## HNCO

# Influence of the learning rate on the performance of PBIL

#### November 1, 2017

#### Abstract

PBIL is applied many times to the same collection of fitness functions (bit vector size n = 100), each time with a different learning rate taken from a finite set of values. All learning rates are ranked according to their median fitness over 20 independent runs, first for each fitness function, then across the entire collection of fitness functions. The mean and standard deviation of fitness are also plotted as a function of the learning rate.

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#### 1 Plan

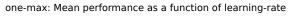
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"num_runs": 20,
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    "values": [ 1e-2, 2e-2, 5e-2, 1e-1, 2e-1, 5e-1, 1 ],
    "logscale": true,
    "boxwidth": "$1 * 0.3"
},
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        "opt": "-F 10 --stop-on-maximum",
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    },
        "id": "jmp-5",
        "opt": "-F 30 --stop-on-maximum -t 5",
        "col": ">{{\\nprounddigits{0}}}N{3}{0}"
    },
        "id": "nk",
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    },
        "id": "max-sat",
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        "id": "cancel",
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        "reverse": true,
        "col": ">{{\\nprounddigits{2}}}N{1}{2}"
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```

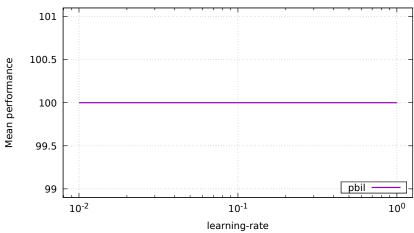
## 2 Rankings

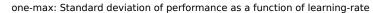
algorithm	learning-rate	rai	nk d	istri	ibut	ion		
		1	2	3	4	5	6	7
pbil	1	7	0	0	1	0	1	0
pbil	0.01	4	2	0	2	1	0	0
pbil	0.02	3	2	2	1	1	0	0
pbil	0.05	3	0	1	1	$^{2}$	2	0
pbil	0.5	2	2	2	1	0	1	1
pbil	0.2	2	0	1	0	1	2	3
pbil	0.1	2	0	0	1	2	2	2

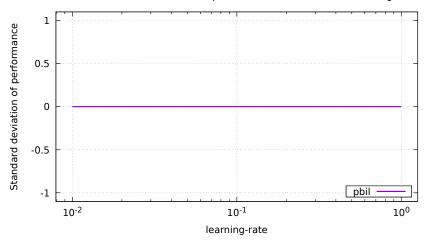
## 3 Function one-max

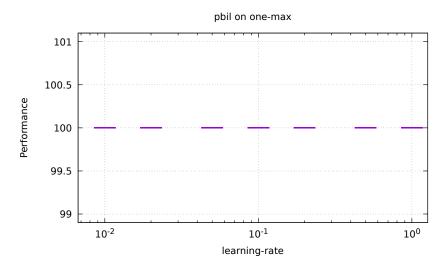
algorithm	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	100	100	100	100	100	1
pbil	0.02	100	100	100	100	100	1
pbil	0.05	100	100	100	100	100	1
pbil	0.1	100	100	100	100	100	1
pbil	0.2	100	100	100	100	100	1
pbil	0.5	100	100	100	100	100	1
pbil	1	100	100	100	100	100	1







