YH1(*), EWT(*), SAVF(*),

```

```

1  ACOR(*), WM(*), IWM(*)
   INTEGER IOWND, IALTH, IPUP, LMAX, MEO, NQNYH, NSLP,
1  ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
2  LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
3  MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU
   INTEGER I, I1, IREDO, IRET, J, JB, M, NCF, NEWQ
   DOUBLE PRECISION CONIT, CRATE, EL, ELCO, HOLD, RMAX, TESCO,
2  CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND
   DOUBLE PRECISION DCON, DDN, DEL, DELP, DSM, DUP, EXDN, EXSM, EXUP,
1  R, RH, RHDN, RHSM, RHUP, TOLD, DVNORM
   COMMON /DLS001/ CONIT, CRATE, EL(13), ELCO(13,12),
1  HOLD, RMAX, TESCO(3,12),
2  CCMAX, EL0, H, HMIN, HMXI, HU, RC, TN, UROUND,
3  IOWND(6), IALTH, IPUP, LMAX, MEO, NQNYH, NSLP,
4  ICF, IERPJ, IERSL, JCUR, JSTART, KFLAG, L,
5  LYH, LEWT, LACOR, LSAVF, LWM, LIWM, METH, MITER,
5  MAXORD, MAXCOR, MSBP, MXNCF, N, NQ, NST, NFE, NJE, NQU

```

C

C***FIRST EXECUTABLE STATEMENT DSTODE

```

   KFLAG = 0
   TOLD = TN
   NCF = 0
   IERPJ = 0
   IERSL = 0
   JCUR = 0
   ICF = 0
   DELP = 0.0D0
   IF (JSTART .GT. 0) GO TO 200
   IF (JSTART .EQ. -1) GO TO 100
   IF (JSTART .EQ. -2) GO TO 160

```

C-----

C On the first call, the order is set to 1, and other variables are
C initialized. RMAX is the maximum ratio by which H can be increased
C in a single step. It is initially 1.E4 to compensate for the small
C initial H, but then is normally equal to 10. If a failure
C occurs (in corrector convergence or error test), RMAX is set to 2
C for the next increase.

C-----

```

   LMAX = MAXORD + 1
   NQ = 1
   L = 2
   IALTH = 2
   RMAX = 10000.0D0
   RC = 0.0D0
   EL0 = 1.0D0
   CRATE = 0.7D0
   HOLD = H
   MEO = METH
   NSLP = 0
   IPUP = MITER
   IRET = 3
   GO TO 140

```

C-----

C The following block handles preliminaries needed when JSTART = -1.
C IPUP is set to MITER to force a matrix update.
C If an order increase is about to be considered (IALTH = 1),
C IALTH is reset to 2 to postpone consideration one more step.
C If the caller has changed METH, DCFODE is called to reset
C the coefficients of the method.
C If the caller has changed MAXORD to a value less than the current
C order NQ, NQ is reduced to MAXORD, and a new H chosen accordingly.
C If H is to be changed, YH must be rescaled.
C If H or METH is being changed, IALTH is reset to L = NQ + 1
C to prevent further changes in H for that many steps.

C-----

```

100 IPUP = MITER
   LMAX = MAXORD + 1
   IF (IALTH .EQ. 1) IALTH = 2
   IF (METH .EQ. MEO) GO TO 110
   CALL DCFODE (METH, ELCO, TESCO)
   MEO = METH
   IF (NQ .GT. MAXORD) GO TO 120
   IALTH = L

```

```

      IRET = 1
      GO TO 150
110  IF (NQ .LE. MAXORD) GO TO 160
120  NQ = MAXORD
      L = LMAX
      DO 125 I = 1,L
125  EL(I) = ELCO(I,NQ)
      NQNYH = NQ*NYH
      RC = RC*EL(1)/EL0
      EL0 = EL(1)
      CONIT = 0.5D0/(NQ+2)
      DDN = DVNORM (N, SAVF, EWT)/TESCO(1,L)
      EXDN = 1.0D0/L
      RHDN = 1.0D0/(1.3D0*DDN**EXDN + 0.0000013D0)
      RH = MIN(RHDN,1.0D0)
      IREDO = 3
      IF (H .EQ. HOLD) GO TO 170
      RH = MIN(RH,ABS(H/HOLD))
      H = HOLD
      GO TO 175
C-----
C DCFODE is called to get all the integration coefficients for the
C current METH. Then the EL vector and related constants are reset
C whenever the order NQ is changed, or at the start of the problem.
C-----
140  CALL DCFODE (METH, ELCO, TESCO)
150  DO 155 I = 1,L
155  EL(I) = ELCO(I,NQ)
      NQNYH = NQ*NYH
      RC = RC*EL(1)/EL0
      EL0 = EL(1)
      CONIT = 0.5D0/(NQ+2)
      GO TO (160, 170, 200), IRET
C-----
C If H is being changed, the H ratio RH is checked against
C RMAX, HMIN, and HMXI, and the YH array rescaled. IALTH is set to
C L = NQ + 1 to prevent a change of H for that many steps, unless
C forced by a convergence or error test failure.
C-----
160  IF (H .EQ. HOLD) GO TO 200
      RH = H/HOLD
      H = HOLD
      IREDO = 3
      GO TO 175
170  RH = MAX(RH,HMIN/ABS(H))
175  RH = MIN(RH,RMAX)
      RH = RH/MAX(1.0D0,ABS(H)*HMXI*RH)
      R = 1.0D0
      DO 180 J = 2,L
          R = R*RH
          DO 180 I = 1,N
180  YH(I,J) = YH(I,J)*R
      H = H*RH
      RC = RC*RH
      IALTH = L
      IF (IREDO .EQ. 0) GO TO 690
C-----
C This section computes the predicted values by effectively
C multiplying the YH array by the Pascal Triangle matrix.
C RC is the ratio of new to old values of the coefficient H*EL(1).
C When RC differs from 1 by more than CCMAX, IPUP is set to MITER
C to force PJAC to be called, if a Jacobian is involved.
C In any case, PJAC is called at least every MSBP steps.
C-----
200  IF (ABS(RC-1.0D0) .GT. CCMAX) IPUP = MITER
      IF (NST .GE. NSLP+MSBP) IPUP = MITER
      TN = TN + H
      I1 = NQNYH + 1
      DO 215 JB = 1,NQ
          I1 = I1 - NYH
Cdir$ ivdep
      DO 210 I = I1,NQNYH
210  YH1(I) = YH1(I) + YH1(I+NYH)

```

```

215     CONTINUE
C-----
C Up to MAXCOR corrector iterations are taken. A convergence test is
C made on the R.M.S. norm of each correction, weighted by the error
C weight vector EWT. The sum of the corrections is accumulated in the
C vector ACOR(i). The YH array is not altered in the corrector loop.
C-----
220     M = 0
        DO 230 I = 1,N
230       Y(I) = YH(I,1)
          CALL F (NEQ, TN, Y, SAVF)
          NFE = NFE + 1
          IF (IPUP .LE. 0) GO TO 250
C-----
C If indicated, the matrix P = I - h*el(1)*J is reevaluated and
C preprocessed before starting the corrector iteration. IPUP is set
C to 0 as an indicator that this has been done.
C-----
          CALL PJAC (NEQ, Y, YH, NYH, EWT, ACOR, SAVF, WM, IWM, F, JAC)
          IPUP = 0
          RC = 1.0D0
          NSLP = NST
          CRATE = 0.7D0
          IF (IERPJ .NE. 0) GO TO 430
250       DO 260 I = 1,N
260         ACOR(I) = 0.0D0
270       IF (MITER .NE. 0) GO TO 350
C-----
C In the case of functional iteration, update Y directly from
C the result of the last function evaluation.
C-----
        DO 290 I = 1,N
          SAVF(I) = H*SAVF(I) - YH(I,2)
290       Y(I) = SAVF(I) - ACOR(I)
          DEL = DVNORM (N, Y, EWT)
        DO 300 I = 1,N
          Y(I) = YH(I,1) + EL(1)*SAVF(I)
300       ACOR(I) = SAVF(I)
        GO TO 400
C-----
C In the case of the chord method, compute the corrector error,
C and solve the linear system with that as right-hand side and
C P as coefficient matrix.
C-----
350       DO 360 I = 1,N
360         Y(I) = H*SAVF(I) - (YH(I,2) + ACOR(I))
          CALL SLVS (WM, IWM, Y, SAVF)
          IF (IERSL .LT. 0) GO TO 430
          IF (IERSL .GT. 0) GO TO 410
          DEL = DVNORM (N, Y, EWT)
        DO 380 I = 1,N
          ACOR(I) = ACOR(I) + Y(I)
380       Y(I) = YH(I,1) + EL(1)*ACOR(I)
C-----
C Test for convergence. If M.gt.0, an estimate of the convergence
C rate constant is stored in CRATE, and this is used in the test.
C-----
400       IF (M .NE. 0) CRATE = MAX(0.2D0*CRATE,DEL/DELP)
          DCON = DEL*MIN(1.0D0,1.5D0*CRATE)/(TESCO(2,NQ)*CONIT)
          IF (DCON .LE. 1.0D0) GO TO 450
          M = M + 1
          IF (M .EQ. MAXCOR) GO TO 410
          IF (M .GE. 2 .AND. DEL .GT. 2.0D0*DELP) GO TO 410
          DELP = DEL
          CALL F (NEQ, TN, Y, SAVF)
          NFE = NFE + 1
          GO TO 270
C-----
C The corrector iteration failed to converge.
C If MITER .ne. 0 and the Jacobian is out of date, PJAC is called for
C the next try. Otherwise the YH array is retracted to its values
C before prediction, and H is reduced, if possible. If H cannot be
C reduced or MXNCF failures have occurred, exit with KFLAG = -2.

```

