

## Sorting

*David Croft*

Introduction

Bubblesort

Stable sort

In-place

Selection sort

Other  
algorithms

Quicksort

Divide & Conquer

Comparing

Quiz

Recap

# Sorting algorithms

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March 18, 2018

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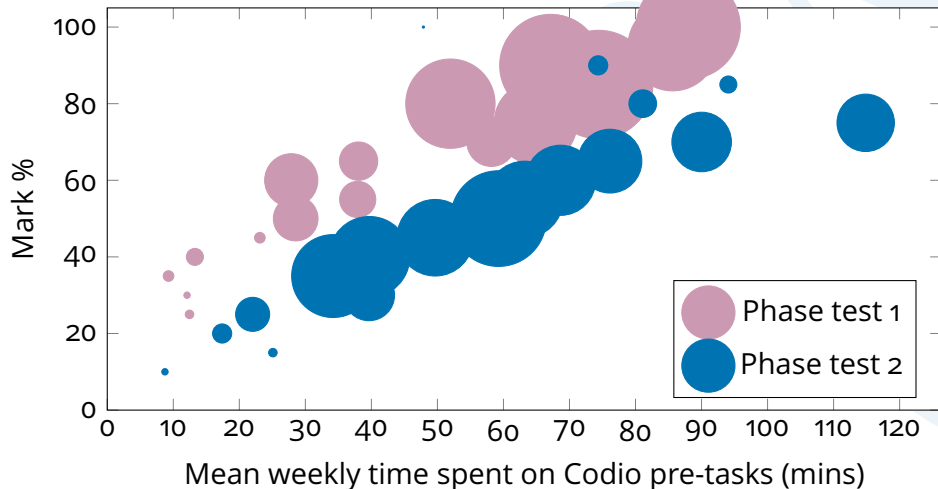
Quiz

Recap

- 1 Introduction
- 2 Bubblesort
  - Stable sort
  - In-place
- 3 Selection sort
- 4 Other algorithms
- 5 Quicksort
  - Divide & Conquer
- 6 Comparing
- 7 Quiz
- 8 Recap

You have all attempted the green Codio exercises for this week.

122COM results 2016-17 September starters.



Sorting is one of the classic problems for learning algorithms.

- Requirement for everything.
- Obvious applications like sorting text, statistics (median calculations).
- Less obvious, sorting objects in games for FOV (Field Of View) calculations.
- Route planning.

# Different algorithms

C

Lots of different algorithms, different ways to achieve the same thing.

- Going to be looking at several common/well known algorithms.
  - Bubblesort.
  - Selection sort.
  - Quick sort.
- Comparing and contrasting, advantages and disadvantages.

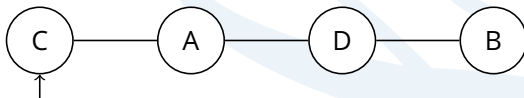
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- Compares each item to the next in the sequence.
  - Swap items if in wrong order.

## Pass 1

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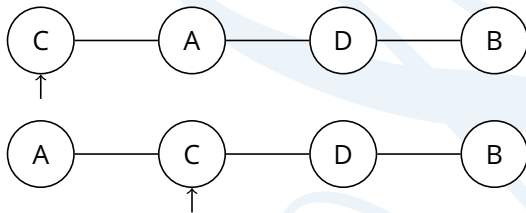
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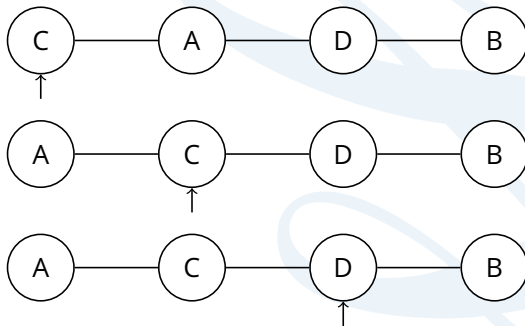
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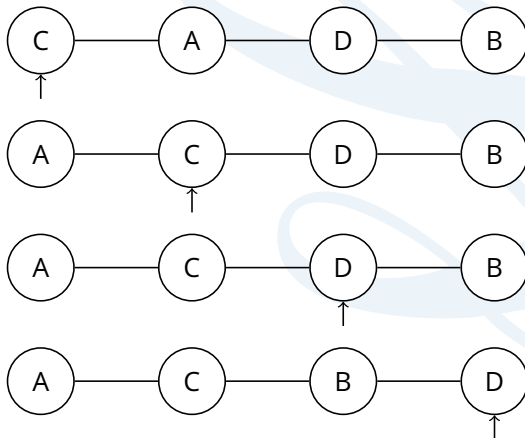
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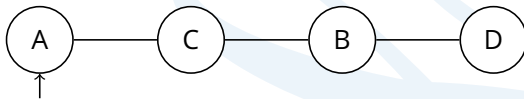
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Iterating over the sequence once isn't typically enough.

