HNCO
Visualization of Walsh transforms of various functions defined on bit vectors

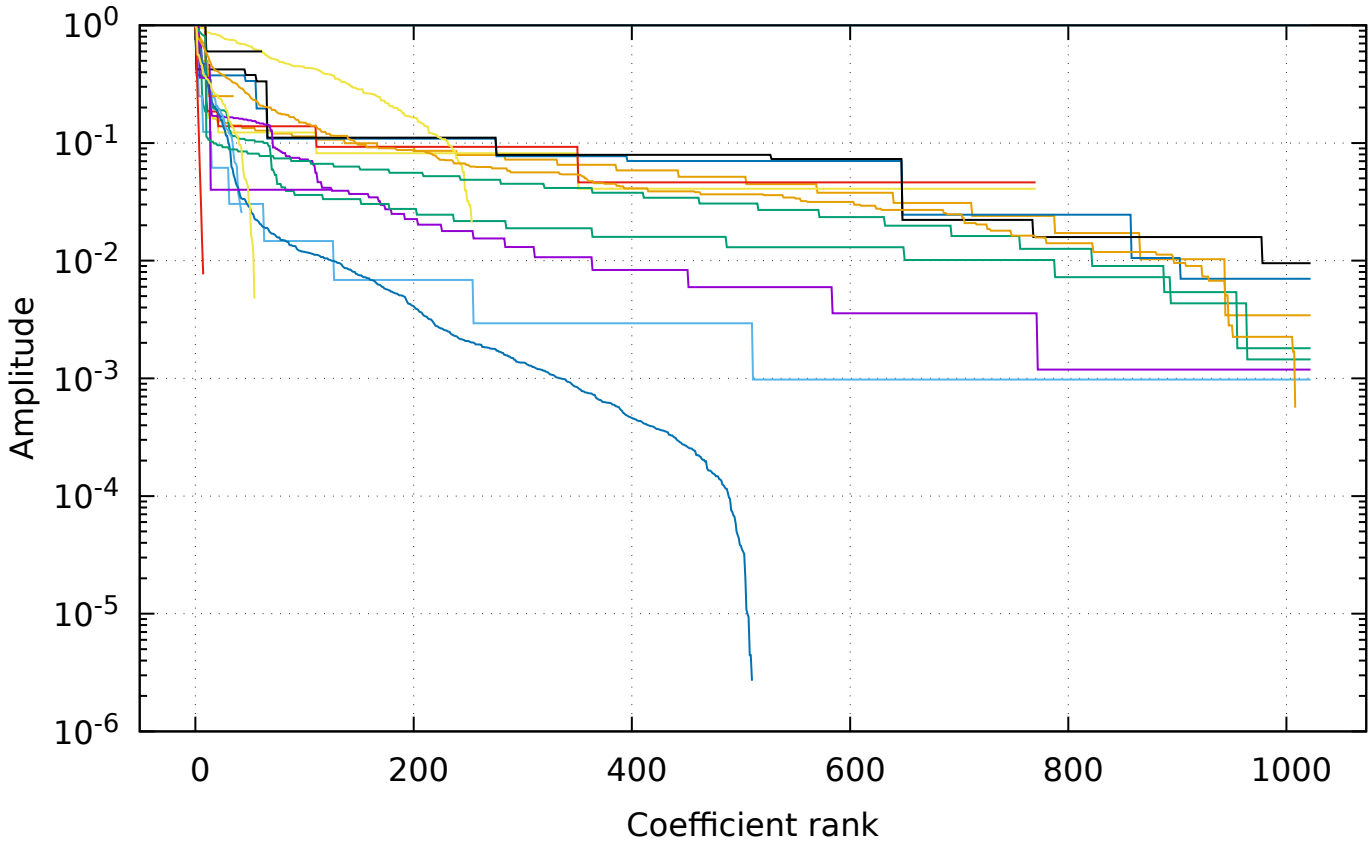
July 16, 2018

Abstract

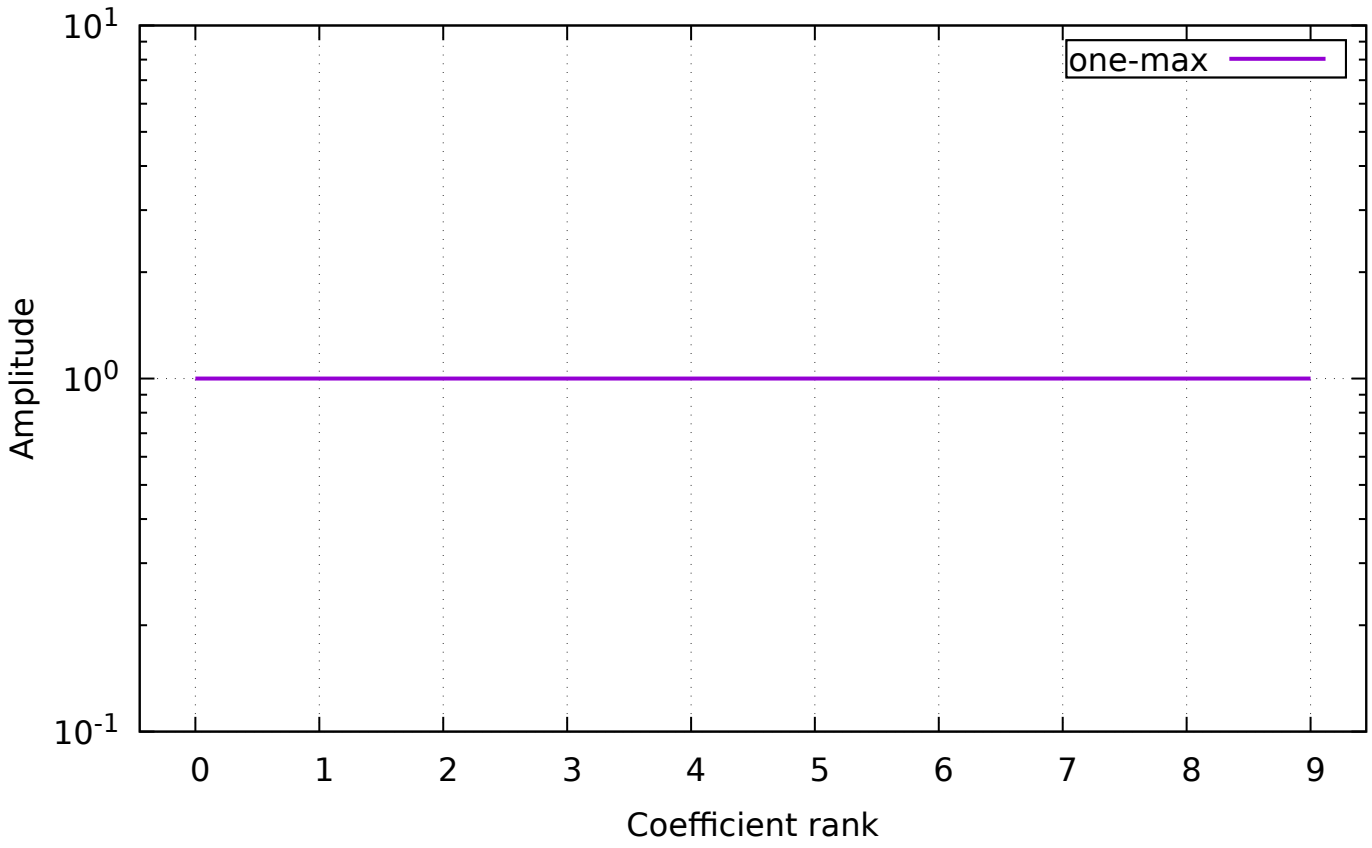
This document proposes to visualize Walsh (or Fourier) transforms of various functions defined on bit vectors (hypercube) of size $n = 10$. For each function, two graphics are displayed. In the first one, coefficients of the Walsh transform are sorted in decreasing order of amplitude and normalized relatively to the largest amplitude. The second graphics displays the energy (sum of square of coefficients) as a function of the Hamming weight of features. This can be thought of as a spectrum. Coefficients c such that $0 < |c/c_{\max}| < 10^{-15}$ have been filtered out as they mostly result from accumulated errors in floating point arithmetic.

