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# 1 Model for electrical conductivity of muscle meat during 2 Ohmic heating

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## 6 **Abstract**

A model is presented for predicting the electrical conductivity of muscle meat, which can be used for the evaluation of Ohmic heating. The model computes the conductivity as a function of composition, temperature and microstructure. The muscle meat is thought to be composed of protein, water, salt. Concerning the microstructure, the model takes into account the muscle fiber orientation with respect to the electric field, and the development of drip channels due to protein denaturation. The model includes a description of the protein denaturation kinetics. The model has been validated for different types of meat, varying in composition and heating rate. The submodel for protein denaturation is validated using independent DSC measurements. For meats heated faster than 20 degrees per minute, the conductivity is a linear function of temperature - due to the absence of protein denaturation, and thus drip channel formation. If meat is heated slower than 10 degrees per minute the conductivity is showing non-linear behaviour, with a significant decrease at temperatures above 70 degrees Celsius. This decrease is explained by the action of the complete protein denaturation. Our study

shows that if Ohmic heating of meat is performed at fast rates, there is a large potential to retain most of its moisture during heating.

7 *Keywords:* Electrical conductivity, protein denaturation, Ohmic heating

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## 8 **1. Introduction**

9 Ohmic heating of meat is a promising technique compared to conventional  
10 cooking as it is considerably fast (Yildiz-Turp et al., 2013). Consequently,  
11 it is better in retaining water within the meat (Lyng et al., 2013). This is  
12 believed to be due to the fact that heating times are significantly shorter than  
13 that of protein denaturation. However, the Ohmic heating method can be  
14 impaired by uneven heating, which makes it difficult to determine the point  
15 with lowest temperature and thus the microbial safety (Marra, 2014; Jaeger  
16 et al., 2016). This holds particularly for composite foods having components  
17 with starkly varying electrical conductivity. Prediction of these phenomena  
18 can be improved by numerical modelling (McKenna et al., 2006; Varghese  
19 et al., 2014; Marra, 2014).

20 The greatest hurdle for predictive numerical modelling of Ohmic heating  
21 is the lack of knowledge on the electrical conductivity of food (Varghese  
22 et al., 2014; Kaur and Singh, 2016). Meat is particularly challenging, as  
23 the composition and structure change during heating (Oroszvári et al., 2006;  
24 Pearce et al., 2011; Bouhrara et al., 2011; Kondjoyan et al., 2013). The change  
25 in microstructure and composition is due to meat proteins denaturation.  
26 These changes influence the conductivity to a large extent (Bircan et al.,  
27 2001; Bircan and Barringer, 2002; Brunton et al., 2006; Damez and Clerjon,

28 2013). Furthermore, it is shown that there is a significant dependence of the  
29 conductivity on the muscle fiber direction (Zell et al., 2009).

30 In order to resolve this research question, we have constructed a predictive  
31 model for the electrical conductivity of meat, as function of composition, tem-  
32 perature and the degree of protein denaturation. Muscle meat will be viewed  
33 as a (structured) mixture of water, salt, and proteins. Regarding electrical  
34 conductivity, we will assume proteins as insulators. For salt solutions we  
35 will determine how their electrical conductivity depends on temperature and  
36 concentration, via fitting an analytical function to literature data. The con-  
37 ductivity of salt is mainly determined by its diffusion coefficient, or rather  
38 its mobility. The mobility of salt is hindered by the presence of the dense  
39 protein matrix in meat. This effect will be introduced via a hindrance fac-  
40 tor. The effect of the microstructure of meat, the aligned protein fibers in  
41 the intracellular phase and the drip channels in the extracellular phase will  
42 be taken into account. The formation of drip channels is driven by protein  
43 denaturation. We account for the evolution of microstructure via modelling  
44 of the protein denaturation kinetics, and linking the state of the denatured  
45 proteins to particular microstructure. The protein denaturation submodel  
46 will be validated using independent literature data. Via combining various  
47 submodels, we compare numerical predictions with literature data on the  
48 electrical conductivity of muscle meat and meat batters, as function of tem-  
49 perature and heating rate.

## 2. Theory

### 2.1. Assumptions

We will regard meat as a hierarchical composite material. A composite material has a distinct dispersed phase, embedded in a continuous phase. Often the dispersed and the continuous phase differ significantly in material properties, such as electrical conductivity. During cooking meat has a composite character at two different length scales. At the larger length scale, we distinguish the extracellular and intracellular phase. The extracellular phase is filled with serum, a mixture of water, salt and soluble proteins, which has been expelled from the intracellular phase during cooking. The intracellular phase contains the muscle fibers, which are viewed as a composite material of protein fibers and serum. The electrical conductivity of the intracellular phase is considerable lower than that of the extracellular phase, due to the high volume fraction of proteins in the intracellular phase, and the steric hindrance they impose on the ion mobility.

The intracellular phase is bounded by collagenous connective tissue, the so-called epimysium. Together they form the muscle fibers, which are organized in fiber bundles. A muscle contains several fiber bundles. Both the whole muscle and fiber bundles are bounded by connective tissue, which are called epimysium and perimysium respectively. Connective tissue is predominantly made up of collagen. A schematic representation of the hierarchical structure of cooking meat is shown in figure 1.

If the proteins in the intracellular phase denature, part of the intracellu-

lar liquid will be expelled to the extracellular phase. If the collagen of the perimysium and epimysium denatures, the liquid in the extracellular phase will be expelled to the environment. We will assume that both liquid transport processes is instantaneous. Or, in other words the time scale of liquid transport is faster than that of protein denaturation. This assumption holds of course only for thin slices of meat. Moreover, for thicker slices of meat there might even be a significant temperature gradient.

Similar to meat, our model for electrical conductivity will have a hierarchical structure. At the lowest length scale, we have a model for the serum phase. At the next level, we have a model describing the conductivity of the intracellular phase. At the highest level, we describe the conductivity of the complete meat, being a composite with an intracellular and extracellular phase, with the latter having the conductivity of serum.

The model for the serum will build upon the conductivity model for salt solutions. Later, this model will be modified for the presence of soluble proteins. For dilute salt solutions there are fundamental physical models like Debye-Hueckel. The conductivity is linked to the ion charge density and its diffusivity (or rather its inverse the mobility), for which the Stokes-Einstein relation is often used. But, this theory breaks down at higher salt concentrations as found in meat products. Hence, we have to resort to empirical relations (Anderko and Lencka, 1997). Because of the relation between conductivity and ionic mobility, one can state that the temperature dependency is independent of the concentration. Hence, the following decomposition holds:  $\sigma_s = \sigma_{s,c}(c)\sigma_{s,T}(T)$ , with  $c$  the concentration and  $T$  temperature (Anderko

97 and Lencka, 1997).

98 Similarly, the contributions of soluble proteins depend on their charge  
 99 and mobility. Proteins are polyelectrolytes, and they can carry charges via  
 100 (dis)association with protons. However, in meat products the  $\text{pH} \approx 5.8$ , which  
 101 is near the isoelectric point  $\text{pI} \approx 5.3$  (Hamoen et al., 2013). Hence, the charge  
 102 density of the soluble proteins will be negligible compared to that of salts  
 103 present in meat. Moreover, due to their size their mobility is also small  
 104 compared to that of salts. Hence, one can neglect their direct ionic contribu-  
 105 tion compared to salts, similar to milk (Bazinet et al., 2005). Consequently,  
 106 the soluble proteins can be viewed effectively as insulators. However, they  
 107 do have an indirect contribution to the conductivity via two effects: 1) the  
 108 soluble proteins increase the viscosity of the fluid (Shibata-Ishiwatari et al.,  
 109 2015), and decrease the mobility of salt ions, and 2) as insulators they occupy  
 110 a fraction of volume, and influence the overall conductivity of serum similar  
 111 to composites. Similar arguments hold for the proteins in the muscle fibers,  
 112 which are quite immobilized too.

113 The electrical conductivity of composites is described by effective medium  
 114 theory, as pioneered by Maxwell (Choy, 2015). The effective medium theory  
 115 can equally be applied to other material properties like thermal conduc-  
 116 tivity and diffusivity, as these transport phenomena are governed by similar  
 117 mathematical equations. Maxwells theory only holds for spherical inclusions,  
 118 but the theory has been extended to arbitrary shape by Torquato and Sen  
 119 (1990). This theory we have applied successfully to the thermal conductivity  
 120 of (frozen) meat (van der Sman, 2008). There, we have assumed that meat

121 protein fibers in muscle meat products can be represented as straight cylin-  
 122 ders. For the (electrical) conductivity it is important to know the orientation  
 123 of the meat fibers with respect to the gradients of the field (temperature or  
 124 electric potential). In minced meat products or meat emulsions the pro-  
 125 teins fibers are randomly oriented, and Maxwells effective medium theory for  
 126 spherical inclusions can be used.