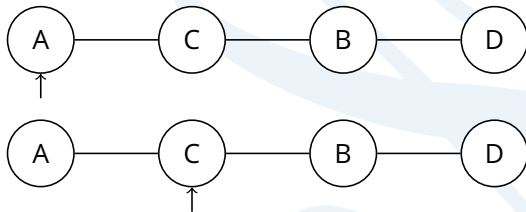
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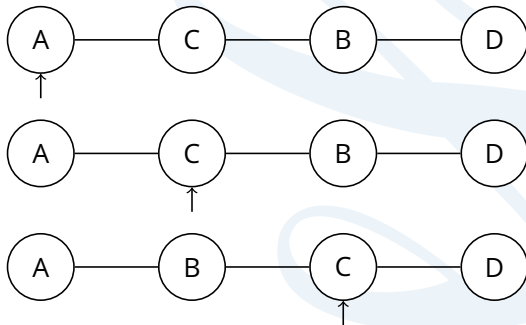


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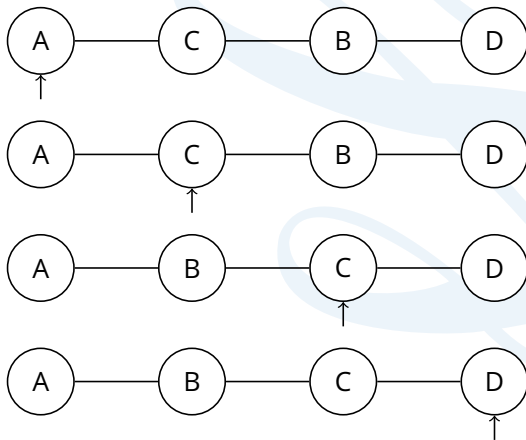
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Stable meaning that equivalent elements do not change their relative orders.



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Stable meaning that equivalent elements do not change their relative orders.

- Not important if e.g. sorting people by height.
- Important if e.g. you are sorting people by height and then sorting them by surname.
  - People with the same surname would still be in height order.
  - Can have performance benefits.

With unstable sorting algorithm the relative orders of equivalent elements can be changed.

In-place meaning that it only needs a small amount of additional memory in order to work.

- More memory efficient than the alternative.
  - Can be slower though.
- Can be important if...
  - ...dealing with large amounts of data.
  - ...have limited resources (i.e. embedded systems).
- Bubble sort only needs a few extra variables to swap the elements and to step through the sequence.

One of the simplest sorting algorithms.

- Explained here to introduce you to sorting concepts.
  - In-place, stable.

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  - Horrible performance, average is  $O(n^2)$ .
  - But best case is only  $O(n)$ .



The time taken to sort a sequence depends on:

- The starting order of the sequence.

For example, Bubblesorting a 100 elements:

So sorting algorithms have 3  $O()$  values.

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- Best case, already sorted.
  - Iterate over sequence once.
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- Worst case, in reverse order.
  - Iterate over sequence 100 times.
  - 10,000 comparisons.
- Average case, random order.
  - Somewhere in between.

So sorting algorithms have 3  $O()$  values.

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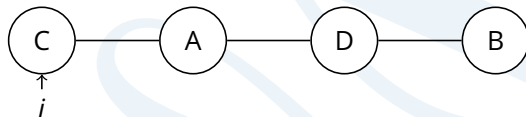
Recap

# Break

- Divides sequence into sorted and unsorted regions.
  - Stable/Unstable, depends on implementation.
  - In place.
- 1 Iterate over sequence.
  - 2 For each element search the remaining elements on its right for the smallest value.
  - 3 Swap smallest element with current element.

## Selection sort II

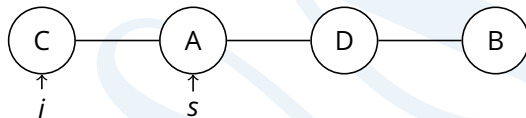
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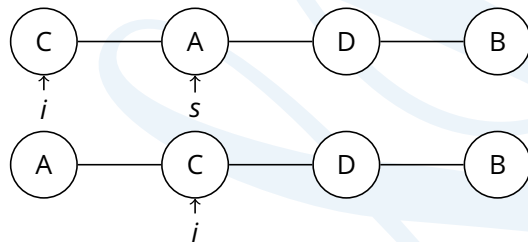


