HNCO

Visualization of Walsh transforms of various functions defined on bit vectors

July 16, 2018

Abstract

This document proposes to visualize Walsh (or Fourier) transforms of various functions defined on bit vectors (hypercube) of size n=10. For each function, two graphics are displayed. In the first one, coefficients of the Walsh transform are sorted in decreasing order of amplitude and normalized relatively to the largest amplitude. The second graphics displays the energy (sum of square of coefficients) as a function of the Hamming weight of features. This can be thought of as a spectrum. Coefficients c such that $0 < |c/c_{\rm max}| < 10^{-15}$ have been filtered out as they mostly result from accumulated errors in floating point arithmetic.

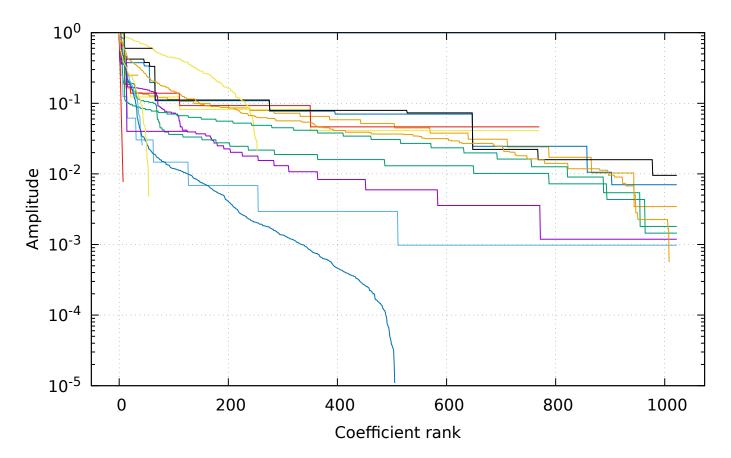
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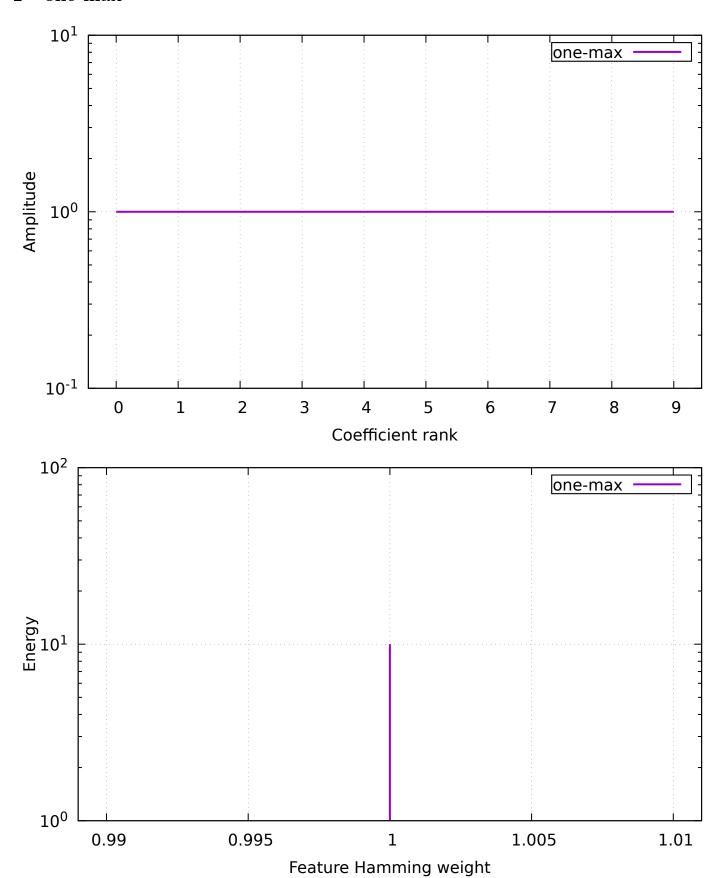
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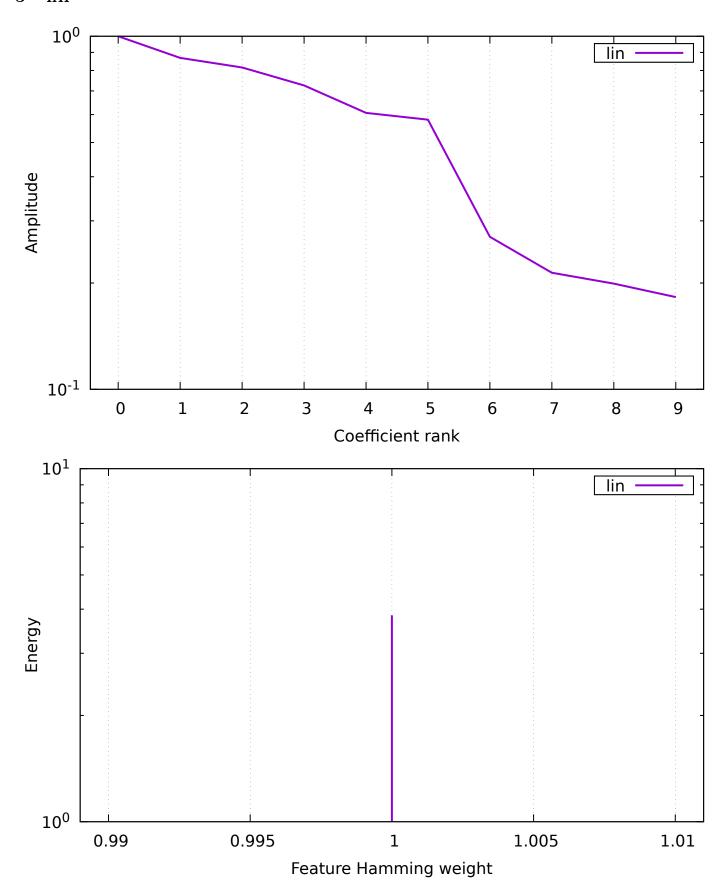
1 All functions



