

Sorting algorithms

David Croft

Coventry University

david.croft@coventry.ac.uk

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 - Stable sort
 - In-place
- 3 Selection sort
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Sorting is one of the classic problems for learning algorithms.

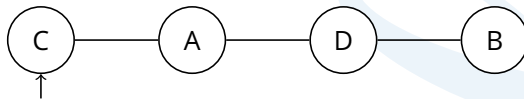
- Requirement for everything.
- Obvious applications like sorting text, statistics (median calculations).
- Less obvious, sorting objects in games for FOV (Field Of View) calculations.
- Route planning.

Very simple sort.

- Compares each item to the next in the sequence.
 - Swap items if in wrong order.

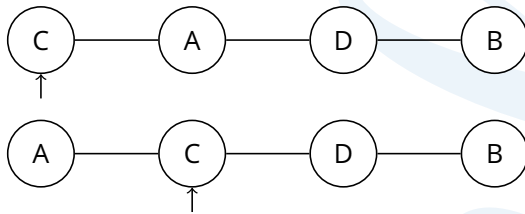
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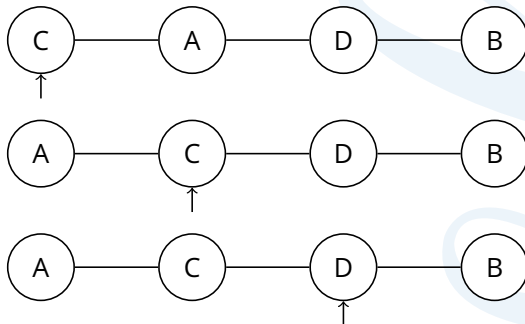
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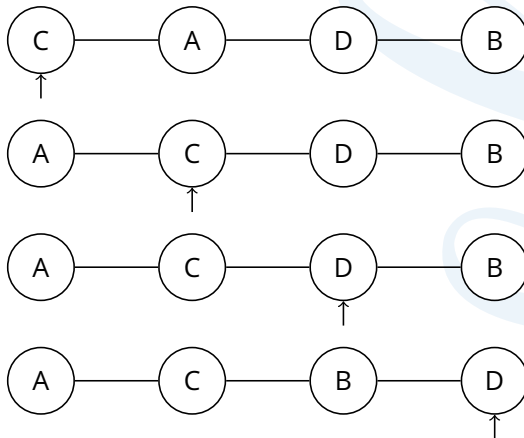
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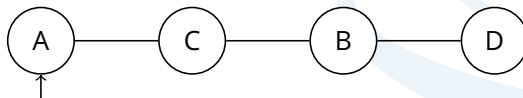
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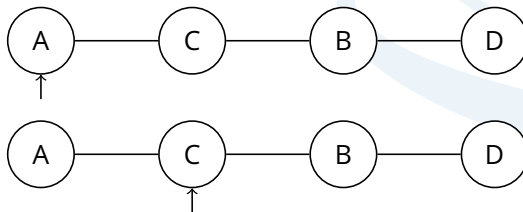
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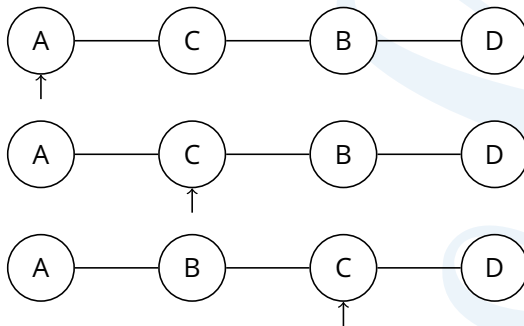
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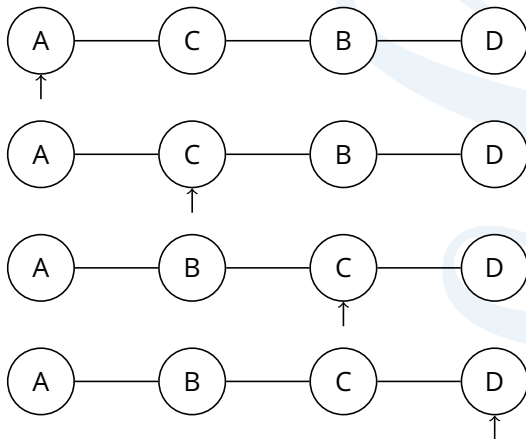
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With unstable sorting algorithm the relative orders of equivalent elements can be changed.

