

JSC Engineering Orbital Dynamics Atmosphere Model

Simulation and Graphics Branch (ER7)
Software, Robotics, and Simulation Division
Engineering Directorate

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National Aeronautics and Space Administration
Lyndon B. Johnson Space Center
Houston, Texas

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Abstract

Aerodynamic effects can greatly influence the dynamics of an orbiting spacecraft. These aerodynamic effects depend greatly on modeling of both the Earth's atmosphere, as well as winds present in the atmosphere. Needed elements from the atmosphere include density, pressure, and temperature, as well as wind velocity.

This document presents the JEOD v5.0 Atmosphere Model framework, designed as a generic interface for the modeling of planet atmospheres. This framework is extensible. This allows for reuse of code by different atmosphere models, including models for bodies other than the Earth, while taking advantage of a common framework.

This document also presents a specific implementation of the generic JEOD atmosphere framework. This specific implementation is of the Marshall Engineering Thermosphere (MET) Model, an Earth-based atmosphere model. This implementation provides atmospheric pressure, temperature, and density, as well as other parameters specific to the MET Model, based on the current geodetic position and altitude.

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Chapter 1

Introduction

1.1 Model Description

A major effort in the simulation of space vehicle dynamics is the modeling of aerodynamic drag. Key to this aerodynamic drag is information regarding the atmosphere the vehicle travels in. Current density, pressure, and temperature can all play into how atmosphere affects the long term orbit of an orbiting vehicle. Additionally, winds present in the atmosphere can also dramatically affect the dynamics of a space vehicle.

The JEOD v5.0 Atmosphere Model gives an extensible, generic framework for the modeling of planet atmospheres, allowing for reuse of code by different models. While basic atmosphere modeling parameters are included in the atmosphere framework by default, other model-specific parameters can be added, and this can be done without changing the underlying methods used to update current atmospheric state for a specific vehicle. Additionally, an interface for wind velocity models has also been included, with an architecture and framework similar to that implemented for the atmosphere models.

Specific implementations for atmosphere will also be presented. The specific implementation for the atmosphere model is described in the following section.

1.1.1 NASA Marshall Engineering Thermosphere Model-Version 2.0

Early models of the upper atmosphere (thermosphere) emerged about 1965 [5]. These, as well as their descendants, were based on a numerical quadrature of the species diffusion equations. In these models the altitude profiles of the number densities are determined by the magnitude of the exospheric temperature T . This quantity is used to accommodate all activity concerning the diurnal effects, while semiannual variations are introduced via empirical correction functions. In the Jacchia-77 model, species corrections are also introduced for the diurnal, seasonal-latitudinal, and geomagnetic effects.

The MET model, NASA Marshall Engineering Thermosphere Model-Version 2.0, J.K Owens 2002 [12], is based on all Jacchia atmospheres [5], but it extends the range of output quantities, including the pressure, the pressure scale height and the ratio of specific heats.

1.2 Document History

Author	Date	Revision	Description
Andrew Spencer	July, 2009	1.0	Initial Version
Andrew Spencer	October, 2010	1.1	Added Metrics
Zu Qun Li & Christina Chomel	August, 2021	1.1	Added TCAM model

This document derives heavily from it's predecessor, JSC Engineering Orbital Dynamics Atmosphere Models, released with JEOD v1.5.2.

The following document is parent to this document:

- *JSC Engineering Orbital Dynamics* [8]

1.3 Document Organization

This document is formatted in accordance with the NASA Software Engineering Requirements Standard [11] and is organized into the following chapters:

Chapter 1: Introduction - This introduction contains three sections: description of model, document history, and organization. The first section provides the introduction to the Atmosphere Model and its reason for existence. It also contains a brief description of the interconnections with other models, and references to any supporting documents. The second section displays the history of this document which includes author, date, and reason for each revision; it also lists the document that is parent to this one. The final section contains a description of the how the document is organized.

Chapter 2: Product Requirements - Describes requirements for the Atmosphere Model.

Chapter 3: Product Specification - Describes the underlying theory, architecture, and design of the Atmosphere Model in detail. It is organized in three sections: Conceptual Design, Mathematical Formulations, and Detailed Design.

Chapter 4: User Guide - Describes how to use the Atmosphere Model in a Trick simulation. It is broken into three sections to represent the JEOD defined user types: Analysts or users of simulations (Analysis), Integrators or developers of simulations (Integration), and Model Extenders (Extension).

Chapter 5: Verification and Validation - Contains Atmosphere Model verification and validation procedures and results.

Chapter 2

Product Requirements

This chapter will describe the requirements for the Atmosphere Model.

Requirement atmosphere_1: Top-level requirement

Requirement:

This model shall meet the JEOD project requirements specified in the JEOD v5.0 [top-level document](#).

Rationale:

This model shall, at a minimum, meet all external and internal requirements applied to the JEOD v5.0 release.

Verification:

Inspection

2.1 General Requirements

This section identifies general requirements for the Atmosphere Model.

Requirement atmosphere_2: MET Atmosphere

Requirement:

This model must be provided the date, solar activity, geomagnetic activity, and location as input. It will output the density, temperature, and pressure, of the atmosphere for that location and time in kilograms per cubic meter.

Rationale:

These output parameters, particularly the atmospheric density, are critical for low-Earth orbit satellite operations.

Verification:

Several tests were run as verification for this model. The output of the MET model was compared against existing published data for the MET model. The output was then compared against the MSIS model [16] available on the Internet. The output was then compared against the Trick Jacchia model to determine model consistency even though the Jacchia model is unverified. And lastly, the output was compared against a FORTRAN version of the GRAM 99 model which uses MET as the upper atmosphere model.

*Requirement atmosphere_3: Atmosphere Extensibility***Requirement:**

The Atmosphere Model shall be extensible to user defined implementations of atmosphere.

Rationale:

Other atmosphere models exist that should be usable, after user extension, in the JEOD package.

Verification:

The verification of this requirement shall be done by inspection.

*Requirement atmosphere_4: Wind Model***Requirement:**

The Atmosphere Model shall provide the ability to represent the rigid rotation of Earth's atmosphere of molecules with selectable parameters.

Rationale:

The purpose of the Atmosphere Model is to simulate effects on a vehicle, including wind.

Verification:

The verification of this requirement shall be done by inspection.

Chapter 3

Product Specification

3.1 Conceptual Design

This section will present the conceptual design for both the general Atmosphere Model framework and the MET specific implementation of this framework.

3.1.1 General Framework

The basis of the JEOD v5.0 Atmosphere Model is three generic classes:

- The generic atmosphere state class, containing basic and common parameters associated with output of atmosphere models (the results of atmosphere calculations),
- The generic atmosphere base class, containing basic member functions useful to most implementations of atmosphere models (the algorithms and specific math contained in an atmosphere model),
- The generic wind velocity base class, containing basic member functions useful to most implementations of wind velocity models (the algorithms and specific math contained in a wind velocity model).

These classes are meant to be extended through basic C++ programming techniques for specific implementations of atmosphere models. Additional parameters which are contained in a specific atmosphere model can be added to the generic atmosphere state class (however, through correct extension of the generic framework, a generic atmosphere state object should be useable with any implementation of atmosphere, giving the option of changing atmosphere models easily mid-simulation). Specific functional implementations for different atmosphere and wind velocity models can then be created through extension of the generic atmosphere base class and generic wind velocity class.

3.1.2 MET Specific Implementation

The purpose of the MET Atmosphere Model is, given input atmosphere parameters to the MET model as well as the current time and position in space, output the atmospheric parameters for that state. These outputs include the generic density, pressure and temperature, as well as information on various densities of ambient elements (oxygen, nitrogen, etc). These numbers are available on a per vehicle basis, and allow for one MET atmosphere model to be used to update many individual atmosphere states.

3.1.3 Wind Velocity Model

The purpose of the wind velocity model is, given a position and altitude in space, calculate the velocity of the wind in the Earth Centered Inertial reference frame.

3.2 Mathematical Formulations

3.2.1 General Framework

The generic Atmosphere Model framework does not have a mathematical formulation. All mathematical formulations will be contained in specific instances of the generic framework, such as the MET model, described below.

3.2.2 Marshall Engineering Thermosphere

This section describes the mathematical formulation behind the Marshall Engineering Thermosphere model.

THERMOSPHERE REGION

The region of the earth's atmosphere lying between about 90 and 500 kilometers is known as the thermosphere, while that region lying above 500 kilometers is known as the exosphere. The temperature in the lower thermosphere increases rapidly with increasing altitude from a minimum at 90 kilometers. Eventually it becomes altitude-independent at upper thermospheric altitudes. This asymptotic temperature, known as the exospheric temperature, is a constant due to the extremely short thermal conduction time.

The thermospheric gases are heated by the absorption of the solar extreme ultraviolet (EUV) radiation. At the lowest thermospheric altitudes the absorption of ultraviolet (UV) radiation is also important. The EUV and UV radiation initially heat only the day side thermosphere, and although conductive and convective processes act to redistribute some of this energy, a large temperature gradient always exists between the daytime and the nighttime thermosphere. An average daytime exospheric temperature is 1060°K and an average nighttime exospheric temperature is 840°K . The longitudinal temperature gradient causes a wind to flow from the day side to the night side thermosphere, with speeds typically reaching 100 m/sec.

An additional heat source for the thermosphere is the interaction of the earth's magnetic field at

very great distances (at least several earth radii) in the region known as the magnetosphere with the solar wind (a stream of high speed plasma emanating from the sun). This interaction causes energetic particles to penetrate down into the lower thermosphere at high geographic latitudes and directly heat the thermospheric gas. These energetic particles are also responsible for the aurora seen at these high latitudes. In addition, electric fields mapped down from the magnetosphere onto the high latitude ionosphere cause electric currents to flow. The ionosphere is a small fraction of the thermosphere that remains ionized due to the solar radiation. It never totally disappears at night, and during daylight hours the ionization density never exceeds more than one percent of the neutral density. These currents lose energy through Ohmic or Joule dissipation and heat the neutral thermospheric gas. The ions also collide directly with the neutral gas, setting the whole gas into motion. At these high latitudes the wind speeds generated by this process can be very large, at times as large as 1.5 km/sec. Eventually viscous effects dissipate these winds and their lost kinetic energy provides an additional heat source for the neutral thermospheric gas.

The high latitude heat sources are effective both during the day and night. Although an intermittent source of energy for the thermosphere, they can at times exceed the global EUV energy absorbed by the thermosphere. In addition, although the energy is deposited at high latitudes (greater than 60° or so), the disturbance effects are transmitted to lower latitudes through the actions of winds and waves. However, the disturbance effects at low latitudes are significantly smaller than they are at higher latitudes. The high latitude ionospheric currents that flow perturb the geomagnetic field, so that such disturbances, which can be detected by ground-based magnetometers, are referred to as geomagnetic storms.

Whenever the neutral thermospheric gas is heated, it expands radially outwards. Because the undisturbed thermospheric density decreases with increasing altitude, an outward expansion of the gas results in an increase of density at high altitudes. Thus, the daytime thermospheric density is greater than the nighttime density, while during times of geomagnetic storms the high latitude density is greater than it is during undisturbed periods. This anisotropic heating leads to the so-called diurnal and polar bulges, which were first inferred from the increased drag experience by orbiting satellites.

