HNCO

Comparison of various black box optimization algorithms

November 5, 2017

Contents

| 1 | Plan | 2 |
|-----------|-----------------------|------------|
| 2 | Rankings | 4 |
| 3 | Function one-max | 5 |
| 4 | Function lin | 6 |
| 5 | Function leading-ones | 7 |
| 6 | Function ridge | 8 |
| 7 | Function jmp-5 | 9 |
| 8 | Function jmp-10 | 10 |
| 9 | Function djmp-5 | 11 |
| 10 | Function djmp-10 | 12 |
| 11 | Function fp-5 | 13 |
| 12 | Function fp-10 | 14 |
| 13 | Function nk | 15 |
| 14 | Function max-sat | 16 |
| 15 | Function labs | 17 |
| 16 | Function ep | 18 |
| 17 | Function cancel | 19 |
| 18 | Function trap | 2 0 |
| 19 | Function hiff | 21 |
| 20 | Function plateau | 22 |
| 21 | Function walsh2 | 23 |
| 22 | Default parameters | 24 |

1 Plan

```
"exec": "hnco",
"opt": "--print-performance --map 1 --map-random -s 100 -i 0 -b 300000",
"num_runs": 20,
"parallel": false,
"results": "results",
"graphics": "graphics",
"report": "report",
"functions": [
    {
        "id": "one-max",
        "opt": "-F 0 --stop-on-maximum",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "lin",
        "opt": "-F 1 -p instances/lin.100",
        "col": ">{{\\nprounddigits{2}}}N{2}{2}"
    },
        "id": "leading-ones",
        "opt": "-F 10 --stop-on-maximum",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "ridge",
        "opt": "-F 11 --stop-on-maximum",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "jmp-5",
        "opt": "-F 30 --stop-on-maximum -t 5",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "jmp-10",
        "opt": "-F 30 --stop-on-maximum -t 10",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
   },
        "id": "djmp-5",
        "opt": "-F 31 --stop-on-maximum -t 5",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "djmp-10",
        "opt": "-F 31 --stop-on-maximum -t 10",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "fp-5",
        "opt": "-F 40 --stop-on-maximum -t 5",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "fp-10",
        "opt": "-F 40 --stop-on-maximum -t 10",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "nk",
```

```
"opt": "-F 60 -p instances/nk.100.4",
        "col": ">{{\\nprounddigits{2}}}N{1}{2}"
   },
        "id": "max-sat",
        "opt": "-F 70 -p instances/ms.100.3.1000 --cache",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "labs",
        "opt": "-F 80",
        "col": ">{{\\nprounddigits{2}}}N{1}{2}"
    },
        "id": "ep",
        "opt": "-F 90 -p instances/ep.100",
        "reverse": true,
        "logscale": true,
        "col": ">{{\\nprounddigits{1}}}N{1}{1}"
   },
        "id": "cancel",
        "opt": "-F 100 -s 99",
        "reverse": true,
        "col": ">{{\\nprounddigits{2}}}N{1}{2}"
    },
        "id": "trap",
        "opt": "-F 110 --stop-on-maximum --fun-num-traps 10",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
   },
        "id": "hiff",
        "opt": "-F 120 --stop-on-maximum -s 128",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "plateau",
        "opt": "-F 130 --stop-on-maximum",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "walsh2",
        "opt": "-F 162 -p instances/walsh2.100 --cache",
        "col": ">{{\\nprounddigits{2}}}N{3}{2}"
    }
"algorithms": [
    {
        "id": "rls",
        "opt": "-A 100 --restart"
    },
        "id": "hc",
        "opt": "-A 150 --restart"
    },
        "id": "sa",
        "opt": "-A 200 --sa-rate 1.05 --sa-num-trials 10"
   },
        "id": "ea-1p1",
        "opt": "-A 300"
```

],

```
},
    {
        "id": "ea-1p10",
        "opt": "-A 310 --ea-mu 1 --ea-lambda 10"
    },
        "id": "ea-10p1",
        "opt": "-A 310 --ea-mu 10 --ea-lambda 1"
    },
        "id": "ea-1c10",
        "opt": "-A 320 --ea-mu 1 --ea-lambda 10"
    },
        "id": "ga",
        "opt": "-A 400 --ea-mu 100"
    },
        "id": "pbil",
        "opt": "-A 500 -r 5e-3"
    },
        "id": "umda",
        "opt": "-A 600 -x 100 -y 10"
    }
]
```

2 Rankings

}

| algorithm | ran | k di | strib | outio | n | | | | | |
|-----------------------|-----|--------|--------|-------|--------|---|---|---|---|----|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| pbil | 10 | 1 | 0 | 2 | 1 | 1 | 1 | 2 | 0 | 1 |
| \mathbf{sa} | 7 | 3 | 1 | 3 | 0 | 1 | 0 | 0 | 2 | 2 |
| umda | 7 | 2 | 0 | 1 | 2 | 1 | 2 | 2 | 0 | 2 |
| hc | 6 | 4 | 2 | 2 | 1 | 0 | 0 | 0 | 2 | 2 |
| ga | 6 | 3 | 0 | 1 | 1 | 3 | 3 | 0 | 1 | 1 |
| rls | 5 | 5 | 0 | 5 | 1 | 0 | 0 | 1 | 0 | 2 |
| ea-1c10 | 5 | 4 | 2 | 5 | 1 | 1 | 0 | 0 | 1 | 0 |
| ea-1p1 | 4 | 3 | 0 | 4 | 1 | 4 | 0 | 1 | 1 | 1 |
| ea-10p1 | 4 | 2 | 4 | 5 | 2 | 1 | 1 | 0 | 0 | 0 |
| ea-1p10 | 4 | 2 | 0 | 3 | 0 | 3 | 1 | 3 | 3 | 0 |

