

JSC Engineering Orbital Dynamics Surface Model

Simulation and Graphics Branch (ER7)
Software, Robotics, and Simulation Division
Engineering Directorate

Package Release JEOD v5.1

Document Revision 1.2
July 2023



National Aeronautics and Space Administration
Lyndon B. Johnson Space Center
Houston, Texas

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Abstract

Many environmental effects can interact with a vehicle in orbit. Often, to accurately model these effects, models of the surface geometry of the vehicle are necessary. It is often useful to be able to use one surface geometry to calculate many different environmental interactions with the vehicle. Additionally, it is important to allow both for new interactions to be applied to existing surface models, as well as for the extension of new ways of modeling the surface geometry.

The Surface Model gives an extensible framework for representing the surface geometry of a vehicle. This framework can be used to produce models appropriate for calculating any user defined environmental interaction. Additionally, it is extensible to user defined representations of surface geometry.

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Chapter 1

Introduction

1.1 Purpose and Objectives of the Surface Model

The JEOD Surface Model gives an extensible framework for specifying general models of vehicle surface geometry. These models can then be converted to “interaction specific” (applying to only one type of environmental interaction, such as aerodynamic or radiation forces) surface models. The extensible framework allows for new methods of modeling the general surface geometry to be implemented, as well as allowing for extension to any other user specified interaction.

The Surface Model can either be made up of individual components that remain fixed with respect to the vehicle structure, or it can have components that are allowed to move with respect to the vehicle structure. This optional ability to move components with respect to the vehicle structure is accomplished by defining position and orientation of surface model components with respect to atomic mass components in a mass tree [9]. The mass tree can then be updated, and the surface model will update its own geometry accordingly. This feature can be used to model any vehicle surface feature that will change with respect to time, such as the articulation of solar arrays or the movements of a robotic arm.

1.2 Context within JEOD

The following document is parent to this document:

- *JSC Engineering Orbital Dynamics* [4]

The Surface Model forms a component of the utilities suite of models within JEOD v5.1. It is located at `models/utis/surface_model`.

1.3 Document History

Author	Date	Revision	Description
Andrew Spencer	November, 2009	1.0	Initial Version
Andrew Spencer	October, 2010	1.1	Added Articulation, metrics
Andrew Spencer	February, 2012	1.2	Added Trick 10 Allocation Information

1.4 Document Organization

This document is formatted in accordance with the NASA Software Engineering Requirements Standard [5].

The document comprises chapters organized as follows:

Chapter 1: Introduction -This introduction describes the objective and purpose of the Surface Model.

Chapter 2: Product Requirements -The requirements chapter describes the requirements on the Surface Model.

Chapter 3: Product Specification -The specification chapter describes the architecture and design of the Surface Model.

Chapter 4: User Guide -The user guide chapter describes how to use the Surface Model.

Chapter 5: Inspections, Tests, and Metrics -The inspections, tests, and metrics describes the procedures and results that demonstrate the satisfaction of the requirements for the Surface Model.

Chapter 2

Product Requirements

This chapter will describe the requirements for the Surface Model.

Requirement SM_1: Top-level requirement

Requirement:

This model shall meet the JEOD project requirements specified in the JEOD v5.1 [top-level document](#).

Rationale:

This model shall, at a minimum, meet all external and internal requirements applied to the JEOD v5.1 release.

Verification:

Inspection

Requirement SM_2: Geometric Modeling

Requirement:

The Surface Model shall supply a method for representing the geometry of a vehicle surface.

Rationale:

The basic requirement of the surface model is to represent the geometry of a vehicle, and this representation is useful in orbital simulations.

Verification:

The verification for this item shall be done by inspection.

Requirement SM_3: Environmental Interaction

Requirement:

The Surface Model shall supply functionality for interactions between the surface of a vehicle and its environment.

Rationale:

Environmental interactions with the vehicle are necessary for orbit simulations, and a geometrical surface model can aid in the calculation of these interactions.

Verification:

The verification for this item shall be done by a demonstration test.

*Requirement SM_4: Extensible Geometrical Modeling***Requirement:**

The Surface Model shall create an extensible method for modeling the geometry of a surface.

Rationale:

Users may want to specify new and unforeseen methods for modeling a surface. The framework should be able to handle this.

Verification:

The verification for this item shall be done by a demonstration test.

*Requirement SM_5: Extensible to Environmental Interactions***Requirement:**

The Surface Model shall be extendable to different environmental interactions.

Rationale:

The Surface Model should be useful in the context of many different environmental interactions, including those specified by the end user.

Verification:

The verification for this item shall be done by a demonstration test.

*Requirement SM_6: Re-use of Models***Requirement:**

One surface model representation of a vehicle shall be useable with many different environmental interactions at the same time.

Rationale:

The user should not have to recreate the same geometrical surface model in the same simulation to be used with different environmental interactions.

Verification:

The verification for this item shall be done by a demonstration test.

Requirement SM_7: Articulation

Requirement:

The Surface Model shall provide the ability to make its geometry consistent with the geometry embodied in a mass tree.

Rationale:

The Surface Model geometry, if consistent with a mass tree's, would then reflect any changes made to the mass tree geometry, allowing for changing Surface Model geometry including articulation and other movements.

Verification:

The verification for this item shall be done testing.

Chapter 3

Product Specification

3.1 Conceptual Design

The JEOD Surface Model is designed to give an extensible framework for both describing the geometry of a vehicle, as well as calculating environmental interactions with that geometry.

First, a geometry only surface is specified, using what this model refers to as “facets”. These facets are a very general concept and can accomodate any user defined representation of a part of a vehicle. One example is the FlatPlate representation described below, which models a part of the vehicle as a flat surface with only an area, position, and normal vector from the surface.

Then, from this pure geometry representation, an “interaction-specific” surface model can be created. This interaction specific version will share the geometry of the surface it is created from, but with the added functionality of calculating some user defined environmental interaction such as aerodynamics or radiation pressure.

This design gives many advantages to the end user:

- Allows different interaction models to be created from the same basic surface model,
- Allows for complete extensibility of the basic surface model,
- Allows the interaction specific surface models to be extended to any user defined interaction.

Each facet found in a surface model will - in an interaction specific surface model created from that geometric model - have an interaction specific equivalent facet. This equivalent will know everything about the original geometric Facet, but will also have the ability to calculate a specific interaction’s effects on itself.

This interaction specific facet is created from the original facet, using interaction facet specific parameters specified by the user at runtime, through use of an interaction facet factory, a concept that will be described below. An illustration of this process can be seen below in Figure 3.1.

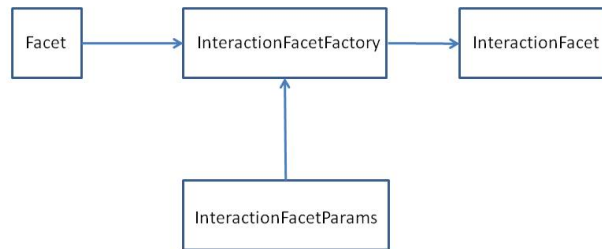


Figure 3.1: An interaction specific facet is created from a general facet, using a set of facet parameters

The process shown in Figure 3.1 is encapsulated within an interaction surface factory, which creates an interaction specific surface from a general surface. This interaction surface factory will be loaded at runtime by the user with the appropriate interaction facet factories and facet parameter objects necessary to fully create the interaction specific surface from the original geometry only surface model. An illustration of this process can be seen below in Figure 3.2.

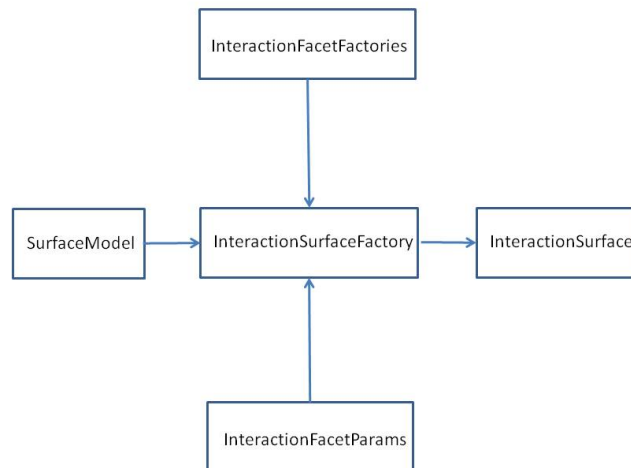


Figure 3.2: An interaction specific surface is created from a general surface, using a set of facet parameters and interaction facet factories

The Surface Model can be split into three parts:

- General Surface Geometry Classes,
- Interaction Specific Classes, and
- Factory Classes, those that create interaction specific classes from general surface geometry classes.

The following sections will describe these groups of classes.

3.1.1 General Surface Geometry Classes

This section will describe the classes associated with establishing a general surface geometry.

Facet

The Facet class is the basic building block of the surface model geometry. A Facet specifies actual geometry of a vehicle. How big of a slice of geometry a Facet represents is up to the user; a single facet can be a complete representation of a vehicle, or just a small component. This gives flexibility to the end user in how they wish to represent the geometry of the vehicle.

Facet geometry can be described in two ways. One option is the specifying the geometry directly in the user desired structural frame of the vehicle. The facet geometry can also be specified relative to the structural reference frame inherently contained in a user supplied MassBody object [9], thus tying each facet in the model to a MassBody in a mass body tree. In this second case, the position and orientation of the facet in the user desired structural frame will then be calculated, where the desired structural frame is defined as being the structural frame of a MassBody object in the same mass body tree as the one tied to the facet. This allows for re-positioning of facets relative to one another or to the structural reference frame during run time, merely by adjusting the relative states of MassBodys in the mass body tree. Note that the articulation option is only available for Facet (and classes deriving from Facet) that have been specifically designed to support articulation. Currently, the only JEOD supplied Facet that supports articulation is the FlatPlate class. However, a user can add articulation to any Facet derived type simply by inheriting from the type and implementing the correct functions, as described in the Users Guide of this document.

Additional flexibility is given because Facet is intended to be a base class for other classes, thus it can be derived from and have user desired parameters attached to it. An example of this is FlatPlate, described momentarily, which inherits from the Facet class and adds its own necessary parameters. Thus, new types of facets can be created by inheriting from Facet. Creating facets in this way is the suggested usage when using the Surface Model.

SurfaceModel

The SurfaceModel class represents the complete geometry of a vehicle. It contains a list of pointers to Facet objects (pointers in order to take advantage of types inheriting from Facet and that allow

multiple types of facets to be used within the same SurfaceModel object). These individual facets make up the complete geometry of the surface model, and SurfaceModel is thus a containing class for a list of Facet derived objects.

FlatPlate

The FlatPlate class is an inheriting object from Facet. It represents a flat plate form of surface geometry, and includes information about the flat plate's area and normal vector.

The FlatPlate class inherits from the Facet class, and fully implements all Facet functionality. Its geometry can be specified either in a user defined structural frame, or using the interface to a MassBody tree as described in the Facet class description and in the Users Guide of this document.

FlatPlateThermal

The FlatPlateThermal class extends the FlatPlate class with the Thermal-Rider Model [11]. Further information about this functionality can be found in the appropriate documentation.

SurfaceModelMessages

The SurfaceModelMessages class enumerates messages associated with warnings and failures of the Surface Model.

3.1.2 Interaction Specific Classes

The interaction specific classes of the Surface Model are designed to mirror the pure geometry classes, while adding information and functionality associated with a specific “interaction.” Interaction in this usage refers to a specific environmental interaction with the vehicle, such as aerodynamics or radiation pressure, however, it can refer to anything that will successfully fit into the presented framework.

InteractionFacet

The InteractionFacet is the interaction specific equivalent of the Facet class. For any particular interaction desiring to use the Surface Model, an InteractionFacet inheriting class will be created. Interaction specific equivalent classes for facet types (classes inheriting from the Facet class) can then be created.

For example, the JEOD Aerodynamics model [7] creates an InteractionFacet inheriting class AeroFacet, which adds the pure virtual functionality for calculating aerodynamic forces. Then, a new class is inherited from AeroFacet, FlatPlateAeroFacet, which is the aerodynamic interaction equivalent of flat plate. When an aerodynamic interaction specific surface model is created from a surface model containing a flat plate facet, the aerodynamic specific surface model will contain a FlatPlateAeroFacet equivalent for each FlatPlate object found in the original SurfaceModel.

InteractionSurface

The InteractionSurface class is a pure virtual base class that defines the interface for interaction specific surface models. Any new interaction that is meant to interact with the Surface Model will create an interaction specific class inheriting from InteractionSurface. This inheriting class will then contain an array of pointers to the appropriate class that inherits from InteractionFacet, and this array will then be populated when the interaction surface is created from a base SurfaceModel object.

An example of this inheritance can be found in the JEOD Aerodynamics Model [7]. AeroSurface inherits from InteractionSurface, and contains an array of pointers to AeroFacet objects. These pointers will then be populated with the correct type of aerodynamic specific interaction facets when the AeroSurface is created from a SurfaceModel object.

FacetParams

The FacetParams class is a base class for specifying interaction specific parameters that are necessary when creating an interaction specific facet. A user will inherit from FacetParams, populating the class with parameters necessary for the specific facet type and interaction in question. These parameters will then be used to create the InteractionFacet from the Facet, and will be matched to facets in a SurfaceModel object by name lookup. These parameters are especially useful for values associated with a specific type of interaction facet that need to be specified by the user at runtime.

3.1.3 Factory Classes

This section will describe the classes used to create both specific interaction surfaces from general surfaces, as well as specific interaction facets from general facets.

InteractionSurfaceFactory

The InteractionSurfaceFactory is a utility class that creates an interaction specific surface model from a basic, geometry only surface model. It is meant to be a base class for an interaction specific surface factory, creating surfaces for a particular interaction from base SurfaceModel objects. These objects are able to, given the correct inputs, create their specific interaction surface models from a base SurfaceModel object.

InteractionFacetFactory

The InteractionFacetFactory is a pure virtual class. It creates an interface for classes which will take a specific Facet type (such as FlatPlate), and create from it an interaction specific version of that Facet (for the aerodynamics interaction, a FlatPlate will be turned into a FlatPlateAeroFacet, an aerodynamic specific version of FlatPlate). These classes will be vital utility classes for the InteractionSurfaceFactory, which will create an interaction specific surface from a basic geometric surface by creating interaction specific facets from all of the basic surface's facets.

3.1.4 Additional Classes

There are additional classes found in the Surface Model directory, such as PlatePolygon, PlateEllipse, and others. While these files are found in the Surface Model directory, they are mainly Facet derived classes created for the JEOD Contact Model [10]. Please see the appropriate documentation for additional information, and note that these Facet derived classes do not support the articulation feature of the Surface Model.

3.2 Mathematical Formulations

There is no accompanying mathematical formulation for the Surface Model. All mathematical formulations will occur in interaction specific implementations of the surface model. Examples of this can be seen in the Aerodynamics Model [7] and the Radiation Pressure Model [12].

3.3 Detailed Design

The complete API for the Surface Model can be found in the *Reference Manual* [1].

3.4 Inventory

All Surface Model files are located in `${JEOD_HOME}/models/utis/surface_model`. Relative to this directory,

- Model header and source files are located in model `include` and `src` subdirectories. See table ?? for a list of these configuration-managed files.
- Model documentation files are located in the model `docs` subdirectory. See table ?? for a list of the configuration-managed files in this directory.

