

From the list  $x + y = m^2$ ,  $x - y = k^2$ ,  $x + z = l^2$ ,  $x - z$ ,  $y + z$  and  $y - z$  we have  $m > l > k$  because

$$x + y > x + z \implies m > l$$

and

$$x + z > x - y \implies l > k$$

Solving for  $x$ ,  $y$  and  $z$  we have

$$x = \frac{k^2 + m^2}{2}, y = \frac{-k^2 + m^2}{2}, z = \frac{-k^2 + 2l^2 - m^2}{2}$$

so

$$x - z = k^2 - l^2 + m^2, y + z = -k^2 + l^2, y - z = -l^2 + m^2$$

This means we iterate for all  $l > k$  and  $l < m < \sqrt{2l^2 - k^2}$ .

To speed things up, we cache a matrix of squares.