3 Function one-max

| $\overline{ m algorithm}$ | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|---------------------------|-------|---------------|------------------------|----------|-----|----|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 100 | 100 | 100 | 100 | 100 | 1 | 0.000 | 0.000 |
| hc | 100 | 100 | 100 | 100 | 100 | 1 | 0.000 | 0.000 |
| sa | 100 | 100 | 100 | 100 | 100 | 1 | 0.005 | 0.005 |
| ea-1p1 | 100 | 100 | 100 | 100 | 100 | 1 | 0.000 | 0.000 |
| ea-1p10 | 100 | 100 | 100 | 100 | 100 | 1 | 0.001 | 0.002 |
| ea-10p1 | 100 | 100 | 100 | 100 | 100 | 1 | 0.020 | 0.007 |
| ea-1c10 | 100 | 100 | 100 | 100 | 100 | 1 | 0.003 | 0.005 |
| ga | 100 | 100 | 100 | 100 | 100 | 1 | 0.010 | 0.000 |
| pbil | 100 | 100 | 100 | 100 | 100 | 1 | 0.037 | 0.005 |
| $\underline{\text{umda}}$ | 100 | 100 | 100 | 100 | 100 | 1 | 0.000 | 0.000 |

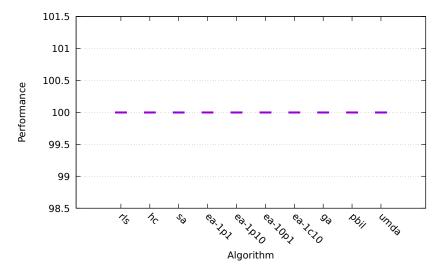


Figure 1: one-max

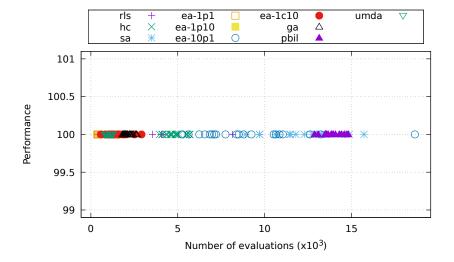


Figure 2: one-max \mathbf{r}

4 Function lin

| algorithm | perfori | mance | | | | | time (s | s) |
|-----------|---------|-------|------------------------|-------|-------|----|---------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.101 | 0.008 |
| hc | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.080 | 0.007 |
| sa | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.094 | 0.005 |
| ea-1p1 | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.158 | 0.004 |
| ea-1p10 | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.510 | 0.005 |
| ea-10p1 | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.537 | 0.007 |
| ea-1c10 | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.516 | 0.007 |
| ga | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 1.032 | 0.010 |
| pbil | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.539 | 0.004 |
| umda | 45.03 | 45.03 | 45.03 | 45.03 | 45.03 | 1 | 0.523 | 0.006 |

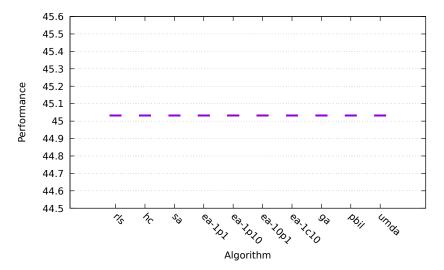


Figure 3: lin

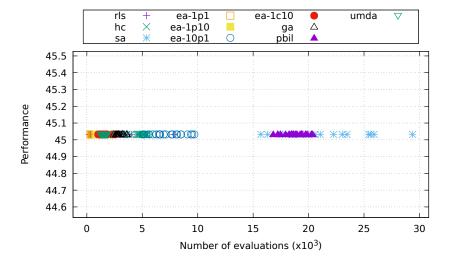


Figure 4: lin

5 Function leading-ones

| algorithm | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|-----------|-------|---------------|------------------------|----------|-----|----|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 100 | 100 | 100 | 100 | 100 | 1 | 0.006 | 0.006 |
| hc | 100 | 100 | 100 | 100 | 100 | 1 | 0.000 | 0.000 |
| sa | 3 | 100 | 100 | 100 | 100 | 10 | 0.009 | 0.022 |
| ea-1p1 | 100 | 100 | 100 | 100 | 100 | 1 | 0.004 | 0.005 |
| ea-1p10 | 100 | 100 | 100 | 100 | 100 | 1 | 0.016 | 0.005 |
| ea-10p1 | 100 | 100 | 100 | 100 | 100 | 1 | 0.118 | 0.023 |
| ea-1c10 | 100 | 100 | 100 | 100 | 100 | 1 | 0.021 | 0.006 |
| ga | 100 | 100 | 100 | 100 | 100 | 1 | 0.048 | 0.010 |
| pbil | 100 | 100 | 100 | 100 | 100 | 1 | 0.157 | 0.010 |
| umda | 100 | 100 | 100 | 100 | 100 | 1 | 0.025 | 0.006 |

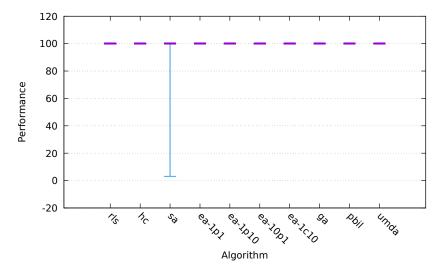


Figure 5: leading-ones

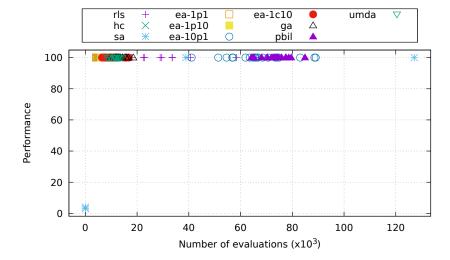


Figure 6: leading-ones

6 Function ridge

| algorithm | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|-----------|-------|---------------|------------------------|----------|-----|----|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 103 | 105 | 106 | 106 | 111 | 10 | 0.074 | 0.005 |
| hc | 200 | 200 | 200 | 200 | 200 | 1 | 0.005 | 0.005 |
| sa | 200 | 200 | 200 | 200 | 200 | 1 | 0.008 | 0.005 |
| ea-1p1 | 200 | 200 | 200 | 200 | 200 | 1 | 0.011 | 0.004 |
| ea-1p10 | 200 | 200 | 200 | 200 | 200 | 1 | 0.049 | 0.004 |
| ea-10p1 | 193 | 200 | 200 | 200 | 200 | 7 | 0.471 | 0.047 |
| ea-1c10 | 117 | 121 | 126 | 127 | 141 | 9 | 0.504 | 0.006 |
| ga | 200 | 200 | 200 | 200 | 200 | 1 | 0.170 | 0.011 |
| pbil | 153 | 154 | 155 | 156 | 157 | 8 | 0.532 | 0.008 |
| umda | 200 | 200 | 200 | 200 | 200 | 1 | 0.086 | 0.008 |

