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Bachelor Project

Barycentric Data Visualization for Triangle Meshes

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Abstract

Abstract goes here

Dedication

to somebody

Declaration

I declare that..

Acknowledgements

I want to thank...

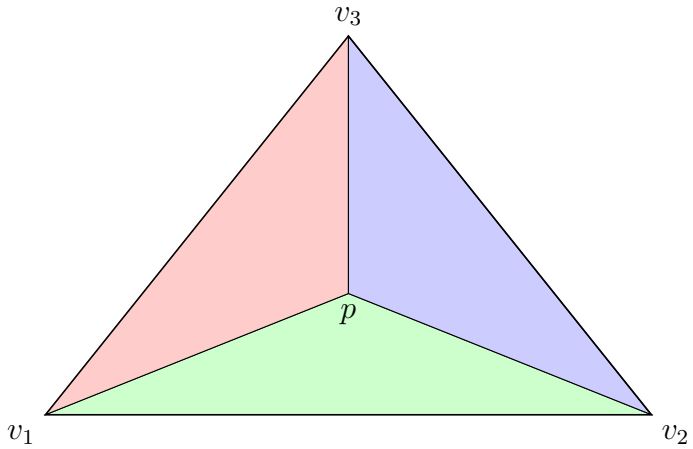
Contents

Chapter 1

Introduction

1.1 Barycentric coordinates

Let us consider a triangle with top, bottom left and bottom right vertices to which we have assigned the colors red, green and blue respectively. The triangle barycentre divides each median into two parts that have a 2:1 ratio.



Let call the red area w_1, the blue green one w_2 and the blue one w_3. Normalazing each of them by the area of the triangle, we will get three values $(\lambda_1, \lambda_2, \lambda_3)$ that are the barycentric coordinates of p with respect to the triangle $[v_1, v_2, v_3]$.

WRITE!!!!!!! introduction and all properties

1.2 Linear Interpolation

The standard linear interpolated visualisation is made passing three attributes (colors) for each vertex of a triangle. OpenGL will interpolate linearly the colors. That is possible thanks to the barycentric coordinates that will tell how much of each color is being mixed at any position.

1.3 Flat Shading

1.4 Gouraud Shading

Chapter 2

GPU program

shaders (geometry, vertex, fragment) + model view etc. arcball/trackball

Vertex shader is done on every vertex (before rasterization). Fragment shader is done on every pixel (coloring per fragment).

Chapter 3

Flat shading extension

Alternative data visualization techniques can be found using the power of barycentric coordinates and GPU programming.

The usual way to visualize data for a triangle mesh is to associate data to vertices and then interpolating over the mesh triangles, that does not work in case of edges and triangles.

3.1 Region around a vertex

We can split the surface of triangle meshes into regions around vertex (Fig. 3.2) and color them.

These regions can be determined using barycentric coordinates and GPU fragment program. Visualizing data given at the vertices or edges of the mesh in a piecewise constant simulates the classical triangle flat shading. An example of this vertex data is the discrete Gaussian curvature.

3.2 Max diagram - Vertex based area

Passing barycentric coordinates to the fragment shader will clearly demonstrate that we can get results different from the classic color interpolation.

There are different approaches to color interpolation focusing on the distance from vertices. For each point in a triangle, we can easily determine its closest vertex, which we use as a cue for coloring.

A different approach from interpolating, can be found coloring vertex areas based on the minimum barycentric coordinate. The color is given by the region farthest from a vertex (Fig. 3.1).

