

CS 5012: Foundations of Computer Science

Asymptotic Complexity Exercise

Given the following code snippets, provide the worst case time complexity in the form of Big-O notation. Justify your response and state any assumptions made. Treat these functions as constant runtime: print(), append()

```
► def measure(inputList):
    int n = len(inputList)  O(1)
    int sum = 0;            O(1)
    for i in range(0, n):   O(n)
        for j in range(0, 5): n*O(1)
            sum += j * inputList[i]  n*O(1) = O(n)
        for k in range(0, n): n*O(n)
            sum -= inputList[k]      O(1)
```

The asymptotic complexity of this algorithm is: $O(n^2)$

$$T(n) = O(1) + O(1) + O(n) + O(1) + n \cdot O(1) + O(n) + n \cdot O(n) + O(1)$$

```
► def addElement(ele):
    myList = []          O(1)
    myList.append(666)    O(1)
    print myList         O(1)
```

The asymptotic complexity of this algorithm is: $O(1)$

$$T(n) = O(1) + O(1) + O(1)$$

Assume that num is a fixed!!!!

```
► num = 10                                O(1)

def addOnesToTestList(num):
    testList = []                          O(1)
    for i in range(0,num):                  O(num) = O(10) = O(1)
        testList.append(1)                  O(1)
        print(testList)                     O(1)

    return testList                         O(1)
```

The asymptotic complexity of this algorithm is: $O(n)$

$T(n) = O(1) + O(1) + O(n) + O(1) + O(1) + O(1)$

Assume that num is not fixed!!!

```
► testList = [1, 43, 31, 21, 6, 96, 48, 13, 25, 5]  O(1)

def someMethod(testList):
    for i in range(len(testList)):              O(n)
        for j in range(i+1, len(testList)):      n*O(n)
            if testList[j] < testList[i]:          n*n*O(1)
                testList[j], testList[i] = testList[i], testList[j]  n*n*O(1)
            print(testList)                        O(1)
```

The asymptotic complexity of this algorithm is: $O(n^2)$

$T(n) = O(1) + O(n) + n*O(n) + n*n*O(1) + n*n*O(1) + O(1)$

```
► def searchTarget(target_word):
    # Assume range variables are unrelated to size of aList

    for (i in range1):                          O(n)
        for (j in range2):                      n*O(n)
            for (k in range3):                  n*n*O(n)
                if (aList[k] == target_word):  n*n*O(n)
                    return 1                    O(1)

    return -1                                    O(1)
return -1                                       O(1)
```

The asymptotic complexity of this algorithm is: $O(n^3)$

$T(n) = O(n) + n*O(n) + n*n*O(n) + n*n*O(n) + O(1) + O(1) + O(1)$

Redo all above this section

```
► def someSearch(sortedList, target):  
    left = 0                                O(1)  
    right = len(sortedList) - 1             O(1)  
  
    while (left <= right):                   O(?)  
        mid = (left + right) / 2             O(1)*?  
        if (sortedList[mid] == target):      O(1)*?  
            return mid                       O(1)  
        elif (sortedList[mid] < target):     O(1)*?  
            left = mid + 1  
        else:  
            right = mid - 1  
  
    return -1
```

The asymptotic complexity of this algorithm is: O (_____)

```
► #Assume data is a list of size n  
    total = 0  
    for j in range(n):  
        total += data[j]  
    big = data[0]  
    for k in range(1, n):  
        big = max(big,  
data[k])
```

The asymptotic complexity of this algorithm is: O (_____)

```
► powers = 0  
k = 1  
while k < n:  
    k = 2*k  
    powers += 1
```

The asymptotic complexity of this algorithm is: O (_____)

```
► k = 1  
while k < n:  
    for j in range(k):  
        steps += 1  
    k = 2*k
```

The asymptotic complexity of this algorithm is: O (_____)

```
► for k in range(1,n):  
    j = 1  
    while j < k:  
        total += 1  
        j = 2 * j
```

The asymptotic complexity of this algorithm is: O (_____)