

Tutorial 1: Mathematical Preliminaries

APL 104 - 2022 (Solid Mechanics)

Q1. Show that $\underline{a} \cdot (\underline{A} \underline{b}) = (\underline{A}^T \underline{a}) \cdot \underline{b}$

Q2. There exists a tensor \underline{A} such that $\underline{A} \cdot \underline{e}_1 = \underline{a}$, $\underline{A} \cdot \underline{e}_2 = \underline{b}$, $\underline{A} \cdot \underline{e}_3 = \underline{c}$. What will be the matrix form of \underline{A} in $(\underline{e}_1, \underline{e}_2, \underline{e}_3)$ coordinate system?

Q3. Show that

$$(a) \quad (\underline{a} \otimes \underline{b}) \underline{C} = \underline{a} \otimes (\underline{C} \underline{b})$$

$$(b) \quad \underline{C} (\underline{a} \otimes \underline{b}) = (\underline{C} \underline{a}) \otimes \underline{b}$$

Q4. Given an anti-symmetric tensor \underline{A} , prove that $(\underline{A} \underline{x}) \cdot \underline{x} = 0 \quad \forall \underline{x}$

Q5. In class we learnt that a unique rotation tensor \underline{R} can be associated with transforming a set of orthonormal triad into another say $(\underline{e}_1, \underline{e}_2, \underline{e}_3) \rightarrow (\underline{\hat{e}}_1, \underline{\hat{e}}_2, \underline{\hat{e}}_3)$. In particular, we discussed a specific case where $(\underline{\hat{e}}_1, \underline{\hat{e}}_2, \underline{\hat{e}}_3)$ is obtained by rotation of $(\underline{e}_1, \underline{e}_2, \underline{e}_3)$ about \underline{e}_3 axis by angle θ . Find the matrix form of this rotation tensor \underline{R} in $(\underline{\hat{e}}_1, \underline{\hat{e}}_2, \underline{\hat{e}}_3)$ coordinate system.

