## Quiz 2

Total marks: 15, Total time: 45 mins, Multiple options MAY BE CORRECT. For every incorrect option, you would lose 50% of the total marks of the question!

- 1. [1 mark] Which of the following assumptions are required to have a linear-elastic stressstrain relation?
  - (a) material should be isotropic (unrelated)

(b) all strain components should be small

- (c) material should be homogeneous (unrelated) (d) stress-strain relation is considered only up to the elastic limit (propositionality limit)
- 2. [1 mark] For a linear elastic anisotropic material, the number of independent material constants are
- (b) 21 (a) 2 (c) 36 (d) 81
  - 3. [1 mark] A material is heated up while it is rigidly restrained such that it undergoes no strain. Then which of the following could be true:
    - (Material properties can change with temperature charge)

      Etchar = Eelastic + Ethermal

      Elastic = - Ethermal (a) the material property of the bar may change (b) thermal strain will be zero (c) thermal strain could be non-zero
    - (d) the elastic part of the strain could be non-zero
  - 4. [1 mark] A body is made of an *incompressible* material that is non-homogeneous but isotropic in nature. Which of the following would be true: > means v = 0.5 everywhere
    - (a) the volumetric strain is zero at every point in the body (because it is incompressible
      - (b) only the total volume of the body does not change but local volume can always increase or decrease
      - (c) the Poisson's ratio is different at every point within the body
    - (d) the Poisson's ratio is the same at every point within the body
  - 5. [3 marks] A body is subjected to a biaxial test under plane stress condition ( $\sigma_{zz} = \tau_{zx} =$  $\tau_{zy} = 0$ ) with an in-plane loading such that  $\sigma_{xx} = 2\sigma_{yy}$ .

(a) [1.5 marks] The ratio of 
$$\sigma_{xx}$$
 to  $\epsilon_{xx}$  will be

i.  $(2-\nu)/2E$ 

ii.  $(1-\nu)/2E$ 

iii.  $2E/(2-\nu)$ 

iv.  $2E/(1-\nu)$ 

$$\epsilon_{xx} = \frac{1}{E} \left( \sum_{x} - y \left( \frac{1}{2} \right) + \frac{1}{2} \right)$$

iv.  $2E/(1-\nu)$ 

(b) [1.5 marks] The ratio between  $\epsilon_{xx}$  and  $\epsilon_{yy}$  in terms of  $\nu$  will be

i. 
$$(1-2\nu)/(2-\nu)$$
  
ii.  $(2-\nu)/(2+\nu)$   
iii.  $(1+2\nu)/(2+\nu)$   
iv.  $(2-\nu)/(1-2\nu)$   

$$= \frac{1}{\mathbb{E}} \left( \frac{1}{2} \sqrt{2} \times \frac{1}{2} \sqrt{2} \times \frac{1}{2} \right) = \frac{1-2\nu}{2\mathbb{E}} \sqrt{2} \times \frac{1}{2} \sqrt{2} \times \frac{1}{2} = \frac{1-2\nu}{2} \sqrt{2} \times \frac{1}{2} \times \frac$$

$$1 \qquad \frac{\mathcal{E}_{xx}}{\mathcal{E}_{yy}} = \frac{(2-y)}{(1-2y)}$$

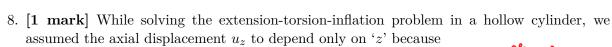
6. [1 mark] Which of the following statements is/are true regarding the partial derivative of basis vectors?