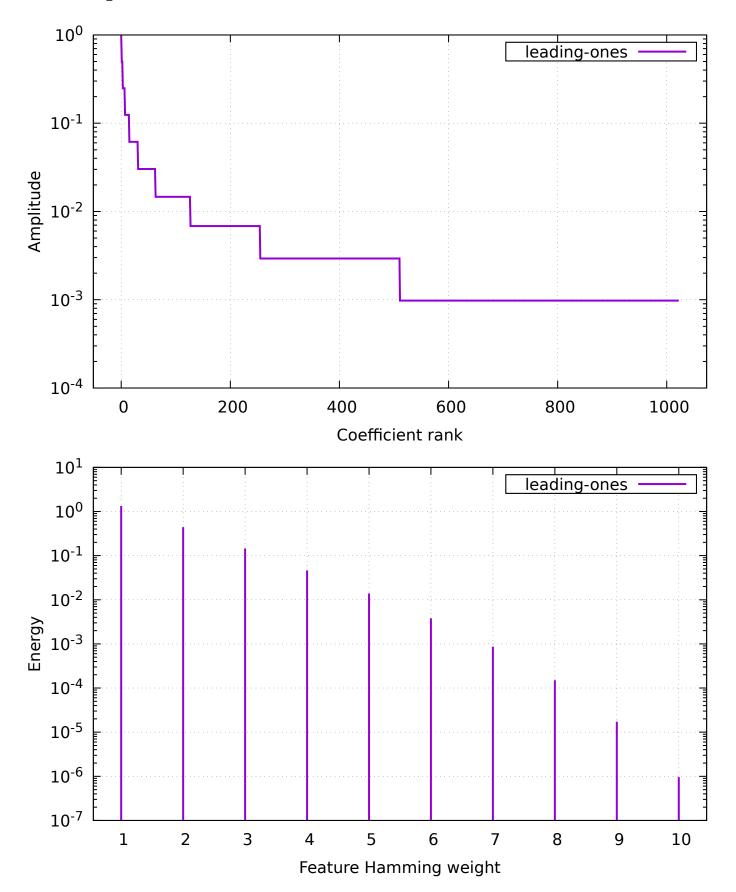
2 one-max



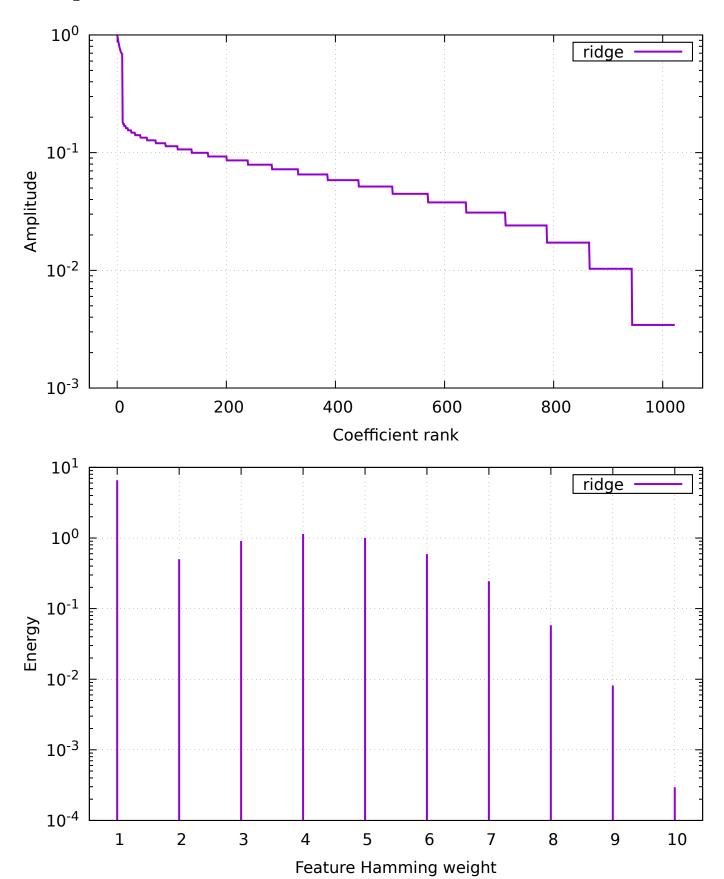


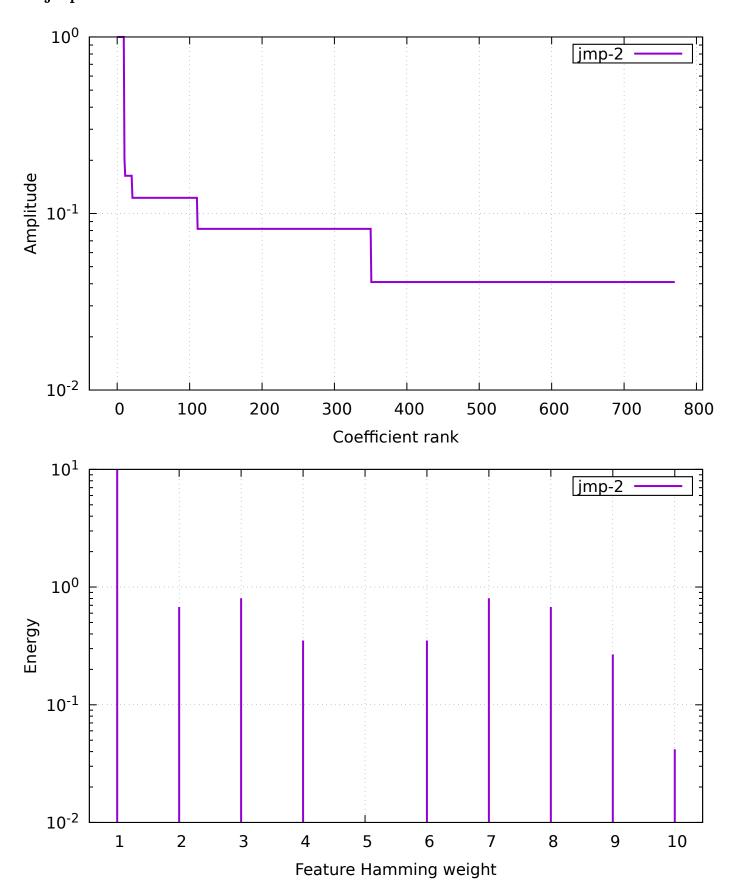


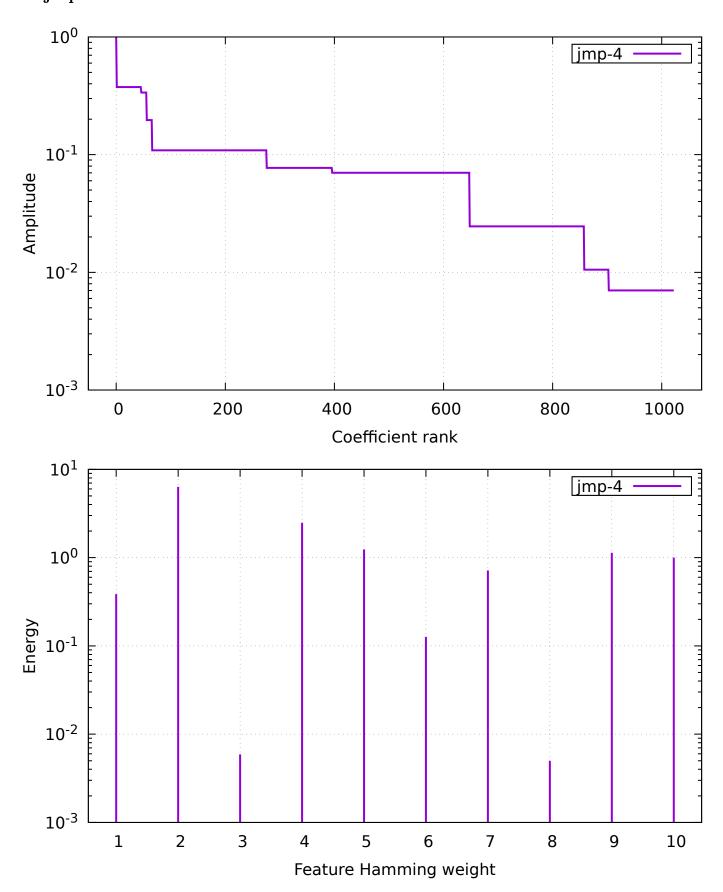
4 leading-ones

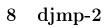


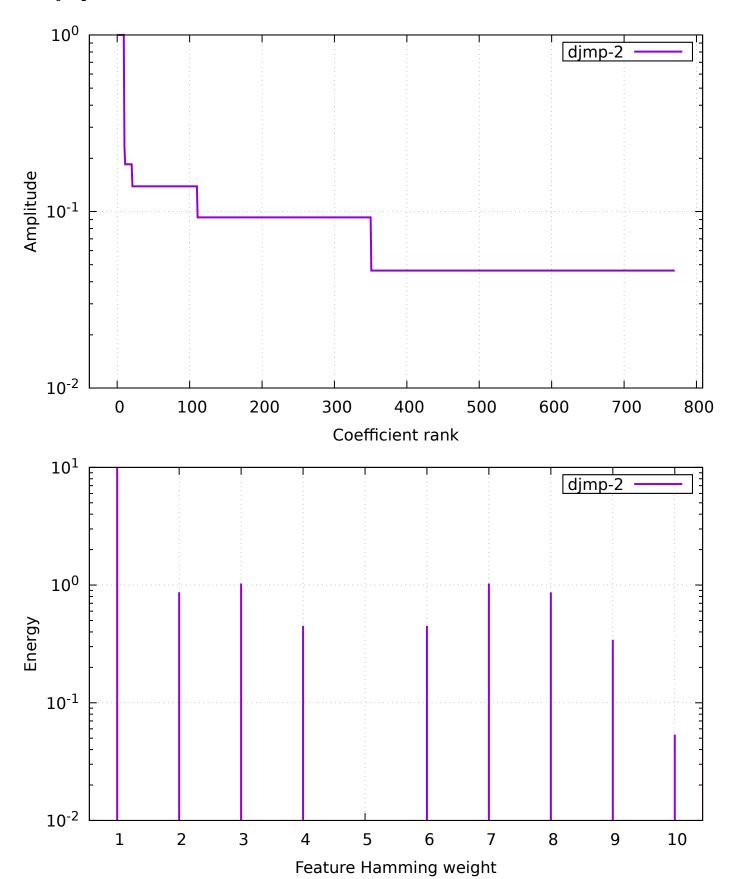




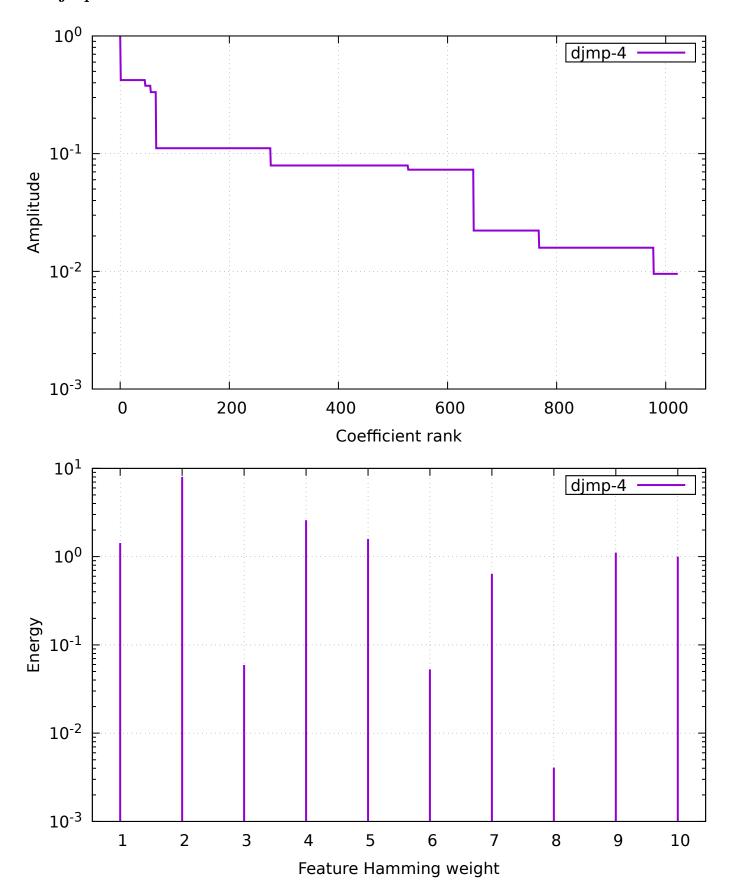




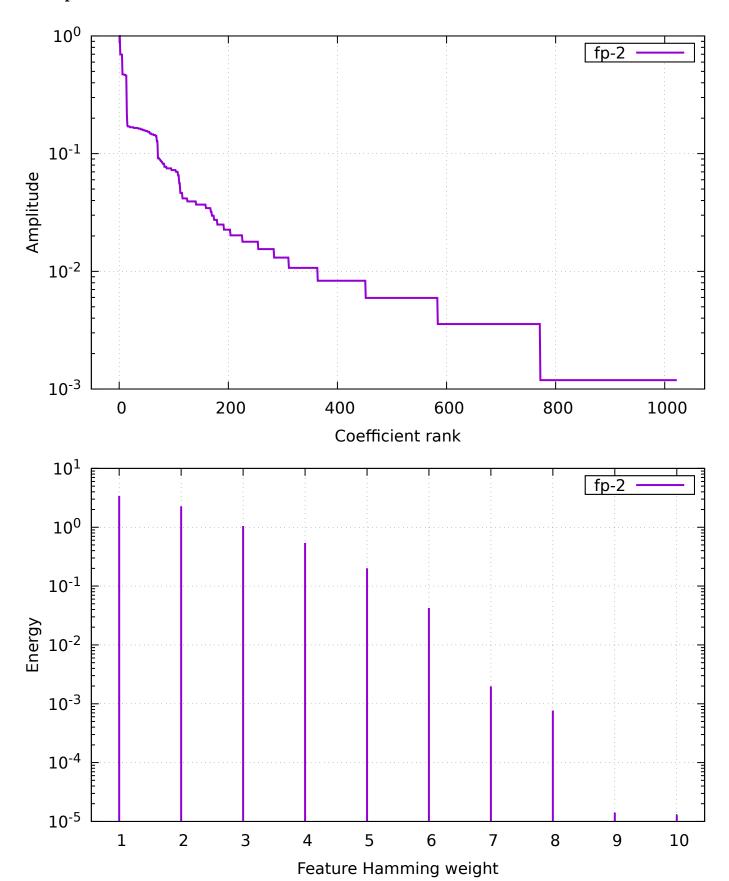




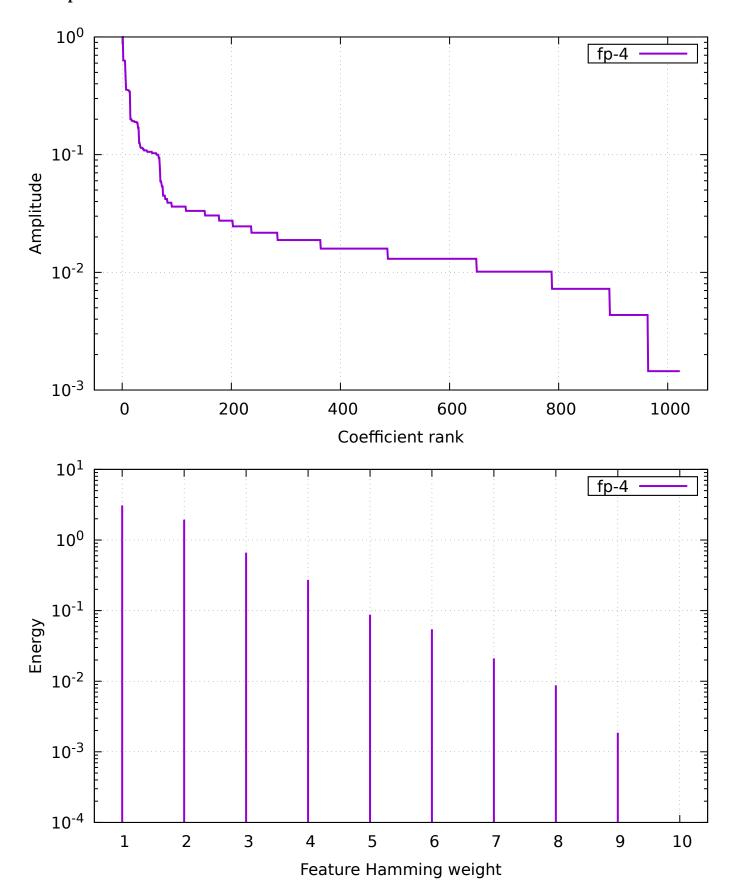
9 djmp-4



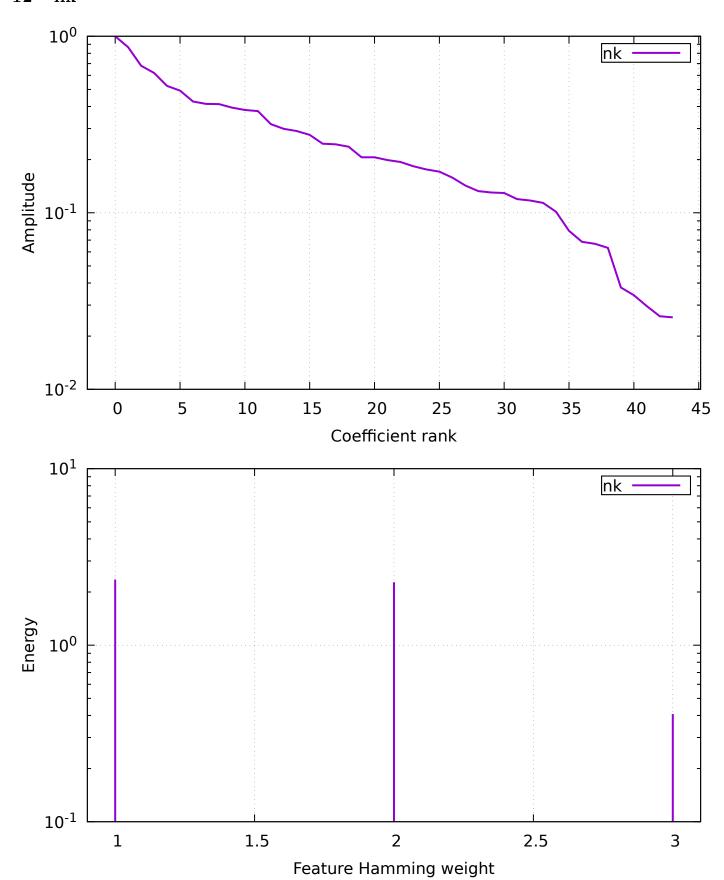




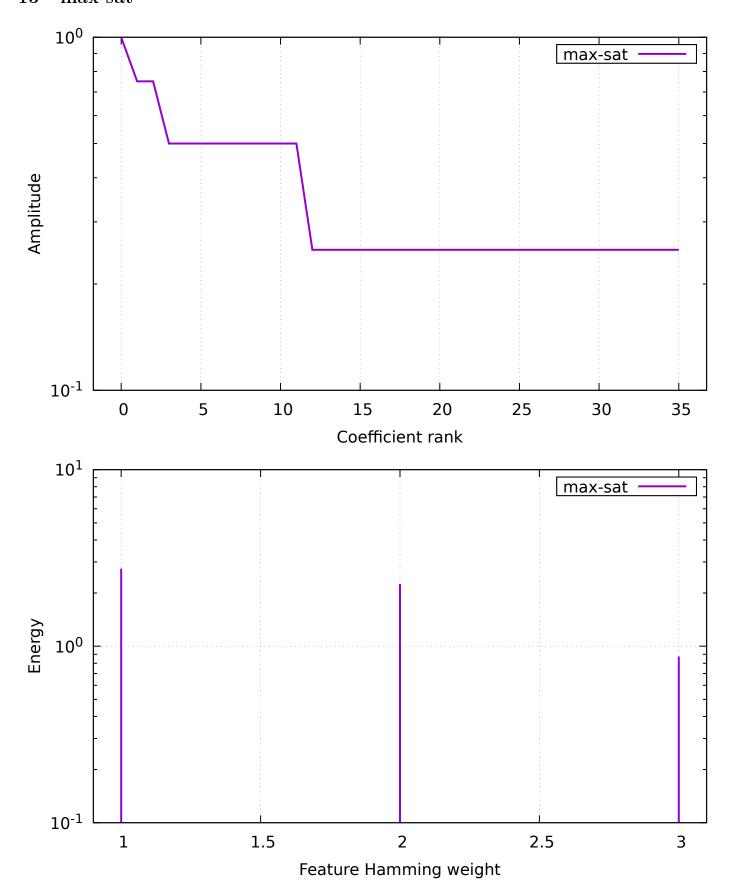