Chapter 4

User Guide

The Instructions for Simulation Users section of the user guide is intended primarily for users of pre-existing simulations. It contains:

- A description of how to modify Surface Model variables after the simulation has compiled, including an in-depth discussion of the input file,
- An overview of how to interpret (but not edit) the S_define file,
- A sample of some of the typical variables that may be logged.

The Instructions for Simulation Developers section of the user guide is intended for simulation developers. It describes the necessary configuration of the Surface Model within an S_define file, and the creation of standard run directories. The latter component assumes a thorough understanding of the preceding Analysis section of the user guide. Where applicable, the user may be directed to selected portions of Product Specification (Chapter 3).

The Instructions for Model Developers section of the user guide is intended primarily for developers needing to extend the capability of the Surface Model. Such users should have a thorough understanding of how the model is used in the preceding Integration section, and of the model specification (described in Chapter 3).

4.1 Instructions for Simulation Users

For this section, the following S_define object will be assumed:

```
sim_object {  
  
    utils/surface_model: SurfaceModel surface;  
    utils/surface_model: DemoSurface inter_surface;  
    utils/surface_model: DemoSurfaceFactory surf_fact;  
  
    unsigned int integer;
```

```

/* Scheduled Jobs */
utils/surface_model: Facet ** facet_ptr;

utils/surface_model: DemoFacet * demo_facet;

(0.0, environment) utils/surface_model:
surface_model.surface.add_facets(
    In Facet** new_facets = surface_model.facet_ptr,
    In unsigned int num_new_facets = surface_model.integer);

utils/surface_model: DemoParams * dp1;

utils/surface_model: FacetParams * facet_params;

(0.0, environment) utils/surface_model:
surface_model.surf_fact.add_facet_params(
    In FacetParams* to_add = surface_model.facet_params);

// These are only here so trick can see them. they are not
// used otherwise.
utils/surface_model: DemoFacetFactory dff;

utils/surface_model: InteractionFacetFactory * facet_factory;
(0.0, environment) utils/surface_model:
surface_model.surf_fact.add_facet_factory(
    In InteractionFacetFactory* to_add = surface_model.facet_factory
);

(initialization) utils/surface_model:
surface_model.surf_fact.create_surface(
    In SurfaceModel* surface = &surface_model.surface,
    Out InteractionSurface* inter_surface = &surface_model.inter_surface);
} surface_model;

```

There are a variety of theoretical objects in this `sim_object`, used for demonstration purposes. They are:

- `DemoSurface`, a class inheriting from `InteractionSurface`, meant to interact with a theoretical interaction class,
- `DemoSurfaceFactory`, a class inheriting from `InteractionSurfaceFactory`,
- `DemoFacet`, a class inheriting from `Facet`,

- DemoFacetFactory, a class inheriting from InteractionFacetFactory that creates an interaction facet (DemoInteractionFacet), representing the theoretical interaction specific version of DemoFacet,
- DemoParams, a FacetParams derived object used to create a DemoInteractionFacet from a DemoFacet through use of a DemoFacetFactory.

Note that, for JEOD supplied interaction models such as Aerodynamics [7] and Radiation Pressure [12], a thorough explanation of using those interactions with the Surface Model is contained in the respective model’s documentation, and should be consulted.

There are two options for creating facets that are then added to the SurfaceModel object:

- statically allocating them, either in a user defined object or directly in the S_define, or
- dynamically allocating them either in code or in the input file.

If the facets are statically allocated, then the user must simply add them to the instantiated SurfaceModel using either the ‘add_facets’ or ‘add_facet’ SurfaceModel member functions, as shown in the API document [1].

If the user dynamically allocates the facets in code, and the user requires the simulation to be fully checkpointable, then the user is responsible to use the appropriate methods through Trick to insure that the facets are checkpointable. This is not an inherent requirement of the surface model, and is only necessary if the user requires checkpointing.

The user can also allocate facets in the input file. The following section demonstrates this procedure.

4.1.1 Allocating Facets

This section demonstrates allocating facets in the input file. While this User Guide mainly focuses on a Trick 7 implementation (as a Trick 10 implementation is mostly analagous), care must be taken in allocating facets in Trick 10 such that they will be fully accessible and checkpointable by Trick. Thus, this section will give specific examples of both.

The example S_define presented in the previous section will be used for the Trick 7 demonstration. The Trick 10 demonstration will use its own.

Allocating Facets in Trick 7

In Trick 7, dynamic allocation of facets can be done through the following code:

```
#define NUM_DEMO_FACETS 2 // Two for example purposes only

DemoFacet** temp_demo_facets;
temp_demo_facets = alloc(NUM_DEMO_FACETS);
temp_demo_facets[0] = new DemoFacet[1];
```

```

temp_demo_facets[1] = new DemoFacet[1];

temp_demo_facets[0]->parameter = demo_value;
temp_demo_facets[1]->parameter = other_demo_value;

temp_demo_facets[0]->name = "demo_facet";
temp_demo_facets[1]->name = "demo_facet";

temp_demo_facets[0]->param_name = "demo_params";
temp_demo_facets[1]->param_name = "demo_params";

surface_model.facet_ptr = temp_demo_facets;
surface_model.integer = NUM_DEMO_FACETS;

call surface_model.surface_model.surface.add_facets(surface_model.facet_ptr);

```

This code snippet will allocate the DemoFacet objects to be added to the SurfaceModel object, populate them with the appropriate values associated with that particular class (demonstrated here by populating the member values “parameter” with “demo_value” and “other_demo_value”) and calling the function to dynamically add the newly allocated DemoFacets to the SurfaceModel. This procedure may be repeated any number of times, to add any type of Facet inherited objects to the SurfaceModel object that the user wishes.

Next, the appropriate parameters used to create the DemoInteractionFacet objects from the DemoFacet objects must be allocated, populated and added to the DemoSurfaceFactory. This can be done with the following code snippet:

```

DemoParams* params;
params = new DemoParams;
params->parameter = example_value;

params->name = "demo_params";

surface_model.facet_params = params;

call surface_model.surface_model.surf_fact.add_facet_params(
    surface_model.facet_params);

```

This example allocates a set of DemoParams, populates them, and adds them to the surface factory that will be responsible for creating the DemoInteractionFacet from the DemoFacet. This procedure may be done for as many FacetParams inheriting params as is necessary to create the corresponding InteractionFacet inherited objects from all Facet derived objects that were added to the surface model.

Note that the DemoFacet object has a field called “param_name”, and DemoParams has a field called “name.” It is these name fields that the DemoSurfaceFactory will use to match the parameters

that are loaded onto it with the Facet inherited objects it finds in the SurfaceModel object supplied to it. If a correctly named FacetParams inherited object is not found for a particular Facet inherited object found in the SurfaceModel, then a message will be sent through the JEOD Message Handler [6] and a failure will occur.

Finally, the InteractionFacetFactory objects necessary for creating the DemoSurface object from the supplied SurfaceModel object must be added to the InteractionSurfaceFactory subclass DemoSurfaceFactory. This can be done with the following code snippet:

```
DemoFactory* = df;
df = new DemoFactory;

surface_model.facet_factory = df;

call surface_model.surface_model.surf_fact.add_facet_factory(
    surface_model.facet_factory);
```

Care must be taken that, for every type of Facet added to the SurfaceModel above, an appropriate InteractionFacetFactory inherited class that is also appropriate for the Interaction at hand, must be added to the InteractionSurfaceFactory. If this is not done then the initialization of the InteractionSurface will fail, as the InteractionSurfaceFactory will find a Facet that it does not know how to handle.

The InteractionSurface derived class DemoSurface may now be used in the appropriate, user defined manner.

Allocating Facets in Trick 10

The steps for dynamically allocating facets in the input file in Trick 10 are mostly analogous to those used in Trick 7. Outside of a few minor and noted details, the procedure is the same, with only syntactic resulting in the input file.

These examples will rely heavily on built in utilities provided to the user by Trick. A thorough understanding of the input file, as it applies to Trick 10, are recommended, and the Trick 10 documentation on that subject should be well understood.

To demonstrate this, the following example S_define will be used:

```
##include "utils/surface_model/verif/include/demo_facet.hh"
##include "utils/surface_model/verif/include/demo_factory.hh"
##include "utils/surface_model/verif/include/demo_interaction.hh"
##include "utils/surface_model/verif/include/demo_interaction_facet.hh"
##include "utils/surface_model/verif/include/demo_params.hh"
##include "utils/surface_model/verif/include/demo_surface.hh"
##include "utils/surface_model/verif/include/demo_surface_factory.hh"
```



```

class SurfaceModelSimObject : public Trick::SimObject {

public:

    // Objects
    SurfaceModel surface;
    DemoSurface inter_surface;
    DemoSurfaceFactory surf_fact;

    // Pointers used for dynamic allocation
    DemoFacet* demo_facet;
    DemoParams* demo_params;
    DemoFactory* demo_factory;

    SurfaceModelSimObject()
    {

        ("initialization") surf_fact.create_surface(&surface, &inter_surface);

    }

};

// Instantiate the surface model sim object.
SurfaceModelSimObject surface_model;

```

The zero rate jobs ('add_facets', 'add_facet_params' and 'add_facet_factory') as seen in the earlier Trick 7 version are no longer necessary, as member functions can now be called from the input file without registering them as a job with Trick. Also, it is necessary to include the definition of any type of facet intended to be allocated through a Trick '##include' declaration.

If the allocated facets need to be checkpointable, the following Python code can be used for allocation:

```

surface_model.demo_facet = trick.alloc_type(1, "DemoFacet")
# A temporary reference to the facet to save typing
temp_facet = surface_model.demo_facet
temp_facet.parameter = demo_value
temp_facet.param_name = "demo_params"
surface_model.surface.add_facet(temp_facet)

```

This code allocates a single facet, fills out the appropriate values, then adds it to the SurfaceModel object. This differs slightly from the Trick 7 version, in that it is much easier to add facets one at a time in Trick 10. Note the use of the intermediate pointer 'surface_model.demo_facet,' which is of type DemoFacet*. This is necessary for Python to be able to correctly type the returned value from 'trick.alloc_type.'

If the ability to checkpoint is not a requirement, then the following code can instead be used:

```
temp_facet = trick.DemoFacet()
temp_facet.thisown = 0
temp_facet.parameter = demo_value
temp_facet.param_name = "demo_params"
surface_model.surface.add_facet(temp_facet)
```

A similar pattern is followed to allocate the facet parameter objects and the interaction surface factories. For the case where checkpointing is required:

```
surface_model.demo_params = trick_alloc_type(1, "DemoParams")
# A temporary reference to the params to save typing
temp_params = surface_model.demo_params
temp_params.parameter = example_value
surface_model.surface.add_facet_params(temp_params)
```

For the case where checkpointing is not required:

```
temp_params = trick.DemoParams()
temp_params.thisown = 0
params.parameter = example_value
surface_model.surface.add_facet_params(temp_params)
```

Similarly, allocating checkpointable interaction facet factories can be done using the following code:

```
surface_model.demo_factory = trick.alloc_type(1, "DemoFactory")
# A temporary reference to the factory to save typing
temp_factory = surface_model.demo_factory
surface_model.surface.add_factory(temp_factory)
```

If checkpointing is not a requirement:

```
temp_factory = trick.DemoFactory()
temp_factory.thisown = 0
surface_model.surface.add_factory(temp_factory)
```

4.1.2 Specifying Facet Geometry

There are two possible ways to specify geometry of a facet:

- Specifying the geometry directly in the desired frame, usually the structural frame of the represented vehicle, or

- Specifying the geometry with respect to a MassBody’s structural frame, through the articulation interface.

The following sections will describe both of these methods.

Specifying Geometry Directly in the Desired Frame

The first, and easiest, method for specifying facet geometry is to specify it directly in the user desired frame, most commonly the structural frame of the represented vehicle.

In the case of a FlatPlate, the position and the normal direction can be specified directly by setting the parameters “position” and “normal,” as shown below:

```
FlatPlate flat_plate;

flat_plate.position[0] {M} = 5.0, 2.0, 1.0;
flat_plate.normal[0] = 1.0 , 0.0 , 0.0;
```

This command places the flat plate at the position noted, with a normal completely in the “X” direction, with respect to the frame implicitly chosen by the user.

Note that the variables being set are “position” and “normal”. These are fundamentally different than the corresponding “local_position” and “local_normal”. These “local_” versions of the variables are only for use when the articulation capability is in use. If the user wishes to directly set the normal and position in their chosen frame, this example should be followed and the “local_” versions should be left untouched.

Also note that, when using this method, JEOD does not enforce a specific frame for specifying facet geometry. While the vehicle structural frame is the most common (as seen both in the Aerodynamics [7] and Radiation Pressure [12] interaction models), this is not enforced. Additionally, this frame is never explicitly set, and is only implicit based on the user’s intent. It is up to the user to ensure that all facets in a surface model are represented with respect to a common frame, and that it is the frame that other models using the surface model are expecting.

Finally, it should be noted that any interaction model that is using a surface model, for a FlatPlate or any Facet inheriting the “position” attribute, should only access these variables. The “local_” versions of these variables are not intended to be used as an output, and should be treated as such.

Specifying Geometry through the Articulation Interface

The second way a user can specify the geometry of a Facet is by connecting Facets to MassBody objects in a mass tree, through the provided articulation interface. This section will describe this method. This section will rely heavily on knowledge of the JEOD Mass Model and its documentation [9].

This method allows the user to attach a Facet to a movable reference frame, where a “global” position and orientation for that reference frame will automatically be calculated by the surface

model. This is accomplished by attaching all Facets to frames associated with individual mass bodies in a tree, as well as specifying a single “output frame” for the global position and orientation.

In this method of specifying geometry, each Facet is specified with respect to the structural reference frame of a specific mass body. This differs from the method described in the previous section, where all facets were specified in a common, user defined implicit frame. For example, this specification is done for a FlatPlate by setting the following variables:

```
FlatPlate flat_plate;  
  
flat_plate.local_position[0] {M} = 5.0, 2.0, 1.0;  
flat_plate.local_normal[0] = 1.0 , 0.0 , 0.0;
```

Note that this is different than the previous example, as instead of “position” and “normal,” the variables being set are “local_position” and “local_normal”.

The specified position and normal is relative to the structural frame of a particular mass body. The user specifies which mass body by name, as in the following example:

```
flat_plate.mass_body_name = "name_of_mass_body";
```

This name must match that of a mass body contained in the mass tree of the vehicle this surface represents. For details on making sure this name is correct, as usual, see the MassBody documentation [\[9\]](#).

Next, the user must tell the surface model which mass body structural frame will be the “global” frame, by naming the associated mass body in the following manner:

```
SurfaceModel surface;  
surface.struct_body_name = "name_of_struct_body";
```

As with the Facet’s “mass_body_name,” this name must correspond to the name of a mass body in the mass tree of the vehicle this surface represents. Additionally, the named mass must be in the same mass tree as all of the named masses associated with all of the Facets in the surface model. If this is not true then the articulation component will throw a failure message through the JEOD Message Handler [\[6\]](#).

The Facet geometry, specified in this manner, is meant to be static with respect to the Facet’s specified mass body. Once the articulation feature of the surface model is invoked, the appropriate transformations will be applied to this specified geometry to represent the position and orientation of the Facet in the structural frame of the mass body that is named by SurfaceModel’s “struct_body_name”. For a FlatPlate, this information will then be stored in the “position” and “normal” variables. As mentioned in the previous section, these are the variables that should then be accessed by an interaction model using this surface.