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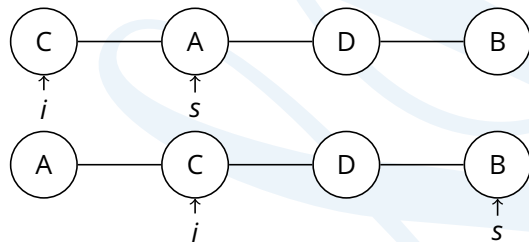
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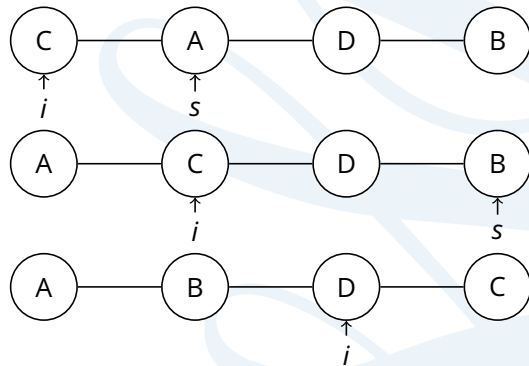




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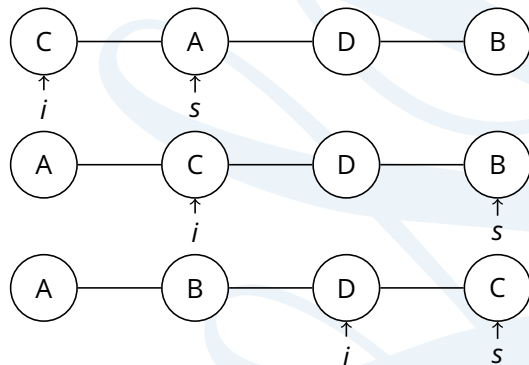
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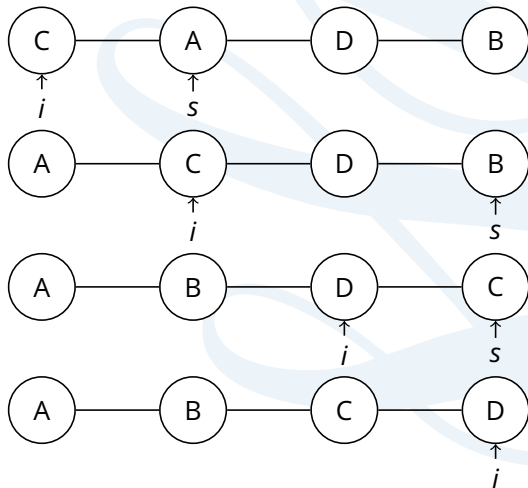
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Bubblesort is  $O(n^2)$  worst and average case .

Selection sort is  $O(n^2)$  worst and average case.

- Selection sort is generally faster than bubble.
  - But have same  $O()$  complexity.
  - What?

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Selection sort is  $O(n^2)$  worst and average case.

- Selection sort is generally faster than bubble.
  - But have same  $O()$  complexity.
  - What?
- $O()$  notation describes how an algorithm will grow.
- Not good at absolute performances.
- Selection sort typically does fewer comparisons and swaps than bubblesort.
  - Therefore typically faster.
- Best case bubblesort is  $O(n)$ , selection is  $O(n^2)$ .
  - So is occasionally faster.

## Many sorting algorithms

- Different trade-offs, performances.
- Some are just jokes.

1 Bead

2 Bogo

3 Bubble

4 Circle

5 Cocktail

6 Comb

7 Counting

8 Cycle

9 Gnome

10 Heap

11 Insert

12 Merge

13 Pancake

14 Patience

15 Permutation

16 Quick

17 Radix

18 Selection

19 Shell

20 Sleep

21 Stooge

22 Strand

23 Tree

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# Break

<https://www.youtube.com/watch?v=ZZuD6iUe3Pc>

Neither bubble or selection sort are very good.

- Simple algorithms but slow.
- Not (typically) used in real code.

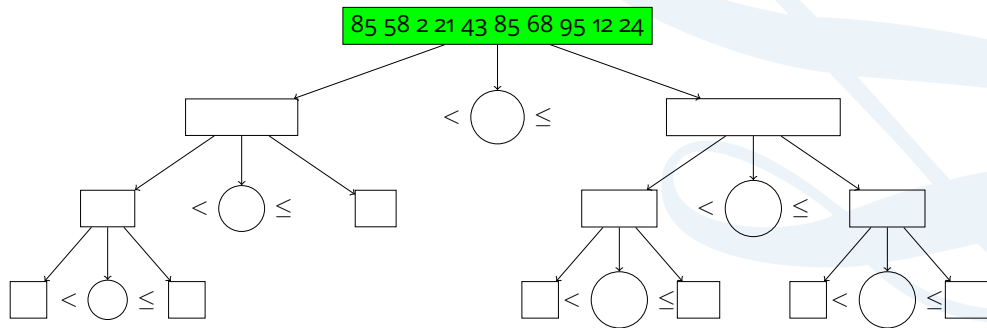
One of the fastest sorting algorithms.

- Used in real life.
- Recursively breaks the sequence in half.
  - Divide & Conquer.

