2-9 Sorting and Selection

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How to Argue?

Best-Case Complexity of QUICKSORT $(7.4-2)$

Show that QUICKSORT's best-case running time is $\Omega(n \log n)$.

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By substitution.

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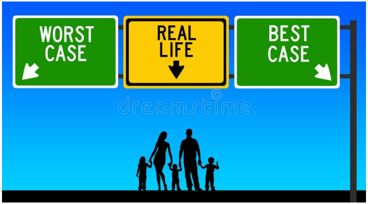

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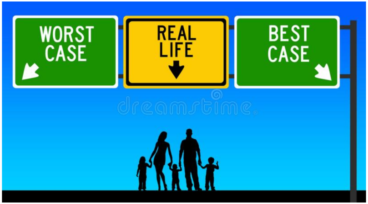

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Thank
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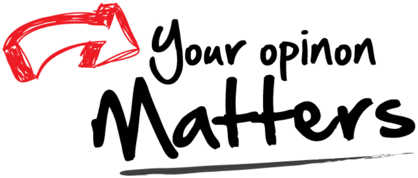

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