8 Z R F V Y C X J N W 'RYDXYVT[L

0^RXYFRYDRTW 1aPFW



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Θέμα Α

Τη στιγμή όπου
$$v=rac{v_{o
ho}}{2}=6m/s$$

$$\begin{split} I' = \frac{Bvl}{R_{o\lambda}} = \frac{Bvl}{R_{\text{K}\Lambda} + R_{1,\Sigma}} = \frac{6}{4} = 1, 5A \\ \frac{dP}{dt} = \Sigma F = mg - F_L = mg - BIl = 3 - 1, 5 = 1, 5kg\frac{m}{s^2} \end{split}$$

Όταν
$$v_{o\rho}=12m/s\Rightarrow I_{o\rho}=\frac{Bv_{o\rho}l}{R_{\rm K\Lambda}+R_{1,\Sigma}}=3A$$

$$V_{\rm K\Lambda}=V_{\pi o\lambda}=I_{o\rho}R_{1,\Sigma}=3\cdot 2=6V$$

Άρα
$$V_{
m MN}=V_{
m K\Lambda}=6V=V_{\Sigma}\Rightarrow$$
 κανονική λειτουργία

$$\begin{split} \Sigma_{\tau(\Gamma)} = 0 \Rightarrow W \frac{l}{2} \sigma \upsilon \nu \varphi + N_B \frac{l}{2} \sigma \upsilon \nu \varphi &= T_1 \frac{l}{2} \eta \mu \varphi \Rightarrow \\ N_B \sigma \upsilon \nu \varphi &= T_1 \eta \mu \varphi - W \sigma \upsilon \nu \varphi \Rightarrow \\ 0, 6N_B = 10, 5 \cdot 0, 8 - 10 \cdot 0, 6 \Rightarrow 0, 6N_B = 8, 4 - 6 \Rightarrow N_B = 4N \end{split}$$

$$\begin{split} I_{o\lambda} &= I_{\rho} + I_{\sigma\varphi} = \frac{1}{12} M_{\rho} l^2 + m \left(\frac{l}{2}\right)^2 = \frac{1}{12} \cdot 3 \cdot 4 + 1 \cdot 1 = 2kg \cdot m^2 \\ & \Sigma_{\tau(\Gamma)} = I_{o\lambda} \alpha_{\gamma\omega\nu} \Rightarrow mg \frac{l}{2} \sigma v \nu \varphi = I_{o\lambda} \cdot \alpha_{\gamma\omega\nu} \Rightarrow \\ & 10 \cdot 0, 6 = 2\alpha_{\gamma\omega\nu} \Rightarrow \alpha_{\gamma\omega\nu} = 3rad/s^2 \\ & \frac{dL_{\rho}}{dt} = I_{\rho} \cdot \alpha_{\gamma\omega\nu} = 3kg \cdot m^2/s^2 \end{split}$$



Θέμα Α

Γωνιακή ταχύτητα ω ωριακά πριν φτάσει στο οριζόντιο δάπεδο

$$\begin{split} E_{o\lambda(\alpha\rho\chi)} &= E_{o\lambda(\tau\varepsilon\lambda)} \Rightarrow \\ mgl\eta\mu\varphi + M_{\rho}g\frac{l}{2}\eta\mu\varphi &= 0 + M_{\rho}g\frac{l}{2}\eta\mu\varphi + \frac{1}{2}I_{o\lambda}\omega^2 \Rightarrow \\ 10 \cdot 2 \cdot 0, 8 &= \frac{1}{2}2\omega^2 \Rightarrow \omega = 4rad/s \\ |\overrightarrow{L}_{\pi\rho\iota\nu}| &= I_{o\lambda}|\overrightarrow{\omega}| = 2 \cdot 4 = 8kg \cdot m^2/s \\ |\overrightarrow{L}_{\mu\varepsilon\tau}| &= I_{o\lambda}|\overrightarrow{\omega}'| = 2 \cdot 2 = 4kg \cdot m^2/s \\ \Delta \overrightarrow{L} &= \overrightarrow{L}_{u\varepsilon\tau} - \overrightarrow{L}_{\pi\rho\iota\nu} \Rightarrow \Delta L = 4 - (-8) = 12kg \cdot m^2/s \end{split}$$



Θέμα Γ

Κύλιση χωρίς ολίσθηση

$$v_E = 0 \Rightarrow v_{cm} = \omega R \Rightarrow a_{cm} = a_{\gamma\omega\nu}$$

Μεταφορική

$$\Sigma F = F + T_{\sigma\sigma} = M_T \cdot a_{\sigma\sigma}$$

Περιστροφική

$$\begin{split} \Sigma_{\tau(\mathcal{O})} &= I_{\tau\rho} \cdot a_{\gamma\omega\nu} \Rightarrow F \cdot r - T_{\sigma\tau}R = \frac{1}{2}M_TR^2 \cdot a_{\gamma\omega\nu} \Rightarrow \\ &F \frac{r}{R} - T_{\sigma\tau} = \frac{1}{2}M_T \cdot a_{cm} \\ &F \left(1 + \frac{V}{R}\right) = \frac{3}{2}M_T \cdot a_{\gamma\omega\nu} \Rightarrow \end{split}$$

$$F\left(1+\frac{3}{4}\right) = \frac{3}{2}M_T \cdot a_{\gamma(x)\nu} \Rightarrow a_{\gamma(x)\nu} = \frac{7F}{23f} = 2m/s^2$$

Θέμα Α

$$\Delta x_{cm}=\frac{1}{2}a_{cm}t_1^2=\frac{1}{2}\cdot 2\cdot 4=4m$$
 Μετατόπιση άκρου νήματος:

$$\Delta x_z = \Delta x_{cm} + r \cdot \Delta \varphi = \Delta x_{cm} + r \frac{\Delta x_{cm}}{R} = \Delta x_{cm} \left(1 + \frac{r}{R} \right) = \frac{7}{4} \Delta x_{cm}$$

$$W_F = F \cdot \Delta x_z \cdot \sigma v \nu 0^\circ = 12 \cdot 7 = 84J$$