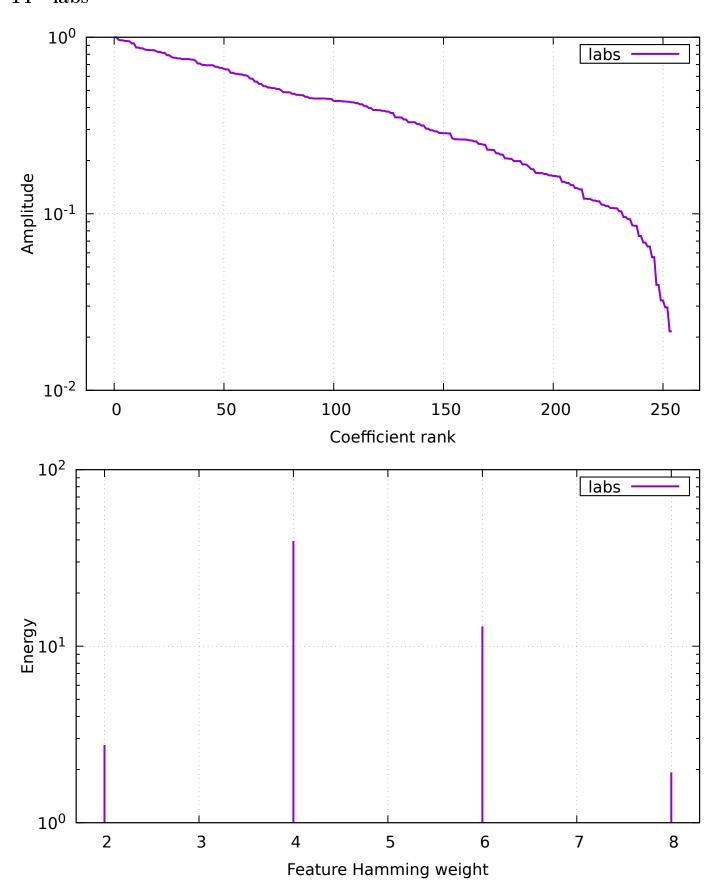




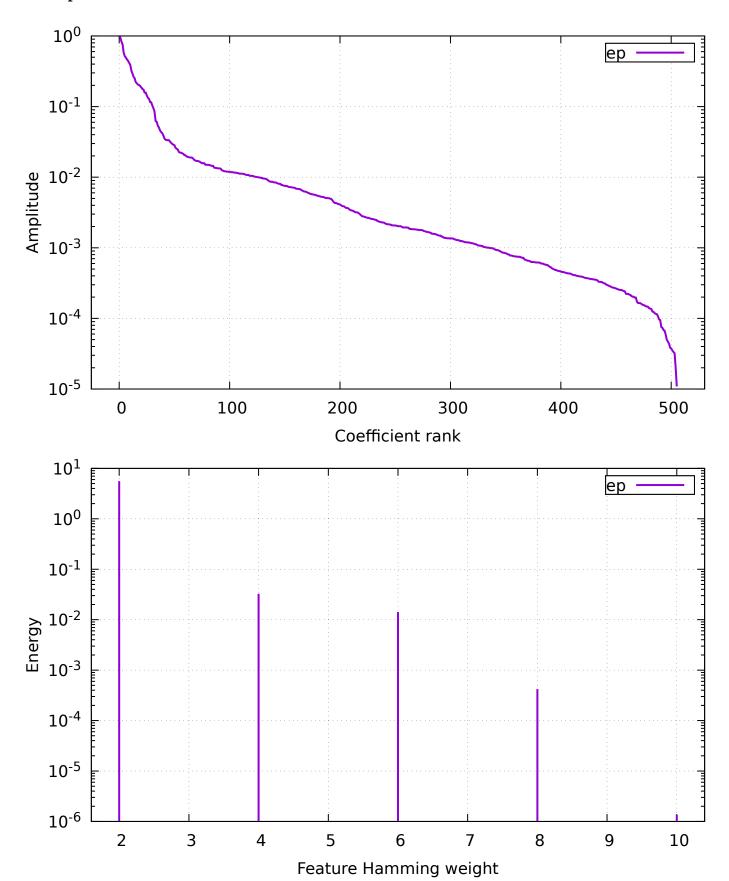
13 max-sat



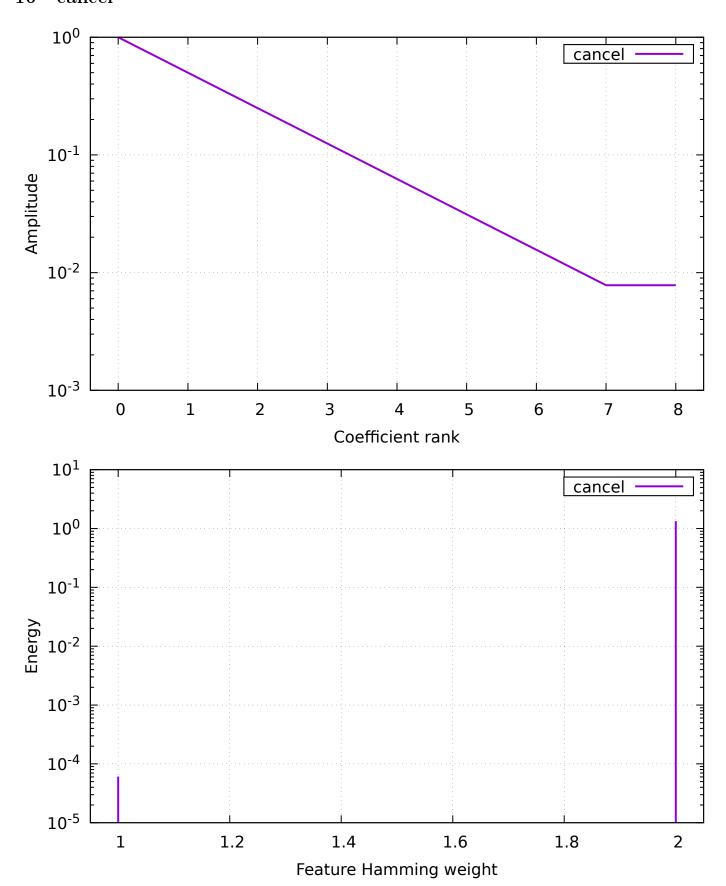
14 labs



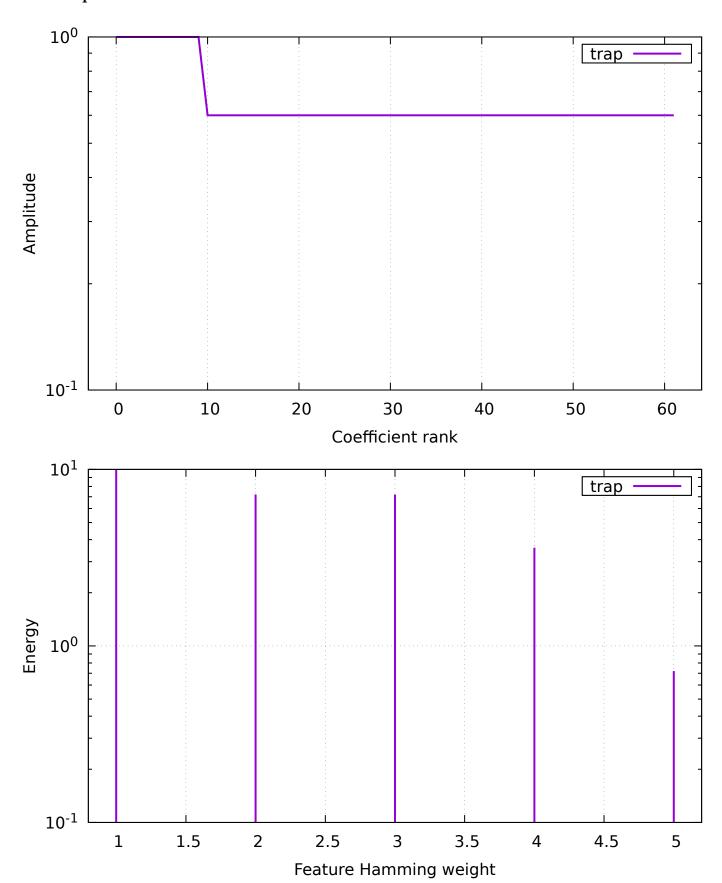




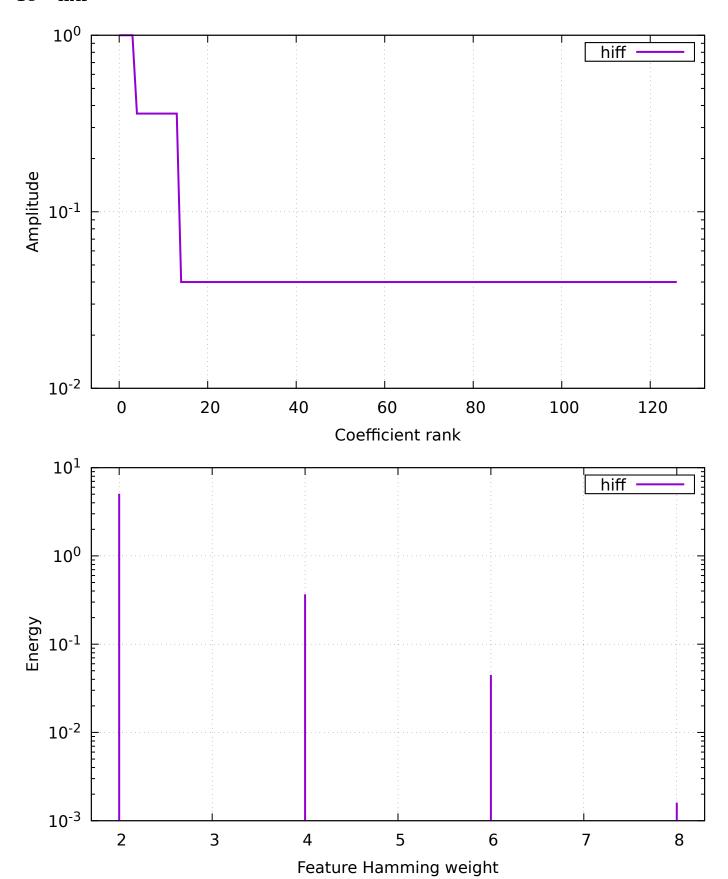
16 cancel



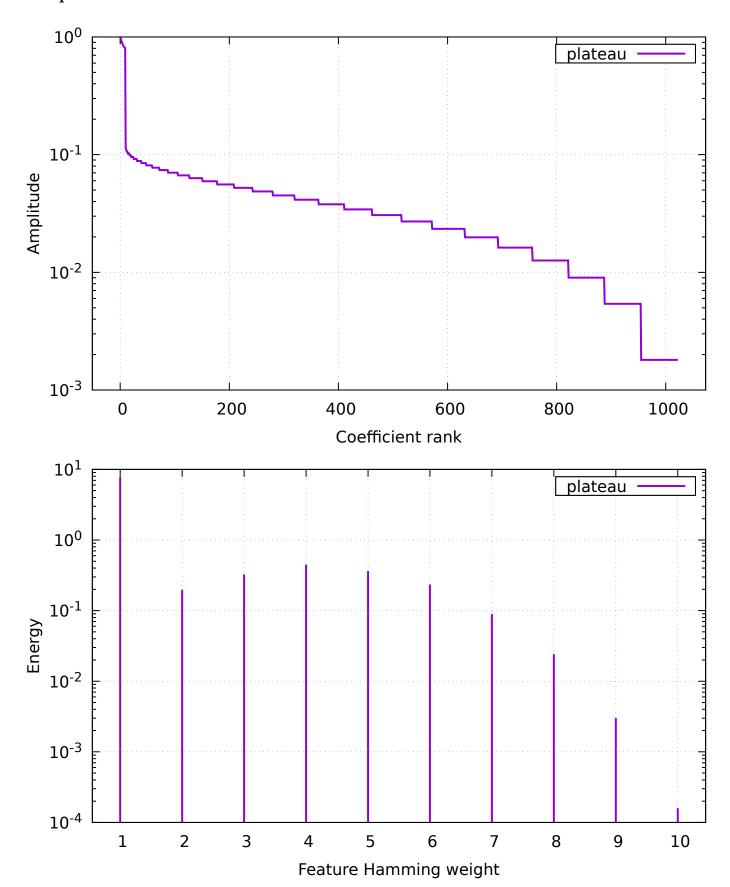


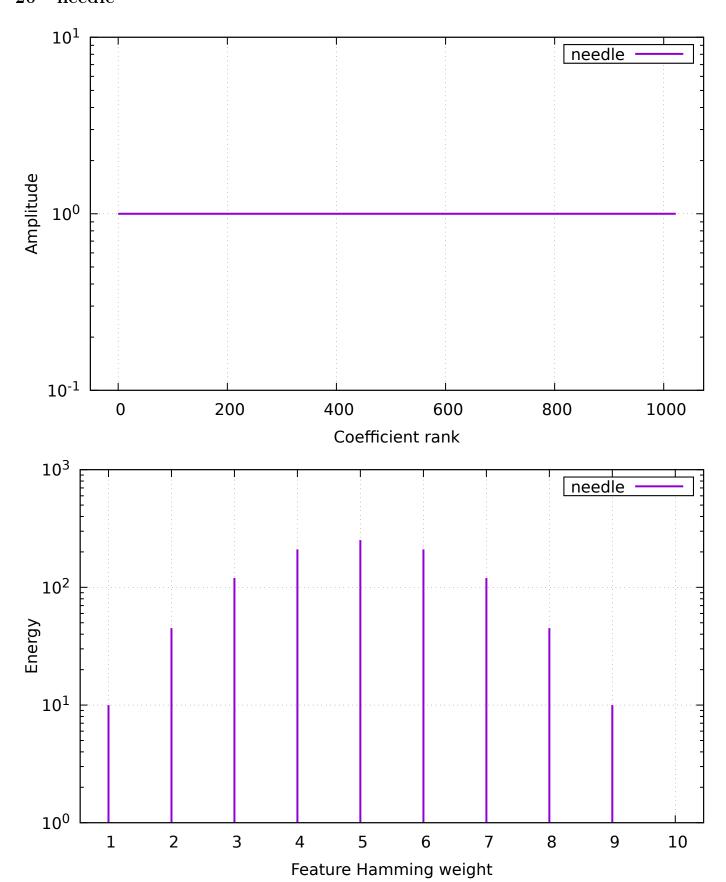




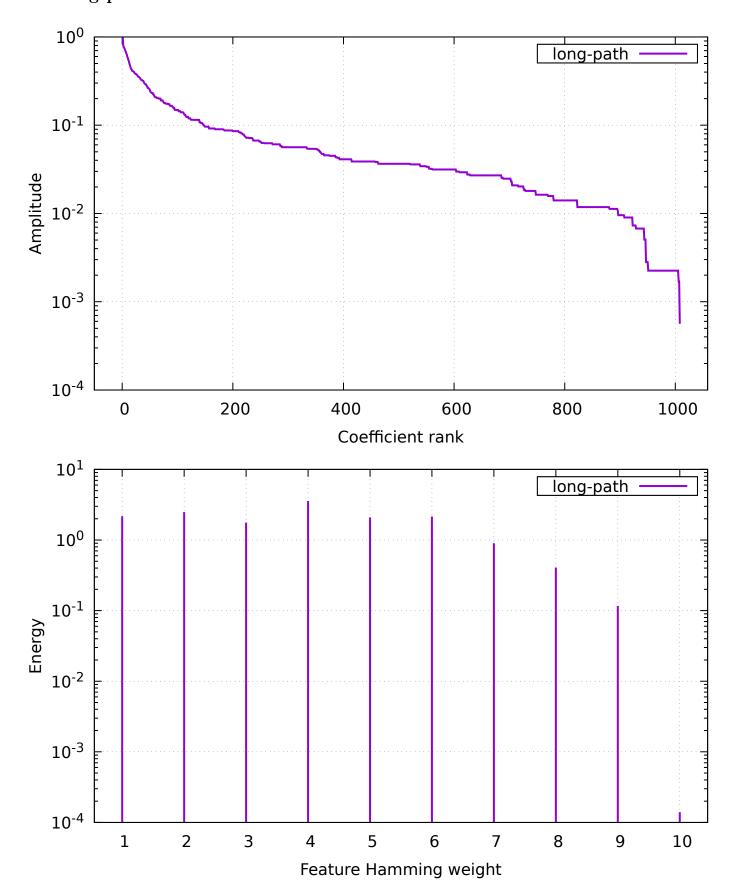


19 plateau

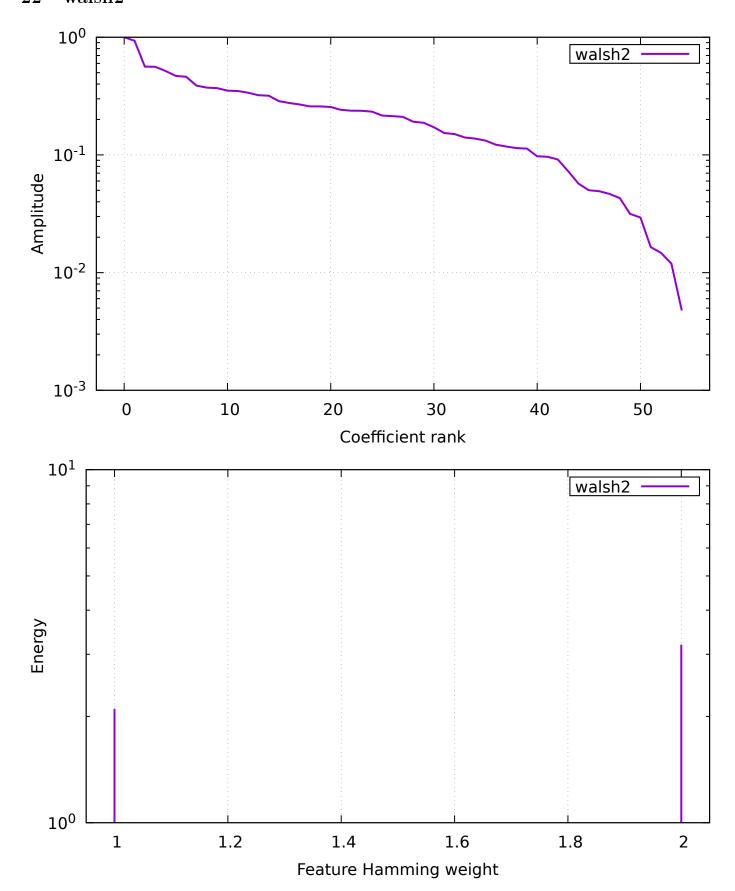




21 long-path



22 walsh2



A Plan

```
{
   "exec": "hnco",
   "opt": "--fn-walsh-transform -b 0 -s 10",
```

