```
File - D:\cpl\cpl-coding-0\2022-CPL\6-recursion\main-re.c
 1 //
 2 // Created by hfwei on 2022/11/1.
 3 //
 4 // You can even call `main` in the `main` function.
 5 // WARNING: Do not write code like this!!!
 6 //
 8 #include <stdio.h>
10 int main(int argc, char *argv[]) {
     if (argc == 1) {
11
12
     return 0;
13
14
    printf("%s", argv[argc - 1]);
15
16
17
    main(argc - 1, argv);
18
19
    return 0;
20 }
```

```
File - D:\cpl\cpl-coding-0\2022-CPL\6-recursion\gcd-euclid-iter.c
 1 #include <stdio.h>
 2 /**
 3 * file: gcd-euclid-iter.c
 5 * Visualization (gcd(64, 18) for illustration):
 6 * https://pythontutor.com/c.html#code=int%20main%28%29%20%7B%0A%0A%
   20%20int%20a%20%3D%2064%3B%0A%20%20int%20b%20%3D%2018%3B%0A%0A%20%
   20while%20%28a%20!%3D%20b%29%20%7B%0A%20%20%20%20if%20%28a%20%3E%20b%
   29%20%7B%0A%20%20%20%20%20%20a%20%3D%20a%20-%20b%3B%0A%20%20%20%20%7D%
   20else%20%7B%0A%20%20%20%20%20b%20b%20b%20b%20-%20a%3B%0A%20%20%20%20
   %7D%0A%20%20%7D%0A%20%20%0A%20%20return%200%3B%0A%7D&curInstr=28&mode=
   display&origin=opt-frontend.js&py=c_gcc9.3.0&rawInputLstJSON=%5B%5D
 7
   * Created by hengxin on 11/01/22.
 9 */
10
11 int main() {
     int a;
12
13
     int b;
     scanf("%d %d", &a, &b);
14
15
16
     while (a != b) {
17
       if (a > b) {
18
         a = a - b;
19
       } else {
20
         b = b - a;
21
     }
22
23
24
     printf("gcd = %d\n", a);
25
26
     return 0;
27 }
28
```

```
File - D:\cpl\cpl-coding-0\2022-CPL\6-recursion\fib-array.c
 1 /**
 2 * file: fib-iter.c
 3 *
 4 * Iteratively computing the first n Fibonacci numbers with an array.
 5 *
 6 * Created by hengxin on 11/13/21.
 7 */
 8
 9 #include <stdio.h>
10 #include <limits.h>
11
12 #define LEN 93
13
14 int main() {
15
    long long fibs[LEN] = \{0, 1\};
16
17
    int n;
18 scanf("%d", &n);
19
20 for (int i = 2; i < n; i++) {
21
       fibs[i] = fibs[i - 1] + fibs[i - 2];
22
        printf("%lld ", fibs[i]);
23
     }
24
__ _ _ , _ < n; i++)
26 // printf("%lld ", fibs[i]);
27 // }
25 // for (int i = 0; i < n; i++) {
28 //
29 // printf("\n%lld\n", LLONG_MAX);
31 return 0;
32 }
```

```
File - D:\cpl\cpl-coding-0\2022-CPL\6-recursion\fib-iter.c
 1 #include <stdio.h>
 2 /**
 3 * file: fib-iter.c
 5 * Iteratively computing the first n Fibonacci numbers without using
   an array.
 7 * Created by hengxin on 11/13/21.
 8 */
 9
10 int main() {
11 int n;
12
    scanf("%d", &n);
13
14
    long long fib1 = 0;
15
     long long fib2 = 1;
16
     printf("%lld %lld ", fib1, fib2);
17
18
     long long fib3;
19
     for (int i = 3; i < n; i++) {
20
       fib3 = fib1 + fib2;
21
       printf("%lld ", fib3);
22
23
       fib1 = fib2;
24
       fib2 = fib3;
    }
25
26
27
    return 0;
28 }
```

```
1 /**
2 * file: gcd-euclid.c
3 *
4 * Euclid's algorithm:
5 *
6 * if a > b
7 * then gcd(a, b) = gcd(a - b, b)
8 * else gcd(a, b) = gcd(a, b - a)
10 * Created by hengxin on 11/01/22.
11 */
12
13 #include <stdio.h>
14
15 int GCDEuclid(int a, int b);
16
17 int main() {
18
    int a;
19
    int b;
20
    scanf("%d %d", &a, &b);
21
22 printf("gcd(%d, %d) = %d\n", a, b, GCDEuclid(a, b));
23
24
   return 0;
25 }
26
27 int GCDEuclid(int a, int b) {
28
    if (a == b) {
29
      return a;
30
31
32
    if (a > b) {
33
    return GCDEuclid(a - b, b);
34
35
36
    if (a < b) {
37
      return GCDEuclid(a, b - a);
38
     }
39 }
```

```
1 /**
 2 * file: merge-sort.c
 3 *
 4 * Created by hengxin on 11/14/21.