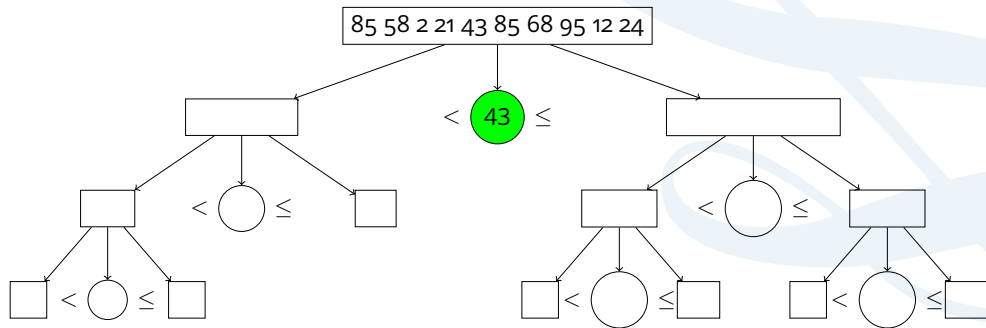


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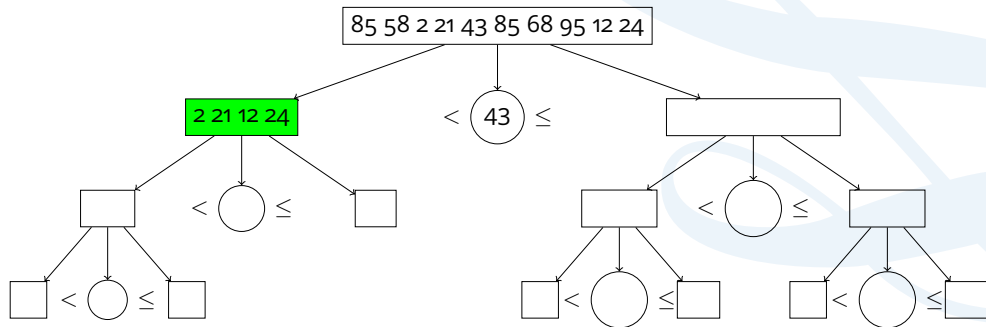
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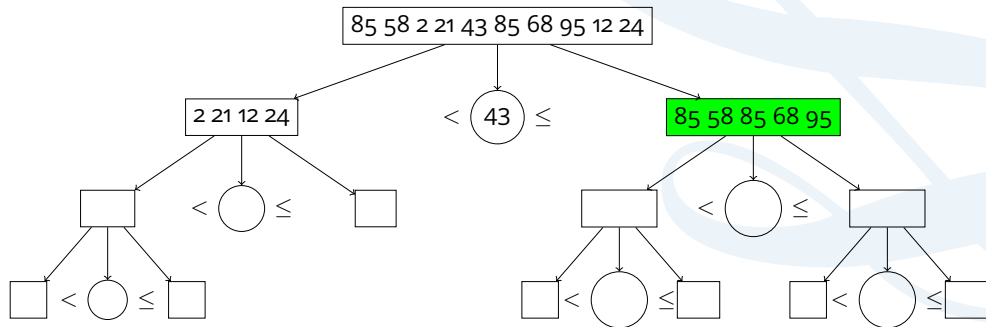
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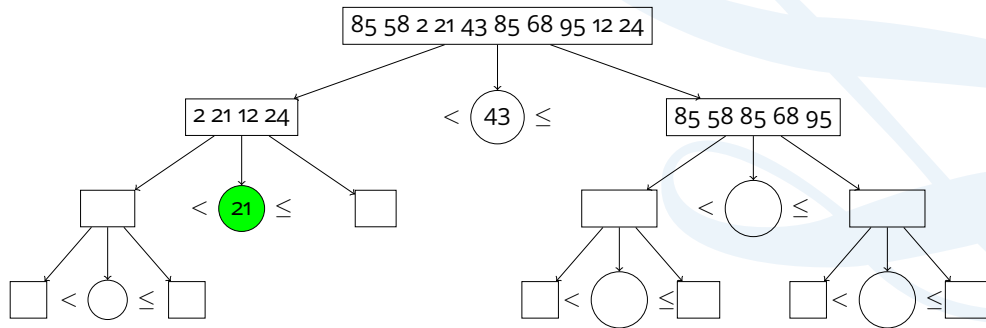
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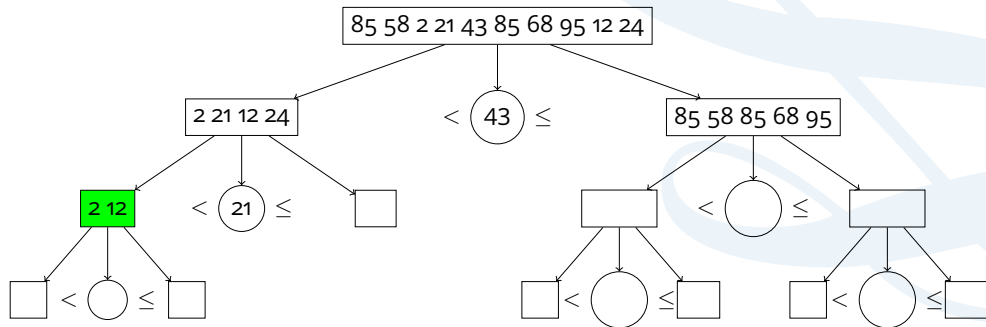
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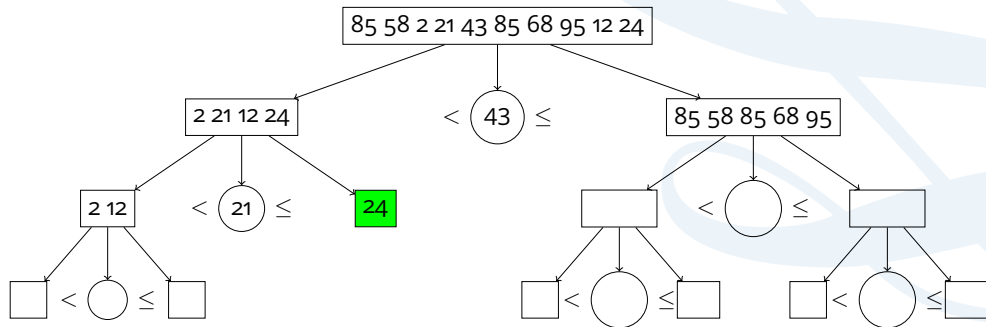
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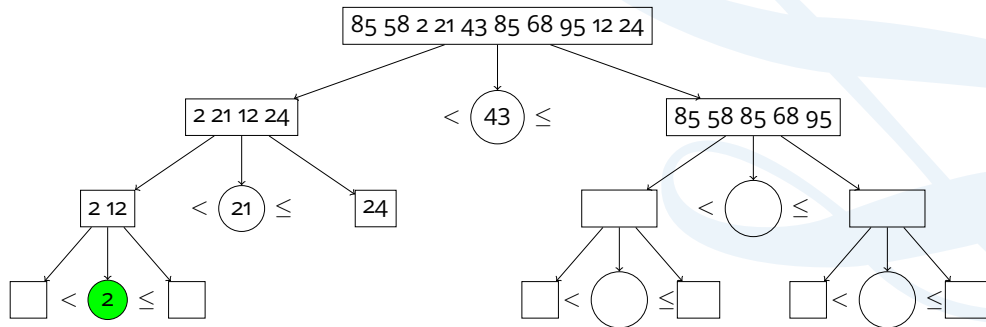