```
"parallel": true,
"results": "results",
"graphics": "graphics",
"report": "report",
"functions": [
    {
        "id": "one-max",
        "opt": "-F 0"
    },
        "id": "lin",
        "opt": "-F 1 -p instances/lin.10"
   },
        "id": "leading-ones",
        "opt": "-F 10"
    },
        "id": "ridge",
        "opt": "-F 11"
   },
        "id": "jmp-2",
        "opt": "-F 30 -t 2"
    },
        "id": "jmp-4",
        "opt": "-F 30 -t 4"
   },
        "id": "djmp-2",
        "opt": "-F 31 -t 2"
    },
        "id": "djmp-4",
        "opt": "-F 31 -t 4"
   },
        "id": "fp-2",
        "opt": "-F 40 -t 2"
    },
        "id": "fp-4",
        "opt": "-F 40 -t 4"
    },
        "id": "nk",
        "opt": "-F 60 -p instances/nk.10.2"
    },
        "id": "max-sat",
        "opt": "-F 70 -p instances/ms.10.3.10"
    },
        "id": "labs",
        "opt": "-F 80"
    },
        "id": "ep",
        "opt": "-F 90 -p instances/ep.10"
   },
    {
        "id": "cancel",
```

```
"opt": "-F 100 -s 9"
    },
        "id": "trap",