Below the turbopause, the region where the atmosphere transitions from turbulent mixing to molecular diffusion (located at about 105 kilometers altitude), the atmosphere is well mixed by turbulence, so that the composition of the atmosphere does not vary with altitude. Above the turbopause, however, diffusion becomes so rapid that the altitude variation of the various species becomes dependent on molecular mass, with the result that composition varies with altitude. Thus, the number densities of the heavier thermospheric species (N_2 and O_2) decrease with increasing altitude much faster than those of the lighter species (H and He). This means that the heavier molecular species predominate in the lower thermosphere, while the lighter atomic species predominate in the upper thermosphere. A typical altitude profile for the individual thermospheric constituents is shown below in *NASA Marshall Document 1 MET98* [4]. Lifting of the thermosphere will cause the mean molecular weight at a given altitude to increase, while a sinking motion will cause it to decrease.

VARIATIONS

Variations in the density of the neutral atmosphere at orbital altitudes are associated with variations in solar activity, geomagnetic activity, the diurnal variation, the semiannual variation, seasonal-latitude variations of the lower thermosphere density, seasonal-latitude variations of helium, atmospheric waves, and thermospheric winds. These variations are described in the paragraphs

that follow.

VARIATIONS WITH SOLAR ACTIVITY

The short wavelength solar electromagnetic radiation (EUV and UV) changes substantially with the level of solar activity, with the result that the thermospheric density, especially at orbital altitudes, is strongly dependent on the level of solar activity. Thus, there is an average 11-year variation in the thermospheric density, corresponding to the average 11-year solar cycle variation; similarly, there is also an average 27-day variation in density that is related to the average 27-day solar rotation period, although the variation tends to be slightly longer than 27 days early in the cycle when regions occur more frequently at higher latitude and slightly shorter than 27 days later in the cycle when regions occur more frequently closer to the Sun's equator. The appearance of coronal holes and active longitudes also affects this average 27-day variation. Changes in the thermospheric density related to changes in the level of solar (and geomagnetic) activity (e.g., flares, eruptions, coronal mass ejection (CME's) and coronal holes (CH's)) can begin almost instantaneously (mins to hrs), although more often a day or more lag is seen. *NASA Marshall Document 1 MET98* [4] shows typical neutral densities for periods of high and low solar activity.

VARIATIONS WITH GEOMAGNETIC ACTIVITY

As previously described, the enhanced interaction of the solar wind with the Earth's magnetosphere (referred to as geomagnetic activity) leads to a high latitude heat and momentum source for the thermospheric gases. Some of this heat and momentum is convected to low latitudes. Geomagnetic activity varies over the solar cycle and usually has two or more major peaks, one during the rise of the cycle and other, larger peaks, during the decline of the cycle. Also, more intense solar cycles seem to have more intense geomagnetic activity. Finally, there is a seasonal variation with geomagnetic activity usually being greatest in March (± 1 month) and September (± 1 month) of each year. This variation is possibly related to the tilt of the Sun's rotational axis toward the Earth.

THE DIURNAL VARIATION

The rotation of the earth with respect to the solar EUV heat source induces a diurnal (24 hour period) variation (or, diurnal tide) in the thermospheric temperature and density. Due to a lag in the response of the thermosphere to the EUV heat source the density maximizes around 2 p.m. local solar time at orbital altitudes at a latitude approximately equal to that of the subsolar point. The lag, which is a function of altitude, decreases with decreasing altitude. Similarly, the density minimum occurs between 3 and 4 a.m. local solar time at about the same latitude in the opposite hemisphere. In the lowest regions of the thermosphere (120 kilometers and below) where the characteristic thermal conduction time is on the order of a day or more, the diurnal variation is not a predominant effect.

The various constituents of the thermosphere do not all respond to the diurnal variation of the solar EUV heat source with the same amplitude and phase. The time lag is longer, by as much as 2 hours at orbital altitudes, for the heavier constituents (N_2 , O_2 and Ar) than for O. By contrast, the lighter species number densities maximize in the early morning hours (3 a.m. and 7 a.m. local solar time, for H and He, respectively). This is due to dynamical (buoyancy) effects.

Harmonics of the diurnal tide are also induced in the Earth's atmosphere. In particular, a semi-diurnal tide (period of 12 hours) and a ter-diurnal tide (period of 8 hours) are important in the lower thermosphere (below some 160 kilometers for the semi-diurnal tide, and much lower for the

ter-diurnal tide). These tides are not important at orbital altitudes.

SEMIANNUAL VARIATION

This variation is believed to be a conduction mode of oscillation driven by a semiannual variation in Joule heating in the high latitude thermosphere (as a consequence of a semiannual variation in geomagnetic activity). The variation is latitudinally independent, and is modified by composition effects. The amplitude of the variation is height dependent and variable from year to year with a primary minimum in July, primary maximum in October, and a secondary minimum in January followed by a secondary maximum in April. It has been found that the magnitude and altitude dependence of the semiannual oscillation vary considerably from one solar cycle to the next. This variation is important at orbital altitudes.

SEASONAL–LATITUDINAL VARIATIONS OF THE LOWER THERMOSPHERE DENSITY

This variation is driven in the thermosphere by the dynamics of the lower atmosphere (mesosphere and below). The amplitude of the variation maximizes in the lower thermosphere somewhere between about 105 and 120 kilometers, diminishing to zero at altitudes around 200 kilometers. Although the temperature oscillation amplitude is quite large, the corresponding density oscillation amplitude is small. This variation is not important at orbital altitudes.

SEASONAL–LATITUDINAL VARIATIONS OF HELIUM

Satellite mass spectrometers have measured a strong increase of helium above the winter pole. Over a year the helium number density varies by a factor of 42 at 275 km, 12 at 400 km and 3 or 4 above 500 km. The formation of this winter helium bulge has been shown to be primarily due to the effects of global scale winds that blow from the summer to the winter hemisphere. The amplitude of the bulge decreases with increasing levels of solar activity, due to the increased effectiveness of exospheric transport above 500 km which carries helium back to the summer hemisphere. There is also a very weak dependence of the helium bulge amplitude on the magnitude of the lower thermospheric eddy diffusivity.

SOLAR AND GEOMAGNETIC INDICES

Various surrogate indices are used to quantitatively assess the levels of solar activity. One of these is the 10.7 cm solar radio noise flux, designated F10.7. Although it is the EUV radiation that heats the thermosphere, it cannot be measured at the ground. The F10.7 can be measured from the ground, and it also correlates quite well with the EUV radiation. Although there are instances when the correlation is not good, it appears unlikely that the F10.7 radio flux will be replaced by another index in the foreseeable future.

An index that is used as a measure of geomagnetic activity is the planetary geomagnetic activity index a_p (or k_p , which is essentially the logarithm of a_p). It is based on magnetic fluctuation data taken every 3 hours at 12 stations between geomagnetic latitudes 48° and 63° and selected for good longitude coverage. Although it is the high latitude ionospheric current fluctuations that drive the magnetic field fluctuations as observed at these stations, it is not the magnetic field fluctuations which are driving the thermosphere and so good correlations between observed density changes and the a_p index are not always found. The daily planetary geomagnetic index, a_p , is the average of the 8 3-hourly a_p values for that particular day.

MET

The Marshall Engineering Thermosphere (MET) model has been developed to represent, in so far as practical for engineering applications, the variability of the ambient mass density at orbital altitudes. It is the standard neutral atmospheric density model used for control and lifetime studies involving all orbiting spacecraft projects.

The MET model is an empirical model whose coefficients were obtained from satellite drag analyses. It is a static diffusion model and is essentially the Smithsonian's Jacchia 1970 model with two additions from the Jacchia 1971 model. Inputs to the model are time (year, month, day, hour and minute), position (altitude and geographic latitude and longitude), the previous day's solar radio flux (F10.7), the centered solar radio flux averaged over 6 solar rotations (F10.7B) and the a_p index at 6 to 7 hours before the time in question (for some studies the daily planetary geomagnetic index, a_p , may be used instead of the 3-hourly a_p value).

With these inputs the exospheric temperature can be calculated. It should be stressed that in the original development of the model the prime objective was to model the total neutral density of the thermosphere by adjusting temperature profiles until agreement between modeled and measured total densities was achieved. Thus, agreement between modeled and measured temperature is not always achieved. Thomson-scatter temperature measurements generally show that the temperature lags the density by a couple of hours, whereas in the MET model the temperature and density are in phase.

With the exospheric temperature specified the temperature can be calculated for any altitude between the lower boundary (90 kilometers) and the upper level (2500 kilometers) of the model from an empirically determined temperature profile. The density for all points on the globe at 90 kilometers altitude is assumed constant, and mixing prevails to 105 kilometers. Between these two altitudes the mean molecular mass varies as a result of the dissociation of molecular to atomic oxygen. At 120 kilometers altitude the ratio of atomic to molecular oxygen is assumed to be 1.5. Density between 90 and 105 kilometers is calculated by integration of the barometric equation. For altitudes above 105 kilometers the diffusion equation for each of the individual species (O_2 , O , N_2 , He and Ar) is integrated upwards from the 105 kilometer level. For hydrogen the integration of the diffusion equation proceeds upwards from 500 kilometers altitude. The total mass density is calculated by summing the individual specie mass densities.

The total density is then further modified by the effects of the seasonal-latitudinal density variation of the lower thermosphere below 170 kilometers altitude and seasonal-latitudinal variations of helium above 500 kilometers. These two effects have been incorporated in the MET model using equations developed by Jacchia for his 1971 thermospheric model.

The final output of the MET model is total mass density, temperature, pressure, individual specie number densities, mean molecular weight, scale-height, specific heats and the local gravitational acceleration.

The total mass density, the temperature and the individual species all have the same phase variation in the MET model (i.e., they all maximize at the same local time). For some studies involving the effects of various species on an orbiting spacecraft it may be required to use the MSIS (Mass Spectrometer Incoherent Scatter) model [3] if accurate phases of the various species are required. The total math modeling of MET is given in the following NASA Technical Memorandums. The specific model in the Atmosphere Model is MET98 [4] ([NASA Marshall Document 1 MET98](#)); additions and improvements are in MET Version 2 [12] ([NASA Marshall Document 2 MET-Version 2](#)).

Lower Atmosphere

At this time, there is no verified atmosphere model for portions of the atmosphere below 100 km for the public release version of JEOD. For the NASA internal release, the TCAM atmosphere model is available, which contains data from Global Upper Air Climatic Atlas (GUACA) or Global Gridded Upper Air Statistics (GGUAS) are for region between 0 to 27km and data compiled from the Middle Atmosphere Program (MAP) for region between 20 to 120 km.

3.2.3 Wind Velocity Model

There is a simple wind velocity model implemented in the JEOD v5.0 Atmosphere Model. The basis for this implementation can be found in [17] and [10]. The full derivation for this model can also be found in these references.

This particular wind velocity model is based on winds caused by the rotation of a planet under the point in question. Much of the work of this algorithm will be done in the inertial reference frame associated with this planet, and this will be the frame where the final wind velocity is calculated.

