# HNCO Influence of the learning rate on the performance of PBIL

## September 16, 2018

#### Abstract

PBIL is applied many times to the same collection of fitness functions (bit vector size n = 100), each time with a different learning rate taken from a finite set of values. All learning rates are ranked according to their median fitness over 20 independent runs, first for each fitness function, then across the entire collection of fitness functions. The mean and standard deviation of fitness are also plotted as a function of the learning rate.

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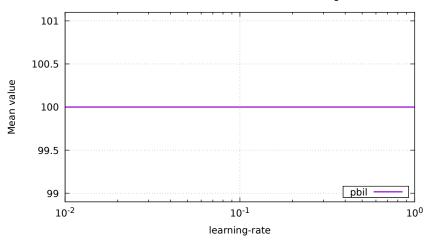
## 1 Rankings

algorithm	learning-rate	rai	nk d	listri	ibut	ion		
		1	2	3	4	5	6	7
pbil	1	6	0	1	1	0	1	0
pbil	0.01	5	1	1	0	1	0	1
pbil	0.02	3	2	1	2	1	0	0
pbil	0.5	$^{2}$	3	1	1	1	1	0
pbil	0.2	$^{2}$	0	2	0	3	1	1
pbil	0.05	$^{2}$	0	1	1	1	4	0
pbil	0.1	2	0	1	1	1	0	4

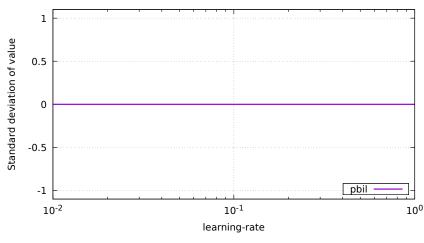
## 2 Function one-max

algorithm	learning-rate	funct	ion va	lue			
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	100	100	100	100	100	1
pbil	0.02	100	100	100	100	100	1
pbil	0.05	100	100	100	100	100	1
pbil	0.1	100	100	100	100	100	1
pbil	0.2	100	100	100	100	100	1
pbil	0.5	100	100	100	100	100	1
pbil	1	100	100	100	100	100	1

one-max: Mean value as a function of learning-rate



one-max: Standard deviation of value as a function of learning-rate



pbil on one-max

101

100.5

100

99.5

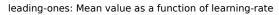
10-2

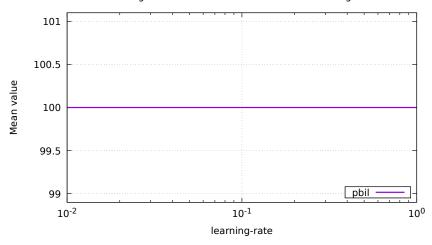
10-1

learning-rate

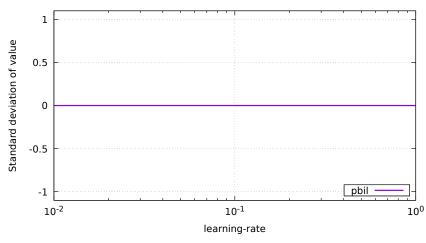
# 3 Function leading-ones

$\operatorname{algorithm}$	learning-rate	function value							
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk		
pbil	0.01	100	100	100	100	100	1		
pbil	0.02	100	100	100	100	100	1		
pbil	0.05	100	100	100	100	100	1		
pbil	0.1	100	100	100	100	100	1		
pbil	0.2	100	100	100	100	100	1		
pbil	0.5	100	100	100	100	100	1		
pbil	1	100	100	100	100	100	1		