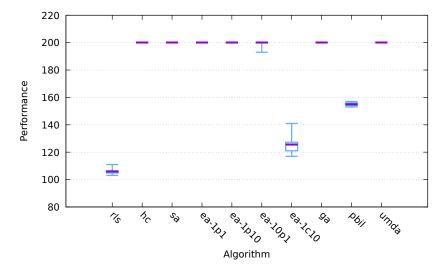


Figure 7: ridge

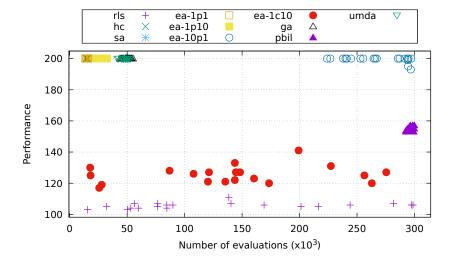


Figure 8: ridge

7 Function jmp-5

| algorithm | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|---------------------------|-------|---------------|------------------------|----------|-----|------|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 95 | 95 | 95 | 95 | 95 | 4 | 0.071 | 0.003 |
| hc | 95 | 95 | 95 | 95 | 95 | 4 | 0.056 | 0.006 |
| \mathbf{sa} | 95 | 95 | 95 | 95 | 95 | $_4$ | 0.076 | 0.005 |
| ea-1p1 | 95 | 95 | 95 | 95 | 95 | $_4$ | 0.142 | 0.005 |
| ea-1p10 | 95 | 95 | 95 | 95 | 95 | $_4$ | 0.492 | 0.006 |
| ea-10p1 | 95 | 95 | 95 | 95 | 95 | $_4$ | 0.513 | 0.005 |
| ea-1c10 | 95 | 95 | 95 | 95 | 95 | $_4$ | 0.496 | 0.008 |
| ga | 100 | 100 | 100 | 100 | 100 | 1 | 0.170 | 0.116 |
| pbil | 100 | 100 | 100 | 100 | 100 | 1 | 0.039 | 0.004 |
| $\underline{\text{umda}}$ | 100 | 100 | 100 | 100 | 100 | 1 | 0.053 | 0.056 |

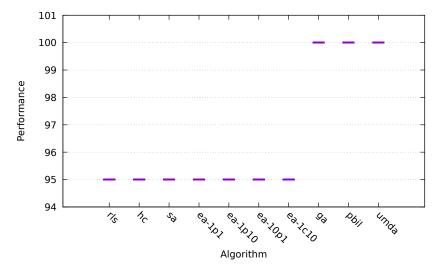


Figure 9: jmp-5

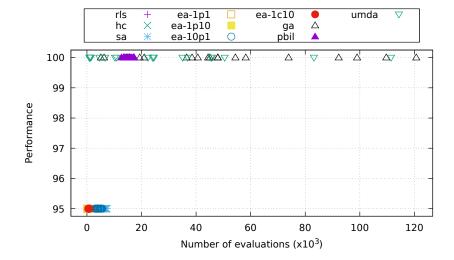


Figure 10: jmp-5

8 Function jmp-10

| algorithm | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|---------------|-------|---------------|------------------------|----------|-----|--------|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 90 | 90 | 90 | 90 | 90 | 2 | 0.075 | 0.005 |
| hc | 90 | 90 | 90 | 90 | 90 | 2 | 0.059 | 0.004 |
| \mathbf{sa} | 90 | 90 | 90 | 90 | 90 | 2 | 0.078 | 0.005 |
| ea-1p1 | 90 | 90 | 90 | 90 | 90 | 2 | 0.140 | 0.003 |
| ea-1p10 | 90 | 90 | 90 | 90 | 90 | 2 | 0.492 | 0.005 |
| ea-10p1 | 90 | 90 | 90 | 90 | 90 | 2 | 0.519 | 0.009 |
| ea-1c10 | 90 | 90 | 90 | 90 | 90 | 2 | 0.492 | 0.004 |
| ga | 90 | 90 | 90 | 90 | 90 | 2 | 1.003 | 0.006 |
| pbil | 90 | 90 | 90 | 100 | 100 | 1 | 0.381 | 0.258 |
| umda | 90 | 90 | 90 | 90 | 90 | 2 | 0.551 | 0.007 |

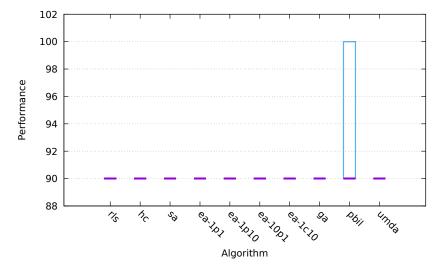


Figure 11: jmp-10

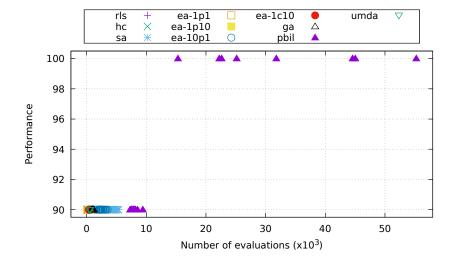


Figure 12: jmp-10

9 Function djmp-5

| algorithm | perfo | $_{ m rmanc}$ | time (s | time (s) | | | | |
|---------------|-------|---------------|------------------------|----------|-----|----|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 100 | 100 | 100 | 100 | 100 | 4 | 0.071 | 0.002 |
| hc | 100 | 100 | 100 | 100 | 100 | 4 | 0.057 | 0.005 |
| \mathbf{sa} | 100 | 100 | 100 | 100 | 100 | 4 | 0.074 | 0.005 |
| ea-1p1 | 100 | 100 | 100 | 100 | 100 | 4 | 0.141 | 0.005 |
| ea-1p10 | 100 | 100 | 100 | 100 | 100 | 4 | 0.492 | 0.006 |
| ea-10p1 | 100 | 100 | 100 | 100 | 100 | 4 | 0.519 | 0.007 |
| ea-1c10 | 100 | 100 | 100 | 100 | 100 | 4 | 0.497 | 0.009 |
| ga | 105 | 105 | 105 | 105 | 105 | 1 | 0.201 | 0.163 |
| pbil | 105 | 105 | 105 | 105 | 105 | 1 | 0.036 | 0.006 |
| umda | 105 | 105 | 105 | 105 | 105 | 1 | 0.039 | 0.034 |