Winds are assumed to have rotational symmetry. This results in imaginary circles, centered at and perpendicular to the assumed planet axis of rotation, where all wind velocities have equal magnitudes and all wind directions are perpendicular to the imaginary circle.

Winds are based on a user defined base rotational velocity of the planet, defined here as $\omega_{nominal}$. This nominal rotational velocity is then scaled based on the altitude of the point of interest, to produce ω_{scaled} as so:

$$\omega_{scaled} = \omega_{nominal} * \alpha \quad (3.1)$$

where α is the scaling factor based on the altitude. The mapping from altitude to α is a simple interpolation table, with points defined by the user.

For this simple wind velocity algorithm, the axis of rotation of the planet is assumed to be aligned with the Z axis of the inertial reference frame of the planet. Currently for Earth this only introduces a small error; however, as the nutation and precession of the Earth axis of rotation continues this error will increase. Hence,

$$\vec{\omega} = \{0, 0, 1\} \quad (3.2)$$

The complete wind velocity, including both magnitude and direction, is then calculated using a vector cross product, as follows:

$$wind = \omega_{scaled} * (\vec{\omega} \times p\vec{os}_{inertial}) \quad (3.3)$$

where $vecpos_{inertial}$ is the position of the point of interest, in the planet centered inertial reference frame.

3.3 Detailed Design

The complete API for the Atmosphere Model can be found in the [Reference Manual \[1\]](#).

3.4 Inventory

All Atmosphere Model files are located in the directory

`${JEOD_HOME}/models/environment/atmopshere`. Relative to this directory,

- Header and source files are located in the model **include** and **src** subdirectories. Table 3.1 lists the configuration-managed files in these directories.
- Data files are located in the model **data** subdirectory. See table ?? for a listing of the configuration-managed files in this directory.
- Documentation files are located in the model **docs** subdirectory. See table 3.2 for a listing of the configuration-managed files in this directory.
- Verification files are located in the model **verif** subdirectory. See table 3.3 for a listing of the configuration-managed files in this directory.

Table 3.1: Source Files

File Name
MET/include/MET_atmosphere.hh
MET/include/MET_atmosphere_state.hh
MET/include/MET_atmosphere_state_vars.hh
MET/include/class_declarations.hh
MET/src/MET_atmosphere.cc
MET/src/MET_atmosphere_state.cc
MET/src/MET_atmosphere_state_vars.cc
base_atmos/include/atmosphere.hh
base_atmos/include/atmosphere_messages.hh
base_atmos/include/atmosphere_state.hh
base_atmos/include/class_declarations.hh
base_atmos/include/wind_velocity.hh
base_atmos/include/wind_velocity_base.hh
base_atmos/src/atmosphere_messages.cc
base_atmos/src/atmosphere_state.cc
base_atmos/src/wind_velocity.cc
base_atmos/src/wind_velocity_base.cc
MET/data/include/met_data_wind_velocity.hh

Continued on next page

Table 3.1: Source Files (continued from previous page)

File Name
MET/data/include/solar_max.hh
MET/data/include/solar_mean.hh
MET/data/include/solar_min.hh
MET/data/src/data_met_wind_velocity.cc
MET/data/src/solar_max.cc
MET/data/src/solar_mean.cc
MET/data/src/solar_min.cc

Table 3.2: Documentation Files

File Name
docs/atmosphere.pdf
docs/refman.pdf
docs/refs/gram99.pdf
docs/refs/marshallMETTM.pdf
docs/refs/met98.pdf
docs/tex/atmosphere.bib
docs/tex/atmosphere.sty
docs/tex/atmosphere.tex
docs/tex/atmosphereAbstract.tex
docs/tex/atmosphereChapters.tex
docs/tex/makefile
docs/tex/model_name.mk
docs/tex/pics/MET_GRA_T01_density.jpg
docs/tex/pics/MET_GRA_T01_pressure.jpg
docs/tex/pics/MET_GRA_T01_temperature.jpg
docs/tex/pics/MET_GRA_T02_density.jpg
docs/tex/pics/MET_GRA_T02_pressure.jpg
docs/tex/pics/MET_GRA_T02_temperature.jpg
docs/tex/pics/MET_GRA_T03_density.jpg
docs/tex/pics/MET_GRA_T03_pressure.jpg
docs/tex/pics/MET_GRA_T03_temperature.jpg
docs/tex/pics/MET_JAC_T01_temperature.jpg
docs/tex/pics/MET_JAC_T02_temperature.jpg
docs/tex/pics/MET_MSIS_T01_temperature.jpg

Continued on next page

Table 3.2: Documentation Files (continued from previous page)

File Name
docs/tex/pics/MET_T01_density.jpg
docs/tex/pics/MET_T01_pressure.jpg
docs/tex/pics/MET_T01_temperature.jpg

Table 3.3: Verification Files

File Name
MET/verif/SIM_MET/S_define
MET/verif/SIM_MET/S_overrides.mk
MET/verif/SIM_MET/Log_data/log_met.py
MET/verif/SIM_MET/SET_test/input_core.py
MET/verif/SIM_MET/SET_test/RUN_T01_GRAM_MET/input.py
MET/verif/SIM_MET/SET_test/RUN_T01_JAC_COMP/input.py
MET/verif/SIM_MET/SET_test/RUN_T01_MET_VER/input.py
MET/verif/SIM_MET/SET_test/RUN_T02_GRAM_MET/input.py
MET/verif/SIM_MET/SET_test/RUN_T02_JAC_COMP/input.py
MET/verif/SIM_MET/SET_test/RUN_T02_MET_VER/input.py
MET/verif/SIM_MET/SET_test/RUN_T03_GRAM_MET/input.py
MET/verif/SIM_MET/SET_test/RUN_data_compare/input.py
MET/verif/SIM_MET/SET_test_val/input_core.py
MET/verif/SIM_MET/SET_test_val/RUN_T01_GRAM_MET/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T01_GRAM_MET/log_atmos_
verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T01_GRAM_MET/log_atmos_
verif.header
MET/verif/SIM_MET/SET_test_val/RUN_T01_JAC_COMP/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T01_JAC_COMP/log_atmos_
verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T01_JAC_COMP/log_atmos_
verif.header
MET/verif/SIM_MET/SET_test_val/RUN_T01_MET_VER/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T01_MET_VER/log_atmos_
verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T01_MET_VER/log_atmos_
verif.header

Continued on next page

Table 3.3: Verification Files (continued from previous page)

File Name
MET/verif/SIM_MET/SET_test_val/RUN_T02_GRAM_MET/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T02_GRAM_MET/log_atmos_ verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T02_GRAM_MET/log_atmos_ verif.header
MET/verif/SIM_MET/SET_test_val/RUN_T02_JAC_COMP/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T02_JAC_COMP/log_atmos_ verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T02_JAC_COMP/log_atmos_ verif.header
MET/verif/SIM_MET/SET_test_val/RUN_T02_MET_VER/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T02_MET_VER/log_atmos_ verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T02_MET_VER/log_atmos_ verif.header
MET/verif/SIM_MET/SET_test_val/RUN_T03_GRAM_MET/input.py
MET/verif/SIM_MET/SET_test_val/RUN_T03_GRAM_MET/log_atmos_ verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_T03_GRAM_MET/log_atmos_ verif.header
MET/verif/SIM_MET/SET_test_val/RUN_data_compare/input.py
MET/verif/SIM_MET/SET_test_val/RUN_data_compare/log_atmos_ verif.csv
MET/verif/SIM_MET/SET_test_val/RUN_data_compare/log_atmos_ verif.header
MET/verif/SIM_wind/S_define
MET/verif/SIM_wind/S_overrides.mk
MET/verif/SIM_wind/Log_data/log_test.py
MET/verif/SIM_wind/SET_test/RUN_test/input.py
MET/verif/SIM_wind/SET_test_val/RUN_test/input.py
MET/verif/SIM_wind/SET_test_val/RUN_test/log_test_data.csv
MET/verif/SIM_wind/SET_test_val/RUN_test/log_test_data.header

Chapter 4

User Guide

The Analysis section of the user guide is intended primarily for users of pre-existing simulations. It contains:

- A description of how to modify Atmosphere Model variables after the simulation has compiled, including an in-depth discussion of the input file,
- An overview of how to interpret (but not edit) the S_define file,
- A sample of some of the typical variables that may be logged.

The Integration section of the user guide is intended for simulation developers. It describes the necessary configuration of the Atmosphere Model within an S_define file, and the creation of standard run directories. The latter component assumes a thorough understanding of the preceding Analysis section of the user guide. Where applicable, the user may be directed to selected portions of Product Specification (Chapter 3).

The Extension section of the user guide is intended primarily for developers needing to extend the capability of the Atmosphere Model. Such users should have a thorough understanding of how the model is used in the preceding Integration section, and of the model specification (described in Chapter 3).

Note that, for analysis and integration, the detail of Atmosphere Model generic framework will not be discussed, as only a specific implementation of the framework is intended to be used for these endeavors. Similarly, only the generic framework will be discussed in the extension section, as it is the part of the Atmosphere Model intended to be used by a third party for implementation of new atmosphere and wind velocity models.

4.1 Analysis

This section provides information for users of pre-existing simulation that contains the atmospheric model using MET atmosphere

4.1.1 Atmosphere

The base Atmosphere is a pure virtual class to inherit from when creating Atmosphere models. It defines the parameters for calling the `update_atmosphere` function. The MET atmosphere model is a derivative of the Base Atmosphere model.

Atmosphere State

An AtmosphereState object (and any object type that inherits from it) will have an active/inactive flag, a *bool* type called *active* which defaults to *true*. An AtmosphereState object will only update if this flag is *true*.

Three basic atmosphere parameters related to atmosphere are available in the base AtmosphereState objects:

- temperature: The temperature at the point of interest,
- density: The density at the point of interest, and
- pressure: The total pressure at the point of interest.

4.1.2 MET Atmosphere

For the purpose of illustrating the MET Atmosphere model, this analysis section will assume an S_define object of the following form:

```
class TimeSimObject : public Trick::SimObject {
    jeod::TimeUTC time_utc;
    ...
};
TimeSimObject time;

class AtmosStateSimObject : public Trick::SimObject {
    jeod::AtmosphereState      atmos_state;
    jeod::METAtmosphereState   met_atmos_state;
    ...
};
AtmosStateSimObject atmos_state;
```

```

class EarthSimObject : public Trick::SimObject {

    jeod::WindVelocity wind_velocity;
    jeod::METAtmosphere met_atmos;

    ...

}
EarthSimObject planet;

```

Note that this code is only representative of objects necessary for this discussion, and does not hold a complete implementation.

For a METAtmosphere object (shown here as *planet.met_atmos*), there are four atmosphere related variable parameters that can be set. These are:

- *geo_index*: The geomagnetic variations index,
- *F10*: The solar radio noise flux,
- *F10B*: The 90 day average of solar radio noise flux, and
- *geo_index_type*: An enumeration determining how the geomagnetic variations in temperature will be calculated.

Further information on appropriate values for these can be found in [\[12\]](#).