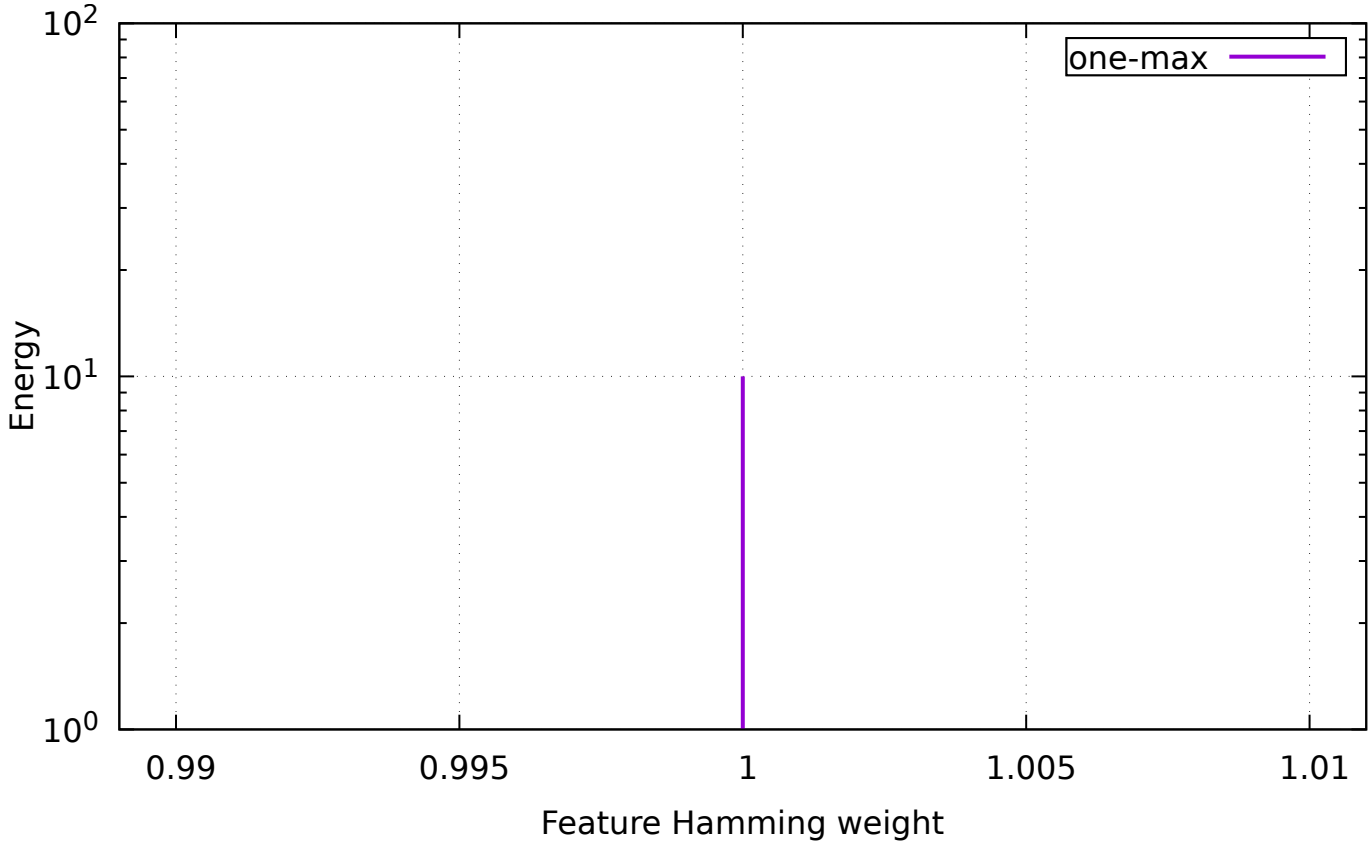
Contents

1 All functions

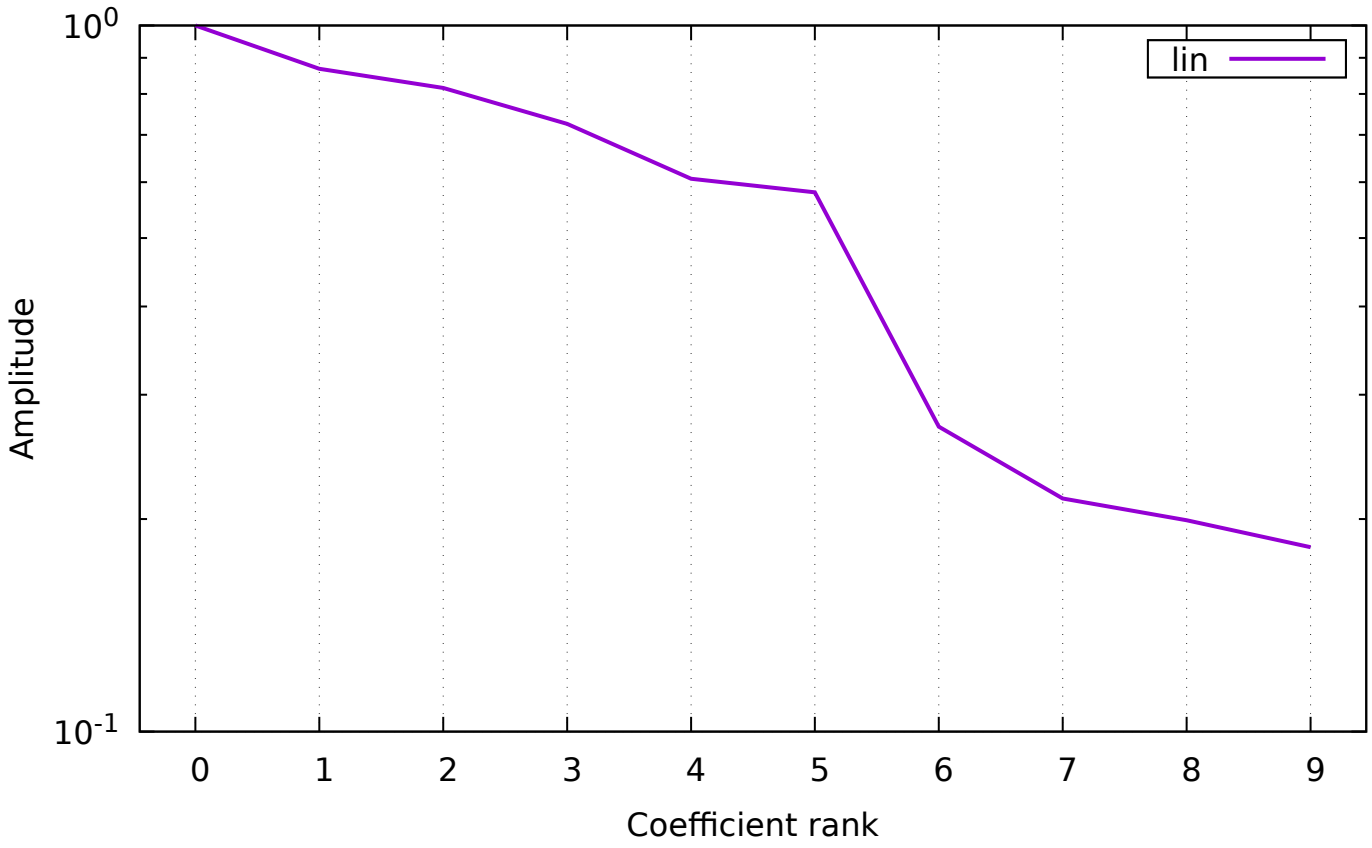


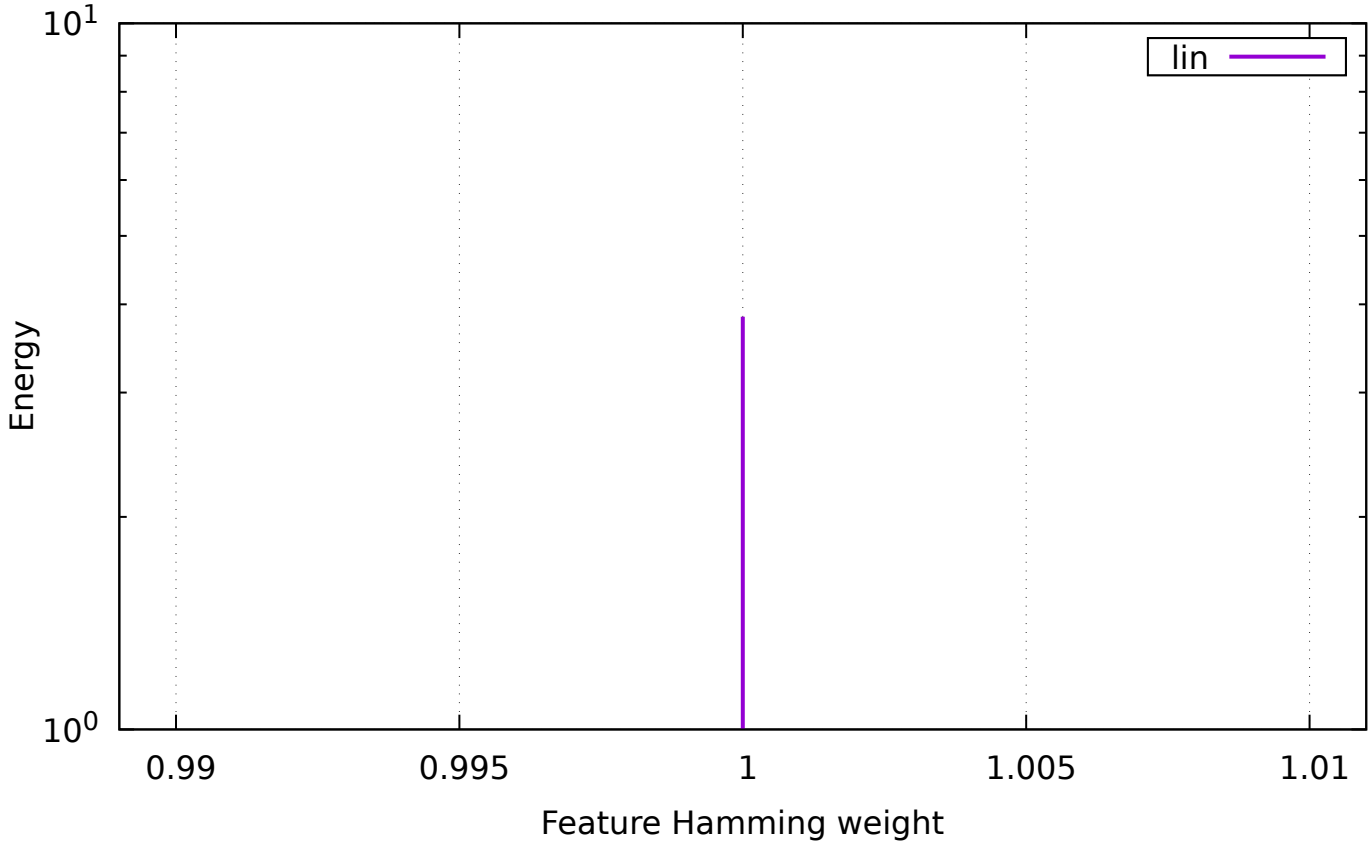
2 one-max


one-max
Amplitude
Coefficient rank
10^1
10^0
10^{-1}
0
1
2
3
4
5
6
7
8
9

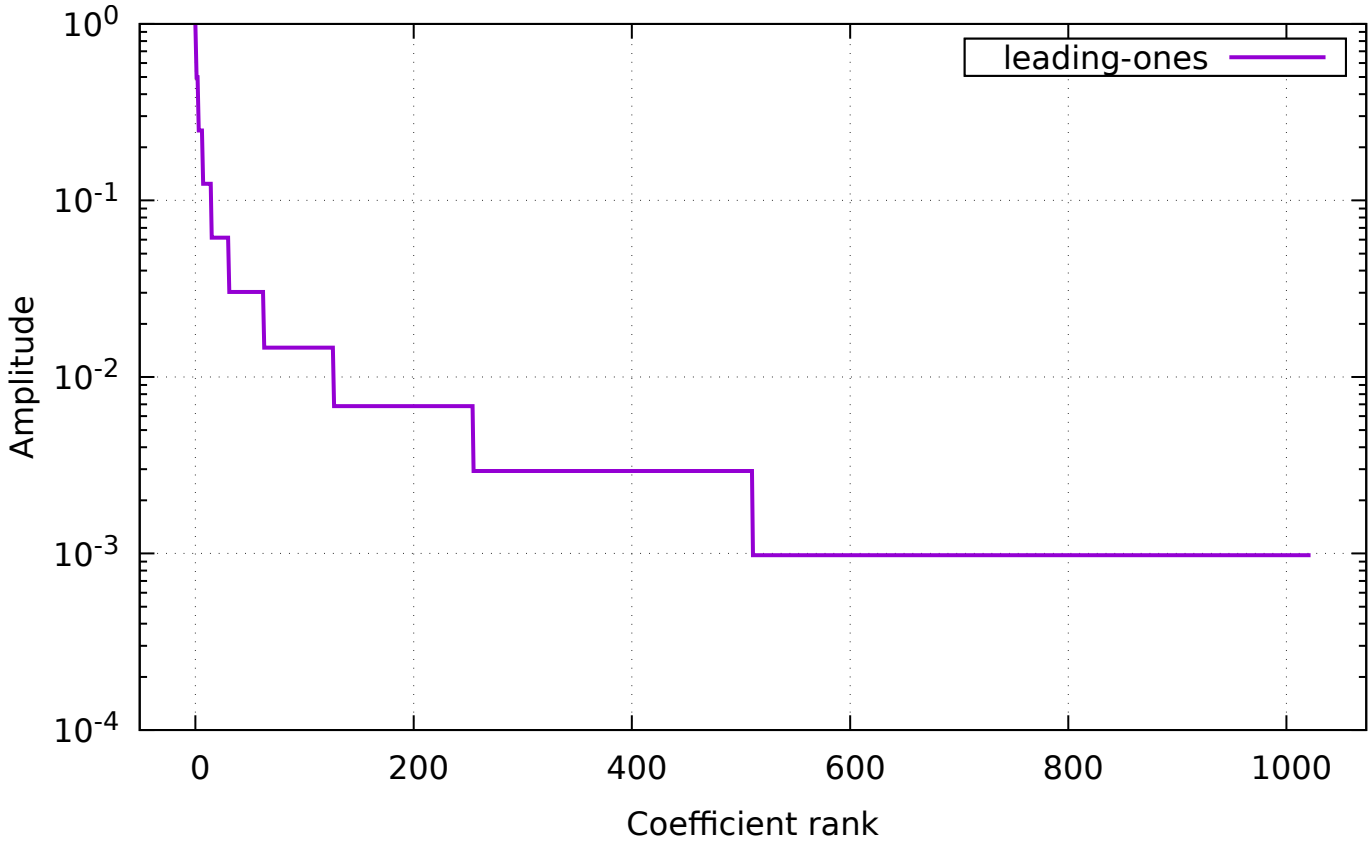

one-max
Energy
Feature Hamming weight
10^2
10^1
10^0
0.99
0.995
1
1.005
1.01

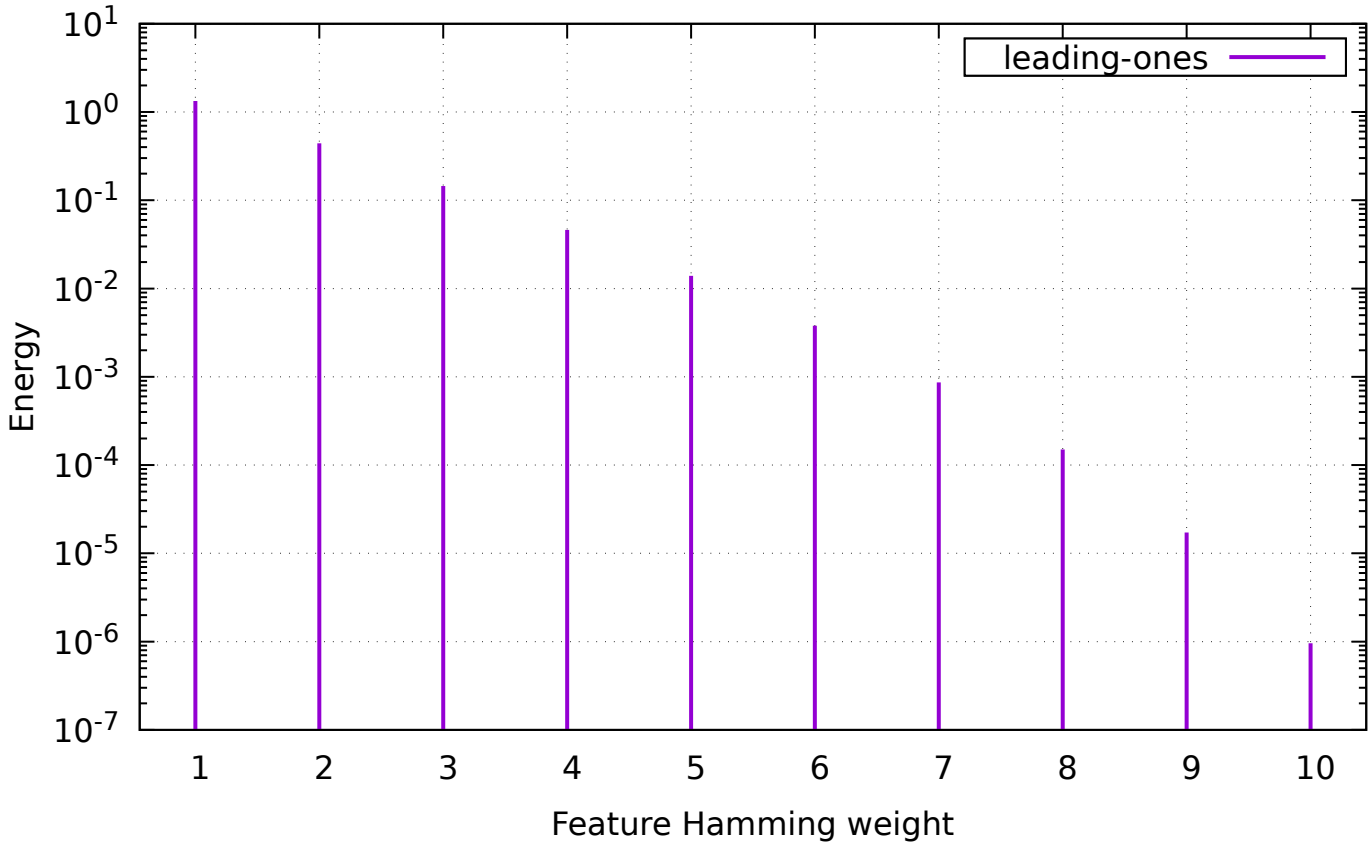
3 lin


lin
Amplitude
Coefficient rank
10^0
10^{-1}
0
1
2
3
4
5
6
7
8
9

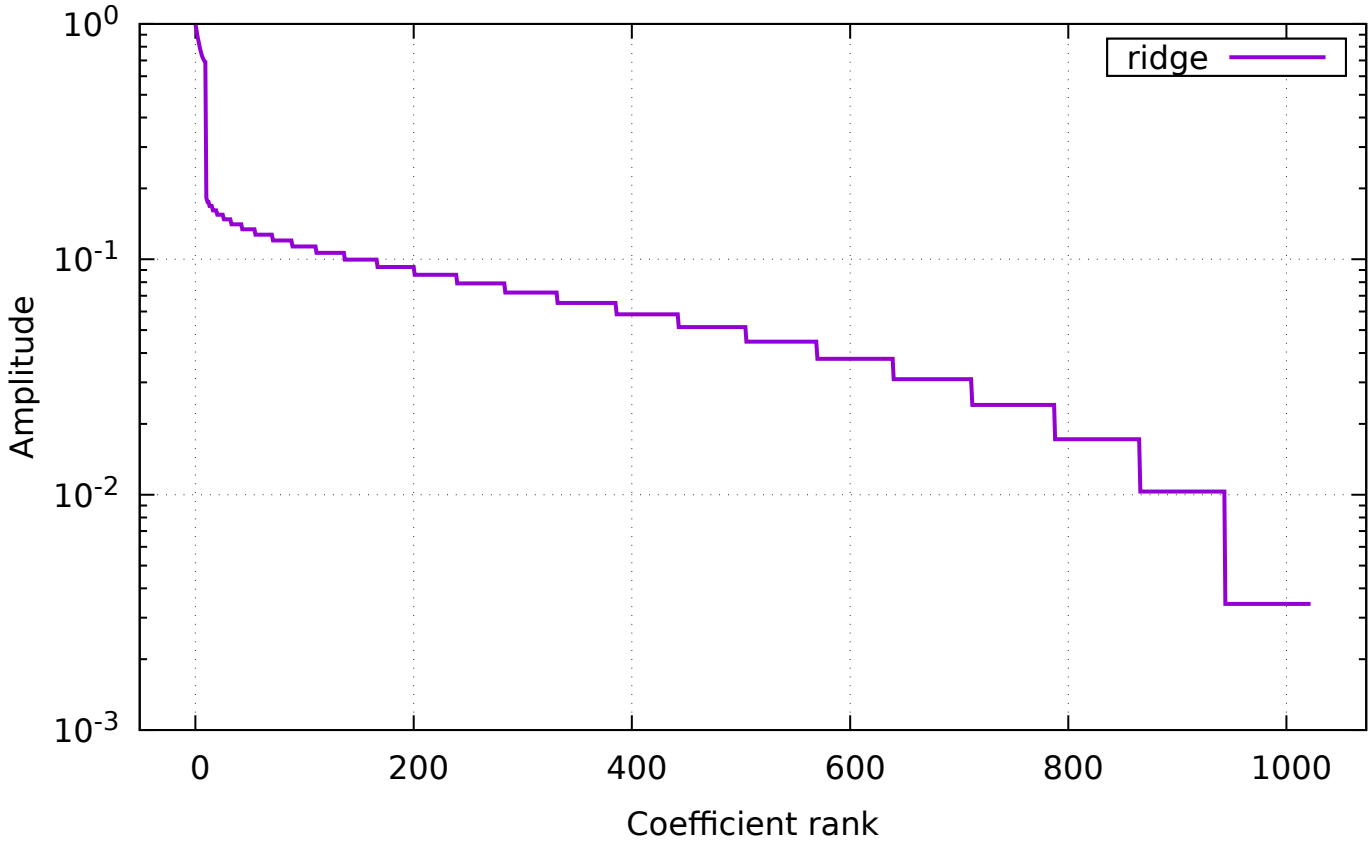

lin
Energy
Feature Hamming weight
10^1
10^0
0.99
0.995
1
1.005
1.01

4 leading-ones





5 ridge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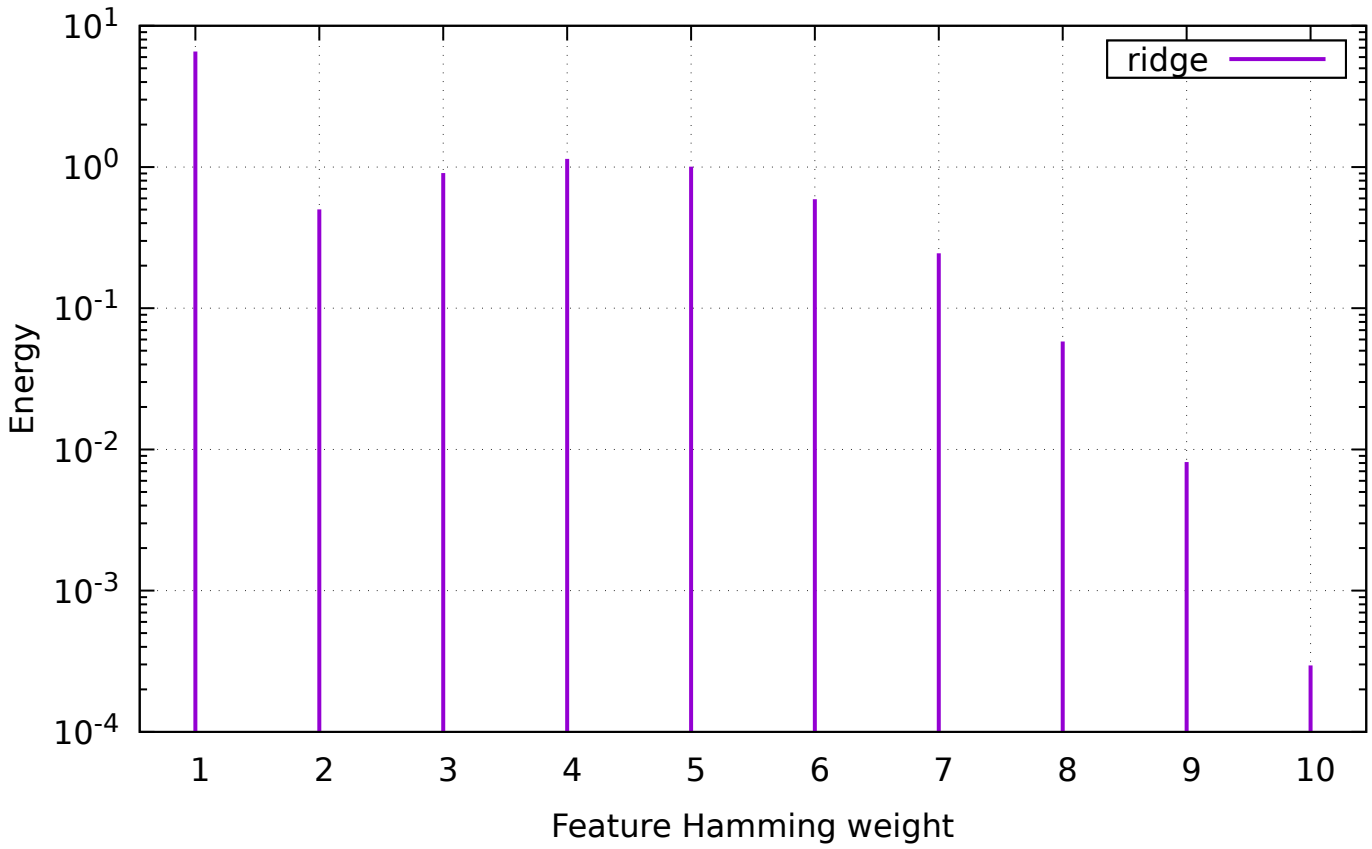
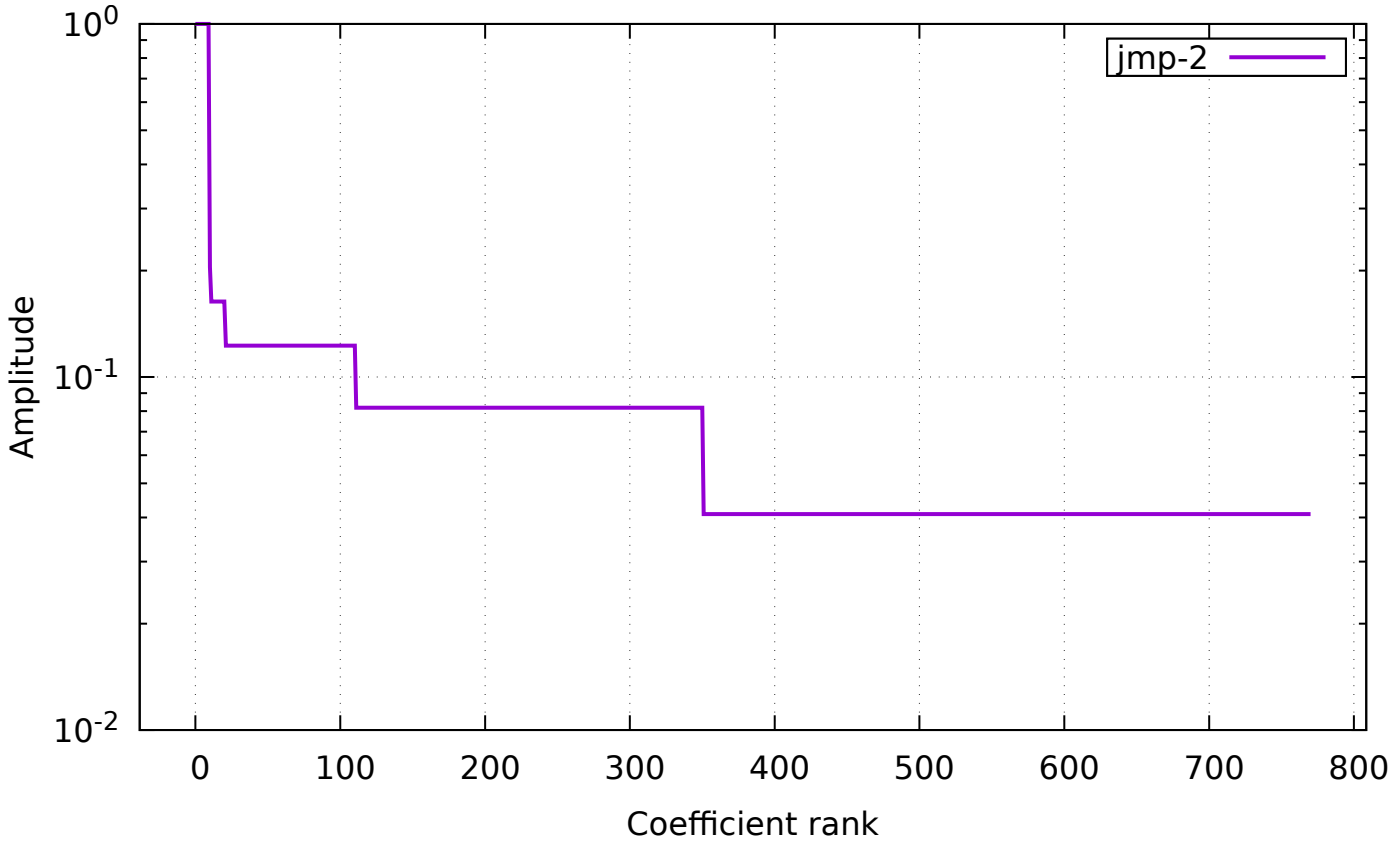
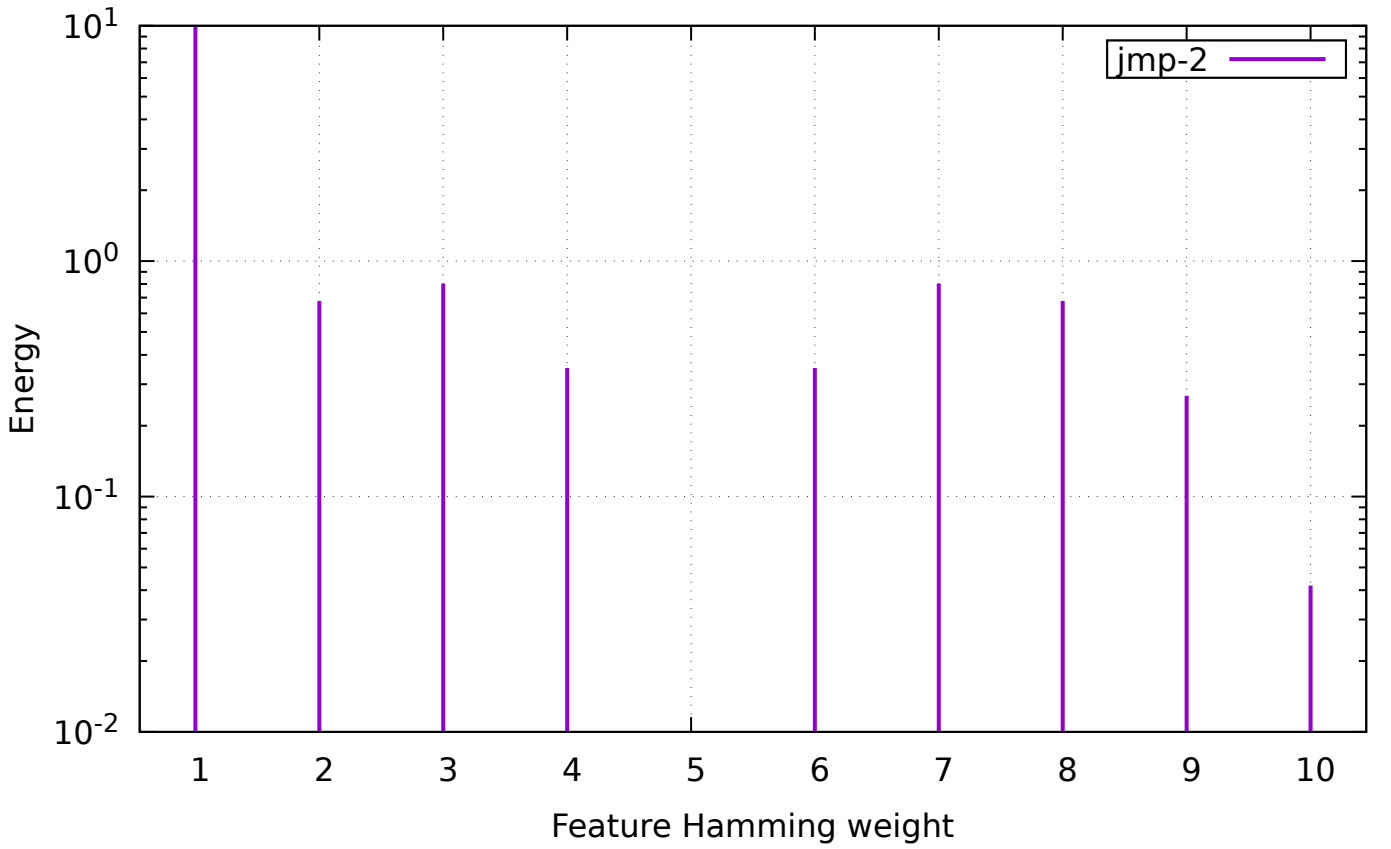
Amplitude
Coefficient rank
10^{0}
10^{-1}
10^{-2}
10^{-3}
0
200
400
600
800
1000

