

HNCO

Visualization of Walsh transforms

of various functions defined on bit vectors

August 7, 2020

Abstract

This document proposes a visualization of Walsh (or Fourier) transforms of various functions defined on bit vectors (hypercube) of size $n = 10$. For each function, two graphics are displayed. In the first one, coefficients of the Walsh transform are sorted in decreasing order of amplitude and normalized relatively to the largest amplitude. The second graphics displays the energy (sum of squares of coefficients) as a function of the feature Hamming weight. This can be thought of as a power spectrum. The coefficient of the feature zero has been filtered out. Coefficients c such that $0 < |c/c_{\max}| < 10^{-10}$ have also been filtered out as they mostly result from accumulated errors in floating point arithmetic.

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22 walsh2

23

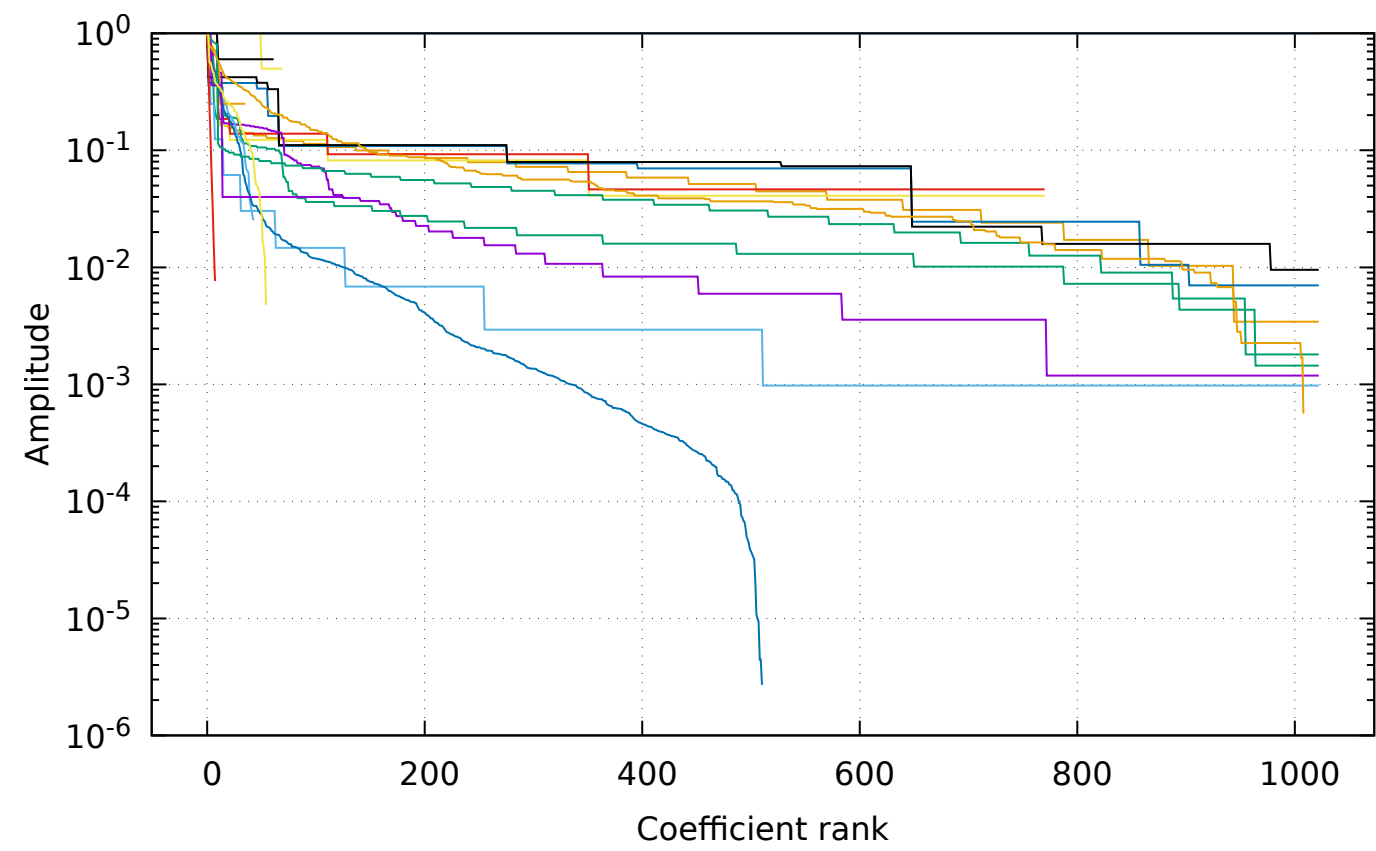
A Plan

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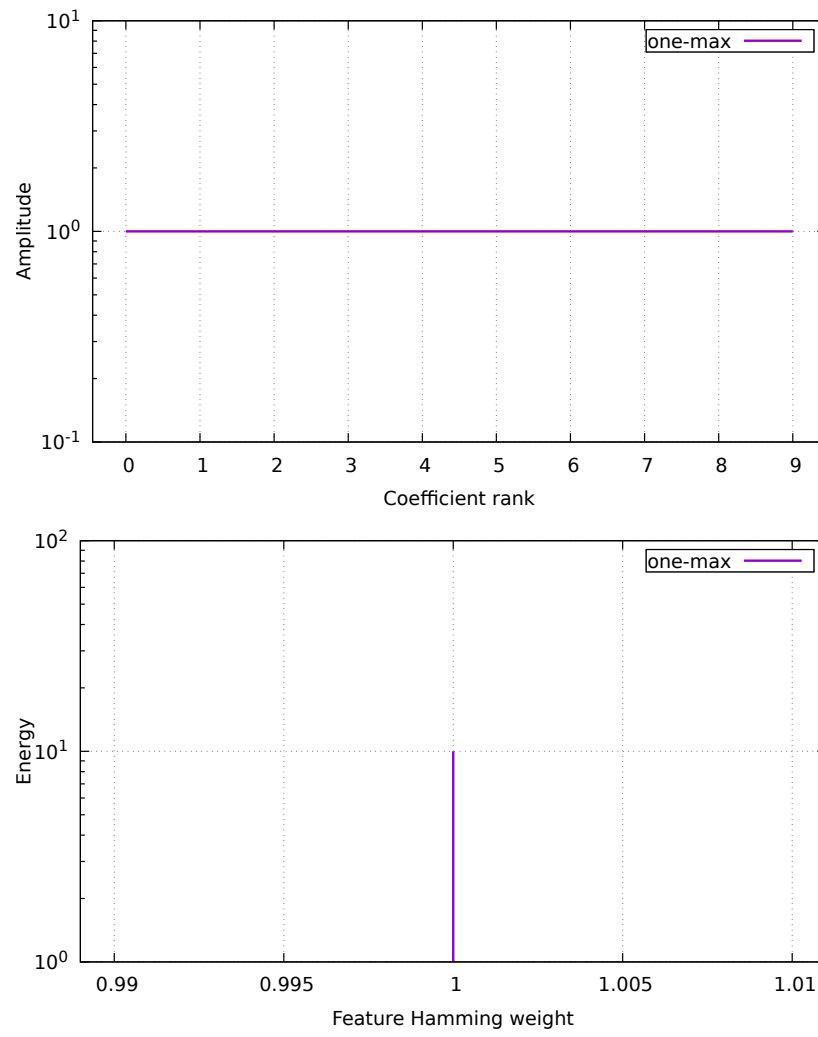
B Default parameters