In-place meaning that it only needs a small amount of additional memory in order to work.

- More memory efficient than the alternative.
- Can be important if...
 - ...dealing with large amounts of data.
 - ...have limited resources (i.e. embedded systems).
- Bubble sort only needs a few extra variables to swap the elements and to step through the sequence.

One of the simplest sorting algorithms.

- Explained here to introduce you to sorting concepts.
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- Is rubbish.
 - Horrible performance, average is $O(n^2)$.
 - But best case is only $O(n)$.



The time taken to sort a sequence depends on:

- The starting order of the sequence.

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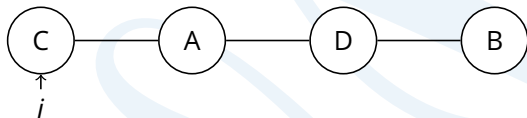
- Best case, are already sorted.
 - Iterate over sequence once.
 - 100 comparisons.
- Worst case, in reverse order.
 - Iterate over sequence 100 times.
 - 10,000 comparisons.
- Average case, random order.
 - Somewhere in between.

So sorting algorithms have 3 $O()$ values.

- Divides sequence into sorted and unsorted regions.
 - Not stable.
 - In place.
- 1 Iterate over sequence.
 - 2 For each element search the remaining elements on its right for the smallest value.
 - 3 Swap smallest element with current element.

Selection sort II

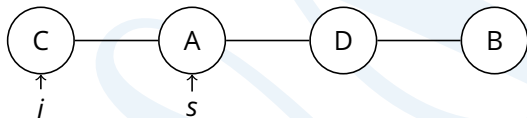
C



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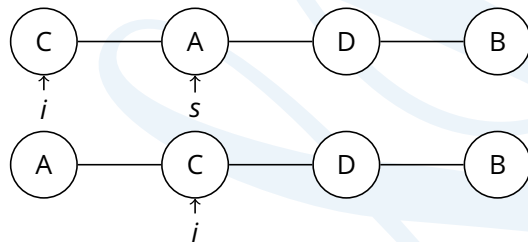