Finally, the user must turn on the articulation feature, using the following code as an example:

```
surface.articulation_active = true;
```

Note that this is set to false by default.

This association to a mass body then allows for articulation by movement of mass bodies, within the tree, relative to one another. For details on moving mass bodies relative to one another in a tree, see the appropriate documentation [9].

Please note that, at this time, the only Facet derived type that supports this articulation feature is the FlatPlate. Any other Facets supplied by JEOD will have undefined behavior if they are used in association with the articulation feature. For any other user created Facets, check with the individual developer to see if the correct functionality has been implemented.

Additionally, the articulation feature will only work if the correct functionality has been placed in the S_define. Details for this can be found in the Integration section of this document.

4.2 Instructions for Simulation Developers

This section will be broken into two versions, one for simulation development in Trick 7 and one for Trick 10.

4.2.1 Simulation Development in Trick 7

This section will use the following S_define object as an example:

```
sim_object {

    utils/surface_model: SurfaceModel surface;
    utils/surface_model: DemoSurface inter_surface;
    utils/surface_model: DemoSurfaceFactory surf_fact

    unsigned int integer;

    utils/surface_model: Facet ** facet_ptr;

    utils/surface_model: DemoFacet * demo_facet;

    (0.0, environment) utils/surface_model:
    surface_model.surface.add_facets(
        In Facet** new_facets = surface_model.facet_ptr,
        In unsigned int num_new_facets = surface_model.integer);

    utils/surface_model: DemoParams * dp1;

    utils/surface_model: FacetParams * facet_params;

    (0.0, environment) utils/surface_model:
    surface_model.surf_fact.add_facet_params(
```

```

        In FacetParams* to_add = surface_model.facet_params);

// These are only here so Trick can see them. they are not
// used otherwise.
utils/surface_model: DemoFacetFactory dff;

utils/surface_model: InteractionFacetFactory * facet_factory;
(0.0, environment) utils/surface_model:
surface_model.surf_fact.add_facet_factory(
    In InteractionFacetFactory* to_add = surface_model.facet_factory
    );

(initialization) utils/surface_model:
surface_model.surf_fact.create_surface(
    In SurfaceModel* surface = &surface_model.surface,
    Out InteractionSurface* inter_surface = &surface_model.inter_surface);
} surface_model;

```

This section will also use the same theoretical SurfaceModel classes, for demonstration purposes, as found in the Analysis section.

Note that, for JEOD supplied interaction models such as Aerodynamics [7] and Radiation Pressure [12], a thorough explanation of using those interactions with the Surface Model is contained in the respective model's documentation, and should be consulted.

First, a basic surface model object and a surface model appropriate for the specific interaction at hand must be instantiated. Additionally, the surface factory necessary to populate the interaction surface must be instantiated. This is shown in the following S_define snippet:

```

utils/surface_model: SurfaceModel surface;
utils/surface_model: DemoSurface inter_surface;
utils/surface_model: DemoSurfaceFactory surf_fact;

```

Next, the hooks for dynamically allocating the Facet derived objects and adding them to the SurfaceModel object through an input file are added:

```

unsigned int integer;

utils/surface_model: Facet ** facet_ptr;

utils/surface_model: DemoFacet * demo_facet;

(0.0, environment) utils/surface_model:
surface_model.surface.add_facets(

```

```
In Facet** new_facets = surface_model.facet_ptr,
In unsigned int num_new_facets = surface_model.integer);
```

Note that the DemoFacet pointer “demo_facet” is never legitimately used. It is only included so that Trick is aware of its existence and so that it can be dynamically allocated in the input file. This inclusion of all Facet derived types that will be added in the input file that uses this S_define is necessary, or the dynamic allocation will not work, and must be done by the Integrator that is creating the S_define.

Next, the hooks to dynamically add FacetParams derived objects must be added to the S_define using the following code:

```
utils/surface_model: DemoParams * dp1;

utils/surface_model: FacetParams * facet_params;

(0.0, environment) utils/surface_model:
surface_model.surf_fact.add_facet_params(
    In FacetParams* to_add = surface_model.facet_params);
```

Similar to the DemoFacet pointer described above, the DemoParams pointer seen here is never used. It is only necessary for Trick awareness. An inclusion in the S_define of this type is necessary for every type of FacetParams derived object that will be used with this particular S_define, or the dynamic allocation of that particular type in the input file will be unsuccessful.

Next, the hooks to dynamically add InteractionFacetFactory derived objects to the DemoSurfaceFactory must be added, using the following code:

```
utils/surface_model: DemoFacetFactory* dff;

utils/surface_model: InteractionFacetFactory * facet_factory;

(0.0, environment) utils/surface_model:
surface_model.surf_fact.add_facet_factory(
    In InteractionFacetFactory* to_add = surface_model.facet_factory
);
```

Once again, the DemoFacetFactory pointer is never used, and is only present to make Trick aware of the type so that dynamic allocation in the input file is possible.

Finally, the DemoSurface must be created from the SurfaceModel, using the following code:

```
(initialization) utils/surface_model:
surface_model.surf_fact.create_surface(
    In SurfaceModel* surface = &surface_model.surface,
    Out InteractionSurface* inter_surface = &surface_model.inter_surface);
```

The DemoSurface has now been populated and is ready for use with the appropriate interaction model.

4.2.2 Simulation Development in Trick 10

The following S_define example will be used to demonstration simulation development in Trick 10. This is a similar example to that used in the previous Trick 10 example of allocating checkpointable facets in the input file, and the same usage will be assumed.

```
##include "utils/surface_model/verif/include/demo_facet.hh"
##include "utils/surface_model/verif/include/demo_factory.hh"
##include "utils/surface_model/verif/include/demo_interaction.hh"
##include "utils/surface_model/verif/include/demo_interaction_facet.hh"
##include "utils/surface_model/verif/include/demo_params.hh"
##include "utils/surface_model/verif/include/demo_surface.hh"
##include "utils/surface_model/verif/include/demo_surface_factory.hh"

class SurfaceModelSimObject : public Trick::SimObject {

public:

    // Objects
    SurfaceModel surface;
    DemoSurface inter_surface;
    DemoSurfaceFactory surf_fact;

    // Pointers used for dynamic allocation, when checkpointing is necessary
    DemoFacet* demo_facet;
    DemoParams* demo_params;
    DemoFactory* demo_factory;

    SurfaceModelSimObject()
    {

        ("initialization") surf_fact.create_surface(&surface, &inter_surface);

    }

};

// Instantiate the surface model sim object.
SurfaceModelSimObject surface_model;
```

Because of Python's ability to directly call object member functions from the input file, the S_define

in Trick 10 is slightly cleaner.

The first thing a developer must do is include all definitions for objects that will be instantiated in the sim object, as well as objects that are intended to be dynamically allocated in the input file, as ‘`##include`’ commands, shown in this example as:

```
##include "utils/surface_model/verif/include/demo_facet.hh"
##include "utils/surface_model/verif/include/demo_factory.hh"
##include "utils/surface_model/verif/include/demo_interaction.hh"
##include "utils/surface_model/verif/include/demo_interaction_facet.hh"
##include "utils/surface_model/verif/include/demo_params.hh"
##include "utils/surface_model/verif/include/demo_surface.hh"
##include "utils/surface_model/verif/include/demo_surface_factory.hh"
```

A basic surface model object and an interaction specific surface model, as well as a surface factory necessary to populate the interaction surface, must be instantiated. This is demonstrated in the following S.define snippet:

```
SurfaceModel surface;
DemoSurface inter_surface;
DemoSurfaceFactory surf_fact;
```

If facets are to be allocated dynamically, and the user wishes for them to be checkpointable, then any allocable types must have an intermediate pointer declared for them in the S.define, demonstrated in this code snippet:

```
DemoFacet* demo_facet;
DemoParams* demo_params;
DemoFactory* demo_factory;
```

This code will allow for types DemoFacet, DemoParams and DemoFactory to be allocated and checkpointable in the input file. If checkpointing is not a requirement, then these declarations are optional and can be left out.

Finally, all that is left is to register the initialization job for creating the interaction surface.

```
("initialization") surf_fact.create_surface(&surface, &inter_surface);
```

4.2.3 Articulation

There are additional pieces necessary to enable the use of articulation in an S.define. The following additional calls, and pieces, should be added:

```
sim_object {
```

```

    DynManager dyn_manager;

}

sim_object {
    (initialization) utils/surface_model:
    surface_model.surface.initialize_mass_connections(
        In DynManager& manager = mngr.dyn_manager);

    (1.0, environment) utils/surface_model:
        surface_model.surface.update_articulation();
} surface_model;

```

As usual, this is a partial code snippet only used to illustrate this procedure.

Two jobs must be added to allow use of the articulation feature. The first is an initialization job, which will use the DynManager interface to connect all Facets to their appropriate mass bodys, as described in the Analysis section of this document. This job is called “initialize_mass.connections,” and must be supplied with a DynManager object. This object must be pre-loaded with all masses (or MassBody derived objects, such as DynBody objects [2]) that are named by the user, as described in the Analysis section, for use with the invoking SurfaceModel object.

The second job tells the surface model to update the current “global” state of all facets. This is a simple call, as illustrated above, to the “update_articulation” function. Once this function has been called, all updates to the “global” position and orientation of Facets will have occurred.

All of these instructions are completely analogous for Trick 10, and as a result a specific Trick 10 example will not be presented. However, the same jobs can merely be added to a Trick 10 sim object, and will have the same effect.

4.3 Instructions for Model Developers

There are two ways to extend the Surface Model. The first is to add new representations for facets to the geometric surface model. The second is to extend the surface model to work with other environmental interactions. Both will be discussed in this section.

4.3.1 Extending the Facet Class

To extend the Facet class, a user must create a new class that inherits from Facet, and populate it with the required data for the new representation. Because of the design of the SurfaceModel object (containing an array of pointers to the Facet base class), this new Facet inherited class can now be added to a SurfaceModel object.

Note that, to use this new Facet inherited class in an interaction, the interaction specific version of the surface model will also need to be extended. This, however, is a part of extending the environmental interaction, and thus will be covered in the next section.

Extending the Facet Class for Articulation

To enable articulation for an extension of the facet class, one protected virtual method must be implemented. This method is:

```
virtual void update_articulation_internal();
```

and is inherited from the Facet class.

When this method is called, the member variable:

```
MassPointState mass_rel_struct;
```

also inherited from the Facet class, will be populated with the relative state between the structural frame of the mass body associated with this particular facet, and the structural frame of the “global” mass body associated with the entire surface model, from the global frame to the facet frame. For details of this class, see the Mass Model documentation [9].

The extender must now correctly use this information to transform any user specified local geometry, as determined by the extender and correctly added to their class, into the “global” frame, and this information must then be stored in the extended Facet. How this is done is ultimately left up to the user, and example implementation are found in both the Facet class and the FlatPlate class.

Note that, for the “position” parameter found in all Facet classes, the Facet version of this function can be called explicitly from the extended version, using the call:

```
Facet::update_articulation_internal();
```

Additionally, an extender inheriting from the FlatPlate class can also call the FlatPlate version to update both the global position and normal.

Note that it may be advantageous to a user, if one is not intending for a particular Facet derived class to be used for articulation, for the extender to explicitly override this function, and have the function issue information to the user through the JEOD Message Handler. Details on this can, of course, be found in the appropriate documentation [6].

4.3.2 Extending to New Environmental Interactions

Extending the Surface Model to new environmental classes involves creating a variety of subclasses to take advantage of the architecture of the Surface Model. This section will describe the steps that must be taken.

Note that both the JEOD Aerodynamics Model [7] and the Radiation Pressure Model [12] extend the Surface Model for their own use, and these models serve as examples for the information that will be given here.

For the purpose of demonstration, an interaction called “NewInteraction” will be supposed. This is, obviously, illustrative only.

The first step is to create a subclass of InteractionFacet particular to the new interaction. This subclass is what will actually be contained in the eventual NewInteraction specific InteractionSurfaceModel class, and will, through virtual functionality, dictate the API for the calculation of “NewInteraction”. An example of this is the class AeroFacet [7], which inherits from InteractionFacet and adds the pure virtual function shown below:

```
virtual void aerodrag_force(
    const double velocity_mag,
    const double rel_vel_hat[3],
    AeroDragParameters* aero_drag_param_ptr,
    double center_grav[3]) = 0;
```

This now gives the InteractionFacet class implicit aerodrag functionality. A similar path should be taken for the “NewInteraction”. The extender should create an InteractionFacet inherited class (hypothetically called “NewInteractionFacet”) and add the pure virtual function that will be responsible for calculating the new interaction’s effects on all interaction facets contained in the model.

Next, the user must create a specific subclass of InteractionSurfaceModel for the new interaction. This new class, hypothetically called “NewInteractionSurfaceModel,” will contain an array of pointers to the previously created “NewInteractionFacet.” An example of this inheritance is the AeroSurface class found in the Aerodynamics Model [7].

Additionally, two functions must be implemented in the “NewInteractionSurfaceModel” class; “allocate_array” and “allocate_interaction_facet.” These are pure virtual functions in the InteractionSurface class, and there is standard code that can be used to implement them in a “NewInteractionSurfaceModel” class. The follow code snippet, intended for a header file, will help illustrate this concept.

```
NewInteractionFacet** inter_facets;

unsigned int facets_size; /* cnt Size of the inter_facets array */

// Allocates the inter_facets array from the given size
virtual void allocate_array (unsigned int size);

// Allocates the facet at the "index" value in inter_facets, using
// the base Facet given by the pointer facet, and using the parameter
// object pointed to by params pointer and using the
// InteractionFacetFactory pointed to by factory.
virtual void allocate_interaction_facet (
    Facet* facet,
    InteractionFacetFactory* factory,
    FacetParams* params,
    unsigned int index);
```

Given this code snippet, the code for the pure virtual functions can be implemented in the following manner.

```

void
NewInteractionSurface::allocate_array ( // Return: -- void
    unsigned int size) // In: cnt: The size of the needed array
{

    if (inter_facets != nullptr) {
        // USE THE JEOD MESSAGE HANDLER TO SEND A FAILURE MESSAGE.
        return;
    }

    // Allocate the array we want, and set the size
    inter_facets = JEOD_ALLOC_CLASS_POINTER_ARRAY (size, AeroFacet);
    facets_size = size;

    // Make sure all pointers are NULL so destructor never crashes
    for (unsigned int ii = 0; ii < facets_size; ++ii) {
        aero_facets[ii] = nullptr;
    }

    return;
}

void
AeroSurface::allocate_interaction_facet ( // Return: -- void
    Facet* facet, /* In: -- The basic facet used to create the
                    interaction facet */
    InteractionFacetFactory* factory, /* In: -- The factory used to create
                    the interaction facet */
    FacetParams* params, /* In: -- The aero params used to create the
                    interaction facet */
    unsigned int index) /* In: cnt Where the new interaction facet will be placed
                    in the aero_facets array */
{
    if (facets_size <= index) {

        // SEND A MESSAGE USING THE JEOD MESSAGE HANDLER
        return;

    }

    /* need to temporarily save off the InteractionFacet returned before
       dynamic casting it. If the dynamic cast fails, we want to destroy
       the InteractionFacet so we don't get a memory leak */

```

```

InteractionFacet* temp_facet = nullptr;

// attempt to create the facet
temp_facet = factory->create_facet (facet, params);

// if the facet is nullptr, then we have a problem
if (temp_facet == nullptr) {

    // SEND A MESSAGE USING THE JEOD MESSAGE HANDLER

}

// Facet is currently an interaction facet. Try to make it a
// NewInteractionFacet

NewInteractionFacet* temp_inter_facet =
    dynamic_cast<NewInteractionFacet*> (temp_facet);

// If that fails, it doesn't belong in this surface so there is a problem
if (temp_inter_facet == nullptr) {

    // temp_facet can NOT be NULL, since it was already checked for above
    JEOD_DELETE_OBJECT (temp_facet);

    // SEND A MESSAGE THROUGH THE JEOD MESSAGE HANDLER

    return;

}

// Store the aero_facet into the aero_facets array
inter_facets[index] = temp_inter_facet;

return;

}

```

This prepares the NewInteractionSurface class to successfully allocate its own array of Interaction-Facet derived objects, as well as populate an index of that array given a correct Facet pointer, InteractionFacetFactory pointer and FacetParams pointer.

