

$$(c) \quad t_s \approx 10s \Rightarrow \frac{4.6}{\zeta \omega_n} = 10 \Rightarrow \zeta \omega_n = 0.46$$

$$\text{steady state error to ramp input} = 0.1 \Rightarrow \frac{1}{K_V} = 0.1 \quad K_V = 10$$

$$\text{need } \lim_{s \rightarrow 0} s C(s) G(s) = 10$$

$$s C(s) G(s) = \frac{s \left(K_P + \frac{1}{s} K_I \right) \frac{1}{10}}{s + \frac{1}{440}}$$

$$\lim_{s \rightarrow 0} s C(s) G(s) = \frac{\frac{1}{10} K_I}{\frac{1}{440}} = 44 K_I \Rightarrow \text{put } K_I = \frac{10}{44}$$

closed loop:

$$\frac{T_o(s)}{T_{ref}(s)} = \frac{\left(K_P + \frac{K_I}{s} \right) \frac{1}{10}}{s + \frac{1}{440}} = \frac{\frac{1}{10} (K_P s + K_I) \frac{1}{s}}{1 + \frac{\left(K_P + \frac{K_I}{s} \right) \frac{1}{10}}{s + \frac{1}{440}}}$$

$$= \frac{\frac{1}{10} (K_P s + K_I)}{s^2 + \left(\frac{1}{440} + \frac{K_P}{10} \right) s + \frac{K_I}{10}}$$

$2\zeta\omega_n$ $\frac{1}{44} \Rightarrow \omega_n =$

$$\text{want } 2\zeta\omega_n = 2(0.46) = 0.92 = \frac{1}{440} + \frac{K_P}{10}$$

$$K_P = 10 \left(0.92 - \frac{1}{440} \right) = 9.18$$

$$\underline{K_P = 9.18}$$