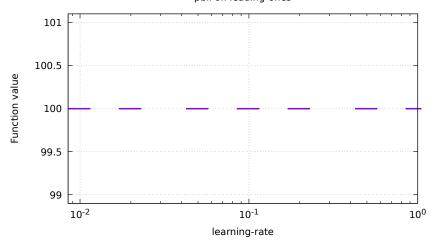




#### leading-ones: Standard deviation of value as a function of learning-rate



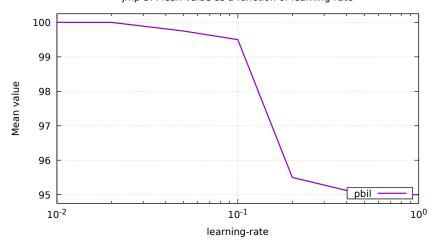
### pbil on leading-ones



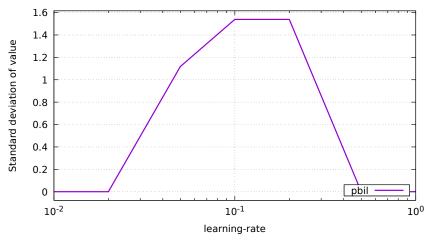
# 4 Function jmp-5

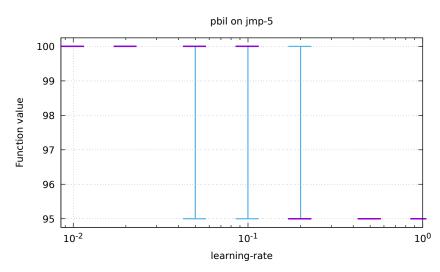
algorithm	learning-rate	function value						
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk	
pbil	0.01	100	100	100	100	100	1	
pbil	0.02	100	100	100	100	100	1	
pbil	0.05	95	100	100	100	100	3	
pbil	0.1	95	100	100	100	100	3	
pbil	0.2	95	95	95	95	100	5	
pbil	0.5	95	95	95	95	95	6	
pbil	1	95	95	95	95	95	6	

jmp-5: Mean value as a function of learning-rate



jmp-5: Standard deviation of value as a function of learning-rate

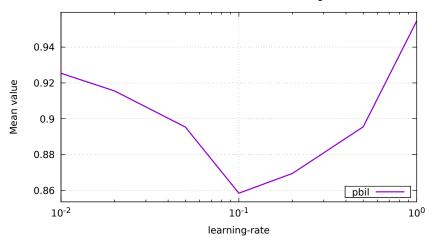




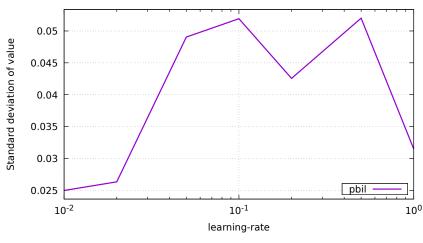
## 5 Function nk

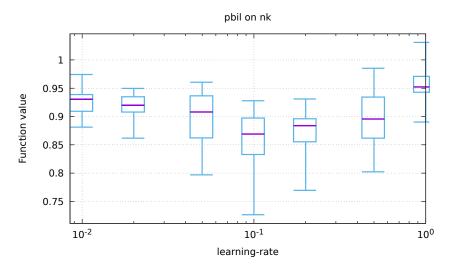
algorithm	learning-rate	$\operatorname{funct}$	function value						
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk		
pbil	0.01	0.88	0.91	0.93	0.94	0.97	2		
pbil	0.02	0.86	0.91	0.92	0.93	0.95	3		
pbil	0.05	0.80	0.86	0.91	0.94	0.96	4		
pbil	0.1	0.73	0.83	0.87	0.90	0.93	7		
pbil	0.2	0.77	0.86	0.88	0.90	0.93	6		
pbil	0.5	0.80	0.86	0.90	0.93	0.99	5		
pbil	1	0.89	0.94	0.95	0.97	1.03	1		

#### nk: Mean value as a function of learning-rate



#### nk: Standard deviation of value as a function of learning-rate

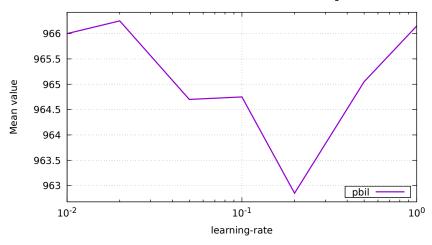




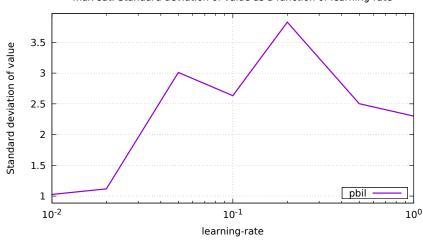
## 6 Function max-sat

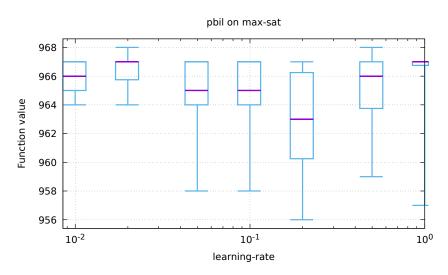
algorithm	learning-rate	funct	ion va	lue			
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	964	965	966	967	967	3
pbil	0.02	964	966	967	967	968	2
pbil	0.05	958	964	965	967	967	5
pbil	0.1	958	964	965	967	967	5
pbil	0.2	956	960	963	966	967	7
pbil	0.5	959	964	966	967	968	4
pbil	1	957	967	967	967	967	1