25

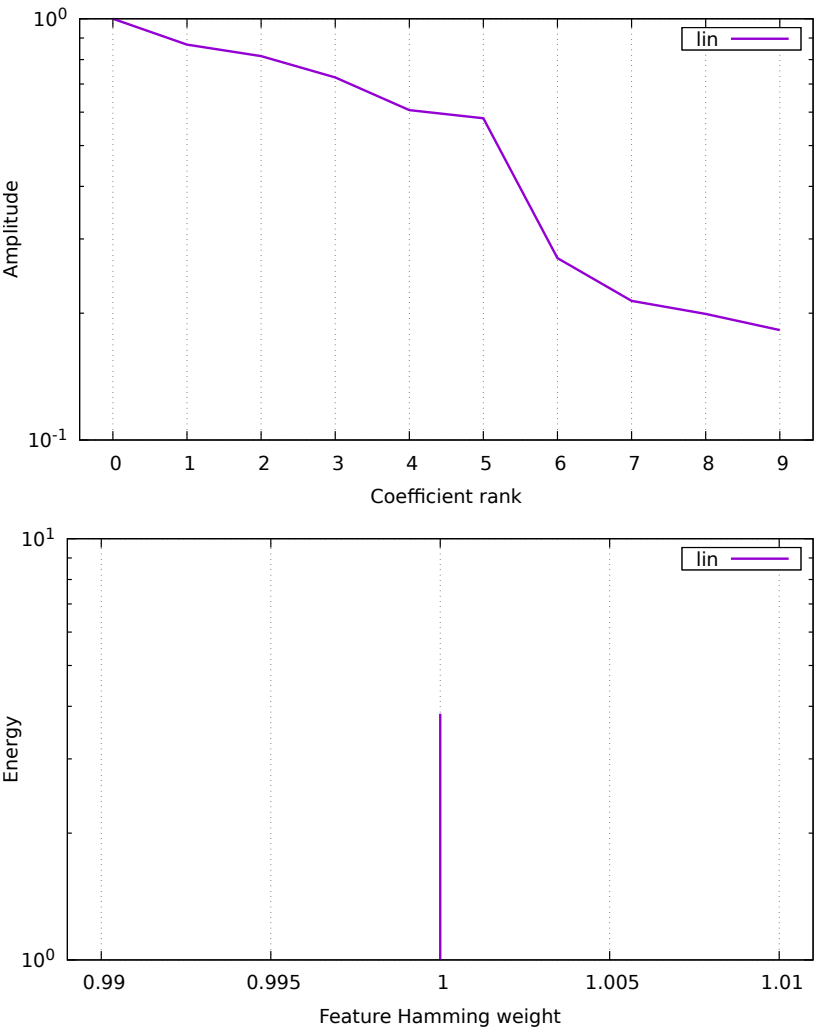
1 All functions



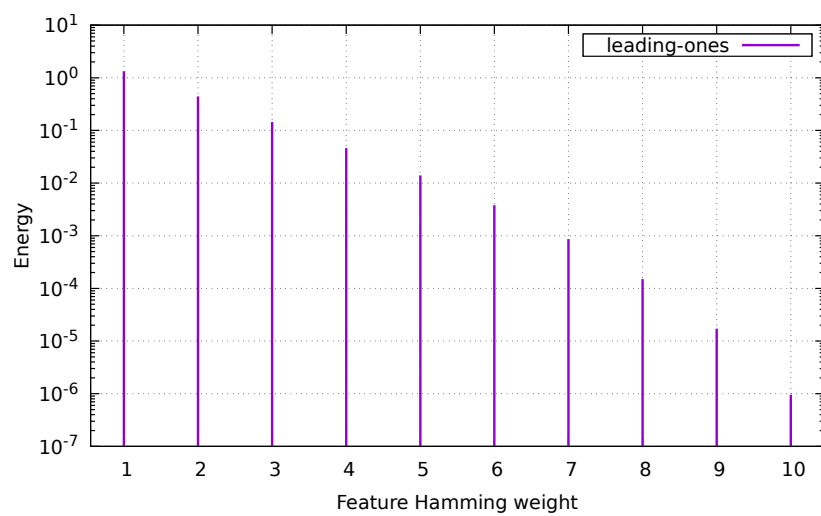
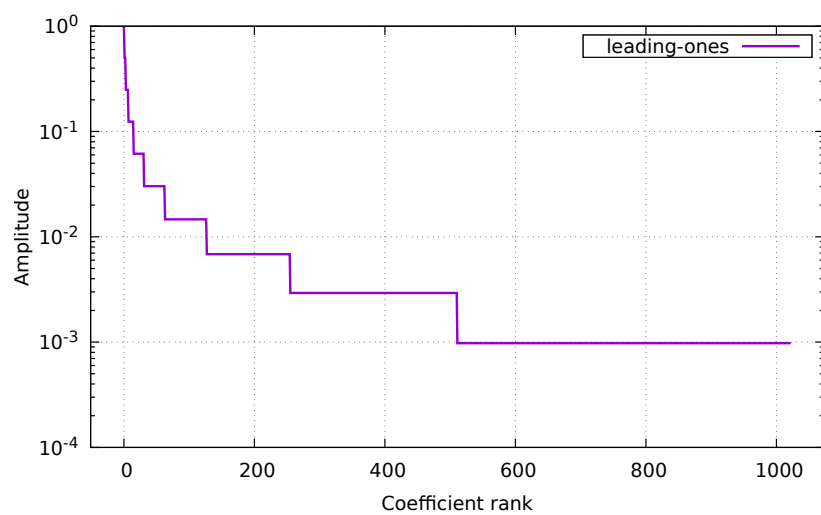
2 one-max