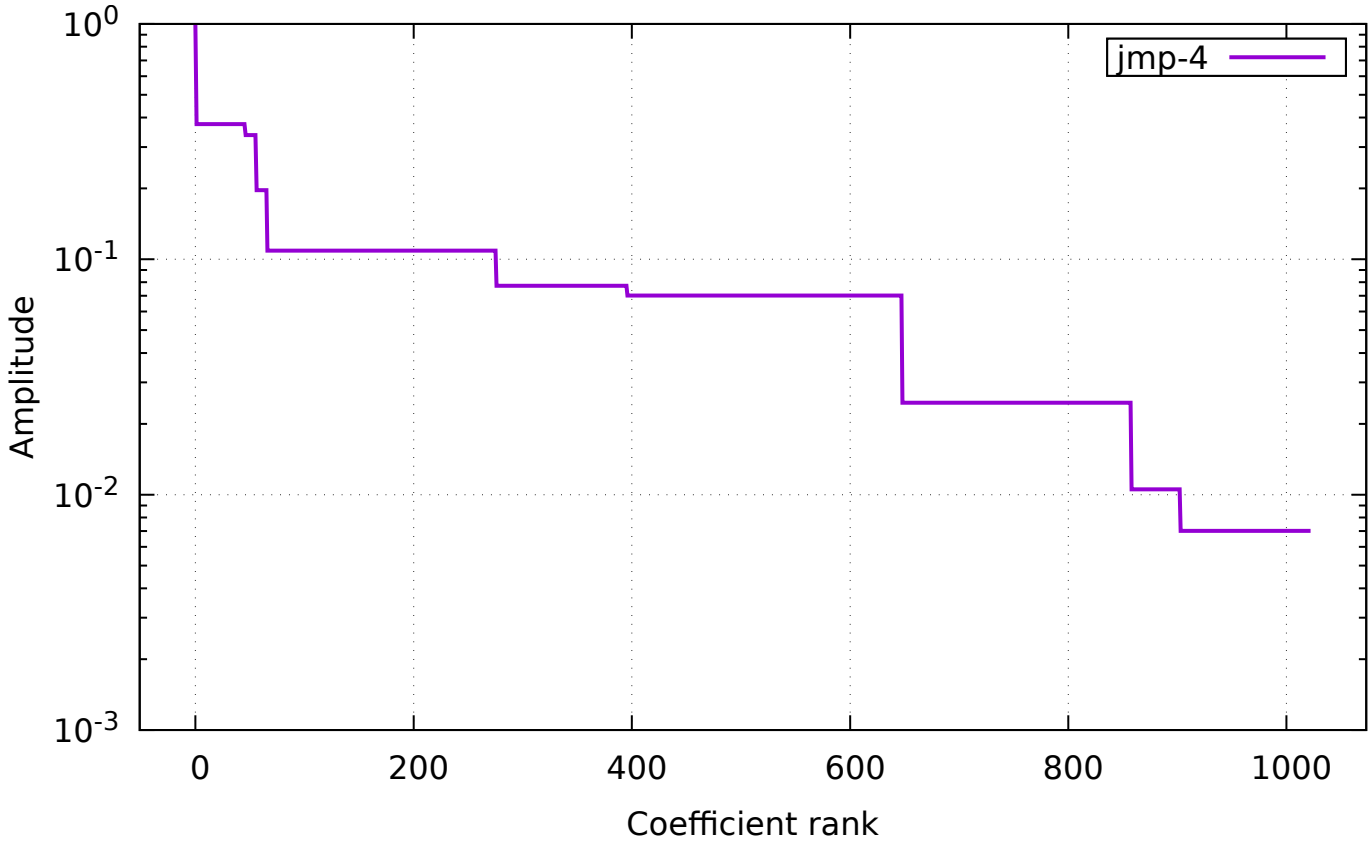

ridge
Energy
Feature Hamming weight
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
1
2
3
4
5
6
7
8
9
10

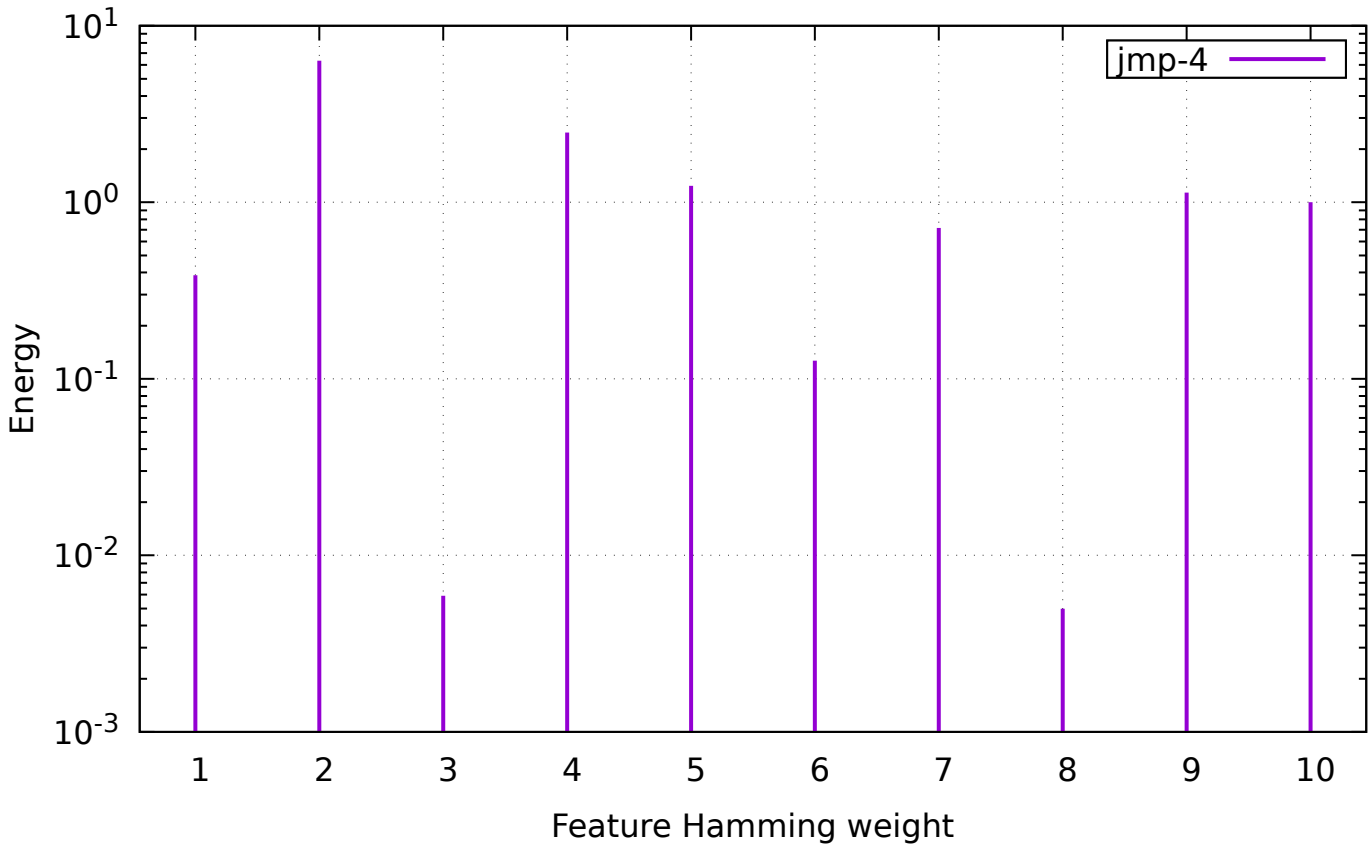
6 jmp-2


jmp-2
Amplitude
Coefficient rank
10^0
10^{-1}
10^{-2}
0
100
200
300
400
500
600
700
800

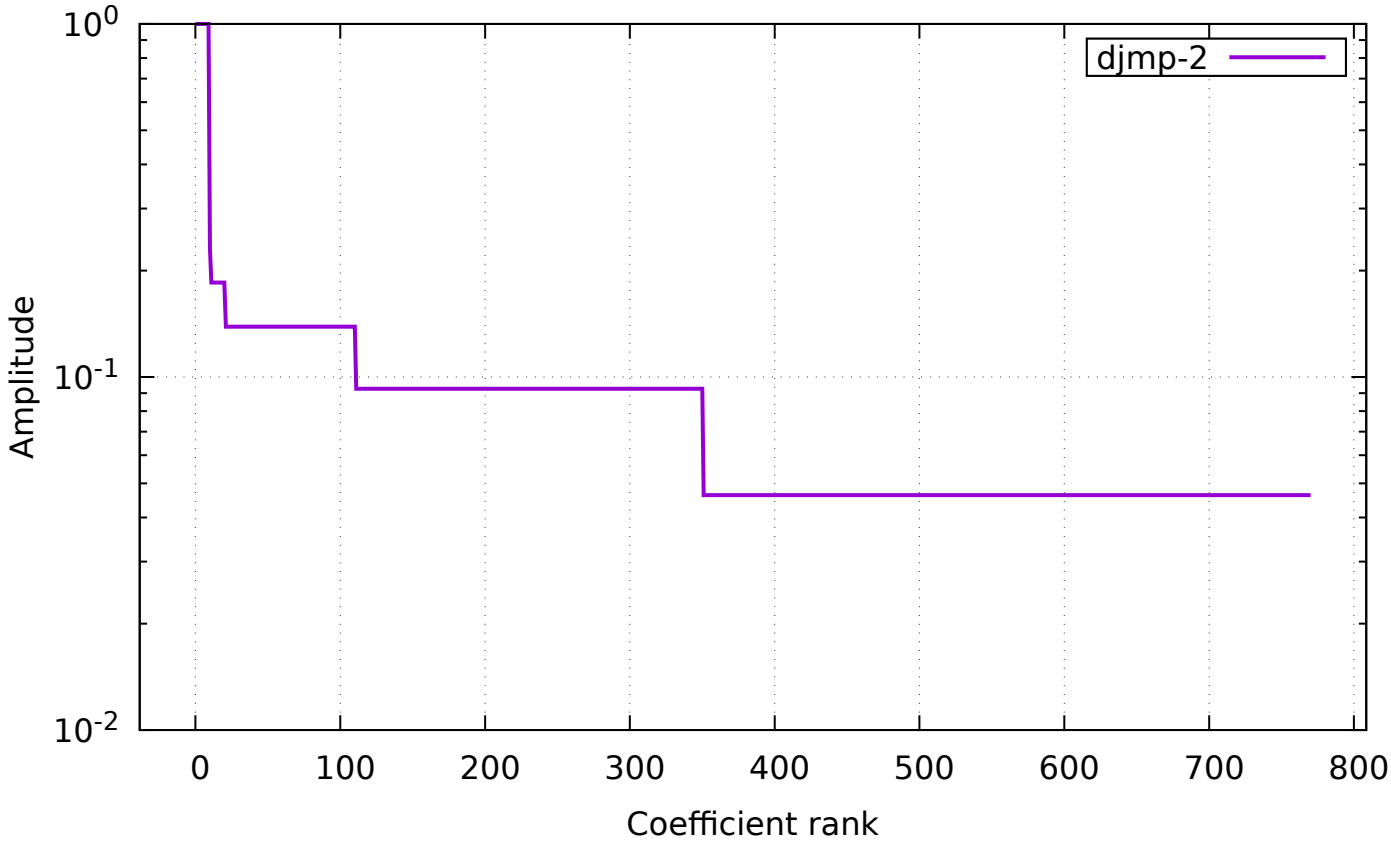

jmp-2
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
10^{-2}
1
2
3
4
5
6
7
8
9
10

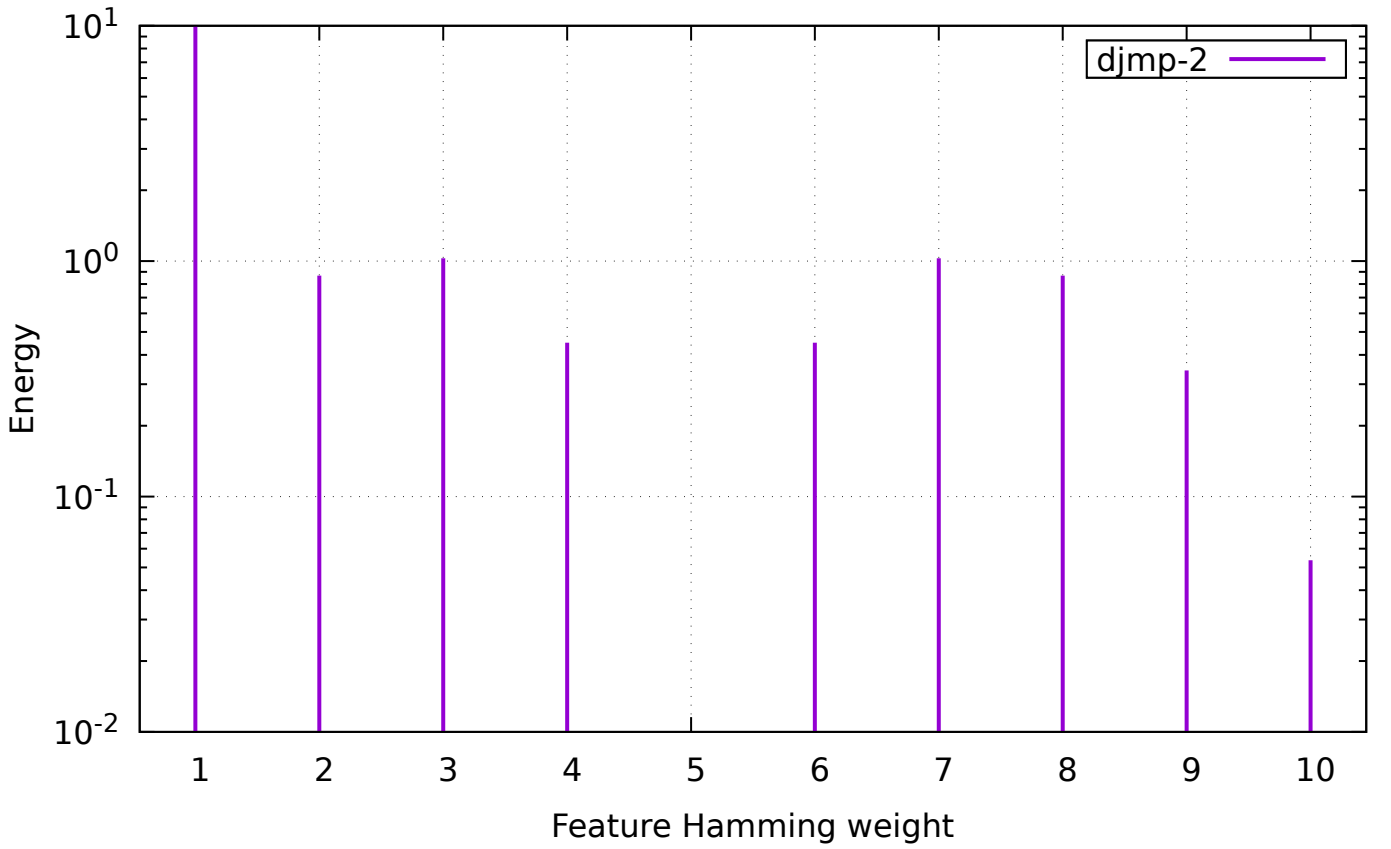
7 jmp-4


jmp-4
Amplitude
Coefficient rank
10^0
10^{-1}
10^{-2}
10^{-3}
0
200
400
600
800
1000

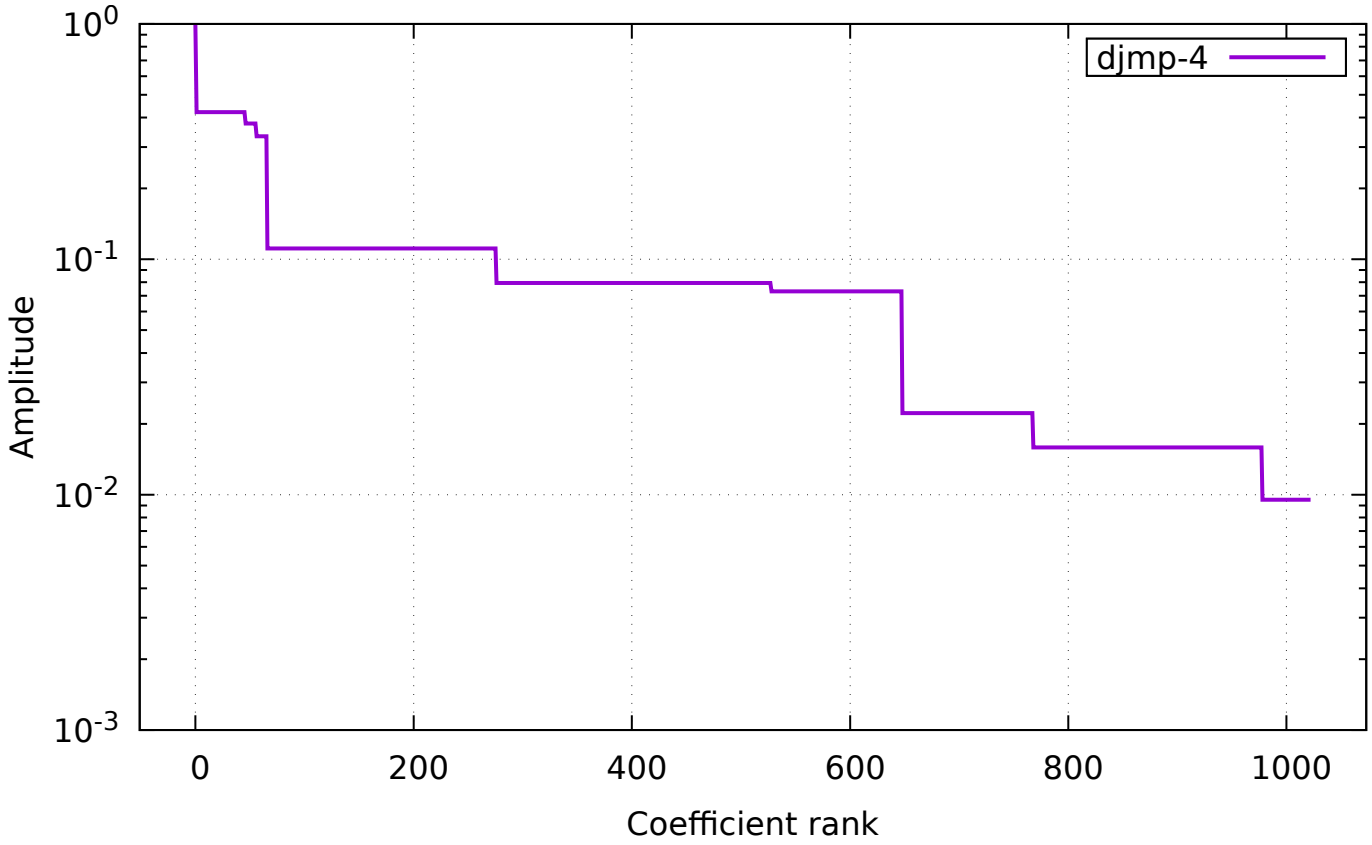

jmp-4
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
10^{-2}
10^{-3}
1
2
3
4
5
6
7
8
9
10

8 djmp-2


djmp-2
Amplitude
Coefficient rank
10^0
10^{-1}
10^{-2}
0
100
200
300
400
500
600
700
800


djmp-2
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
10^{-2}
1
2
3
4
5
6
7
8
9
10