127 Effective medium theory does not account for the steric effects of the  
 128 meat structure on the mobility of ions. This effect has been accounted for  
 129 in theories for the electrical conductivity of poly-electrolyte gels (Gu et al.,  
 130 2004). The ion diffusivity depends on the porosity and structure of the gel  
 131 (Amsden, 1998; Gu et al., 2004; Rossi et al., 2016). Various theories exist,  
 132 but there is no universally accepted theory for that (Amsden, 1998). The  
 133 structural dependence is assumed to be dependent on the ratio between mesh  
 134 size of the gel and the ions radius  $r_i$ . We will capture this steric hindrance  
 135 effect by an empirical prefactor in the equations of effective medium theory.

136 It is assumed that not all soluble proteins from the intracellular phase  
 137 will migrate to the extracellular phase. It can happen that they have dena-  
 138 tured and aggregated, before the contraction of the connective tissue. Conse-  
 139 quently, these aggregates will be immobilized, or they will not be able to pass  
 140 through the mesh of the connective tissue (endomysium). Hence, we assume  
 141 that all proteins in the intracellular phase are practically immobilized, and  
 142 they are all absorbed in the dispersed phase. The continuous phase of the  
 143 intracellular phase is the salt solution only.

144 The model for the conductivity of the intracellular phase will be tested for



145 fast heated meats, where the heating rate is faster than the rate of protein de-  
 146 naturation. Under this condition, we assume that the microstructure of meat  
 147 does not change, and remains comparable to the structure of post-mortem  
 148 meat. Post-mortem there is a slight extracellular phase with a volume frac-  
 149 tion of about 5% (Offer and Cousins, 1992; Oroszvári et al., 2006), but we will  
 150 neglect this contribution for fast heated meats. Under this assumption the  
 151 conductivity of fast heated meat is representative for that of the intracellular  
 152 phase.

153 For the conductivity of the whole meat, we will assume that meat consists  
 154 of an array of cylindrical unit cells, with each unit cell having an extracellular  
 155 and intracellular phase. The intracellular space is regarded as homogenized  
 156 phase, that has a conductivity modelled with the above described effective  
 157 medium theory. At the level of the whole meat we reuse the same effec-  
 158 tive medium theory, with the intracellular phase as the cylindrical dispersed  
 159 phase, and the extracellular phase as the continuous phase, with the same  
 160 conductivity as the exuded serum.

161 During cooking the volumes of the intracellular and extracellular phases  
 162 will change due to protein denaturation. We will model explicitly the protein  
 163 denaturation using the Lumrey-Eyring two-state model, building upon the  
 164 earlier work of Ishiwatari et al. (2013). That model only considers myosin  
 165 and actin. However, the model is still useful for our purposes because the  
 166 denaturation behaviour of collagen of the epimysium and perimysium and  
 167 actin more or less overlap, i.e. perimysium shrinks at 64°C (Tornberg, 2005),  
 168 which is the melting temperature  $T_m$  of actin (Ishiwatari et al., 2013). Fur-

thermore, only denaturation of actin and/or myosin leads to expulsion of liquid from the intracellular phase to the extracellular phase. If the connective tissue of the epimysium and perimysium denatures, the serum from the extracellular phase will be expelled out of the meat, and the total volume of intracellular and extracellular phase will decrease.

It is noted that in fish products dielectric loss factor is mainly determined by the ionic conductivity up to moderate radio frequencies (27 MHz) (Wang et al., 2008). It is reasonable to assume this also holds for meat products. Hence, for validation of our model we can also use data from Ohmic heating of meat up to such frequencies.

## 2.2. Electrical conductivity models

Using data obtained from standard works and literature (Zell et al., 2009), one can show that at constant temperature and in the range of  $c < 5\%$  the conductivity can be approximated by a linear function. Hence, we will use the following bilinear function:

$$\sigma_s = \sigma_0 c (1 + \nu T) \quad (1)$$

with  $\sigma_s$  the conductivity of salt,  $c$  the salt concentration, and  $T$  is the temperature. The other symbols are just parameters, which will be fitted.

The Torquato model applied to the intracellular phase reads:

$$\frac{\sigma_{fib}}{\sigma_s} = f \frac{1 + \delta(1 - \phi_w + Q\phi_w)}{1 + \delta Q\phi_w} \quad (2)$$

$\sigma_{fib}$  is the total conductivity of the fibrous intracellular phase,  $\sigma_s$  is the conductivity of the salt solution, which follows Eq.(1).  $\phi_w = 1 - \phi_p$  is the

189 volume fraction of water in the intracellular phase.  $\delta$  is the relative difference  
 190 between the conductivity of protein fibers and salt solution. As we assume  
 191 the protein to be insulating, it follows that  $\delta = -1$  (Torquato and Sen, 1990).  
 192  $Q$  is a shape factor, which is  $Q = \frac{1}{3}$  for spherical inclusions,  $Q = 0$  for parallel  
 193 to fibers, and  $Q = \frac{1}{2}$  perpendicular to fibers (Torquato and Sen, 1990).  $f$  is  
 194 the hindrance factor, accounting for the reduction of ion mobility due to the  
 195 muscle protein structure (i.e. gel).

196 We describe the conductivity of the serum in the extracellular phase,  $\sigma_{s,ex}$ .  
 197 The serum is a salt solution with soluble sarcoplasmic proteins at a volume  
 198 fraction of  $\phi_{ssp} = 0.08$  (Shibata-Ishiwatari et al., 2015). The enhancement  
 199 of the viscosity by the soluble proteins is described by the Einstein relation  
 200  $\eta_{ex} = \eta_w(1 + 2.5\phi_{ssp})$ , with  $\eta_{ex}$  the viscosity of the serum,  $\eta_w$  is the viscosity  
 201 of the salt solution. The increase of viscosity will lead to reduction of the  
 202 mobility of the salt ions, which is inversely proportional to the viscosity.  
 203 The soluble proteins act as insulating spheres, which can be captured by the  
 204 Torquato model, using  $Q_{ex} = \frac{1}{3}$ . Hence, the conductivity of the serum can  
 205 be estimated as:

$$\sigma_{s,ex} = \frac{\sigma_s}{1 + 2.5\phi_{ssp}} \frac{1 - \phi_{ssp} - (1 - \phi_{ssp})Q_{ex}}{1 - Q_{ex}(1 - \phi_{ssp})} \quad (3)$$

206 Subsequently, we apply the Torquato model at the level of the total mus-  
 207 cle. The extracellular phase is the continuous phase, and the fibrous intra-  
 208 cellular phase is the dispersed phase - whose conductivity is described with  
 209 Eq.(2). For the conductivity of the total meat  $\sigma_{meat}$  holds:

$$\frac{\sigma_{meat}}{\sigma_{s,ex}} = \frac{1 + \delta_{ex}(1 - \phi_{ex} + Q\phi_{ex})}{1 + \delta_{ex}Q\phi_{ex}} \quad (4)$$

210 with  $\delta_{ex} = (\sigma_{fib} - \sigma_{s,ex})/\sigma_{s,ex}$ , the relative difference in conductivity between  
 211 the fibrous intracellular phase, and the serum in the extracellular phase.  $Q$  is  
 212 the same shape factor as for the intracellular phase.  $\phi_{ex}$  is the volume fraction  
 213 of the extracellular phase with respect to the whole meat. In a following  
 214 section, we will compute  $\phi_{ex}$  and  $\phi_w$  as a function of the degree of protein  
 215 denaturation. But, first the protein denaturation models are discussed.

### 216 2.3. Protein denaturation

217 The model for the denaturation of muscle proteins builds upon the work  
 218 of Ishiwatari et al. (2013). These authors have considered the denaturation  
 219 of both myosin and actin only. They have assumed that protein denaturation  
 220 is irreversible. However, this assumption is not consistent with the notion  
 221 of water holding of meat. In the recent theories developed for water holding  
 222 capacity (WHC) we have assumed that it is an equilibrium property (van der  
 223 Sman, 2012). This means that meat can hold a certain defined amount of  
 224 water, if it is held at a certain temperature for a long period of time. We have  
 225 treated WHC within the framework of thermodynamics, which presumes that  
 226 the protein denaturation is (partly) reversible (van der Sman, 2012). Hence,  
 227 we will extend the Ishiwatari model with reversibility. Only reversibility of  
 228 the protein denaturation can explain the thermodynamic property of the  
 229 water holding capacity of meat. After a very long period (days) of heating  
 230 at constant temperature, the WHC is still a strong function of temperature  
 231 (Zielbauer et al., 2016). This implies that at temperatures below 80°C protein  
 232 denaturation is only partial, and that it has reached thermodynamic equi-

librium. The partial denaturation follows indeed from DSC measurements (Zielbauer et al., 2016).

The kinetic model of protein denaturation can be made consistent with the framework of thermodynamics, if the denaturation reactions are assumed reversible, similar to the Lumry-Eyring models of protein denaturation (Lumry and Eyring, 1954). Protein denaturation is often compared to melting behaviour of (semi)-crystalline biopolymers, having a defined melting temperature  $T_m$  and melting enthalpy  $\Delta H_m$ . The melting transition takes places over a broad temperature range. We will assume that the reaction constant of the protein denaturation will follow similar temperature dependency as melting crystals.