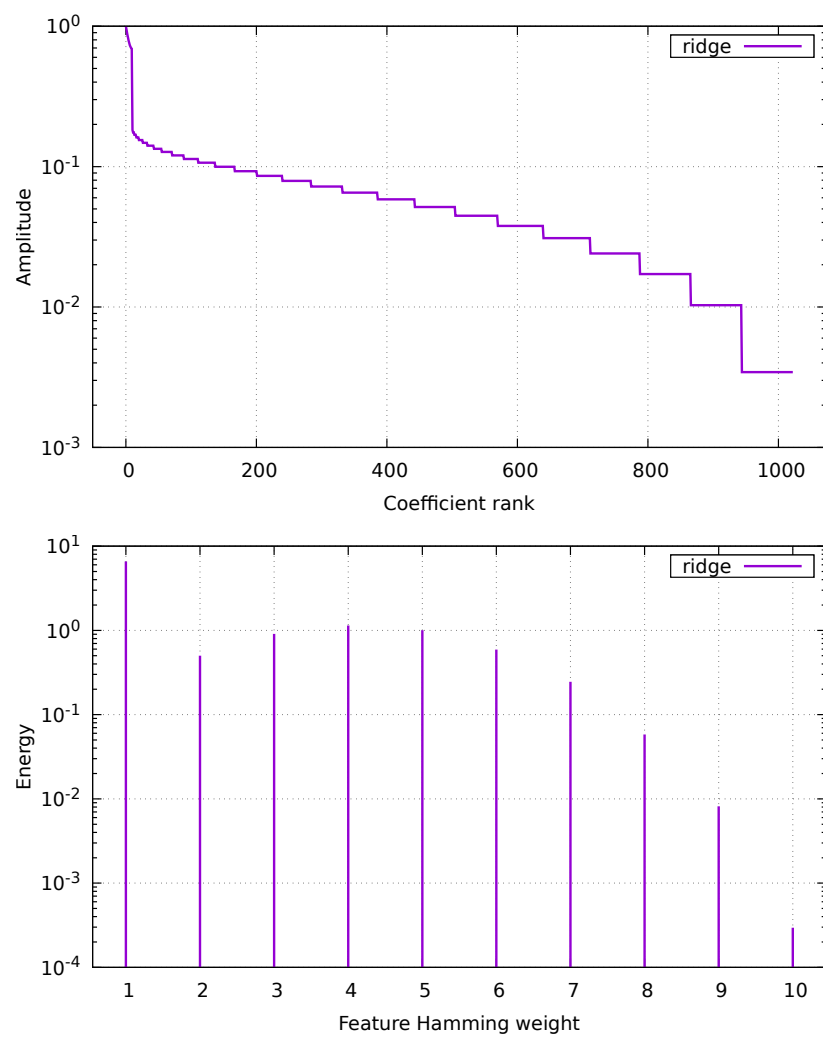
3 lin



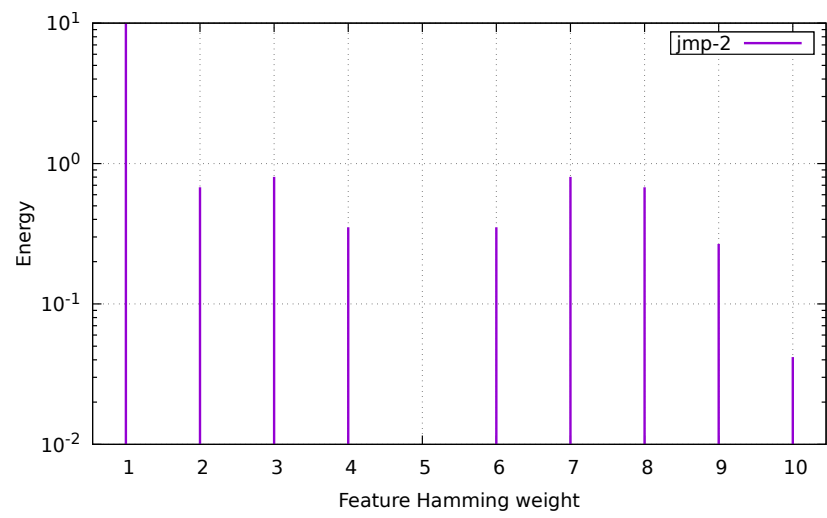
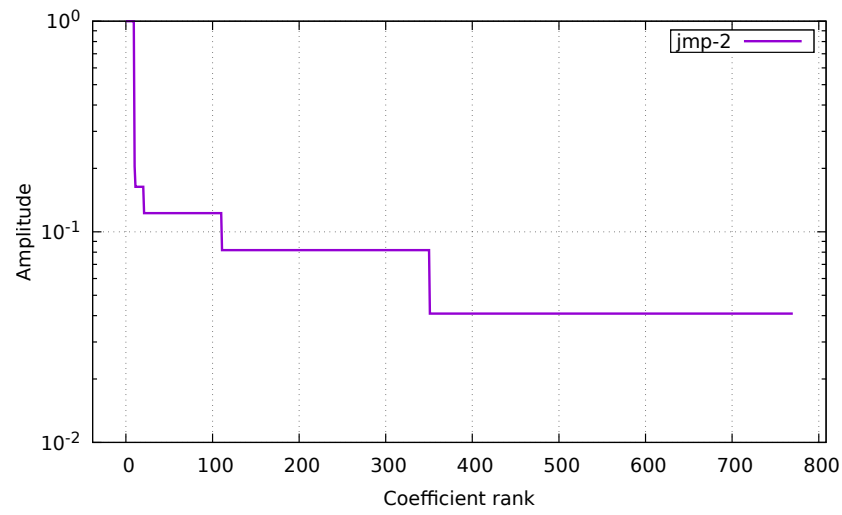
4 leading-ones



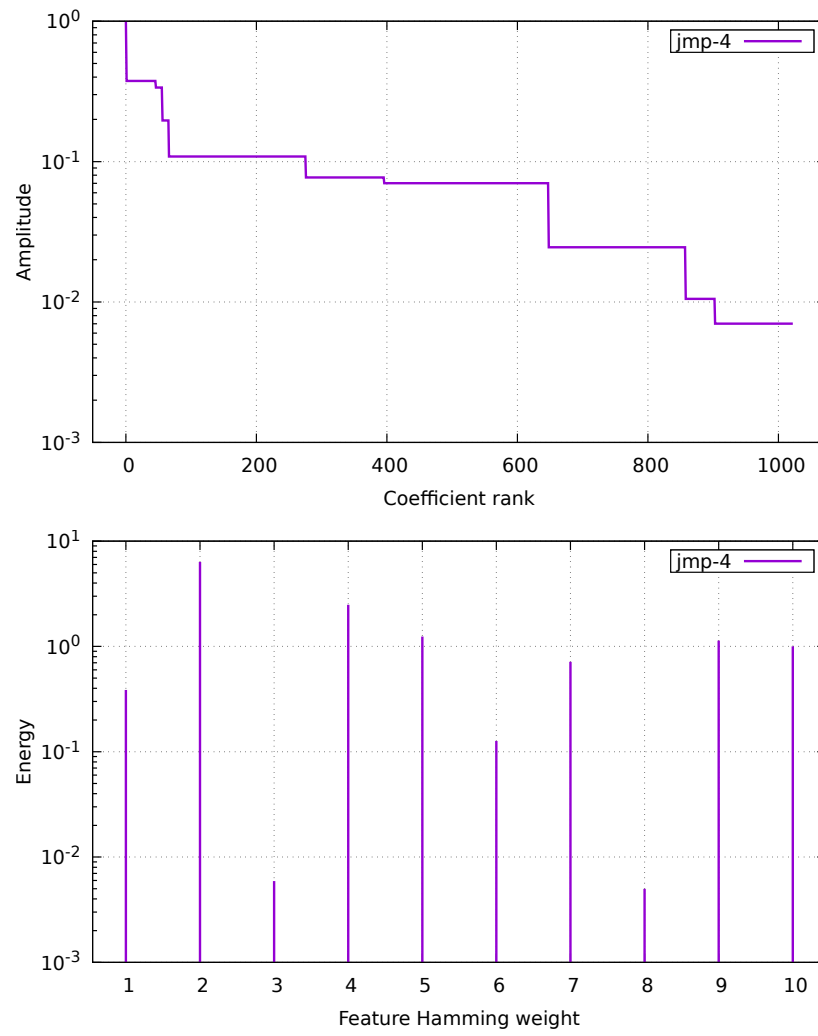
5 ridge



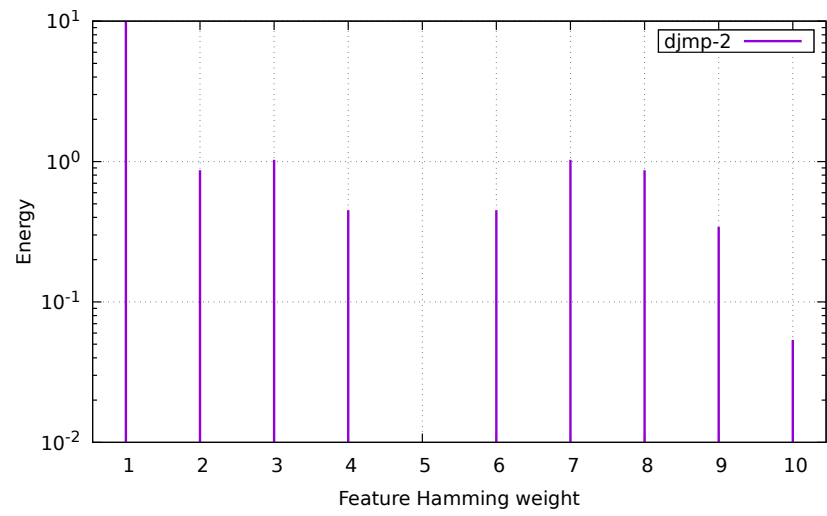
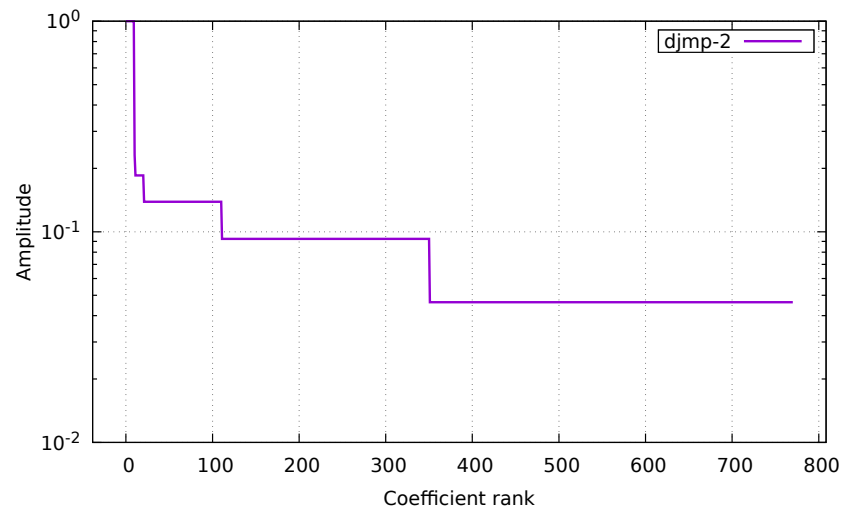
6 jmp-2