max-sat: Mean value as a function of learning-rate



max-sat: Standard deviation of value as a function of learning-rate

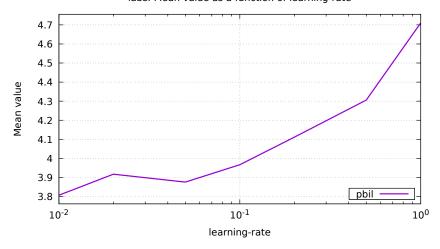




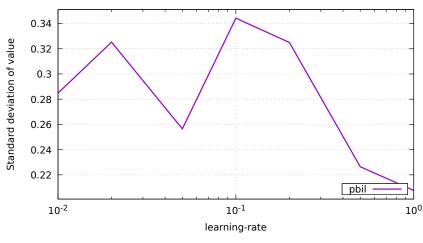
# 7 Function labs

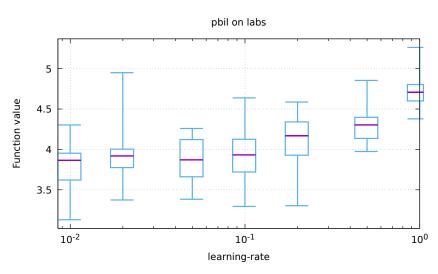
algorithm	learning-rate	funct	function value						
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk		
pbil	0.01	3.13	3.62	3.86	3.95	4.30	7		
pbil	0.02	3.37	3.78	3.92	4.00	4.95	5		
pbil	0.05	3.38	3.66	3.87	4.12	4.26	6		
pbil	0.1	3.29	3.72	3.93	4.13	4.64	4		
pbil	0.2	3.30	3.93	4.17	4.34	4.59	3		
pbil	0.5	3.97	4.14	4.30	4.40	4.85	2		
pbil	1	4.38	4.60	4.71	4.80	5.26	1		

labs: Mean value as a function of learning-rate



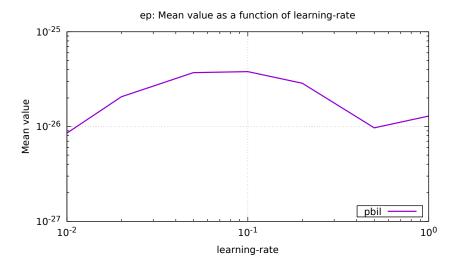
labs: Standard deviation of value as a function of learning-rate