Additionally, to prevent a memory leak, the allocated array of NewInteractionFacet pointers and their allocated memory must be deleted by the destructor of this new class. Example code for doing this can be seen below:

```

NewInteractionSurface::~NewInteractionSurface (
    void)
{
    if (inter_facets != nullptr) {

        for (unsigned int ii = 0; ii < facets_size; ++ii) {
            if (inter_facets[ii] != nullptr) {
                JEOD_DELETE_OBJECT (aero_facets[ii]);
            }
        }

        JEOD_DELETE_ARRAY (inter_facets);

    }
}

```

Note that references are made in these code snippets to the JEOD Message Handler [6]. These messages will involve interaction model specific messages, and need to be written by the user themselves. Additional information can be found in the Message Handler documentation. Additionally, references are made to JEOD alloc and delete functions. Details on this functionality can be found in the JEOD Memory utility [3].

Next, a subclass of FacetParams should be created that defines a NewInteraction specific set of parameters. While this is not a necessary step, it insures type safety when working with the Surface Model. This inherited class, theoretically called “NewInteractionParams,” can be empty.

Next, an interaction specific class inheriting from InteractionSurfaceFactory must be created. Like the creation of the NewInteractionParams, this insures type safety. This new class, theoretically called “NewInteractionSurfaceFactory” will have one function implemented:

```

virtual void add_facet_params (FacetParams* to_add);

```

This function will check that the FacetParams pointer is of an object of the correct type (i.e. inheriting from NewInteractionParams), then add the FacetParams object to the surface factory through the already existing SurfaceFactory function of the same name. Example code for this is as follows:

```

void
NewInteractionSurfaceFactory::add_facet_params (
    FacetParams* to_add)
{
    if ((to_add->name == NULL) || (to_add->name[0] == '\0')) {

```

```

        // SEND A FAILUTRE MESSAGE THROUGH THE MESSAGE HANDLER

    }

    // The param MUST be an
    NewInteractionParams* temp_ptr = nullptr;

    temp_ptr = dynamic_cast<NewInteractionParams*> (to_add);

    if (temp_ptr == nullptr) {

        // SEND A MESSAGE THROUGH THE MESSAGE HANDLER
        return;
    }

    // Add the parameter through the inherited function
    InteractionSurfaceFactory::add_facet_params (to_add);

    return;
}

```

Finally, a set of classes must be created for every basic type of geometric facet (in other words, class that inherits from the Facet class) the extender wants to make available to the new interaction. Three classes will be created, inheriting from:

- NewInteractionFacet, which will be the NewInteraction specific version of the particular Facet subclass at hand,
- InteractionFacetFactory, the class that will be responsible for creating the interaction specific version of the facet from the facet itself, and
- NewInteractionParams, the parameters necessary to create the NewInteractionFacet subclass from the Facet subclass (typically NewInteraction specific values necessary for the calculation of the interaction).

For illustrative purposes, the remainder of this section will assume that the extender wishes to use the FlatPlate representation of Facet in the NewInteraction already being discussed. Obviously the Surface Model can be extended to any Facet subclass following these instructions, but FlatPlate will be used as the example.

The extender would create three classes:

- NewInteractionFlatPlate, a version of flat plate, inheriting from NewInteractionFacet, that knows how to calculate the effects of NewInteraction on itself,
- NewInteractionFlatPlateParams, parameters necessary to the NewInteractionFlatPlate class to calculate the new interaction effects on the flat plate, and

- NewInteractionFlatPlateFactory, inheriting from InteractionFacetFactory and with the ability to create a NewInteractionFlatPlate from a FlatPlate given the correct parameters.

The NewInteractionFlatPlate class inherits from NewInteractionFacet. It will contain all data necessary for calculating the new interaction effect on the flat plate in question. Also, the extender will have to implement the pure virtual function created in NewInteractionFacet, as described earlier. This implementation should calculate the interaction effects on the flat plate itself. If force and torque are a product of the interaction then these results can be stored in the appropriately named variables that have been inherited from the InteractionFacet class. Once the data members have been added and the pure virtual function implemented, the NewInteractionFlatPlate is ready for use in the Surface Model.

The NewInteractionFlatPlateParams object is simple to create. Inheriting from NewInteractionParams, the extender can add any parameters necessary for calculating the new interaction's effects on a flat plate that must be set at run time by the user. Once the class has been created and the parameters added to it, the NewInteractionFlatPlateParams class is ready to be used in the Surface Model.

The NewInteractionFlatPlateFactory class, inheriting from InteractionFacetFactory, is responsible for creating a NewInteractionFlatPlate from a FlatPlate. To do this, two functions must be implemented in the NewInteractionFlatPlateFactory class:

```
virtual bool is_correct_factory (Facet* facet);

virtual InteractionFacet* create_facet (Facet* facet, FacetParams* params);
```

These are functions inherited from InteractionFacetFactory, where they are pure virtual.

The “is_correct_factory” function is simple to create. Given a pointer to a Facet (usually pointing to an object of a Facet subclass), the function returns a true if the pointer is to an object that the class was meant to work on, and false otherwise. This function can be easily programmed using a simple pattern, shown below for the case of the NewInteractionFlatPlateFactory class.

```
bool
NewInteractionFlatPlateFactory::is_correct_factory (
    Facet* facet)
{
    // Simple. do a typeid, if it is true return true, otherwise
    // return false.
    if (typeid(*facet) == typeid(FlatPlate)) {
        return true;
    }
    else {
        return false;
    }
}
```

```
}
```

The “create_facet” function takes in a Facet pointer and a FacetParams pointer, and returns a pointer to an allocated InteractionFacet. Taking advantage of polymorphism, the Facet pointer is most commonly pointing to a subclass of Facet, and the FacetParams pointer is pointing to a subclass of FacetParams. Type-checking is done at a variety of levels: the Facet is checked to insure that it is the correct Facet subclass associated with this particular InteractionFacetFactory, and the FacetParams is checked for the same criteria. Once these steps are both taken, the NewInteractionFlatPlate object will be created, populated with the parameters found in the NewInteractionFlatPlateParams object sent in, and return the new object. Example of this complete function can be found in the following code snippet:

```
InteractionFacet*
FlatPlateAeroFactory::create_facet (
    Facet* facet,
    FacetParams* params)
{

    NewInteractionFlatPlateParams* inter_params = nullptr;
    FlatPlate* flat_plate = nullptr;

    inter_params = dynamic_cast<NewInteractionFlatPlateParams*> (params);
    flat_plate = dynamic_cast<FlatPlate*> (facet);

    // We have tried casting the facet and params to the correct types.
    // if they were not the correct type, send out an error message

    if (inter_params == nullptr) {

        // SEND A MESSAGE THROUGH THE MESSAGE HANDLER
    }
    if (flat_plate == nullptr) {

        // SEND A MESSAGE THROUGH THE MESSAGE HANDLER
    }

    // Create the interaction facet
    NewInteractionFlatPlate* inter_facet =
        JEOD_ALLOC_CLASS_OBJECT (NewInteractionFlatPlate, ());

    // Fill it out from the parameters and from the facet itself
    inter_facet->base_facet = facet;

    // Populate the NewInteractionFlatPlate with the parameters from
```

```
// the passed in NewInteractionFlatPlateParams here. This step
// is left up to the individual extender, as it will be
// interaction specific.

return inter_facet;

}
```

All pieces are now in place, and the new classes may be used as described above in the Analysis and Intergration sections.

Chapter 5

Verification and Validation

5.1 Verification

Inspection SM_1: Top-level inspection

This document structure, the code, and associated files have been inspected, and together satisfy requirement [SM.1](#).

Inspection SM_2: Geometric Modeling Inspection

The Surface Model contains the following fully implemented classes:

- Facet, an extensible class that models one part of a surface, and
- SurfaceModel, a collection of facets representing a complete vehicle geometric surface.

Thus, by inspection, the Surface Model satisfies requirement [SM.2](#).

5.2 Validation

Test SM_1: Multiple Interaction, Multiple Facet Demo

Purpose:

The purpose of this test is to demonstrate the following:

- Extensibility of the geometric representation of the surface model,
- Functionality of the surface model with environmental interactions,
- Usability of a single SurfaceModel object with multiple environmental interactions,

- Extensibility of the Surface Model to multiple environmental interactions.

Requirements:

By passing this test, the Surface Model satisfies requirement [SM_3](#), requirement [SM_4](#), requirement [SM_5](#), and requirement [SM_6](#).

Procedure:

A set of demonstration test classes were created. These classes demonstrate a variety of features of the Surface Model, and include:

- DemoFacet, a new subclass of Facet,
- DemoInteraction1, a demonstration interaction meant to interact with the Surface Model,
- DemoInteraction2, a second demonstration interaction meant to interact with the Surface Model,
- DemoSurface1, a subclass of InteractionSurface specifically for DemoInteraction1,
- DemoSurface2, a subclass of InteractionSurface specifically for DemoInteraction2.

This is not a complete list of the classes created for this verification; other utility classes were also created to facilitate the complete implementation of the Surface Model for the new interactions DemoInteraction1 and DemoInteraction2. Both of these interactions will ask each interaction facet in their supplied interaction surface model to execute its interaction specific function, as described later in this section.

A SurfaceModel object will be created and populated with both a FlatPlate object and a DemoFacet object. This will demonstrate the extensible nature of the geometric modeling of the Surface Model.

Two surface models, one each for the new interactions DemoInteraction1 and DemoInteraction2, will be created and demonstrated to be usable with the interactions. This will demonstrate the usefulness of the Surface Model with environmental interactions, as well as the reusability of a single SurfaceModel object for multiple environmental interactions. Additionally, it will demonstrate that the surface model is extensible to many interactions.

The two new interactions will be simple; they will trigger the individual interaction facet contained within the appropriate interaction facets contained within the created interaction surfaces. This output will be triggered through a pure virtual function declared in the InteractionFacet base classes for each interaction. The InteractionFacet base class for DemoInteraction1 is “DemoFacet1”, which declares the pure virtual function:

```
virtual void execute_demo_1(
    unsigned int interaction_number
) = 0;
```

where the argument “interaction_number” is an integer set in DemoInteraction1 itself, which will be printed out. This will demonstrate that the interaction is indeed working with the individual interaction facets of the interaction surface.

The InteractionFacet base class for DemoInteraction2 is “DemoFacet2,” which declares the pure virtual function:

```
virtual void execute_demo_2(
    char* interaction_name
) = 0;
```

where the argument “interaction_name” is a string set in DemoInteraction2 itself, which will be printed. This will demonstrate that the interaction is indeed working with the individual interaction facets of the interaction surface.

Other information will be printed out during the run of the test. This information is controlled from the input file, and will serve to demonstrate the extensibility of the Surface Model.

The DemoFacet contains the following parameters:

```
char* name;
int some_int;
```

There are four specific interaction facets in this demonstration: a DemoInteraction1 specific FlatPlate facet, a DemoInteraction2 specific FlatPlate facet, a DemoInteraction1 specific DemoFacet, and a DemoInteraction2 specific DemoFacet. These interaction facets all have parameters set by the user, through FacetParams objects, at runtime.

The FlatPlateDemo1 (DemoInteraction1 specific FlatPlate) contains:

```
char* shape;
```

The FlatPlateDemo2 (DemoInteraction2 specific FlatPlate) contains:

```
int sides;
```

The DemoInteractionFacet1 (DemoInteraction1 specific DemoFacet) contains:

```
double weight;
```

The DemoInteractionFacet2 (DemoInteraction2 specific DemoFacet) contains:

```
char* color;
```

Both FlatPlateDemo1 and DemoInteractionFacet1 implement the pure virtual function “execute_demo_1”. Their implementations are:

```
void FlatPlateDemo1::execute_demo_1 (
    unsigned int interaction_number){
    FlatPlate* base_plate = dynamic_cast<FlatPlate*> (base_facet);

    printf("\n\n\n");
    printf("FlatPlateDemo1::execute_demo_1\n");
    printf("The interaction number is: %d\n", interaction_number);
```

```

    printf("The shape is: %s\n", shape);
    printf("Area of flat plate is: %f\n", base_plate->area);
    printf("normal of flat plate is: %f %f %f\n",
        base_plate->normal[0],
        base_plate->normal[1],
        base_plate->normal[2]);

    return;
}

void DemoInteractionFacet1::execute_demo_1 (
    unsigned int interaction_number){
    DemoFacet* base_plate = dynamic_cast<DemoFacet*> (base_facet);
    printf("\n\n\n");
    printf("DemoInteractionFacet1::execute_demo_1\n");
    printf("The interaction number is: %d\n", interaction_number);
    printf("The weight is: %f\n", weight);
    printf("the name of the DemoFacet is: %s\n", base_plate->name);
    printf("the semi-random int of the DemoFacet is: %d\n",
        base_plate->some_int);
}

```

As can be seen, both implementations print out information supplied by the interaction itself, the original geometric facet the interaction facet was created from, and from the interaction facet itself.

Both FlatPlateDemo2 and DemoInteractionFacet2 implement the pure virtual function “execute_demo_2.” Their implementations are:

```

void FlatPlateDemo2::execute_demo_2 (
    char* interaction_name){
    FlatPlate* base_plate = dynamic_cast<FlatPlate*> (base_facet);
    printf("\n\n\n");
    printf("FlatPlateDemo2::execute_demo_2\n");
    printf("The interaction name is: %s\n", interaction_name);
    printf("The number of sides is: %d\n", sides);
    printf("Area of flat plate is: %f\n", base_plate->area);
    printf("normal of flat plate is: %f %f %f\n",
        base_plate->normal[0],
        base_plate->normal[1],
        base_plate->normal[2]);
}

void DemoInteractionFacet2::execute_demo_2 (

```

```

    char* interaction_name){
    DemoFacet* base_plate = dynamic_cast<DemoFacet*> (base_facet);
    printf("\n\n\n");
    printf("DemoInteractionFacet2::execute_demo_2\n");
    printf("The interaction name is: %s\n", interaction_name);
    printf("The color is: %s\n", color);
    printf("the name of the DemoFacet is: %s\n", base_plate->name);
    printf("the semi-random int of the DemoFacet is: %d\n",
        base_plate->some_int);

}

```

Like the implementations of “execute_demo_1,” both implementations print out information supplied by the interaction itself, the original geometric facet the interaction facet was created from, and from the interaction facet itself.