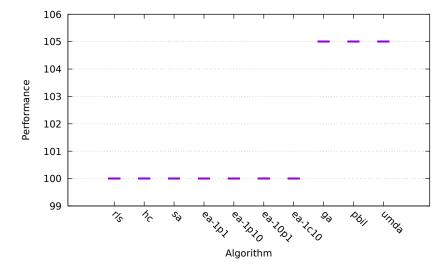


Figure 13: djmp-5

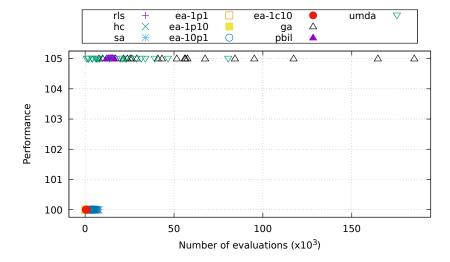


Figure 14: djmp-5

10 Function djmp-10

| algorithm | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|-----------|-------|---------------|------------------------|----------|-----|--------|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 100 | 100 | 100 | 100 | 100 | 2 | 0.073 | 0.004 |
| hc | 100 | 100 | 100 | 100 | 100 | 2 | 0.060 | 0.005 |
| sa | 100 | 100 | 100 | 100 | 100 | 2 | 0.077 | 0.005 |
| ea-1p1 | 100 | 100 | 100 | 100 | 100 | 2 | 0.141 | 0.003 |
| ea-1p10 | 100 | 100 | 100 | 100 | 100 | 2 | 0.495 | 0.007 |
| ea-10p1 | 100 | 100 | 100 | 100 | 100 | 2 | 0.515 | 0.005 |
| ea-1c10 | 100 | 100 | 100 | 100 | 100 | 2 | 0.494 | 0.005 |
| ga | 100 | 100 | 100 | 100 | 100 | 2 | 1.026 | 0.019 |
| pbil | 100 | 100 | 110 | 110 | 110 | 1 | 0.260 | 0.248 |
| umda | 100 | 100 | 100 | 100 | 100 | 2 | 0.558 | 0.010 |

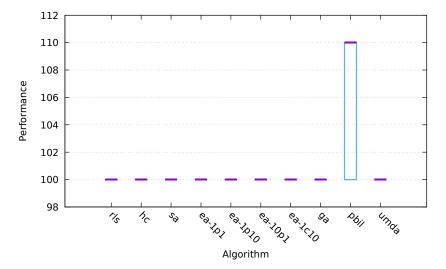


Figure 15: djmp-10

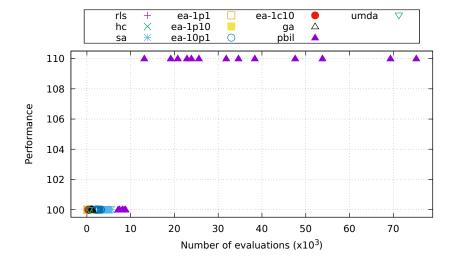


Figure 16: djmp-10

11 Function fp-5

| algorithm | perfo | rmanc | | time (s) | | | | |
|-----------|-------|-------|------------------------|----------|-----|----|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 194 | 194 | 194 | 194 | 194 | 1 | 0.005 | 0.006 |
| hc | 100 | 100 | 194 | 194 | 194 | 10 | 0.046 | 0.022 |
| sa | 4 | 194 | 194 | 194 | 194 | 9 | 0.018 | 0.031 |
| ea-1p1 | 100 | 194 | 194 | 194 | 194 | 6 | 0.009 | 0.033 |
| ea-1p10 | 100 | 194 | 194 | 194 | 194 | 6 | 0.093 | 0.183 |
| ea-10p1 | 194 | 194 | 194 | 194 | 194 | 1 | 0.110 | 0.016 |
| ea-1c10 | 194 | 194 | 194 | 194 | 194 | 1 | 0.027 | 0.018 |
| ga | 100 | 194 | 194 | 194 | 194 | 6 | 0.095 | 0.218 |
| pbil | 194 | 194 | 194 | 194 | 194 | 1 | 0.175 | 0.011 |
| umda | 194 | 194 | 194 | 194 | 194 | 1 | 0.025 | 0.005 |

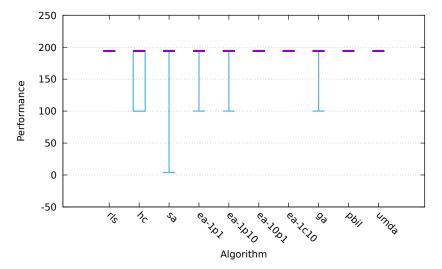


Figure 17: fp-5

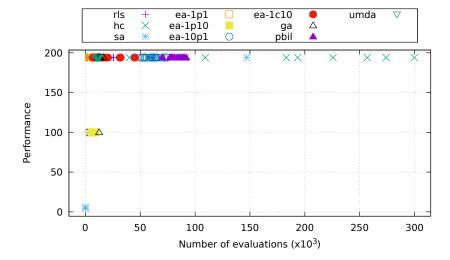


Figure 18: fp-5

12 Function fp-10

| algorithm | perfo | $_{ m rmanc}$ | | time (s) | | | | |
|-----------|-------|---------------|------------------------|----------|-----|----|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 184 | 189 | 189 | 189 | 189 | 2 | 0.026 | 0.020 |
| hc | 100 | 100 | 100 | 100 | 100 | 9 | 0.060 | 0.000 |
| sa | 4 | 100 | 100 | 100 | 189 | 10 | 0.067 | 0.026 |
| ea-1p1 | 100 | 100 | 100 | 189 | 189 | 5 | 0.096 | 0.071 |
| ea-1p10 | 100 | 100 | 100 | 100 | 189 | 8 | 0.462 | 0.153 |
| ea-10p1 | 100 | 189 | 189 | 189 | 189 | 3 | 0.175 | 0.152 |
| ea-1c10 | 100 | 167 | 189 | 189 | 189 | 4 | 0.255 | 0.188 |
| ga | 100 | 100 | 100 | 189 | 189 | 5 | 0.674 | 0.475 |
| pbil | 189 | 189 | 189 | 189 | 189 | 1 | 0.156 | 0.009 |
| umda | 100 | 100 | 100 | 189 | 189 | 5 | 0.345 | 0.244 |