Below, we will give a general description of protein denaturation, which is assumed to hold also for the meat proteins, myosin and actin. The protein is assumed to have two states:  $N$  the native state, and  $D$  the denatured state. The corresponding mass balance is as follows:

$$\begin{aligned} dN/dt &= -k_D N + k_N D \\ dD/dt &= +k_D N - k_N D \end{aligned} \quad (5)$$

In equilibrium holds that  $dN/dt = dD/dt = 0$ . The initial amount of native protein is  $N(0) = N_0 = N + D$  and  $D(0) = 0$ . The fraction denaturated proteins is denoted as  $D/N_0 = x$ . The equilibrium condition is:

$$dx/dt = -k_D(1 - x) + k_N x = 0 \quad (6)$$

251 And hence, the equilibrium value of the fraction of denatured proteins is:

$$x_{eq} = \frac{k_D}{k_N + k_D} = \frac{1}{K + 1} \quad (7)$$

252  $K = k_N/k_D$  is the reaction constant, which follows the temperature depen-  
253 dency of melting crystals:

$$K = K_0 \exp(-\Delta G/RT) \quad (8)$$

254 The change in free energy  $\Delta G$  is due to melting of crystalline parts:

$$\Delta G = \Delta H_m(1 - T/T_m) \quad (9)$$

255  $k_N$  is often modelled following the Eyring transition state theory, where  
256 it is assumed that an energy barrier with height  $\Delta E$  must be overcome:

$$k_N = k_{N,0} \exp(-\Delta E/RT) \quad (10)$$

257 Hence, the denaturation kinetics follows:

$$k_D = k_{N,0} \exp(-\Delta E/RT) \exp(-\Delta G/RT) \quad (11)$$

258 The above model will be applied to actin and myosin, whose denaturation  
259 will be described by the fractions  $x_{act}$  and  $x_{myo}$ . Below, we describe how the  
260 volume fractions  $\phi_w$  and  $\phi_{ex}$  can be related to these numbers.

#### 261 2.4. Evolution of microstructure as function of protein denaturation

262 The consequences of muscle protein denaturation is indicated schemat-  
263 ically in figure 2. There we have represented the meat with a cylindrical

unit cell, having an extracellular and intracellular phase. The figure shows the sequence of the principal steps in the evolution of the intracellular and extracellular volumes. At low temperatures, the cell volume  $V_{cell}$  equals the initial volume  $V_0$ . There is no extracellular phase, meaning the total volume equals the cell volume ( $V_{tot} = V_{cell}$ ). Above 40°C myosin starts to denature, and the cell volume (the intracellular phase) shrinks linear with the fraction of denatured myosin,  $x_{myo}$ . The shrinking cells expels liquid to the extracellular phase. The total volume still remains equal to the initial volume  $V_{tot} = V_0$ . At temperatures above 60°C actin and collagen of the perimysium and epimysium will denature. The denaturation of actin will have similar effect as the denaturation of myosin: the intracellular phase shrinks linear with the fraction of denatured protein,  $x_{myo} + x_{act}$ , and the excess liquid is expelled to the extracellular phase. Due to the denaturation of collagen in the connective tissues the total volume will shrink:  $V_{tot} < V_0$ . The total volume is thought to be linear with the fraction of denatured actin,  $x_{act}$ , which is assumed to coincide with the denaturation of collagen in the perimysium and epimysium. At the end of the protein denaturation,  $T > 90^\circ C$ , all liquid from the extracellular phase is expelled and the cell volume equals the total volume again,  $V_{tot} = V_{cell} = V_e$ . The final cell volume  $V_e$  follows from the known water holding capacity of fully cooked meat.

From the above assumptions follows the following linear relations between volumes and fractions of denatured proteins:

$$\frac{V_0 - V_{cell}}{V_0 - V_e} = \frac{1}{2}(x_{myo} + x_{act})$$

$$\frac{V_0 - V_{tot}}{V_0 - V_e} = x_{act} \quad (12)$$

From the above equations we derive relations for the volume fraction of proteins in the intracellular phase,  $\phi_p = 1 - \phi_w$ , and the volume fraction of the extracellular phase  $\phi_{ex}$  (relative to the whole meat).

In our earlier paper we have shown that there is quite some universal behaviour regarding water holding capacity (WHC) of meat from different animal sources (van der Sman, 2012). Hence, we will take the values for WHC from there, which are expressed in terms of mass fraction of water  $y_w$ , or equivalently the mass fraction of proteins  $y_p = 1 - y_w$ . The WHC of raw meat is denoted as  $y_{p,0}$ , and the WHC of fully denatured meat is  $y_{p,e}$ . Using the mass densities of proteins and water,  $\rho_w$  and  $\rho_p$ , the initial and final protein volume fraction can be computed:

$$\begin{aligned} \phi_{p,0} &= \frac{y_{p,0}}{(y_{w,0}\rho_p/\rho_w + y_{p,0})} \\ \phi_{p,e} &= \frac{y_{p,e}}{(y_{w,e}\rho_p/\rho_w + y_{p,e})} \end{aligned} \quad (13)$$

Consequently, the instantaneous protein volume fraction in the intracellular phase is given by:

$$\frac{\phi_p}{\phi_{p,0}} = \frac{V_{cell}}{V_0} \quad (14)$$

This value will be substituted in Eq.(2), with use of  $\phi_w = 1 - \phi_p$ .

The volume fraction of the extracellular phase, relative to the total volume is given by:

$$\phi_{ex} = \frac{V_{tot} - V_{cell}}{V_{tot}} \quad (15)$$

This value will be substituted in Eq.(4).



## 303 2.5. Use of the model

304 In the following we describe the use the complete model for the description  
 305 of the electrical conductivity of slowly heated meat. Furthermore, several  
 306 submodels can be validated using literature data for special cases. A visual  
 307 representation of the various uses of the model is given in figure 3, which can  
 308 be used as a guide in the following discussion.

309 The basis of the model is the conductivity of a salt solution, Eq.(1). This  
 310 equation will be tested for salt concentration up to 5%. We will use this  
 311 equation for the conductivity of the continuous phase of the intracellular  
 312 phase, which is modelled using the Torquato model for composites, Eq.(2).  
 313 This model is also assumed to hold for fast heated meat, whose data is used  
 314 for validation. Using the shape factor we can acknowledge the orientation  
 315 of the cylindrical fibers with respect to the electric field. The same model  
 316 with  $Q = \frac{1}{3}$  can be used for minced meat, or meat emulsions, where the  
 317 proteins are randomly oriented. These meat products can contain also some  
 318 fat, which can also be viewed as an insulating dispersed phase similar to the  
 319 proteins.

320 The protein denaturation is described by the two-state model, Eq.(5).  
 321 Model parameters will be determined separately for the main proteins myosin  
 322 and actin, using literature data on denaturation as measured by DSC.

323 In slowly heated muscle meat a temporary extracellular phase will form.  
 324 The intracellular phase is regarded as a homogenized material, whose con-  
 325 ductivity is given by Eq.(2). The serum in the extracellular phase is a salt  
 326 solution with some soluble proteins, whose conductivity is given by Eq.(3).

327 The total conductivity of muscle meat is again described by the Torquato  
328 model, Eq.(4), where the intracellular phase is assumed as a homogenized  
329 dispersed phase having a conductivity  $\sigma_{fib}$ , embedded in the serum of the  
330 extracellular phase with conductivity  $\sigma_{s,ex}$ . With shape factor  $Q$  we account  
331 for the fiber direction with respect to the electric field.

332 The volume fraction of the extracellular phase  $\phi_{ex}$ , and the volume frac-  
333 tion of water in the intracellular phase  $\phi_w$  are coupled to the amount of  
334 protein denaturation via Eqs.(12)-(15).

### 335 3. Results

#### 336 3.1. Conductivity of salt solutions

337 The data for the electrical conductivity of salt (NaCl) solutions have been  
338 obtained from standard works and literature (Zell et al., 2009). At room  
339 temperature the conductivity can be fitted with a third order polynomial for  
340 concentrations up to  $c=25\%$  (see figure 4a). However, for the temperature  
341 dependency, only data is available for  $c = 1.5\%$  and  $c = 2.5\%$ . In the range of  
342  $c < 5\%$  the conductivity as function of concentration can be approximated by  
343 a function linear in  $c$ . In this concentration range the literature data shows  
344 that  $\sigma/c$  versus temperature renders a master curve (see figure 4b). Hence  
345 the above decomposition holds, i.e.  $\sigma_s = \sigma_{s,c}(c) \times \sigma_{s,T}(T)$ . Linear regression  
346 shows that the conductivity follows:

$$\sigma_s = c(1.47 + 0.027(T - 25)) \quad (16)$$

347 with  $T$  given in degrees Celsius, and  $\sigma_s$  in S/m.

### 3.2. *Electrical conductivity of fast heated meat*

We extend our investigations towards meat products, which are heated fast via Ohmic heating at rates between 10-160°C/min (Zell et al., 2009; Shirsat et al., 2004; Piette et al., 2004; Jin et al., 2015). We assume that at temperatures below 60°C there is no significant change in microstructure due protein denaturation. The experimental data will be compared to the submodel describing the electrical conductivity of the intracellular phase, Eq.(2).