9 djmp-4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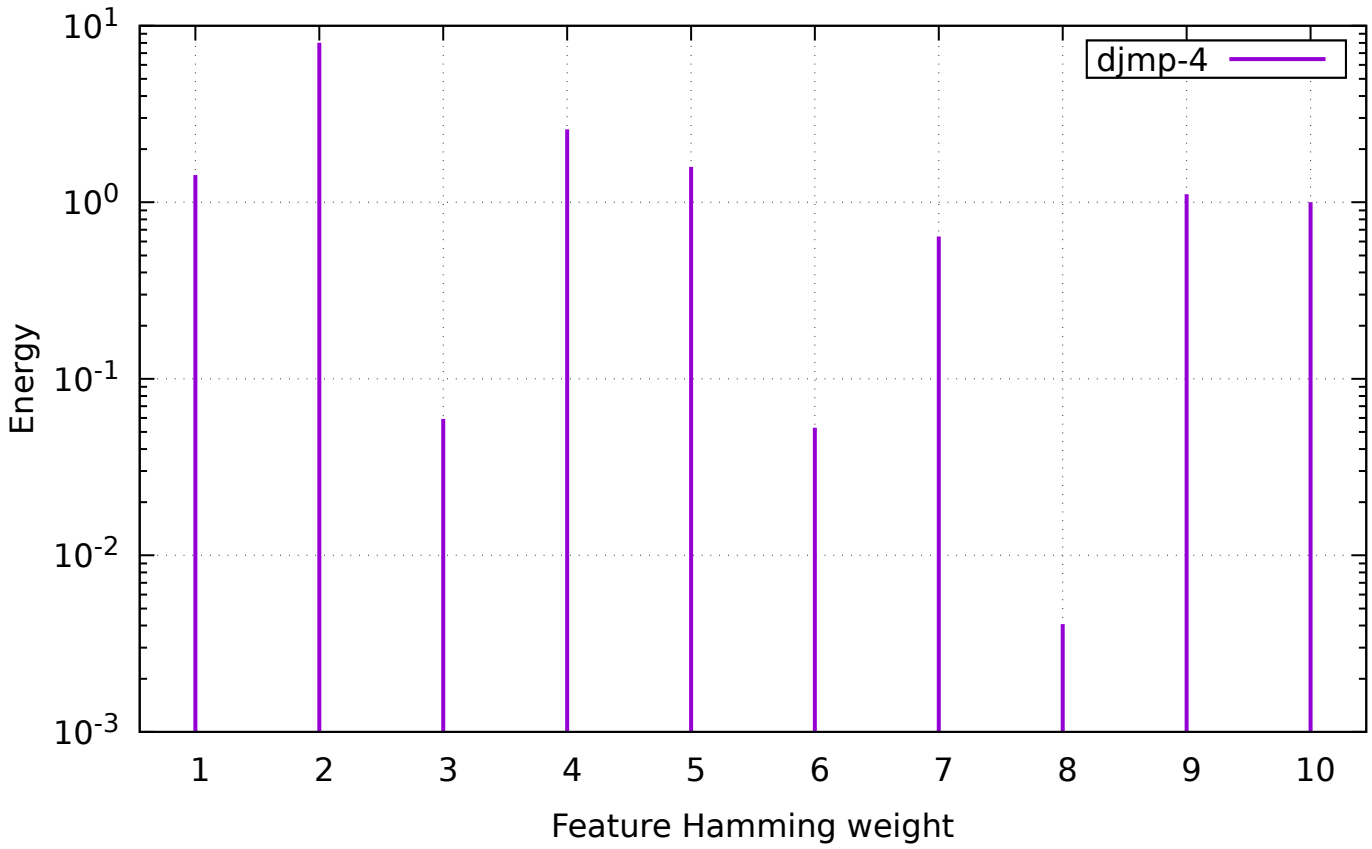
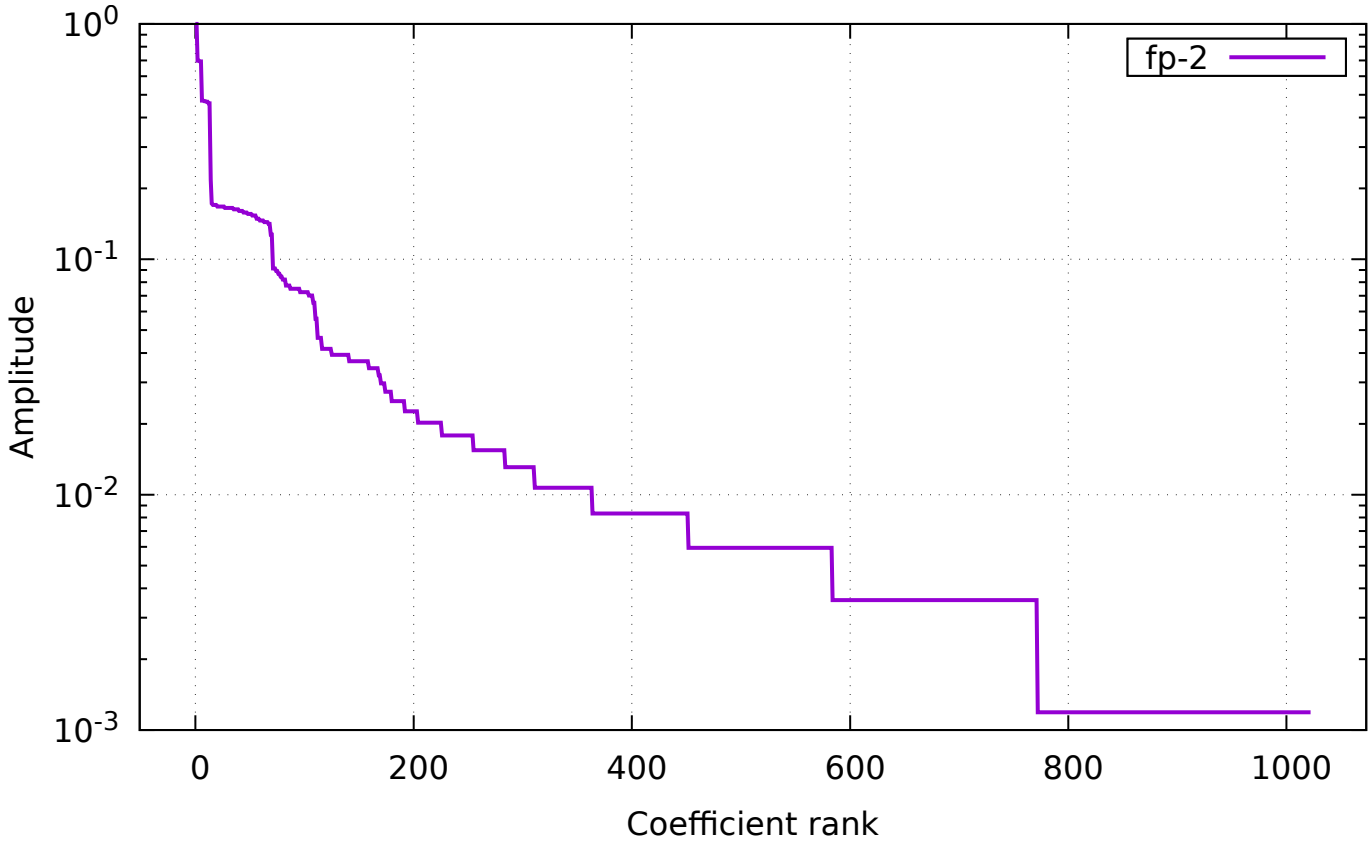
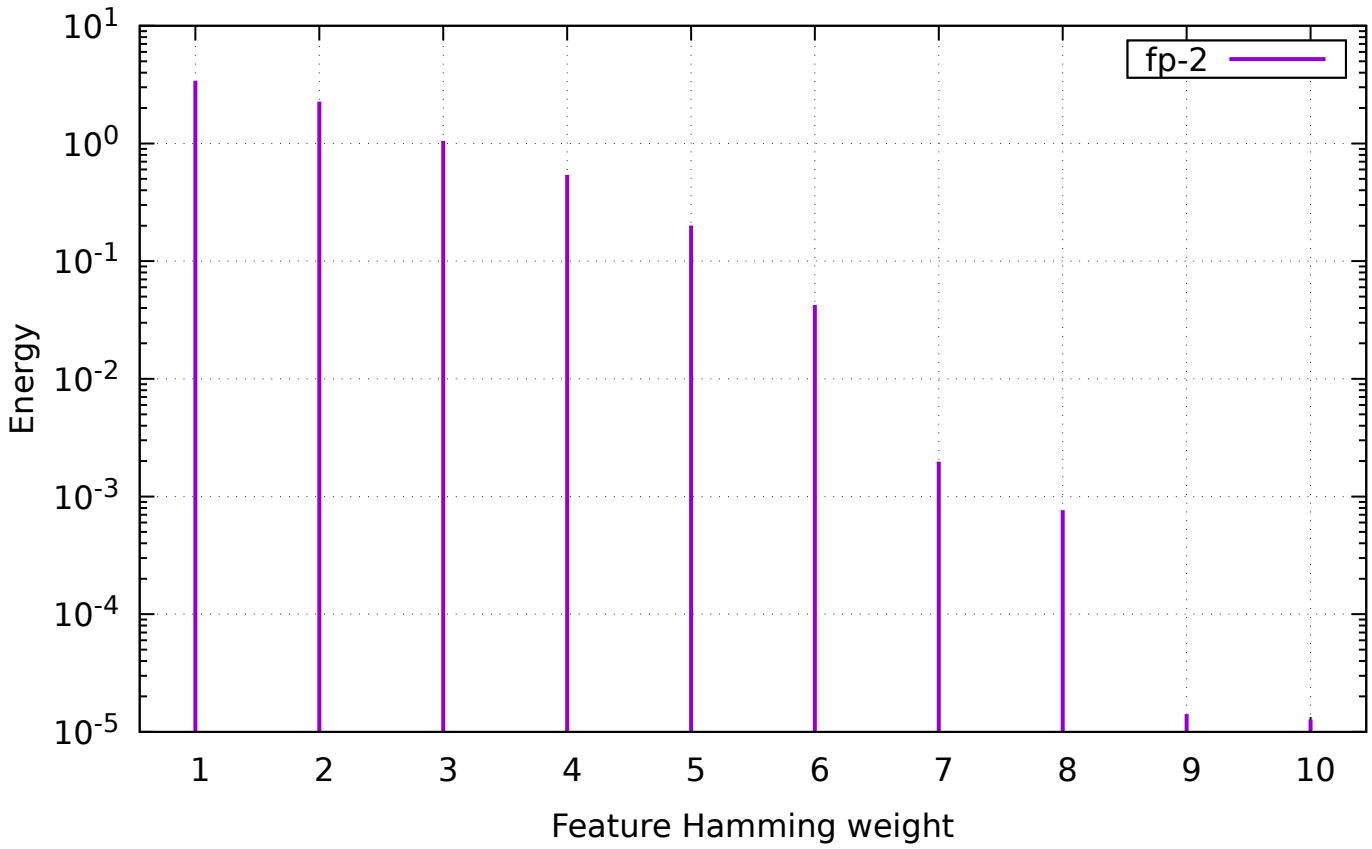
Coefficient rank
10^0
10^{-1}
10^{-2}
10^{-3}
0
200
400
600
800
1000


djmp-4
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
10^{-2}
10^{-3}
1
2
3
4
5
6
7
8
9
10

10 fp-2


fp-2
Amplitude
Coefficient rank
10^{0}
10^{-1}
10^{-2}
10^{-3}
0
200
400
600
800
1000


fp-2
Energy
Feature Hamming weight
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
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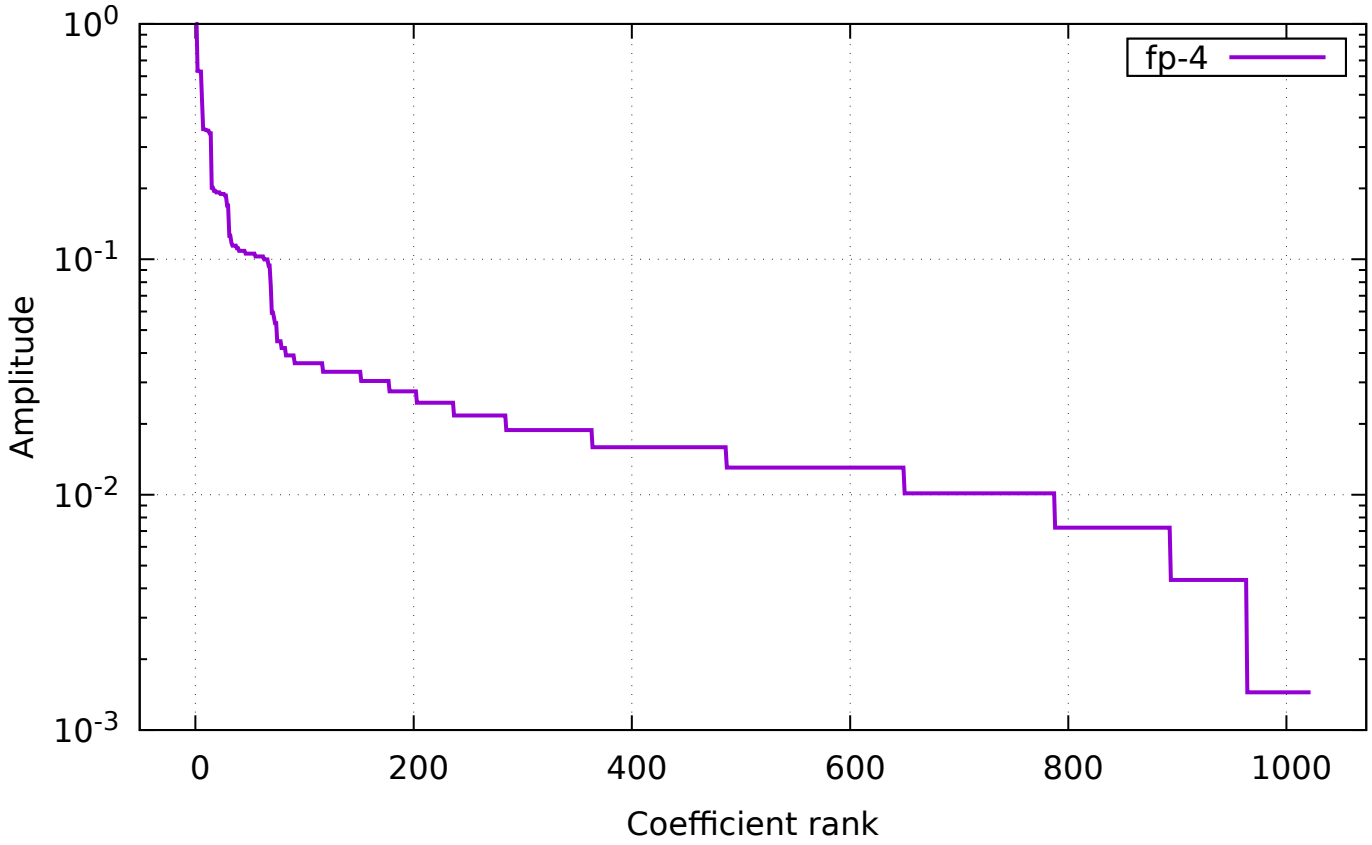
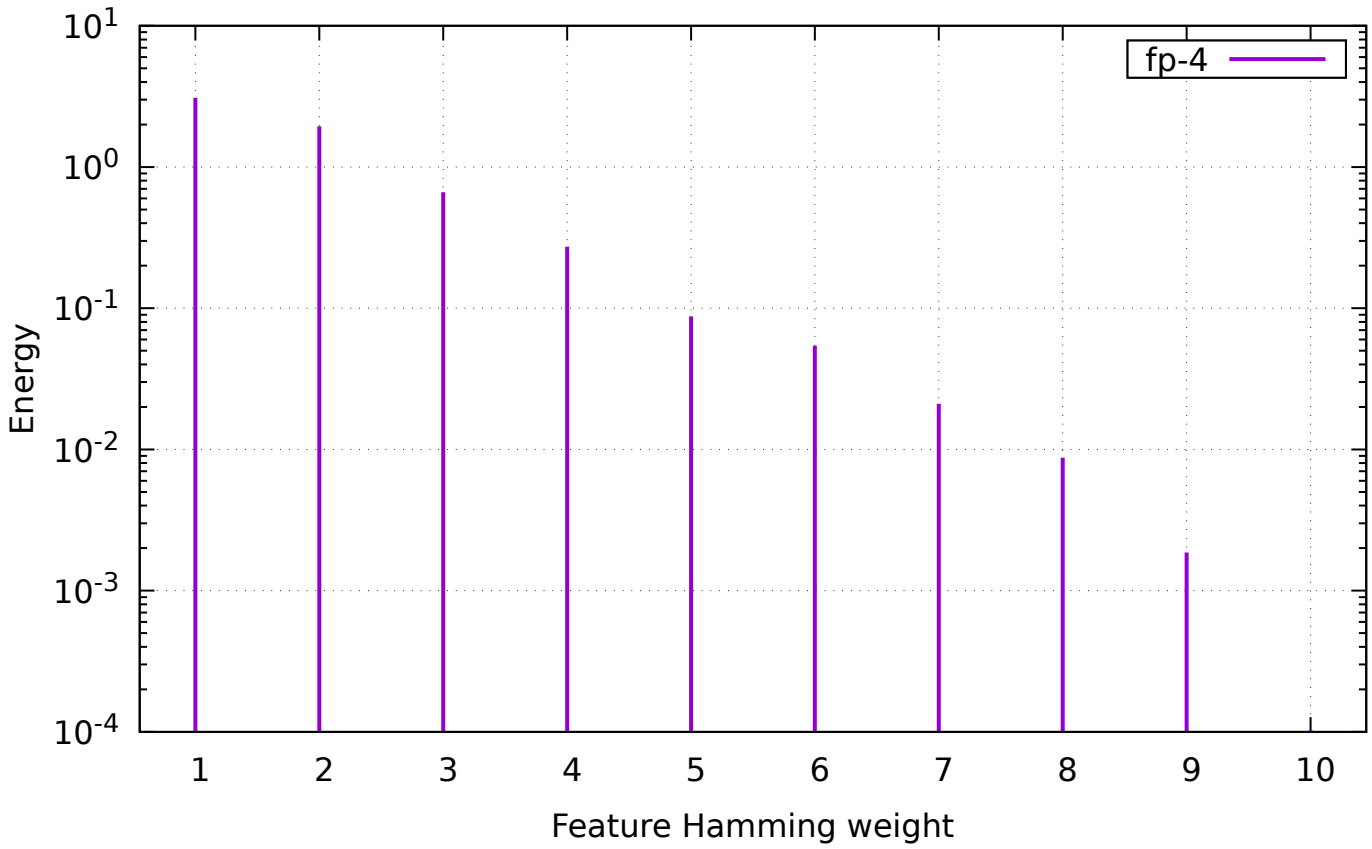
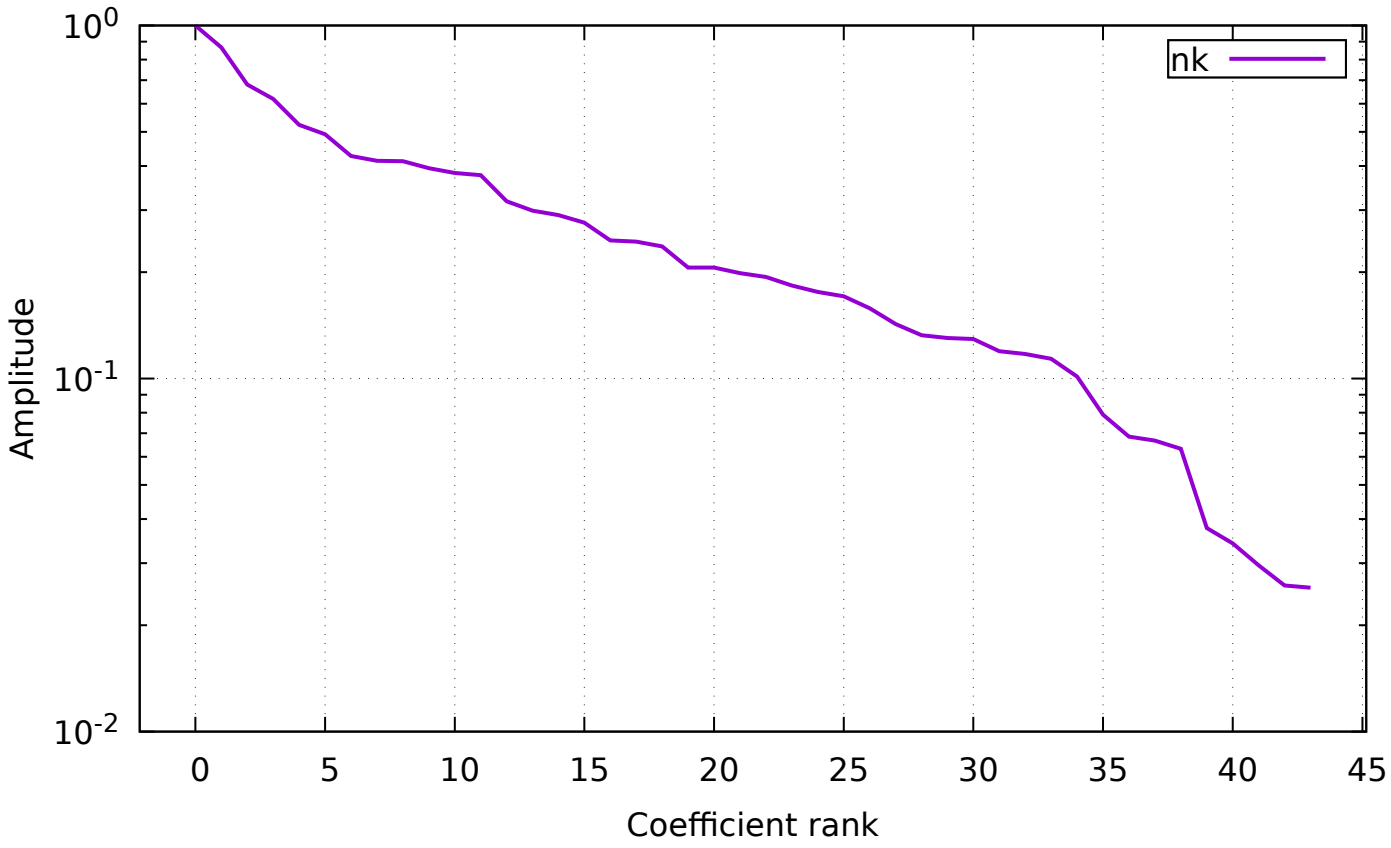
3
4
5
6
7
8
9
10

