

According to Heron the area of a triangle with sides a, b, c is

$$E = \sqrt{s(s-a)(s-b)(s-c)}$$

For circles $C_0 - C_1 - C_8$ the area of the triangle $K_0K_1K_8$ is according to Heron

$$\begin{aligned} s &= \frac{1}{2} (r_0 + r_1 + r_1 + r_8 + r_8 + r_0) \\ s &= r_0 + r_1 + r_8 \\ E &= \sqrt{r_0 r_1 r_8 (r_0 + r_1 + r_8)} \end{aligned}$$

with $r_k = d^k \cdot r_0$ and $r_0=1$

$$\begin{aligned} E &= \sqrt{d^9(1+d+d^8)} \\ E &= d^4 \sqrt{d+d^2+d^9} \end{aligned}$$

The sector of C_0 has area

$$\begin{aligned} A &= \frac{1}{2} r_0^2 \theta_0 \\ A &= \frac{1}{2} \theta_0 \end{aligned}$$

From the cosine rule we have

$$\begin{aligned} \cos \theta_0 &= \frac{(r_0 + r_1)^2 + (r_0 + r_8)^2 - (r_1 + r_8)^2}{2(r_0 + r_1)(r_0 + r_8)} \\ \cos \theta_0 &= \frac{(1+d)^2 + (1+d^8)^2 - (d+d^8)^2}{2(1+d)(1+d^8)} \\ \cos \theta_0 &= \frac{1+2d+d^2+1+2d^8+d^{16}-d^2-2d^9-d^{16}}{2(1+d)(1+d^8)} \\ \cos \theta_0 &= \frac{2+2d+2d^8-2d^9}{2(1+d)(1+d^8)} \\ \cos \theta_0 &= \frac{1+d+d^8-d^9}{(1+d)(1+d^8)} \end{aligned}$$