If it is not specified in literature, we will assume that the volume fraction of water in the myofibers  $\phi_w$  can be estimated from the normal mass fraction of water in meat, which is 75% (van der Sman, 2007). Furthermore, for all meat products we assume there is a contribution of salts naturally occurring in meat, on top of the contribution of added salts. The level of salts naturally present in meat is assumed 0.9%, similar to a physiological saline solution (van der Sman and Boer, 2005).

The model contains only one unknown parameter, which is the hindrance factor  $f$ . We will estimate that using the data set on the conductivity of Ohmic heated beef (Zell et al., 2009). Its conductivity is measured at two salt concentrations, namely 1% and 2%. The applied heating rate is 40°C/min for unsalted meat, and 80°C/min for salted meat. The data for the lower salt concentration have been used to parameter estimation, and the higher salt concentration is used for validation. Results are shown in figure 5. Parameter estimation using least squares renders  $f = 0.67$ . The conductivity data for 2% salt for temperatures below 50°C complies with the prediction of our

372 model using  $f = 0.67$ . The effect of the fiber direction is also well predicted.  
 373 Above 50°C there is less good agreement between model predictions and  
 374 experimental data for the pork meat with high salt concentration. The above  
 375 estimated value of the hindrance factor  $f$  will be used for the remainder of  
 376 this paper.

377 The validity of the model is also tested using the conductivity data of  
 378 Ohmic heated fish (Jin et al., 2015). The fish conductivity has been mea-  
 379 sured both perpendicular and parallel to the muscle fibers. The applied  
 380 heating rate is about 15°C/min for fish with fibers parallel to the electric  
 381 field, and 10°C/min for fish with fibers perpendicular to the electric field.  
 382 Model predictions and experimental data are compared in figure 6. Again,  
 383 we obtain a reasonable prediction of the experimental data at temperatures  
 384 up to 80°C. Also the difference due to the fiber orientation is captured.

385 As a last validation we predict the electrical conductivity of Ohmic heated  
 386 meat emulsions, as measured in (Shirsat et al., 2004; Piette et al., 2004). The  
 387 applied heating rates are 160°C/min for meat emulsion without added salt  
 388 and about 20°C/min for meat emulsions with added salts. We apply Eq.(2)  
 389 with  $Q = \frac{1}{3}$ , due to the random orientation of the muscle fibers. Furthermore,  
 390 the fat droplets acting as insulators are assumed to be a dispersed phase  
 391 similar to proteins. The meat emulsions have varied in salt content from  
 392 1-5% and in fat content from 5-30%.

393 The comparison of the model and experimental data is shown figures 7  
 394 and 8. The model predicts reasonable well the observed values. For one odd  
 395 composition the model prediction deviates strongly from the experimental

396 data, even at room temperature. We attribute that to experimental error,  
 397 because for the majority of the investigated compositions the model predic-  
 398 tions at temperature below 60°C are well in agreement. Moreover, the meat  
 399 emulsion with no added salt (thus with total 1% salt) heated at the rate of  
 400 160°C/min (Shirsat et al., 2004) shows very good agreement even upto 80°C.  
 401 At this fast heating rates we expect little effects of protein denaturation.  
 402 At the slower heated emulsion one finds deviations from the predictions at  
 403 temperatures above 60°C, where one can expect deviations due to protein  
 404 denaturation. There is also some shrinkage of meat due to protein denatu-  
 405 ration, which can impart the contact of electrodes and meat, and thus also  
 406 the conductivity measurement.

407 All-in-all the model predicts well the observed trends for fast-heated  
 408 meats: 1) the conductivity is about linear for temperatures upto 60°C, 2)  
 409 the conductivity increases with the salt concentration, 3) the conductivity  
 410 lowers with the increase of fat content, 4) the conductivity is higher if the  
 411 electric field is parallel to the fibers, as opposed to the situation where the  
 412 electric field is perpendicular to the fibers, and 5) at temperatures above  
 413 60°C there is often some deviation from the linear increase of conductivity  
 414 with temperature, which is probably due to structural changes induced by  
 415 protein denaturation. In the next sections, we will investigate the kinetics of  
 416 protein denaturation, and its consequences for the electric conductivity.

### 417 3.3. Denaturation kinetics of meat proteins

418 In this section we investigate the thermodynamics and kinetics of protein  
419 denaturation, using the model described in section 2.4. The values for the  
420 parameter characterizing the melting behaviour of myosin and actin are ob-  
421 tained from (Ishiwatari et al., 2013). For myosin it holds  $T_{m,myo} = 50^\circ C$ , and  
422  $\Delta H_{m,myo} = 241$  kJ/mol, while for actin holds  $T_{m,act} = 65^\circ C$  and  $\Delta H_{m,act} = 380$   
423 kJ/mol.

424 First, we check the hypothesis concerning the reversibility of protein de-  
425 naturation using data of Water Holding Capacity (van der Sman, 2013). We  
426 assume that water is equally distributed over myosin and actin, and conse-  
427 quently that the WHC is linear with  $x_{eq} = \frac{1}{2}(x_{eq,myo} + x_{eq,act})$ , with  $x_{eq,i}$  given  
428 by Eq.(7-9). The WHC of meat is shown to be quite universal, and we com-  
429 pare  $x_{eq}$  with WHC data from (van der Sman, 2013). We have normalized  
430 the WHC as:

$$w = \frac{WHC(T) - WHC_{cooked}}{WHC_{raw} - WHC_{cooked}} \quad (17)$$

431 The WHC changed from  $WHC_{raw} = 79\%$  for raw meat to  $WHC_{cooked} = 45\%$   
432 for cooked meat (van der Sman, 2013).

433 If the hypothesis concerning reversibility of protein denaturation is true,  
434 we expect that  $w = x_{eq}$ , with  $x_{eq}$  computed using the denaturation model  
435 using the above parameter values. Both quantities are compared in figure 9.  
436 One can observe that the equilibrium value of the protein denaturation  $x_{eq}$   
437 nicely follows the trend in  $w$ . Hence, we assume our hypothesis of reversibility  
438 to be valid.

439 The model validation for the kinetics of protein denaturation is performed  
 440 using literature data concerning the peak temperature of myosin and actin  
 441 denaturation as measured with DSC (Differential Scanning Calorimetry) as a  
 442 function of scanning rate. If the time scale of heating is faster or comparable  
 443 to the time scale of protein denaturation the peak temperature shifts up to  
 444 higher temperatures with increasing scanning rate. For the analysis of the  
 445 denaturation of myosin and actin we have found the relevant DSC data in  
 446 refs. (Kijowski and Mast, 1988; Wagner and Anon, 1985; Ishiwatari et al.,  
 447 2013; Deng et al., 2002).

448 The literature data we have analysed with the above model. The peak  
 449 in the DSC trace we have compared to the peak in the protein denaturation  
 450 rate,  $dx/dt$ . Examples of such peaks in denaturation rates are shown in figure  
 451 10, as computed with the above model. One can observe that the peak shifts  
 452 to higher temperature with higher heating rates.

453 From these traces we have determined how the peak temperatures shift  
 454 with heating rate, for both myosin and actin. We have matched the model  
 455 predictions with the experimental observations via tuning the reaction rates  
 456  $k_N$ . The results of this analysis are presented in figure 11. Observe the large  
 457 scatter in experimental data, but still there is a clear trend that the peak  
 458 shifts towards higher temperature with higher heating rates.

459 The results of the parameter estimation are the following. For both pro-  
 460 teins holds that the activation energy is  $E_a/R_{gas}=5500$  K, which is often  
 461 found for biological processes - as expressed in the rule of van't Hof. At  
 462  $T = 60^\circ C$ , the reaction rates are  $k_N = 5.5 \pm 1.5 \times 10^{-3} s^{-1}$  for myosin, and

463  $k_N = 7.0 \pm 0.9 \times 10^{-3} \text{ s}^{-1}$  for actin. The 80% confidence intervals for the  
 464 peak temperature are indicated as dashed lines in the graph of figure 11.

465 In the figure one can observe that the model is following the trend in the  
 466 literature data, which does have quite a lot of scatter - as is also evident in  
 467 the large confidence intervals. If one compares the graphs, one can state that  
 468 the denaturation kinetics of actin and mysosin are very similar. Their dif-  
 469 ferences in denaturation behaviour is only due to differences in their melting  
 470 temperature and enthalpy, which are really thermodynamic factors.

### 471 3.4. *Electrical conductivity of meat at specific heating rates*

472 Having a valid model for protein denaturation and for electrical conduc-  
 473 tivity for fast heated meat (i.e. the intracellular phase) we can perform  
 474 the analysis for the electrical conductivity of slower heated meat, and faster  
 475 heated meats above 60 degrees Celsius. Data on electrical conductivity of  
 476 slower heated muscle meat is obtained from the studies (Brunton et al., 2006;  
 477 Basaran-Akgul et al., 2008), where the heating rate is  $10^\circ\text{C}/\text{min}$  or lower.  
 478 The experimental data is only available for conductivity perpendicular to the  
 479 meat fiber. Both sets of experimental studies show a significant decrease in  
 480 conductivity at temperatures above  $70^\circ\text{C}$ . Model predictions will be made  
 481 with the complete model, as explained in section 2.5. Please note, that all  
 482 required model parameters are already estimated in the previous section.  
 483 Hence, the presented values are really model predictions.