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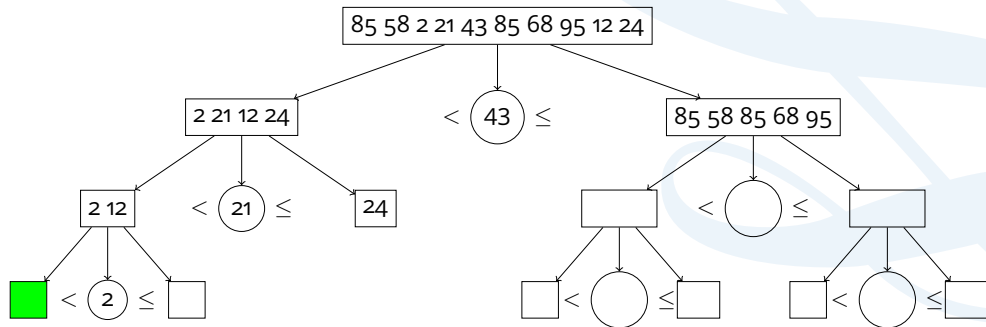




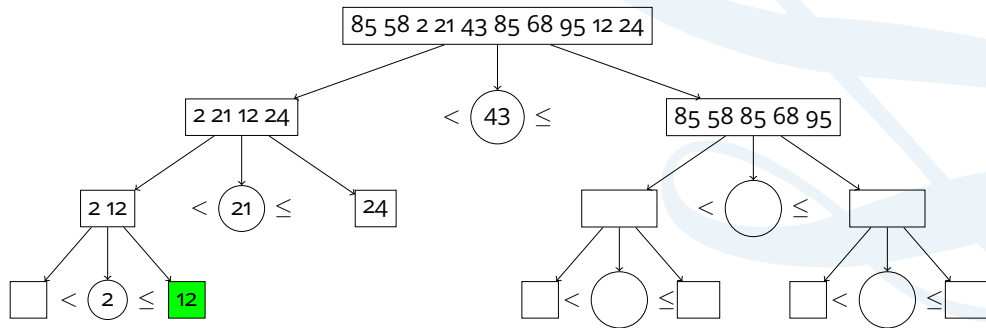
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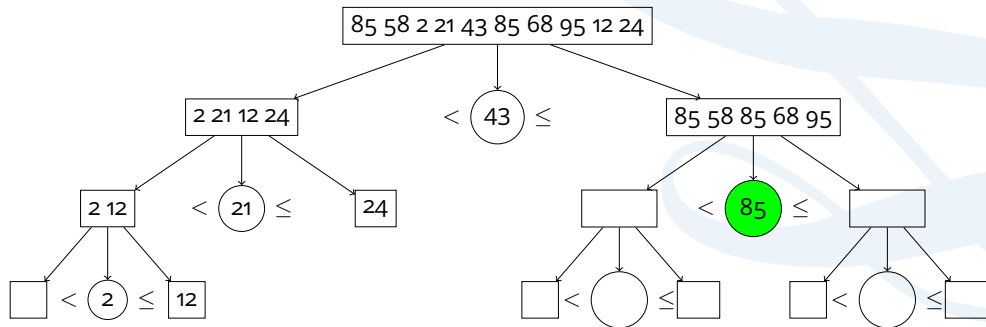
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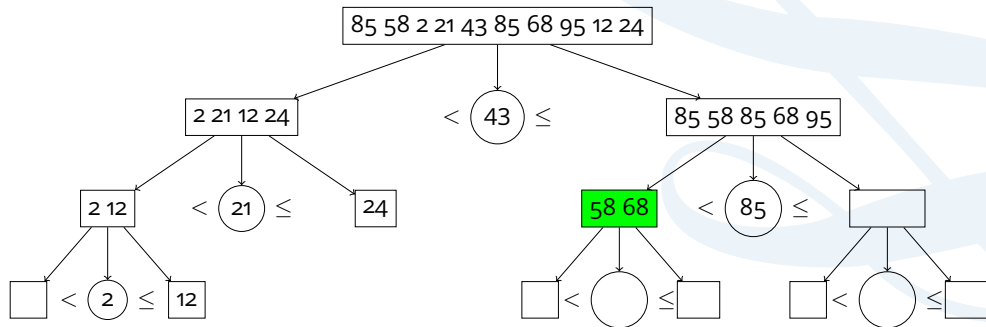