```

C-----
410 IF (MITER .EQ. 0 .OR. JCUR .EQ. 1) GO TO 430
    ICF = 1
    IPUP = MITER
    GO TO 220
430 ICF = 2
    NCF = NCF + 1
    RMAX = 2.0D0
    TN = TOLD
    I1 = NQNYH + 1
    DO 445 JB = 1,NQ
        I1 = I1 - NYH
Cdir$ ivdep
    DO 440 I = I1,NQNYH
440     YH1(I) = YH1(I) - YH1(I+NYH)
445     CONTINUE
    IF (IERPJ .LT. 0 .OR. IERSL .LT. 0) GO TO 680
    IF (ABS(H) .LE. HMIN*1.00001D0) GO TO 670
    IF (NCF .EQ. MXNCF) GO TO 670
    RH = 0.25D0
    IPUP = MITER
    IREDO = 1
    GO TO 170

C-----
C The corrector has converged. JCUR is set to 0
C to signal that the Jacobian involved may need updating later.
C The local error test is made and control passes to statement 500
C if it fails.
C-----
450 JCUR = 0
    IF (M .EQ. 0) DSM = DEL/TESCO(2,NQ)
    IF (M .GT. 0) DSM = DVNORM (N, ACOR, EWT)/TESCO(2,NQ)
    IF (DSM .GT. 1.0D0) GO TO 500

C-----
C After a successful step, update the YH array.
C Consider changing H if IALTH = 1. Otherwise decrease IALTH by 1.
C If IALTH is then 1 and NQ .lt. MAXORD, then ACOR is saved for
C use in a possible order increase on the next step.
C If a change in H is considered, an increase or decrease in order
C by one is considered also. A change in H is made only if it is by a
C factor of at least 1.1. If not, IALTH is set to 3 to prevent
C testing for that many steps.
C-----
    KFLAG = 0
    IREDO = 0
    NST = NST + 1
    HU = H
    NQU = NQ
    DO 470 J = 1,L
        DO 470 I = 1,N
470     YH(I,J) = YH(I,J) + EL(J)*ACOR(I)
    IALTH = IALTH - 1
    IF (IALTH .EQ. 0) GO TO 520
    IF (IALTH .GT. 1) GO TO 700
    IF (L .EQ. LMAX) GO TO 700
    DO 490 I = 1,N
490     YH(I,LMAX) = ACOR(I)
    GO TO 700

C-----
C The error test failed. KFLAG keeps track of multiple failures.
C Restore TN and the YH array to their previous values, and prepare
C to try the step again. Compute the optimum step size for this or
C one lower order. After 2 or more failures, H is forced to decrease
C by a factor of 0.2 or less.
C-----
500 KFLAG = KFLAG - 1
    TN = TOLD
    I1 = NQNYH + 1
    DO 515 JB = 1,NQ
        I1 = I1 - NYH
Cdir$ ivdep
    DO 510 I = I1,NQNYH
510     YH1(I) = YH1(I) - YH1(I+NYH)

```

```

515  CONTINUE
      RMAX = 2.0D0
      IF (ABS(H) .LE. HMIN*1.00001D0) GO TO 660
      IF (KFLAG .LE. -3) GO TO 640
      IREDO = 2
      RHUP = 0.0D0
      GO TO 540
C-----
C Regardless of the success or failure of the step, factors
C RHDN, RHSM, and RHUP are computed, by which H could be multiplied
C at order NQ - 1, order NQ, or order NQ + 1, respectively.
C In the case of failure, RHUP = 0.0 to avoid an order increase.
C The largest of these is determined and the new order chosen
C accordingly. If the order is to be increased, we compute one
C additional scaled derivative.
C-----
520  RHUP = 0.0D0
      IF (L .EQ. LMAX) GO TO 540
      DO 530 I = 1,N
530    SAVF(I) = ACOR(I) - YH(I,LMAX)
      DUP = DVNORM (N, SAVF, EWT)/TESCO(3,NQ)
      EXUP = 1.0D0/(L+1)
      RHUP = 1.0D0/(1.4D0*DUP**EXUP + 0.0000014D0)
540  EXSM = 1.0D0/L
      RHSM = 1.0D0/(1.2D0*EXSM**EXSM + 0.0000012D0)
      RHDN = 0.0D0
      IF (NQ .EQ. 1) GO TO 560
      DDN = DVNORM (N, YH(1,L), EWT)/TESCO(1,NQ)
      EXDN = 1.0D0/NQ
      RHDN = 1.0D0/(1.3D0*DDN**EXDN + 0.0000013D0)
560  IF (RHSM .GE. RHUP) GO TO 570
      IF (RHUP .GT. RHDN) GO TO 590
      GO TO 580
570  IF (RHSM .LT. RHDN) GO TO 580
      NEWQ = NQ
      RH = RHSM
      GO TO 620
580  NEWQ = NQ - 1
      RH = RHDN
      IF (KFLAG .LT. 0 .AND. RH .GT. 1.0D0) RH = 1.0D0
      GO TO 620
590  NEWQ = L
      RH = RHUP
      IF (RH .LT. 1.1D0) GO TO 610
      R = EL(L)/L
      DO 600 I = 1,N
600    YH(I,NEWQ+1) = ACOR(I)*R
      GO TO 630
610  IALTH = 3
      GO TO 700
620  IF ((KFLAG .EQ. 0) .AND. (RH .LT. 1.1D0)) GO TO 610
      IF (KFLAG .LE. -2) RH = MIN(RH,0.2D0)
C-----
C If there is a change of order, reset NQ, l, and the coefficients.
C In any case H is reset according to RH and the YH array is rescaled.
C Then exit from 690 if the step was OK, or redo the step otherwise.
C-----
      IF (NEWQ .EQ. NQ) GO TO 170
630  NQ = NEWQ
      L = NQ + 1
      IRET = 2
      GO TO 150
C-----
C Control reaches this section if 3 or more failures have occurred.
C If 10 failures have occurred, exit with KFLAG = -1.
C It is assumed that the derivatives that have accumulated in the
C YH array have errors of the wrong order. Hence the first
C derivative is recomputed, and the order is set to 1. Then
C H is reduced by a factor of 10, and the step is retried,
C until it succeeds or H reaches HMIN.
C-----
640  IF (KFLAG .EQ. -10) GO TO 660
      RH = 0.1D0