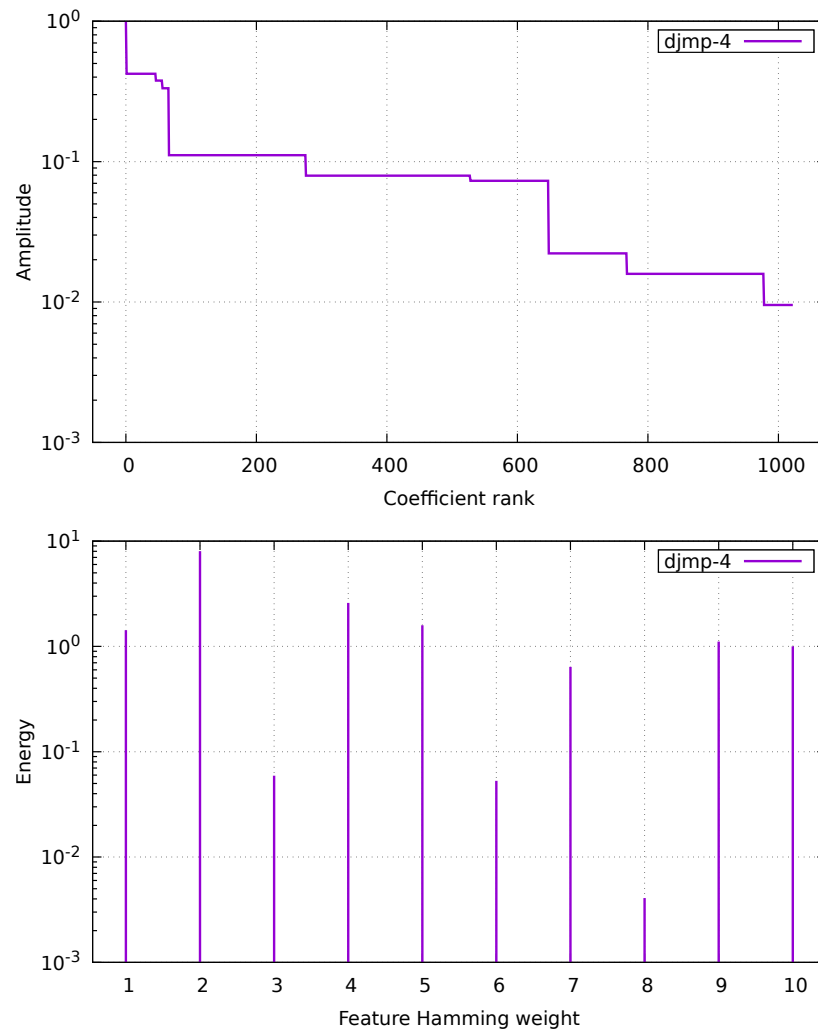
7 jmp-4

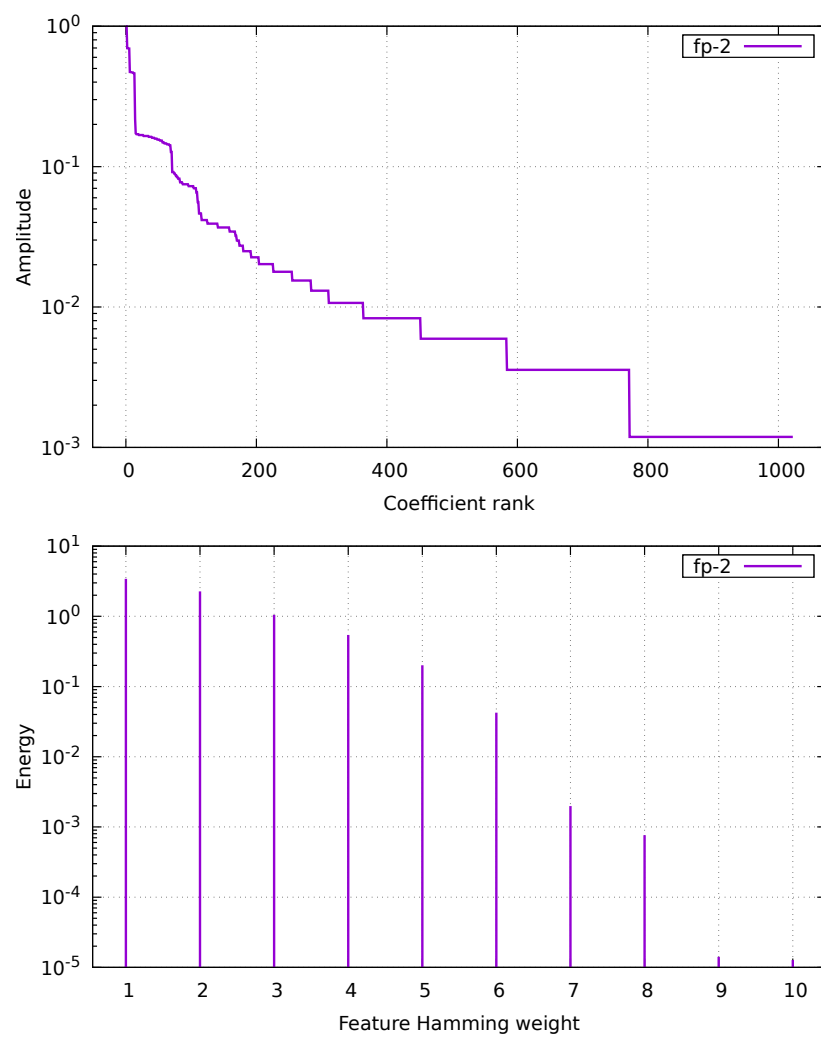


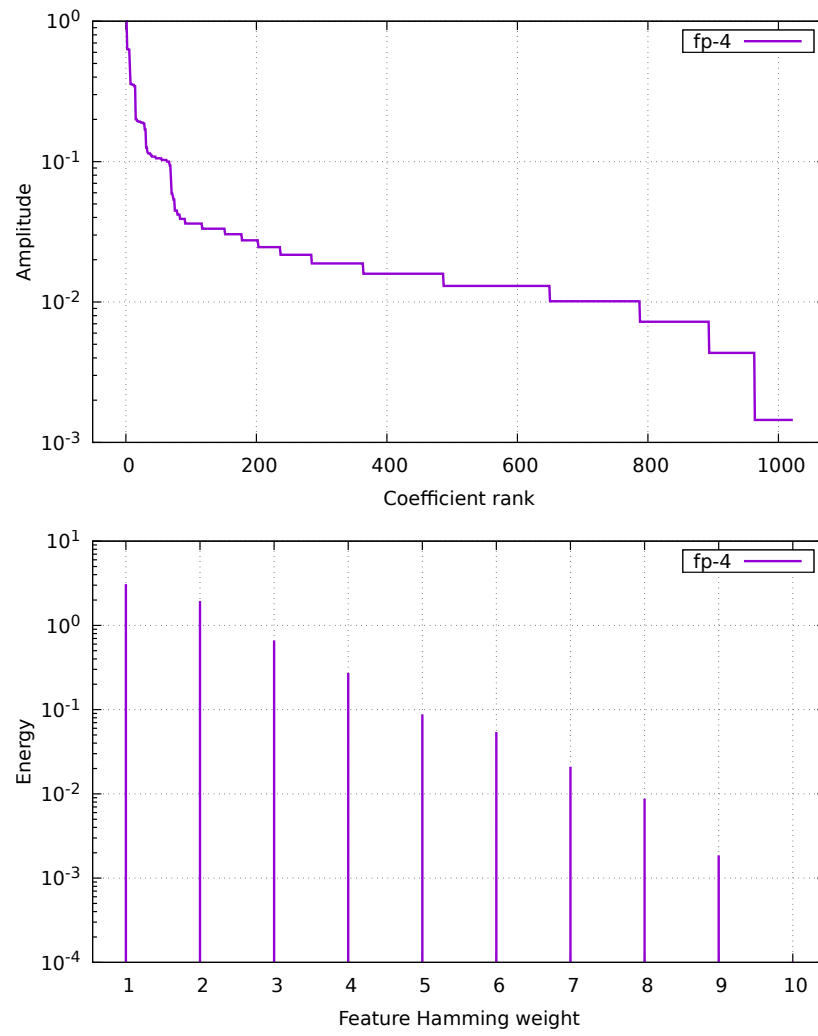
8 djump-2

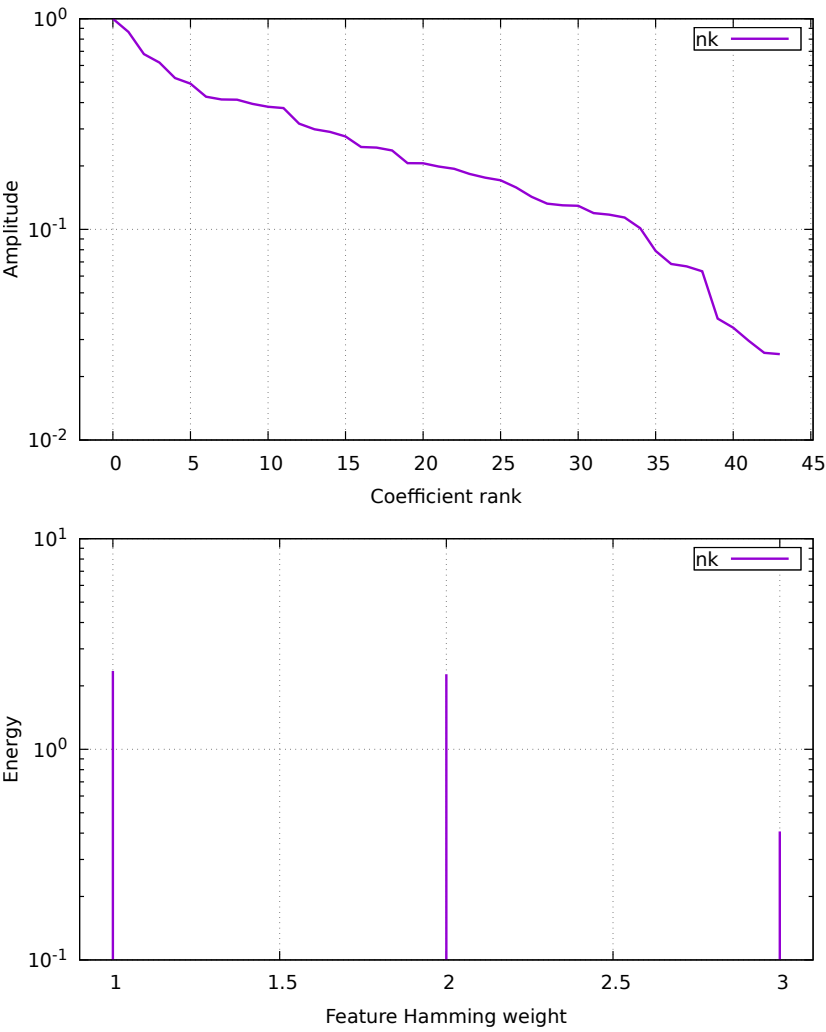


9 djmp-4

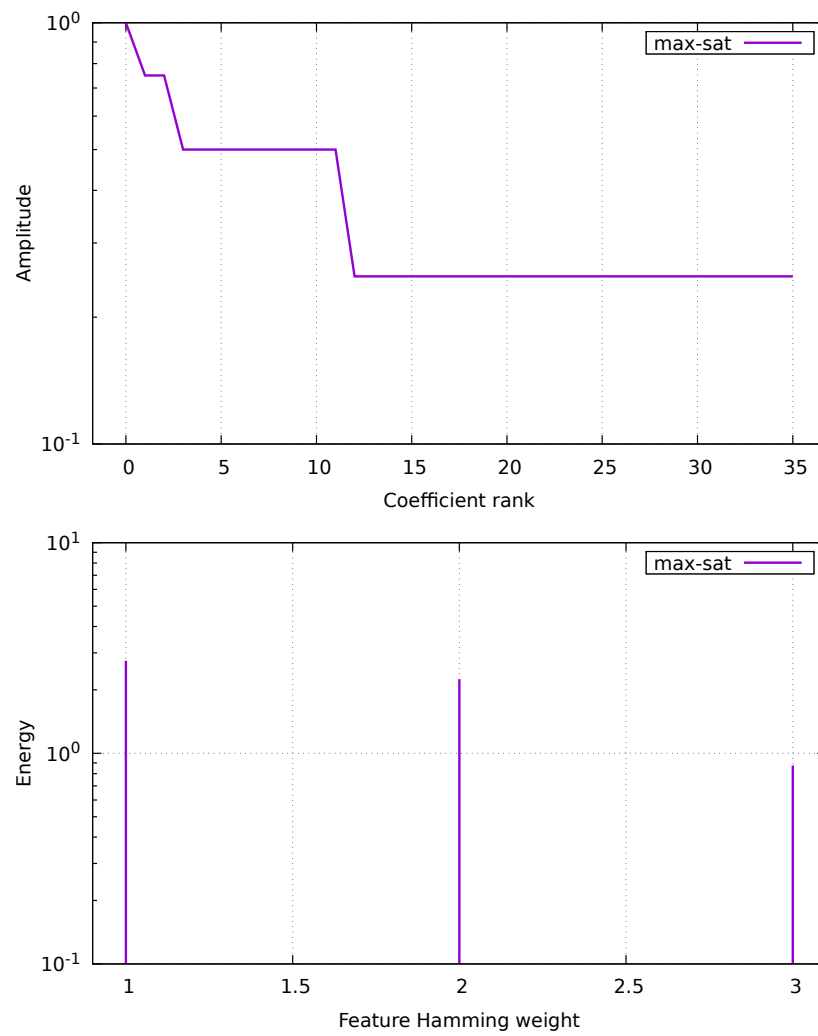




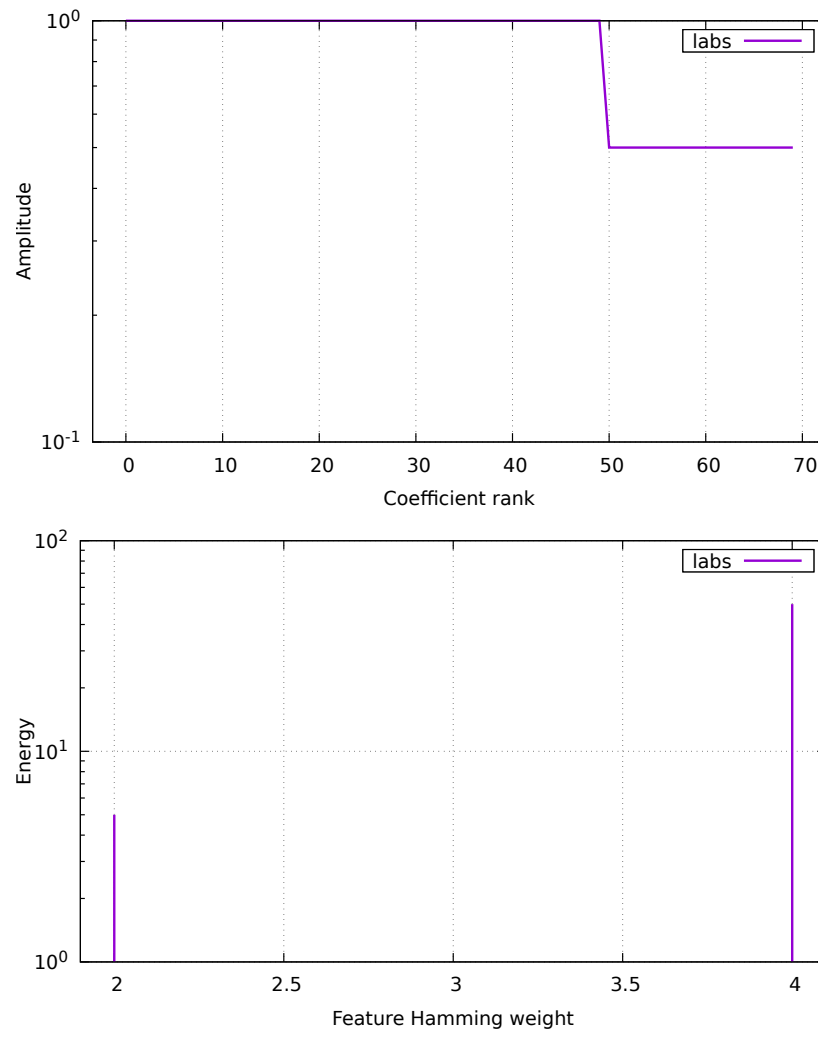


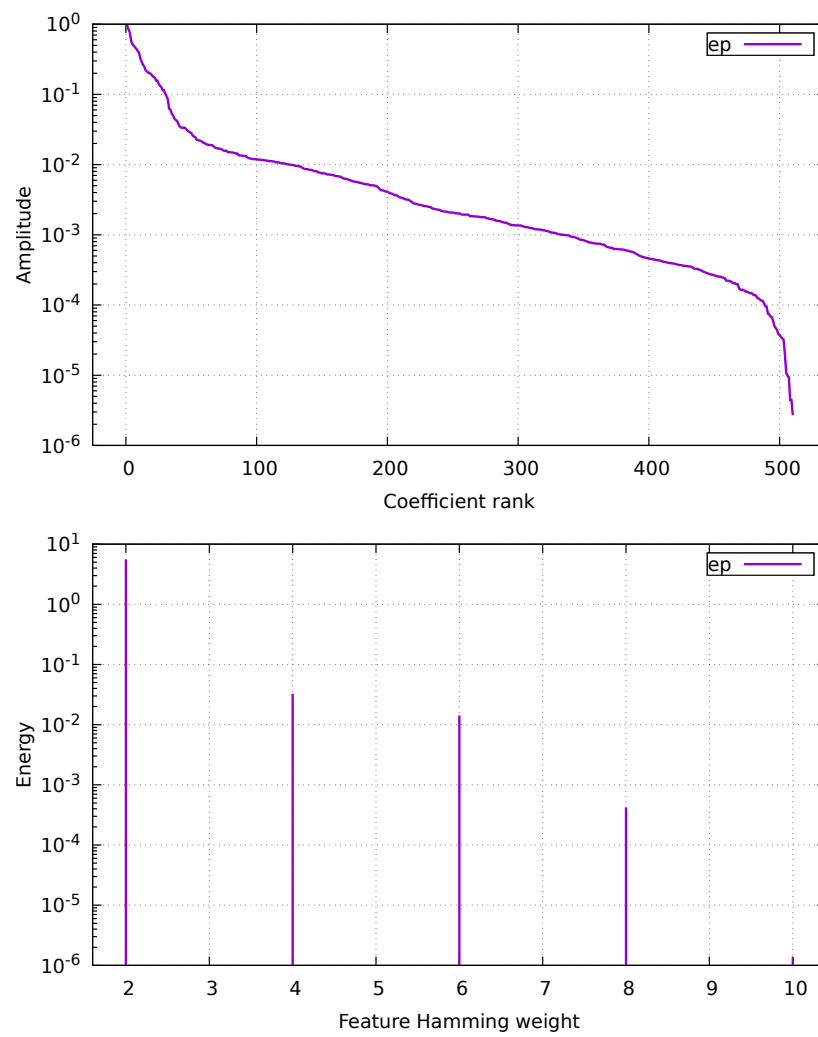


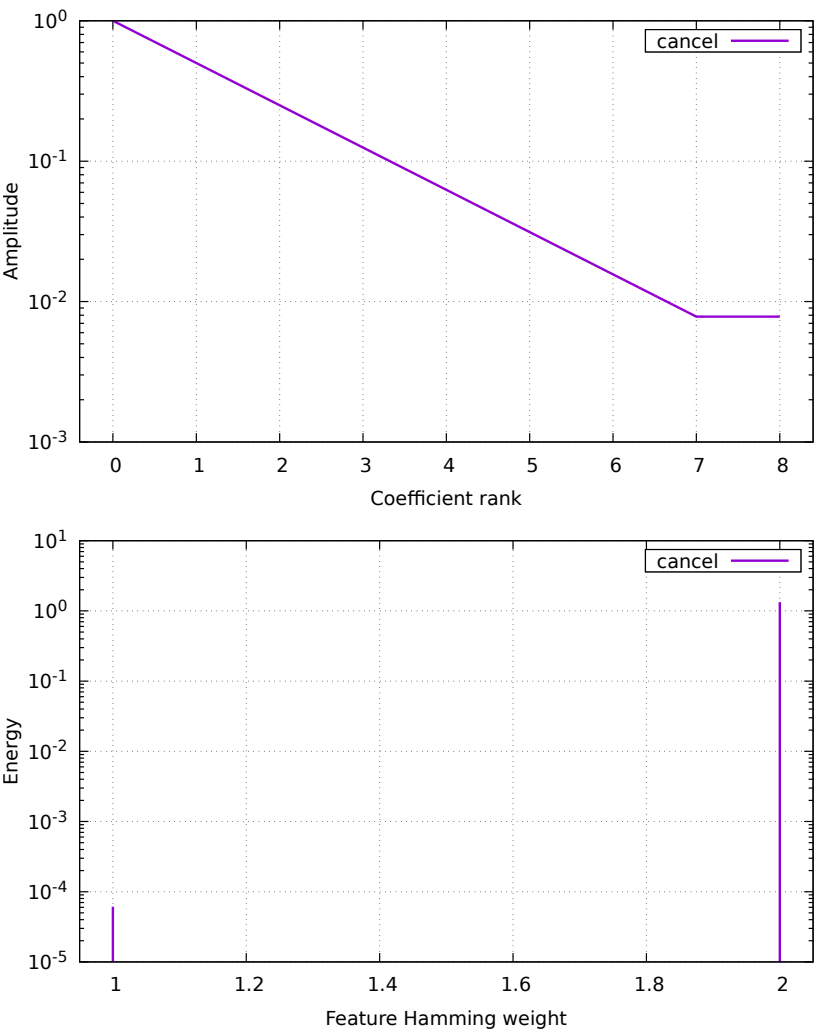
13 max-sat



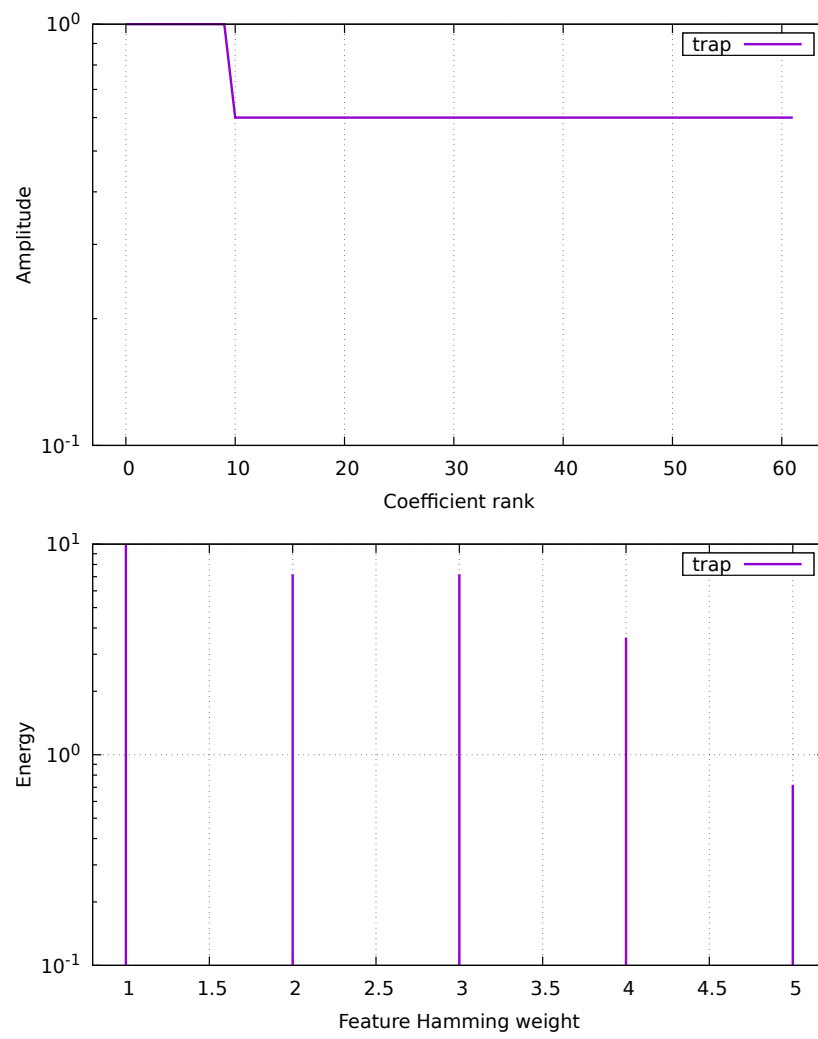
14 labs

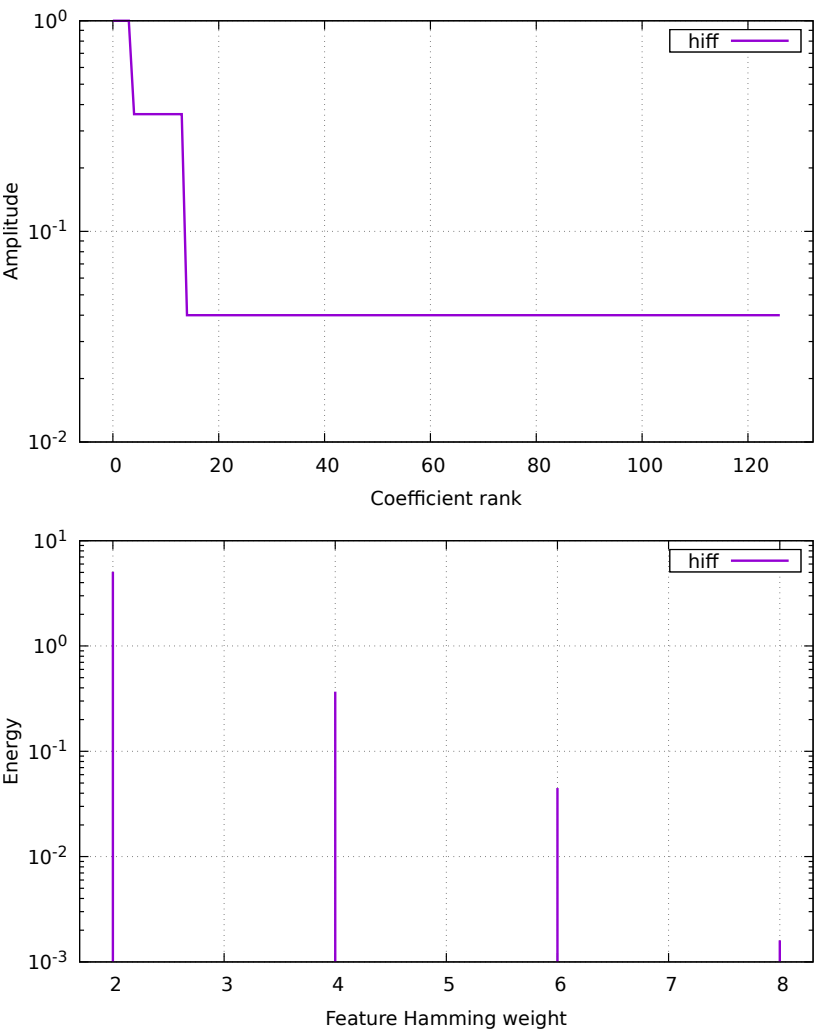




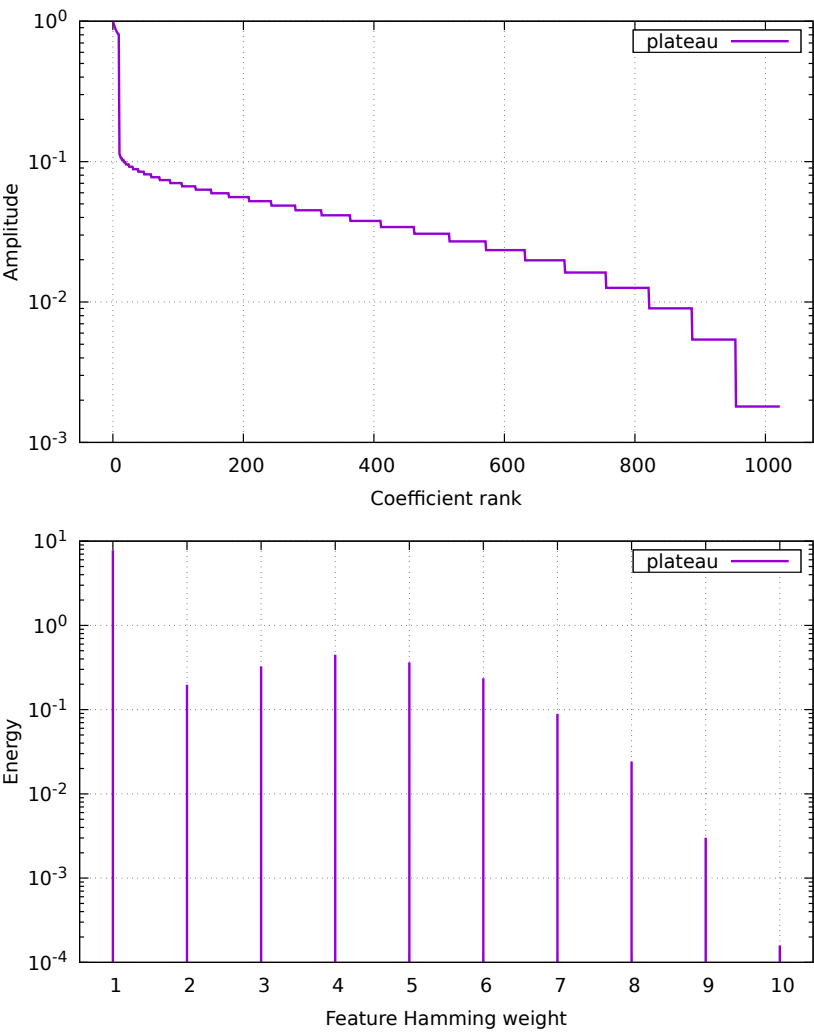


17 trap

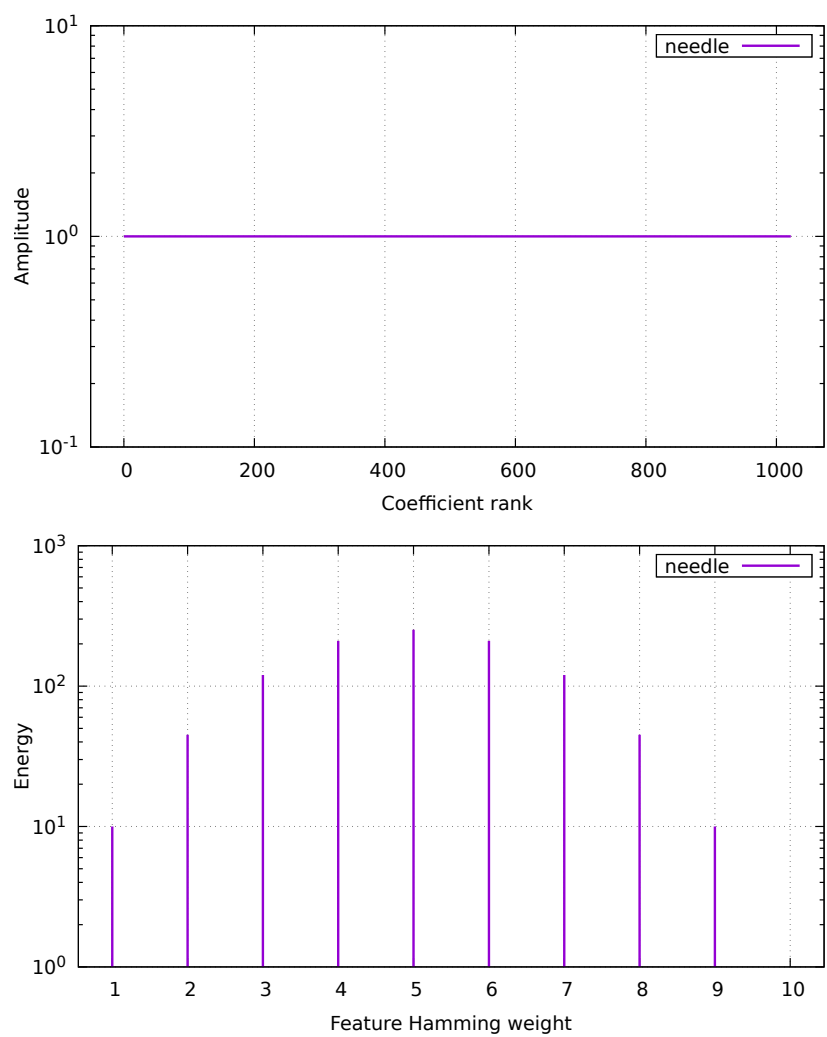




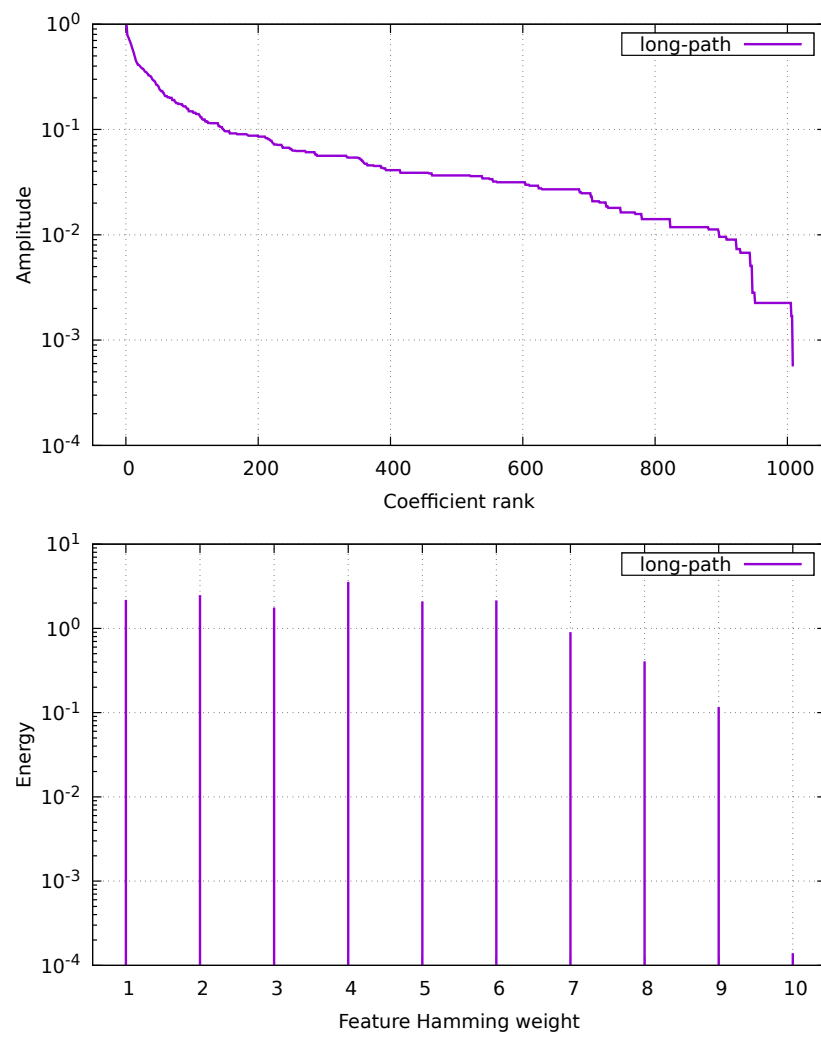
19 plateau

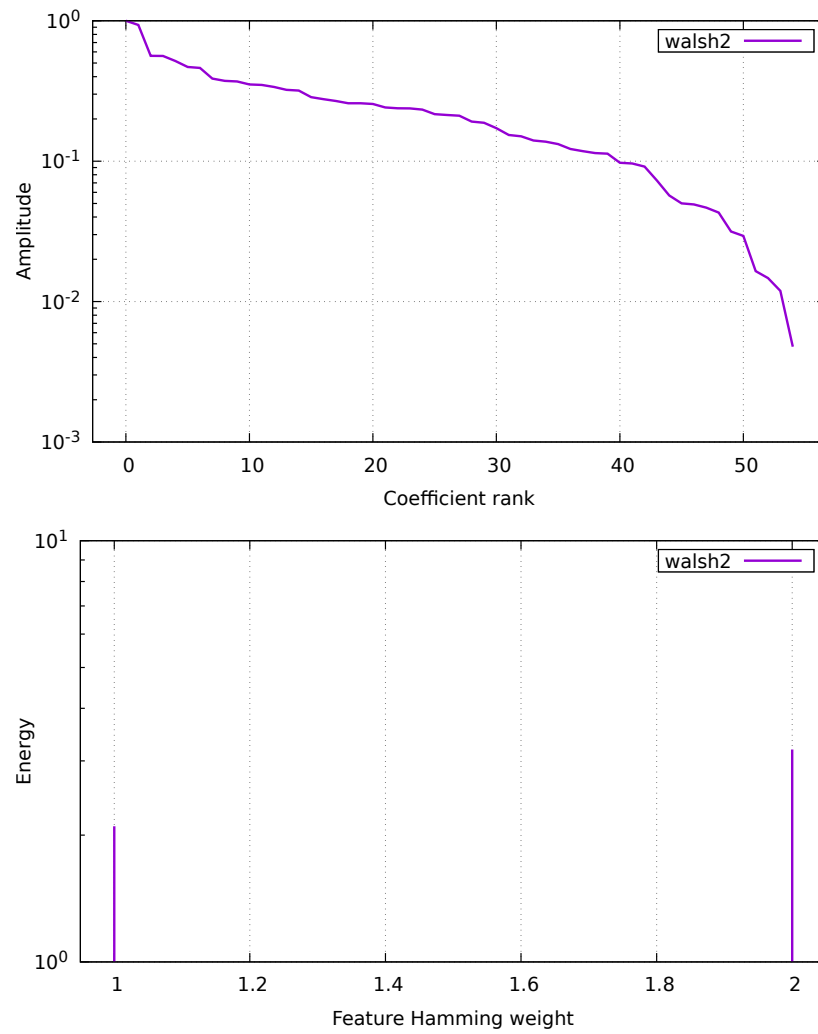


20 needle



