Hashing

**David Croft** 

Finding things

Hashes

What is a ha

Collisions

Using them in coi

Bloom filters

# Hashing

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What is a hash Load Collisions

Bloom filter

# 1 Finding things

- 2 Hashes
  - What is a hash
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  - Collisions
  - Using them in code
- 3 Bloom filters



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Already seen binary search faster than linear.

- But binary search only works on ordered sequences.
  - Sorted list/array, Binary Search Trees (BSTs) etc.
- lacksquare  $O(\log n)$  vs. O(n).
- What's better than O(n)?
  - O(1).

Can we lookup values in O(1) time?



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Want to store information on all UK motorways.

49 motorways.

# Option 1.

- Unordered sequence.
- List/array/vector.
- Finding specific motorway is O(n).
- Space required, O(n).

Pos	Motorways
0	M9
1	M55
2	M898
3	M4
4	M1
5	M6

. . .

45	M2
46	M56
47	M53
48	M3



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## Option 2.

- Ordered sequence.
- Sorted List/array/vector or BST.
- Finding specific motorway is  $O(\log n)$ .
- Space required, O(n).

Pos	Motorways
0	M1
1	M2
2	M3
3	M4
4	M5
5	M6

. .

45	M606
46	M621
47	M876
48	M898



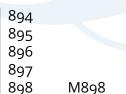
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# Option 3

- Lookup table.
- Each motorway stored in position corresponding to it's number.
  - E.g. M<sub>1</sub> in position 1, M<sub>53</sub> in position 53.
- Finding specific motorway is O(1).
  - Very fast.
- Space required, O(max(n)), 899 spaces.
  - Very inefficient...in this case.
  - Can be VERY efficient, massive time savings for small memory cost.

Pos	Motorways
0	
1	M1
2	M2
3	M3

53	M53		
54	M54		
55	M55		
56	M56		





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# Option 4

- Hash table.
- Pass each motorway through a hash function.
- Store hashes in lookup table.
- Finding specific motorway is O(1) ish.
- igoplus Space required, O(n).



### Hash tables.

Unordered associative arrays.

- Unordered we have no control over the item orders.
- Associative Lookup a value based on a key.
  - I.e. Python dict(), C++ map<>.
- Fast.
  - O(1) lookup (potentially).
  - $\bigcirc$  O(1) < Reality < <math>O(n).



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Hash is just a number.

- Based on some other value.
- Motorway example hash could just be the M-number.
  - $\blacksquare \text{ l.e. M898} \rightarrow 898.$

What if key is not an int?

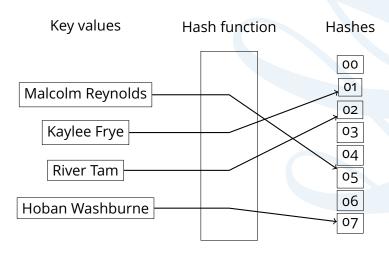
- Hash function.
- Converts an input of any size/range to a fixed size/range.
- Related to, but distinct from:
  - Checksums.
  - Fingerprints.
  - Parity codes.



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Signs of a good hash table hashing algorithms.

- Computationally lightweight.
- Evenly distributed hashes.
  - E.g. len() would be terrible hash function, loads of different inputs produce same value.

CRC32 hash
3840495446
3523407757
1191942644
3877468994
192271774



# Finding things Hashes What is a hash Load Collisions Using them in c

### So how does a hash function work?

- Depends on hash function and purpose.
- Not going to be implementing any real algorithms.
  - Optimized to be very fast, not understandable.
  - Generally full of binary representations.
  - Bit shifting.
- Simple hashing algorithm (division method).
  - Break the thing being hashed into blocks.
    - 1, 2, 4, 8, 16 bytes in size.
  - 2 Add up all the blocks.
  - Modulo by a prime number.



# Cryptographic hashses.

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Side note, different hashes for different purposes.

- Hash table hashes.
  - Computationally lightweight as possible.
- Cryptographic hashes.
  - $\blacksquare$  Computationally lightweight-ish to go key  $\rightarrow$  hash.
  - $lue{}$  Computationally expensive to go hash o key.
  - MD (Message-Digest algorithm)
    - Famously MD5, widely used, no longer secure.
    - MD6 still good.
  - SHA (Secure Hash Algorithm)
    - SHA-o, SHA-1 not secure.
    - SHA-2, SHA-3 still good.



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Hang on a minute, there's problem.

- Hashed "buckeroo" with CRC32.
  - CRC32 **NOT** best choice for hash table but is easy and widespread.
    - Hash of 1306201125
- So our hash table needs at least 1,306,201,125 slots.
  - 4 bytes per integer \* 1306201125 slots = 5.2 gigabytes.
  - Not going to work.
- Solution? Take the modulo of the hash.
  - Create table of small size.
  - slot = hash % len(hashtable)



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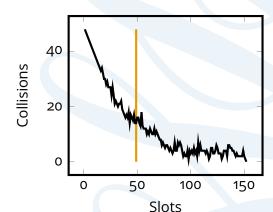
Converting big sequences into short hashes.