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```

        RH = MAX(HMIN/ABS(H),RH)
        H = H*RH
        DO 645 I = 1,N
645      Y(I) = YH(I,1)
        CALL F (NEQ, TN, Y, SAVF)
        NFE = NFE + 1
        DO 650 I = 1,N
650      YH(I,2) = H*SAVF(I)
        IPUP = MITER
        IALTH = 5
        IF (NQ .EQ. 1) GO TO 200
        NQ = 1
        L = 2
        IRET = 3
        GO TO 150
C-----
C All returns are made through this section.  H is saved in HOLD
C to allow the caller to change H on the next step.
C-----
660      KFLAG = -1
        GO TO 720
670      KFLAG = -2
        GO TO 720
680      KFLAG = -3
        GO TO 720
690      RMAX = 10.0D0
700      R = 1.0D0/TESCO(2,NQU)
        DO 710 I = 1,N
710      ACOR(I) = ACOR(I)*R
720      HOLD = H
        JSTART = 1
        RETURN
C----- END OF SUBROUTINE DSTODE -----
        END
*DECK DEWSET
        SUBROUTINE DEWSET (N, ITOL, RTOL, ATOL, YCUR, EWT)
C***BEGIN PROLOGUE  DEWSET
C***SUBSIDIARY
C***PURPOSE  Set error weight vector.
C***TYPE      DOUBLE PRECISION (SEWSET-S, DEWSET-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  This subroutine sets the error weight vector EWT according to
C      EWT(i) = RTOL(i)*ABS(YCUR(i)) + ATOL(i),  i = 1,...,N,
C  with the subscript on RTOL and/or ATOL possibly replaced by 1 above,
C  depending on the value of ITOL.
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions.  (ACH)
C***END PROLOGUE  DEWSET
C**End
        INTEGER N, ITOL
        INTEGER I
        DOUBLE PRECISION RTOL, ATOL, YCUR, EWT
        DIMENSION RTOL(*), ATOL(*), YCUR(N), EWT(N)
C
C***FIRST EXECUTABLE STATEMENT  DEWSET
        GO TO (10, 20, 30, 40), ITOL
10      CONTINUE
        DO 15 I = 1,N
15      EWT(I) = RTOL(1)*ABS(YCUR(I)) + ATOL(1)
        RETURN
20      CONTINUE
        DO 25 I = 1,N
25      EWT(I) = RTOL(1)*ABS(YCUR(I)) + ATOL(I)
        RETURN
30      CONTINUE

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      DO 35 I = 1,N
35      EWT(I) = RTOL(I)*ABS(YCUR(I)) + ATOL(1)
      RETURN
40      CONTINUE
      DO 45 I = 1,N
45      EWT(I) = RTOL(I)*ABS(YCUR(I)) + ATOL(I)
      RETURN
C----- END OF SUBROUTINE DEWSET -----
      END
*DECK DVNORM
      DOUBLE PRECISION FUNCTION DVNORM (N, V, W)
C***BEGIN PROLOGUE  DVNORM
C***SUBSIDIARY
C***PURPOSE  Weighted root-mean-square vector norm.
C***TYPE      DOUBLE PRECISION (SVNORM-S, DVNORM-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  This function routine computes the weighted root-mean-square norm
C  of the vector of length N contained in the array V, with weights
C  contained in the array W of length N:
C    DVNORM = SQRT( (1/N) * SUM( V(i)*W(i) )**2 )
C
C***SEE ALSO  DLSODE
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YYMMDD)
C   791129  DATE WRITTEN
C   890501  Modified prologue to SLATEC/LDOC format.  (FNF)
C   890503  Minor cosmetic changes.  (FNF)
C   930809  Renamed to allow single/double precision versions. (ACH)
C***END PROLOGUE  DVNORM
C**End
      INTEGER N, I
      DOUBLE PRECISION V, W, SUM
      DIMENSION V(N), W(N)
C
C***FIRST EXECUTABLE STATEMENT  DVNORM
      SUM = 0.0D0
      DO 10 I = 1,N
10      SUM = SUM + (V(I)*W(I))**2
      DVNORM = SQRT(SUM/N)
      RETURN
C----- END OF FUNCTION DVNORM -----
      END
*DECK DGEFA
      SUBROUTINE DGEFA (A, LDA, N, IPV, INFO)
C***BEGIN PROLOGUE  DGEFA
C***PURPOSE  Factor a matrix using Gaussian elimination.
C***CATEGORY  D2A1
C***TYPE      DOUBLE PRECISION (SGEFA-S, DGEFA-D, CGEFA-C)
C***KEYWORDS  GENERAL MATRIX, LINEAR ALGEBRA, LINPACK,
C              MATRIX FACTORIZATION
C***AUTHOR  Moler, C. B., (U. of New Mexico)
C***DESCRIPTION
C
C  DGEFA factors a double precision matrix by Gaussian elimination.
C
C  DGEFA is usually called by DGECC, but it can be called
C  directly with a saving in time if RCOND is not needed.
C  (Time for DGECC) = (1 + 9/N)*(Time for DGEFA) .
C
C  On Entry
C
C    A      DOUBLE PRECISION(LDA, N)
C            the matrix to be factored.
C
C    LDA    INTEGER
C            the leading dimension of the array A .
C
C    N      INTEGER
C            the order of the matrix A .
C
C  On Return

```

```

C
C      A      an upper triangular matrix and the multipliers
C              which were used to obtain it.
C              The factorization can be written  $A = L*U$  where
C              L is a product of permutation and unit lower
C              triangular matrices and U is upper triangular.
C
C      IPVT    INTEGER(N)
C              an integer vector of pivot indices.
C
C      INFO    INTEGER
C              = 0 normal value.
C              = K if  $U(K,K) \text{ .EQ. } 0.0$  . This is not an error
C                  condition for this subroutine, but it does
C                  indicate that DGESL or DGEDI will divide by zero
C                  if called. Use RCOND in DGECCO for a reliable
C                  indication of singularity.
C
C***REFERENCES J. J. Dongarra, J. R. Bunch, C. B. Moler, and G. W.
C              Stewart, LINPACK Users' Guide, SIAM, 1979.
C***ROUTINES CALLED DAXPY, DSCAL, IDAMAX
C***REVISION HISTORY (YMMDD)
C      780814 DATE WRITTEN
C      890831 Modified array declarations. (WRB)
C      890831 REVISION DATE from Version 3.2
C      891214 Prologue converted to Version 4.0 format. (BAB)
C      900326 Removed duplicate information from DESCRIPTION section.
C              (WRB)
C      920501 Reformatted the REFERENCES section. (WRB)
C***END PROLOGUE DGEFA
      INTEGER LDA,N,IPVT(*),INFO
      DOUBLE PRECISION A(LDA,*)
C
      DOUBLE PRECISION T
      INTEGER IDAMAX,J,K,KP1,L,NM1
C
      GAUSSIAN ELIMINATION WITH PARTIAL PIVOTING
C
C***FIRST EXECUTABLE STATEMENT DGEFA
      INFO = 0
      NM1 = N - 1
      IF (NM1 .LT. 1) GO TO 70
      DO 60 K = 1, NM1
        KP1 = K + 1
C
C        FIND L = PIVOT INDEX
C
C        L = IDAMAX(N-K+1,A(K,K),1) + K - 1
C        IPVT(K) = L
C
C        ZERO PIVOT IMPLIES THIS COLUMN ALREADY TRIANGULARIZED
C
C        IF (A(L,K) .EQ. 0.0D0) GO TO 40
C
C        INTERCHANGE IF NECESSARY
C
C        IF (L .EQ. K) GO TO 10
C        T = A(L,K)
C        A(L,K) = A(K,K)
C        A(K,K) = T
10      CONTINUE
C
C      COMPUTE MULTIPLIERS
C
C      T = -1.0D0/A(K,K)
C      CALL DSCAL(N-K,T,A(K+1,K),1)
C
C      ROW ELIMINATION WITH COLUMN INDEXING
C
C      DO 30 J = KP1, N
C        T = A(L,J)
C        IF (L .EQ. K) GO TO 20
C        A(L,J) = A(K,J)