- (a)  $\partial \underline{e}_r/\partial r = 0$  and  $\partial \underline{e}_z/\partial z = 0$
- er ] -> varies only with &
- (b)  $\partial \underline{e}_r / \partial r = 0$  and  $\partial \underline{e}_\theta / \partial \theta = 0 \star$ (c)  $\partial \underline{e}_z / \partial z = 0$  and  $\partial \underline{e}_\theta / \partial \theta = 0 \star$
- (d) none of these
- 7. [1 mark] If the three displacement components in a cylindrical coordinate system are all constant

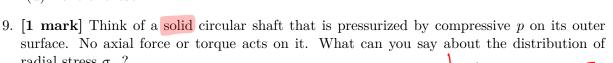


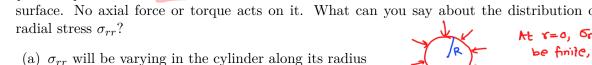
- (a) all strain components will be zero
- (b) all except hoop strain  $(\epsilon_{\theta\theta})$  will be zero
- $\checkmark$ (c) both  $\epsilon_{\theta\theta}$  and  $\epsilon_{r\theta}$  will be non-zero
  - (d) none of these



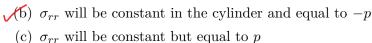


- (a) the dependence of  $u_z$  on r would lead to warping in the cross-section
- (b) the dependence of  $u_z$  on r on would violate axisymmetry
- (c) the dependence of  $u_z$  on r would lead to axial inhomogeneity
- (d) none of these

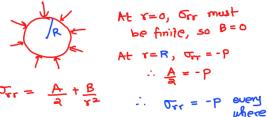




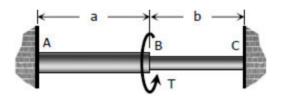




(d) None of these



10. [4 marks] The compound shaft shown in the figure below is attached to rigid supports. For the bronze segment AB, the diameter is 75mm,  $\tau \leq 60 \text{MPa}$ , and G = 35 GPa. For the steel segment BC, the diameter is 50mm,  $\tau \leq$  80MPa, and G = 83GPa. Determine the ratio of lengths  $\frac{b}{a}$  so that each material will be stressed to its permissible limit. What torque T is required?





## Solu:

In torsion, 
$$T = \frac{Tr}{J} \Rightarrow T = \frac{TJ}{r}$$

$$\frac{For \ bronze}{B} = \frac{60 \text{ MPa}}{B} = \frac{60 \text{ N/mm}^2}{60 \text{ MPa}} = \frac{35 \text{ GPa}}{35 \text{ MPa}} = \frac{35 \times 10^3 \text{ N/mm}^2}{35 \text{ MPa}}$$

$$J_B = \frac{\pi d_b^4}{32} = \frac{\pi (75)^4}{323}$$

Maximum allowable torque for bronze, 
$$T_b^{max} = \frac{C_b^{max} J_b}{r_b}$$

$$T_b^{max} = (60) \frac{\Pi(75)^q}{32} = 4970097 \text{ N mm}$$

$$\frac{75}{32} = 4.970 \text{ kN m}$$

For steel: 
$$T_s^{max} = 80 \text{ MPa} = 80 \text{ N/mm}^2$$
  
 $G_{1S} = 83 \text{ GPa} = 83 \times 10^3 \text{ N/mm}^2$   
 $J_S = \frac{\pi d_s^4}{33} = \frac{\pi (50^4)}{32}$ 

Maximum allowable torque for steel,  $T_s^{max} = \frac{T_s^{max} J_s}{T_s}$ 

$$T_s^{\text{max}} = \frac{(80) \frac{\pi (50)^4}{32}}{\frac{50}{2}} = 1963.495 \text{ N mm}$$

We have from geometric compatibility that the angle of twist O from bronze & steel must be same.

$$\Theta_{b} = \Theta_{s} - \Omega_{s}$$

$$\Rightarrow \frac{T_b^{max} L_b}{G_b J_b} = \frac{T_s^{max} L_s}{G_s J_s}$$

$$\Rightarrow \frac{4.970 \text{ (a)}}{\frac{1}{32}\pi(75^4) \text{ (35000)}} = \frac{1.963 \text{ (b)}}{\frac{1}{32}\pi(50^4) \text{ (83000)}}$$

$$\Rightarrow \frac{b}{a} = 1.186 \qquad \text{or} \quad \frac{a}{b} = 0.843 \quad \boxed{0}$$

Torque required, 
$$T = T_b^{max} + T_s^{max}$$
] (1)  
=  $4.970 + 1.963$   
=  $6.933 \text{ kNm}$