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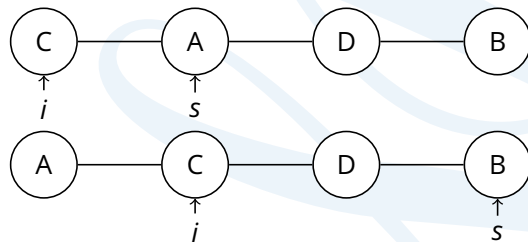
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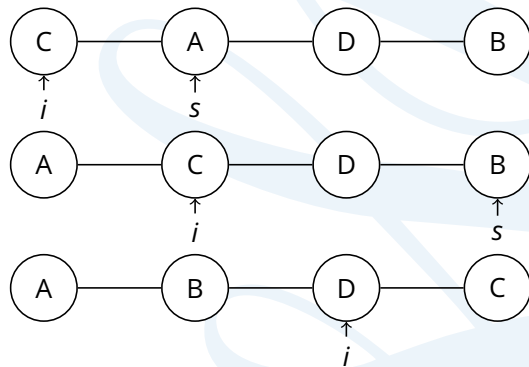
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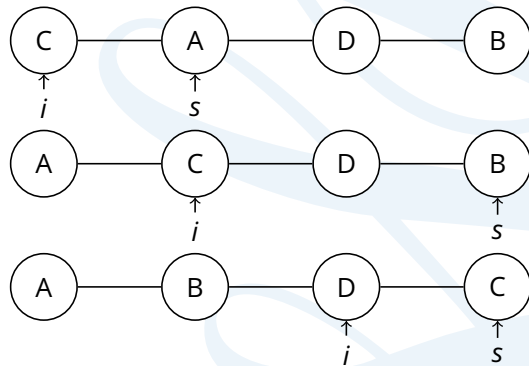
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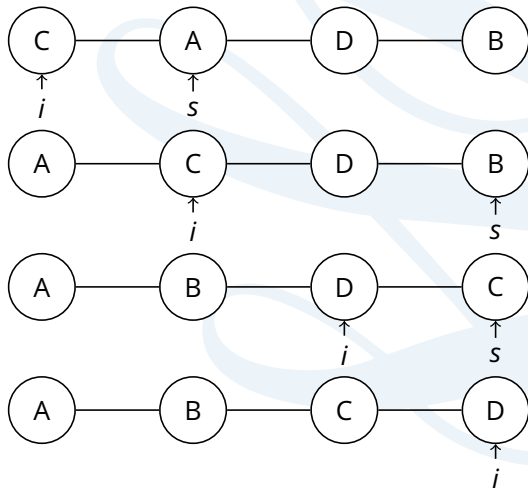
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Bubblesort is $O(n^2)$ worst and average case .

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- Selection sort is generally faster than bubble.
 - But have same $O()$ complexity.
 - What?

Bubblesort is $O(n^2)$ worst and average case .

Selection sort is $O(n^2)$ worst and average case.

- Selection sort is generally faster than bubble.
 - But have same $O()$ complexity.
 - What?
- $O()$ notation describes how an algorithm will grow.
- Not good at absolute performances.
- Selection sort typically does fewer comparisons and swaps than bubblesort.
 - Therefore typically faster.
- Best case bubblesort is $O(n)$, selection is $O(n^2)$.
 - Occasionally faster.

Many sorting algorithms

- Different trade-offs, performances. <https://www.youtube.com/watch?v=ZZuD6iUe3Pc>
- Some are just jokes.

1 Bead

2 Bogo

3 Bubble

4 Circle

5 Cocktail

6 Comb

7 Counting

8 Cycle

9 Gnome

10 Heap

11 Insert

12 Merge

13 Pancake

14 Patience

15 Permutation

16 Quick

17 Radix

18 Selection

19 Shell

20 Sleep

21 Stooge

22 Strand

23 Tree

Neither bubble or selection sort are very good.

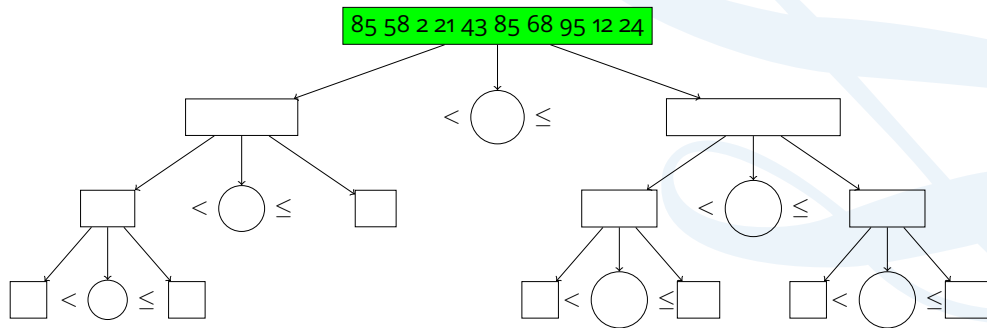
- Simple algorithms but slow.
- Not used in real life.

One of the fastest sorting algorithms.