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        A(K,J) = T
20      CONTINUE
        CALL DAXPY(N-K,T,A(K+1,K),1,A(K+1,J),1)
30      CONTINUE
        GO TO 50
40      CONTINUE
        INFO = K
50      CONTINUE
60      CONTINUE
70      CONTINUE
        IPVT(N) = N
        IF (A(N,N) .EQ. 0.0D0) INFO = N
        RETURN
        END
*DECK DGESL
        SUBROUTINE DGESL (A, LDA, N, IPVT, B, JOB)
C***BEGIN PROLOGUE  DGESL
C***PURPOSE        Solve the real system A*X=B or TRANS(A)*X=B using the
C                   factors computed by DGECCO or DGEFA.
C***CATEGORY       D2A1
C***TYPE           DOUBLE PRECISION (SGESL-S, DGESL-D, CGESL-C)
C***KEYWORDS       LINEAR ALGEBRA, LINPACK, MATRIX, SOLVE
C***AUTHOR         Moler, C. B., (U. of New Mexico)
C***DESCRIPTION
C
C   DGESL solves the double precision system
C   A * X = B  or  TRANS(A) * X = B
C   using the factors computed by DGECCO or DGEFA.
C
C   On Entry
C
C       A       DOUBLE PRECISION(LDA, N)
C               the output from DGECCO or DGEFA.
C
C       LDA     INTEGER
C               the leading dimension of the array  A .
C
C       N       INTEGER
C               the order of the matrix  A .
C
C       IPVT    INTEGER(N)
C               the pivot vector from DGECCO or DGEFA.
C
C       B       DOUBLE PRECISION(N)
C               the right hand side vector.
C
C       JOB     INTEGER
C               = 0      to solve  A*X = B ,
C               = nonzero to solve TRANS(A)*X = B  where
C                       TRANS(A) is the transpose.
C
C   On Return
C
C       B       the solution vector  X .
C
C   Error Condition
C
C       A division by zero will occur if the input factor contains a
C       zero on the diagonal.  Technically this indicates singularity
C       but it is often caused by improper arguments or improper
C       setting of LDA .  It will not occur if the subroutines are
C       called correctly and if DGECCO has set RCOND .GT. 0.0
C       or DGEFA has set INFO .EQ. 0 .
C
C   To compute INVERSE(A) * C  where  C  is a matrix
C   with  P  columns
C       CALL DGECCO(A,LDA,N,IPVT,RCOND,Z)
C       IF (RCOND is too small) GO TO ...
C       DO 10 J = 1, P
C           CALL DGESL(A,LDA,N,IPVT,C(1,J),0)
C       10 CONTINUE
C
C***REFERENCES      J. J. Dongarra, J. R. Bunch, C. B. Moler, and G. W.

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C          Stewart, LINPACK Users' Guide, SIAM, 1979.
C***ROUTINES CALLED  DAXPY, DDOT
C***REVISION HISTORY  (YYMMDD)
C   780814  DATE WRITTEN
C   890831  Modified array declarations.  (WRB)
C   890831  REVISION DATE from Version 3.2
C   891214  Prologue converted to Version 4.0 format.  (BAB)
C   900326  Removed duplicate information from DESCRIPTION section.
C          (WRB)
C   920501  Reformatted the REFERENCES section.  (WRB)
C***END PROLOGUE  DGESL
      INTEGER LDA,N,IPVT(*),JOB
      DOUBLE PRECISION A(LDA,*),B(*)

C
      DOUBLE PRECISION DDOT,T
      INTEGER K,KB,L,NM1
C***FIRST EXECUTABLE STATEMENT  DGESL
      NM1 = N - 1
      IF (JOB .NE. 0) GO TO 50

C
C      JOB = 0 , SOLVE  A * X = B
C      FIRST SOLVE  L*Y = B
C
      IF (NM1 .LT. 1) GO TO 30
      DO 20 K = 1, NM1
          L = IPVT(K)
          T = B(L)
          IF (L .EQ. K) GO TO 10
          B(L) = B(K)
          B(K) = T
10      CONTINUE
          CALL DAXPY(N-K,T,A(K+1,K),1,B(K+1),1)
20      CONTINUE
30      CONTINUE

C
C      NOW SOLVE  U*X = Y
C
      DO 40 KB = 1, N
          K = N + 1 - KB
          B(K) = B(K)/A(K,K)
          T = -B(K)
          CALL DAXPY(K-1,T,A(1,K),1,B(1),1)
40      CONTINUE
      GO TO 100
50 CONTINUE

C
C      JOB = NONZERO, SOLVE  TRANS(A) * X = B
C      FIRST SOLVE  TRANS(U)*Y = B
C
      DO 60 K = 1, N
          T = DDOT(K-1,A(1,K),1,B(1),1)
          B(K) = (B(K) - T)/A(K,K)
60      CONTINUE

C
C      NOW SOLVE TRANS(L)*X = Y
C
      IF (NM1 .LT. 1) GO TO 90
      DO 80 KB = 1, NM1
          K = N - KB
          B(K) = B(K) + DDOT(N-K,A(K+1,K),1,B(K+1),1)
          L = IPVT(K)
          IF (L .EQ. K) GO TO 70
          T = B(L)
          B(L) = B(K)
          B(K) = T
70      CONTINUE
80      CONTINUE
90      CONTINUE
100 CONTINUE
      RETURN
      END
*DECK DGBFA
      SUBROUTINE DGBFA (ABD, LDA, N, ML, MU, IPVT, INFO)

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C***BEGIN PROLOGUE  DGBFA
C***PURPOSE  Factor a band matrix using Gaussian elimination.
C***CATEGORY  D2A2
C***TYPE      DOUBLE PRECISION (SGBFA-S, DGBFA-D, CGBFA-C)
C***KEYWORDS  BANDED, LINEAR ALGEBRA, LINPACK, MATRIX FACTORIZATION
C***AUTHOR  Moler, C. B., (U. of New Mexico)
C***DESCRIPTION
C
C      DGBFA factors a double precision band matrix by elimination.
C
C      DGBFA is usually called by DGBCO, but it can be called
C      directly with a saving in time if RCOND is not needed.
C
C      On Entry
C
C          ABD      DOUBLE PRECISION(LDA, N)
C                   contains the matrix in band storage. The columns
C                   of the matrix are stored in the columns of ABD and
C                   the diagonals of the matrix are stored in rows
C                   ML+1 through 2*ML+MU+1 of ABD .
C                   See the comments below for details.
C
C          LDA      INTEGER
C                   the leading dimension of the array ABD .
C                   LDA must be .GE. 2*ML + MU + 1 .
C
C          N        INTEGER
C                   the order of the original matrix.
C
C          ML        INTEGER
C                   number of diagonals below the main diagonal.
C                   0 .LE. ML .LT. N .
C
C          MU        INTEGER
C                   number of diagonals above the main diagonal.
C                   0 .LE. MU .LT. N .
C                   More efficient if ML .LE. MU .
C
C      On Return
C
C          ABD      an upper triangular matrix in band storage and
C                   the multipliers which were used to obtain it.
C                   The factorization can be written  $A = L*U$  where
C                   L is a product of permutation and unit lower
C                   triangular matrices and U is upper triangular.
C
C          IPVT      INTEGER(N)
C                   an integer vector of pivot indices.
C
C          INFO      INTEGER
C                   = 0 normal value.
C                   = K if  $U(K,K) \leq 0.0$  . This is not an error
C                   condition for this subroutine, but it does
C                   indicate that DGBSL will divide by zero if
C                   called. Use RCOND in DGBCO for a reliable
C                   indication of singularity.
C
C      Band Storage
C
C      If A is a band matrix, the following program segment
C      will set up the input.
C
C          ML = (band width below the diagonal)
C          MU = (band width above the diagonal)
C          M = ML + MU + 1
C          DO 20 J = 1, N
C              I1 = MAX(1, J-MU)
C              I2 = MIN(N, J+ML)
C              DO 10 I = I1, I2
C                  K = I - J + M
C                  ABD(K,J) = A(I,J)
C              10 CONTINUE
C          20 CONTINUE

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C      This uses rows ML+1 through 2*ML+MU+1 of ABD .
C      In addition, the first ML rows in ABD are used for
C      elements generated during the triangularization.
C      The total number of rows needed in ABD is 2*ML+MU+1 .
C      The ML+MU by ML+MU upper left triangle and the
C      ML by ML lower right triangle are not referenced.
C
C***REFERENCES  J. J. Dongarra, J. R. Bunch, C. B. Moler, and G. W.
C                Stewart, LINPACK Users' Guide, SIAM, 1979.
C***ROUTINES CALLED  DAXPY, DSCAL, IDAMAX
C***REVISION HISTORY  (YYMMDD)
C   780814  DATE WRITTEN
C   890531  Changed all specific intrinsics to generic.  (WRB)
C   890831  Modified array declarations.  (WRB)
C   890831  REVISION DATE from Version 3.2
C   891214  Prologue converted to Version 4.0 format.  (BAB)
C   900326  Removed duplicate information from DESCRIPTION section.
C           (WRB)
C   920501  Reformatted the REFERENCES section.  (WRB)
C***END PROLOGUE  DGBFA
      INTEGER LDA,N,ML,MU,IPVT(*),INFO
      DOUBLE PRECISION ABD(LDA,*)