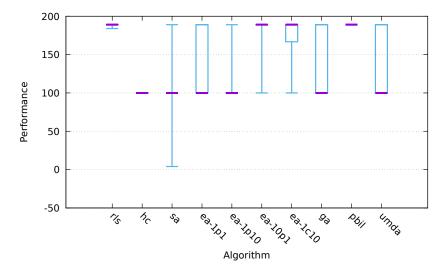


Figure 19: fp-10

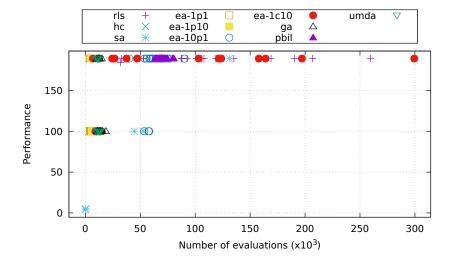


Figure 20: fp-10

13 Function nk

| algorithm | performance time | | | | | time (s | s) | |
|---------------------------|------------------|-------|------------------------|-------|------|---------|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 0.97 | 0.98 | 0.99 | 1.01 | 1.06 | 4 | 0.272 | 0.007 |
| hc | 0.96 | 0.98 | 1.00 | 1.02 | 1.07 | 3 | 0.255 | 0.005 |
| sa | 1.00 | 1.04 | 1.06 | 1.06 | 1.10 | 1 | 0.276 | 0.005 |
| ea-1p1 | 0.81 | 0.91 | 0.93 | 0.98 | 1.06 | 10 | 0.347 | 0.005 |
| ea-1p10 | 0.89 | 0.93 | 0.94 | 0.95 | 1.04 | 9 | 0.693 | 0.008 |
| ea-10p1 | 0.86 | 0.96 | 0.98 | 1.02 | 1.05 | 6 | 0.716 | 0.009 |
| ea-1c10 | 0.97 | 0.99 | 1.01 | 1.03 | 1.06 | 2 | 0.697 | 0.009 |
| ga | 0.88 | 0.92 | 0.95 | 0.99 | 1.01 | 7 | 1.211 | 0.013 |
| pbil | 0.94 | 0.97 | 0.99 | 1.01 | 1.05 | 5 | 0.736 | 0.010 |
| $\underline{\text{umda}}$ | 0.80 | 0.91 | 0.95 | 0.96 | 0.99 | 8 | 0.707 | 0.007 |

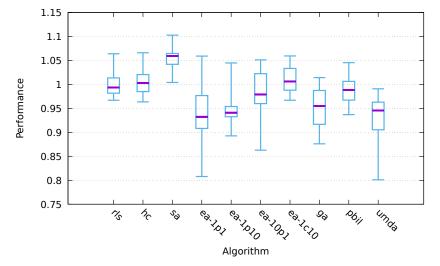
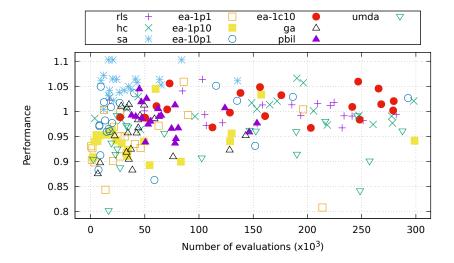


Figure 21: nk



 $Figure\ 22:\ nk$

14 Function max-sat

| algorithm | perfo | $_{ m rmanc}$ | e | | | | time (s | s) |
|-----------|-------|---------------|------------------------|-------|-----|----|---------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 971 | 971 | 972 | 972 | 972 | 2 | 1.930 | 0.011 |
| hc | 952 | 965 | 967 | 968 | 972 | 9 | 0.258 | 0.047 |
| sa | 971 | 972 | 972 | 972 | 972 | 1 | 0.620 | 0.108 |
| ea-1p1 | 958 | 966 | 968 | 972 | 972 | 6 | 0.848 | 0.216 |
| ea-1p10 | 959 | 964 | 967 | 968 | 972 | 8 | 1.098 | 0.123 |
| ea-10p1 | 960 | 967 | 968 | 968 | 972 | 4 | 2.005 | 0.071 |
| ea-1c10 | 964 | 967 | 968 | 971 | 972 | 3 | 1.252 | 0.094 |
| ga | 957 | 963 | 965 | 969 | 972 | 10 | 1.621 | 0.092 |
| pbil | 964 | 966 | 967 | 967 | 969 | 7 | 1.411 | 0.049 |
| umda | 962 | 966 | 968 | 970 | 972 | 5 | 1.158 | 0.077 |