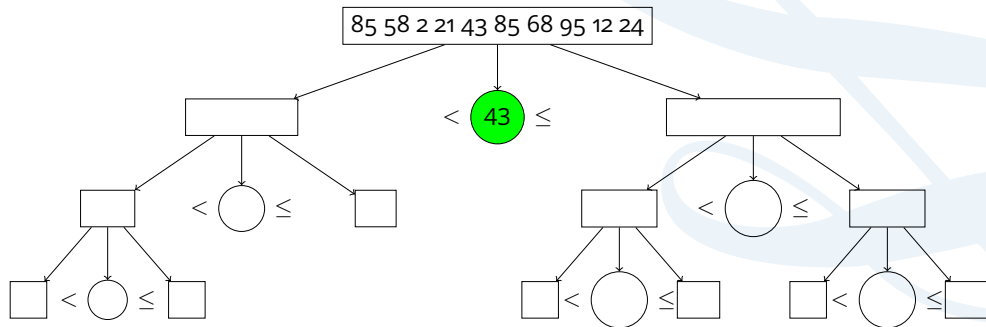
- Used in real life.
- Recursively breaks the sequence in half.
 - Divide & Conquer.

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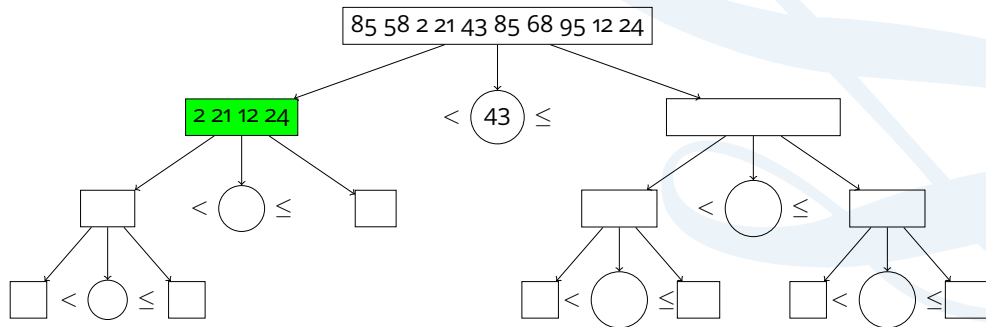
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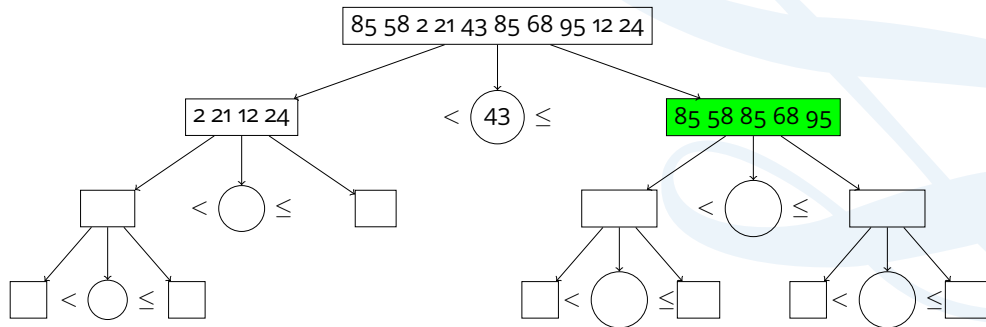