C
      DOUBLE PRECISION T
      INTEGER I,IDAMAX,I0,J,JU,JZ,J0,J1,K,KP1,L,LM,M,MM,NM1
C
C***FIRST EXECUTABLE STATEMENT  DGBFA
      M = ML + MU + 1
      INFO = 0

C
C      ZERO INITIAL FILL-IN COLUMNS
C
      J0 = MU + 2
      J1 = MIN(N,M) - 1
      IF (J1 .LT. J0) GO TO 30
      DO 20 JZ = J0, J1
         I0 = M + 1 - JZ
         DO 10 I = I0, ML
            ABD(I,JZ) = 0.0D0
10      CONTINUE
20      CONTINUE
30      CONTINUE
      JZ = J1
      JU = 0

C
C      GAUSSIAN ELIMINATION WITH PARTIAL PIVOTING
C
      NM1 = N - 1
      IF (NM1 .LT. 1) GO TO 130
      DO 120 K = 1, NM1
         KP1 = K + 1

C
C      ZERO NEXT FILL-IN COLUMN
C
      JZ = JZ + 1
      IF (JZ .GT. N) GO TO 50
      IF (ML .LT. 1) GO TO 50
      DO 40 I = 1, ML
         ABD(I,JZ) = 0.0D0
40      CONTINUE
50      CONTINUE

C
C      FIND L = PIVOT INDEX
C
      LM = MIN(ML,N-K)
      L = IDAMAX(LM+1,ABD(M,K),1) + M - 1
      IPVT(K) = L + K - M

C
C      ZERO PIVOT IMPLIES THIS COLUMN ALREADY TRIANGULARIZED
C
      IF (ABD(L,K) .EQ. 0.0D0) GO TO 100

C
C      INTERCHANGE IF NECESSARY

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C      IF (L .EQ. M) GO TO 60
C      T = ABD(L,K)
C      ABD(L,K) = ABD(M,K)
C      ABD(M,K) = T
60     CONTINUE
C
C      COMPUTE MULTIPLIERS
C
C      T = -1.0D0/ABD(M,K)
C      CALL DSCAL(LM,T,ABD(M+1,K),1)
C
C      ROW ELIMINATION WITH COLUMN INDEXING
C
C      JU = MIN(MAX(JU,MU+IPVT(K)),N)
C      MM = M
C      IF (JU .LT. KP1) GO TO 90
C      DO 80 J = KP1, JU
C      L = L - 1
C      MM = MM - 1
C      T = ABD(L,J)
C      IF (L .EQ. MM) GO TO 70
C      ABD(L,J) = ABD(MM,J)
C      ABD(MM,J) = T
70     CONTINUE
C      CALL DAXPY(LM,T,ABD(M+1,K),1,ABD(MM+1,J),1)
80     CONTINUE
90     CONTINUE
C      GO TO 110
100    CONTINUE
C      INFO = K
110    CONTINUE
120    CONTINUE
130    CONTINUE
C      IPVT(N) = N
C      IF (ABD(M,N) .EQ. 0.0D0) INFO = N
C      RETURN
C      END
*DECK DGBSL
SUBROUTINE DGBSL (ABD, LDA, N, ML, MU, IPVT, B, JOB)
C***BEGIN PROLOGUE DGBSL
C***PURPOSE Solve the real band system A*X=B or TRANS(A)*X=B using
C      the factors computed by DGBCO or DGBFA.
C***CATEGORY D2A2
C***TYPE DOUBLE PRECISION (SGBSL-S, DGBSL-D, CGBSL-C)
C***KEYWORDS BANDED, LINEAR ALGEBRA, LINPACK, MATRIX, SOLVE
C***AUTHOR Moler, C. B., (U. of New Mexico)
C***DESCRIPTION
C
C      DGBSL solves the double precision band system
C      A * X = B or TRANS(A) * X = B
C      using the factors computed by DGBCO or DGBFA.
C
C      On Entry
C
C      ABD      DOUBLE PRECISION(LDA, N)
C               the output from DGBCO or DGBFA.
C
C      LDA      INTEGER
C               the leading dimension of the array ABD .
C
C      N        INTEGER
C               the order of the original matrix.
C
C      ML       INTEGER
C               number of diagonals below the main diagonal.
C
C      MU       INTEGER
C               number of diagonals above the main diagonal.
C
C      IPVT     INTEGER(N)
C               the pivot vector from DGBCO or DGBFA.

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C      B      DOUBLE PRECISION(N)
C      the right hand side vector.
C
C      JOB      INTEGER
C      = 0      to solve  $A \cdot X = B$  ,
C      = nonzero to solve  $TRANS(A) \cdot X = B$  , where
C      TRANS(A) is the transpose.
C
C      On Return
C
C      B      the solution vector X .
C
C      Error Condition
C
C      A division by zero will occur if the input factor contains a
C      zero on the diagonal. Technically this indicates singularity
C      but it is often caused by improper arguments or improper
C      setting of LDA . It will not occur if the subroutines are
C      called correctly and if DGBCO has set RCOND .GT. 0.0
C      or DGBFA has set INFO .EQ. 0 .
C
C      To compute  $INVERSE(A) \cdot C$  where C is a matrix
C      with P columns
C      CALL DGBCO(ABD,LDA,N,ML,MU,IPVT,RCOND,Z)
C      IF (RCOND is too small) GO TO ...
C      DO 10 J = 1, P
C      CALL DGBSL(ABD,LDA,N,ML,MU,IPVT,C(1,J),0)
C      10 CONTINUE
C
C***REFERENCES J. J. Dongarra, J. R. Bunch, C. B. Moler, and G. W.
C      Stewart, LINPACK Users' Guide, SIAM, 1979.
C***ROUTINES CALLED DAXPY, DDOT
C***REVISION HISTORY (YMMDD)
C      780814 DATE WRITTEN
C      890531 Changed all specific intrinsics to generic. (WRB)
C      890831 Modified array declarations. (WRB)
C      890831 REVISION DATE from Version 3.2
C      891214 Prologue converted to Version 4.0 format. (BAB)
C      900326 Removed duplicate information from DESCRIPTION section.
C      (WRB)
C      920501 Reformatted the REFERENCES section. (WRB)
C***END PROLOGUE DGBSL
C      INTEGER LDA,N,ML,MU,IPVT(*),JOB
C      DOUBLE PRECISION ABD(LDA,*),B(*)
C
C      DOUBLE PRECISION DDOT,T
C      INTEGER K,KB,L,LA,LB,LM,M,NM1
C***FIRST EXECUTABLE STATEMENT DGBSL
C      M = MU + ML + 1
C      NM1 = N - 1
C      IF (JOB .NE. 0) GO TO 50
C
C      JOB = 0 , SOLVE  $A \cdot X = B$ 
C      FIRST SOLVE  $L \cdot Y = B$ 
C
C      IF (ML .EQ. 0) GO TO 30
C      IF (NM1 .LT. 1) GO TO 30
C      DO 20 K = 1, NM1
C      LM = MIN(ML,N-K)
C      L = IPVT(K)
C      T = B(L)
C      IF (L .EQ. K) GO TO 10
C      B(L) = B(K)
C      B(K) = T
C      10 CONTINUE
C      CALL DAXPY(LM,T,ABD(M+1,K),1,B(K+1),1)
C      20 CONTINUE
C      30 CONTINUE
C
C      NOW SOLVE  $U \cdot X = Y$ 
C
C      DO 40 KB = 1, N
C      K = N + 1 - KB