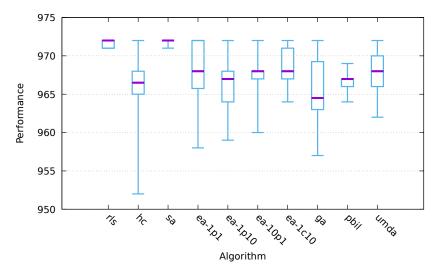


Figure 23: max-sat

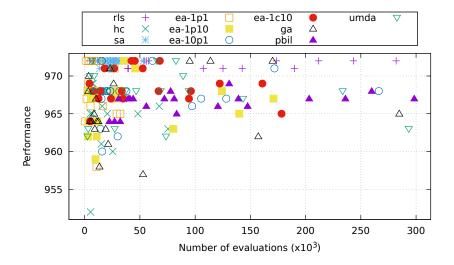


Figure 24: max-sat

15 Function labs

| algorithm | perfo | $_{ m rmance}$ | : | | | | time (s) | | | | |
|---------------------------|-------|----------------|------------------------|-------|------|--------|----------|-------|--|--|--|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. | | | |
| rls | 4.16 | 4.36 | 4.47 | 4.57 | 5.18 | 5 | 1.593 | 0.011 | | | |
| hc | 4.54 | 4.58 | 4.76 | 4.90 | 5.33 | 2 | 1.607 | 0.041 | | | |
| \mathbf{sa} | 4.36 | 4.61 | 4.69 | 4.90 | 5.07 | $_4$ | 1.633 | 0.045 | | | |
| ea-1p1 | 3.51 | 4.04 | 4.17 | 4.36 | 4.55 | 6 | 1.705 | 0.069 | | | |
| ea-1p10 | 3.60 | 3.80 | 3.96 | 4.19 | 4.60 | 9 | 2.021 | 0.033 | | | |
| ea-10p1 | 4.26 | 4.47 | 4.73 | 4.88 | 5.33 | 3 | 2.043 | 0.046 | | | |
| ea-1c10 | 4.66 | 4.76 | 4.84 | 5.02 | 5.29 | 1 | 2.003 | 0.006 | | | |
| ga | 3.61 | 3.79 | 4.05 | 4.23 | 4.57 | 7 | 2.516 | 0.014 | | | |
| pbil | 3.84 | 3.96 | 4.03 | 4.13 | 5.05 | 8 | 2.122 | 0.008 | | | |
| $\underline{\text{umda}}$ | 3.54 | 3.80 | 3.91 | 4.08 | 4.62 | 10 | 2.021 | 0.010 | | | |

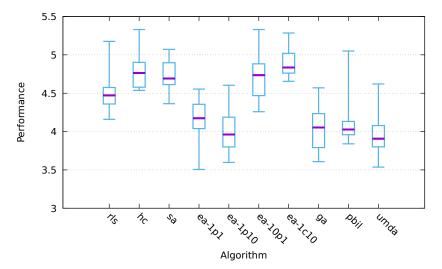


Figure 25: labs

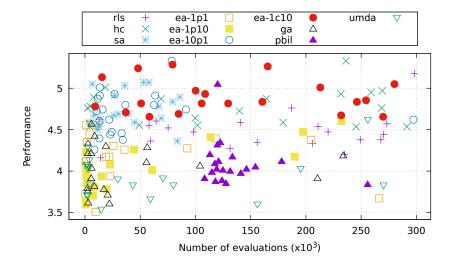


Figure 26: labs

16 Function ep

| algorithm | performance | | | | | | time (s | s) |
|---------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|----|---------|-------|
| | min | Q_1 | med. | Q_3 | max | rk | mean | dev. |
| rls | 6.1×10^{-32} | 8.4×10^{-31} | 2.1×10^{-30} | 4.5×10^{-30} | 1.2×10^{-29} | 1 | 0.121 | 0.002 |
| hc | 2.8×10^{-31} | 1.9×10^{-30} | 5.7×10^{-30} | 8.5×10^{-30} | 2.9×10^{-29} | 3 | 0.094 | 0.005 |
| \mathbf{sa} | 3.2×10^{-31} | 1.9×10^{-30} | 9.6×10^{-30} | 1.8×10^{-29} | 1.4×10^{-25} | 6 | 0.107 | 0.005 |
| ea-1p1 | 3.2×10^{-31} | 6.2×10^{-30} | 1.6×10^{-29} | 2.7×10^{-29} | 7.1×10^{-29} | 8 | 0.169 | 0.004 |
| ea-1p10 | 4.7×10^{-31} | 9.1×10^{-30} | 2.1×10^{-29} | 3.1×10^{-29} | 1.0×10^{-28} | 9 | 0.519 | 0.004 |
| ea-10p1 | 4.3×10^{-31} | 2.8×10^{-30} | 7.8×10^{-30} | 1.4×10^{-29} | 2.5×10^{-29} | 5 | 0.553 | 0.006 |
| ea-1c10 | 1.4×10^{-31} | 1.9×10^{-30} | 6.1×10^{-30} | 1.2×10^{-29} | 2.7×10^{-29} | 4 | 0.522 | 0.004 |
| ga | 2.5×10^{-30} | 9.5×10^{-30} | 1.5×10^{-29} | 2.9×10^{-29} | 5.2×10^{-29} | 7 | 1.038 | 0.006 |
| pbil | 3.2×10^{-31} | 1.4×10^{-30} | 2.9×10^{-30} | 4.8×10^{-30} | 9.1×10^{-30} | 2 | 0.755 | 0.019 |
| umda | 6.1×10^{-32} | 6.8×10^{-30} | 2.4×10^{-29} | 5.7×10^{-29} | 1.5×10^{-28} | 10 | 0.541 | 0.007 |

