

CS 5012: Foundations of Computer Science

Asymptotic Complexity Exercise

Given the following code snippets, provide the worst case time complexity in the form of Big-O notation. Justify your response and state any assumptions made. Treat these functions as constant runtime: `print()`, `append()`

```
► def measure(inputList):
    int n = len(inputList)  O(1)
    int sum = 0;            O(1)
    for i in range(0, n):  O(n)
        for j in range(0, 5):  n*O(1)
            sum += j * inputList[i]  n*O(1) = O(n)
            for k in range(0, n):  n*O(n)
                sum -= inputList[k]  O(1)
```

The asymptotic complexity of this algorithm is: $O(n^2)$

$$T(n) = O(1) + O(1) + O(n) + O(1) + n \cdot O(1) + O(n) + n \cdot O(n) + O(1)$$

```
► def addElement(ele):
    myList = []  O(1)
    myList.append(666)  O(1)
    print myList  O(1)
```

The asymptotic complexity of this algorithm is: $O(1)$

$$T(n) = O(1) + O(1) + O(1)$$

► num = 10 O(1)

```
def addOnesToTestList(num):  
    testList = [] O(1)  
    for i in range(0,num): O(n)  
        testList.append(1) O(1)  
        print(testList) O(1)  
  
    return testList O(1)
```

The asymptotic complexity of this algorithm is: O (n)

$$T(n) = O(1) + O(1) + O(n) + O(1) + O(1) + O(1)$$

► testList = [1, 43, 31, 21, 6, 96, 48, 13, 25, 5] O(1)

```
def someMethod(testList):  
    for i in range(len(testList)): O(n)  
        for j in range(i+1, len(testList)): n*O(n)  
            if testList[j] < testList[i]: n*n*O(1)  
                testList[j], testList[i] = testList[i], testList[j] n*n*O(1)  
            print(testList) O(1)
```

The asymptotic complexity of this algorithm is: O (n^2)

$$T(n) = O(1) + O(n) + n*O(n) + n*n*O(1) + n*n*O(1) + O(1)$$

► def searchTarget(target_word):
 # Assume range variables are unrelated to size of aList

```
    for (i in range1): O(n)  
        for (j in range2): n*O(n)  
            for (k in range3): n*n*O(n)  
                if (aList[k] == target_word): n*n*O(n)  
                    return 1 O(1)  
  
    return -1 O(1)  
return -1 O(1)
```

The asymptotic complexity of this algorithm is: O (n^3)

$$T(n) = O(n) + n*O(n) + n*n*O(n) + n*n*O(n) + O(1) + O(1)+O(1)$$

```

▶ def someSearch(sortedList, target):
    left = 0
    right = len(sortedList) - 1

    while (left <= right):
        mid = (left + right) / 2
        if (sortedList[mid] == target):
            return mid
        elif (sortedList[mid] < target):
            left = mid + 1
        else:
            right = mid - 1

    return -1

```

The asymptotic complexity of this algorithm is: O (_____)

```

▶ #Assume data is a list of size n
    total = 0
    for j in range(n):
        total += data[j]
    big = data[0]
    for k in range(1, n):
        big = max(big,
            data[k])

```

The asymptotic complexity of this algorithm is: O (_____)

```

▶ powers = 0
    k = 1
    while k < n:
        k = 2*k
        powers += 1

```

The asymptotic complexity of this algorithm is: O (_____)

```

▶ k = 1
    while k < n:
        for j in range(k):
            steps += 1
        k = 2*k

```

The asymptotic complexity of this algorithm is: O (_____)

```
► for k in range(1,n):  
    j = 1  
    while j < k:  
        total += 1  
        j = 2 * j
```

The asymptotic complexity of this algorithm is: O (_____)