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        B(K) = B(K)/ABD(M,K)
        LM = MIN(K,M) - 1
        LA = M - LM
        LB = K - LM
        T = -B(K)
        CALL DAXPY(LM,T,ABD(LA,K),1,B(LB),1)
40     CONTINUE
        GO TO 100
50     CONTINUE
C
C     JOB = NONZERO, SOLVE TRANS(A) * X = B
C     FIRST SOLVE TRANS(U)*Y = B
C
        DO 60 K = 1, N
            LM = MIN(K,M) - 1
            LA = M - LM
            LB = K - LM
            T = DDOT(LM,ABD(LA,K),1,B(LB),1)
            B(K) = (B(K) - T)/ABD(M,K)
60     CONTINUE
C
C     NOW SOLVE TRANS(L)*X = Y
C
        IF (ML .EQ. 0) GO TO 90
        IF (NM1 .LT. 1) GO TO 90
        DO 80 KB = 1, NM1
            K = N - KB
            LM = MIN(ML,N-K)
            B(K) = B(K) + DDOT(LM,ABD(M+1,K),1,B(K+1),1)
            L = IPVT(K)
            IF (L .EQ. K) GO TO 70
            T = B(L)
            B(L) = B(K)
            B(K) = T
70         CONTINUE
80     CONTINUE
90     CONTINUE
100    CONTINUE
        RETURN
        END
*DECK DAXPY
        SUBROUTINE DAXPY (N, DA, DX, INCX, DY, INCY)
C***BEGIN PROLOGUE DAXPY
C***PURPOSE Compute a constant times a vector plus a vector.
C***CATEGORY D1A7
C***TYPE DOUBLE PRECISION (SAXPY-S, DAXPY-D, CAXPY-C)
C***KEYWORDS BLAS, LINEAR ALGEBRA, TRIAD, VECTOR
C***AUTHOR Lawson, C. L., (JPL)
C           Hanson, R. J., (SNLA)
C           Kincaid, D. R., (U. of Texas)
C           Krogh, F. T., (JPL)
C***DESCRIPTION
C
C           B L A S Subprogram
C     Description of Parameters
C
C     --Input--
C     N number of elements in input vector(s)
C     DA double precision scalar multiplier
C     DX double precision vector with N elements
C     INCX storage spacing between elements of DX
C     DY double precision vector with N elements
C     INCY storage spacing between elements of DY
C
C     --Output--
C     DY double precision result (unchanged if N .LE. 0)
C
C     Overwrite double precision DY with double precision DA*DX + DY.
C     For I = 0 to N-1, replace DY(LY+I*INCY) with DA*DX(LX+I*INCX) +
C     DY(LY+I*INCY),
C     where LX = 1 if INCX .GE. 0, else LX = 1+(1-N)*INCX, and LY is
C     defined in a similar way using INCY.
C

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C***REFERENCES  C. L. Lawson, R. J. Hanson, D. R. Kincaid and F. T.
C                Krogh, Basic linear algebra subprograms for Fortran
C                usage, Algorithm No. 539, Transactions on Mathematical
C                Software 5, 3 (September 1979), pp. 308-323.
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YYMMDD)
C   791001  DATE WRITTEN
C   890831  Modified array declarations.  (WRB)
C   890831  REVISION DATE from Version 3.2
C   891214  Prologue converted to Version 4.0 format.  (BAB)
C   920310  Corrected definition of LX in DESCRIPTION.  (WRB)
C   920501  Reformatted the REFERENCES section.  (WRB)
C***END PROLOGUE  DAXPY
      DOUBLE PRECISION DX(*), DY(*), DA
C***FIRST EXECUTABLE STATEMENT  DAXPY
      IF (N.LE.0 .OR. DA.EQ.0.0D0) RETURN
      IF (INCX .EQ. INCY) IF (INCX-1) 5,20,60

C
C      Code for unequal or nonpositive increments.
C
      5 IX = 1
      IY = 1
      IF (INCX .LT. 0) IX = (-N+1)*INCX + 1
      IF (INCY .LT. 0) IY = (-N+1)*INCY + 1
      DO 10 I = 1,N
          DY(IY) = DY(IY) + DA*DX(IX)
          IX = IX + INCX
          IY = IY + INCY
      10 CONTINUE
      RETURN

C
C      Code for both increments equal to 1.
C
C      Clean-up loop so remaining vector length is a multiple of 4.
C
      20 M = MOD(N,4)
      IF (M .EQ. 0) GO TO 40
      DO 30 I = 1,M
          DY(I) = DY(I) + DA*DX(I)
      30 CONTINUE
      IF (N .LT. 4) RETURN
      40 MP1 = M + 1
      DO 50 I = MP1,N,4
          DY(I) = DY(I) + DA*DX(I)
          DY(I+1) = DY(I+1) + DA*DX(I+1)
          DY(I+2) = DY(I+2) + DA*DX(I+2)
          DY(I+3) = DY(I+3) + DA*DX(I+3)
      50 CONTINUE
      RETURN

C
C      Code for equal, positive, non-unit increments.
C
      60 NS = N*INCX
      DO 70 I = 1,NS,INCX
          DY(I) = DA*DX(I) + DY(I)
      70 CONTINUE
      RETURN
      END

*DECK DDOT
      DOUBLE PRECISION FUNCTION DDOT (N, DX, INCX, DY, INCY)
C***BEGIN PROLOGUE  DDOT
C***PURPOSE  Compute the inner product of two vectors.
C***CATEGORY  D1A4
C***TYPE      DOUBLE PRECISION (SDOT-S, DDOT-D, CDOTU-C)
C***KEYWORDS  BLAS, INNER PRODUCT, LINEAR ALGEBRA, VECTOR
C***AUTHOR  Lawson, C. L., (JPL)
C            Hanson, R. J., (SNLA)
C            Kincaid, D. R., (U. of Texas)
C            Krogh, F. T., (JPL)
C***DESCRIPTION
C
C            B L A S  Subprogram
C      Description of Parameters

```

```

C
C  --Input--
C      N  number of elements in input vector(s)
C      DX  double precision vector with N elements
C  INCX  storage spacing between elements of DX
C      DY  double precision vector with N elements
C  INCY  storage spacing between elements of DY
C
C  --Output--
C  DDOT  double precision dot product (zero if N .LE. 0)
C
C  Returns the dot product of double precision DX and DY.
C  DDOT = sum for I = 0 to N-1 of DX(LX+I*INCX) * DY(LY+I*INCY),
C  where LX = 1 if INCX .GE. 0, else LX = 1+(1-N)*INCX, and LY is
C  defined in a similar way using INCY.
C
C***REFERENCES  C. L. Lawson, R. J. Hanson, D. R. Kincaid and F. T.
C                Krogh, Basic linear algebra subprograms for Fortran
C                usage, Algorithm No. 539, Transactions on Mathematical
C                Software 5, 3 (September 1979), pp. 308-323.
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C   791001  DATE WRITTEN
C   890831  Modified array declarations.  (WRB)
C   890831  REVISION DATE from Version 3.2
C   891214  Prologue converted to Version 4.0 format.  (BAB)
C   920310  Corrected definition of LX in DESCRIPTION.  (WRB)
C   920501  Reformatted the REFERENCES section.  (WRB)
C***END PROLOGUE  DDOT
      DOUBLE PRECISION DX(*), DY(*)
C***FIRST EXECUTABLE STATEMENT  DDOT
      DDOT = 0.0D0
      IF (N .LE. 0) RETURN
      IF (INCX .EQ. INCY) IF (INCX-1) 5,20,60
C
C      Code for unequal or nonpositive increments.
C
      5  IX = 1
         IY = 1
         IF (INCX .LT. 0) IX = (-N+1)*INCX + 1
         IF (INCY .LT. 0) IY = (-N+1)*INCY + 1
         DO 10 I = 1,N
            DDOT = DDOT + DX(IX)*DY(IY)
            IX = IX + INCX
            IY = IY + INCY
      10 CONTINUE
         RETURN
C
C      Code for both increments equal to 1.
C
C      Clean-up loop so remaining vector length is a multiple of 5.
C
      20 M = MOD(N,5)
         IF (M .EQ. 0) GO TO 40
         DO 30 I = 1,M
            DDOT = DDOT + DX(I)*DY(I)
      30 CONTINUE
         IF (N .LT. 5) RETURN
      40 MP1 = M + 1
         DO 50 I = MP1,N,5
            DDOT = DDOT + DX(I)*DY(I) + DX(I+1)*DY(I+1) + DX(I+2)*DY(I+2) +
            1      DX(I+3)*DY(I+3) + DX(I+4)*DY(I+4)
      50 CONTINUE
         RETURN
C
C      Code for equal, positive, non-unit increments.
C
      60 NS = N*INCX
         DO 70 I = 1,NS,INCX
            DDOT = DDOT + DX(I)*DY(I)
      70 CONTINUE
         RETURN
      END

```

