3-11 Matchings and Factors

(Part I: Matchings and Covers)

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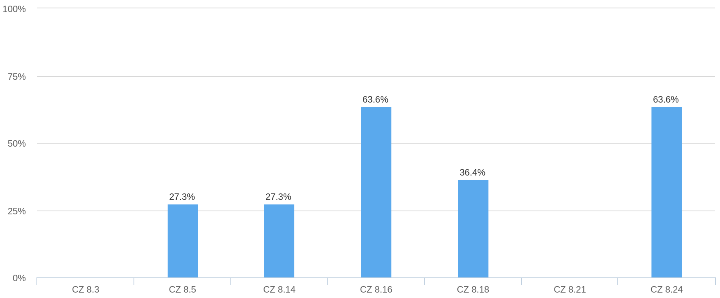
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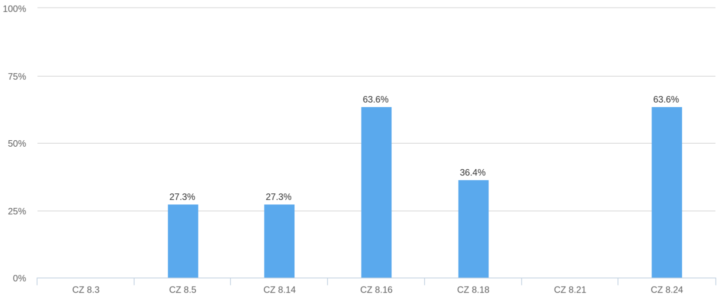
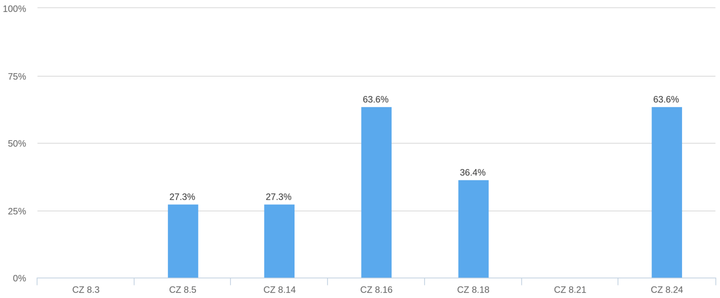


8.5 8.14 8.16

8.18 8.24 (Next Class)



8.5 8.14 8.16 Chinese Postman Problem

8.18 8.24 (Next Class)

Theorem (Hall's Theorem, 1935; Theorem 8.3)

Let G be a bipartite graph with partite sets U and W such that $r = |U| \leq |W|$.
G contains a matching of cardinality $r \iff G$ satisfies Hall's Condition:

$$\forall X \subseteq U : \left|N(X)\right| \geq \left|X\right|$$

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TONCAS

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TONCAS

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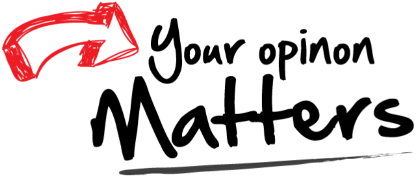
Other TONCAS?


THANK YOU



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