The following is the input file that is used for this demonstration test. This input file will dictate what will be expected from the output of the two interactions.

```

// allocate the flat plate and populate it

FlatPlate** temp_flat_plate;
temp_flat_plate = alloc(1);
temp_flat_plate[0] = new FlatPlate[1];

temp_flat_plate[0]->position[0] = 1255.0, 0.0, 383.4;
temp_flat_plate[0]->area = 119.4454385;
temp_flat_plate[0]->normal[0] = 1.0, 0.0, 0.0;
temp_flat_plate[0]->param_name = "flat_plate_material";

// allocate the DemoFacet and populate it

DemoFacet** temp_demo_facet;
temp_demo_facet = alloc(1);
temp_demo_facet[0] = new DemoFacet[1];

temp_demo_facet[0]->name = "demo_basic_facet";
temp_demo_facet[0]->some_int = 1337; // random integer
temp_demo_facet[0]->param_name = "demo_basic_facet";

// load the facets onto the surface

surface_model.facet_ptr = temp_flat_plate;
surface_model.integer = 1;

call surface_model.surface_model.surface.add_facets(
    surface_model.facet_ptr);

```



```

surface_model.facet_ptr = temp_demo_facet;

call surface_model.surface_model.surface.add_facets(
    surface_model.facet_ptr);

// facets have now been added to the surface.
// add the facet factories onto the surface factories

// Add the factory to create a FlatPlateDemo1 from a FlatPlate

FlatPlateDemoFactory1* fpf1_ptr;
fpf1_ptr = new FlatPlateDemoFactory1;

surface_model.facet_factory = fpf1_ptr;

call surface_model.surface_model.surf_fact1.add_facet_factory(
    surface_model.facet_factory);

// Add the factory to create a FlatPlateDemo2 from a FlatPlate

FlatPlateDemoFactory2* fpf2;
fpf2 = new FlatPlateDemoFactory2;

surface_model.facet_factory = fpf2;

call surface_model.surface_model.surf_fact2.add_facet_factory(
    surface_model.facet_factory);

// Add the factory to create a DemoInteractionFacet1 from a DemoFacet

DemoFacetFactory1* dff1;
dff1 = new DemoFacetFactory1;

surface_model.facet_factory = dff1;

call surface_model.surface_model.surf_fact1.add_facet_factory(
    surface_model.facet_factory);

// Add the factory to create a DemoINteractionFacet2 from a DemoFacet

DemoFacetFactory2* dff2;
dff2 = new DemoFacetFactory2;

surface_model.facet_factory = dff2;

```

```

call surface_model.surface_model.surf_fact2.add_facet_factory(
    surface_model.facet_factory);

// The facet factories have now all been added.
// Now add the params to the facet factories

DemoParams1* params1;
params1 = new DemoParams1;

params1->weight = 3.14;
params1->name = "demo_basic_facet";

surface_model.facet_params = params1;

call surface_model.surface_model.surf_fact1.add_facet_params(
    surface_model.facet_params);

// Add demo params to surface factory 2

DemoParams2* params2;
params2 = new DemoParams2;

params2->color = "burnt orange";
params2->name = "demo_basic_facet";

surface_model.facet_params = params2;

call surface_model.surface_model.surf_fact2.add_facet_params(
    surface_model.facet_params);

// add flat plate demo params to surface factory 1

FlatPlateDemoParams1* fpparams1;
fpparams1 = new FlatPlateDemoParams1;

fpparams1->shape = "octagon";
fpparams1->name = "flat_plate_material";

surface_model.facet_params = fpparams1;

call surface_model.surface_model.surf_fact1.add_facet_params(
    surface_model.facet_params);

// add the flat plate demo params to surface actory 2

FlatPlateDemoParams2* fpparams2;

```

```

fpparams2 = new FlatPlateDemoParams2;

fpparams2->sides = 6;
fpparams2->name = "flat_plate_material";

surface_model.facet_params = fpparams2;

call surface_model.surface_model.surf_fact2.add_facet_params(
    surface_model.facet_params);

surface_model.inter1.interaction_number = 24601;
surface_model.inter2.interaction_name = "demonstration interaction";

stop = 0.1;

```

Running this verification test should output, correctly, the values defined by the input file, demonstrating the geometric extensibility, the environmental interaction extensibility, the reusability of surface models across different interactions, and the successful use of the surface model for environmental interactions.

Results:

The output from the demonstration test is as follows:

```

FlatPlateDemo1::execute_demo_1
The interaction number is: 24601
The shape is: octagon
Area of flat plate is: 119.445438
normal of flat plate is: 1.000000 0.000000 0.000000

```

```

DemoInteractionFacet1::execute_demo_1
The interaction number is: 24601
The weight is: 3.140000
the name of the DemoFacet is: demo_basic_facet
the semi-random int of the DemoFacet is: 1337

```

```

FlatPlateDemo2::execute_demo_2
The interaction name is: demonstration interaction
The number of sides is: 6
Area of flat plate is: 119.445438
normal of flat plate is: 1.000000 0.000000 0.000000

```

```
DemoInteractionFacet2::execute_demo_2
The interaction name is: demonstration interaction
The color is: burnt orange
the name of the DemoFacet is: demo_basic_facet
the semi-random int of the DemoFacet is: 1337
```

All values match correctly, which makes this a successful demonstration of the utility of the Surface Model.

Test SM.2: Basic Articulation Test

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_0

The purpose of this test is to qualitatively demonstrate the basic functionality of the articulation feature.

Requirements:

By passing this test, the Surface Model partially satisfies the requirement **SM.7**

Procedure:

This is a simple test, used to qualitatively demonstrate that the articulation feature of the Surface Model is behaving in an expected fashion.

For this demonstration, three mass bodies will be used: A, B and C. Body A will be a parent to both Body B and Body C; thus Body B and Body C will be siblings to one another. Initially, all bodies will have zero relative state, meaning that their structural frames will be coincident and aligned.

Six FlatPlates will be examined, two connected to each MassBody. For all MassBodys, the first FlatPlate has a normal pointing in the positive X direction, and the second FlatPlate has a normal pointing in the negative X direction. All FlatPlates are positioned coincident with the structural frame of the MassBody to which they are attached.

This test runs for 360 seconds. MassBody B will be reoriented with respect to MassBody A, rotating it around the Z axis with no change in position, at a rate of one degree per second. This should cause the normals of the two FlatPlates associated with to make a full rotation in the X-Y plane, with no change in position.

MassBody C will be re-positioned with respect to MassBody A. The functions used to reposition are as follows:

$$x = t \tag{5.1}$$

$$y = -t \tag{5.2}$$

$$z = 2 * t \quad (5.3)$$

Results:

The following items are expected to always hold their nominal value.

- All FlatPlate 1 attributes,
- All FlatPlate 2 attributes,
- FlatPlate 3's local and global position,
- FlatPlate 4's local and global position,
- FlatPlate 5's local and global normal,
- FlatPlate 6's local and global normal.

All of these values have been checked, and it has been verified that they hold their nominal values throughout the simulation.

FlatPlate 3's local normal is completely in the X direction. Thus, if MassBody B rotates in the Z direction relative to , it is expected that FlatPlate's local normal will remain stationary, but the “global” normal will rotate through the X-Y plane, in a counter-clockwise manner, returning to its original position at the end of the simulation. This behavior is shown below in Figure 5.1.

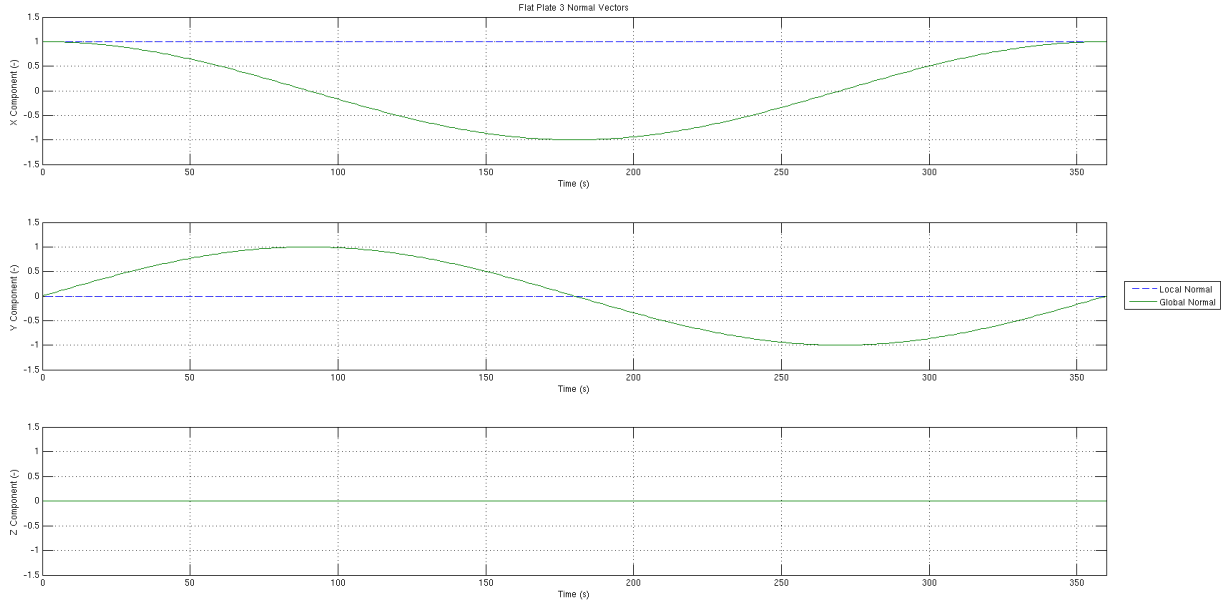


Figure 5.1: FlatPlate 3's Local and “Global” Normal

Similarly, FlatPlate 4's local normal stays in the negative X direction, and the “global” normal rotates through the X-Y plane in a counter-clockwise manner, returning to its original position at the end of the simulation. This behavior is shown below in Figure 5.2.

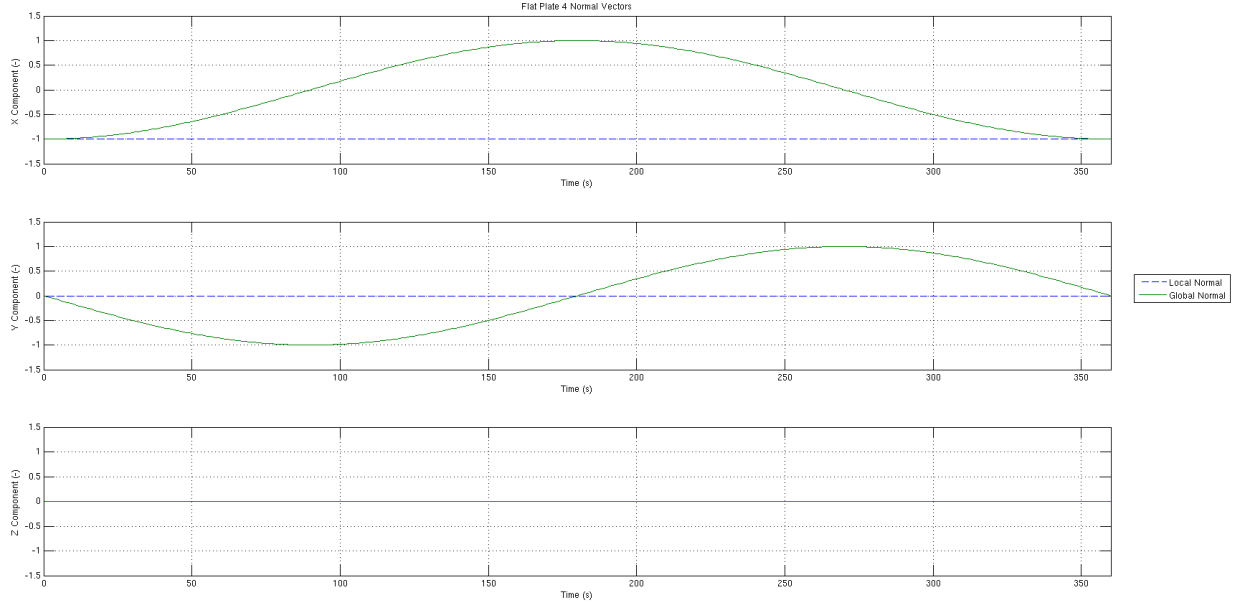


Figure 5.2: FlatPlate 4's Local and “Global” Normal

FlatPlate 5 and 6's local positions stays constant at the origin. Their “global” positions move in the manner described in Equations 5.1, 5.2, and 5.3. as shown in Figures 5.3 and 5.4, shown below.