MET Atmosphere State

The METAtmosphere state uses the elliptical coordinate portion of a PlanetFixedPosition object. The details of this object's use can be found in [\[7\]](#). Additionally, METAtmosphere is time-dependent, specifically on the UTC clock which is often found at *jeod.time.time_utc*. The *METAtmosphere* class contains a method *update_time(TimeUTC &)* by which the clocks value is copied into the class for later usage. Further instructions for interaction with the JEOD v5.0 time model can be found in the JEOD Time Representations Model documentation [\[14\]](#).

Output from the METAtmosphere model will be contained in an AtmosphereState object: either an METAtmosphereState object (illustrated above by *atmos_met.met_atmos.state*), or a generic AtmosphereState object (illustrated by *atmos_met.atmos.state*). By design, and when correctly implemented, any JEOD v5.0 atmosphere object can accept a generic AtmosphereState object.

Additionally, a METAtmosphereState object will also include parameters specific to the calculation of the METAtmosphere, such as:

- *mol_weight*: The average molecular weight,
- *N2*: The Nitrogen (N_2) density number

- Ox2: The Oxygen (O_2) density number
- Ox: The Oxygen density number

A full list of the values can be found in the Detailed Design section of this document.

4.1.3 Wind Velocity

There are a handful of input parameters for the WindVelocity object. One parameter is

- omega: The nominal rotational velocity of the planet causing the winds.

The other input parameters to the WindVelocity object are associated with the interpolation table to scale the nominal rotational velocity of the planet to a scaled velocity (as seen in (3.1)) depending on the altitude of the point of interest. These parameters are:

- omega_scale_alt: The independent variable of the interpolation table, the altitude, in the form of an array,
- omega_scale_fac: The dependent variable of the interpolation table, the scaling factor as seen in (3.1), in the form of an array,
- num_layers: The length of the omega_scale_alt and omega_scale_fac arrays

Note that the arrays are in the form of a double pointer, thus they must have memory allocated for them before their values are set.

Note that for the most part these values will be set through a default data file found in the S_define, so there is no need to set them in the input file.

The output of the WindVelocity object is the wind velocity in the inertial frame associated with the planet. It is in the form of an array of doubles that is three long, representing a three vector of velocity. This output can be found either in an AtmosphereState object, or an object deriving from an AtmosphereState object. In the case of the example at the start of this section, the wind velocity will either be:

- `atmos_met.met_atmos_state.wind`
- `atmos_met.atmos_state.wind`

4.2 Integration

This section provides information for simulation developers who are planning to incorporate the MET atmosphere model in a simulation.

4.2.1 MET Atmosphere

The following S_define contents is used throughout this section as an example for incorporating the MET Atmosphere model in a simulation.

Note that this is not a full, working S_define, it is only representative of the necessary usage of the MET Atmosphere Model. For other aspects of the S_define necessary for the Atmosphere Model, such as the JEOD Time Model [14] and the JEOD Planet Fixed Model [7], please see the appropriate documentation.

```
class TimeSimObject : public Trick::SimObject {

    jeod::TimeUTC time_utc;

};

TimeSimObject time;

class EarthSimObject : public Trick::SimObject {

    jeod::WindVelocity wind_velocity;
    jeod::METAtmosphere atmos;

    // The default data objects
    jeod::METAtmosphere_solar_mean_default_data solar_mean_data;
    jeod::WindVelocity_wind_velocity_default_data wind_data;

    EarthSimObject( const jeod::TimeUTC& utc)
        :
        time_utc( utc)
    {
        ("default_data") solar_mean_data.initialize( &atmos);
        ("default_data") wind_data.initialize( &wind_velocity);

        /* Note: Before calling any update of an atmosphere state using
           METAtmosphere, the TimeUTC.calendar_update(double) function MUST be
           called for the TimeUTC given to the AtmosphereState function */
        ("initialization") atmos.update_time( time_utc);
        (DYNAMICS, "environment") atmos.update_time( time_utc);
    }

    ...

};

EarthSimObject planet(jeod_time.time_utc);

class VehicleSimObject : public Trick::SimObject {
```

```

    jeod::DynBody          body;
    jeod::PlanetFixedPosition pos;
    jeod::PlanetaryDerivedState pfix;

    ...

};
VehicleSimObject vehicle(planet.atmos);

class AtmosStateSimObject : public Trick::SimObject {

    jeod::AtmosphereState      atmos_state;
    jeod::METAtmosphereState   met_atmos_state;

    // External Reference
    jeod::WindVelocity         * wind;
    jeod::RefFrameTrans        * inertial_trans;
    jeod::PlanetaryDerivedState * pfix_pos;

    // MetAtmosSimObject is just a container for a pos, so nothing is to be
    // done in the constructor
    AtmosStateSimObject( jeod::METAtmosphere          & atmos_model_,
                        const jeod::PlanetFixedPosition & pos_,
                        jeod::WindVelocity             * wind_,
                        jeod::RefFrameTrans             * inertial_trans_,
                        jeod::PlanetaryDerivedState     * pfix_pos_)
    :
    atmos_state(      atmos_model_, pos_),
    met_atmos_state( atmos_model_, pos_),
    wind(            wind_),
    inertial_trans(  inertial_trans_),
    pfix_pos(        pfix_pos_)
    {
        ("initialization") atmos_state.update_state();
        ("initialization") met_atmos_state.update_state();
        (DYNAMICS, "environment") atmos_state.update_state();
        (DYNAMICS, "environment") met_atmos_state.update_state();

        ("initialization") atmos_state.update_wind(wind,
                                                    inertial_trans->position,
                                                    pfix_pos->state.ellip_coords.altitude);
        ("initialization") met_atmos_state.update_wind(wind,
                                                         inertial_trans->position,
                                                         pfix_pos->state.ellip_coords.altitude);
        (DYNAMICS, "environment") atmos_state.update_wind(wind,

```

```

                                inertial_trans->position,
                                pfix_pos->state.ellip_coords.altitude);
(DYNAMICS, "environment") met_atmos_state.update_wind(wind,
                                inertial_trans->position,
                                pfix_pos->state.ellip_coords.altitude);

}

...

};
AtmosStateSimObject atmos_state ( planet.atmos,
                                vehicle.pos,
                                &planet.wind_velocity,
                                &vehicle.body.composite_body.state.trans,
                                &vehicle.pfix);

```

To use the MET Atmosphere model in an S_define, the following objects must be instantiated, in some form:

- An METAtmosphere object,
- A TimeUTC object,
- A PlanetFixedPosition object,
- Either an AtmosphereState derived object or an METAtmosphereState object.

The TimeUTC object will often come from a complete instantiation of the JEOD v5.0 Time Model. Instructions for this component can be found in the Time Model Documentation [\[14\]](#).

The PlanetFixedPosition object will often come from a PlanetaryDerivedState object. Details on how to accomplish this can be found in the PlanetaryDerivedState documentation [\[15\]](#). In the case of METAtmosphere, the elliptical coordinates (geodetic latitude, longitude and altitude) are used, so it must be assured that these coordinates are being properly calculated.

The instantiation of the METAtmosphere object will often be accompanied by an initialization of data with a default data class instance. In our example, the following instantiation can be seen:

```

jeod::METAtmosphere atmos;
jeod::METAtmosphere_solar_mean_default_data solar_mean_data;
...
("default_data") solar_mean_data.initialize( &atmos);
...

```

The default data class instance is setting variables associated with solar activity, which can affect the output of the MET Atmosphere model. These variables are:

- METAtmosphere.geo_index_type,
- METAtmosphere.geo_index,
- METAtmosphere.F10,
- METAtmosphere.F10B.

Details on the exact meaning of these variables can be found in the Mathematical Formulation section of this document, as well as the Detailed Design section.

There are three appropriate data class that can be used for the solar activity initialization, and are as follows:

- METAtmosphere_solar_mean_default_data: To simulate mean, average solar activity,
- METAtmosphere_solar_min_default_data: To simulate minimum solar activity,
- METAtmosphere_solar_max_default_data: To simulate maximum solar activity.

The last item to be instantiated is either an AtmosphereState or an METAtmosphereState object. As has been pointed out in this document, either object can be successfully used to calculate basic atmosphere information from an METAtmosphere object. As illustrated in the Detailed Design section of this document, the METAtmosphere object does contains more parameters associated with the calculation of the MET implementation of atmosphere; however, using an AtmosphereState object allows for multiple atmosphere models to be used with the same AtmosphereState object, in the same simulation, which can be useful for simulations involving multiple planets or when different fidelity atmosphere models can be used for different situations around the same planet.

Recommended practice is to instantiate AtmosphereState objects on a per vehicle basis. This is possible because a single Atmosphere derived object can be used with multiple AtmosphereState objects, useful in the common case of more than one vehicle traveling in planetary orbit around the same body.

The first thing that must happen to the METAtmosphere object is to have the current time set. Because the METAtmosphere uses a specific time scale (represented by the JEOD v5.0 TimeUTC object) and because this is not a time scale common to all atmosphere models, the setting of the time for METAtmosphere has been split into a separate function, represented in our example above with the initialization and scheduled job calls:

```
("initialization") atmos.update_time( time_utc);  
(DYNAMICS, "environment") atmos.update_time( time_utc);
```

One thing that must be noted in this simulation is how the METAtmosphere object uses the TimeUTC object. The METAtmosphere object requires the current time, in the UTC timescale, in calendar date, i.e. year, month, day, etc. This requires that the calendar date in the TimeUTC object MUST have been updated before it is sent to the METAtmosphere object. Information on how to update this calendar date can be found in the JEOD v5.0 Time Representations Model Documentation [14].

After the update_time function has been called, all that remains is to invoke the update_state function through either the METAtmosphereState or AtmosphereState object. Since the required parameters, PlanetFixedPosition and Atmosphere (or METAtmosphere) objects, was passed by reference to the AtmosphereState and METAtmosphereState constructors, it is not necessary to pass them to the update_state function. However, overloaded function are provided in the model for backward compatibility. From the earlier example S_define snippet, this code appears, in both initialization and scheduled job form, as:

```
MetAtmosSimObject( jeod::METAtmosphere          & atmos_model_,
                   const jeod::PlanetFixedPosition & pos_,
                   jeod::WindVelocity             * wind_,
                   jeod::RefFrameTrans            * inertial_trans_,
                   jeod::PlanetaryDerivedState     * pfix_pos_)
:
atmos_state(      atmos_model_, pos_),
met_atmos_state(  atmos_model_, pos_),
...
{
  ("initialization") atmos_state.update_state();
  ("initialization") met_atmos_state.update_state();
  (DYNAMICS, "environment") atmos_state.update_state();
  (DYNAMICS, "environment") met_atmos_state.update_state();
  ...
}
```

Note again that only one instantiation of an AtmosphereState type object is needed; either the basic AtmosphereState or the METAtmosphereState. Instantiating and using the METAtmosphereState object has the advantage of the full compliment of parameters associated with the METAtmosphere being available; however, an METAtmosphereState can only compute atmosphere given an METAtmosphere, making it less versatile. An AtmosphereState, on the other hand, can be given any type of Atmosphere derived object and work properly assuming the Atmosphere derived object was properly implemented. As mentioned before, this gives the versatility of changing Atmosphere derived objects in the middle of a simulation, giving the possibility of both vehicles traveling from one planet to another, or using different fidelity atmosphere models in different situations around the same planet.