 5 */
 6
 7 #include <stdio.h>
 9 // #define LEN 8
10 #define LEN 7
11
12 void MergeSort(int nums[], int left, int right);
14 /**
15 * Merge two subarrays nums[left .. mid] and nums[mid + 1 .. right]
16
17 * @param nums
18 * @param left
19
   * @param mid
20 * @param right
21 */
22 void Merge(int nums[], int left, int mid, int right);
24 int main() {
25
    // int numbers[LEN] = {6, 5, 3, 1, 8, 7, 2, 4};
26
     int numbers[LEN] = {38, 27, 43, 3, 9, 82, 10};
     MergeSort(numbers, 0, LEN - 1);
27
28
29
     for (int i = 0; i < LEN; i++) {
30
       printf("%d ", numbers[i]);
31
     }
32
33
     return 0;
34 }
35
36 void MergeSort(int nums[], int left, int right) {
37
     if (left == right) {
38
       return;
39
40
41
     int mid = (left + right) / 2;
42
     MergeSort(nums, left, mid);
43
     MergeSort(nums, mid + 1, right);
44
45
     Merge(nums, left, mid, right);
46 }
47
48 void Merge(int nums[], int left, int mid, int right) {
    // make a copy of nums[left .. right]
49
50
     int size = right - left + 1;
51
    // use VLA (variable-length arrays)
52
    // introduced since C99
53
    // but made optional since C11
```

```
int copy[size];
55
     for (int i = 0, j = left; i < size; i++, j++) {
56
       copy[i] = nums[j];
57
58
59
     int left_index = left;
     int right_index = mid + 1;
60
     int copy_index = 0;
61
62
     while (left_index <= mid && right_index <= right) {</pre>
63
64
       if (nums[left_index] <= nums[right_index]) {</pre>
65
         copy[copy_index] = nums[left_index];
         left_index++;
66
67
       } else {
         copy[copy_index] = nums[right_index];
68
69
         right_index++;
       }
70
71
72
       copy_index++;
73
74
75
     while (left_index <= mid) {</pre>
76
       copy[copy_index] = nums[left_index];
77
       left_index++;
78
       copy_index++;
     }
79
80
81
     while (right_index <= right) {</pre>
82
       copy[copy_index] = nums[right_index];
83
       right_index++;
84
       copy_index++;
     }
85
86
87
     // copy back
     for (int i = 0, j = left; i < size; i++, j++) {
88
89
       nums[j] = copy[i];
90
     }
91 }
```

```
1 /**
   * file: sum-re.c
 2
 3
   * Recursively computing the sum of an array of integers.
 4
 5
   * Visualization: https://pythontutor.com/visualize.html#code=%
   23include%20%3Cstdio.h%3E%0A%0Aint%20Sum%28int%20numbers%5B%5D,%20int%
   20len%29%3B%0A%0Aint%20main%28%29%20%7B%0A%20%20%20%20int%20numbers%5B
   %5D%20%3D%20%7B1,%202,%203,%204,%205%7D%3B%0A%0A%20%20%20%20int%20sum%
   20%3D%20Sum%28numbers,%20sizeof%20numbers%20/%20sizeof%20numbers%5B0%
   5D%29%3B%0A%20%20%20%20printf%28%22sum%20%3D%20%25d%5Cn%22,%20sum%29%
   3B%0A%0A%20%20%20%20return%200%3B%0A%7D%0A%0Aint%20Sum%28int%20numbers
   %5B%5D,%20int%20len%29%20%7B%0A%20%20%20if%20%28len%20%3D%3D%200%29
  %20%7B%0A%20%20%20%20%20%20%20%20return%200%3B%0A%20%20%20%20%7D%0A%0A
  %20%20%20%20int%20partial_sum%20%3D%20Sum%28numbers,%20len%20-%201%29%
   3B%0A%0A%20%20%20%20int%20sum%20%3D%20numbers%5Blen%20-%201%5D%20%2B%
   20partial_sum%3B%0A%0A%20%20%20%20return%20sum%3B%0A%7D&cumulative=
  false&heapPrimitives=nevernest&mode=edit&origin=opt-frontend.js&py=
   c_gcc9.3.0&rawInputLstJSON=%5B%5D&textReferences=false
 7
   * Created by hengxin on 11/01/22.