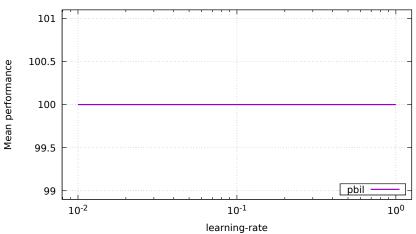




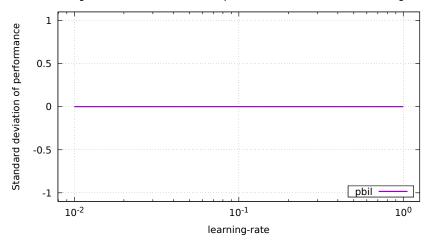
## 4 Function leading-ones

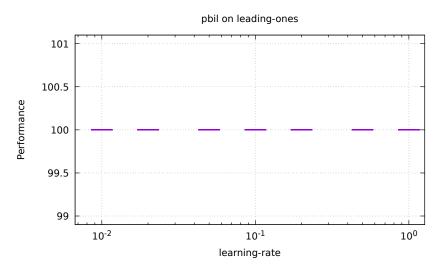
$\overline{ ext{algorithm}}$	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	100	100	100	100	100	1
pbil	0.02	100	100	100	100	100	1
pbil	0.05	100	100	100	100	100	1
pbil	0.1	100	100	100	100	100	1
pbil	0.2	100	100	100	100	100	1
pbil	0.5	100	100	100	100	100	1
pbil	1	100	100	100	100	100	1

leading-ones: Mean performance as a function of learning-rate





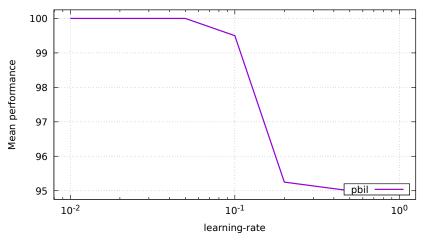




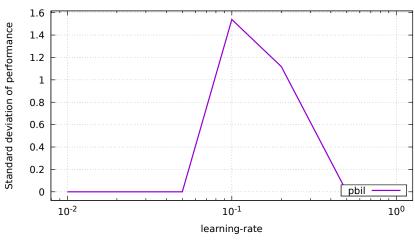
## 5 Function jmp-5

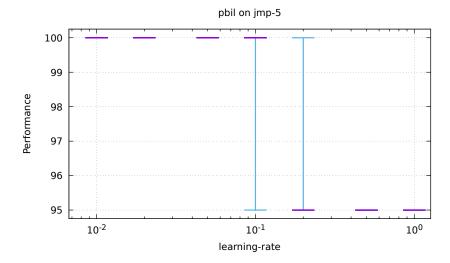
$\overline{ ext{algorithm}}$	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	100	100	100	100	100	1
pbil	0.02	100	100	100	100	100	1
pbil	0.05	100	100	100	100	100	1
pbil	0.1	95	100	100	100	100	4
pbil	0.2	95	95	95	95	100	5
pbil	0.5	95	95	95	95	95	6
pbil	1	95	95	95	95	95	6

jmp-5: Mean performance as a function of learning-rate



jmp-5: Standard deviation of performance as a function of learning-rate

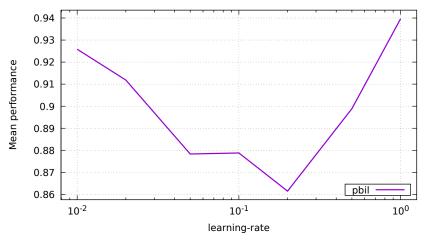


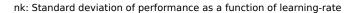


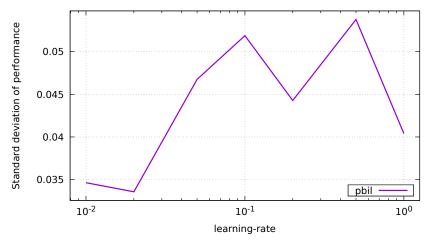
## 6 Function nk

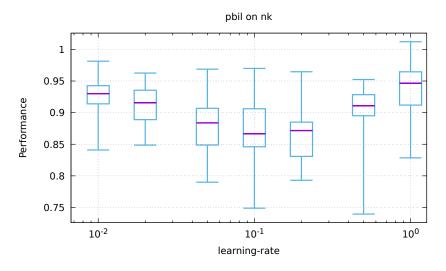
$\overline{ ext{algorithm}}$	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	0.84	0.91	0.93	0.94	0.98	2
pbil	0.02	0.85	0.89	0.92	0.94	0.96	3
pbil	0.05	0.79	0.85	0.88	0.91	0.97	5
pbil	0.1	0.75	0.85	0.87	0.91	0.97	7
pbil	0.2	0.79	0.83	0.87	0.88	0.96	6
pbil	0.5	0.74	0.90	0.91	0.93	0.95	4
pbil	1	0.83	0.91	0.95	0.96	1.01	1

