

$$\textcircled{c} \quad t_S = 10s \Rightarrow \frac{4.6}{5\omega} = \omega \Rightarrow \omega_n = 0.46$$

Steady state error to ramp input = 0.1 $\Rightarrow \frac{1}{K_V} = 0.1 \quad K_V = 10$

need: $s C(s) G(s) = 10$
 $\lim_{s \rightarrow 0}$

$$s C(s) G(s) = s \left(K_p + \frac{1}{s} K_I \right) \frac{1}{10} \\ s + \frac{1}{440}$$

$$\lim_{s \rightarrow 0} s C(s) G(s) = \frac{\frac{1}{10} K_I}{\frac{1}{440}} = 44 K_I \Rightarrow \underline{K_I = \frac{10}{44}}$$

Closed loop:

$$\frac{T_d(s)}{T_M(s)} = \frac{\left(K_p + \frac{K_I}{s} \right) \frac{1}{10}}{s + \frac{1}{440}} = \frac{\frac{1}{10} (K_p s + K_I) \frac{1}{s}}{s + \frac{1}{440} + \frac{1}{10} (K_p s + K_I) \frac{1}{s}}$$

$$= \frac{\frac{1}{10} (K_p s + K_I)}{s^2 + \underbrace{\left(\frac{1}{440} + \frac{K_p}{10} \right)}_{2\{\omega_n\}} s + \underbrace{\frac{K_I}{10}}_{1/44} \Rightarrow \omega_n =}$$

$$\omega_n + 2\{\omega_n\} = 2(0.46) = 0.92 = \frac{1}{440} + \frac{K_p}{10}$$

$$K_p = 10 \left(0.92 - \frac{1}{440} \right) = 9.18$$

$$\underline{K_p = 9.18}$$