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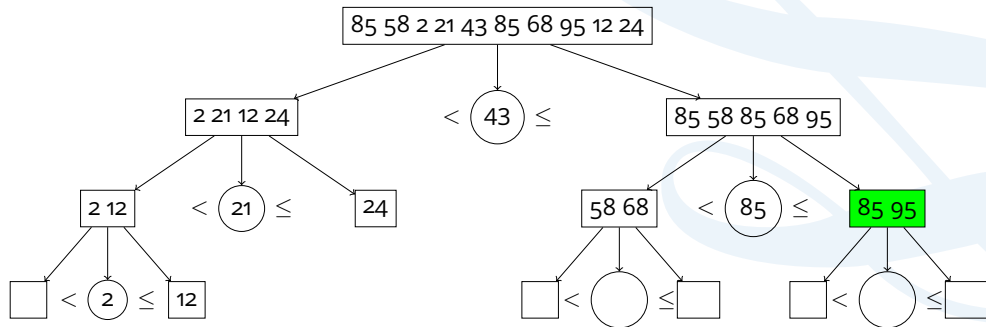
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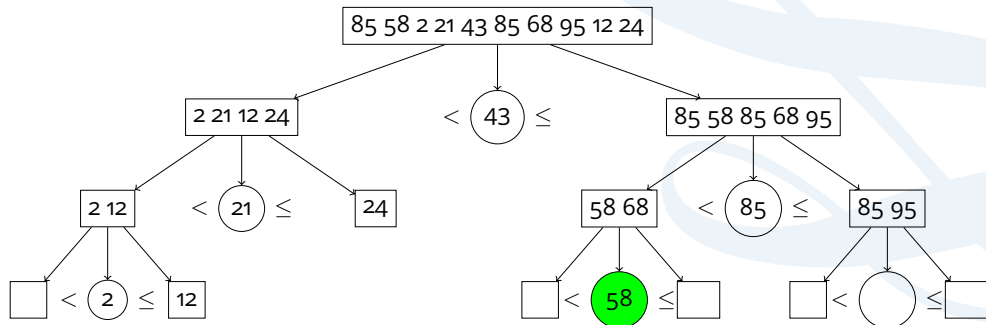
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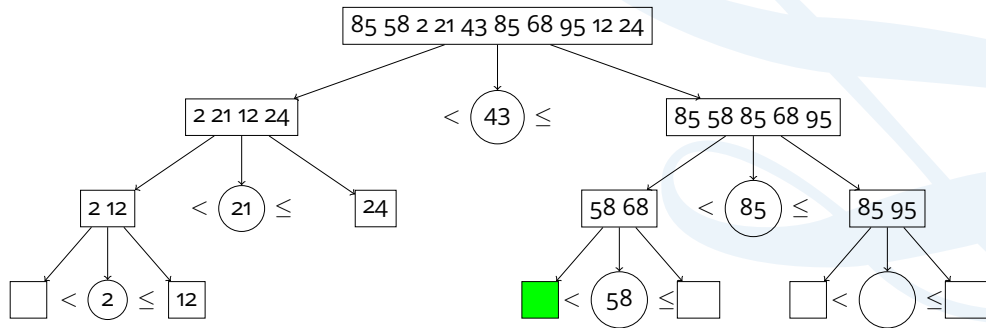
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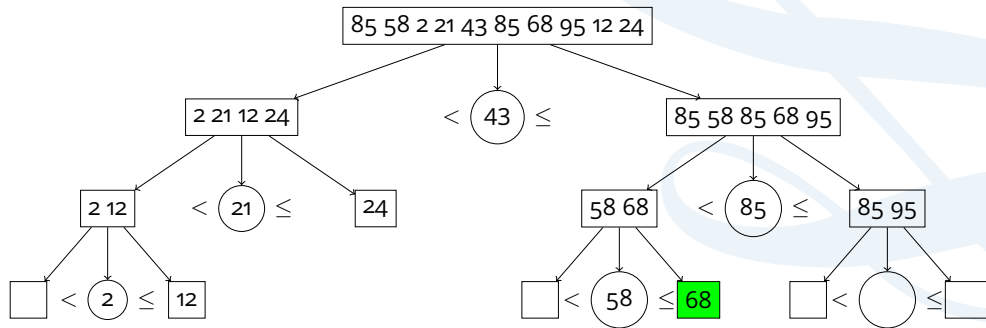