4.2.2 Wind Velocity

To use the simple Wind Velocity model in an S_define, the following objects/elements must be instantiated, in some form:

- A WindVelocity object,
- An array of doubles, 3 long, representing the position of the point of interest in the inertial reference frame of the planet causing the wind,
- A double representing the altitude of the point of interest, often taken from a PlanetFixed-Position object,
- An AtmosphereState object or an AtmosphereState derived object.

A typical instantiation of the WindVelocity object, as seen in the example code presented earlier, would be:

```
jeod::WindVelocity wind_velocity;  
jeod::WindVelocity_wind_velocity_default_data wind_data;  
...  
("default_data") wind_data.initialize( &wind_velocity);  
...
```

As described in the Analysis section for WindVelocity, the interpolation table to convert from altitude to the rotation velocity scaling factor (as seen in (3.1)) must have memory allocated and be populated with appropriate values. This is most often done with a default data class instance, as shown in the above example. This data was created from [10] and [17], and is most often used with the JEOD v5.0 wind velocity model.

The inertial position of the point of interest will most often be tracked within a reference frame structure [13], usually instantiated by and kept within a DynamicsManager object [2]. Additionally, it may be necessary to instantiate a DerivedState object [15]. Information on these objects can be found in the appropriate documentation.

As mentioned in the list of instantiated objects, the altitude necessary for calling the wind velocity model will most often be pulled from a PlanetFixedState object. This PlanetFixedState object is identical to the one used for the METAtmosphere object in the previous section, and further information on it can be seen there.

Calling the WindVelocity object is then a simple matter, as illustrated below in both initialization and schedule job form:

```
("initialization") atmos_state.update_wind(wind,  
                                             inertial_trans->position,
```

```

        prefix_pos->state.ellip_coords.altitude);
("initialization") met_atmos_state.update_wind(wind,
        inertial_trans->position,
        prefix_pos->state.ellip_coords.altitude);
(DYNAMICS, "environment") atmos_state.update_wind(wind,
        inertial_trans->position,
        prefix_pos->state.ellip_coords.altitude);
(DYNAMICS, "environment") met_atmos_state.update_wind(wind,
        inertial_trans->position,
        prefix_pos->state.ellip_coords.altitude);

```

Similar to the calling of `update_state` for the METAtmosphere model, `update_wind` is called through an `AtmosphereState` or an `AtmosphereState` derived object. As is seen in the example, both an `AtmosphereState` object and an `METAtmosphereState` object can be used with a `WindVelocity` object.

4.3 Extension

This section will explain how to correctly extend the JEOD v5.0 Atmosphere Model and the Wind Velocity model to other implementations.

4.3.1 Atmosphere Model

Typical extension of the generic Atmosphere Model framework involves extending two base classes:

- The `AtmosphereState` class, and
- The `Atmosphere` class.

It should be noted that the implementation of the `METAtmosphereState` and `METAtmosphere` classes is a direct example of this extension, and can be used as a model for future developers.

Extension of the `AtmosphereState` Class

The extension of the `AtmosphereState` class is technically optional. It is only necessary if the developer of the new atmosphere implementation feels the need to give access to information about the atmosphere that is not already included in the `Atmosphere` base class. If this is necessary, then a new class (for illustrative purposes called “`NewAtmosphereState`”) should be created that inherits from `AtmosphereState`.

If the `AtmosphereState` base class is extended, one additional function should be implemented. A new function should overload the `update_state` function, in the following manner:

```

void update_state(                                // RETURN: -- None.
    NewAtmosphereClass * atmos_model, // IN: -- New Atmosphere Model.
    PlanetFixedPosition * pfix_pos    );// IN: -- Current vehicle position.

```

Using the example of the current implementation of METAtmosphereState, this function is now a simple body, checking for a NULL pointer and if the AtmosphereState derived object is active. If these requirements are met, then the appropriate METAtmosphere function is called, updating the atmosphere parameters in the AtmosphereState derived object.

Extension of the Atmosphere Base Class

To extend the Atmosphere base class, a new atmosphere class (for point of illustration called “NewAtmosphere”) should be created that inherits from the Atmosphere class.

There is one function that absolutely must be implemented, as it is pure-virtual). This function, from the Atmosphere class, is shown below:

```

virtual void update_atmosphere(    // RETURN: -- None
    PlanetFixedPosition * position, // In:      -- planet fixed position
    AtmosphereState      * state) = 0; // Out:    -- The AtmosphereState

```

This function supplies the derived Atmosphere class with a generic AtmosphereState. The implementation should then be calculating the generic AtmosphereState information (pressure, density and temperature) and populating the supplied AtmosphereState with that information.

Additionally, if the implementer has chosen to create a “NewAtmosphereState” class, then a function specifically to update that class should also be added, in the following form:

```

void update_atmosphere(          /* RETURN: -- None. */
    PlanetFixedPosition * pfix_pos, /* IN:  -- Geodetic altitude, latitude
                                     and longitude. */
    NewAtmosphereState * state);    /* OUT: -- Where the state results will
                                     be stored. */

```

The implementation for this function should, of course, be calculating the NewAtmosphere parameters and completely filling out the supplied NewAtmosphereState.

Often, an atmosphere model will need more information than is supplied by the generic Atmosphere Model framework. For instance, an additional function was added to the METAtmosphere object, shown below:


```
void update_time(          /* RETURN: -- None. */
    TimeUTC & time_utc); /* IN: -- Time with which to update. */
```

This function was a necessary addition in order to get METAtmosphere knowledge of the current time on the UTC scale. This model can be used for any additional information the NewAtmosphere class needs to fully operate.

4.3.2 Wind Velocity Model

Extending the generic wind velocity framework is a rather simple task, as the expected output is a simple three vector.

A new class, that inherits from WindVelocityBase, must be implemented. Then, the following function must be overridden by the deriving class:

```
virtual void update_wind( // Return: -- none */
    double position[3], /* IN: M position */
    double altitude, /* IN: M Vehicle altitude */
    double wind_inertial[3]); /* OUT: M/s inertial wind velocity */
```

This will cause the correct call to be made when the new wind velocity class is based to the update_wind function of an atmosphere state object.

Note that the wind velocity can also be built straight into an Atmosphere object, and be updated at the same time as the rest of the atmosphere. Additionally, an AtmosphereState object can be tailored, through extension of the AtmosphereState base class, to handle a more complicated wind velocity model. This would be similar to how the AtmosphereState model is extended for different atmosphere models.

Chapter 5

Verification and Validation

5.1 Verification

Inspection atmosphere_1: Top-level inspection

This document structure, the code, and associated files have been inspected, and together satisfy requirement [atmosphere_1](#).

Inspection atmosphere_2: Atmosphere Extensibility

As described in the Extension section of this document, it is possible to extend the Atmosphere Model to different implementations of atmosphere through inheritance. Additionally, the MET specific implementation of atmosphere uses this framework.

This fulfils the requirement [atmosphere_3](#).

Inspection atmosphere_3: Wind Model Verification

The following classes:

```
WindVelocityBase
WindVelocity
```

found in the Atmosphere Model, represent a model of the rigid rotation of Earth's atmosphere of molecules with selectable parameters. This fulfils requirement [atmosphere_4](#).

5.2 Validation

5.2.1 MET Atmosphere

Two different simulations were constructed to verify the performance of the MET model. The first directory (SIM_wind) simply executes the wind model, verifying that the table interpolation algorithm functions correctly.

The second simulation, SIM_MET, runs the MET atmosphere model and comprises 3 distinct tests:

- Confirmation that the MET atmosphere model can be used with a basic *AtmosphereState* as well as with a *METAtmosphereState*. Instances of both are created in this sim; it is confirmed that the components of the *AtmosphereState* that are common to both classes match between the two instances.
- The runs labeled *RUN_*_MET_VER* are intended to verify the MET atmosphere-state. These runs log the full MET Atmosphere state.
- The runs labeled *RUN_*_GRAM** are intended to validate the model against a set of published GRAM model data.
- The runs labeled *RUN_*_JAC** are intended to validate the model against a set of published Jacchia model data.

Within each run grouping, there are two or three runs, identified with a *T01*, *T02*, or *T03* label. For example, *RUN_T01_JAC_COMP* is the first Jacchia comparison run. In this convention, the # ranges from 01-02 or 03. The run numbers associated with a particular test are called out in the test bullet.

Test atmosphere_1: MET Comparison with GRAM 99 results

Purpose:

SIM directory: SIM_MET

RUN directory: SET_test/RUN_T01_MET_VER

The purpose of this test is to verify that the model agrees with published data from the GRAM 99 model as documented in the GRAM 99 user's guide, [9].

Requirements:

By passing this test, the MET module partially satisfies requirement [atmosphere.2](#)

Procedure:

This test is designed to compare the density, pressure and temperature computed by the MET model with results from the GRAM 99 model. The GRAM 99 model is an amalgam of several different atmosphere models of which the MET models is the upper portion. However, in the published results from the GRAM model, only the results from 120 to 140 km that use the MET model were available.

Results:

Figure 5.1 shows a plot of the results of the density comparison between Trick's MET model and the published GRAM results.

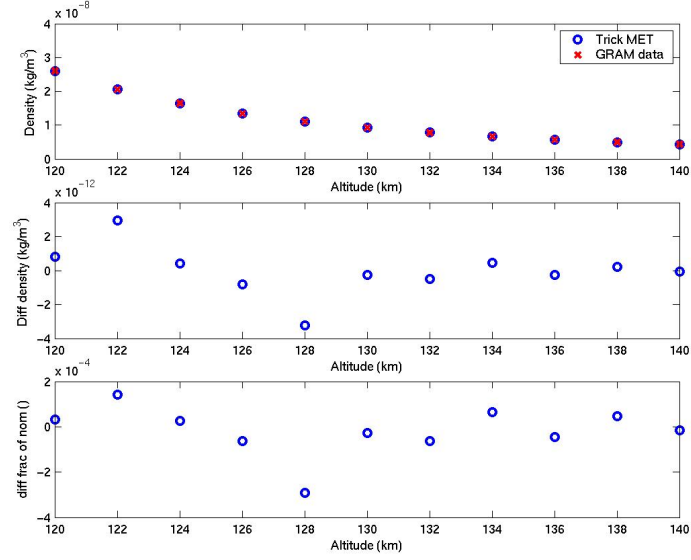


Figure 5.1: Density Comparison Between MET and Published GRAM Data

As Figure 5.1 shows, the comparison between the MET model and the GRAM outputs is excellent. In the documentation, the density is only given to four decimal places and this is why the comparison is only accurate to a fraction of this fourth decimal place.

Figures 5.2 and 5.3 show the results of a comparison between the pressure and temperature output from the GRAM and published results.