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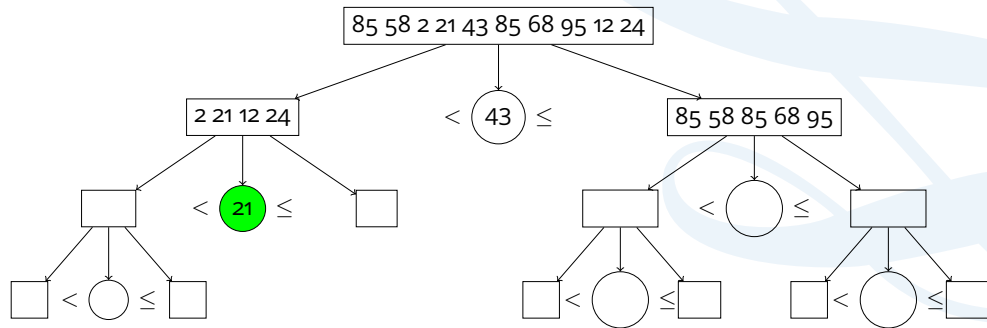
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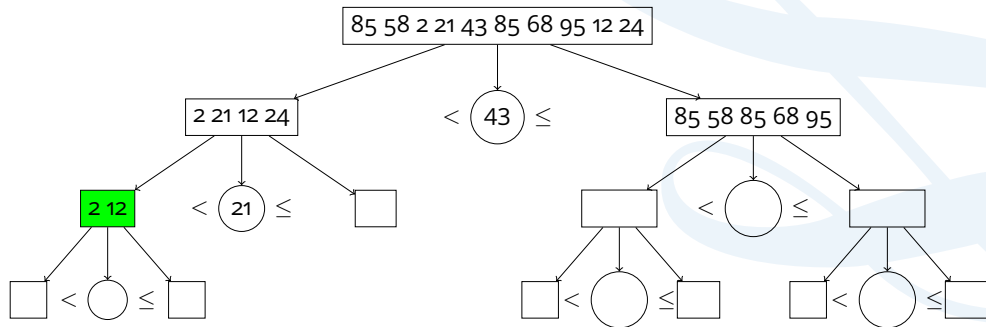
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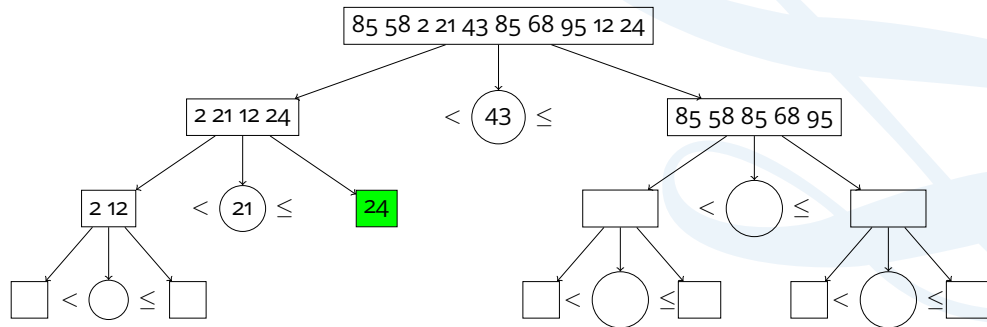
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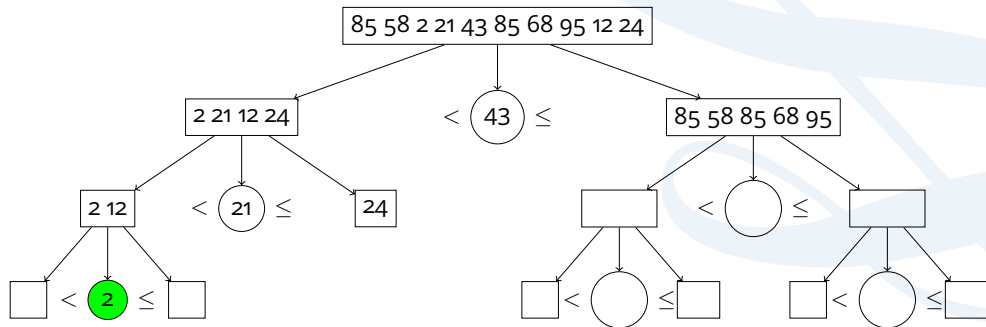