484 As an example of how protein denaturation modifies the structure of meat,  
 485 we show in figure 12 how the volume of the intracellular phase  $V_{cell}$ , and the



total of intra- and extracellular phase  $V_{tot}$  changes with temperature during slow heating at a rate of  $dT/dt=10^{\circ}\text{C}/\text{min}$ . The difference between the two volumes is a measure for the relative volume of the extracellular phase. Note, that at the start and at the end of heating the extracellular phase is absent. It is only present when proteins are actually denaturing, which happens in the temperature range of  $50 < T < 80^{\circ}\text{C}$ . In this temperature range we expect significant deviations of the electrical conductivity from the behaviour as discussed above in case of fast heating.

The model predictions for slow and fast heated muscle (meat) is given in figure 13, where it is compared to the experimental data. We have computed electrical conductivity for muscle meat (without added salts) using slow and fast heating rates of  $10^{\circ}\text{C}/\text{min}$  and  $160^{\circ}\text{C}/\text{min}$  respectively.

We observe that the electrical conductivity is linear dependent on temperature for fast heating rates at and above  $160^{\circ}\text{C}/\text{min}$ , where there is little development of the drip channels. In the figure for the fast heating rate one can observe first a slight increase in the electrical conductivity due to drip channel (extracellular phase) formation at temperatures above  $80^{\circ}\text{C}$ . At the slower heating rates the model predictions of the electrical conductivity indeed follow the trends shown in the experiments. First, there is a slight increase above the linear increase with temperature (due to onset on drip channel formation), followed by a significant decrease at temperatures above  $70^{\circ}\text{C}$ , which is due to the disappearance of the drip channels and the densification of the intracellular protein matrix. Also, quantitatively the model predictions are quite comparable to the experimental values obtained at the

510 slow heating rate.

#### 511 4. Conclusions

512 In this paper we have presented a predictive model for the development  
 513 of electrical conductivity of muscle meat during Ohmic heating. The model  
 514 computes the conductivity as a function of composition, temperature and  
 515 microstructure. We have assumed that the muscle meat is composed of  
 516 protein, water, and salt. Concerning the microstructure, the model takes  
 517 into account the muscle fiber orientation with respect to the electric field,  
 518 and the development of drip channels due to protein denaturation. The model  
 519 includes a description of the protein denaturation kinetics, which has been  
 520 validated independently using DSC measurements. The degree of protein  
 521 denaturation has been coupled to the development of drip channels, i.e. the  
 522 extracellular phase.

523 If the heating rate is faster than  $10^{\circ}\text{C}/\text{min}$ , the electrical conductivity  
 524 is more or less linear with temperature in the range  $T < 60^{\circ}\text{C}$ . In this  
 525 regime the time scale of heat transfer is much faster than that of the protein  
 526 denaturation, and consequently there is little drip channel formation. The  
 527 muscle meat behaves as a homogeneous gel, where the polymers are oriented  
 528 in a defined direction. The proteins act as insulators, and also hinder the  
 529 mobility of salt ions.

530 If the heating rate is slower than  $15^{\circ}\text{C}/\text{min}$ , the electrical conductivity is  
 531 showing a strong non-linear dependence with temperature. The most striking  
 532 effect is the strong decrease in conductivity at temperatures above  $70^{\circ}\text{C}$ . This

non-linear behaviour is explained by the changes in microstructure (i.e. drip channels). At the maximal conductivity, the drip channel volume is maximal, and the collagen in the connective tissue has not shrunk yet. The serum in the drip channels is not hindered in its mobility by a protein matrix as in the intracellular phase, leading to an increase of conductivity above that of the fast heated meat.

The subsequent shrinkage of the collagen of the perimysium and epimysium makes the drip channels to disappear, and the protein matrix densifies even more due to the denaturation of actin. The conductivity is lowered due to the absence of the drip channels, and the densified protein matrix of the intracellular phase (which is due to the loss in Water Holding Capacity). This decrease of conductivity with temperature is also shown for other meat products as in the study on Ohmic heating of thick pieces of minced meat Bozkurt and Icier (2010), which occurs at  $T > 65^{\circ}\text{C}$ . At temperatures above  $90^{\circ}\text{C}$  one can expect a further increase of the conductivity due to increase of the conductivity of the salt solution with temperature.

Take note that the above model presumes immediate loss of extracellular water, where as in large pieces of meat it will take time for the drip to flow through the channels. Hence, for proper modelling of water holding also the kinetics of water loss, as modelled previously (van der Sman, 2007), needs to be taken into account. Such a model can be extended to meat emulsions if water loss is accompanied by fat loss, as observed by Bozkurt and Icier (2010). Such a model for electrical conductivity can well be used in a simulation model for evaluating Ohmic heating for meat products. Be

557 aware that at slow heating rates there is some degree of protein denaturation,  
 558 and consequently there is also some shrinkage of the meat. This can lead to  
 559 poor contact of the meat with the electrodes, and possible dissipation of heat  
 560 in the fluid in between electrode and meat. Hence, for proper evaluation of  
 561 Ohmic heating the shrinkage problem has to be taken into account.

562 Furthermore, the presented model can be a basis for computing the WHC  
 563 as function of heating rate. From the protein denaturation model follows the  
 564 distribution of water over intra- and extracellular phase. The water binding  
 565 in the intracellular phase can be described by the Flory-Rehner theory, as we  
 566 have applied earlier to muscle meat, vegetables and other food gels (van der  
 567 Sman, 2007, 2012; van der Sman et al., 2013; Paudel et al., 2015; van der  
 568 Sman, 2015; Paudel et al., 2016). The water in the extracellular phase is  
 569 held by capillary pressure, which can be related to the radius of the drip  
 570 channels. The water in the drip channels is easily drained upon exertion of  
 571 mechanical force. If the water binding in the drip channels by the capillary  
 572 pressure can be incorporated in the thermodynamic framework of the Flory-  
 573 Rehner theory, one can predict how much water can be held under defined  
 574 mechanical forces.

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- 579 B Amsden. Solute diffusion within hydrogels. mechanisms and models.  
580 *Macromolecules*, 31(23):8382–8395, 1998.
- 581 A Anderko and MM Lencka. Computation of electrical conductivity of  
582 multicomponent aqueous systems in wide concentration and temperature  
583 ranges. *Industrial & Engineering chemistry research*, 36(5):1932–1943,  
584 1997.
- 585 N Basaran-Akgul, P Basaran, and BA Rasco. Effect of temperature (- 5 to  
586 130 c) and fiber direction on the dielectric properties of beef semitendinosus  
587 at radio frequency and microwave frequencies. *Journal of Food Science*, 73  
588 (6):E243–E249, 2008.
- 589 L Bazinet, F Castaigne, and Y Pouliot. Relative contribution of proteins to  
590 conductivity changes in skim milk during chemical acidification. *Applied*  
591 *Engineering in Agriculture*, 21(3):455–464, 2005.
- 592 C Bircan and SA Barringer. Determination of protein denaturation of muscle  
593 foods using the dielectric properties. *Journal of Food Science*, 67(1):202–  
594 205, 2002.
- 595 C Bircan, SA Barringer, and ME Mangino. Use of dielectric properties to  
596 detect whey protein denaturation. *Journal of microwave power and elec-*  
597 *tromagnetic energy*, 36(3):179–186, 2001.
- 598 M Bouhrara, S Clerjon, JL Damez, C Chevarin, S Portanguen, Al Kondjoyan,  
599 and JM Bonny. Dynamic mri and thermal simulation to interpret defor-

- 600 mation and water transfer in meat during heating. *Journal of agricultural*  
 601 *and food chemistry*, 59(4):1229–1235, 2011.
- 602 H Bozkurt and F Icier. Electrical conductivity changes of minced beef–fat  
 603 blends during ohmic cooking. *Journal of Food Engineering*, 96(1):86–92,  
 604 2010.
- 605 NP Brunton, JG Lyng, L Zhang, and JC Jacquier. The use of dielectric  
 606 properties and other physical analyses for assessing protein denaturation  
 607 in beef biceps femoris muscle during cooking from 5 to 85 c. *Meat Science*,  
 608 72(2):236–244, 2006.
- 609 TC Choy. *Effective medium theory: principles and applications*, volume 165.  
 610 Oxford University Press, 2015.
- 611 JL Damez and S Clerjon. Quantifying and predicting meat and meat prod-  
 612 ucts quality attributes using electromagnetic waves: An overview. *Meat*  
 613 *science*, 95(4):879–896, 2013.
- 614 Y Deng, K Rosenvold, AH Karlsson, P Horn, J Hedegaard, CL Steffensen,  
 615 and HJ Andersen. Relationship between thermal denaturation of porcine  
 616 muscle proteins and water-holding capacity. *Journal of Food Science*, 67  
 617 (5):1642–1647, 2002.
- 618 WY Gu, H Yao, AL Vega, and D Flagler. Diffusivity of ions in agarose gels  
 619 and intervertebral disc: effect of porosity. *Annals of biomedical Engineer-*  
 620 *ing*, 32(12):1710–1717, 2004.

