

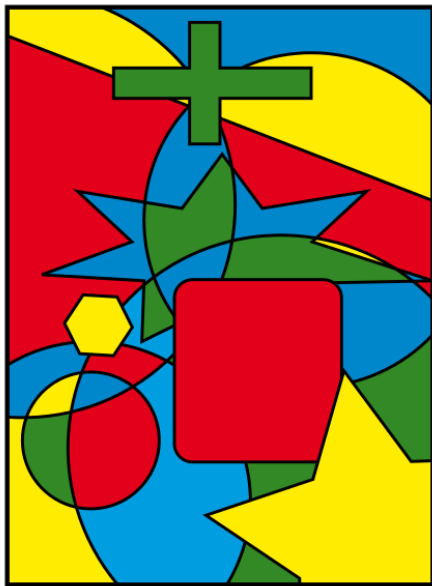
# (十二) 图论: 匹配与网络流 (Matching and Network Flow)

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2021 年 05 月 27 日



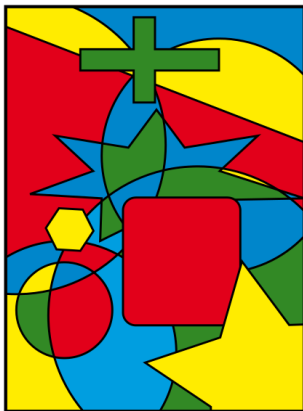


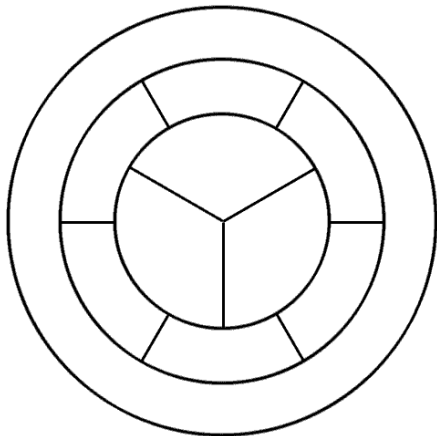
## Theorem (Four Color (Map) Theorem (informal))

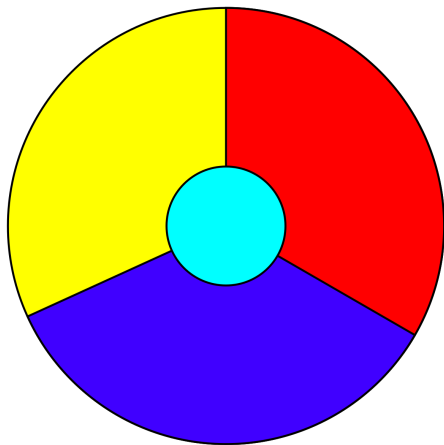
*Every **map** can be colored with only **four** colors such that no two **adjacent regions** share the same color.*

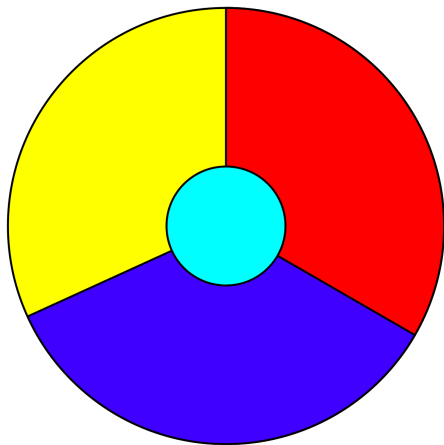
## Theorem (Four Color (Map) Theorem (informal))

Every *map* can be colored with only *four* colors such that no two *adjacent regions* share the same color.









Every region is adjacent to the other 3 regions.

What if we have a map which contains 5 regions so that every region is adjacent to the other 4 regions?

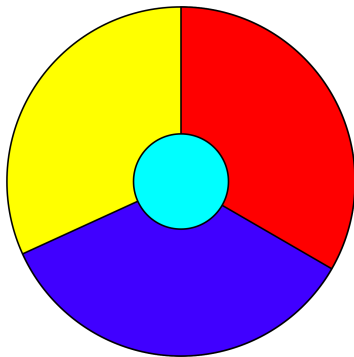


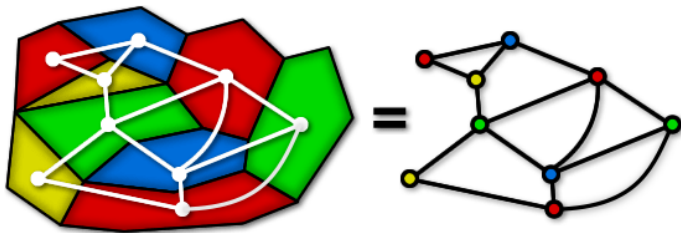
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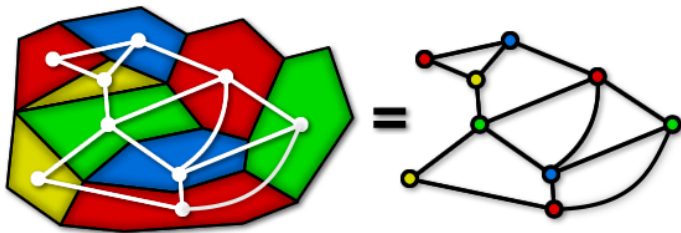


**IMPOSSIBLE™**

What does Four Color Theorem to do with Graph Theory?







Every map produces a **planar** graph.

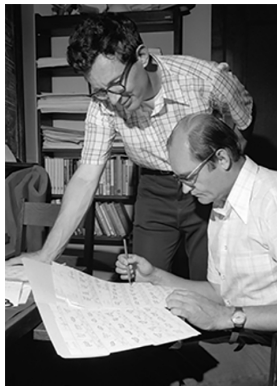
Theorem (Four Color Theorem (Kenneth Appel, Wolfgang Haken; 1976))

Every *simple planar* graph is *4-colorable*.



Theorem (Four Color Theorem (Kenneth Appel, Wolfgang Haken; 1976))

Every *simple planar* graph is *4-colorable*.



I will *not* show its proof (which I don't understand either)!

## Theorem

*Every simple planar graph is 6-colorable.*

## Theorem

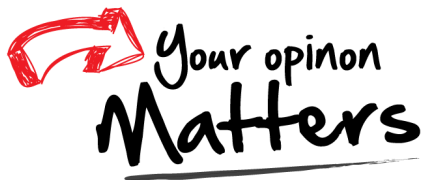
Every *simple planar* graph is *6-colorable*.

## Theorem (Percy John Heawood (1890))

Every *simple planar* graph is *5-colorable*.



Thank  
You!



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