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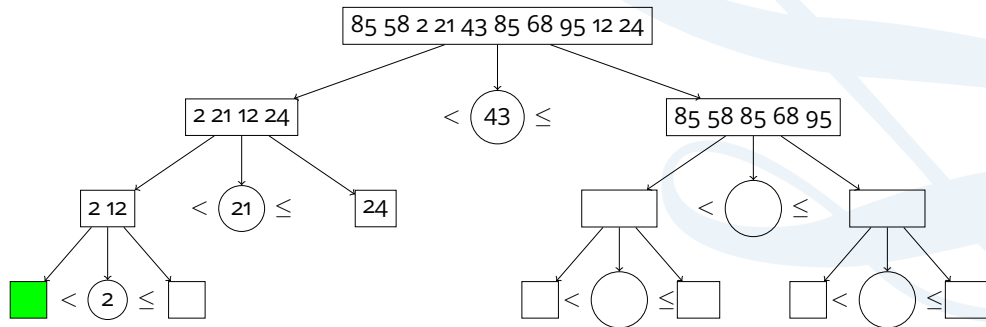
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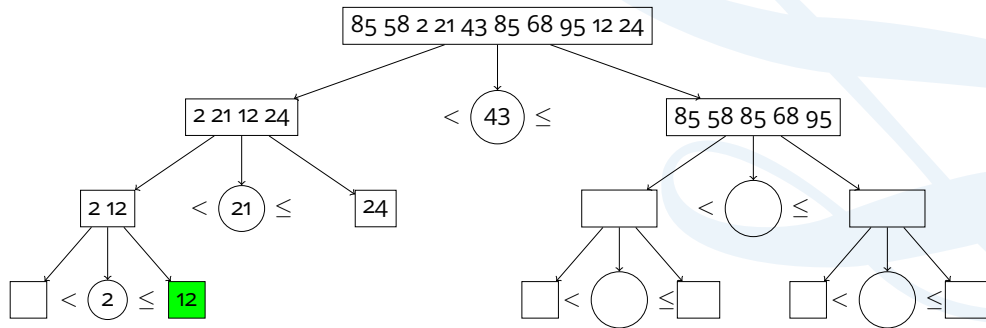
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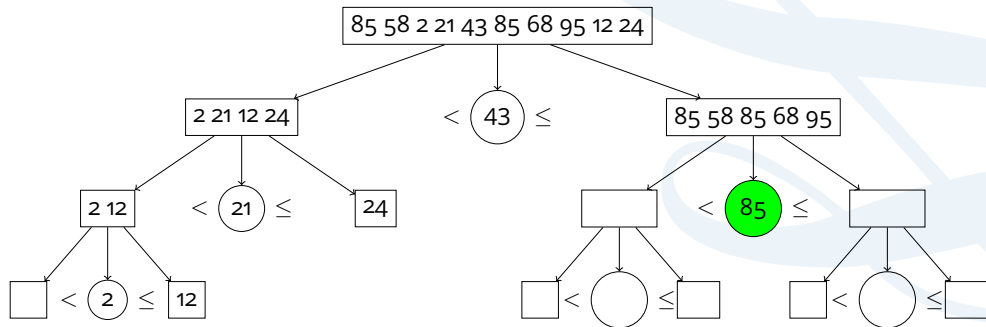
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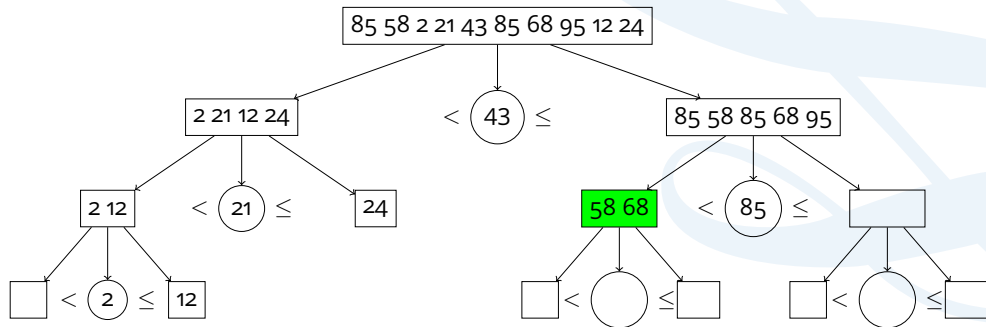