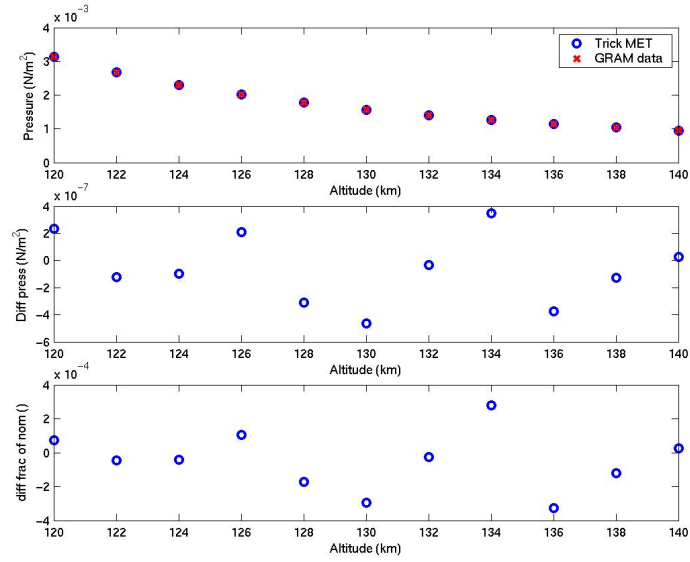


Figure 5.2: Pressure Comparison Between MET and Published GRAM Data

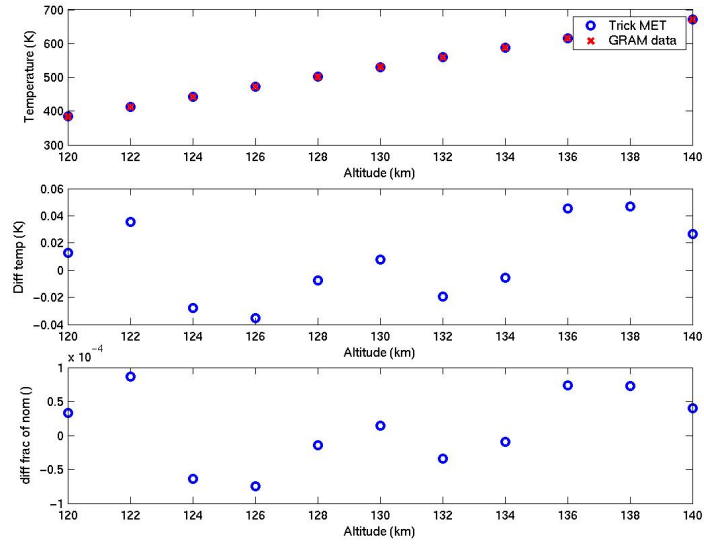


Figure 5.3: Temperature Comparison Between MET and Published GRAM Data

Both of these plots also exhibit the expected behavior. In both cases, the data was only available to 4 decimal places.

Test atmosphere_2: MET Comparison with MSIS results

Purpose:

SIM directory: SIM_MET

RUN directory: SET_test/RUN_T02_MET_VER

The purpose of this test is to compare the output of the Trick MET model with the output from the MSIS model.

Requirements:

By passing this test, the MET module partially satisfies requirement [atmosphere_2](#)

Procedure:

This test is designed to compare the density computed by the MET model with results from the MSIS model. The MSIS model is another atmosphere model whose results are readily available although the results should not compare with the MET model as accurately as the GRAM model does.

Results:

Figure 5.4 shows a plot of a comparison between the density output from the MET model and the density output from the MSIS model.

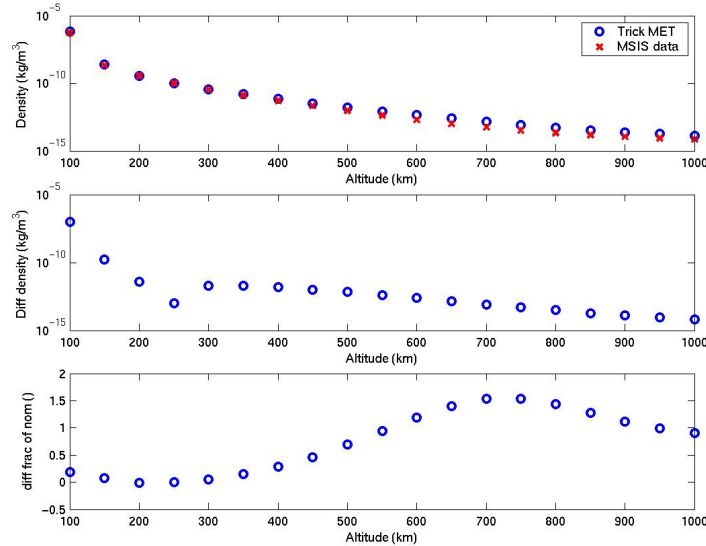


Figure 5.4: Density Comparison Between MET and MSIS Data

As this plot shows, the agreement between the MSIS data and the MET data is not nearly as good as the agreement between MET and GRAM. However, the MET and MSIS model are both very consistent with each other throughout the range of altitudes used. And while they are occasionally off from each other by as much as the MSIS density, this occurs when the value for the density is extremely small.

Test atmosphere_3: MET Comparison with Jacchia results

Purpose:

SIM directory: SIM_MET

RUN directory: SET_test/RUN_T01_JAC_COMP

RUN directory: SET_test/RUN_T02_JAC_COMP

The purpose of this test is to compare the results of the MET model, the Jacchia model, and the MSIS model to determine the consistency of the MET model with respect to the other two and to determine if there is an advantage to using the MET model over the Jacchia model.

Requirements:

By passing this test, the MET module partially satisfies requirement [atmosphere_2](#)

Procedure:

This test is designed to compare the density computed by the MET model with results from the Jacchia model. The Jacchia model is another atmosphere model available in Trick although it has not been verified. The output from both models was compared with the output from the MSIS model to determine whether or not there was a benefit to using the Jacchia model over the MET model.

Results:

Figure 5.5 shows a plot of a comparison between the MET and MSIS models and the Jacchia and MSIS models. This plot is designed to quantify whether or not and how much of an advantage there exists in using one model over the other.

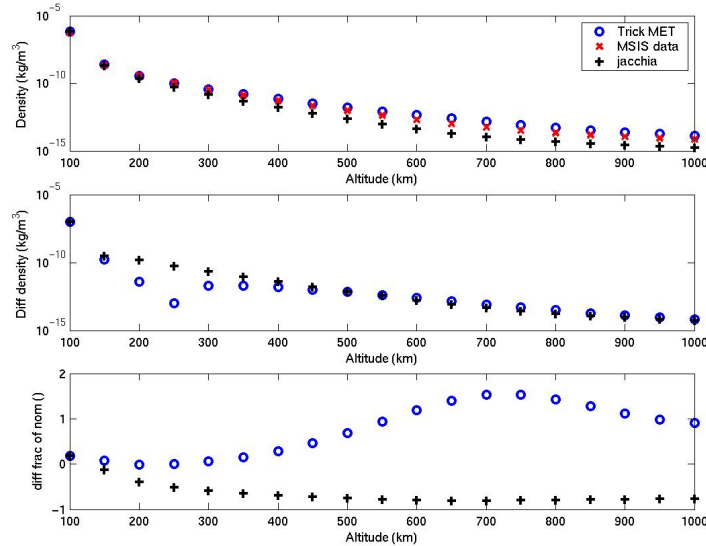


Figure 5.5: Density Comparison Between MET, Jacchia, and MSIS Data

As this plot shows, the Jacchia model actual exhibits more agreement with the MSIS model

for the majority of the altitude range. However, for the critical range of altitudes where atmospheric drag is a factor for rendezvous analyses, (0-500 km), the performance of the two models compared to the MSIS data. Figure 5.6 shows a comparison plot between the three models for this critical range.

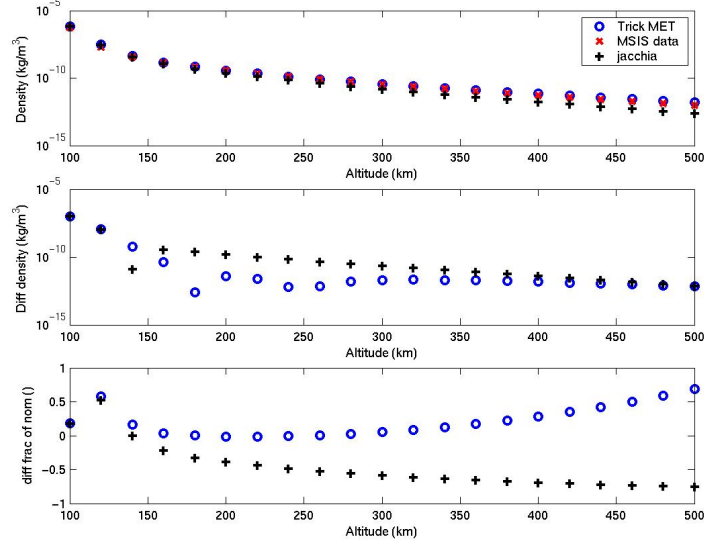


Figure 5.6: Density Comparison (100-500km) Between MET, Jacchia, and MSIS Data

As this plot shows, there is a slight advantage gained by using the MET model instead of the Jacchia model for this range. More importantly, it can be said from these results that the agreement between Jacchia and MET is quite good when the level of error of atmosphere estimation at these altitudes is taken into account. The added complexity of the Jacchia model and the increased overhead required for its use certainly make the argument about why the MET model should be used over the Jacchia model. The MET model is much simpler to use in an S_define and relies on many fewer models and provides at least as good an estimation of the Jacchia model and for the range of altitudes used for RPOC work, it provides better agreement with MSIS.

Test atmosphere_4: MET Comparison with FORTRAN GRAM results

Purpose:

SIM directory: SIM_MET
 RUN directory: SET_test/RUN_T01_GRAM_MET
 RUN directory: SET_test/RUN_T02_GRAM_MET
 RUN directory: SET_test/RUN_T03_GRAM_MET

The purpose of this test is to compare the MET model with a more representative set of data from the GRAM model. There is a version of the GRAM model set up to run in Trick available. This model is FORTRAN code and has been used for several projects and

is considered to be an accurate model. Furthermore, it is very unlikely that MET and this model would both agree and not be representative of the true MET model since they were programmed independently.

Requirements:

By passing this test, the MET module partially satisfies requirement [atmosphere_2](#)

Procedure:

This test is designed to compare the output of the GRAM and MET model for a full range of altitudes, latitudes, and longitudes. Three test cases were run here and the results are shown below. The altitude was varied from 100 to 1500 km above the surface of the ellipsoid. The latitude was varied from -90 to 90 degrees. The longitude was varied from -180 to 180 degrees.

Results:

For each test, the density, pressure, and temperature were compared with each other to determine the level of variation. Figures 5.7, 5.8, and 5.9 show plots of the density, pressure, and temperature variation as a function of the variation in altitude used for the first test.