11 fp-4


fp-4
Amplitude
Coefficient rank
10^0
10^{-1}
10^{-2}
10^{-3}
0
200
400
600
800
1000


fp-4
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
10^{-2}
10^{-3}
10^{-4}
1
2
3
4
5
6
7
8
9
10


nk
Amplitude
Coefficient rank
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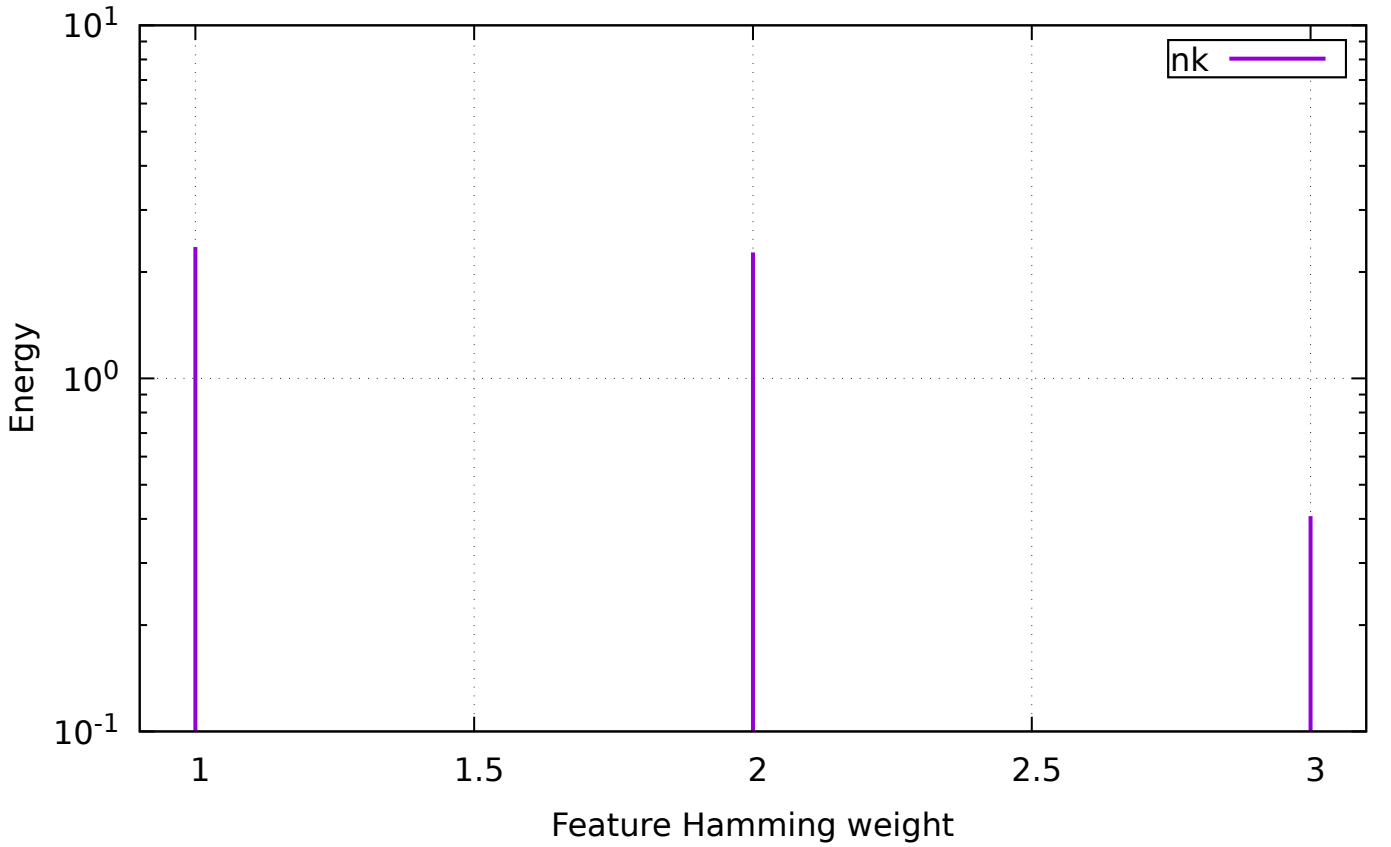
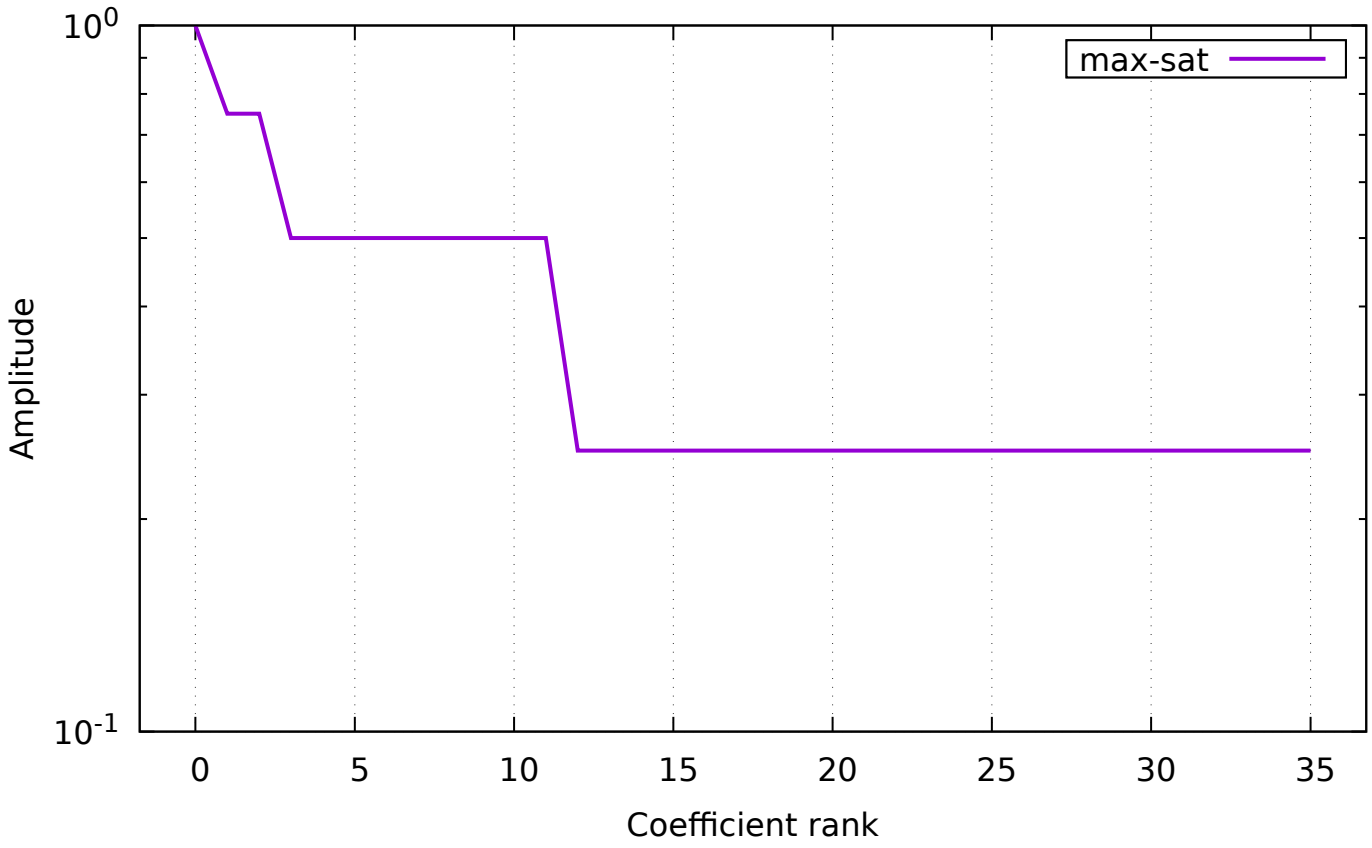
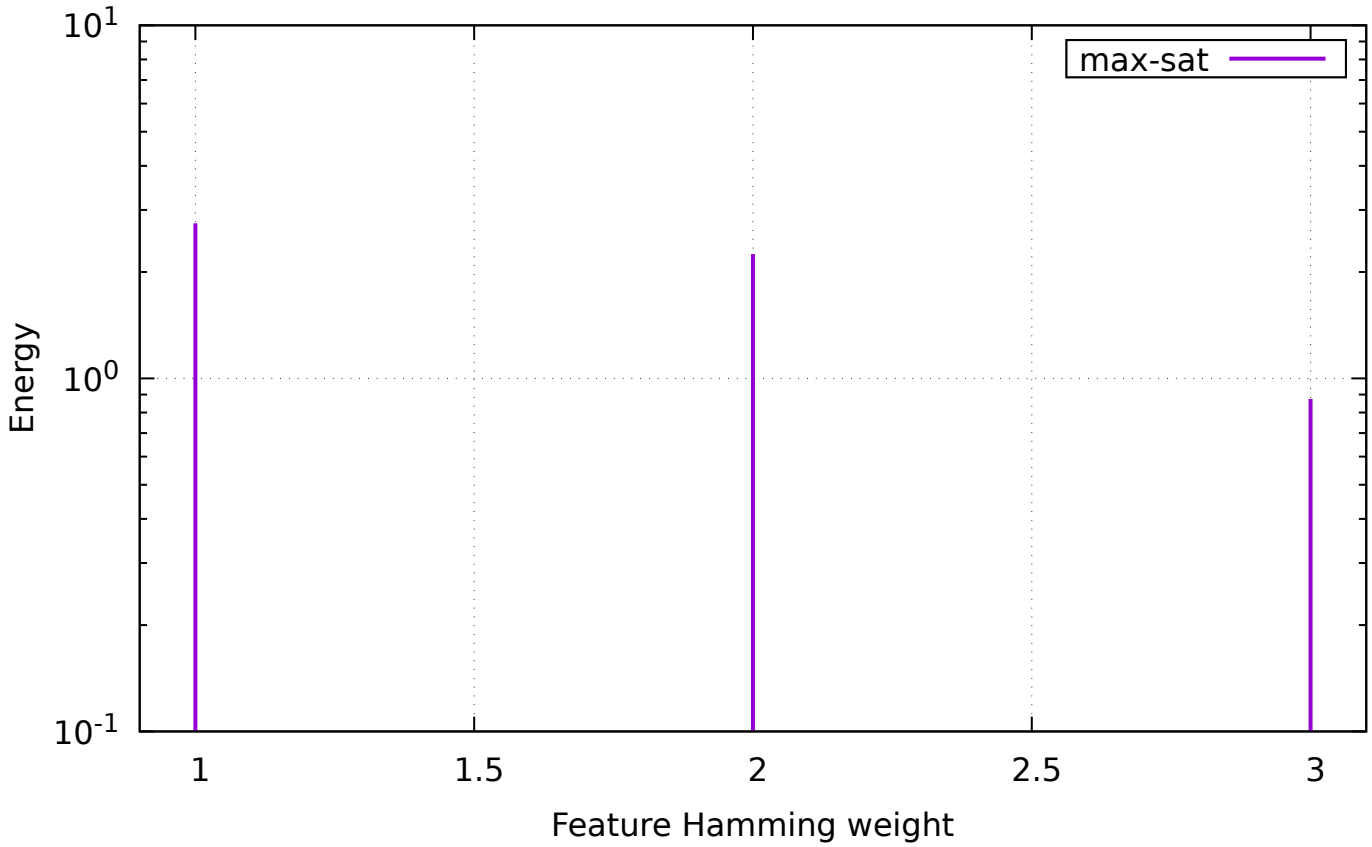
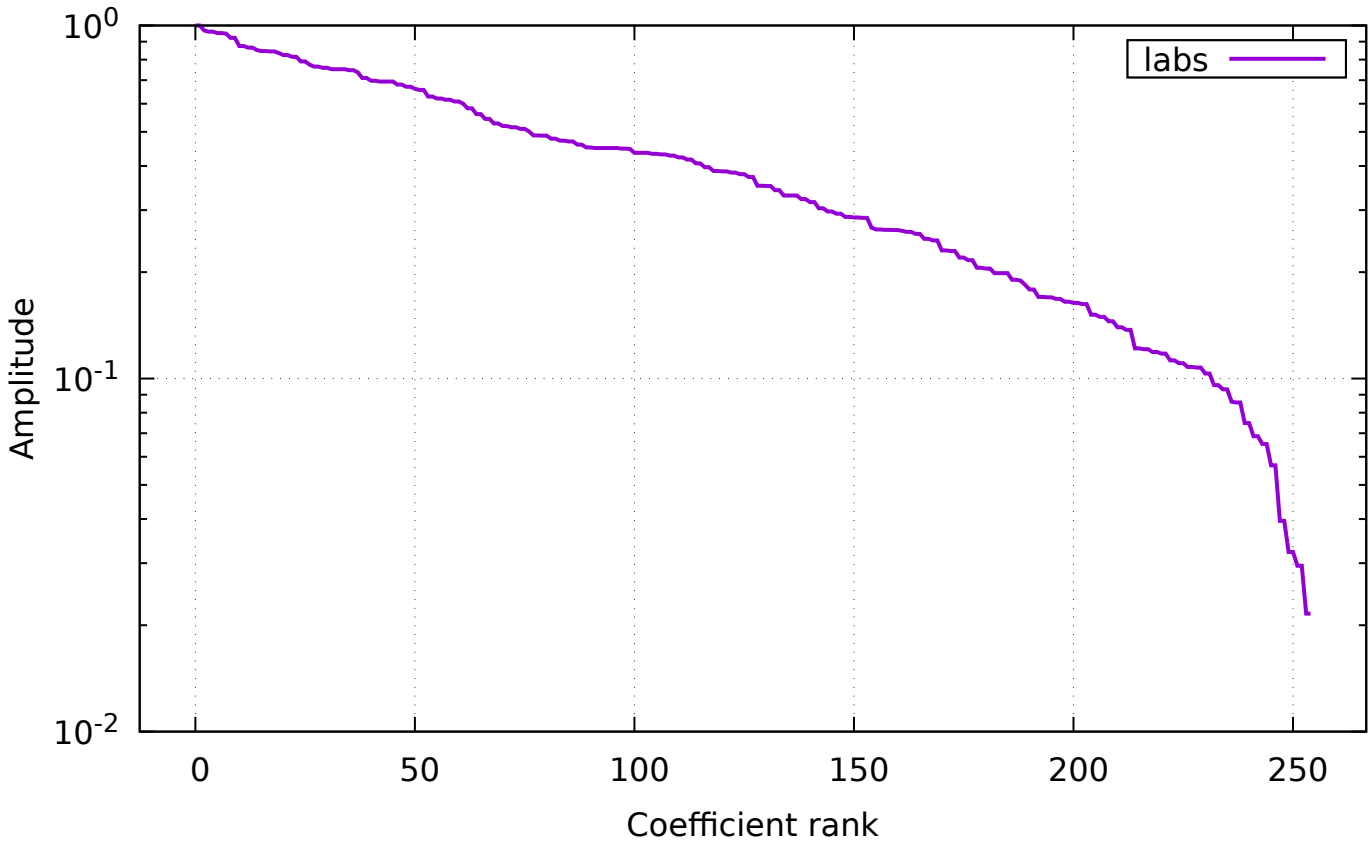
10^{-1}
10^{-2}
0
5
10
15
20
25
30
35
40
45