- 621 JR Hamoen, HM Vollebregt, and RGM van der Sman. Prediction of the time  
622 evolution of pH in meat. *Food chemistry*, 141(3):2363–2372, 2013.
- 623 N Ishiwatari, M Fukuoka, and N Sakai. Effect of protein denaturation degree  
624 on texture and water state of cooked meat. *Journal of Food Engineering*,  
625 117(3):361–369, 2013.
- 626 H Jaeger, A Roth, S Toepfl, T Holzhauser, KH Engel, D Knorr, RF Vogel,  
627 N Bandick, S Kulling, and V Heinz. Opinion on the use of ohmic heating  
628 for the treatment of foods. *Trends in Food Science & Technology*, 55:84–97,  
629 2016.
- 630 Y Jin, YD Cheng, M Fukuoka, and N Sakai. Electrical conductivity of yel-  
631 lowtail (*seriola quinqueradiata*) fillets during ohmic heating. *Food and*  
632 *Bioprocess Technology*, 8(9):1904–1913, 2015.
- 633 N Kaur and AK Singh. Ohmic heating: Concept and applicationsa review.  
634 *Critical reviews in Food Science and nutrition*, 56(14):2338–2351, 2016.
- 635 JM Kijowski and MG Mast. Thermal properties of proteins in chicken broiler  
636 tissues. *Journal of Food Science*, 53(2):363–366, 1988.
- 637 A Kondjoyan, S Ouilic, S Portanguen, and JB Gros. Combined heat transfer  
638 and kinetic models to predict cooking loss during heat treatment of beef  
639 meat. *Meat science*, 95(2):336–344, 2013.
- 640 R Lumry and H Eyring. Conformation changes of proteins. *The Journal of*  
641 *Physical Chemistry*, 58(2):110–120, 1954.

- 642 JG Lyng, BM McKenna, and K Myer. Ohmic pasteurization of meat and  
 643 meat products. *Handbook of Farm, Dairy and Food Machinery Engineering*,  
 644 *2nd ed.*, Academic Press, Elsevier Inc., USA, pages 541–570, 2013.
- 645 F Marra. Mathematical model of solid food pasteurization by ohmic heating:  
 646 Influence of process parameters. *The Scientific World Journal*, 2014, 2014.
- 647 BM McKenna, J Lyng, N Brunton, and N Shirsat. Advances in radio fre-  
 648 quency and ohmic heating of meats. *Journal of Food Engineering*, 77(2):  
 649 215–229, 2006.
- 650 G Offer and T Cousins. The mechanism of drip production: formation of  
 651 two compartments of extracellular space in muscle post mortem. *Journal*  
 652 *of the Science of Food and Agriculture*, 58(1):107–116, 1992.
- 653 BK Oroszvári, CS Rocha, I Sjöholm, and E Tornberg. Permeability and  
 654 mass transfer as a function of the cooking temperature during the frying  
 655 of beefburgers. *Journal of Food Engineering*, 74(1):1–12, 2006.
- 656 E Paudel, RM Boom, and RGM van der Sman. Change in water-holding  
 657 capacity in mushroom with temperature analyzed by flory-rehner theory.  
 658 *Food and Bioprocess Technology*, 2015. doi: 10.1007/s11947-014-1459-7.
- 659 E Paudel, RM Boom, and RGM van der Sman. Effects of porosity and  
 660 thermal treatment on hydration of mushrooms. *Food and Bioprocess Tech-*  
 661 *nology*, 9(3):511–519, 2016.



- KL Pearce, K Rosenvold, HJ Andersen, and DL Hopkins. Water distribution and mobility in meat during the conversion of muscle to meat and ageing and the impacts on fresh meat quality attributesa review. *Meat Science*, 89(2):111–124, 2011.
- G Piette, ML Buteau, D De Halleux, L Chiu, Y Raymond, HS Ramaswamy, and M Dostie. Ohmic cooking of processed meats and its effects on product quality. *Journal of Food Science*, 69(2):fep71–fep78, 2004.
- F Rossi, G Perale, and M Masi. Principles of controlled drug release: A mass transport matter. In *Controlled Drug Delivery Systems*, pages 9–33. Springer, 2016.
- N Shibata-Ishiwatari, M Fukuoka, and N Sakai. Changes in the viscosity of expressible water in meat during heating: Description based on the denaturation kinetics of water-soluble proteins. *Food Science and Technology Research*, 21(4):525–530, 2015.
- N Shirsat, JG Lyng, NP Brunton, and BM McKenna. Conductivities and ohmic heating of meat emulsion batters. *Journal of Muscle Foods*, 15(2):121–137, 2004.
- E Tornberg. Effects of heat on meat proteins—implications on structure and quality of meat products. *Meat science*, 70(3):493–508, 2005.
- S Torquato and AK Sen. Conductivity tensor of anisotropic composite media from the microstructure. *Journal of applied physics*, 67(3):1145–1155, 1990.

- 683 RGM van der Sman. Moisture transport during cooking of meat: An analysis  
684 based on flory–rehner theory. *Meat science*, 76(4):730–738, 2007.
- 685 RGM van der Sman. Prediction of enthalpy and thermal conductivity of  
686 frozen meat and fish products from composition data. *Journal of Food*  
687 *Engineering*, 84(3):400–412, 2008.
- 688 RGM van der Sman. Thermodynamics of meat proteins. *Food Hydrocolloids*,  
689 27(2):529–535, 2012.
- 690 RGM van der Sman. Modeling cooking of chicken meat in industrial tunnel  
691 ovens with the flory–rehner theory. *Meat science*, 95(4):940–957, 2013.
- 692 RGM van der Sman. Hyperelastic models for hydration of cellular tissue.  
693 *Soft matter*, 11(38):7579–7591, 2015.
- 694 RGM van der Sman and E Boer. Predicting the initial freezing point and  
695 water activity of meat products from composition data. *Journal of Food*  
696 *Engineering*, 66(4):469–475, 2005.
- 697 RGM van der Sman, E Paudel, A Voda, and S Khalloufi. Hydration prop-  
698 erties of vegetable foods explained by flory–rehner theory. *Food Research*  
699 *International*, 54(1):804–811, 2013.
- 700 KS Varghese, MC Pandey, K Radhakrishna, and AS Bawa. Technology,  
701 applications and modelling of ohmic heating: a review. *Journal of Food*  
702 *Science and technology*, 51(10):2304–2317, 2014.

- 703 JR Wagner and MC Anon. Denaturation kinetics of myofibrillar proteins in  
704 bovine muscle. *Journal of Food Science*, 50(6):1547–1550, 1985.
- 705 Y Wang, J Tang, B Rasco, F Kong, and S Wang. Dielectric properties of  
706 salmon fillets as a function of temperature and composition. *Journal of*  
707 *Food Engineering*, 87(2):236–246, 2008.
- 708 G Yildiz-Turp, IY Sengun, P Kendirci, and F Icier. Effect of ohmic treatment  
709 on quality characteristic of meat: A review. *Meat science*, 93(3):441–448,  
710 2013.
- 711 M Zell, JG Lyng, DA Cronin, and DJ Morgan. Ohmic heating of meats:  
712 Electrical conductivities of whole meats and processed meat ingredients.  
713 *Meat science*, 83(3):563–570, 2009.
- 714 BI Zielbauer, J Franz, B Viezens, and TA Vilgis. Physical aspects of meat  
715 cooking: Time dependent thermal protein denaturation and water loss.  
716 *Food Biophysics*, 11(1):34–42, 2016.

Table 1: List of symbols

Symbol	Description	Unit
$f$	friction factor	[-]
$k$	reaction rate	[1/s]
$t$	time	[s]
$x$	mole fraction	[-]
$y$	mass fraction	[-]
$D$	amount of denatured proteins	[mol/m <sup>3</sup> ]
$E$	activation energy	[J/mol]
$G$	free energy	[J/mol]
$H$	enthalpy	[J/mol]
$K$	reaction constant	[-]
$N$	amount of native proteins	[mol/m <sup>3</sup> ]
$Q$	shape factor	[-]
$R$	gas constant	[J/mol.K]
$T$	Temperature	[K]
$V$	volume	[m <sup>3</sup> ]
$\delta$	relative difference in conductivity	[-]
$\eta$	viscosity	[Pa.s]
$\phi$	volume fraction	[-]
$\rho$	density	[kg/m <sup>3</sup> ]
$\sigma$	conductivity	[S/m]

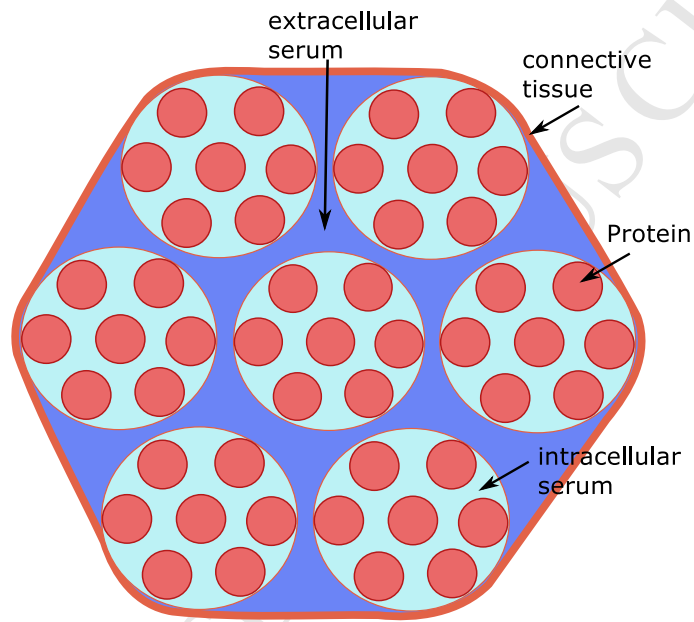


Figure 1: The hierarchical composite structure of cooking meat. At the largest length scale we distinguish the extracellular and intracellular phases. The intracellular phase is bounded by connective tissue, and its internal structure is assumed to consist of protein fibers (cylinders) embedded in serum. The extracellular phase contains the same serum, which is a mixture of water, salt and soluble proteins.