        "opt": "-F 110 --fn-num-traps 2"
    },
        "id": "hiff",
        "opt": "-F 120 -s 8"
    },
        "id": "plateau",
        "opt": "-F 130"
    },
        "id": "needle",
        "opt": "-F 20"
    },
        "id": "long-path",
        "opt": "-F 140"
    },
        "id": "walsh2",
        "opt": "-F 162 -p instances/walsh2.10"
]
```

B Default parameters

}

```
# algorithm = 100
# bm_mc_reset_strategy = 1
# bm_num_gs_cycles = 1
# bm_num_gs_steps = 100
# bm_sampling = 1
# budget = 10000
# bv_size = 100
# cache_budget = 0
\# ea_lambda = 100
\# ea_mu = 10
# fn_name = noname
# fn_num_traps = 10
# fn_prefix_length = 2
# fn_threshold = 10
# function = 0
# ga_crossover_bias = 0.5
# ga_crossover_probability = 0.5
# ga_tournament_size = 10
# hea_binary_dynamics = 0
\# hea_delay = 10000
# hea_num_par_updates = 1
# hea_num_seq_updates = 100
# hea_rate_strategy = 0
# hea_reset_period = 0
# hea_sampling_method = 0
# hea_time_constant = 1000
# hea_weight = 1
# learning_rate = 0.001
\# map = 0
# map_input_size = 100
# map_path = nopath
```

```
# mutation_probability = 1
# neighborhood = 0
# neighborhood_iterator = 0
# noise_stddev = 1
# num_iterations = 0
# num_threads = 1
# path = nopath
# pn_mutation_probability = 1
# pn_neighborhood = 0
# pn_radius = 2
# population_size = 10
# pv_log_num_components = 5
# radius = 2
# rls_patience = 50
# sa_beta_ratio = 1.2
# sa_initial_acceptance_probability = 0.6
# sa_num_transitions = 50
# sa_num_trials = 100
\# seed = 0
# selection_size = 1
# target = 100
# print_defaults
# last_parameter
# exec_name = hnco
\# version = 0.9
# Generated from hnco.json
```