```

*DECK DSCAL
      SUBROUTINE DSCAL (N, DA, DX, INCX)
C***BEGIN PROLOGUE  DSCAL
C***PURPOSE  Multiply a vector by a constant.
C***CATEGORY  D1A6
C***TYPE      DOUBLE PRECISION (SSCAL-S, DSCAL-D, CSCAL-C)
C***KEYWORDS  BLAS, LINEAR ALGEBRA, SCALE, VECTOR
C***AUTHOR  Lawson, C. L., (JPL)
C           Hanson, R. J., (SNLA)
C           Kincaid, D. R., (U. of Texas)
C           Krogh, F. T., (JPL)
C***DESCRIPTION
C
C           B L A S  Subprogram
C   Description of Parameters
C
C   --Input--
C       N  number of elements in input vector(s)
C       DA  double precision scale factor
C       DX  double precision vector with N elements
C   INCX  storage spacing between elements of DX
C
C   --Output--
C       DX  double precision result (unchanged if N.LE.0)
C
C   Replace double precision DX by double precision DA*DX.
C   For I = 0 to N-1, replace DX(IX+I*INCX) with  DA * DX(IX+I*INCX),
C   where IX = 1 if INCX .GE. 0, else IX = 1+(1-N)*INCX.
C
C***REFERENCES  C. L. Lawson, R. J. Hanson, D. R. Kincaid and F. T.
C               Krogh, Basic linear algebra subprograms for Fortran
C               usage, Algorithm No. 539, Transactions on Mathematical
C               Software 5, 3 (September 1979), pp. 308-323.
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YYMMDD)
C   791001  DATE WRITTEN
C   890831  Modified array declarations.  (WRB)
C   890831  REVISION DATE from Version 3.2
C   891214  Prologue converted to Version 4.0 format.  (BAB)
C   900821  Modified to correct problem with a negative increment.
C           (WRB)
C   920501  Reformatted the REFERENCES section.  (WRB)
C***END PROLOGUE  DSCAL
      DOUBLE PRECISION DA, DX(*)
      INTEGER I, INCX, IX, M, MP1, N
C***FIRST EXECUTABLE STATEMENT  DSCAL
      IF (N .LE. 0) RETURN
      IF (INCX .EQ. 1) GOTO 20
C
C   Code for increment not equal to 1.
C
      IX = 1
      IF (INCX .LT. 0) IX = (-N+1)*INCX + 1
      DO 10 I = 1,N
          DX(IX) = DA*DX(IX)
          IX = IX + INCX
10  CONTINUE
      RETURN
C
C   Code for increment equal to 1.
C
C   Clean-up loop so remaining vector length is a multiple of 5.
C
20  M = MOD(N,5)
      IF (M .EQ. 0) GOTO 40
      DO 30 I = 1,M
          DX(I) = DA*DX(I)
30  CONTINUE
      IF (N .LT. 5) RETURN
40  MP1 = M + 1
      DO 50 I = MP1,N,5
          DX(I) = DA*DX(I)
          DX(I+1) = DA*DX(I+1)

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        DX(I+2) = DA*DX(I+2)
        DX(I+3) = DA*DX(I+3)
        DX(I+4) = DA*DX(I+4)
50 CONTINUE
    RETURN
END
*DECK IDAMAX
    INTEGER FUNCTION IDAMAX (N, DX, INCX)
C***BEGIN PROLOGUE  IDAMAX
C***PURPOSE  Find the smallest index of that component of a vector
C             having the maximum magnitude.
C***CATEGORY  D1A2
C***TYPE      DOUBLE PRECISION (ISAMAX-S, IDAMAX-D, ICAMAX-C)
C***KEYWORDS  BLAS, LINEAR ALGEBRA, MAXIMUM COMPONENT, VECTOR
C***AUTHOR  Lawson, C. L., (JPL)
C            Hanson, R. J., (SNLA)
C            Kincaid, D. R., (U. of Texas)
C            Krogh, F. T., (JPL)
C***DESCRIPTION
C
C            B L A S  Subprogram
C            Description of Parameters
C
C            --Input--
C            N  number of elements in input vector(s)
C            DX  double precision vector with N elements
C            INCX  storage spacing between elements of DX
C
C            --Output--
C            IDAMAX  smallest index (zero if N .LE. 0)
C
C            Find smallest index of maximum magnitude of double precision DX.
C            IDAMAX = first I, I = 1 to N, to maximize ABS(DX(IX+(I-1)*INCX)),
C            where IX = 1 if INCX .GE. 0, else IX = 1+(1-N)*INCX.
C
C***REFERENCES  C. L. Lawson, R. J. Hanson, D. R. Kincaid and F. T.
C                Krogh, Basic linear algebra subprograms for Fortran
C                usage, Algorithm No. 539, Transactions on Mathematical
C                Software 5, 3 (September 1979), pp. 308-323.
C***ROUTINES CALLED  (NONE)
C***REVISION HISTORY  (YMMDD)
C   791001  DATE WRITTEN
C   890531  Changed all specific intrinsics to generic.  (WRB)
C   890531  REVISION DATE from Version 3.2
C   891214  Prologue converted to Version 4.0 format.  (BAB)
C   900821  Modified to correct problem with a negative increment.
C           (WRB)
C   920501  Reformatted the REFERENCES section.  (WRB)
C***END PROLOGUE  IDAMAX
        DOUBLE PRECISION DX(*), DMAX, XMAG
        INTEGER I, INCX, IX, N
C***FIRST EXECUTABLE STATEMENT  IDAMAX
        IDAMAX = 0
        IF (N .LE. 0) RETURN
        IDAMAX = 1
        IF (N .EQ. 1) RETURN
C
        IF (INCX .EQ. 1) GOTO 20
C
        Code for increments not equal to 1.
C
        IX = 1
        IF (INCX .LT. 0) IX = (-N+1)*INCX + 1
        DMAX = ABS(DX(IX))
        IX = IX + INCX
        DO 10 I = 2,N
            XMAG = ABS(DX(IX))
            IF (XMAG .GT. DMAX) THEN
                IDAMAX = I
                DMAX = XMAG
            ENDIF
            IX = IX + INCX
10 CONTINUE

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        RETURN
C
C      Code for increments equal to 1.
C
20 DMAX = ABS(DX(1))
   DO 30 I = 2,N
       XMAG = ABS(DX(I))
       IF (XMAG .GT. DMAX) THEN
           IDAMAX = I
           DMAX = XMAG
       ENDIF
30 CONTINUE
   RETURN
   END
*DECK XERRWD
      SUBROUTINE XERRWD (MSG, NMES, NERR, LEVEL, NI, I1, I2, NR, R1, R2)
C***BEGIN PROLOGUE  XERRWD
C***SUBSIDIARY
C***PURPOSE  Write error message with values.
C***CATEGORY  R3C
C***TYPE      DOUBLE PRECISION (XERRWD-S, XERRWD-D)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  Subroutines XERRWD, XSETF, XSETUN, and the function routine IXSAV,
C  as given here, constitute a simplified version of the SLATEC error
C  handling package.
C
C  All arguments are input arguments.
C
C  MSG      = The message (character array).
C  NMES      = The length of MSG (number of characters).
C  NERR      = The error number (not used).
C  LEVEL     = The error level..
C              0 or 1 means recoverable (control returns to caller).
C              2 means fatal (run is aborted--see note below).
C  NI        = Number of integers (0, 1, or 2) to be printed with message.
C  I1,I2     = Integers to be printed, depending on NI.
C  NR        = Number of reals (0, 1, or 2) to be printed with message.
C  R1,R2     = Reals to be printed, depending on NR.
C
C  Note..  this routine is machine-dependent and specialized for use
C  in limited context, in the following ways..
C  1. The argument MSG is assumed to be of type CHARACTER, and
C     the message is printed with a format of (1X,A).
C  2. The message is assumed to take only one line.
C     Multi-line messages are generated by repeated calls.
C  3. If LEVEL = 2, control passes to the statement  STOP
C     to abort the run.  This statement may be machine-dependent.
C  4. R1 and R2 are assumed to be in double precision and are printed
C     in D21.13 format.
C
C***ROUTINES CALLED  IXSAV
C***REVISION HISTORY  (YYMMDD)
C   920831  DATE WRITTEN
C   921118  Replaced MFLGSV/LUNSAV by IXSAV. (ACH)
C   930329  Modified prologue to SLATEC format. (FNF)
C   930407  Changed MSG from CHARACTER*1 array to variable. (FNF)
C   930922  Minor cosmetic change. (FNF)
C***END PROLOGUE  XERRWD
C
C*Internal Notes:
C
C  For a different default logical unit number, IXSAV (or a subsidiary
C  routine that it calls) will need to be modified.
C  For a different run-abort command, change the statement following
C  statement 100 at the end.
C-----
C  Subroutines called by XERRWD.. None
C  Function routine called by XERRWD.. IXSAV
C-----
C**End
C

```