21 long-path





A Plan

```
{
  "exec": "hnco",
  "opt": "--fn-walsh-transform -b 0 -s 10",
  "parallel": true,
  "results": "results",
  "graphics": "graphics",
  "report": "report",
  "functions": [
    {
      "id": "one-max",
      "opt": "-F 0"
    },
    {
      "id": "lin",
      "opt": "-F 1 -p instances/lin.10"
    },
    {
      "id": "leading-ones",
      "opt": "-F 10"
    },
    {
      "id": "ridge",
      "opt": "-F 11"
    }
  ]
}
```

```

    "id": "jmp-2",
    "opt": "-F 30 -t 2"
},
{
    "id": "jmp-4",
    "opt": "-F 30 -t 4"
},
{
    "id": "djmp-2",
    "opt": "-F 31 -t 2"
},
{
    "id": "djmp-4",
    "opt": "-F 31 -t 4"
},
{
    "id": "fp-2",
    "opt": "-F 40 -t 2"
},
{
    "id": "fp-4",
    "opt": "-F 40 -t 4"
},
{
    "id": "nk",
    "opt": "-F 60 -p instances/nk.10.2"
},
{
    "id": "max-sat",
    "opt": "-F 70 -p instances/ms.10.3.10"
},
{
    "id": "labs",
    "opt": "-F 80"
},
{
    "id": "ep",
    "opt": "-F 90 -p instances/ep.10"
},
{
    "id": "cancel",
    "opt": "-F 100 -s 9"
},
{
    "id": "trap",
    "opt": "-F 110 --fn-num-traps 2"
},
{
    "id": "hiff",
    "opt": "-F 120 -s 8"
},
{
    "id": "plateau",
    "opt": "-F 130"
},
{
    "id": "needle",
    "opt": "-F 20"
},
{
    "id": "long-path",
    "opt": "-F 140"
},

```



```

    {
        "id": "walsh2",
        "opt": "-F 162 -p instances/walsh2.10"
    }
]
}

```

B Default parameters