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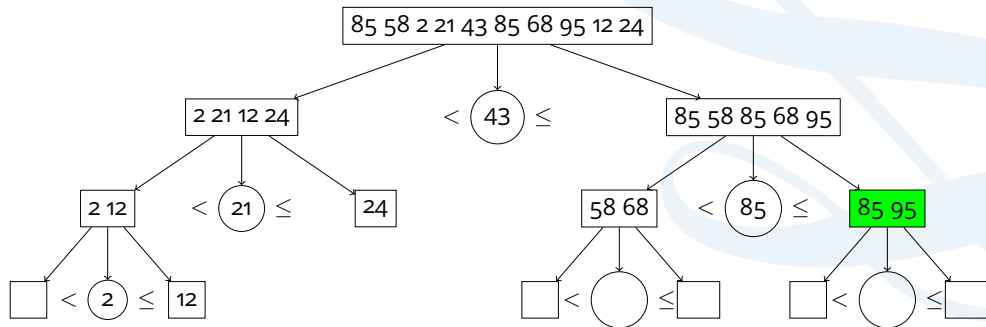
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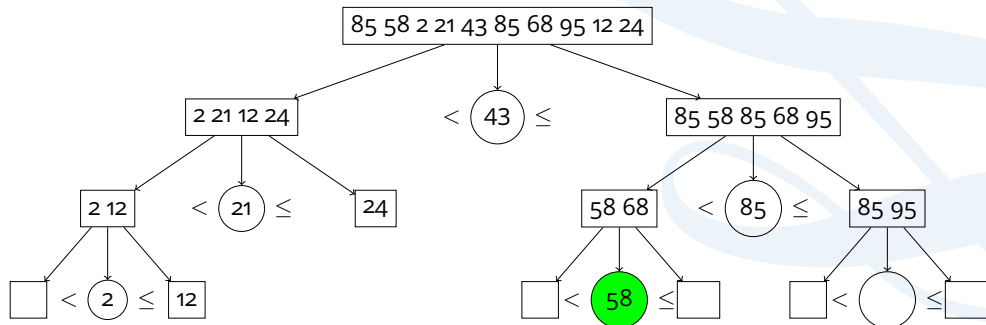
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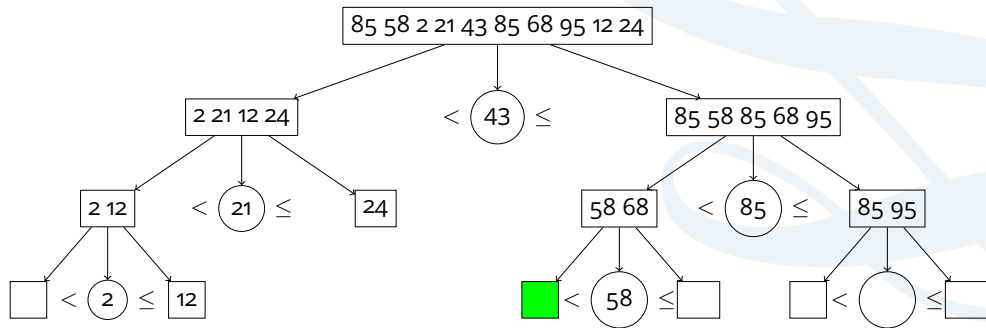
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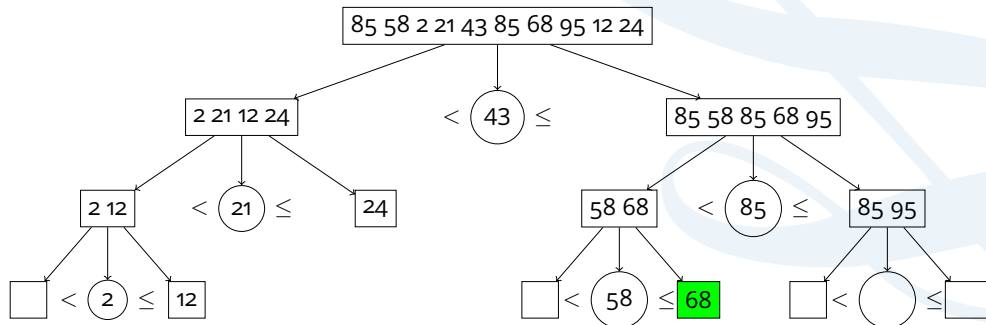
