| distribution | example | parameters | | | probability density mass function for x | mean | standard deviation | supported x | generate 10 numbers in R estimate the likelihood of x in R |
|---------------|-------------------------------------|--|---|---------------------------|---|---|--|------------------------------|---|
| normal | | $\mu = \text{mean} *$ | | | $\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{1}{2}\left(\frac{\mathbf{x}-\mu}{\sigma}\right)^2}$ | μ | σ | continuum $(-\infty,\infty)$ | $rnorm(n=10,mean=\mu,sd=\sigma)$ |
| -5 0 5 10 15 | SAT score | $\sigma = SD$ | | | | | | | $dnorm(x, mean=\mu, sd=\sigma)$ |
| log-normal | | $m = \text{logarithm of median } *$ $= \ln \left(\frac{\mu^2}{\sqrt{\mu^2 + \sigma^2}} \right)$ | | | | | | | rlnorm(n=10,meanlog=m,sdlog=s) |
| -5 0 5 10 15 | plant height | $s = \text{spread} = \sqrt{\ln\left(\frac{e^{2m} + 1}{e^{2m} + 1}\right)}$ | $ \sqrt{\ln\left(1 + \frac{\sigma^2}{\mu^2}\right)} $ $ \frac{\sqrt{e^{4m} + 4e^{2m}\sigma^2}}{2e^{2m}} $ | | $\frac{1}{x s \sqrt{2\pi}} e^{-\frac{1}{2} \left(\frac{\ln(x) - m}{s}\right)^2}$ | $e^{\left(m+\frac{S^2}{2}\right)}$ | $\sqrt{\left(e^{s^2}-1\right)e^{2m+s^2}}$ | continuum $(0, \infty)$ | dlnorm(x,meanlog=m,sdlog=s) |
| exponential | time | $\lambda = \text{rate}$ | | | λe ^{-λx} | $\frac{1}{\lambda}$ | $\frac{1}{\lambda}$ | continuum $[0,\infty)$ | $rexp(n=10, rate=\lambda)$ |
| -5 0 5 10 15 | between two earthquakes | | | | | | | | $dexp(x, rate=\lambda)$ |
| gamma | time it takes | $\mathbb{E} = \text{shape (how many events)}$ $\lambda = \text{rate or } \vartheta = \text{scale} = \frac{1}{\lambda}$ | | | $rac{\lambda^{\mathbb{E}}}{\Gamma(\mathbb{E})} x^{\mathbb{E}-1} e^{-\lambda x}$ | $\mathbb{E} \frac{1}{\lambda}$ | $\sqrt{\mathbb{E}} \frac{1}{\lambda}$ | continuum $[0,\infty)$ | rgamma(n=10,shape= \mathbb{E} ,rate= λ) |
| -5 0 5 10 15 | to finish PhD | | | | | | | | $dgamma(x, shape=E, rate=\lambda)$ |
| beta | proportion of skin | $\mu = \text{mean}$ | $\alpha = \mu\theta$ | | $\Gamma(\alpha + \beta)$ $\alpha = 1$ | μor | $\sqrt{\frac{\mu-\mu^2}{\theta+1}}$ or | continuum | rbeta(n=10, shape1= $\mu * \theta$, shape2=(1- μ)* θ) |
| -5 0 5 10 15 | covered by clothing | $\theta = \text{shape}$ (concentration) | or | $\beta = (1 - \mu)\theta$ | $\frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}$ | $\frac{\alpha}{\alpha+\beta}$ | $ \frac{\sqrt{\frac{\mu - \mu^2}{\theta + 1}}}{\sqrt{\alpha \beta}} \text{ or } $ $ \frac{\sqrt{\alpha \beta}}{(\alpha + \beta)\sqrt{\alpha + \beta + 1}} $ | [0,1] | dbeta(x , shape1= $\mu * \theta$, shape2=(1- μ)* θ) |
| Poisson | customers | 1 | | | $\lambda^{x}e^{-\lambda}$ | 1 | /3 | counts | rpois(n=10, lambda= λ) |
| -5 0 5 10 15 | per day (same shop) | $\lambda = \text{rate}$ | | | $\frac{\lambda^{x}e^{-\lambda}}{x!}$ | λ | $\sqrt{\lambda}$ | {0,1,} | dpois(x , lambda= λ) |
| gamma-Poisson | customers per day | $\mu = \text{mean}$ $\theta = \text{shape (concentration)}$ | | | $\frac{\Gamma(x+\theta)}{x!\Gamma(\theta)} \left(\frac{\theta}{\theta+\mu}\right)^{\theta} \left(\frac{\mu}{\theta+\mu}\right)^{x}$ | μ | $\sqrt{\mu + \frac{\mu^2}{\theta}}$ | counts {0,1,} | rpois(n=10,lambda= rgamma(n=10,shape= θ ,rate= θ/μ)) |
| -5 0 5 10 15 | (different shops) | | | | | | | | $dnbinom(x, size = \theta, prob = \theta/(\mu + \theta))$ |
| binomial | number of dates out of | p = probability of + 1 | | | $\binom{n}{x}p^x(1-p)^{n-x}$ | np | $\sqrt{np-np^2}$ | counts $\{0,\ldots,n\}$ | rbinom(n=10,size=n,prob=p) |
| -5 0 5 10 15 | n invitations for coffee | n = total attempts | | | | | | | dbinom(x, size=n, prob=p) |
| beta-binomial | number of dates out of | $\mu = \text{mean of beta} \qquad \alpha = \mu\theta$ | | | | | [(a) (a) | | rbinom(n=10, size= n , prob=rbeta(n=10, shape1= $\mu^*\theta$, shape2=(1- μ)* θ)) |
| -5 0 5 10 15 | n invitations for coffee (different | $\theta = \text{shape}$ (concentration) | | $\beta = (1 - \mu)\theta$ | $\binom{n}{x} \frac{\Gamma(x+\alpha)\Gamma(n-x+\beta)\Gamma(\alpha+\beta)}{\Gamma(n+\alpha+\beta)\Gamma(\alpha)\Gamma(\beta)}$ | $n\mu \text{ or } \frac{n\alpha}{\alpha+\beta}$ | $\sqrt{\frac{n(\theta+n)(\mu-\mu^2)}{\theta+1}} \text{ or } $ $\sqrt{\frac{n\alpha\beta(\alpha+\beta+n)}{(\alpha+\beta)\sqrt{\alpha+\beta+1}}} $ | counts $\{0,\ldots,n\}$ | <pre>dbetabinom<-function(x,mup,shape,size){ a<-mup*shape; b<-(1-mup)*shape choose(size,x)* (gamma(x+a)*gamma(size-x+b)*gamma(a+b))/ (gamma(size+a+b)*gamma(a)*gamma(b))}</pre> |
| | people) | n = total attempts ooth positive and negative values, other part | | | ramators are always positive for the a | (nlanatica | of the gamma function | on F and intuiti | dbetabinom(x , mup= μ , shape= θ , size= n) |

^{*}parameters with asterisk can assume both positive and negative values, other parameters are always positive, for the explanation of the gamma function Γ and intuition about α , β parameters of beta, flip the paper