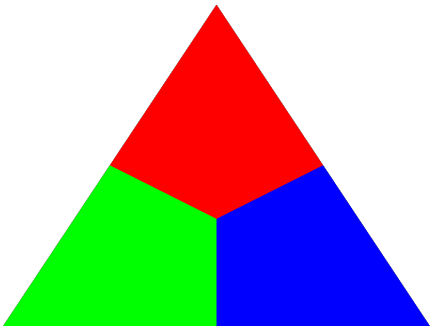


Figure 3.1: Vertex based area

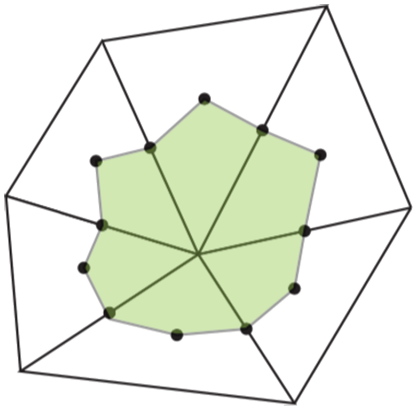


Figure 3.2: Region around a vertex

```
if (Coords.x > Coords.y && Coords.x > Coords.z) {
    vec3 blue = vec3(0.0f, 0.0f, 1.0f);
    FragColor = vec4(blue, 1.0f);
} else if(Coords.y > Coords.x && Coords.y > Coords.z) {
    vec3 green = vec3(0.0f, 1.0f, 0.0f);
    FragColor = vec4(green, 1.0f);
} else {
    vec3 red = vec3(1.0f, 0.0f, 0.0f);
    FragColor = vec4(red, 1.0f);
}
```

3.3 Implementation

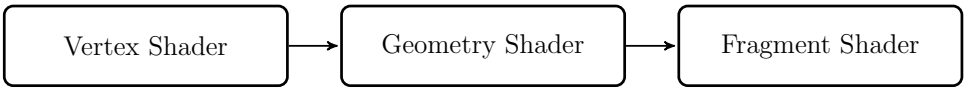
Suppose now that you want each vertex area to be in one constant color. This color can be taken from shading interpolation using the normal at the vertex and the vertex position. Then you can compute the color has it be done in *Gouraud Shading*.

The idea is to compute the color per vertex but instead of linearly interpolated it in each triangle (as *Gouraud shading* does) we color regions around a vertex with that constant color.

To implement that we need to pass the barycentric coordinates, the vertex color, the normal at the vertex and the lighting calculations to the *fragment shader*.

We want to avoid an automatic interpolation of colors, in order to return the resulting color using the *max diagram*, to do that we have used a *Geometry shader* in order to access to all three vertex colors in

fragment shader.



Appendix A

Appendix Title

A.1 Extend Flat Shading

A.2 Gaussian Curvature

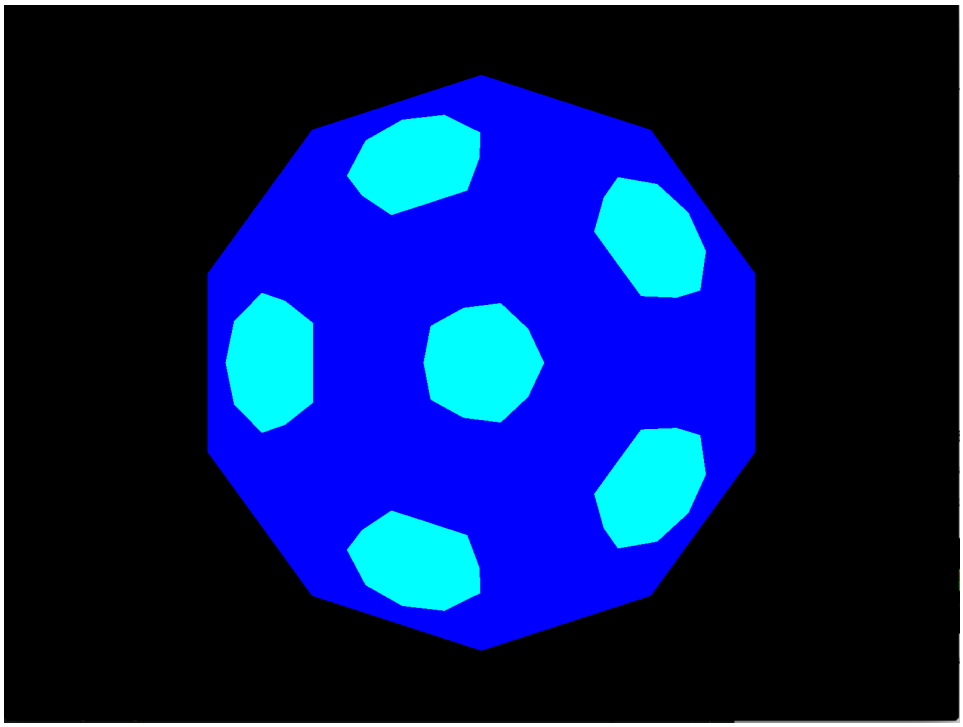


Figure A.1: Gaussian Curvature

A.3 Evaluation and comparison

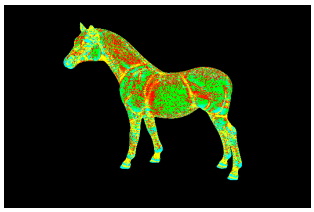


Figure A.2: Gaussian Curvature