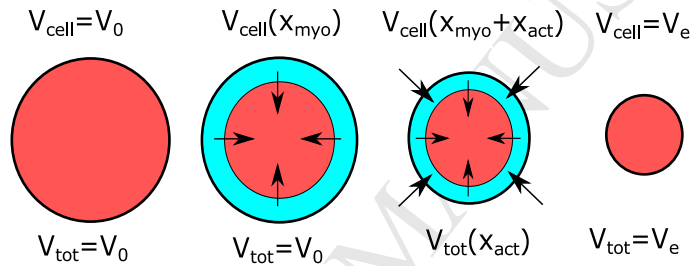


Figure 2: Schematic representation of the development of the microstructure of meat, where we have depicted the volume (cross sections) of intracellular phase ( $V_{cell}$  in pink) and extracellular phase (in blue). The total volume  $V_{tot}$  is the sum of intra- and extracellular phase. The volumes evolves as a function of the fraction of denatured proteins  $x_{act}$  and  $x_{myo}$ .

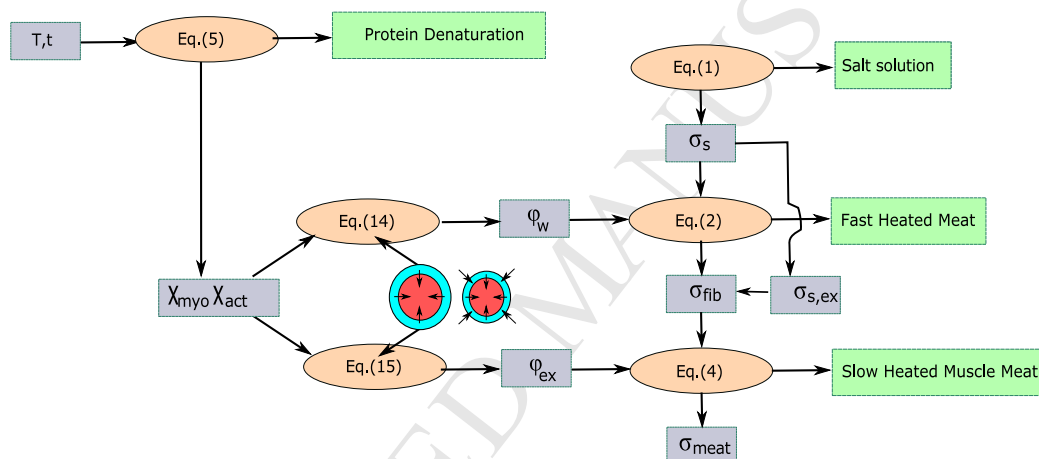


Figure 3: A flowchart showing how the equations of the model connect to each other, and how the submodels can be used for different problems as shown in the green boxes. Inputs and outputs to the equations are shown as blue boxes.

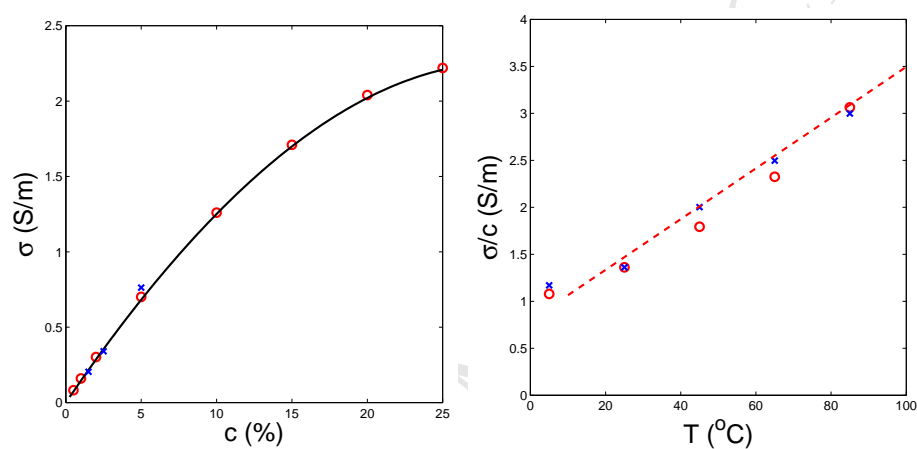


Figure 4: a) Electrical conductivity  $\sigma$  of salt solution at room temperature as function of concentration (mass fraction)  $c$ . Data are obtained from the CRC Handbook of Chemistry and Physics and Zell (Zell et al., 2009) (symbols), and fitted by a third order polynomial (solid line). b) Electrical conductivity (normalized with concentration)  $\sigma/c$  of salt solution as function temperature for  $c=1.5$  and  $2.5\%$ , with data obtained from (Zell et al., 2009). The dashed line is obtained via linear regression.



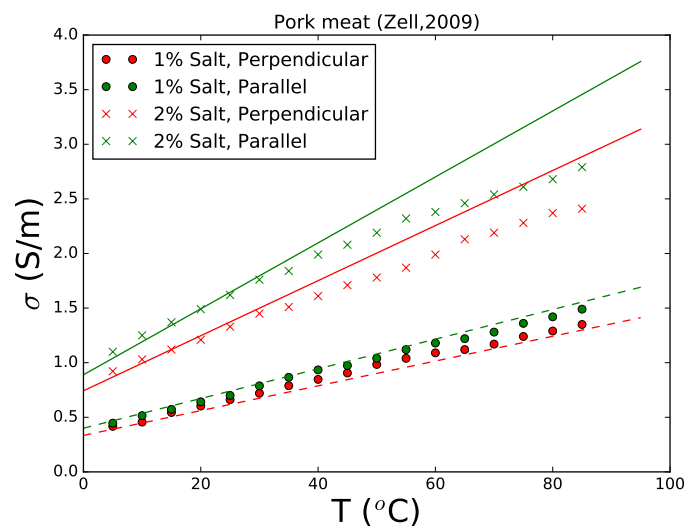


Figure 5: Electrical conductivity of beef, as measured by Zell (Zell et al., 2009), and compared to model calculations (lines). Model has been fitted to low salt meat, using Eq.(2), and the data on high salt meat is used for validation.

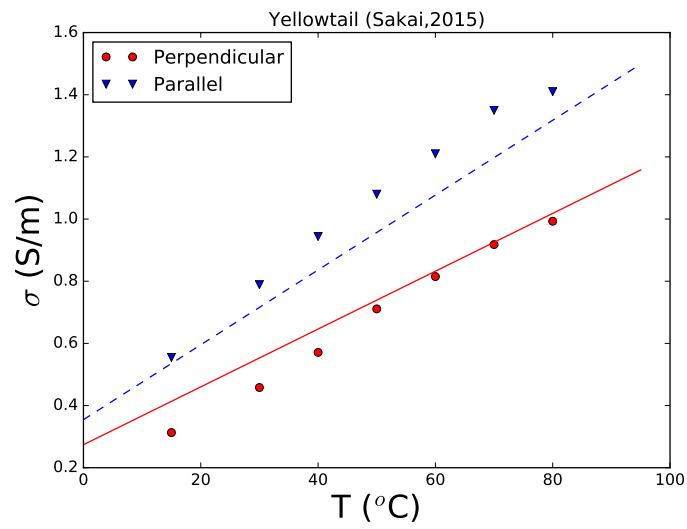


Figure 6: Predictions of electrical conductivity (lines) versus data on Yellowtail fish (Jin et al., 2015) using Eq.(2).