nk: Mean performance as a function of learning-rate





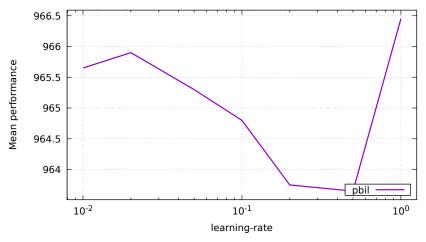




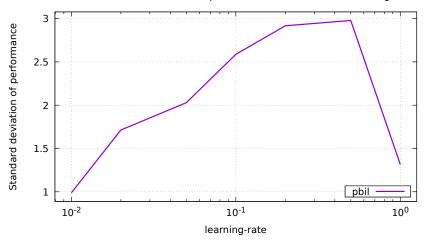
## 7 Function max-sat

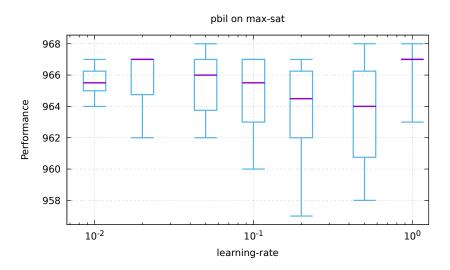
$\overline{ ext{algorithm}}$	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	964	965	966	966	967	4
pbil	0.02	962	965	967	967	967	2
pbil	0.05	962	964	966	967	968	3
pbil	0.1	960	963	966	967	967	5
pbil	0.2	957	962	965	966	967	6
pbil	0.5	958	961	964	966	968	7
pbil	1	963	967	967	967	968	1

max-sat: Mean performance as a function of learning-rate





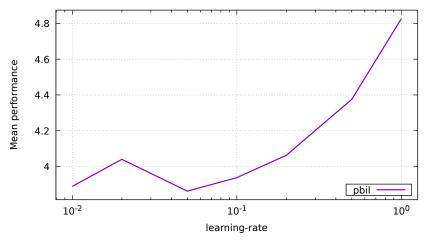




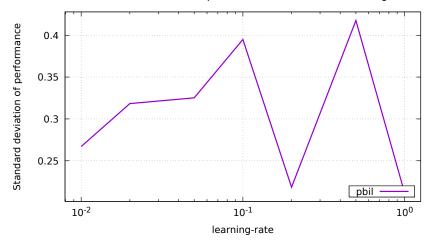
## 8 Function labs

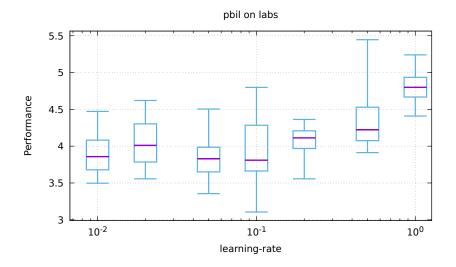
$\overline{ ext{algorithm}}$	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	3.50	3.68	3.86	4.08	4.47	5
pbil	0.02	3.56	3.79	4.01	4.30	4.62	4
pbil	0.05	3.36	3.65	3.83	3.99	4.50	6
pbil	0.1	3.11	3.66	3.81	4.28	4.80	7
pbil	0.2	3.56	3.97	4.11	4.21	4.36	3
pbil	0.5	3.91	4.07	4.22	4.53	5.45	2
pbil	1	4.41	4.67	4.80	4.94	5.24	1