```

C  Declare arguments.
C
      DOUBLE PRECISION R1, R2
      INTEGER NMES, NERR, LEVEL, NI, I1, I2, NR
      CHARACTER*(*) MSG
C
C  Declare local variables.
C
      INTEGER LUNIT, IXSAV, MESFLG
C
C  Get logical unit number and message print flag.
C
C***FIRST EXECUTABLE STATEMENT  XERRWD
      LUNIT = IXSAV (1, 0, .FALSE.)
      MESFLG = IXSAV (2, 0, .FALSE.)
      IF (MESFLG .EQ. 0) GO TO 100
C
C  Write the message.
C
      WRITE (LUNIT,10)  MSG
10  FORMAT(1X,A)
      IF (NI .EQ. 1) WRITE (LUNIT, 20) I1
20  FORMAT(6X,'In above message,  I1 =',I10)
      IF (NI .EQ. 2) WRITE (LUNIT, 30) I1,I2
30  FORMAT(6X,'In above message,  I1 =',I10,3X,'I2 =',I10)
      IF (NR .EQ. 1) WRITE (LUNIT, 40) R1
40  FORMAT(6X,'In above message,  R1 =',D21.13)
      IF (NR .EQ. 2) WRITE (LUNIT, 50) R1,R2
50  FORMAT(6X,'In above,  R1 =',D21.13,3X,'R2 =',D21.13)
C
C  Abort the run if LEVEL = 2.
C
100  IF (LEVEL .NE. 2) RETURN
      STOP
C----- End of Subroutine XERRWD -----
      END
*DECK XSETF
      SUBROUTINE XSETF (MFLAG)
C***BEGIN PROLOGUE  XSETF
C***PURPOSE  Reset the error print control flag.
C***CATEGORY  R3A
C***TYPE  ALL (XSETF-A)
C***KEYWORDS  ERROR CONTROL
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  XSETF sets the error print control flag to MFLAG:
C  MFLAG=1 means print all messages (the default).
C  MFLAG=0 means no printing.
C
C***SEE ALSO  XERRWD, XERRWV
C***REFERENCES  (NONE)
C***ROUTINES CALLED  IXSAV
C***REVISION HISTORY  (YMMDD)
C   921118  DATE WRITTEN
C   930329  Added SLATEC format prologue. (FNF)
C   930407  Corrected SEE ALSO section. (FNF)
C   930922  Made user-callable, and other cosmetic changes. (FNF)
C***END PROLOGUE  XSETF
C
C  Subroutines called by XSETF.. None
C  Function routine called by XSETF.. IXSAV
C-----
C**End
      INTEGER MFLAG, JUNK, IXSAV
C
C***FIRST EXECUTABLE STATEMENT  XSETF
      IF (MFLAG .EQ. 0 .OR. MFLAG .EQ. 1) JUNK = IXSAV (2,MFLAG,.TRUE.)
      RETURN
C----- End of Subroutine XSETF -----
      END
*DECK XSETUN
      SUBROUTINE XSETUN (LUN)

```

```

C***BEGIN PROLOGUE  XSETUN
C***PURPOSE  Reset the logical unit number for error messages.
C***CATEGORY  R3B
C***TYPE      ALL (XSETUN-A)
C***KEYWORDS  ERROR CONTROL
C***DESCRIPTION
C
C  XSETUN sets the logical unit number for error messages to LUN.
C
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***SEE ALSO  XERRWD, XERRWV
C***REFERENCES  (NONE)
C***ROUTINES CALLED  IXSAV
C***REVISION HISTORY  (YMMDD)
C   921118  DATE WRITTEN
C   930329  Added SLATEC format prologue. (FNF)
C   930407  Corrected SEE ALSO section. (FNF)
C   930922  Made user-callable, and other cosmetic changes. (FNF)
C***END PROLOGUE  XSETUN
C
C Subroutines called by XSETUN.. None
C Function routine called by XSETUN.. IXSAV
C-----
C**End
      INTEGER LUN, JUNK, IXSAV
C
C***FIRST EXECUTABLE STATEMENT  XSETUN
      IF (LUN .GT. 0) JUNK = IXSAV (1,LUN,.TRUE.)
      RETURN
C----- End of Subroutine XSETUN -----
      END
*DECK IXSAV
      INTEGER FUNCTION IXSAV (IPAR, IVALUE, ISET)
C***BEGIN PROLOGUE  IXSAV
C***SUBSIDIARY
C***PURPOSE  Save and recall error message control parameters.
C***CATEGORY  R3C
C***TYPE      ALL (IXSAV-A)
C***AUTHOR  Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C
C  IXSAV saves and recalls one of two error message parameters:
C  LUNIT, the logical unit number to which messages are printed, and
C  MESFLG, the message print flag.
C  This is a modification of the SLATEC library routine J4SAVE.
C
C  Saved local variables..
C  LUNIT = Logical unit number for messages. The default is obtained
C          by a call to IUMACH (may be machine-dependent).
C  MESFLG = Print control flag..
C          1 means print all messages (the default).
C          0 means no printing.
C
C  On input..
C  IPAR = Parameter indicator (1 for LUNIT, 2 for MESFLG).
C  IVALUE = The value to be set for the parameter, if ISET = .TRUE.
C  ISET = Logical flag to indicate whether to read or write.
C          If ISET = .TRUE., the parameter will be given
C          the value IVALUE. If ISET = .FALSE., the parameter
C          will be unchanged, and IVALUE is a dummy argument.
C
C  On return..
C  IXSAV = The (old) value of the parameter.
C
C***SEE ALSO  XERRWD, XERRWV
C***ROUTINES CALLED  IUMACH
C***REVISION HISTORY  (YMMDD)
C   921118  DATE WRITTEN
C   930329  Modified prologue to SLATEC format. (FNF)
C   930915  Added IUMACH call to get default output unit. (ACH)
C   930922  Minor cosmetic changes. (FNF)
C   010425  Type declaration for IUMACH added. (ACH)
C***END PROLOGUE  IXSAV

```



```

C
C Subroutines called by IXSAV.. None
C Function routine called by IXSAV.. IUMACH
C-----
C**End
      LOGICAL ISET
      INTEGER IPAR, IVALUE
C-----
      INTEGER IUMACH, LUNIT, MESFLG
C-----
C The following Fortran-77 declaration is to cause the values of the
C listed (local) variables to be saved between calls to this routine.
C-----
      SAVE LUNIT, MESFLG
      DATA LUNIT/-1/, MESFLG/1/
C
C***FIRST EXECUTABLE STATEMENT IXSAV
      IF (IPAR .EQ. 1) THEN
        IF (LUNIT .EQ. -1) LUNIT = IUMACH()
        IXSAV = LUNIT
        IF (ISET) LUNIT = IVALUE
      ENDIF
C
      IF (IPAR .EQ. 2) THEN
        IXSAV = MESFLG
        IF (ISET) MESFLG = IVALUE
      ENDIF
C
      RETURN
C----- End of Function IXSAV -----
      END
*DECK IUMACH
      INTEGER FUNCTION IUMACH()
C***BEGIN PROLOGUE IUMACH
C***PURPOSE Provide standard output unit number.
C***CATEGORY R1
C***TYPE INTEGER (IUMACH-I)
C***KEYWORDS MACHINE CONSTANTS
C***AUTHOR Hindmarsh, Alan C., (LLNL)
C***DESCRIPTION
C *Usage:
C INTEGER LOUT, IUMACH
C LOUT = IUMACH()
C
C *Function Return Values:
C LOUT : the standard logical unit for Fortran output.
C
C***REFERENCES (NONE)
C***ROUTINES CALLED (NONE)
C***REVISION HISTORY (YYMMDD)
C 930915 DATE WRITTEN
C 930922 Made user-callable, and other cosmetic changes. (FNF)
C***END PROLOGUE IUMACH
C
C*Internal Notes:
C The built-in value of 6 is standard on a wide range of Fortran
C systems. This may be machine-dependent.
C**End
C***FIRST EXECUTABLE STATEMENT IUMACH
      IUMACH = 6
C
      RETURN
C----- End of Function IUMACH -----
      END

```