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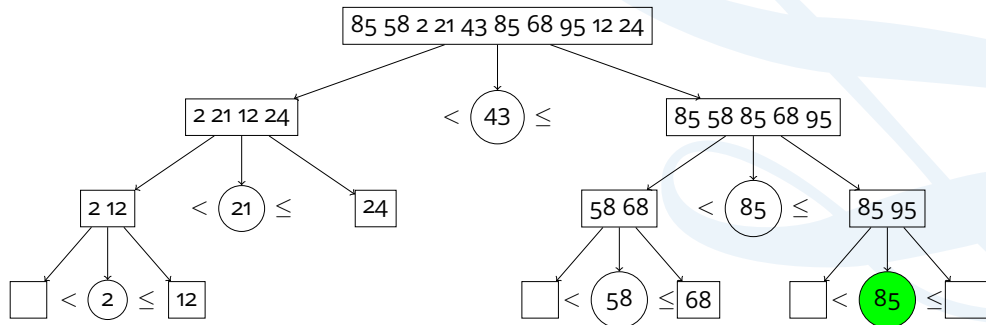




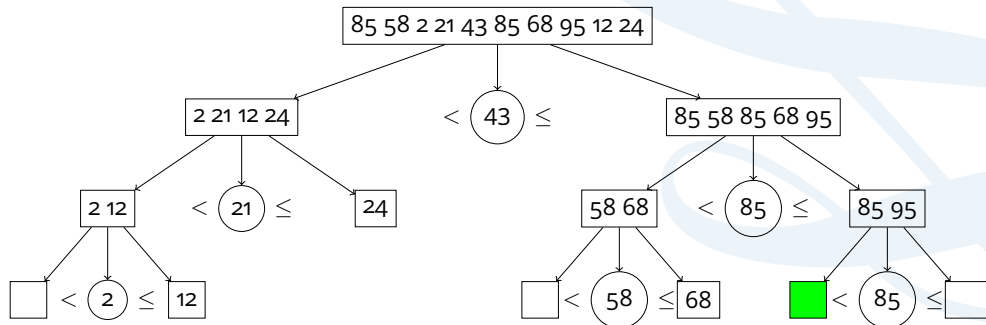
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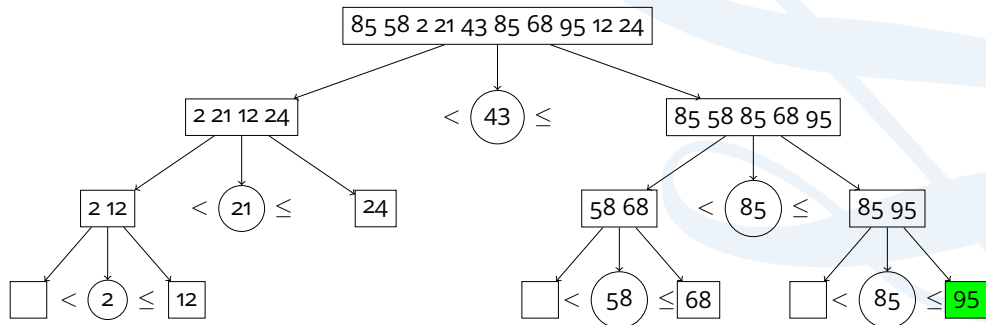
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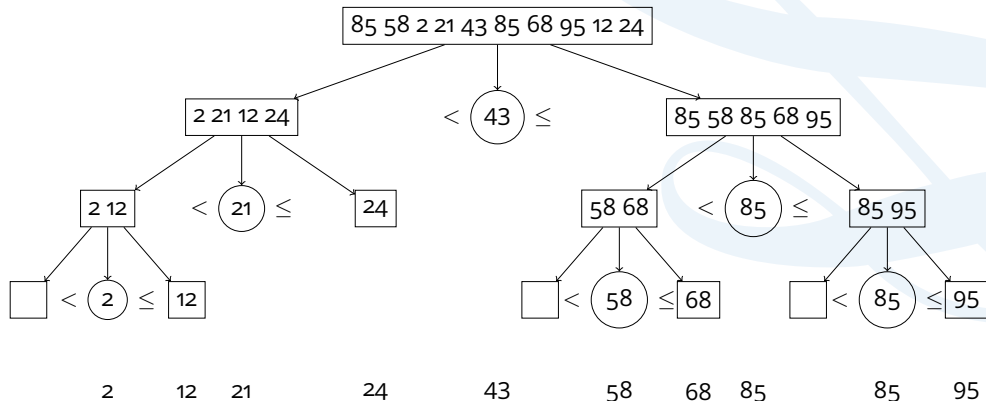
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## Quicksort is...