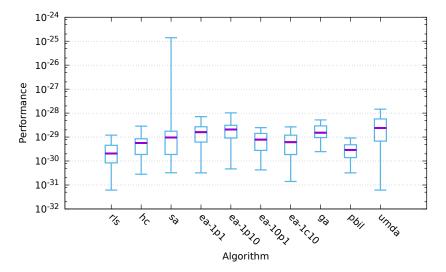


Figure 27: ep

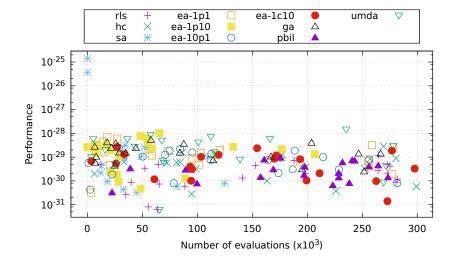


Figure 28: ep

17 Function cancel

| $\overline{ m algorithm}$ | perfo | rmance | ; | | | | time (s) | | | |
|---------------------------|-------|--------|------------------------|-------|------|--------|----------|-------|--|--|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. | | |
| rls | 0.15 | 1.11 | 1.54 | 1.88 | 2.30 | 8 | 0.101 | 0.011 | | |
| hc | 1.38 | 2.23 | 3.07 | 3.94 | 6.34 | 10 | 0.082 | 0.004 | | |
| sa | 0.06 | 1.71 | 2.38 | 2.90 | 4.60 | 9 | 0.100 | 0.000 | | |
| ea-1p1 | 0.06 | 0.42 | 0.60 | 1.19 | 1.65 | 4 | 0.168 | 0.004 | | |
| ea-1p10 | 0.12 | 0.42 | 0.83 | 1.33 | 2.62 | 6 | 0.516 | 0.006 | | |
| ea-10p1 | 0.05 | 0.19 | 0.60 | 1.34 | 2.09 | 3 | 0.541 | 0.008 | | |
| ea-1c10 | 0.08 | 0.20 | 0.69 | 1.35 | 2.58 | 5 | 0.515 | 0.005 | | |
| ga | 0.06 | 0.23 | 0.46 | 0.77 | 1.98 | 2 | 1.033 | 0.015 | | |
| pbil | 0.05 | 0.07 | 0.08 | 0.11 | 1.36 | 1 | 0.586 | 0.011 | | |
| umda | 0.13 | 0.67 | 1.22 | 1.93 | 3.19 | 7 | 0.530 | 0.006 | | |

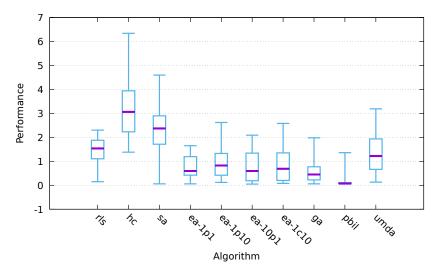


Figure 29: cancel

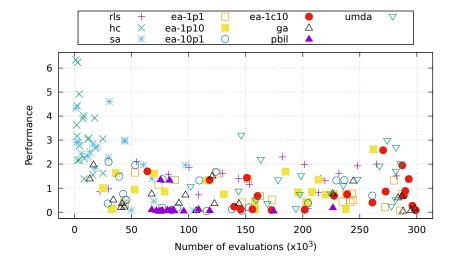


Figure 30: cancel

18 Function trap

| algorithm | performance | | | | | | time (s) | | |
|-----------|-------------|-------|------------------------|-------|-----|----|----------|-------|--|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. | |
| rls | 91 | 91 | 91 | 91 | 92 | 2 | 0.092 | 0.004 | |
| hc | 91 | 91 | 91 | 92 | 92 | 1 | 0.080 | 0.002 | |
| sa | 90 | 90 | 90 | 91 | 91 | 3 | 0.099 | 0.004 | |
| ea-1p1 | 90 | 90 | 90 | 90 | 91 | 4 | 0.162 | 0.004 | |
| ea-1p10 | 90 | 90 | 90 | 90 | 90 | 6 | 0.513 | 0.006 | |
| ea-10p1 | 90 | 90 | 90 | 90 | 91 | 4 | 0.541 | 0.009 | |
| ea-1c10 | 90 | 90 | 90 | 90 | 90 | 6 | 0.519 | 0.011 | |
| ga | 90 | 90 | 90 | 90 | 90 | 6 | 1.025 | 0.009 | |
| pbil | 90 | 90 | 90 | 90 | 90 | 6 | 0.551 | 0.015 | |
| umda | 90 | 90 | 90 | 90 | 90 | 6 | 0.533 | 0.016 | |

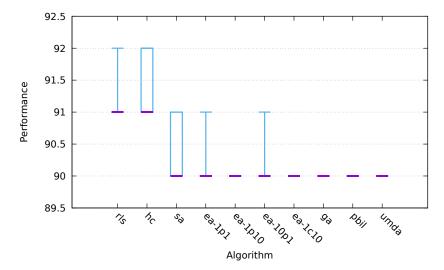


Figure 31: trap

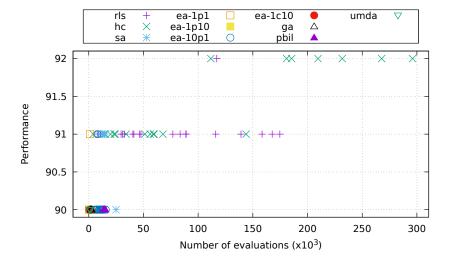


Figure 32: trap

19 Function hiff

| algorithm | perfo | $_{ m rmanc}$ | e | | | | time (s | s) |
|-----------|-------|---------------|------------------------|-------|-----|--------|---------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 400 | 410 | 416 | 420 | 434 | 10 | 0.308 | 0.015 |
| hc | 480 | 500 | 510 | 521 | 568 | 5 | 0.278 | 0.006 |
| sa | 640 | 672 | 704 | 744 | 896 | 1 | 0.317 | 0.012 |
| ea-1p1 | 432 | 456 | 484 | 504 | 536 | 9 | 0.363 | 0.009 |
| ea-1p10 | 456 | 480 | 496 | 524 | 568 | 8 | 0.825 | 0.008 |
| ea-10p1 | 528 | 608 | 656 | 704 | 800 | 3 | 0.879 | 0.008 |
| ea-1c10 | 584 | 640 | 658 | 692 | 776 | 2 | 0.849 | 0.011 |
| ga | 456 | 480 | 504 | 516 | 560 | 6 | 1.442 | 0.008 |
| pbil | 472 | 518 | 536 | 560 | 608 | 4 | 0.898 | 0.008 |
| umda | 452 | 486 | 498 | 528 | 568 | 7 | 0.848 | 0.008 |