nk
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
1
1.5
2
2.5
3

13 max-sat


max-sat
Amplitude
Coefficient rank
10^0
10^{-1}
0
5
10
15
20
25
30
35


max-sat
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
1
1.5
2
2.5
3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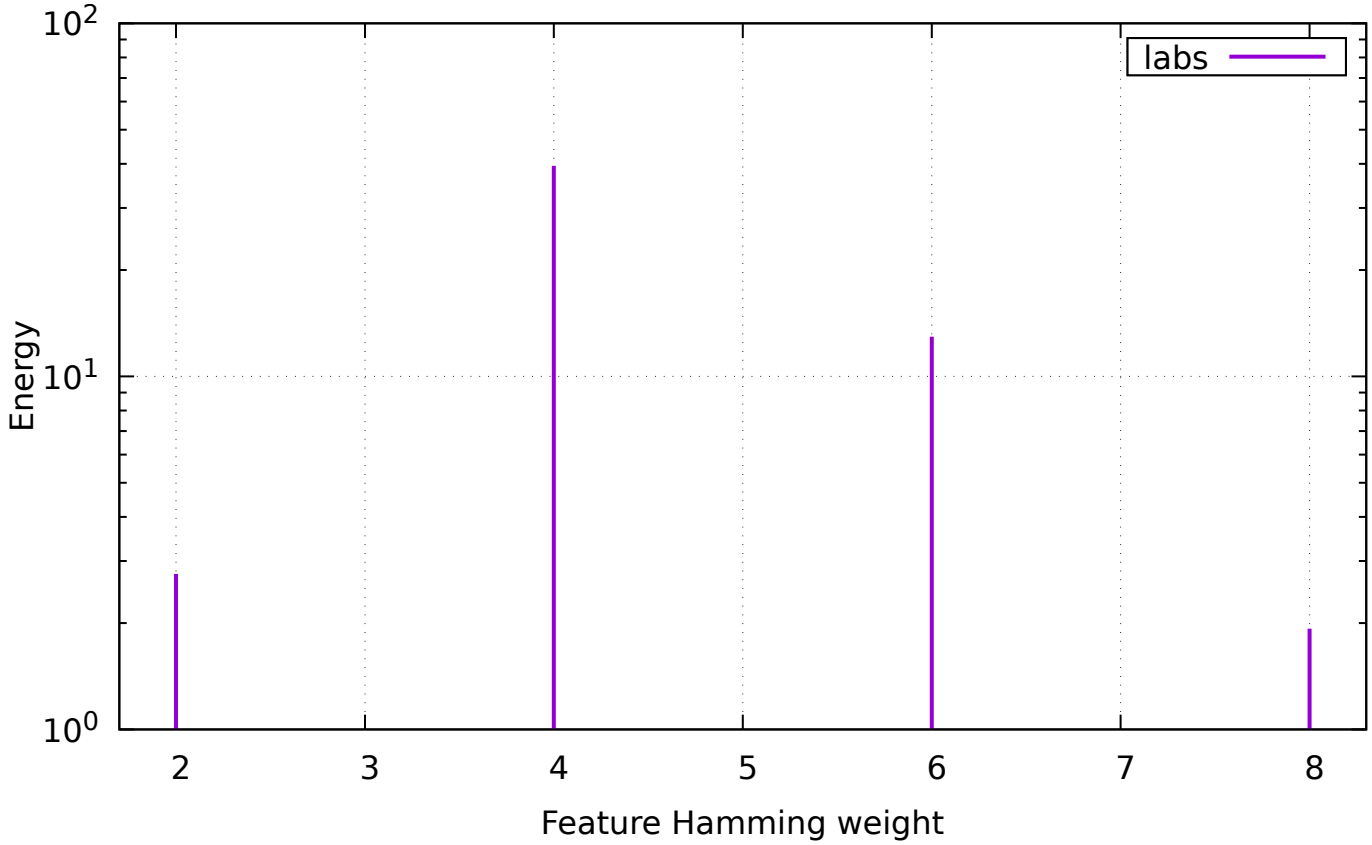
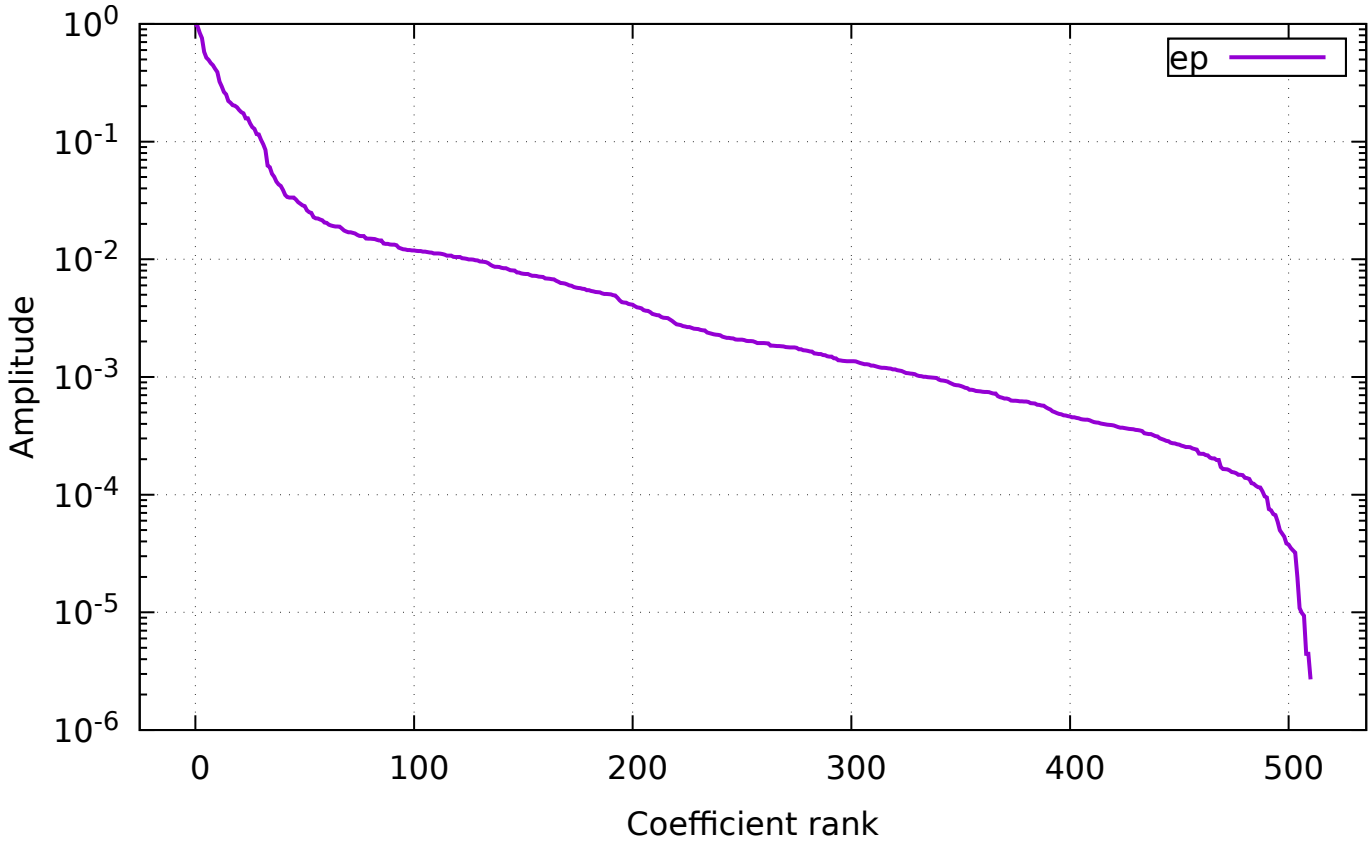
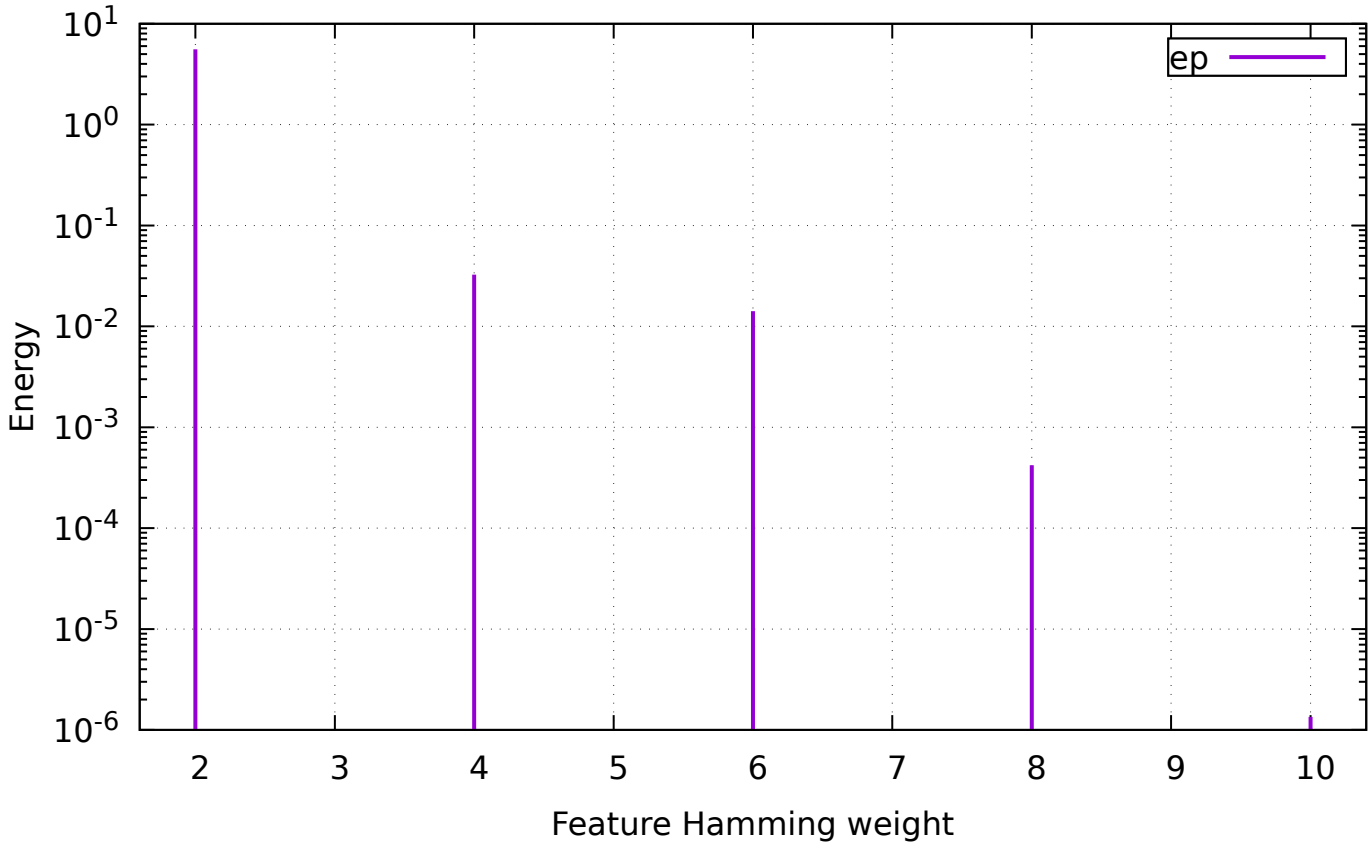
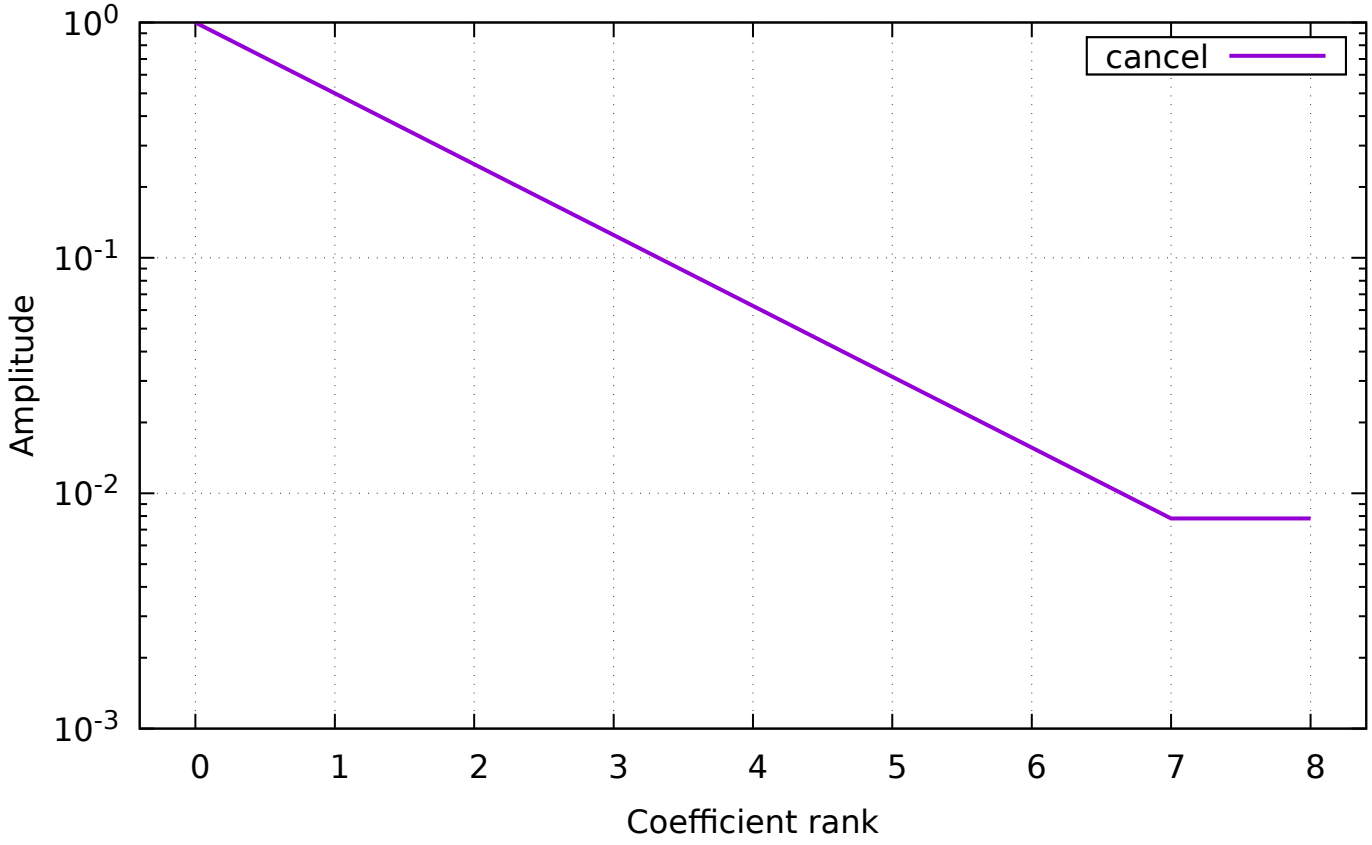
Amplitude
Coefficient rank
10^0
10^{-1}
10^{-2}
0
50
100
150
200
250


labs
Energy
Feature Hamming weight
10^2
10^1
10^0
2
3
4
5
6
7
8

15 ep


ep
Amplitude
Coefficient rank
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
10^{-6}
0
100
200
300
400
500


ep
Energy
Feature Hamming weight
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
10^{-6}
2
3
4
5
6
7
8
9
10


cancel
Amplitude
Coefficient rank
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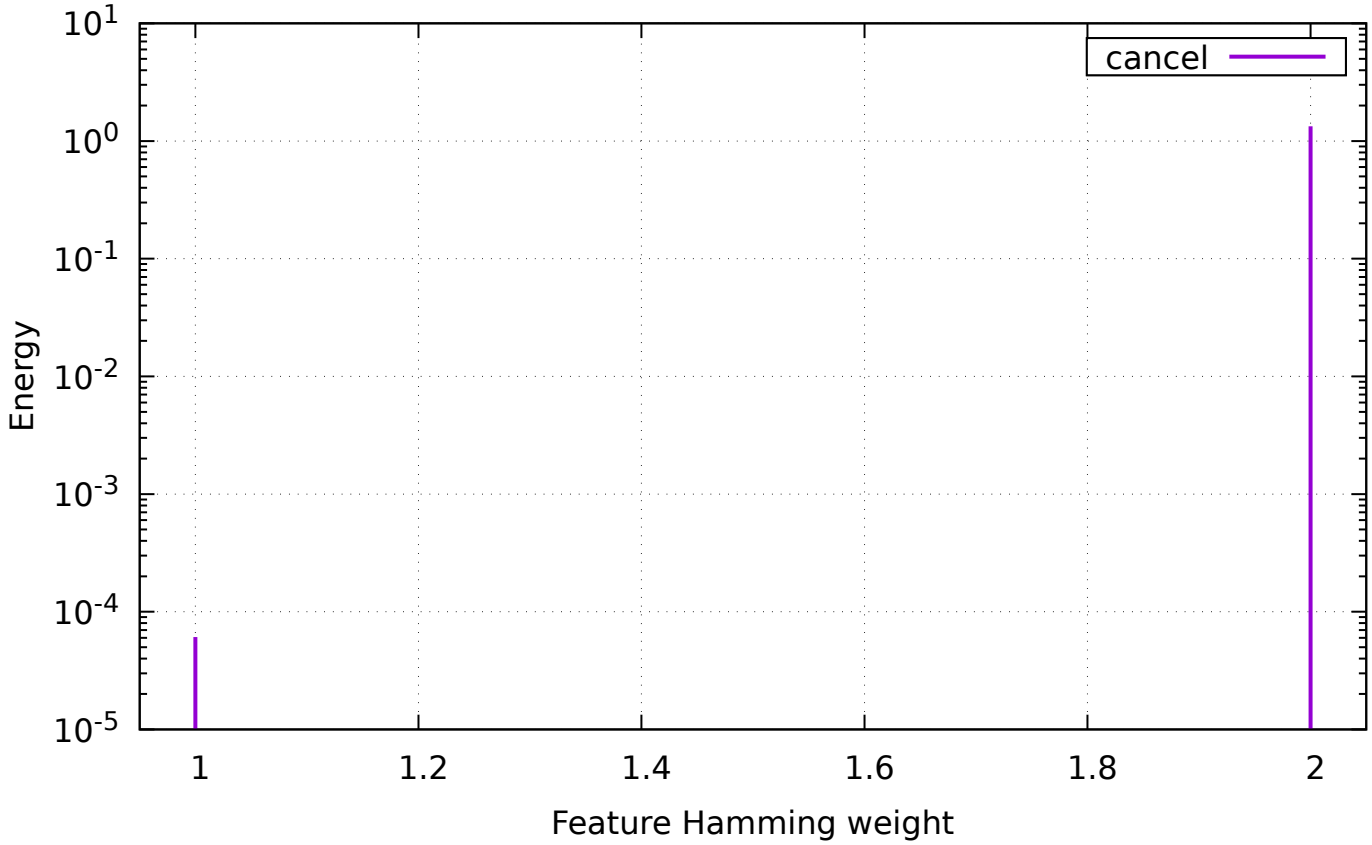
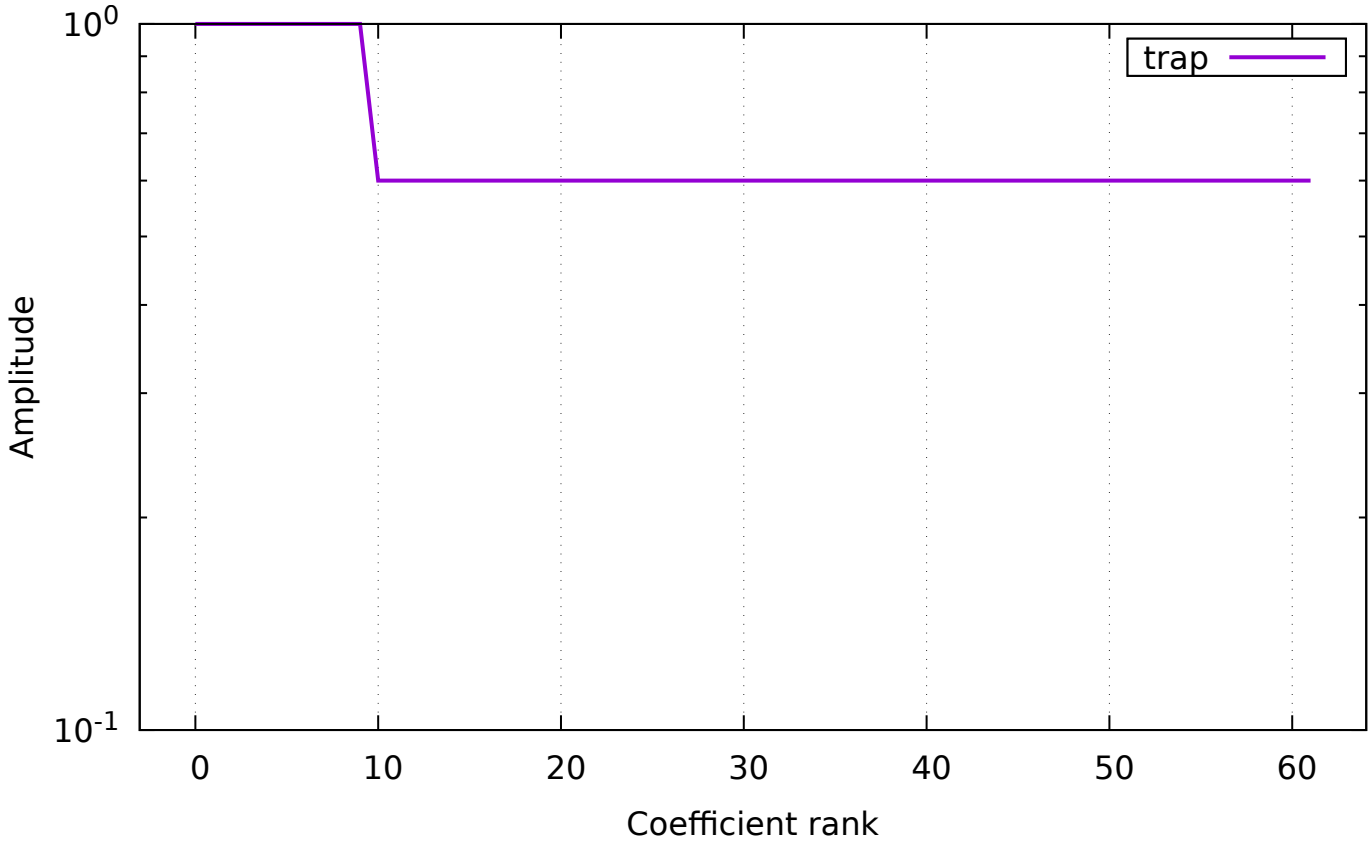
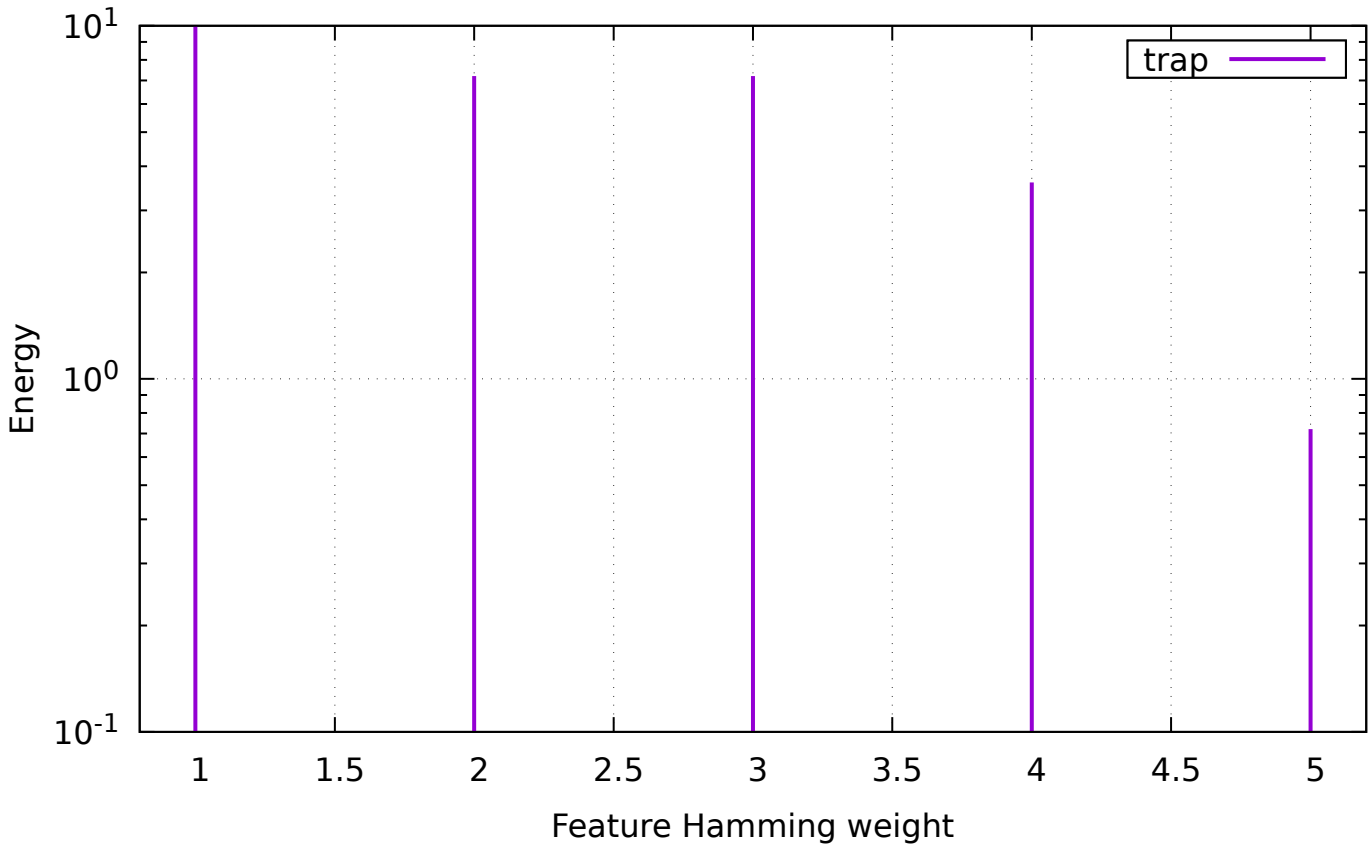
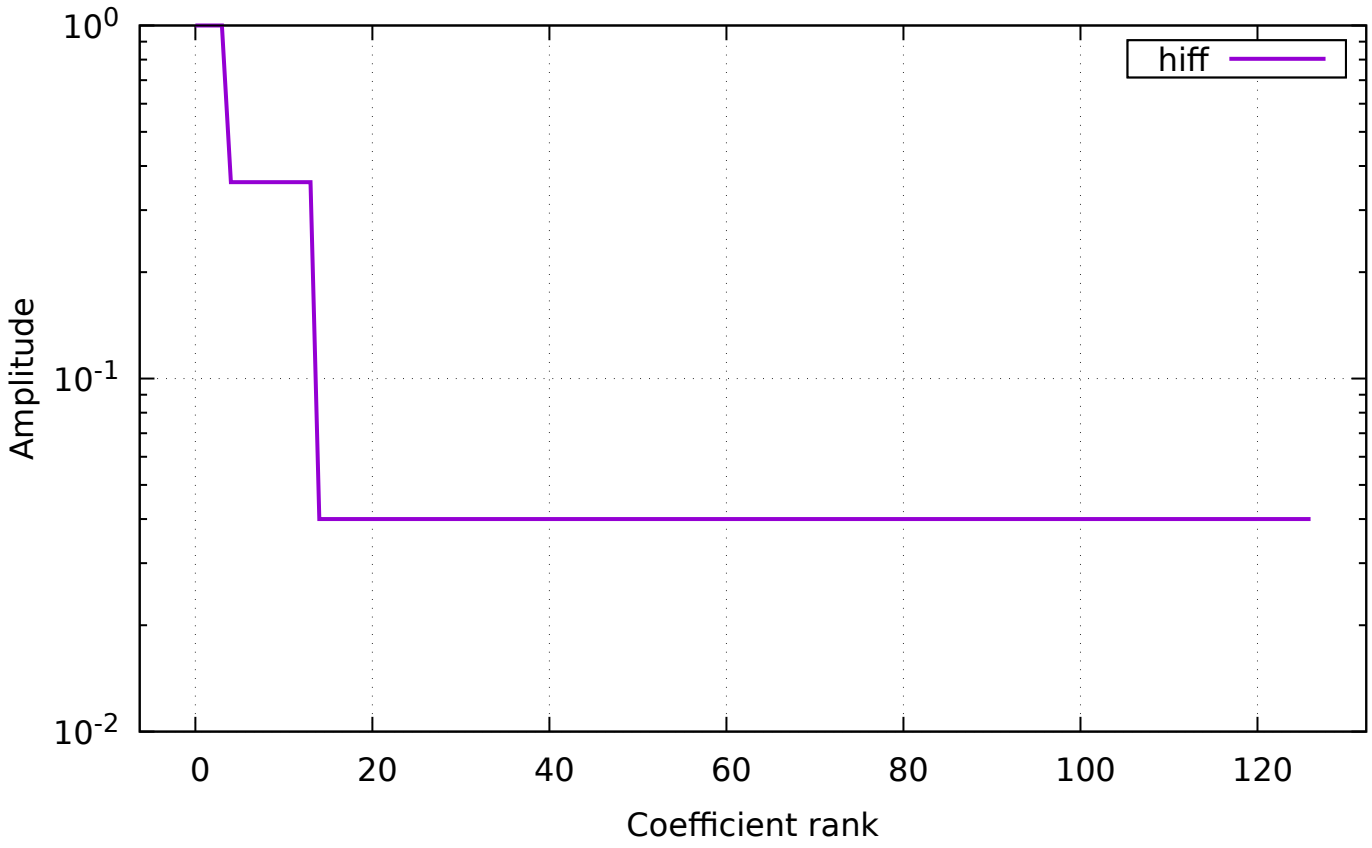
10^{-1}
10^{-2}
10^{-3}
0
1
2
3
4
5
6
7
8

