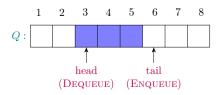
2-10 Elementary Data Structures

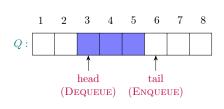
Hengfeng Wei

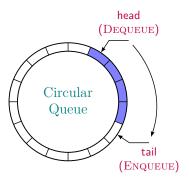
hfwei@nju.edu.cn

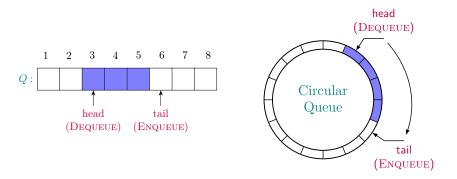
May 30, 2018





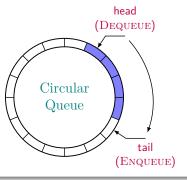




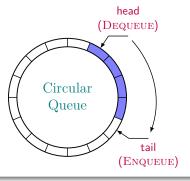


head & teal: following the same direction

Underflow and Overflow of a Circular Queue (Problem 10.1-4)



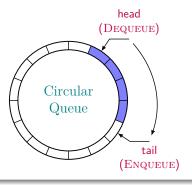
Underflow and Overflow of a Circular Queue (Problem 10.1-4)



```
\begin{array}{l} \textbf{procedure} \ \ \text{DEQUEUE}(Q) \\ \textbf{if} \ \ Q.head = Q.tail \ \ \textbf{then} \\ \textbf{return} \ \ \text{``UNDERFLOW''} \end{array}
```

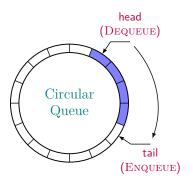
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Underflow and Overflow of a Circular Queue (Problem 10.1-4)

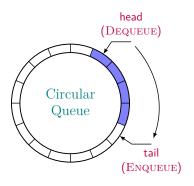


```
 \begin{array}{c} \textbf{procedure} \ \ \text{Dequeue}(Q) \\ \textbf{if} \ \ \underline{Q.head} = \underline{Q.tail} \ \textbf{then} \\ \textbf{return} \ \ \text{"UNDERFLOW"} \\ \end{array}
```

 $\begin{array}{l} \textbf{procedure} \ \ \text{Enqueue}(Q,x) \\ \textbf{if} \ \ \frac{Q.head}{Q.head} = \frac{Q.tail}{Q} + 1 \ \textbf{then} \\ \textbf{return} \ \ \text{"OVERFLOW"} \\ \end{array}$



反馈: tail 为什么指向最后一个元素的后面?这个太难受了。



反馈: tail 为什么指向最后一个元素的后面?这个太难受了。

QUEUE-EMPTY

$$[l,r) \quad (l,r] \quad [l,r] \quad (l,r)$$

$$[l,r) \quad (l,r] \quad [l,r] \quad (l,r)$$

EWD831 - 0

Why numbering should start at zero EWD831.html

To denote the subsequence of natural numbers 2,3,...,12 without the pernicious three dots, four conventions are open to us:

- a) 2 < i < 13
- b) 1 ≺ ¿ ≤ 12
- c) 2 < i < 12
- d) 1< c< 13



Why Numbering Should Start at Zero

Show how to implement a queue using two stacks.

A Queue, Two Stacks (Problem 10.1-6) Show how to implement a queue using two stacks.

```
procedure \text{Enqueue}(x)
Push(S_1, x)

procedure \text{Dequeue}()

if S_2 = \emptyset then
while S_1 \neq \emptyset do
Push(S_2, Pop(S_1))
Pop(S_2)
```

Show how to implement a queue using two stacks.

```
\begin{array}{c} \textbf{procedure } \; \text{EnQUEUE}(x) \\ Push(S_1,x) \\ \\ \textbf{procedure } \; \text{DeQUEUE}() \\ \textbf{if } \; S_2 = \emptyset \; \textbf{then} \\ \textbf{while } \; S_1 \neq \emptyset \; \textbf{do} \\ Push\Big(S_2, Pop(S_1)\Big) \\ Pop(S_2) \end{array}
```

Correctness?