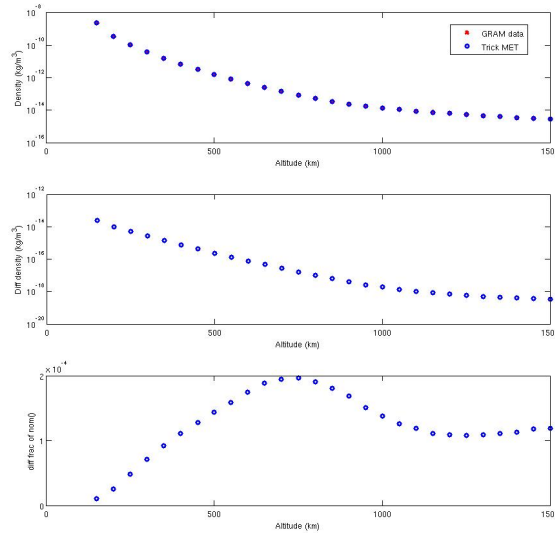


Figure 5.7: Density Comparison Between MET and GRAM for Altitude Variation

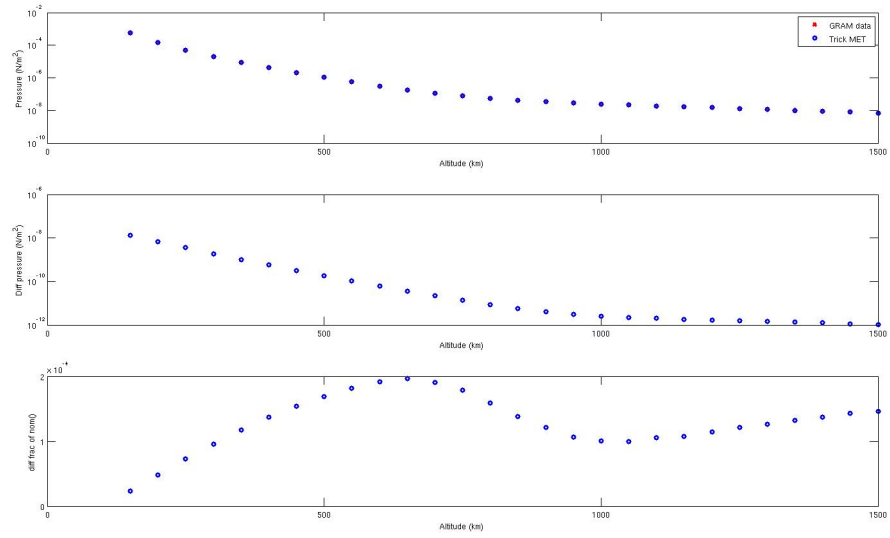


Figure 5.8: Pressure Comparison Between MET and GRAM for Altitude Variation

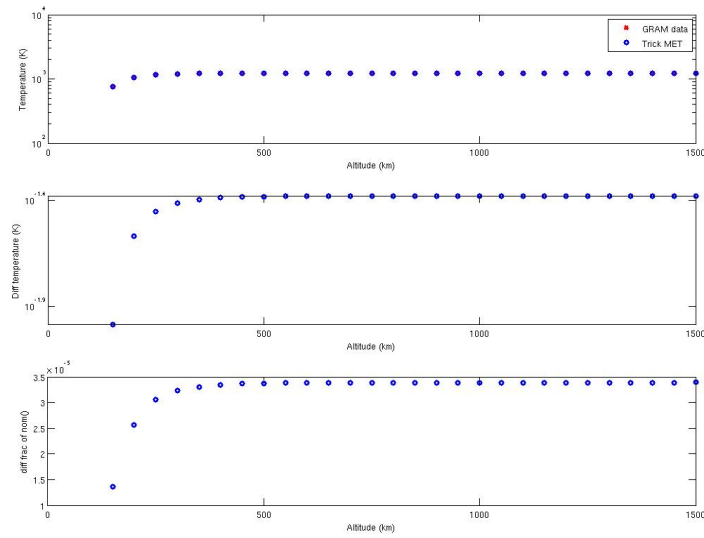


Figure 5.9: Temperature Comparison Between MET and GRAM for Altitude Variation

As these plots show, for the altitude variation test, the results all agree to approximately 4 significant digits. Figures 5.10, 5.11, and 5.12 show the results for the test that varied the latitude of the spacecraft.

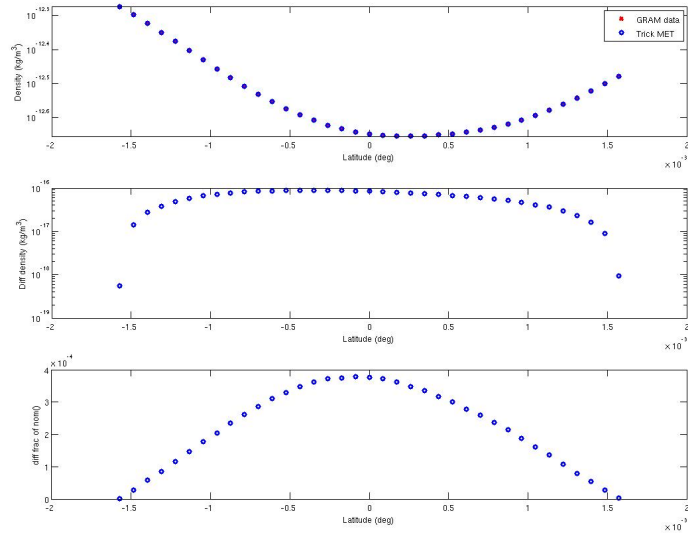


Figure 5.10: Density Comparison Between MET and GRAM for Latitude Variation

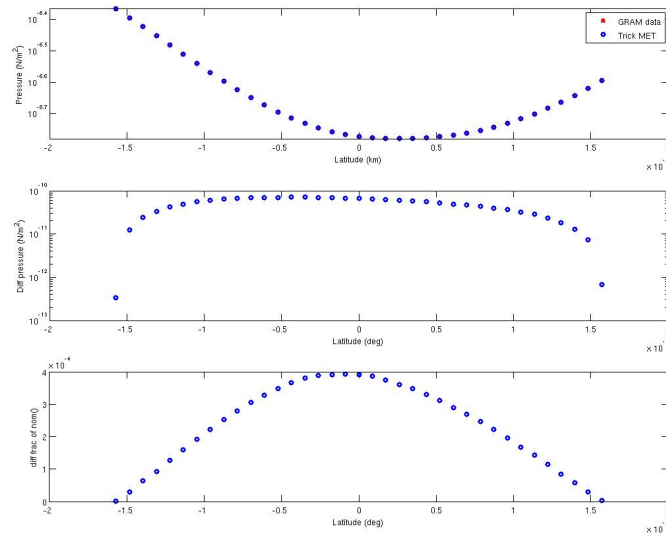


Figure 5.11: Pressure Comparison Between MET and GRAM for Latitude Variation

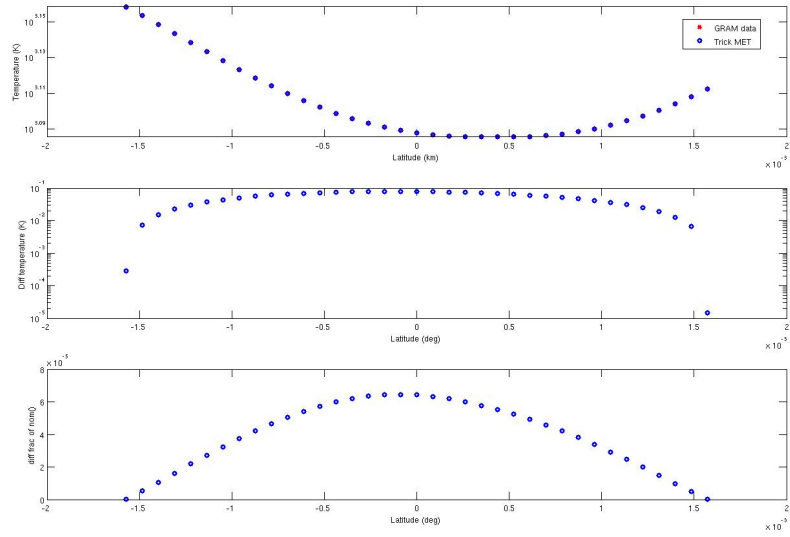


Figure 5.12: Temperature Comparison Between MET and GRAM for Latitude Variation

As these plots show, the results of the test on spacecraft latitude were also consistent to approximately 4 significant digits. In this case, the reference altitude was chosen as 650 meters because that altitude had a higher general level of error in the first set of plots. Figures 5.13, 5.14, and 5.15 show the results for the test that varied the longitude of the spacecraft.

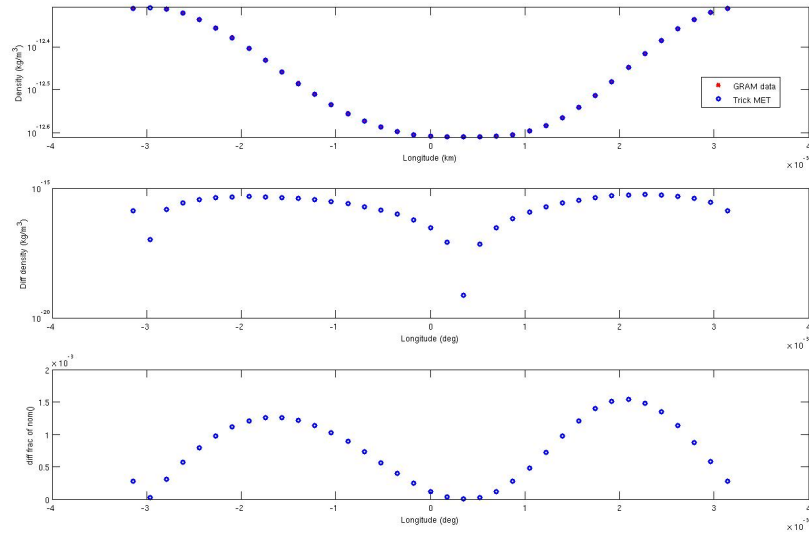


Figure 5.13: Density Comparison Between MET and GRAM for Longitude Variation

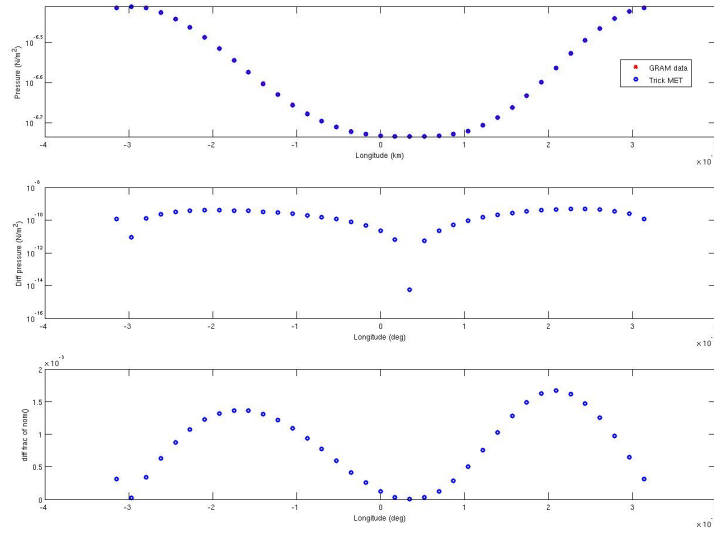


Figure 5.14: Pressure Comparison Between MET and GRAM for Longitude Variation

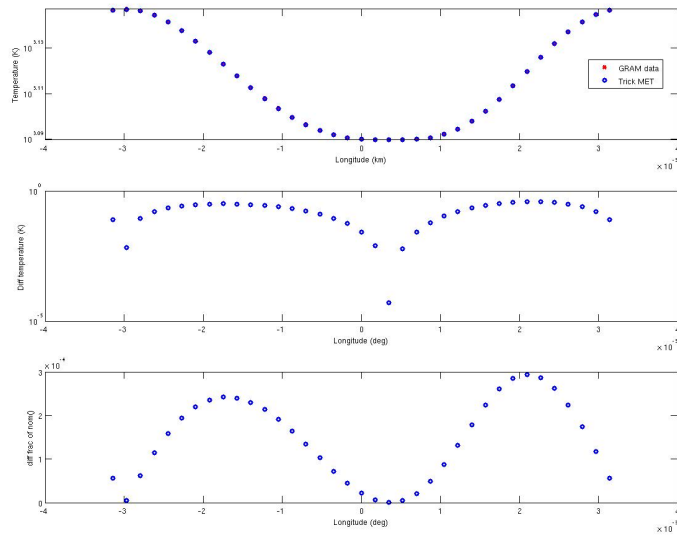


Figure 5.15: Temperature Comparison Between MET and GRAM for Longitude Variation

From all of these plots, it is apparent that the MET model used in Trick matches up with the GRAM model found in the (GRAM/MET 99) to three to four digits. Because the atmosphere parameters are never known to this level of precision, this level of agreement is considered more than accurate for the model.