 9
   */
10
11 #include <stdio.h>
12
13 int Sum(const int numbers[], int len);
14
15 int main() {
    int numbers[] = \{1, 2, 3, 4, 5\};
16
17
18
     int sum = Sum(numbers, sizeof numbers / sizeof numbers[0]);
19
     printf("sum = %d\n", sum);
20
21
    return 0;
22 }
23
24 int Sum(const int numbers[], int len) {
     if (len == 0) {
25
26
       return 0;
27
     }
28
29 // return numbers[len - 1] + Sum(numbers, len - 1);
30
31
     int partial_sum = Sum(numbers, len - 1);
32
33
     int sum = numbers[len - 1] + partial_sum;
34
35
     return sum;
36 }
```

```
1 /**
 2
   * Recursively computing the greatest common divisor of two integers
 3
   * Euclidean algorithm:
 5
   * gcd(a, b) = gcd(b, a % b)
 6
 7
   * Visualization (gcd(64, 48) for illustration):
        https://pythontutor.com/c.html#code=int%20GCD%28int%20a,%20int%
   20b%29%3B%0A%0Aint%20main%28%29%20%7B%0A%20%20int%20a%20%3D%2064%3B%0A
  %20%20int%20b%20%3D%2048%3B%0A%0A%20%20printf%28%22qcd%28%25d,%20%25d%
   29%20%3D%20%25d%5Cn%22,%20a,%20b,%20GCD%28a,%20b%29%29%3B%0A%0A%20%
   20return%200%3B%0A%7D%0A%0A//%20gcd%28130,%20124%29%20%3D%202%0A//%
   20gcd%28662,%20414%29%20%3D%202%0Aint%20GCD%28int%20a,%20int%20b%29%20
  %7B%0A%20%20if%20%28b%20%3D%3D%200%29%20%7B%0A%20%20%20%20return%20a%
   3B%0A%20%20%7D%0A%0A%20%20return%20GCD%28b,%20a%20%25%20b%29%3B%0A%7D&
   curInstr=17&mode=display&origin=opt-frontend.js&py=c_gcc9.3.0&
   rawInputLstJSON=%5B%5D
9
10
   * Created by hengxin on 11/13/21.
11
12
13 #include <stdio.h>
15 int GCD(int a, int b);
16
17 int main() {
18
    int a = 0;
19
    int b = 0;
20
    scanf("%d %d", &a, &b);
21
22
     printf("gcd(%d, %d) = %d\n", a, b, GCD(a, b));
23
24
    return 0;
25 }
26
27 // \gcd(130, 124) = 2
28 // \gcd(414, 662) = 2
29 int GCD(int a, int b) {
30
    if (b == 0) {
31
       return a;
32
    }
33
34
    return GCD(b, a % b);
35 }
```

```
1 /**
 2
   * file: fib.c
3
 4 * Recursively computing the n-th Fibonacci number
 5
 6 * Visualization (for n = 4): https://pythontutor.com/render.html#code
   =%23include%20%3Cstdio.h%3E%0A%0Along%20long%20Fib%28int%20n%29%3B%0A%
   OAint%20main%28%29%20%7B%0A%20%20int%20n%20%3D%204%3B%0A%0A%20%
   20printf%28%22%25lld%5Cn%22,%20Fib%28n%29%29%3B%0A%7D%0A%0Along%20long
   %20Fib%28int%20n%29%20%7B%0A%20%20if%20%28n%20%3D%3D%200%29%20%7B%0A%
   20%20%20%20return%200%3B%0A%20%20%7D%0A%0A%20%20if%20%28n%20%3D%3D%201
  %29%20%7B%0A%20%20%20%20return%201%3B%0A%20%20%7D%0A%0A%20%20return%
   20Fib%28n%20-%201%29%20%2B%20Fib%28n%20-%202%29%3B%0A%7D&cumulative=
  false&curInstr=55&heapPrimitives=nevernest&mode=display&origin=opt-
  frontend.js&py=c_gcc9.3.0&rawInputLstJSON=%5B%5D&textReferences=false
 7 *
   * Created by hengxin on 11/01/22.
8
9
10
11 #include <stdio.h>
12 #include <time.h>
13
14 long long Fib(int n);
15
16 int main() {
17
    int n;
     scanf("%d", &n);
18
19
20
    clock_t start = clock();
21
22
     printf("%lld\n", Fib(n));
23
24
    clock_t end = clock();
25
     double time = ((double) end - start) / CLOCKS_PER_SEC;
26
     printf("time = %f (sec)\n", time);
27
28
     return 0;
29 }
30
31 long long Fib(int n) {
    if (n == 0) {
32
33
      return 0;
34
    }
35
36
    if (n == 1) {
37
      return 1;
38
39
     return Fib(n - 1) + Fib(n - 2);
40
41 }
```

```
1 /**
 2 * Binary Search: the recursive version
 3 *
 4 * Created by hengxin on 11/14/21.