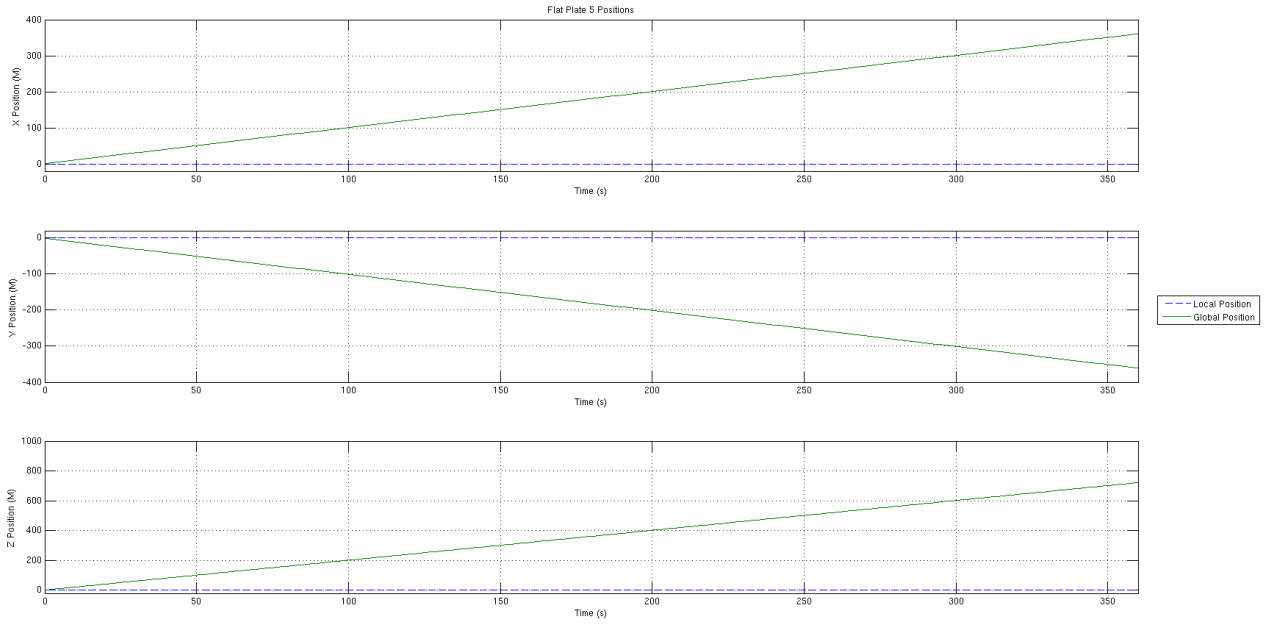


Figure 5.3: FlatPlate 5's Local and "Global" Position

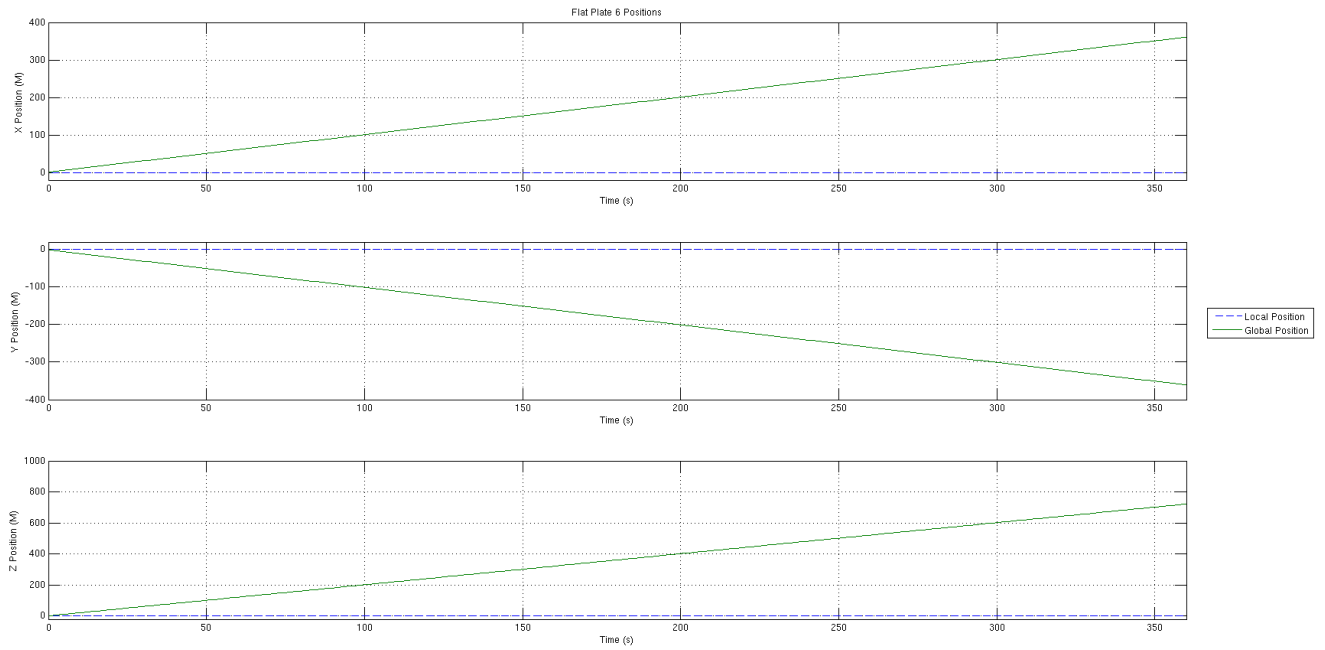


Figure 5.4: FlatPlate 6's Local and "Global" Position

All behavior is qualitatively as expected, which demonstrates the articulation feature of the Surface Model.

Test SM_3: Articulation Test, Configuration 1

The goal of the following tests is to demonstrate the correct relative state computations of FlatPlates associated with MassBody objects that have been placed in various configurations. For these tests, the following configuration will be used.

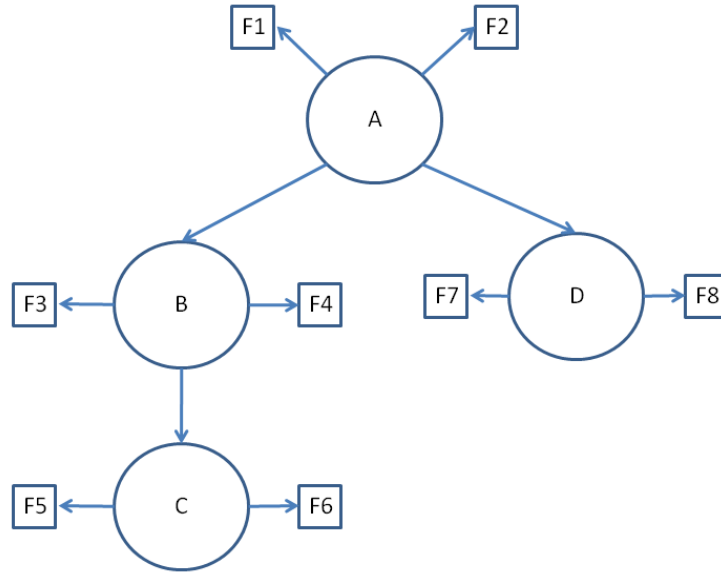


Figure 5.5: The MassBody and FlatPlate configuration for Articulation Validation Testing

Figure 5.5 shows this configuration. Four MassBody objects are used, labeled A through D. MassBody B is a child of MassBody A. MassBody C is a child of MassBody B. MassBody D is a child of MassBody A. Each child body will have a position and orientation (in the form of a rotation matrix) defined. Further information about these definitions can be found in the MassBody documentation [9].

This configuration also involves eight FlatPlate objects, labeled as F1 - F8 in Figure 5.5. FlatPlates 1 and 2 are attached to MassBody A. FlatPlates 3 and 4 are attached to MassBody B. FlatPlates 5 and 6 are attached to MassBody C, and FlatPlates 7 and 8 are attached to MassBody D. Each FlatPlate will have its position and normal defined with respect to its attached MassBody's structural reference frame.

The six tests that follow will use this configuration of MassBodys and FlatPlates. All tests will randomly position and orient MassBodys with respect to their parent, and each FlatPlate with respect to the appropriate MassBody. A final, "global" MassBody structural frame will then be selected, and the position and orientation of all FlatPlates relative to this "global" structural frame will be computed using the articulation feature. These results will then be compared to an independently programmed Matlab solution.

Note that all random relative positions and orientations were created in Matlab, and the states themselves will be presented with each test.

- $x_{A:B}$: (Location of MassBody B's structural origin in MassBody A's structural coordinates.)
- $T_{A:B}$: (The transformation matrix from MassBody A's structural reference frame to MassBody B's structural reference frame.)
- $x_{A:Fn}$: (FlatPlate n's position defined in MassBody A's structural reference frame.)
- $\hat{x}_{A:Fn}$: (FlatPlate n's normal defined in MassBody A's structural reference frame.)

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_1

The purpose of this test is to demonstrate the relative state calculation between mass body structural frames, which is used by the articulation feature.

Requirements:

By passing this test, the Surface Model partially satisfies the requirement [SM_7](#)

Procedure:

The following relative positions and orientations were input for MassBodys B, C and D, and for all FlatPlates, configured as shown in [5.5](#).

$$x_{A:B} = \begin{pmatrix} -2.0381 \\ -4.09991 \\ 3.59179 \end{pmatrix}$$

$$T_{A:B} = \begin{pmatrix} 0.5738961762045672 & -0.6152633149134586 & 0.5404574287207816 \\ 0.6713942538549126 & 0.7313744132614041 & 0.119671314512468 \\ -0.468906104490421 & 0.2941811022962542 & 0.8328172333852003 \end{pmatrix}$$

$$x_{B:C} = \begin{pmatrix} 1.40503 \\ -2.20043 \\ -2.63571 \end{pmatrix}$$

$$T_{B:C} = \begin{pmatrix} 0.1200730155375398 & 0.1674994268654244 & 0.9785327858275759 \\ -0.9674416511940138 & -0.2014627819906493 & 0.1531972552221103 \\ 0.2227983897489432 & -0.9650682304751009 & 0.137855678348538 \end{pmatrix}$$

$$x_{A:D} = \begin{pmatrix} 3.4757 \\ -0.339964 \\ -1.27395 \end{pmatrix}$$

$$T_{A:D} = \begin{pmatrix} 0.8775360833103077 & 0.2816997479818719 & 0.3880408154760973 \\ -0.3435153756221815 & 0.9339299286459263 & 0.0988538066569347 \\ -0.3345558386869913 & -0.2200457687990501 & 0.9163254064108879 \end{pmatrix}$$

$$x_{A:F1} = \begin{pmatrix} 0.00575529 \\ -2.31225 \\ 2.12175 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -1.70562 \\ 3.03695 \\ -0.958726 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} -2.73297 \\ -2.12864 \\ -3.22221 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} 2.29363 \\ -3.30972 \\ 3.85143 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} -1.3239 \\ -1.59037 \\ 0.596073 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} 1.09338 \\ 0.528991 \\ 0.548487 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.694371 \\ -3.48133 \\ -0.4691 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} -2.93046 \\ 1.31073 \\ 0.22227 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.760258 \\ 0.282587 \\ -0.584938 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.69449 \\ -0.396341 \\ 0.600498 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} -0.273795 \\ 0.820658 \\ 0.501555 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} 0.046571 \\ -0.84212 \\ 0.537275 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} 0.2905 \\ 0.71079 \\ 0.640615 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} -0.0100222 \\ -0.542243 \\ 0.840162 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} 0.959905 \\ 0.192204 \\ 0.20406 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} 0.401064 \\ 0.648818 \\ -0.64667 \end{pmatrix}$$

For this test, all FlatPlate positions and normals will be determined in MassBody A's structural reference frame.

Results:

The following are the results from the independently programmed Matlab solution:

$$x_{A:F1} = \begin{pmatrix} 0.005755290000000 \\ -2.312250000000000 \\ 2.121750000000000 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.760258000000000 \\ 0.282587000000000 \\ -0.584938000000000 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -1.705620000000000 \\ 3.036950000000000 \\ -0.958726000000000 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.694490000000000 \\ -0.396341000000000 \\ 0.600498000000000 \end{pmatrix}$$

$$x_{A:F3} = \begin{pmatrix} -3.524783758257438 \\ -4.923159938915734 \\ -0.823513103480981 \end{pmatrix}$$

$$\hat{x}_{A:F3} = \begin{pmatrix} 0.158672960778442 \\ 0.916212285307206 \\ 0.367938327419081 \end{pmatrix}$$

$$x_{A:F4} = \begin{pmatrix} -4.749880541258142 \\ -6.798722997227628 \\ 7.642858106345402 \end{pmatrix}$$

$$\hat{x}_{A:F4} = \begin{pmatrix} -0.790599137524367 \\ -0.486502296998308 \\ 0.371843914602749 \end{pmatrix}$$

$$x_{A:F5} = \begin{pmatrix} -0.242053578687549 \\ -9.056812083026088 \\ 1.439752668545422 \end{pmatrix}$$

$$\hat{x}_{A:F5} = \begin{pmatrix} -0.997026104738064 \\ -0.065859729793698 \\ 0.040021179234804 \end{pmatrix}$$

$$x_{A:F6} = \begin{pmatrix} -2.500561635645481 \\ -7.160482600091685 \\ 2.720484460501432 \end{pmatrix}$$

$$\hat{x}_{A:F6} = \begin{pmatrix} -0.075122497880330 \\ -0.944778584252594 \\ 0.318982975777274 \end{pmatrix}$$

$$x_{A:F7} = \begin{pmatrix} 4.219194918838575 \\ -3.683662944055208 \\ -2.317385259959287 \end{pmatrix}$$

$$\hat{x}_{A:F7} = \begin{pmatrix} 0.708056780351428 \\ 0.405007525010866 \\ 0.578467778466478 \end{pmatrix}$$

$$x_{A:F8} = \begin{pmatrix} 0.379497974748256 \\ 0.009746558872154 \\ -2.077845790037692 \end{pmatrix}$$

$$\hat{x}_{A:F8} = \begin{pmatrix} 0.345416396940049 \\ 0.861227173478076 \\ -0.372792819818084 \end{pmatrix}$$

All Surface Model articulation produced results are a numerical match to the independently programmed Matlab solution.

Test SM_4: Articulation Test, Configuration 2

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_2

The purpose of this test is to demonstrate the relative state calculation between mass body structural frames, which is used by the articulation feature.

Requirements:

By passing this test, the Surface Model partially satisfies the requirement [SM_7](#)

Procedure:

The following relative positions and orientations were input for MassBodys B, C and D, and for all FlatPlates, configured as shown in [5.5](#).

$$x_{A:B} = \begin{pmatrix} 0.0978881 \\ 1.65429 \\ -2.12155 \end{pmatrix}$$

$$T_{A:B} = \begin{pmatrix} 0.1908098464799607 & -0.6966135920642235 & -0.6916076241899547 \\ 0.04030743089433808 & 0.7095182653790713 & -0.703533326934959 \\ 0.9807991198512527 & 0.1063641595879615 & 0.1634617755138939 \end{pmatrix}$$

$$x_{B:C} = \begin{pmatrix} -1.88698 \\ 1.08009 \\ -3.95204 \end{pmatrix}$$

$$T_{B:C} = \begin{pmatrix} -0.7361133641239929 & -0.5508618941680473 & -0.3933043207385965 \\ -0.4364024092758288 & -0.05791070693348288 & 0.897886010137543 \\ -0.517387719545323 & 0.8325848446711333 & -0.197768612493578 \end{pmatrix}$$

$$x_{A:D} = \begin{pmatrix} 4.42141 \\ 2.94013 \\ -0.773762 \end{pmatrix}$$

$$T_{A:D} = \begin{pmatrix} 0.8222190420975497 & -0.3626722656735943 & 0.4386623696231186 \\ 0.04304325740965631 & 0.808117347462562 & 0.5874467045797761 \\ -0.5675412978839106 & -0.4641284094313281 & 0.6800600670198124 \end{pmatrix}$$

$$x_{A:F1} = \begin{pmatrix} 3.39326 \\ 2.47589 \\ 0.948552 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -4.94456 \\ -0.00261188 \\ -4.32719 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} -3.6932 \\ 2.92994 \\ -1.23367 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} -2.90045 \\ 0.0849147 \\ -0.604298 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} 2.44785 \\ 0.962552 \\ 0.615419 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} -2.22592 \\ -0.619661 \\ 2.45179 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.528547 \\ -0.710206 \\ 0.832302 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} 4.29469 \\ 3.92779 \\ 2.56689 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} 0.768477 \\ 0.607306 \\ -0.201548 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.741323 \\ -0.585104 \\ -0.328777 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} 0.338868 \\ -0.512566 \\ 0.788952 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} 0.79904 \\ 0.326973 \\ 0.504603 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} -0.628147 \\ 0.721774 \\ -0.290642 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} 0.772102 \\ 0.554193 \\ 0.311013 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} 0.360979 \\ 0.56045 \\ 0.745379 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} -0.0567124 \\ -0.673532 \\ -0.736979 \end{pmatrix}$$

For this test, all FlatPlate positions and normals will be determined in MassBody A's structural reference frame.