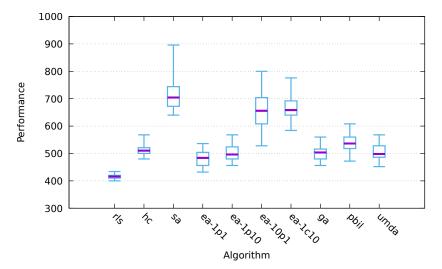


Figure 33: hiff

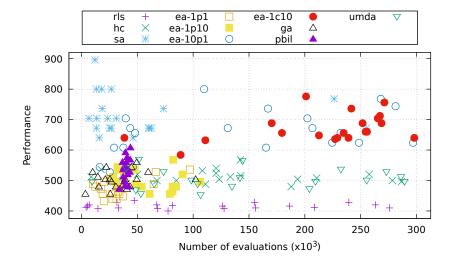


Figure 34: hiff

20 Function plateau

| algorithm | perfo | rmanc | e | | | | time (s) | | | |
|-----------|-------|-------|------------------------|-------|-----|--------|----------|-------|--|--|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. | | |
| rls | 101 | 101 | 101 | 101 | 101 | 4 | 0.071 | 0.003 | | |
| hc | 101 | 101 | 101 | 101 | 102 | 2 | 0.061 | 0.011 | | |
| sa | 101 | 101 | 101 | 102 | 102 | 1 | 0.073 | 0.022 | | |
| ea-1p1 | 101 | 101 | 101 | 101 | 102 | 2 | 0.149 | 0.012 | | |
| ea-1p10 | 101 | 101 | 101 | 101 | 101 | 4 | 0.503 | 0.009 | | |
| ea-10p1 | 101 | 101 | 101 | 101 | 101 | 4 | 0.525 | 0.012 | | |
| ea-1c10 | 101 | 101 | 101 | 101 | 101 | 4 | 0.502 | 0.004 | | |
| ga | 101 | 101 | 101 | 101 | 101 | 4 | 1.039 | 0.034 | | |
| pbil | 101 | 101 | 101 | 101 | 101 | 4 | 0.524 | 0.005 | | |
| umda | 101 | 101 | 101 | 101 | 101 | 4 | 0.511 | 0.003 | | |

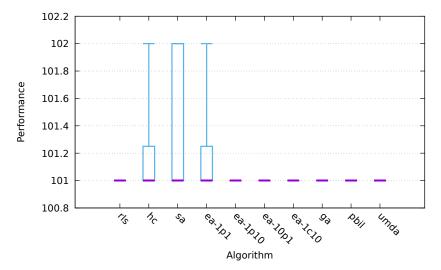


Figure 35: plateau

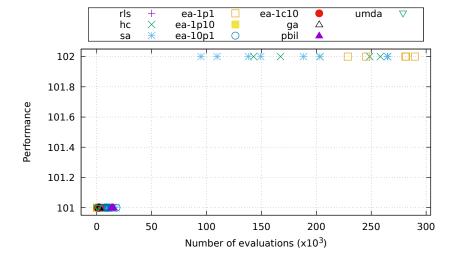


Figure 36: plateau

21 Function walsh2

| algorithm | perform | time (s) | | | | | | |
|-----------|---------|----------|------------------------|--------|--------|--------|-------|-------|
| | min | Q_1 | med . | Q_3 | max | rk | mean | dev. |
| rls | 689.45 | 696.41 | 704.22 | 707.99 | 712.93 | 4 | 2.376 | 0.093 |
| hc | 699.91 | 708.03 | 714.03 | 720.04 | 721.22 | 1 | 2.443 | 0.017 |
| sa | 697.00 | 702.06 | 709.61 | 713.69 | 721.22 | 2 | 0.487 | 0.046 |
| ea-1p1 | 636.33 | 667.22 | 687.25 | 695.02 | 721.22 | 6 | 0.665 | 0.024 |
| ea-1p10 | 609.35 | 662.43 | 672.42 | 681.70 | 716.57 | 7 | 0.913 | 0.024 |
| ea-10p1 | 660.96 | 689.76 | 699.77 | 714.70 | 721.22 | 5 | 1.268 | 0.072 |
| ea-1c10 | 688.35 | 698.69 | 707.77 | 720.24 | 721.22 | 3 | 1.222 | 0.089 |
| ga | 609.04 | 655.74 | 661.75 | 691.01 | 718.26 | 9 | 1.453 | 0.046 |
| pbil | 620.24 | 647.93 | 658.54 | 683.79 | 720.85 | 10 | 1.308 | 0.043 |
| umda | 612.24 | 652.50 | 667.96 | 684.47 | 705.37 | 8 | 0.932 | 0.019 |

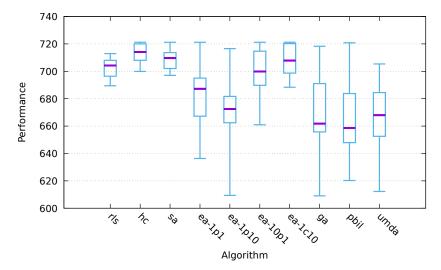


Figure 37: walsh2

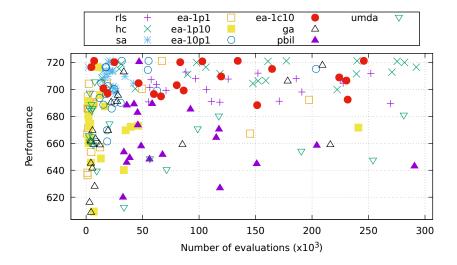


Figure 38: walsh2

22 Default parameters

```
# algorithm = 100
# bm_mc_reset_strategy = 1
# bm_num_gs_cycles = 1
# bm_num_gs_steps = 100
# bm_sampling = 1
# budget = 10000
# bv_size = 100
\# ea_lambda = 100
\# ea_mu = 10
# fun_name = noname
# fun_num_traps = 10
# fun_prefix_length = 2
# fun_threshold = 10
# function = 0
# ga_crossover_probability = 0.5
# ga_tournament_size = 10
# hea_binary_dynamics = 0
\# hea_delay = 10000
# hea_num_par_updates = 1
# hea_num_seq_updates = 100
# hea_rate_strategy = 0
# hea_reset_period = 0
# hea_sampling_method = 0
# hea_time_constant = 1000
# hea_weight = 1
# learning_rate = 0.001
# map = 0
# map_input_size = 100
# map_path = nopath
# neighborhood = 0
# neighborhood_iterator = 0
# noise_stddev = 1
# num_iterations = 0
# num_threads = 1
# path = nopath
# population_size = 10
# pv_log_num_components = 5
# radius = 2
# rls_patience = 50
# sa_initial_acceptance_probability = 0.6
# sa_num_transitions = 50
# sa_num_trials = 100
# sa_rate = 1.2
# scaled_mutation_probability = 1
\# seed = 0
# selection_size = 1
# target = 100
# print_default_parameters
# last_parameter
# exec_name = hnco
\# version = 0.7
# Generated from hnco.json
```