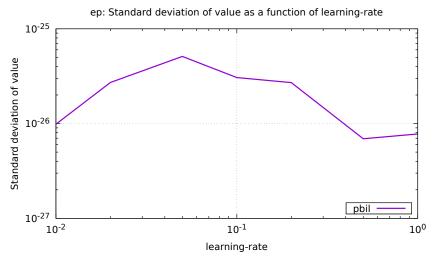


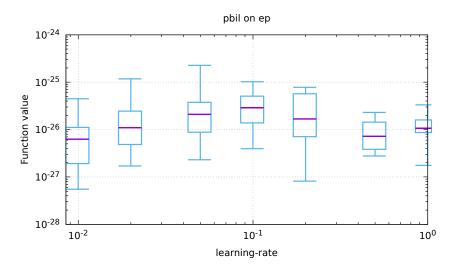


# 8 Function ep

algorithm	${\rm learning\text{-}rate}$	function valu	ıe				
		min	$Q_1$	med.	$Q_3$	max	rk
pbil	0.01	$5.5 \times 10^{-28}$	$1.9 \times 10^{-27}$	$6.3 \times 10^{-27}$	$1.1 \times 10^{-26}$	$4.5 \times 10^{-26}$	
pbil	0.02	$1.7 \times 10^{-27}$	$4.8 \times 10^{-27}$	$1.1 \times 10^{-26}$	$2.4 \times 10^{-26}$	$1.2 \times 10^{-25}$	4
pbil	0.05	$2.3 \times 10^{-27}$	$8.8 \times 10^{-27}$	$2.1 \times 10^{-26}$	$3.8 \times 10^{-26}$	$2.3 \times 10^{-25}$	6
pbil	0.1	$4.0 \times 10^{-27}$	$1.4 \times 10^{-26}$	$2.9 \times 10^{-26}$	$5.1 \times 10^{-26}$	$1.0 \times 10^{-25}$	7
pbil	0.2	$8.2 \times 10^{-28}$	$7.1 \times 10^{-27}$	$1.7 \times 10^{-26}$	$5.7 \times 10^{-26}$	$7.8 \times 10^{-26}$	5
pbil	0.5	$2.8 \times 10^{-27}$	$3.8 \times 10^{-27}$	$7.2 \times 10^{-27}$	$1.4 \times 10^{-26}$	$2.3 \times 10^{-26}$	$^{2}$
pbil	1	$1.8 \times 10^{-27}$	$8.7 \times 10^{-27}$	$1.1 \times 10^{-26}$	$1.6 \times 10^{-26}$	$3.3\times10^{-26}$	3



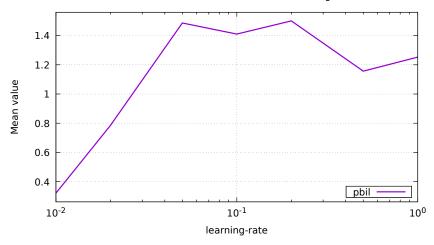




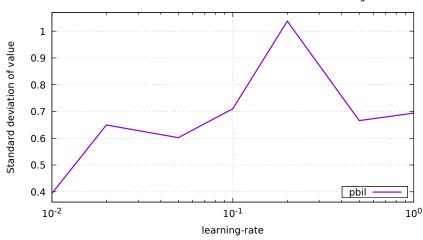
## 9 Function cancel

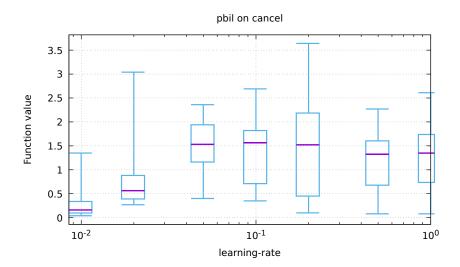
algorithm	learning-rate	funct	ion val	ue			
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	0.04	0.10	0.16	0.34	1.35	1
pbil	0.02	0.27	0.39	0.57	0.88	3.04	2
pbil	0.05	0.40	1.16	1.53	1.94	2.36	6
pbil	0.1	0.35	0.71	1.57	1.82	2.69	7
pbil	0.2	0.10	0.45	1.52	2.19	3.64	5
pbil	0.5	0.08	0.68	1.33	1.61	2.27	3
pbil	1	0.08	0.74	1.35	1.74	2.61	4

#### cancel: Mean value as a function of learning-rate



#### cancel: Standard deviation of value as a function of learning-rate

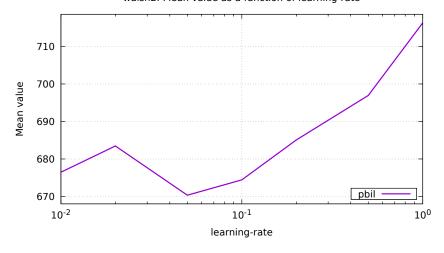




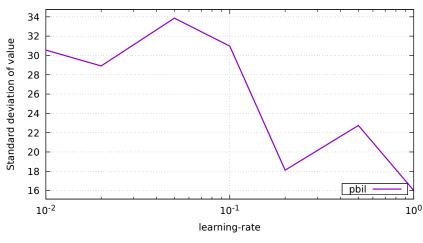
## 10 Function walsh2

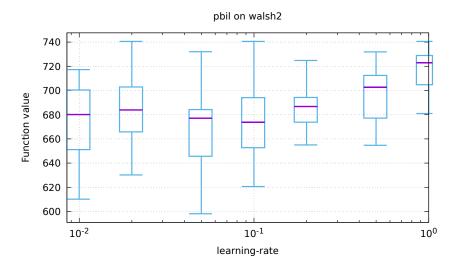
algorithm	learning-rate	function	function value							
		min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk			
pbil	0.01	610.19	651.14	680.15	700.43	717.25	5			
pbil	0.02	630.22	665.78	683.89	702.91	740.55	4			
pbil	0.05	598.14	645.64	677.18	684.24	732.02	6			
pbil	0.1	620.61	652.73	673.79	694.09	740.55	7			
pbil	0.2	654.98	673.82	686.76	694.24	724.80	3			
pbil	0.5	654.72	677.17	702.72	712.46	731.88	2			
pbil	1	680.97	704.77	722.86	728.89	740.55	1			