Results:

The following are the results from the independently programmed Matlab solution:

$$x_{A:F1} = \begin{pmatrix} 3.393260000000000 \\ 2.475890000000000 \\ 0.948552000000000 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} 0.768477000000000 \\ 0.607306000000000 \\ -0.201548000000000 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -4.944560000000000 \\ -0.002611880000000 \\ -4.327190000000000 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.741323000000000 \\ -0.585104000000000 \\ -0.328777000000000 \end{pmatrix}$$

$$x_{A:F3} = \begin{pmatrix} -1.698694921132129 \\ 6.174650991917465 \\ -1.830273046859699 \end{pmatrix}$$

$$\hat{x}_{A:F3} = \begin{pmatrix} 0.817802559638069 \\ -0.515818777492667 \\ 0.255207065574980 \end{pmatrix}$$

$$x_{A:F4} = \begin{pmatrix} -1.044818572348511 \\ 3.670755774841175 \\ -0.274096611834425 \end{pmatrix}$$

$$\hat{x}_{A:F4} = \begin{pmatrix} 0.660558319607464 \\ -0.270957134796642 \\ -0.700175256231008 \end{pmatrix}$$

$$x_{A:F5} = \begin{pmatrix} -4.831430641784406 \\ 4.428271095306710 \\ 0.125952487453193 \end{pmatrix}$$

$$\hat{x}_{A:F5} = \begin{pmatrix} 0.993640457587366 \\ -0.061953197643265 \\ -0.094019015078572 \end{pmatrix}$$

$$x_{A:F6} = \begin{pmatrix} -4.002062137405464 \\ 5.194819674814850 \\ -5.016452941828739 \end{pmatrix}$$

$$\hat{x}_{A:F6} = \begin{pmatrix} -0.063419258454724 \\ 0.549761951194300 \\ 0.832910715802174 \end{pmatrix}$$

$$x_{A:F7} = \begin{pmatrix} 3.483893254973209 \\ 2.171594545706472 \\ -0.856808499849251 \end{pmatrix}$$

$$\hat{x}_{A:F7} = \begin{pmatrix} -0.102105963862838 \\ -0.023959274098709 \\ 0.994484901801080 \end{pmatrix}$$

$$x_{A:F8} = \begin{pmatrix} 6.664834691801769 \\ 3.365313710639066 \\ 5.163163569410596 \end{pmatrix}$$

$$\hat{x}_{A:F8} = \begin{pmatrix} 0.342644991720493 \\ -0.181671987617076 \\ -0.921731737732234 \end{pmatrix}$$

All Surface Model articulation produced results are a numerical match to the independently programmed Matlab solution.

Test SM_5: Articulation Test, Configuration 3

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_3

The purpose of this test is to demonstrate the relative state calculation between mass body structural frames, which is used by the articulation feature.

Requirements:

By passing this test, the Surface Model partially satisfies the requirement [SM_7](#)

Procedure:

The following relative positions and orientations were input for MassBodys B, C and D, and for all FlatPlates, configured as shown in [5.5](#).

$$x_{A:B} = \begin{pmatrix} -0.126141 \\ 4.21103 \\ 2.79516 \end{pmatrix}$$

$$T_{A:B} = \begin{pmatrix} 0.997369704807009 & 0.06997143703733257 & 0.01891216360204106 \\ -0.07007880132551818 & 0.9975285522158546 & 0.005074358966393988 \\ -0.01851036298829154 & -0.006386353660100277 & 0.99980827209469 \end{pmatrix}$$

$$x_{B:C} = \begin{pmatrix} 2.69991 \\ 3.53459 \\ 4.99746 \end{pmatrix}$$

$$T_{B:C} = \begin{pmatrix} -0.07082185013447745 & 0.9972707676557767 & 0.02086340151527186 \\ 0.9728231355161533 & 0.06443288212731174 & 0.2224040258297676 \\ 0.2204527444783792 & 0.03604746426623952 & -0.9747313310712469 \end{pmatrix}$$

$$x_{A:D} = \begin{pmatrix} -1.67924 \\ -0.878345 \\ 1.04473 \end{pmatrix}$$

$$T_{A:D} = \begin{pmatrix} 0.2629583935566351 & 0.4849501785352546 & -0.8340720637910962 \\ -0.2381525060753064 & -0.8051199041282633 & -0.5431991566879935 \\ -0.9349525480515922 & 0.3414751298632461 & -0.09622093627020228 \end{pmatrix}$$

$$x_{A:F1} = \begin{pmatrix} -1.49968 \\ 0.670615 \\ 1.06301 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} 2.28029 \\ 0.508347 \\ 4.97695 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} 3.8862 \\ -4.52567 \\ 2.66886 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} 3.64855 \\ -3.53627 \\ -3.90689 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} -0.639442 \\ -2.7477 \\ -2.42615 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} -3.61362 \\ 0.551767 \\ -0.587464 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.431173 \\ -1.83218 \\ -1.84599 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} 1.14477 \\ -3.2097 \\ 2.4224 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.496347 \\ -0.260678 \\ -0.828062 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.12748 \\ 0.820292 \\ -0.557557 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} -0.247273 \\ -0.23111 \\ -0.940981 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} -0.138757 \\ 0.861377 \\ -0.488648 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} 0.81173 \\ -0.130319 \\ 0.569308 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} 0.798565 \\ -0.347707 \\ -0.491318 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} -0.706014 \\ -0.123783 \\ 0.697296 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} 0.31147 \\ -0.909147 \\ -0.276475 \end{pmatrix}$$

For this test, all FlatPlate positions and normals will be determined in MassBody A's structural reference frame.

Results:

The following are the results from the independently programmed Matlab solution:

$$x_{A:F1} = \begin{pmatrix} -1.499680000000000 \\ 0.670615000000000 \\ 1.063010000000000 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.496347000000000 \\ -0.260678000000000 \\ -0.828062000000000 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} 2.280290000000000 \\ 0.508347000000000 \\ 4.976950000000000 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.127480000000000 \\ 0.820292000000000 \\ -0.557557000000000 \end{pmatrix}$$

$$x_{A:F3} = \begin{pmatrix} 4.017589108250925 \\ -0.048576328121540 \\ 5.514039881109446 \end{pmatrix}$$

$$\hat{x}_{A:F3} = \begin{pmatrix} -0.213008787367317 \\ -0.241831433399704 \\ -0.946649790215024 \end{pmatrix}$$

$$x_{A:F4} = \begin{pmatrix} 3.832947751292330 \\ 0.963744774509309 \\ -1.059923269035887 \end{pmatrix}$$

$$\hat{x}_{A:F4} = \begin{pmatrix} -0.189711243925774 \\ 0.852659803976348 \\ -0.486807571524059 \end{pmatrix}$$

$$x_{A:F5} = \begin{pmatrix} -0.896800453641627 \\ 6.761513732028066 \\ 9.536339519032627 \end{pmatrix}$$

$$\hat{x}_{A:F5} = \begin{pmatrix} -0.105690202004579 \\ 0.819118589489993 \\ -0.563803645853018 \end{pmatrix}$$

$$x_{A:F6} = \begin{pmatrix} 3.127969586147725 \\ 4.355819180534397 \\ 8.474810754421558 \end{pmatrix}$$

$$\hat{x}_{A:F6} = \begin{pmatrix} -0.562542495689039 \\ 0.716526508239595 \\ 0.412474602529563 \end{pmatrix}$$

$$x_{A:F7} = \begin{pmatrix} 0.369630753333818 \\ -0.242677512360114 \\ 2.577220871007037 \end{pmatrix}$$

$$\hat{x}_{A:F7} = \begin{pmatrix} -0.808111747555158 \\ -0.004612216102558 \\ 0.589010901280250 \end{pmatrix}$$

$$x_{A:F8} = \begin{pmatrix} -2.878644073458437 \\ 3.088194126743018 \\ 1.600330060734381 \end{pmatrix}$$

$$\hat{x}_{A:F8} = \begin{pmatrix} 0.556910293004496 \\ 0.788610441057933 \\ 0.260662141351711 \end{pmatrix}$$

All Surface Model articulation produced results are a numerical match to the independently programmed Matlab solution.

Test SM_6: Articulation Test, Configuration 4

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_4

The purpose of this test is to demonstrate the relative state calculation between mass body structural frames, which is used by the articulation feature.

Requirements:

By passing this test, the Surface Model partially satisfies the requirement [SM_7](#)

Procedure:

$$x_{A:B} = \begin{pmatrix} -2.0381 \\ -4.09991 \\ 3.59179 \end{pmatrix}$$

$$T_{A:B} = \begin{pmatrix} 0.5738961762045672 & -0.6152633149134586 & 0.5404574287207816 \\ 0.6713942538549126 & 0.7313744132614041 & 0.119671314512468 \\ -0.468906104490421 & 0.2941811022962542 & 0.8328172333852003 \end{pmatrix}$$

$$x_{B:C} = \begin{pmatrix} 1.40503 \\ -2.20043 \\ -2.63571 \end{pmatrix}$$

$$T_{B:C} = \begin{pmatrix} 0.1200730155375398 & 0.1674994268654244 & 0.9785327858275759 \\ -0.9674416511940138 & -0.2014627819906493 & 0.1531972552221103 \\ 0.2227983897489432 & -0.9650682304751009 & 0.137855678348538 \end{pmatrix}$$

$$x_{A:D} = \begin{pmatrix} 3.4757 \\ -0.339964 \\ -1.27395 \end{pmatrix}$$

$$T_{A:D} = \begin{pmatrix} 0.8775360833103077 & 0.2816997479818719 & 0.3880408154760973 \\ -0.3435153756221815 & 0.9339299286459263 & 0.0988538066569347 \\ -0.3345558386869913 & -0.2200457687990501 & 0.9163254064108879 \end{pmatrix}$$

$$x_{A:F1} = \begin{pmatrix} 0.00575529 \\ -2.31225 \\ 2.12175 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -1.70562 \\ 3.03695 \\ -0.958726 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} -2.73297 \\ -2.12864 \\ -3.22221 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} 2.29363 \\ -3.30972 \\ 3.85143 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} -1.3239 \\ -1.59037 \\ 0.596073 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} 1.09338 \\ 0.528991 \\ 0.548487 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.694371 \\ -3.48133 \\ -0.4691 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} -2.93046 \\ 1.31073 \\ 0.22227 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.760258 \\ 0.282587 \\ -0.584938 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.69449 \\ -0.396341 \\ 0.600498 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} -0.273795 \\ 0.820658 \\ 0.501555 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} 0.046571 \\ -0.84212 \\ 0.537275 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} 0.2905 \\ 0.71079 \\ 0.640615 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} -0.0100222 \\ -0.542243 \\ 0.840162 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} 0.959905 \\ 0.192204 \\ 0.20406 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} 0.401064 \\ 0.648818 \\ -0.64667 \end{pmatrix}$$

The following relative positions and orientations were input for MassBodys B, C and D, and for all FlatPlates, configured as shown in [5.5](#).

For this test, all FlatPlate positions and normals will be determined in MassBody B's structural reference frame.

Results:

The following are the results from the independently programmed Matlab solution:

$$x_{B:F1} = \begin{pmatrix} -0.721414920408415 \\ 2.503759861841939 \\ -1.656755078610698 \end{pmatrix}$$

$$\hat{x}_{B:F1} = \begin{pmatrix} -0.926308660941458 \\ -0.373756250695222 \\ -0.047525074519602 \end{pmatrix}$$

$$x_{B:F2} = \begin{pmatrix} -6.659599317721549 \\ 4.898375725120448 \\ -1.846120705482019 \end{pmatrix}$$

$$\hat{x}_{B:F2} = \begin{pmatrix} 0.966962837940397 \\ 0.248265314055368 \\ 0.057858450240594 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} -2.732970000000000 \\ -2.128640000000000 \\ -3.222210000000000 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} -0.273795000000000 \\ 0.820658000000000 \\ 0.501555000000000 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} 2.293630000000000 \\ -3.309720000000000 \\ 3.851430000000000 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} 0.046571000000000 \\ -0.842120000000000 \\ 0.537275000000000 \end{pmatrix}$$

$$x_{B:F5} = \begin{pmatrix} 2.917459618112097 \\ -2.677033241976651 \\ -4.092657826184467 \end{pmatrix}$$

$$\hat{x}_{B:F5} = \begin{pmatrix} -0.510038649789519 \\ -0.712776331772535 \\ 0.481467266707483 \end{pmatrix}$$

$$x_{B:F6} = \begin{pmatrix} 1.146749527619891 \\ -2.653188853690494 \\ -1.409149805944291 \end{pmatrix}$$

$$\hat{x}_{B:F6} = \begin{pmatrix} 0.710571808220327 \\ -0.703250584113397 \\ 0.022943911883140 \end{pmatrix}$$

$$x_{B:F7} = \begin{pmatrix} 0.141278416984113 \\ 3.798385528453287 \\ -7.732894758882457 \end{pmatrix}$$

$$\hat{x}_{B:F7} = \begin{pmatrix} 0.469802014524136 \\ 0.840823394154425 \\ 0.268891348378292 \end{pmatrix}$$

$$x_{B:F8} = \begin{pmatrix} -4.205267465126678 \\ 3.950366275027509 \\ -4.646413544976000 \end{pmatrix}$$

$$\hat{x}_{B:F8} = \begin{pmatrix} -0.533126985089867 \\ 0.817177495991682 \\ -0.219079382721772 \end{pmatrix}$$

All Surface Model articulation produced results are a numerical match to the independently programmed Matlab solution.

Test SM.7: Articulation Test, Configuration 5

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_5

The purpose of this test is to demonstrate the relative state calculation between mass body structural frames, which is used by the articulation feature.

Requirements:

By passing this test, the Surface Model partially satisfies the requirement [SM.7](#)

Procedure:

The following relative positions and orientations were input for MassBodys B, C and D, and for all FlatPlates, configured as shown in [5.5](#).

$$x_{A:B} = \begin{pmatrix} -2.0381 \\ -4.09991 \\ 3.59179 \end{pmatrix}$$

$$T_{A:B} = \begin{pmatrix} 0.5738961762045672 & -0.6152633149134586 & 0.5404574287207816 \\ 0.6713942538549126 & 0.7313744132614041 & 0.119671314512468 \\ -0.468906104490421 & 0.2941811022962542 & 0.8328172333852003 \end{pmatrix}$$

$$x_{B:C} = \begin{pmatrix} 1.40503 \\ -2.20043 \\ -2.63571 \end{pmatrix}$$

$$T_{B:C} = \begin{pmatrix} 0.1200730155375398 & 0.1674994268654244 & 0.9785327858275759 \\ -0.9674416511940138 & -0.2014627819906493 & 0.1531972552221103 \\ 0.2227983897489432 & -0.9650682304751009 & 0.137855678348538 \end{pmatrix}$$

$$x_{A:D} = \begin{pmatrix} 3.4757 \\ -0.339964 \\ -1.27395 \end{pmatrix}$$

$$T_{A:D} = \begin{pmatrix} 0.8775360833103077 & 0.2816997479818719 & 0.3880408154760973 \\ -0.3435153756221815 & 0.9339299286459263 & 0.0988538066569347 \\ -0.3345558386869913 & -0.2200457687990501 & 0.9163254064108879 \end{pmatrix}$$

$$x_{A:F1} = \begin{pmatrix} 0.00575529 \\ -2.31225 \\ 2.12175 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -1.70562 \\ 3.03695 \\ -0.958726 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} -2.73297 \\ -2.12864 \\ -3.22221 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} 2.29363 \\ -3.30972 \\ 3.85143 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} -1.3239 \\ -1.59037 \\ 0.596073 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} 1.09338 \\ 0.528991 \\ 0.548487 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.694371 \\ -3.48133 \\ -0.4691 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} -2.93046 \\ 1.31073 \\ 0.22227 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.760258 \\ 0.282587 \\ -0.584938 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.69449 \\ -0.396341 \\ 0.600498 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} -0.273795 \\ 0.820658 \\ 0.501555 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} 0.046571 \\ -0.84212 \\ 0.537275 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} 0.2905 \\ 0.71079 \\ 0.640615 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} -0.0100222 \\ -0.542243 \\ 0.840162 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} 0.959905 \\ 0.192204 \\ 0.20406 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} 0.401064 \\ 0.648818 \\ -0.64667 \end{pmatrix}$$

For this test, all FlatPlate positions and normals will be determined in MassBody C's structural reference frame.