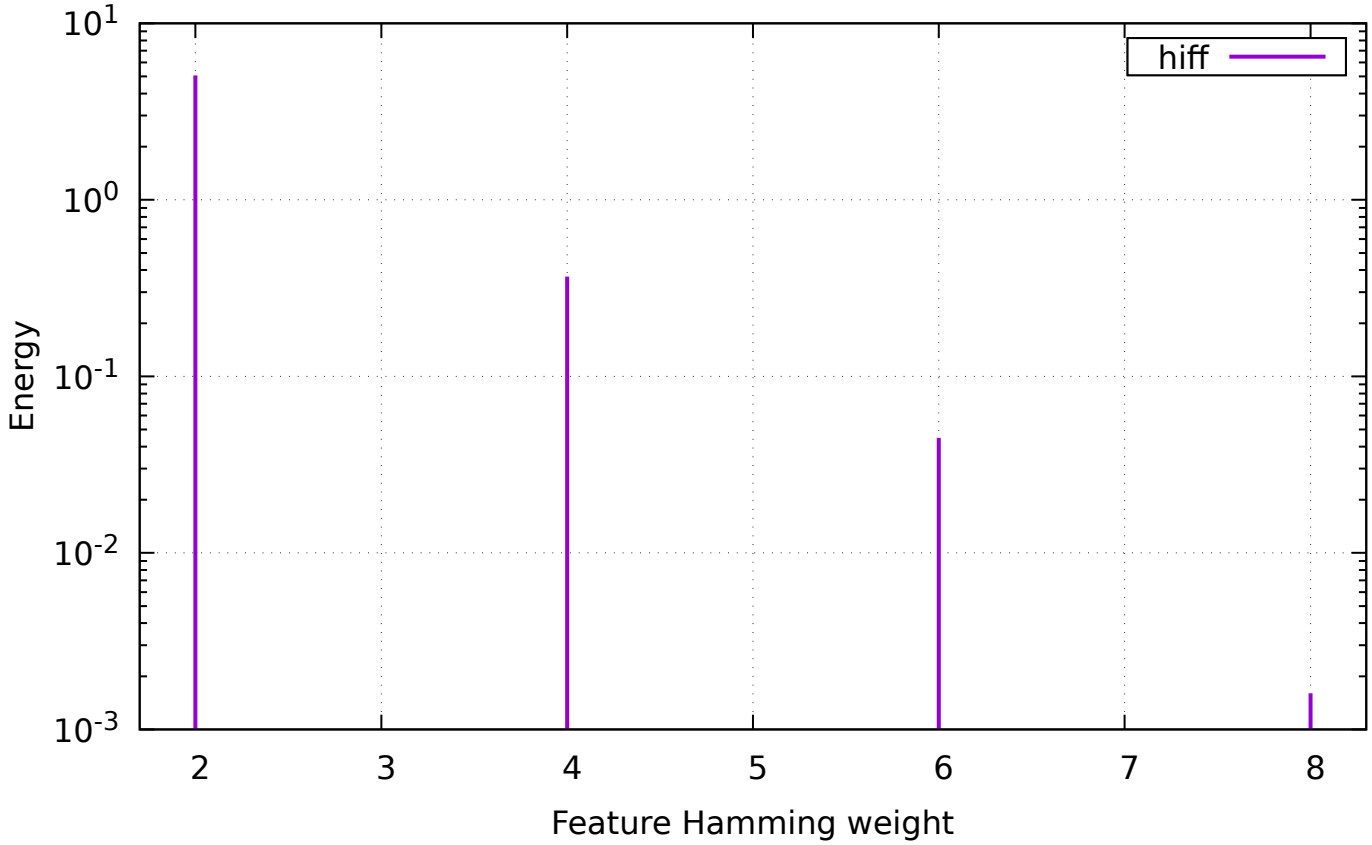

cancel
Energy
Feature Hamming weight
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
10^{-5}
1
1.2
1.4
1.6
1.8
2

17 trap

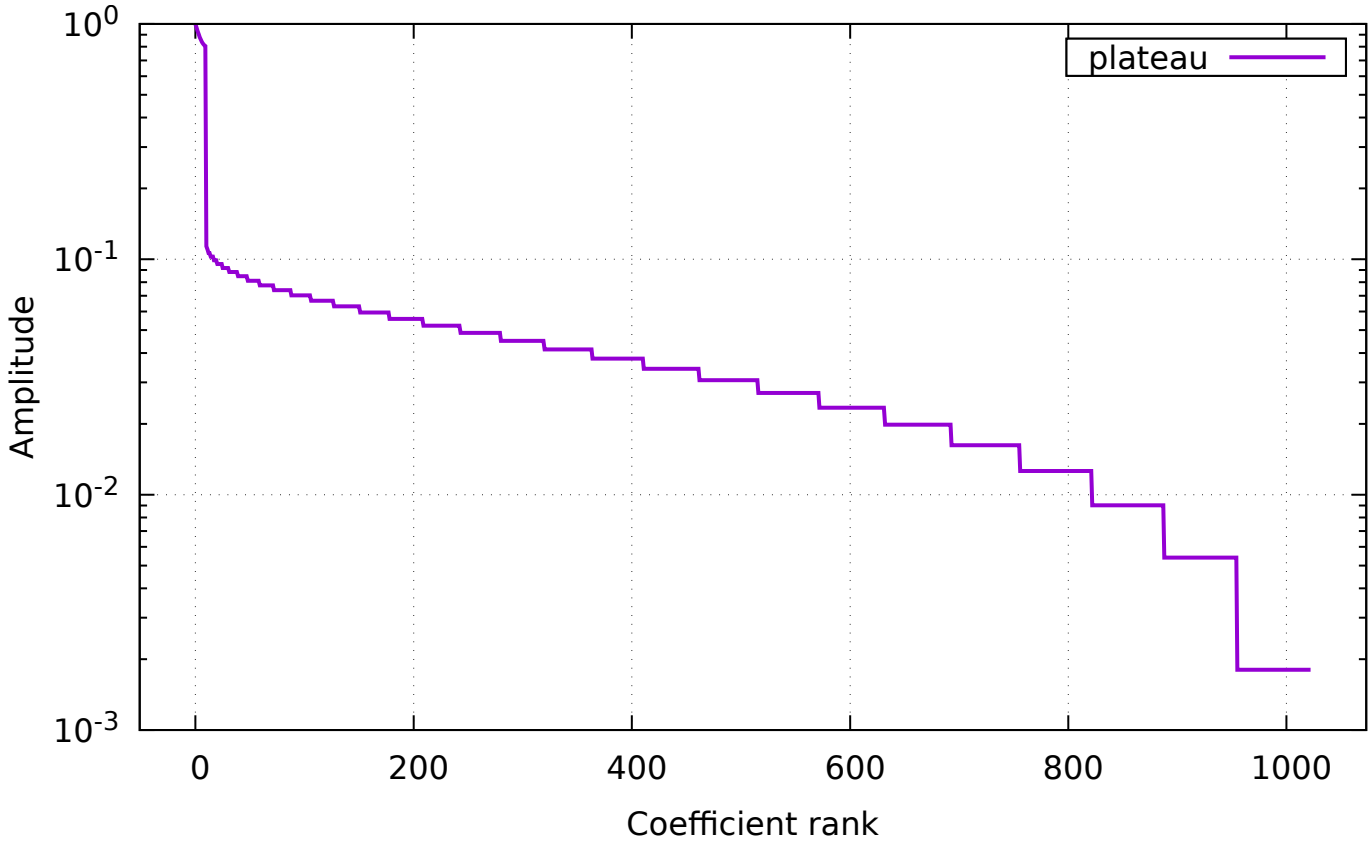

trap
Amplitude
Coefficient rank
10^0
10^{-1}
0
10
20
30
40
50
60

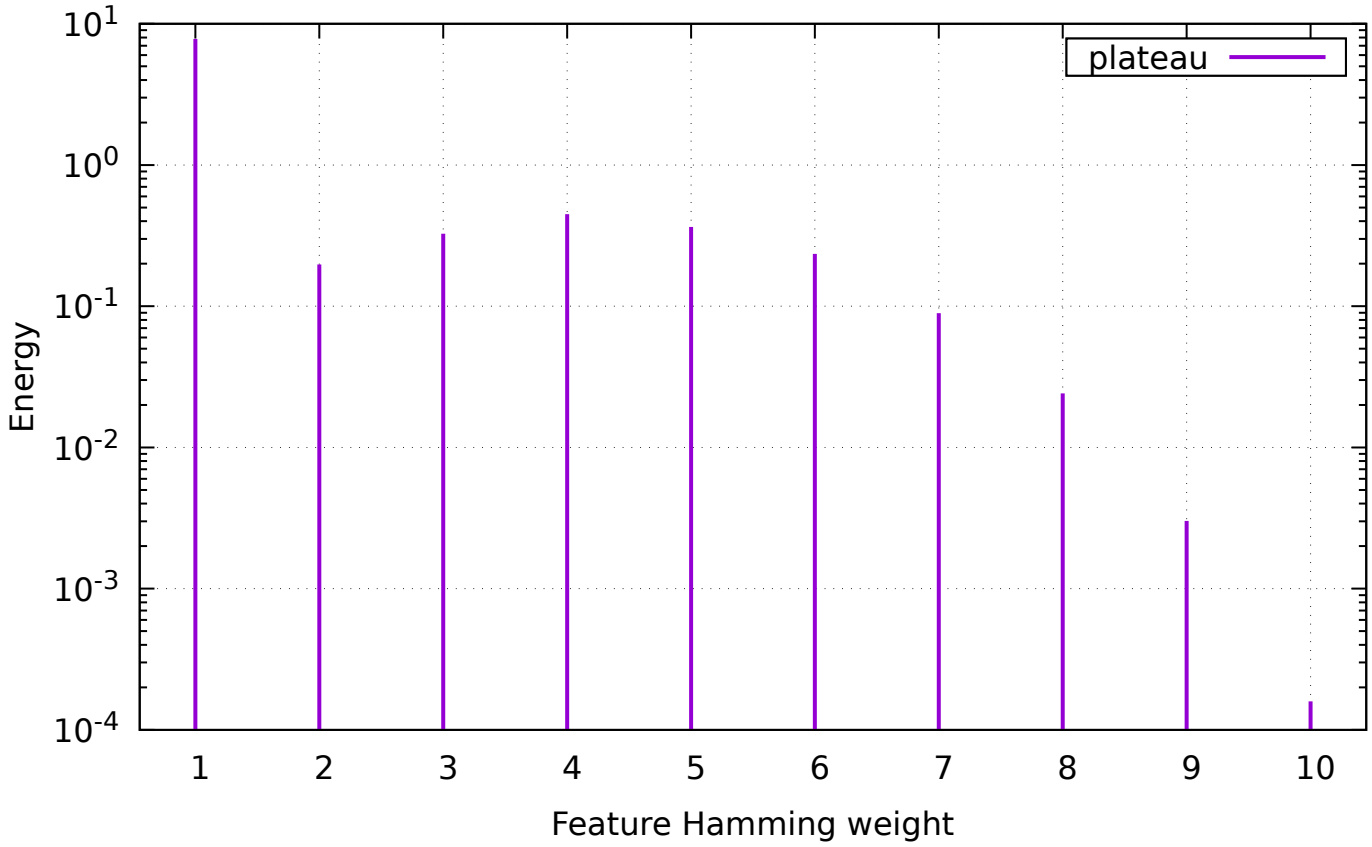

trap
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
1
1.5
2
2.5
3
3.5
4
4.5
5

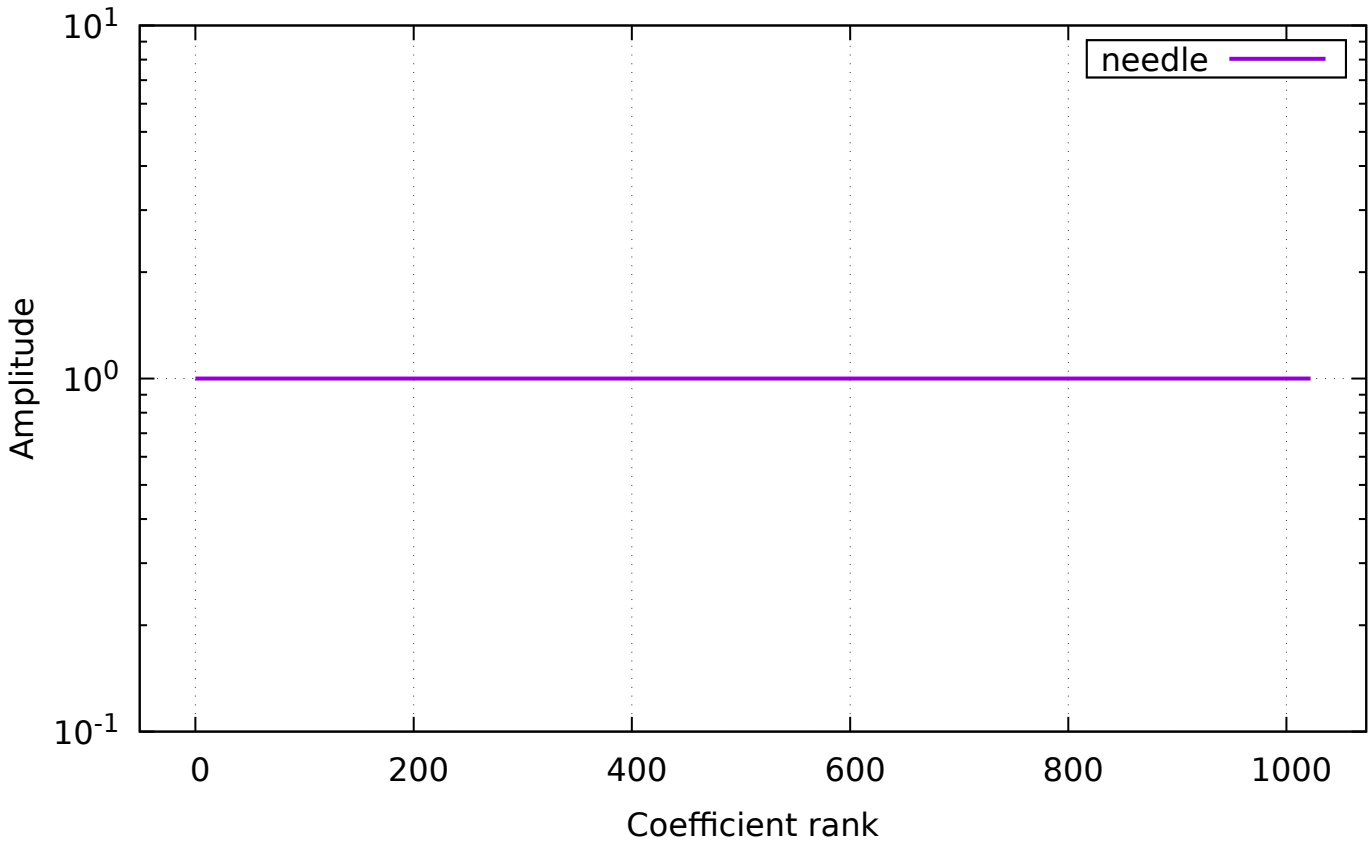

hiff
Amplitude
Coefficient rank
10^0
10^{-1}
10^{-2}
0
20
40
60
80
100
120

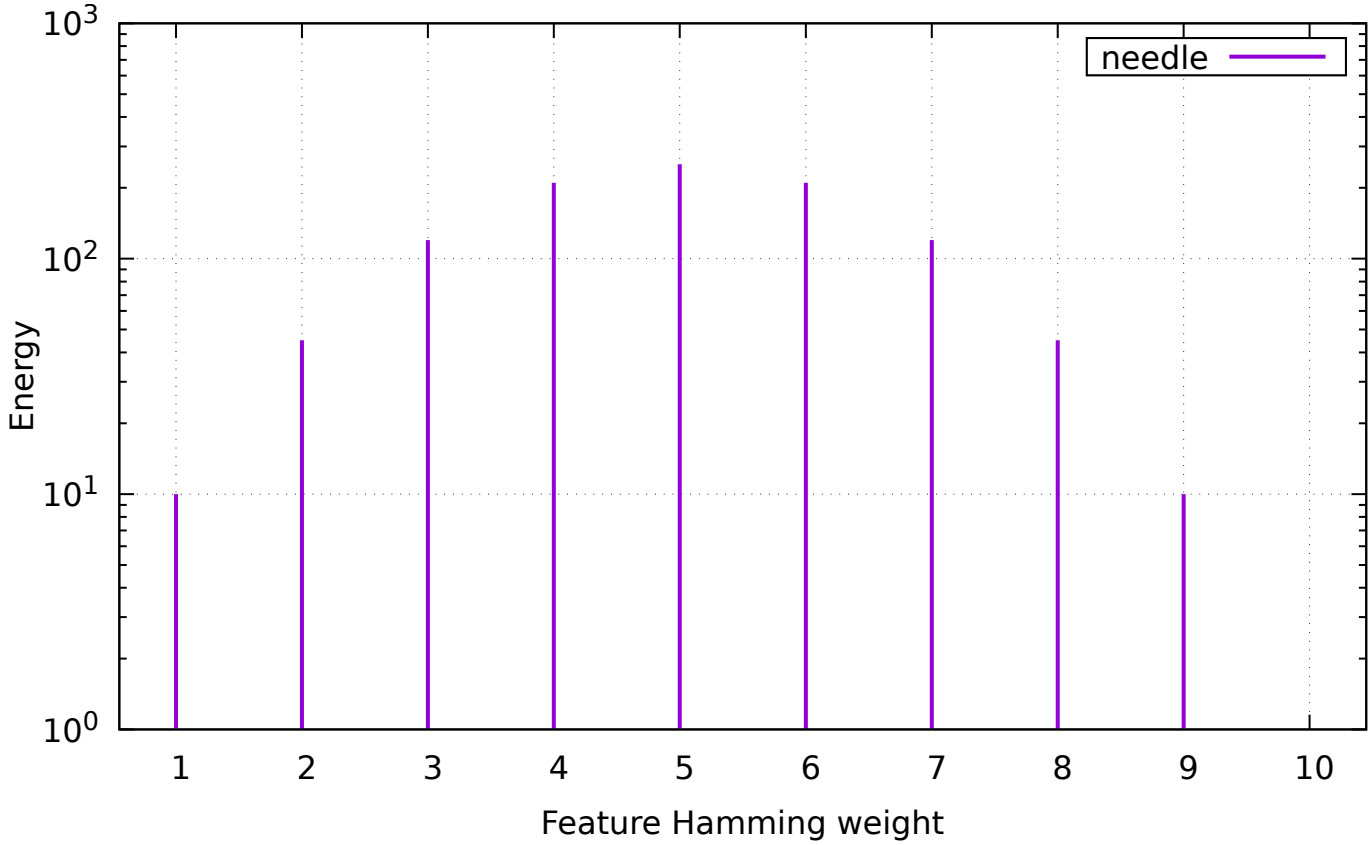

hiff
Energy
Feature Hamming weight
10^1
10^0
10^{-1}
10^{-2}
10^{-3}
2
3
4
5
6
7
8