walsh2: Mean value as a function of learning-rate



walsh2: Standard deviation of value as a function of learning-rate





### A Plan

```
{
    "exec": "hnco",
    "opt": "-s 100 --map 1 --map-random -i 0 -b 200000 --print-performance",
    "num_runs": 20,
    "parallel": true,
    "parameter": {
        "id": "learning-rate",
        "values": [ 1e-2, 2e-2, 5e-2, 1e-1, 2e-1, 5e-1, 1 ],
        "logscale": true,
        "boxwidth": "$1 * 0.3"
    },
    "functions": [
        {
            "id": "one-max",
            "opt": "-F 0 --stop-on-maximum",
            "col": ">{{\\nprounddigits{0}}}N{3}{0}"
        },
        {
            "id": "leading-ones",
            "opt": "-F 10 --stop-on-maximum",
            "col": ">{{\\nprounddigits{0}}}N{3}{0}"
        },
            "id": "jmp-5",
            "opt": "-F 30 --stop-on-maximum -t 5",
            "col": ">{{\\nprounddigits{0}}}N{3}{0}"
       },
            "id": "nk",
            "opt": "-F 60 -p instances/nk.100.4",
            "col": ">{{\\nprounddigits{2}}}N{1}{2}"
       },
            "id": "max-sat",
            "opt": "-F 70 -p instances/ms.100.3.1000",
            "col": ">{{\\nprounddigits{0}}}N{3}{0}"
        },
            "id": "labs",
            "opt": "-F 81",
            "col": ">{{\\nprounddigits{2}}}N{1}{2}"
        },
            "id": "ep",
            "opt": "-F 90 -p instances/ep.100",
            "reverse": true,
            "logscale": true,
            "col": ">{{\\nprounddigits{1}}}N{1}{1}"
        },
            "id": "cancel",
            "opt": "-F 100 -s 99",
            "reverse": true,
            "col": ">{{\\nprounddigits{2}}}N{1}{2}"
        },
            "id": "walsh2",
            "opt": "-F 162 -p instances/walsh2.100",
            "col": ">{{\\nprounddigits{2}}}N{3}{2}"
        }
   ],
```

## B Default parameters

```
# algorithm = 100
# bm_mc_reset_strategy = 1
# bm_num_gs_cycles = 1
# bm_num_gs_steps = 100
# bm_sampling = 1
# budget = 10000
# bv_size = 100
\# ea_lambda = 100
\# ea_mu = 10
# fn_name = noname
# fn_num_traps = 10
# fn_prefix_length = 2
# fn_threshold = 10
# function = 0
# ga_crossover_bias = 0.5
# ga_crossover_probability = 0.5
# ga_tournament_size = 10
# hea_binary_dynamics = 0
\# hea_delay = 10000
# hea_num_par_updates = 1
# hea_num_seq_updates = 100
# hea_rate_strategy = 0
# hea_reset_period = 0
# hea_sampling_method = 0
# hea_time_constant = 1000
# hea_weight = 1
# learning_rate = 0.001
# map = 0
# map_input_size = 100
# map_path = nopath
# mutation_probability = 1
# neighborhood = 0
# neighborhood_iterator = 0
# noise_stddev = 1
# num_iterations = 0
# num_threads = 1
# path = nopath
# pn_mutation_probability = 1
# pn_neighborhood = 0
# pn_radius = 2
# population_size = 10
# pv_log_num_components = 5
# radius = 2
# rls_patience = 50
# sa_beta_ratio = 1.2
# sa_initial_acceptance_probability = 0.6
# sa_num_transitions = 50
# sa_num_trials = 100
\# seed = 0
# selection_size = 1
# target = 100
# print_defaults
```

- # last\_parameter
- # exec\_name = hnco
- # version = 0.10
- # Generated from hnco.json