- Any downsides?
- Some distinct sequences **MUST** produce same hash.
- Hash collision.
- I.e. Hashing an int
  - int has 4 billion possible values.
  - If hash is one byte, then 256 possible slots.
  - 4 billion possible values in 256 possible slots, collisions will happen.
- E.g. CRC32 hash.
  - "plumless"  $\rightarrow$  1306201125  $\leftarrow$  "buckeroo"



Bigger the hash table == less collisions.

- Ideal motorway hash table.
  - 49 motorways.
  - 49 slots.
  - o collisions.
- Reality.
  - 49 slots.
  - 14 collisions.
  - I.e. M<sub>1</sub>8, M<sub>6</sub>7 and M<sub>6</sub>06 in slot 18.



- Optimal.
  - 152 slots.
  - o collisions.
  - Size only 3.1 times ideal.



Number of collisions depends on load factor (1).

- $\blacksquare$  Ratio of elements (*n*) to available slots (*k*).
  - $I = \frac{n}{k}$
- High load = lots of collisions (probably).
- Low load = few collisions (probably).
- I > 1.0 = definitely some collisions.
- Previous motorway example.
  - 49 motorways, 49 slots, *l* = 1
  - 49 motorways, 152 slots, *l* = 0.31



## Real world hash tables.

- Automatically resize to provide more slots as load increases.
- Advantages
  - Table size adjusts for the amount of elements stored in it.
  - Minimal wasted memory.
- Disadvantages
  - Have to shuffle everything around when the table resizes.
  - Not all that time consuming.



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So what do we do when we have collisions?

- If have  $\geq$  1 elements then collisions are possible.
  - Regardless of table size.
- Two main approaches

# Separate chaining.

- Each slot is a linked list.
- Infinitely resizeable.
- Add new item to end of the list.

# Open addressing.

- Slot is already full?
- Try next slot until an empty one is found.



# Handle collisions II

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Separate chaining.

1306201125

buckeroo

 $\begin{array}{c|c}
Slot \\
o \rightarrow & limpet \\
1 \rightarrow & zombie
\end{array}$ 

plumless

gondola

 $\geq$   $\rightarrow$ 

3 -

 $\rightarrow$ 

5 →

Slot

 $\rightarrow$ 

→ buckeroo

Open addressing

buckeroo 1306201125

⇒ 2 ⇒ 3

3 plumless

4 buckeroo

limpet zombie

gondala



# Hash tables in Python

```
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```

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Dictionaries!

```
import sys
def main():
   motorways = {}
   motorways["M1"] = (193.5, 1959)
   motorways["M2"] = (25.7, 1963)
   motorways["M3"] = (58.6, 1971)
   motorways["M4"] = (191.9, 1961)
   motorways["M898"] = (0.5, 1985)
   print( 'The %s is %0.1f miles long' % ("M4",

→ motorways["M4"][0]) )

   print( 'The %s opened in %d' % ("M898",
   motorways["M898"][1]) )
if __name__ == '__main__':
   sys.exit(main())
```



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Maps!

```
#include <iostream>
#include <map>
using namespace std;
int main()
    map< string, pair<float,int> > motorways;
    motorways.emplace( "M1", make_pair<float,int>(193.5, 1959) );
                        [...]
    motorways.emplace( "M898", make_pair<float,int>( 0.5, 1985 ) );
    cout << "The " << "M1" << " is " <<
        motorways.find("M1")->second.first << " miles long" << endl;</pre>
    cout << "The " << "M898" << " opened in " <<
        motorways.find("M898")->second.second << endl;</pre>
    return 0;
```



Using them in code

Hashes have many other possible applications.

- Finding duplicates.
  - Hash table but count number of things in each slots.
- Similarity comparisons.
  - E.g. Soundex, Metaphone.
  - Names that sound the same have same hash.
- Image recognition.
- Bloom filters.
  - Are almost magic.



Harry Potter



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**Bloom filters** 

### Neat trick with hashes.

- Can 'store' 1000 things in the space for 100.
  - Doesn't actually store the items.
  - Can say if an element is not a member of a set.
  - Can say if element is probably a member of a set



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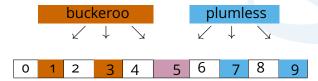
Bloom filters

To add a value to the filter.

- Hash the value using multiple different functions.
- Mark the slots for each of those hashes.

To test for a value in the filter.

- Hash the value using all the functions.
  - If not all the slots are marked then value not in filter.
  - If all slots are marked then value *probably* in filter.







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**Bloom filters** 

# Bloom filters are almost magic.

- 1000 items
- ≤ 1% error
- 7 hash functions
- 9586 slots
  - 1 bit per slot.
- 'Store' 1000 integers in the space for 300.
  - Bigger variables mean bigger savings.



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- Hash table lookups O(1).
  - Pretty much, reality is more complex.
- Different hash algorithms for different purposes.
  - I.e. cryptographic hashes
- Different objects can produce same hash.
  - Hash collision.
- Bloom filters
  - Can say item definitely not in set.
  - Can say item probably in set.



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# The end of 122COM... ... or is it?