19 plateau

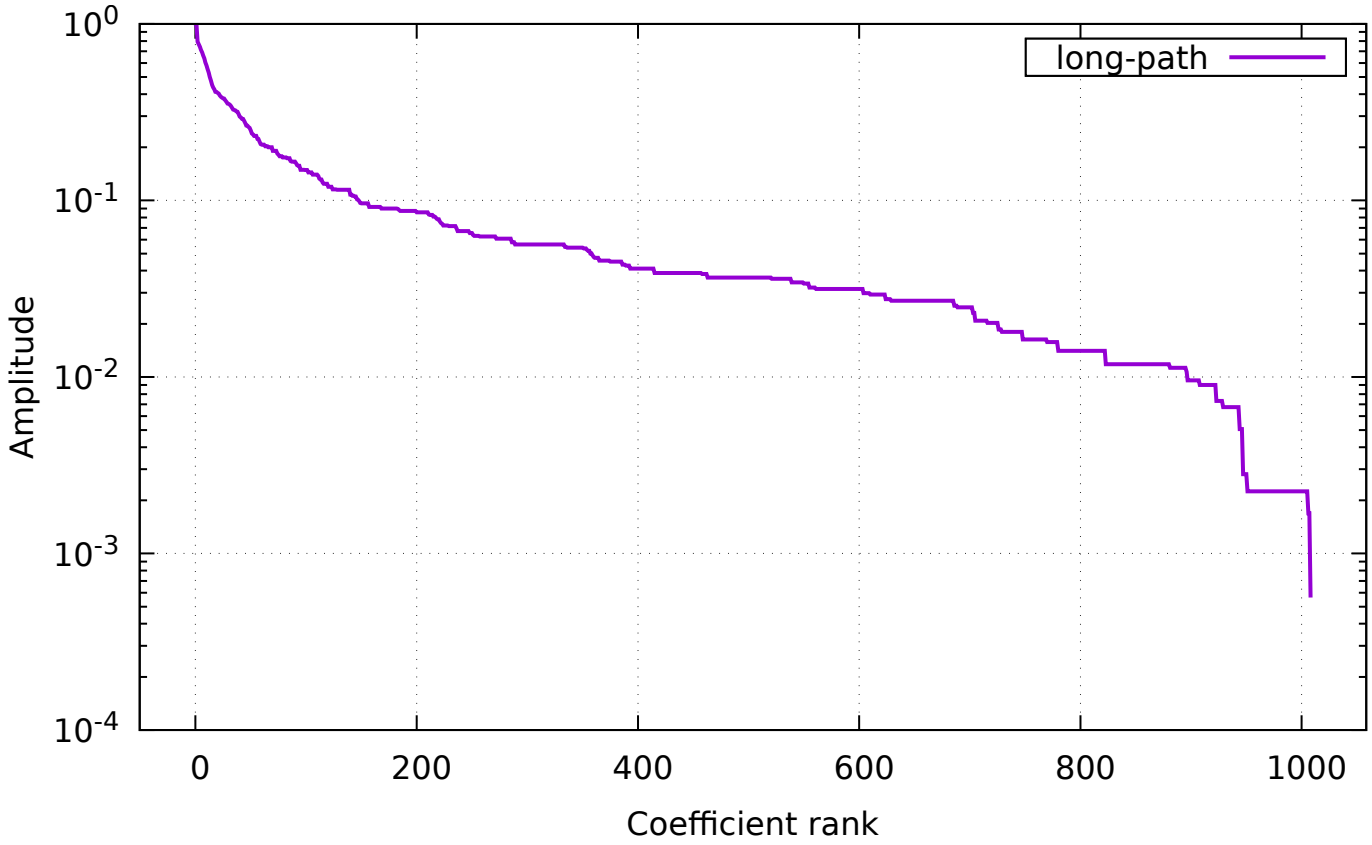

plateau
Amplitude
Coefficient rank
10^{0}
10^{-1}
10^{-2}
10^{-3}
0
200
400
600
800
1000

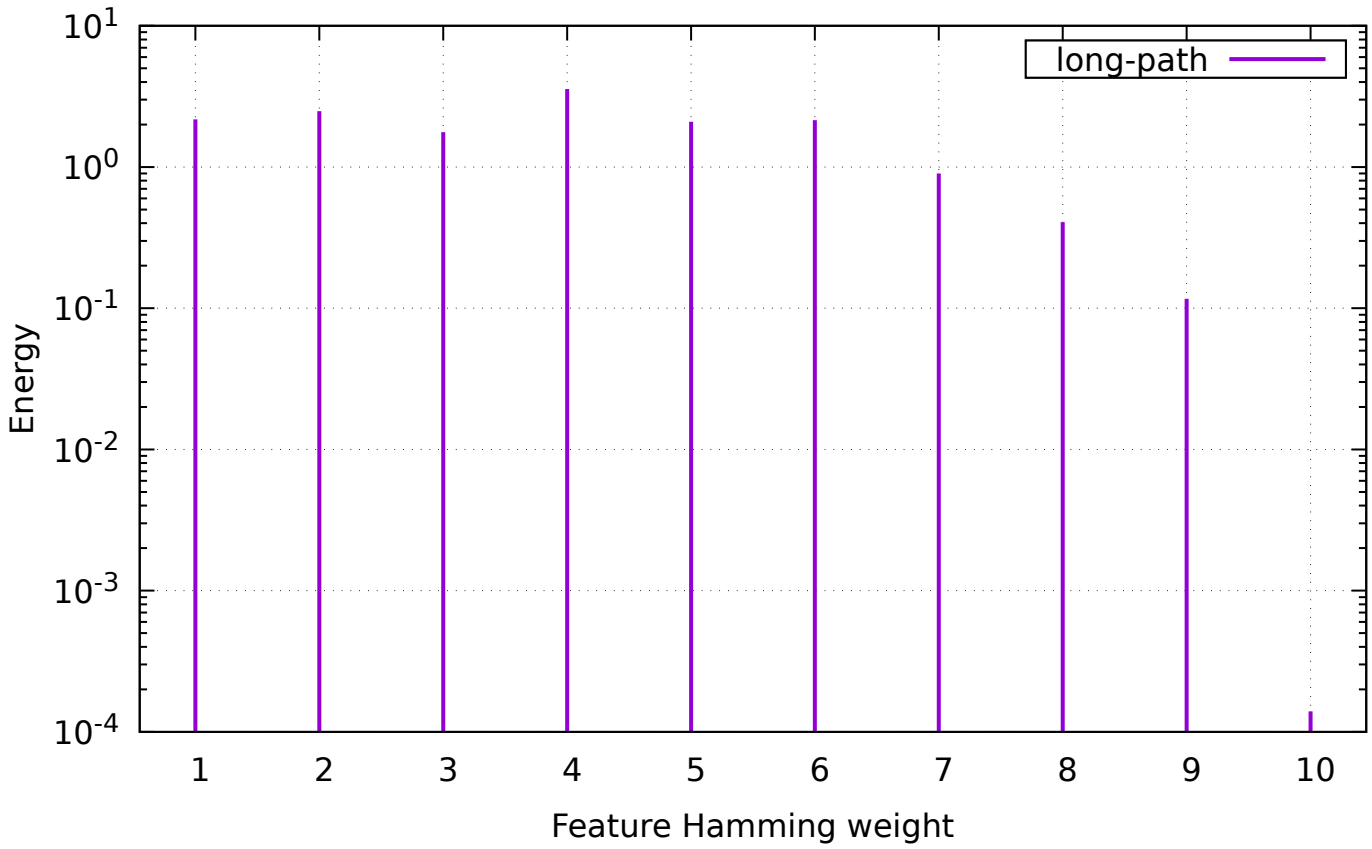

plateau
Energy
Feature Hamming weight
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
1
2
3
4
5
6
7
8
9
10


needle
Amplitude
Coefficient rank
10^1
10^0
10^{-1}
0
200
400
600
800
1000

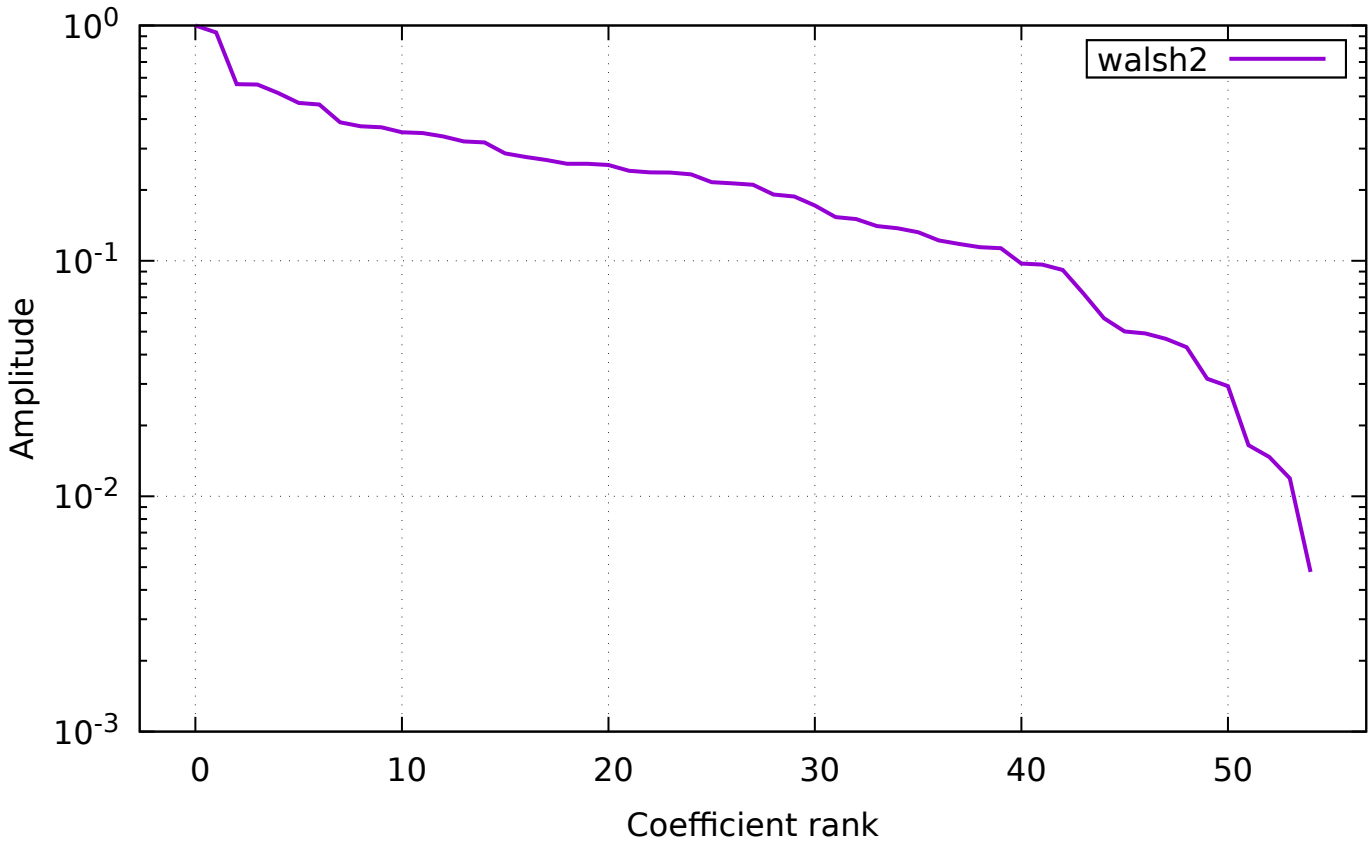

needle
Energy
Feature Hamming weight
10^3
10^2
10^1
10^0
1
2
3
4
5
6
7
8
9
10

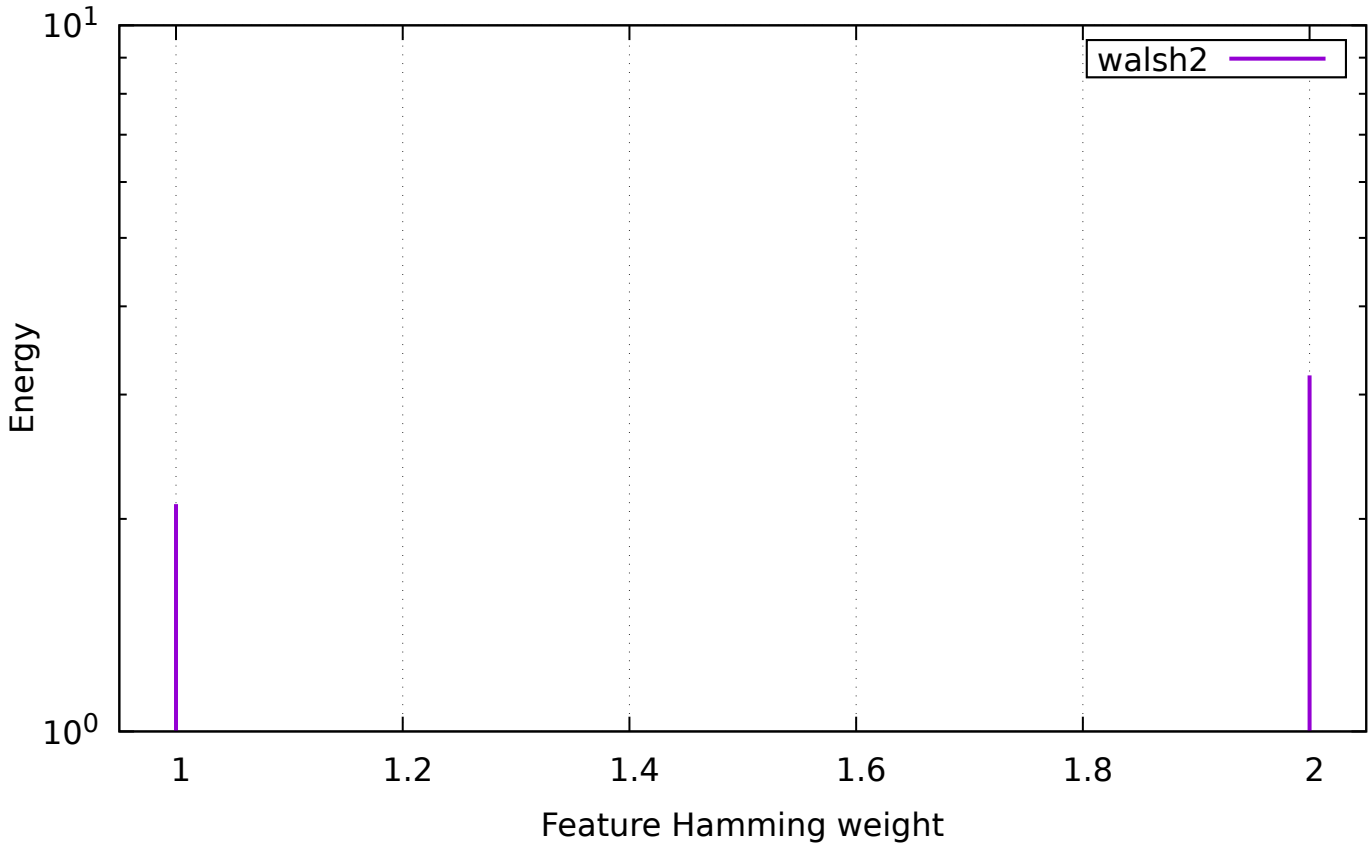
21 long-path


long-path
Amplitude
Coefficient rank
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
0
200
400
600
800
1000


long-path
Energy
Feature Hamming weight
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-3}
10^{-4}
1
2
3
4
5
6
7
8
9
10

22 walsh2





A Plan

```
{
    "exec": "hnco",
    "opt": "--fn-walsh-transform -b 0 -s 10",
```

```
"parallel": true,
"results": "results",
"graphics": "graphics",
"report": "report",
"functions": [
    {
        "id": "one-max",
        "opt": "-F 0"
    },
    {
        "id": "lin",
        "opt": "-F 1 -p instances/lin.10"
    },
    {
        "id": "leading-ones",
        "opt": "-F 10"
    },
    {
        "id": "ridge",
        "opt": "-F 11"
    },
    {
        "id": "jmp-2",
        "opt": "-F 30 -t 2"
    },
    {
        "id": "jmp-4",
        "opt": "-F 30 -t 4"
    },
    {
        "id": "djmp-2",
        "opt": "-F 31 -t 2"
    },
    {
        "id": "djmp-4",
        "opt": "-F 31 -t 4"
    },
    {
        "id": "fp-2",
        "opt": "-F 40 -t 2"
    },
    {
        "id": "fp-4",
        "opt": "-F 40 -t 4"
    },
    {
        "id": "nk",
        "opt": "-F 60 -p instances/nk.10.2"
    },
    {
        "id": "max-sat",
        "opt": "-F 70 -p instances/ms.10.3.10"
    },
    {
        "id": "labs",
        "opt": "-F 80"
    },
    {
        "id": "ep",
        "opt": "-F 90 -p instances/ep.10"
    },
    {
        "id": "cancel",
```

```
            "opt": "-F 100 -s 9"
        },
        {
            "id": "trap",
            "opt": "-F 110 --fn-num-traps 2"
        },
        {
            "id": "hiff",
            "opt": "-F 120 -s 8"
        },
        {
            "id": "plateau",
            "opt": "-F 130"
        },
        {
            "id": "needle",
            "opt": "-F 20"
        },
        {
            "id": "long-path",
            "opt": "-F 140"
        },
        {
            "id": "walsh2",
            "opt": "-F 162 -p instances/walsh2.10"
        }
    ]
}
```

B Default parameters

```
# algorithm = 100
# bm_mc_reset_strategy = 1
# bm_num_gs_cycles = 1
# bm_num_gs_steps = 100
# bm_sampling = 1
# budget = 10000
# bv_size = 100
# cache_budget = 0
# ea_lambda = 100
# ea_mu = 10
# fn_name = noname
# fn_num_traps = 10
# fn_prefix_length = 2
# fn_threshold = 10
# function = 0
# ga_crossover_bias = 0.5
# ga_crossover_probability = 0.5
# ga_tournament_size = 10
# hea_binary_dynamics = 0
# hea_delay = 10000
# hea_num_par_updates = 1
# hea_num_seq_updates = 100
# hea_rate_strategy = 0
# hea_reset_period = 0
# hea_sampling_method = 0
# hea_time_constant = 1000
# hea_weight = 1
# learning_rate = 0.001
# map = 0
# map_input_size = 100
# map_path = nopath
```

```
# mutation_probability = 1
# neighborhood = 0
# neighborhood_iterator = 0
# noise_stddev = 1
# num_iterations = 0
# num_threads = 1
# path = nopath
# pn_mutation_probability = 1
# pn_neighborhood = 0
# pn_radius = 2
# population_size = 10
# pv_log_num_components = 5
# radius = 2
# rls_patience = 50
# sa_beta_ratio = 1.2
# sa_initial_acceptance_probability = 0.6
# sa_num_transitions = 50
# sa_num_trials = 100
# seed = 0
# selection_size = 1
# target = 100
# print_defaults
# last_parameter
# exec_name = hnco
# version = 0.9
# Generated from hnco.json
```