- ...sometimes in-place.
  - Depends on implementation.
- ...sometimes stable.
  - Depends on implementation.

## Some issues with the original algorithms (1959).

- Choosing the pivot.
  - First element.
  - Middle element.
  - Average of first, middle and last.
- Repeated elements.
  - Fat partition.

Quicksort is a divide and conquer algorithm.

- Too hard to sort the whole sequence?
- Divide the problem.
  - Still too hard?
  - Divide the problem.
    - Still too hard?
    - Divide the problem.
    - Etc, etc, etc.

Naturally suited for parallelism.

- Each sub problem can be processed separately.

# Comparing algorithms



Have seen there are many ways to sort.

- Best sorting algorithm depends on multiple factors.
- Good in one situation is bad in another.





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  - Sequential memory (arrays)?

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  - EEPROM? cheap to read, expensive to write.

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- Consistent performance.
  - Selection sort.

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# Quiz

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- The sequence is in reverse order.
- The sequence contains a few distinct values that are repeated.



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Divide & Conquer algorithms work by \_\_\_\_\_

- Dividing the problem in half.
- Breaking problems down into smaller easier problems.
- Simplifying the code so that they run faster.
- Invading Czechoslovakia.

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- Dividing the problem in half.
- Breaking problems down into smaller easier problems.
- Simplifying the code so that they run faster.
- Invading Czechoslovakia.

Which of the following algorithms are NOT divide & conquer?

- Bubblesort.
- Bubblesort and selection sort.
- Selection sort.
- Quicksort.

Which of the following algorithms are NOT divide & conquer?

- Bubblesort.
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- Selection sort.
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Which algorithm uses a pivot value to repeatedly halve the sequence?

- Bubblesort.
- Selection sort.
- Quicksort.
- All of the above.

Which algorithm uses a pivot value to repeatedly halve the sequence?

- Bubblesort.
- Selection sort.
- Quicksort.
- All of the above.

The worst sorting algorithm is \_\_\_\_\_

- Bubblesort.
- Bogo sort.
- Sleep sort.
- Selection sort.



The worst sorting algorithm is \_\_\_\_\_

- Bubblesort.
- **Bogo sort.**
- Sleep sort.
- Selection sort.

# Why do I care?

## Everyone

- Sorting algorithms are key to understanding many important concepts.
  - I.e. Binary Search Trees.
- Key to writing efficient code.
- Key to understanding memory/processor trade offs.
- Useful in teaching algorithmic thinking.
  - Algorithm design.
  - Comparing and contrasting different algorithms.
  - Divide and Conquer concepts.
- Employability skill, popular questions for programming interviews.

- Many sorting algorithms.
- Bubblesort.
- Selection sort.
- Quicksort
- Advantages/disadvantages.
  - In place.
  - Stable.
  - Divide and Conquer.
- Performance
  - $O()$
  - Sequence type.
  - Read/writes.
  - Size of  $n$ .

- Complete the yellow Codio exercises for this week.
- Attempt the green Codio exercises for next week.
- If you have spare time attempt the red Codio exercises.
- If you are having issues come to the PSC.  
<https://gitlab.com/coventry-university/programming-support-lab/wikis/home>

## Sorting

*David Croft*

Introduction

Bubblesort

Stable sort

In-place

Selection sort

Other  
algorithms

Quicksort

Divide & Conquer

Comparing

Quiz

Recap

# The End