```

# algorithm = 100
# bm_mc_reset_strategy = 1
# bm_num_gs_cycles = 1
# bm_num_gs_steps = 100
# bm_sampling = 1
# budget = 10000
# bv_size = 100
# description_path = description.txt
# ea_lambda = 100
# ea_mu = 10
# expression = x
# fn_name = noname
# fn_num_traps = 10
# fn_prefix_length = 2
# fn_threshold = 10
# fp_expression = (1-x)^2+100*(y-x^2)^2
# fp_lower_bound = -2
# fp_num_bits = 8
# fp_upper_bound = 2
# function = 0
# ga_crossover_bias = 0.5
# ga_crossover_probability = 0.5
# ga_tournament_size = 10
# hea_bit_herding = 0
# hea_num_seq_updates = 100
# hea_reset_period = 0
# hea_sampling_method = 0
# hea_weight = 1
# learning_rate = 0.001
# map = 0
# map_input_size = 100
# map_path = map.txt
# map_ts_length = 10
# map_ts_sampling_mode = 0
# mutation_rate = 1
# neighborhood = 0
# neighborhood_iterator = 0
# noise_stddev = 1
# num_iterations = 0
# num_threads = 1
# path = function.txt
# pn_mutation_rate = 1
# pn_neighborhood = 0
# pn_radius = 2
# population_size = 10
# pv_log_num_components = 5
# radius = 2
# results_path = results.json
# rls_patience = 50
# sa_beta_ratio = 1.2
# sa_initial_acceptance_probability = 0.6
# sa_num_transitions = 50
# sa_num_trials = 100

```

```
# seed = 0
# selection_size = 1
# solution_path = solution.txt
# target = 100
# print_defaults
# last_parameter
# exec_name = hnco
# version = 0.15
# Generated from hnco.json
```