labs: Mean performance as a function of learning-rate





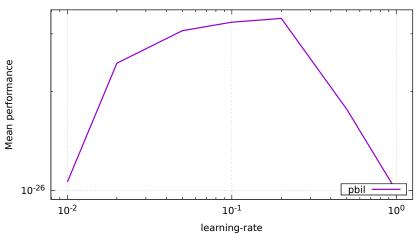




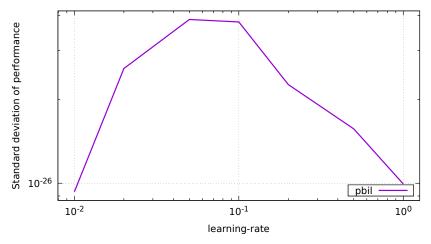
## 9 Function ep

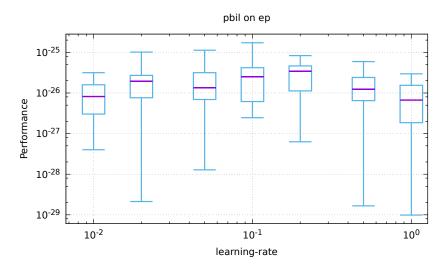
$\overline{ ext{algorithm}}$	learning-rate	min	$Q_1$	med.	$Q_3$	max	rk
pbil	0.01	$4.0 \times 10^{-28}$	$3.0 \times 10^{-27}$	$8.2 \times 10^{-27}$	$1.6 \times 10^{-26}$	$3.2 \times 10^{-26}$	2
pbil	0.02	$2.1 \times 10^{-29}$	$7.6 \times 10^{-27}$	$1.9 \times 10^{-26}$	$2.7 \times 10^{-26}$	$1.0 \times 10^{-25}$	5
pbil	0.05	$1.3\times10^{-28}$	$6.9 \times 10^{-27}$	$1.3\times10^{-26}$	$3.2 \times 10^{-26}$	$1.1 \times 10^{-25}$	4
pbil	0.1	$2.5 \times 10^{-27}$	$6.1 \times 10^{-27}$	$2.5 \times 10^{-26}$	$4.2 \times 10^{-26}$	$1.7 \times 10^{-25}$	6
pbil	0.2	$6.3\times10^{-28}$	$1.1 \times 10^{-26}$	$3.4 \times 10^{-26}$	$4.6 \times 10^{-26}$	$8.3 \times 10^{-26}$	7
pbil	0.5	$1.7 \times 10^{-29}$	$6.5 \times 10^{-27}$	$1.2 \times 10^{-26}$	$2.4\times10^{-26}$	$5.9\times10^{-26}$	3
pbil	1	$9.9 \times 10^{-30}$	$1.9 \times 10^{-27}$	$6.7 \times 10^{-27}$	$1.5 \times 10^{-26}$	$3.0 \times 10^{-26}$	1

ep: Mean performance as a function of learning-rate





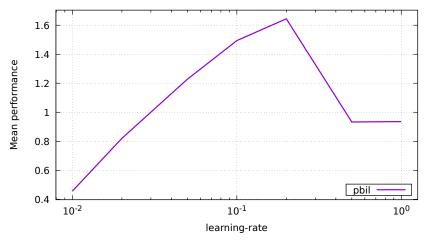




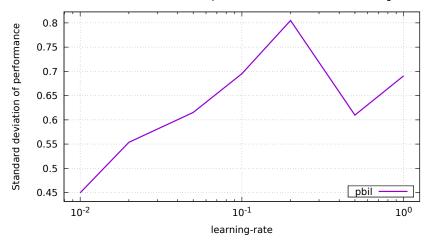
## 10 Function cancel

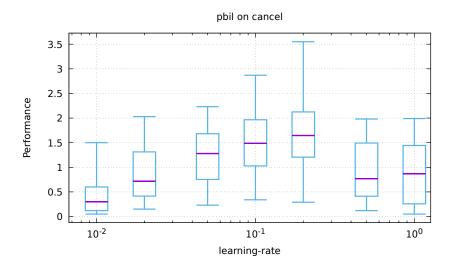
algorithm	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	0.05	0.12	0.30	0.60	1.50	1
pbil	0.02	0.15	0.42	0.72	1.31	2.03	2
pbil	0.05	0.23	0.75	1.28	1.68	2.23	5
pbil	0.1	0.34	1.03	1.49	1.97	2.87	6
pbil	0.2	0.29	1.21	1.65	2.13	3.55	7
pbil	0.5	0.12	0.41	0.77	1.49	1.98	3
pbil	1	0.05	0.26	0.87	1.44	1.99	4