 5 */
 6
 7 #include <stdio.h>
 8 #define LEN 10
10 int BinarySearch(int key, int dict[], int low, int high);
11
12 int main() {
     int dictionary[LEN] = {0, 1, 1, 2, 3, 5, 8, 13, 21, 34};
13
14
15
     int key;
16
    scanf("%d", &key);
17
18
     printf("The index of %d is %d.\n", key,
19
            BinarySearch(key, dictionary, 0, LEN - 1));
20
21
     return 0;
22 }
23
24 int BinarySearch(int key, int dict[], int low, int high) {
25 // if (low == high) {
26 //
         if (dict[low] == key) {
27 //
           return low;
28 //
29 //
        return -1;
30 // }
31
     if (low > high) {
32
33
     return -1;
34
35
36
    int mid = (low + high) / 2;
37
38
     if (dict[mid] == key) {
39
     return mid;
40
41
42
     if (dict[mid] > key) {
43
       return BinarySearch(key, dict, low, mid - 1);
44
45
46
     return BinarySearch(key, dict, low + 1, high);
47 }
48
```

```
1 /**
 2
   * file: min-re.c
 3
   * Recursively find the minimum of an array of integers
 4
 5
   * Visualization: https://pythontutor.com/visualize.html#code=%
   23include%20%3Cstdio.h%3E%0A%0A%23define%20NUM%205%0Aint%20numbers%
   5BNUM%5D%20%3D%20%7B25,%2034,%2037,%2045,%2043%7D%3B%0A%0Aint%20Min%
   28const%20int%20nums%5B%5D,%20int%20len%29%3B%0A%0Aint%20main%28%29%20
   %7B%0A%20%20int%20min%20%3D%20Min%28numbers,%20NUM%29%3B%0A%20%
   20printf%28%22min%20%3D%20%25d%5Cn%22,%20min%29%3B%0A%0A%20%20return%
   200%3B%0A%7D%0A%0Aint%20Min%28const%20int%20numbers%5B%5D,%20int%20len
   %29%20%7B%0A%20%20if%20%28len%20%3D%3D%201%29%20%7B%0A%20%20%20%
   20return%20numbers%5B0%5D%3B%0A%20%20%7D%0A%0A%20%20int%20partial_min%
   20%3D%20Min%28numbers,%20len%20-%201%29%3B%0A%20%20return%20numbers%
   5Blen%20-%201%5D%20%3C%20partial_min%20%3F%20numbers%5Blen%20-%201%5D%
   20%3A%20partial_min%3B%0A%7D&cumulative=false&heapPrimitives=nevernest
   &mode=edit&origin=opt-frontend.js&py=c_gcc9.3.0&rawInputLstJSON=%5B%5D
   &textReferences=false
 7
   * Created by hengxin on 11/01/22.
9
   */
10
11 #include <stdio.h>
12
13 #define NUM 5
14 // Just for illustration. Avoid global variables.
15 int numbers[NUM] = {25, 34, 37, 45, 43};
17 int Min(const int nums[], int len);
18
19 int main() {
20
    int min = Min(numbers, NUM);
21
     printf("min = %d\n", min);
22
23
    return 0;
24 }
25
26 int Min(const int nums[], int len) {
27
    if (len == 1) {
28
       return nums[0];
29
30
31
     int partial_min = Min(nums, len - 1);
     return nums[len - 1] < partial_min ? nums[len - 1] : partial_min;</pre>
32
33 }
```

```
File - D:\cpl\cpl-coding-0\2022-CPL\6-recursion\gcd-euclidean-iter.c
 1 /**
 2 * file: gcd.c
 3 *
 4 * Iteratively computing the greatest common divisor of two integers.
 5 *
 6 * Euclidean algorithm:
 7 * gcd(a, b) = gcd(b, a % b)
 9 * Created by hengxin on 11/01/22.
10 */
11
12 #include <stdio.h>
14 int GCD(int a, int b);
15
16 int main() {
17
   int a = 130;
18
    int b = 124;
19
20
    printf("gcd(%d, %d) = %d\n", a, b, GCD(a, b));
21
22
   return 0;
23 }
24
25 int GCD(int a, int b) {
26
     int tmp;
27
     while (b != 0) {
28
    tmp = b;
29
     b = a % b;
30
       a = tmp;
31
    }
32
33
    return a;
34 }
```