Additionally, there is a known discrepancy between the MET mode used for JEOD and the GRAM model used here for comparison. As stated in the JEOD 1.52 documentation for this model [6], it was discovered that there were small discontinuities in the output of the GRAM model, occurring at each minute. This was because the GRAM model used was constructed to ignore the “seconds” parameter from its inputted calendar date. Thus, the source code for the JEOD implementation of MET, which also originally had this peculiarity, was changed to include the second parameter into the calculation. Prior to this change, the models matched to six digits; they now only match to 3-4 digits, but because this implementation appears to be more consistent and stable, it was decided that this level of error was acceptable.

5.3 Metrics

5.3.1 Code Metrics

Table 5.1 presents coarse metrics on the source files that comprise the model.

Table 5.1: Coarse Metrics

File Name	Number of Lines			
	Blank	Comment	Code	Total
MET/include/MET_atmosphere.hh	64	128	112	304
MET/include/MET_atmosphere_state.hh	21	49	26	96
MET/include/MET_atmosphere_state_vars.hh	15	34	29	78
MET/include/class_declarations.hh	9	22	13	44
MET/src/MET_atmosphere.cc	170	659	502	1331
MET/src/MET_atmosphere_state.cc	20	55	35	110
MET/src/MET_atmosphere_state_vars.cc	21	52	70	143
base_atmos/include/atmosphere.hh	19	41	23	83
base_atmos/include/atmosphere_messages.hh	24	47	18	89
base_atmos/include/atmosphere_state.hh	24	49	33	106
base_atmos/include/class_declarations.hh	9	22	10	41

Continued on next page

Table 5.1: Coarse Metrics (continued from previous page)

File Name	Number of Lines			
	Blank	Comment	Code	Total
base.atmos/include/wind_velocity.hh	26	54	23	103
base.atmos/include/wind_velocity_base.hh	19	35	17	71
base.atmos/src/atmosphere_messages.cc	16	25	12	53
base.atmos/src/atmosphere_state.cc	34	67	83	184
base.atmos/src/wind_velocity.cc	21	69	85	175
base.atmos/src/wind_velocity_base.cc	20	40	26	86
MET/data/include/met_data_wind_velocity.hh	9	12	17	38
MET/data/include/solar_max.hh	7	8	10	25
MET/data/include/solar_mean.hh	7	8	10	25
MET/data/include/solar_min.hh	7	8	10	25
MET/data/src/data_met_wind_velocity.cc	10	30	40	80
MET/data/src/solar_max.cc	15	19	15	49
MET/data/src/solar_mean.cc	15	19	15	49
MET/data/src/solar_min.cc	15	19	15	49
Total	617	1571	1249	3437

Table 5.2 presents the extended cyclomatic complexity (ECC) of the methods defined in the model.

Table 5.2: Cyclomatic Complexity

Method	File	Line	ECC
jeod::METAtmosphere Chemical::~MET AtmosphereChemical ()	MET/include/MET_atmosphere.hh	70	1

Continued on next page

Table 5.2: Cyclomatic Complexity (continued)

Method	File	Line	ECC
jeod::METAtmosphere Thermal::~MET AtmosphereThermal ()	MET/include/MET_ atmosphere.hh	94	1
jeod::METAtmosphere::~~ME TAtmosphere ()	MET/include/MET_ atmosphere.hh	260	1
jeod::METAtmosphere:: update_time (const TimeU TC & time_utc)	MET/include/MET_ atmosphere.hh	269	1
jeod::METAtmosphereState:: ~METAtmosphereState ()	MET/include/MET_ atmosphere.state.hh	65	1
jeod::METAtmosphere Chemical::METAtmosphere Chemical ()	MET/src/MET_ atmosphere.cc	75	1
jeod::METAtmosphere Thermal ()	MET/src/MET_ atmosphere.cc	102	1
jeod::METAtmosphere ()	MET/src/MET_ atmosphere.cc	119	1
jeod::METAtmosphere Thermal::update ()	MET/src/MET_ atmosphere.cc	164	1
jeod::METAtmosphere Thermal::compute_ temperature (double altitude_km_in)	MET/src/MET_ atmosphere.cc	190	2
jeod::METAtmosphere:: update_atmosphere (const PlanetFixedPosition * pfix_ pos, AtmosphereState * ext_state)	MET/src/MET_ atmosphere.cc	278	2
jeod::update_atmosphere ()	MET/src/MET_ atmosphere.cc	313	2
jeod::update_atmosphere (state.density)	MET/src/MET_ atmosphere.cc	339	2
jeod::METAtmosphere:: modify_densities ()	MET/src/MET_ atmosphere.cc	386	4
jeod::METAtmosphere:: compute_solar_angles ()	MET/src/MET_ atmosphere.cc	409	11
jeod::METAtmosphere:: compute_exospheric_ temperature ()	MET/src/MET_ atmosphere.cc	599	5

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Table 5.2: Cyclomatic Complexity (continued)

Method	File	Line	ECC
jeod::METAtmosphere:: jacchia ()	MET/src/MET_ atmosphere.cc	741	9
jeod::METAtmosphere:: compute_seasonal_latitude_ variation ()	MET/src/MET_ atmosphere.cc	954	2
jeod::METAtmosphere:: compute_seasonal_lat_ variation_He ()	MET/src/MET_ atmosphere.cc	1019	2
jeod::METAtmosphere:: atmos_MET_FAIR5 ()	MET/src/MET_ atmosphere.cc	1076	1
jeod::METAtmosphere:: compute_mol_wt (double altitude_km_in)	MET/src/MET_ atmosphere.cc	1133	4
jeod::METAtmosphere:: apply_gauss_quadrature (int altitude_index_start, double altitude_end)	MET/src/MET_ atmosphere.cc	1210	8
jeod::METAtmosphereState:: METAtmosphereState ()	MET/src/MET_atmosphere_ state.cc	52	1
jeod::METAtmosphereState:: METAtmosphereState (ME TAtmosphere & met_ atmos_, const PlanetFixed Position & pfix_pos_)	MET/src/MET_atmosphere_ state.cc	60	1
jeod::METAtmosphereState:: update_state (MET Atmosphere * atmos_ model_, const PlanetFixed Position * pfix_pos_)	MET/src/MET_atmosphere_ state.cc	78	3
jeod::METAtmosphereState:: update_state ()	MET/src/MET_atmosphere_ state.cc	96	3
jeod::METAtmosphereState Vars::METAtmosphere StateVars ()	MET/src/MET_atmosphere_ state_vars.cc	45	1
jeod::METAtmosphereState Vars::METAtmosphere StateVars (Atmosphere & atmos_model_, const Planet FixedPosition & pfix_pos_)	MET/src/MET_atmosphere_ state_vars.cc	61	1

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Table 5.2: Cyclomatic Complexity (continued)

Method	File	Line	ECC
jeod::METAtmosphereState Vars::~~METAtmosphere StateVars ()	MET/src/MET_atmosphere_ state_vars.cc	80	1
jeod::METAtmosphereState Vars::METAtmosphere StateVars (const MET AtmosphereStateVars& rhs)	MET/src/MET_atmosphere_ state_vars.cc	91	1
jeod::METAtmosphereState Vars::operator = (const ME TAtmosphereStateVars& rhs)	MET/src/MET_atmosphere_ state_vars.cc	114	2
jeod::Atmosphere:: Atmosphere ()	base_atmos/include/ atmosphere.hh	53	1
jeod::Atmosphere::~~ Atmosphere ()	base_atmos/include/ atmosphere.hh	58	1
jeod::AtmosphereState:: AtmosphereState ()	base_atmos/src/atmosphere_ state.cc	35	1
jeod::AtmosphereState:: AtmosphereState (Atmosphere & atmos_, const PlanetFixedPosition & pfix_pos_)	base_atmos/src/atmosphere_ state.cc	49	1
jeod::AtmosphereState::~~ AtmosphereState ()	base_atmos/src/atmosphere_ state.cc	64	1
jeod::AtmosphereState:: AtmosphereState (const AtmosphereState& rhs)	base_atmos/src/atmosphere_ state.cc	77	2
jeod::AtmosphereState:: operator = (const AtmosphereState& rhs)	base_atmos/src/atmosphere_ state.cc	99	2
jeod::AtmosphereState:: update_state (Atmosphere * atmos_model_, PlanetFixed Position * pfix_pos_)	base_atmos/src/atmosphere_ state.cc	124	3
jeod::AtmosphereState:: update_state ()	base_atmos/src/atmosphere_ state.cc	144	3

Continued on next page

Table 5.2: Cyclomatic Complexity (continued)

Method	File	Line	ECC
jeod::AtmosphereState:: update_wind (WindVelocity * wind_vel, double inrtl_ pos[3], double altitude)	base_atmos/src/atmosphere_ state.cc	163	3
jeod::WindVelocity::Wind Velocity (void)	base_atmos/src/wind_ velocity.cc	40	1
jeod::WindVelocity::~~Wind Velocity (void)	base_atmos/src/wind_ velocity.cc	56	3
jeod::WindVelocity::update_ wind (double inertial_ pos[3], double altitude, double wind_inertial[3])	base_atmos/src/wind_ velocity.cc	71	13
jeod::WindVelocityBase:: WindVelocityBase (void)	base_atmos/src/wind_ velocity_base.cc	34	1
jeod::WindVelocityBase::~~ WindVelocityBase (void)	base_atmos/src/wind_ velocity_base.cc	46	1
jeod::WindVelocityBase:: update_wind (double[3], double, double[3])	base_atmos/src/wind_ velocity_base.cc	61	1

5.4 Requirements Traceability

Table 5.3: Requirements Traceability

Requirement	Inspection and Testing
atmosphere_1 - Top-level Requirements	Inspection atmosphere_1
atmosphere_2 - MET Atmosphere	Test atmosphere_1 Test atmosphere_2 Test atmosphere_3 Test atmosphere_4
atmosphere_3 - Atmosphere Extensibility	Inspection atmosphere_2
atmosphere_4 - Wind Model	Inspection atmosphere_3

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