cancel: Mean performance as a function of learning-rate





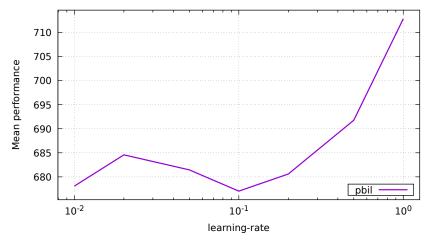




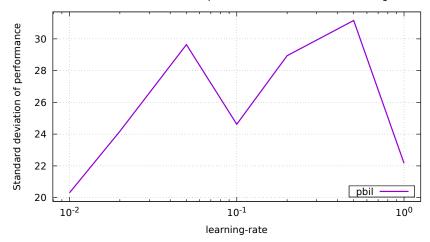
## 11 Function walsh2

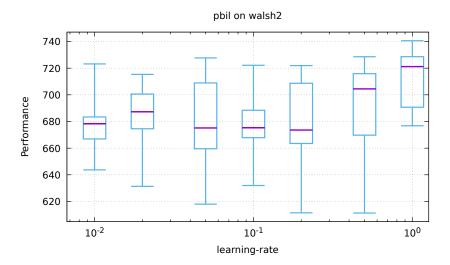
algorithm	learning-rate	min	$Q_1$	$\operatorname{med}$ .	$Q_3$	max	rk
pbil	0.01	643.68	666.90	678.34	683.40	723.16	$\overline{4}$
pbil	0.02	631.35	674.53	687.20	700.56	715.33	3
pbil	0.05	618.02	659.54	675.12	708.89	727.67	6
pbil	0.1	631.98	667.83	675.26	688.39	722.11	5
pbil	0.2	611.50	663.49	673.61	708.69	721.90	7
pbil	0.5	611.32	669.75	704.39	715.85	728.55	2
pbil	1	676.79	690.69	721.20	728.62	740.55	1

walsh2: Mean performance as a function of learning-rate



walsh2: Standard deviation of performance as a function of learning-rate





#### 12 Default parameters

```
# algorithm = 100
# bm_mc_reset_strategy = 1
# bm_num_gs_cycles = 1
# bm_num_gs_steps = 100
# bm_sampling = 1
# budget = 10000
# bv_size = 100
\# ea_lambda = 100
\# ea_mu = 10
# fun_name = noname
# fun_num_traps = 10
# fun_prefix_length = 2
# fun_threshold = 10
# function = 0
# ga_crossover_probability = 0.5
# ga_tournament_size = 10
# hea_binary_dynamics = 0
\# hea_delay = 10000
# hea_num_par_updates = 1
# hea_num_seq_updates = 100
# hea_rate_strategy = 0
# hea_reset_period = 0
# hea_sampling_method = 0
# hea_time_constant = 1000
# hea_weight = 1
# learning_rate = 0.001
# map = 0
# map_input_size = 100
# map_path = nopath
# neighborhood = 0
# neighborhood_iterator = 0
# noise_stddev = 1
# num_iterations = 0
# num_threads = 1
# path = nopath
# population_size = 10
# pv_log_num_components = 5
# radius = 2
# rls_patience = 50
# sa_initial_acceptance_probability = 0.6
# sa_num_transitions = 50
# sa_num_trials = 100
# sa_rate = 1.2
# scaled_mutation_probability = 1
\# seed = 0
# selection_size = 1
# target = 100
# print_default_parameters
# last_parameter
# exec_name = hnco
\# version = 0.7
# Generated from hnco.json
```