Show how to implement a queue using two stacks.

procedure Enqueue(x) $Push(S_1, x)$ procedure Dequeue()if $S_2 = \emptyset$ then while $S_1 \neq \emptyset$ do $Push(S_2, Pop(S_1))$ $Pop(S_2)$

Correctness?

$$\operatorname{EnQ}(x, t_1), \operatorname{EnQ}(y, t_2) \wedge t_1 < t_2$$

$$\Longrightarrow$$

$$\operatorname{DEQ}(x, t_3), \operatorname{DEQ}(y, t_4) \wedge t_3 < t_4$$

Show how to implement a queue using two stacks.

Analyze the running time of the queue operations.

$$\begin{array}{c} \textbf{procedure } \mathbf{ENQUEUE}(x) \\ Push(S_1,x) \\ \\ \\ \textbf{procedure } \mathbf{DEQUEUE}() \\ \textbf{if } S_2 = \emptyset \textbf{ then} \\ \textbf{while } S_1 \neq \emptyset \textbf{ do} \\ Push \Big(S_2, Pop(S_1)\Big) \\ \\ Pop(S_2) \end{array}$$

Correctness?

$$\operatorname{EnQ}(x, t_1), \operatorname{EnQ}(y, t_2) \wedge t_1 < t_2$$

$$\Longrightarrow$$

$$\operatorname{DEQ}(x, t_3), \operatorname{DEQ}(y, t_4) \wedge t_3 < t_4$$

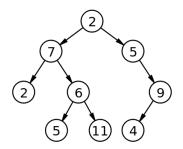
$$\hat{c}_{\text{ENQ}} = 4$$

$$\hat{c}_{\text{DEQ}} = 0$$

$$\hat{c}_{\mathrm{ENQ}} = 4$$
 $\hat{c}_{\mathrm{ENQ}} = 3$ $\hat{c}_{\mathrm{DEQ}} = 0$ $\hat{c}_{\mathrm{DEQ}} = 1$

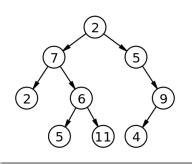
Recursive Binary Tree Traversal (Problem 10.4 - 2)

O(n)



Recursive Binary Tree Traversal (Problem 10.4 - 2)





procedure Recursive-DFS(t) print t.key

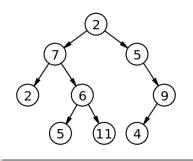
if $t.left \neq NIL$ then RECURSIVE-DFS(t.left)

if $t.right \neq NIL$ then RECURSIVE-DFS(t.right)

RECURSIVE-DFS(T.root)

Recursive Binary Tree Traversal (Problem 10.4 - 2)





procedure Recursive-DFS(t)print t.key

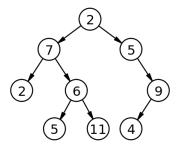
if $t.left \neq NIL$ then RECURSIVE-DFS(t.left)

if $t.right \neq NIL$ then RECURSIVE-DFS(t.right)

RECURSIVE-DFS(T.root)

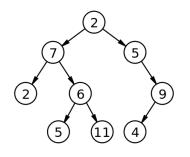
Non-recursive Binary Tree Traversal (Problem 10.4 - 2)





Non-recursive Binary Tree Traversal (Problem 10.4 - 2)





procedure Iterative-DFS(t)

S.Push(t)

 $\triangleright S$: stack

if $v.right \neq NIL$ then S.Push(v.right) if $v.left \neq NIL$ then S.Push(v.left)

ITERATIVE-DFS(T.root)

"LCRS" Tree Traversal (Problem 10.4 - 2)

Thank You!



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