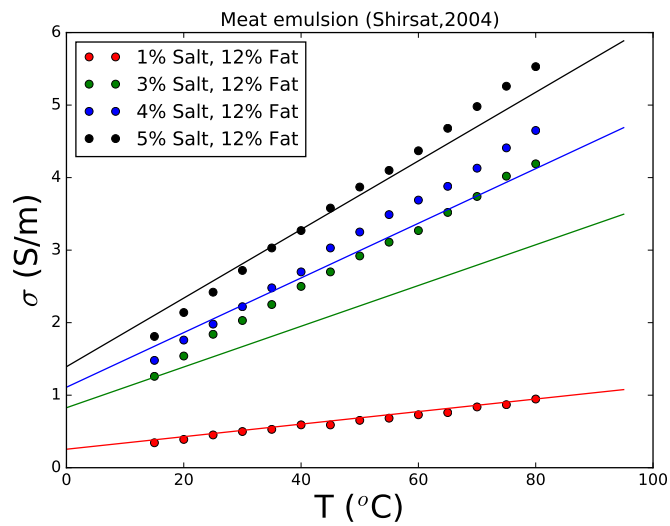


Figure 7: Predictions of electrical conductivity (lines) versus data on meat emulsions (Shirsat et al., 2004) using Eq.(2).

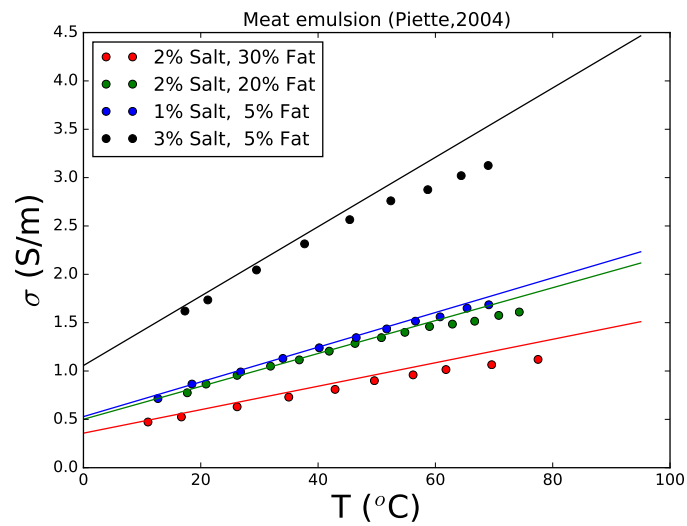


Figure 8: Predictions of electrical conductivity (lines) versus data on meat emulsions (Piette et al., 2004) using Eq.(2).

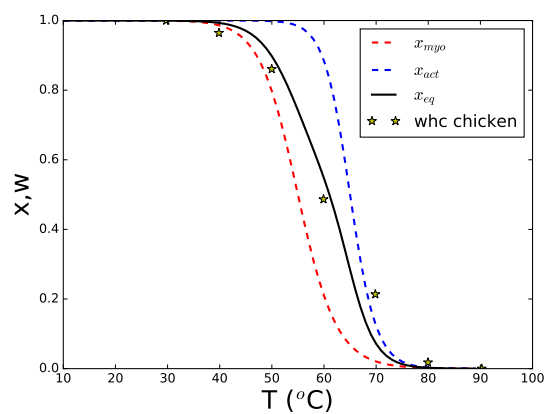


Figure 9: Theoretical fraction of native protein versus temperature (solid line), compared to the dimensionless WHC of chicken meat (symbols), with data obtained from (van der Sman, 2013). The dashed lines indicate the individual contributions of myosin (red) and actin (blue) as computed from the steady state solutions of Eqs.(5).

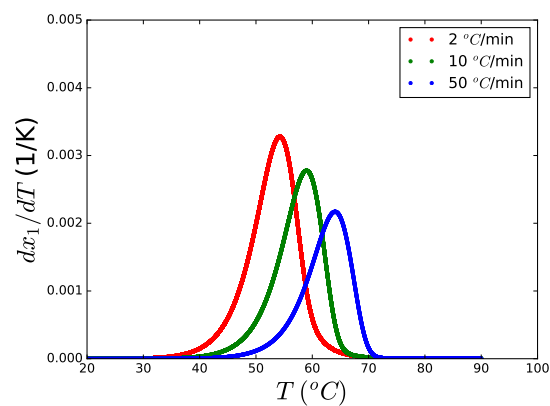


Figure 10: Peaks in denaturation rate of myosin  $dx_{myo}/dt$  as function of heating rate  $dT/dt$ . For clarity of presentation of data the denaturation rate is rescaled with the heating rate, i.e.  $dx_{myo}/dT = (dx_{myo}/dt) \times (dT/dt)^{-1}$ . Traces are shown for three heating rates. DSC traces are proportional to  $dx_{myo}/dt$  due to absorbance of latent heat.

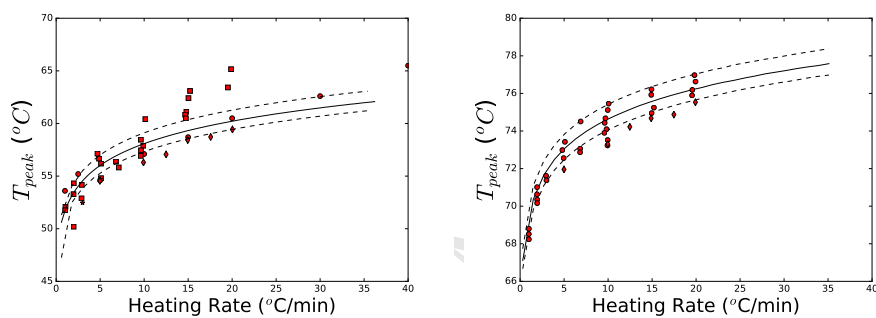


Figure 11: Shift of peak temperature  $T_{peak}$  in the DSC scan as function of heating rate, analysed for myosin (left pane), and actin (right pane). Symbols represent data from different literature sources, and -the solid line represent the fitted model, Eqs.(5), with the dashed lines indicating the 80% confidence intervals.

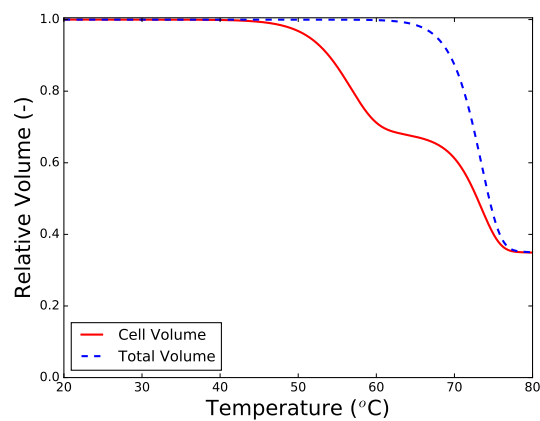


Figure 12: Evolution of the relative volume of intracellular phase,  $V_{cell}$ , and total volume of intra- and extracellular phase,  $V_{tot}$ , as function of temperature during heating at a rate of 10°C per minute. The initial cell volume is taken as a reference.



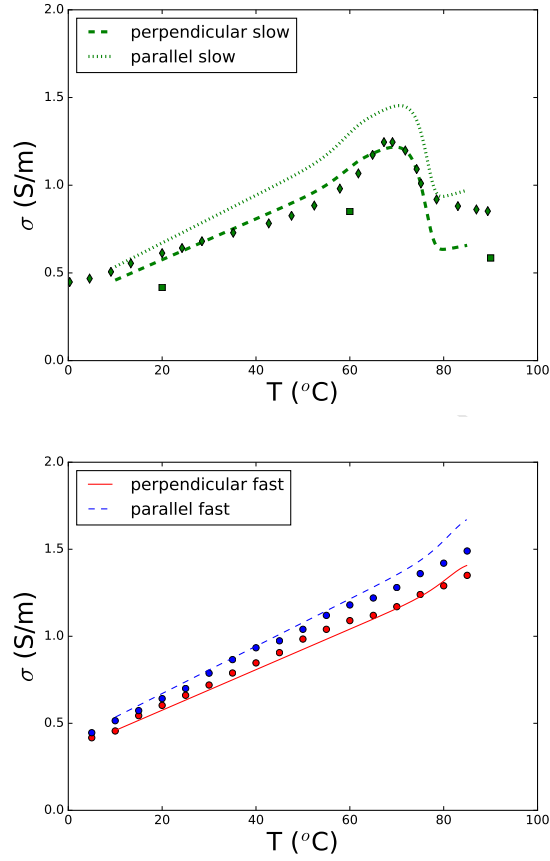


Figure 13: Conductivity of lean meat in perpendicular and parallel direction, following experimental data of (Zell et al., 2009) (for fast heating) and (Brunton et al., 2006; Basaran-Akgul et al., 2008) (for slow heating). Slow heating are indicated with green lines and symbols, and fast heating with red and blue symbols or lines. The lines are model predictions using the complete model, including protein denaturation as function of heating rate. The shown fast heating curves are given for  $160^{\circ}\text{C}/\text{min}$ , while the slow heating curve is computed for  $dT/dt = 10^{\circ}\text{C}/\text{min}$ .

Model predicts electrical conductivity of meat as function of composition and heating rate

Model considers effect of structural changes induced by protein denaturation

Slow to moderate heated meat show a drop in conductivity at  $T > 70$  degrees

A submodel predicts meat protein denaturation kinetics