Results:

The following are the results from the independently programmed Matlab solution:

$$x_{C:F1} = \begin{pmatrix} 1.490559938183432 \\ 1.259465415337173 \\ -4.878678195182763 \end{pmatrix}$$

$$\hat{x}_{C:F1} = \begin{pmatrix} -0.220333475582930 \\ 0.964166843537344 \\ 0.147768604032725 \end{pmatrix}$$

$$x_{C:F2} = \begin{pmatrix} 0.993340541039701 \\ 6.492876065883191 \\ -8.538768937726466 \end{pmatrix}$$

$$\hat{x}_{C:F2} = \begin{pmatrix} 0.214306832176674 \\ -0.976632589653420 \\ -0.016179088177458 \end{pmatrix}$$

$$x_{C:F3} = \begin{pmatrix} -1.058746833327544 \\ 3.898960349333953 \\ -1.072074340398352 \end{pmatrix}$$

$$\hat{x}_{C:F3} = \begin{pmatrix} 0.595372364759175 \\ 0.176385492488708 \\ -0.783849844252446 \end{pmatrix}$$

$$x_{C:F4} = \begin{pmatrix} 6.268770618632612 \\ 0.357624040424968 \\ 2.162808271756570 \end{pmatrix}$$

$$\hat{x}_{C:F4} = \begin{pmatrix} 0.390278505560198 \\ 0.206910168131668 \\ 0.897145611641401 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} -1.323900000000000 \\ -1.590370000000000 \\ 0.596073000000000 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} 0.290500000000000 \\ 0.710790000000000 \\ 0.640615000000000 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} 1.093380000000000 \\ 0.528991000000000 \\ 0.548487000000000 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} -0.010022200000000 \\ -0.542243000000000 \\ 0.840162000000000 \end{pmatrix}$$

$$x_{C:F7} = \begin{pmatrix} -4.134706702562834 \\ -0.766806861259732 \\ -6.773503967333159 \end{pmatrix}$$

$$\hat{x}_{C:F7} = \begin{pmatrix} 0.460366981418975 \\ -0.582707240290149 \\ -0.669712613569149 \end{pmatrix}$$

$$x_{C:F8} = \begin{pmatrix} -1.610929825206028 \\ 3.880444650171289 \\ -7.463090219546920 \end{pmatrix}$$

$$\hat{x}_{C:F8} = \begin{pmatrix} -0.141513761230369 \\ 0.317576038920061 \\ -0.937613210767787 \end{pmatrix}$$

All Surface Model articulation produced results are a numerical match to the independently programmed Matlab solution.

Test SM_8: Articulation Test, Configuration 6

Purpose:

SIM directory: SIM_ARTICULATION RUN directory: SET_test/RUN_articulation_6

The purpose of this test is to demonstrate the relative state calculation between mass body structural frames, which is used by the articulation feature.

Note also that the standard notation for relative states used in the Reference Frame documentation [8] will be followed here. The salient pieces are as follows:

Requirements:

By passing this test, the Surface Model partially satisfies the requirement **SM_7**

Procedure:

The following relative positions and orientations were input for MassBodys B, C and D, and for all FlatPlates, configured as shown in **5.5**.

$$x_{A:B} = \begin{pmatrix} -2.0381 \\ -4.09991 \\ 3.59179 \end{pmatrix}$$

$$T_{A:B} = \begin{pmatrix} 0.5738961762045672 & -0.6152633149134586 & 0.5404574287207816 \\ 0.6713942538549126 & 0.7313744132614041 & 0.119671314512468 \\ -0.468906104490421 & 0.2941811022962542 & 0.8328172333852003 \end{pmatrix}$$

$$x_{B:C} = \begin{pmatrix} 1.40503 \\ -2.20043 \\ -2.63571 \end{pmatrix}$$

$$T_{B:C} = \begin{pmatrix} 0.1200730155375398 & 0.1674994268654244 & 0.9785327858275759 \\ -0.9674416511940138 & -0.2014627819906493 & 0.1531972552221103 \\ 0.2227983897489432 & -0.9650682304751009 & 0.137855678348538 \end{pmatrix}$$

$$x_{A:D} = \begin{pmatrix} 3.4757 \\ -0.339964 \\ -1.27395 \end{pmatrix}$$

$$T_{A:D} = \begin{pmatrix} 0.8775360833103077 & 0.2816997479818719 & 0.3880408154760973 \\ -0.3435153756221815 & 0.9339299286459263 & 0.0988538066569347 \\ -0.3345558386869913 & -0.2200457687990501 & 0.9163254064108879 \end{pmatrix}$$

$$x_{A:F1} = \begin{pmatrix} 0.00575529 \\ -2.31225 \\ 2.12175 \end{pmatrix}$$

$$x_{A:F2} = \begin{pmatrix} -1.70562 \\ 3.03695 \\ -0.958726 \end{pmatrix}$$

$$x_{B:F3} = \begin{pmatrix} -2.73297 \\ -2.12864 \\ -3.22221 \end{pmatrix}$$

$$x_{B:F4} = \begin{pmatrix} 2.29363 \\ -3.30972 \\ 3.85143 \end{pmatrix}$$

$$x_{C:F5} = \begin{pmatrix} -1.3239 \\ -1.59037 \\ 0.596073 \end{pmatrix}$$

$$x_{C:F6} = \begin{pmatrix} 1.09338 \\ 0.528991 \\ 0.548487 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.694371 \\ -3.48133 \\ -0.4691 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} -2.93046 \\ 1.31073 \\ 0.22227 \end{pmatrix}$$

$$\hat{x}_{A:F1} = \begin{pmatrix} -0.760258 \\ 0.282587 \\ -0.584938 \end{pmatrix}$$

$$\hat{x}_{A:F2} = \begin{pmatrix} 0.69449 \\ -0.396341 \\ 0.600498 \end{pmatrix}$$

$$\hat{x}_{B:F3} = \begin{pmatrix} -0.273795 \\ 0.820658 \\ 0.501555 \end{pmatrix}$$

$$\hat{x}_{B:F4} = \begin{pmatrix} 0.046571 \\ -0.84212 \\ 0.537275 \end{pmatrix}$$

$$\hat{x}_{C:F5} = \begin{pmatrix} 0.2905 \\ 0.71079 \\ 0.640615 \end{pmatrix}$$

$$\hat{x}_{C:F6} = \begin{pmatrix} -0.0100222 \\ -0.542243 \\ 0.840162 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} 0.959905 \\ 0.192204 \\ 0.20406 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} 0.401064 \\ 0.648818 \\ -0.64667 \end{pmatrix}$$

For this test, all FlatPlate positions and normals will be determined in MassBody D's structural reference frame.

Results:

The following are the results from the independently programmed Matlab solution:

$$x_{D:F1} = \begin{pmatrix} -2.282923962152712 \\ -0.314319691540555 \\ 4.706449634362594 \end{pmatrix}$$

$$\hat{x}_{D:F1} = \begin{pmatrix} -0.814528959465332 \\ 0.467253421227741 \\ -0.343826871434294 \end{pmatrix}$$

$$x_{D:F2} = \begin{pmatrix} -3.473199658403271 \\ 4.964825229431776 \\ 1.279212980717872 \end{pmatrix}$$

$$\hat{x}_{D:F2} = \begin{pmatrix} 0.730808608295058 \\ -0.549361201875428 \\ 0.405119049540781 \end{pmatrix}$$

$$x_{D:F3} = \begin{pmatrix} -7.259474338796993 \\ -1.831082646567445 \\ 3.763312361159124 \end{pmatrix}$$

$$\hat{x}_{D:F3} = \begin{pmatrix} 0.540113107014310 \\ 0.837543576798951 \\ 0.082457635232693 \end{pmatrix}$$

$$x_{D:F4} = \begin{pmatrix} -5.577589023893677 \\ -2.324954515539580 \\ 12.343836397635599 \end{pmatrix}$$

$$\hat{x}_{D:F4} = \begin{pmatrix} -0.686536229216390 \\ -0.146017909387756 \\ 0.712282355654953 \end{pmatrix}$$

$$x_{D:F5} = \begin{pmatrix} -4.664969425877037 \\ -6.595559952223573 \\ 5.648536405116573 \end{pmatrix}$$

$$\hat{x}_{D:F5} = \begin{pmatrix} -0.877949201168424 \\ 0.284941670041608 \\ 0.384725482866194 \end{pmatrix}$$

$$x_{D:F6} = \begin{pmatrix} -5.615719993914686 \\ -3.922083637064444 \\ 7.160421263092290 \end{pmatrix}$$

$$\hat{x}_{D:F6} = \begin{pmatrix} -0.208288177597411 \\ -0.825018581285846 \\ 0.525319405116621 \end{pmatrix}$$

$$x_{D:F7} = \begin{pmatrix} -0.6943710000000000 \\ -3.4813300000000000 \\ -0.4691000000000000 \end{pmatrix}$$

$$\hat{x}_{D:F7} = \begin{pmatrix} 0.9599050000000000 \\ 0.1922040000000000 \\ 0.2040600000000000 \end{pmatrix}$$

$$x_{D:F8} = \begin{pmatrix} -2.9304600000000000 \\ 1.3107300000000000 \\ 0.2222700000000000 \end{pmatrix}$$

$$\hat{x}_{D:F8} = \begin{pmatrix} 0.4010640000000000 \\ 0.6488180000000000 \\ -0.6466700000000000 \end{pmatrix}$$

All Surface Model articulation produced results are a numerical match to the independently programmed Matlab solution.

5.3 Requirements Traceability

Table 5.1 summarizes the inspections and tests that demonstrate the satisfaction of the requirements levied on the model.

Table 5.1: Requirements Traceability

Requirement	Traces to
SM.1 Top-level requirement	Insp. SM.1 Top-level inspection
SM.2 Geometric Modeling	Insp. SM.2 Geometric Modeling Inspection
SM.3 Environmental Interaction	Test SM.1 Multiple Interaction, Multiple Facet Demo
SM.4 Extensible Geometrical Modeling	Test SM.1 Multiple Interaction, Multiple Facet Demo
SM.5 Extensible to Environmental Interactions	Test SM.1 Multiple Interaction, Multiple Facet Demo
SM.6 Re-use of Models	Test SM.1 Multiple Interaction, Multiple Facet Demo
SM.7 Articulation	Test SM.2 Basic Articulation Test Test SM.3 Articulation Test, Configuration 1 Test SM.4 Articulation Test, Configuration 2 Test SM.5 Articulation Test, Configuration 3 Test SM.6 Articulation Test, Configuration 4 Test SM.7 Articulation Test, Configuration 5 Test SM.8 Articulation Test, Configuration 6

5.4 Metrics

Table 5.2 presents coarse metrics on the source files that comprise the model.

Table 5.2: Coarse Metrics

File Name	Number of Lines			
	Blank	Comment	Code	Total
Total	0	0	0	0

Table 5.3 presents the extended cyclomatic complexity (ECC) of the methods defined in the model.

Table 5.3: Cyclomatic Complexity

Method	File	Line	ECC
jeod::Facet::get_mass_rel_struct ()	include/facet.hh	110	1
jeod::Facet::(std::set_name (std::string name_in)	include/facet.hh	115	1
jeod::FacetParams::(std::set_name (std::string name_in)	include/facet_params.hh	103	1
jeod::InteractionSurface::accumulate_thermal_sources (void)	include/interaction_surface.hh	100	1
jeod::InteractionSurface::thermal_integrator (void)	include/interaction_surface.hh	112	1
jeod::InteractionSurfaceFactory::create_surface (SurfaceModel & surface, InteractionSurface & inter_surface)	include/interaction_surface_factory.hh	105	1
jeod::FacetStateInfo ()	include/surface_model.hh	111	1
jeod::FacetStateInfo (MassBody* new_mass_body)	include/surface_model.hh	116	1
jeod::FacetStateInfo (MassBody& new_mass_body)	include/surface_model.hh	125	1
jeod::operator == (const FacetStateInfo& rhs)	include/surface_model.hh	134	1
jeod::Cylinder::Cylinder (void)	src/cylinder.cc	41	1
jeod::Cylinder::~~Cylinder (void)	src/cylinder.cc	53	1
jeod::Facet::Facet (void)	src/facet.cc	54	1
jeod::Facet::~~Facet (void)	src/facet.cc	75	1
jeod::Facet::initialize_mass_connection (BaseDynManager& manager)	src/facet.cc	90	2
jeod::Facet::update_articulation (void)	src/facet.cc	127	2
jeod::Facet::get_mass_body_ptr (void)	src/facet.cc	166	1

Continued on next page

Table 5.3: Cyclomatic Complexity (continued)

Method	File	Line	ECC
jeod::Facet::update_ articulation_internal (void)	src/facet.cc	181	1
jeod::FacetParams::Facet Params (void)	src/facet_params.cc	46	1
jeod::FacetParams::~~Facet Params (void)	src/facet_params.cc	60	1
jeod::FlatPlate::FlatPlate (void)	src/flat_plate.cc	41	1
jeod::FlatPlate::~~FlatPlate (void)	src/flat_plate.cc	54	1
jeod::FlatPlate::update_ articulation_internal (void)	src/flat_plate.cc	69	1
jeod::FlatPlateCircular::Flat PlateCircular (void)	src/flat_plate_circular.cc	41	1
jeod::FlatPlateCircular::~~Flat PlateCircular (void)	src/flat_plate_circular.cc	53	1
jeod::FlatPlateThermal::Flat PlateThermal (void)	src/flat_plate_thermal.cc	41	1
jeod::FlatPlateThermal::~~Flat PlateThermal (void)	src/flat_plate_thermal.cc	52	1
jeod::InteractionFacet:: InteractionFacet (void)	src/interaction_facet.cc	48	1
jeod::InteractionFacet::~~ InteractionFacet (void)	src/interaction_facet.cc	63	1
jeod::InteractionFacet Factory::InteractionFacet Factory (void)	src/interaction_facet_ factory.cc	43	1
jeod::InteractionFacet Factory::~~InteractionFacet Factory (void)	src/interaction_facet_ factory.cc	57	1
jeod::InteractionSurface:: InteractionSurface (void)	src/interaction_surface.cc	39	1
jeod::InteractionSurface::~~ InteractionSurface (void)	src/interaction_surface.cc	51	1
jeod::InteractionSurface Factory::InteractionSurface Factory (void)	src/interaction_surface_ factory.cc	60	1

Continued on next page

Table 5.3: Cyclomatic Complexity (continued)

Method	File	Line	ECC
jeod::InteractionSurface Factory::~Interaction SurfaceFactory (void)	src/interaction_surface_ factory.cc	74	1
jeod::InteractionSurface Factory::create_surface (SurfaceModel* surface, InteractionSurface* inter_ surface)	src/interaction_surface_ factory.cc	91	11
jeod::InteractionSurface Factory::add_facet_factory (InteractionFacetFactory* to_add)	src/interaction_surface_ factory.cc	198	2
jeod::InteractionSurface Factory::add_facet_params (FacetParams* to_add)	src/interaction_surface_ factory.cc	220	2
jeod::SurfaceModel::Surface Model (void)	src/surface_model.cc	56	1
jeod::SurfaceModel::~~Surface Model (void)	src/surface_model.cc	76	1
jeod::SurfaceModel::add_ facets (Facet** new_facets, unsigned int num_new_ facets)	src/surface_model.cc	88	4
jeod::SurfaceModel::add_facet (Facet* new_facet)	src/surface_model.cc	123	2
jeod::SurfaceModel::initialize_ mass_connections (BaseDyn Manager& manager)	src/surface_model.cc	148	4
jeod::SurfaceModel::update_ articulation (void)	src/surface_model.cc	210	5

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