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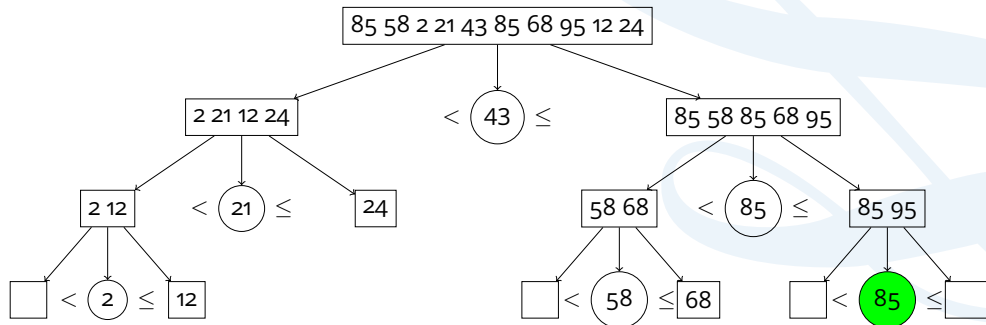
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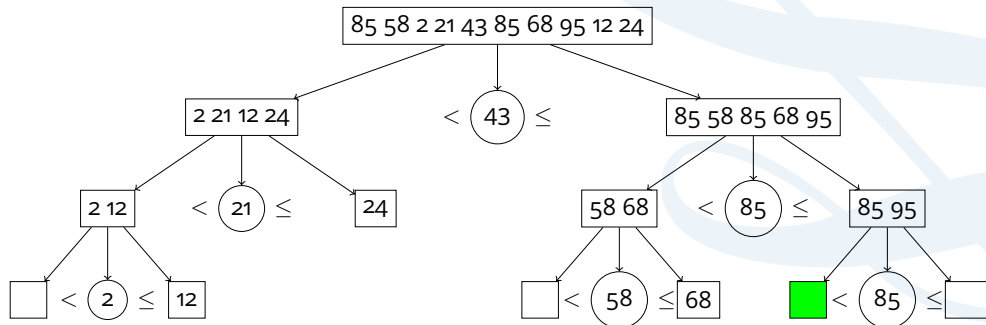
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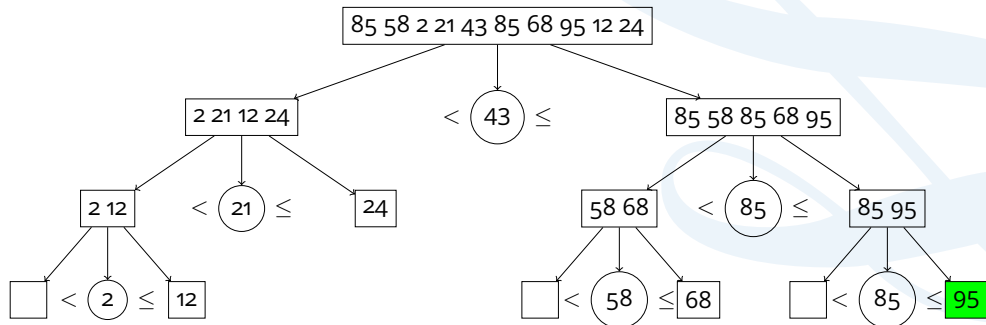
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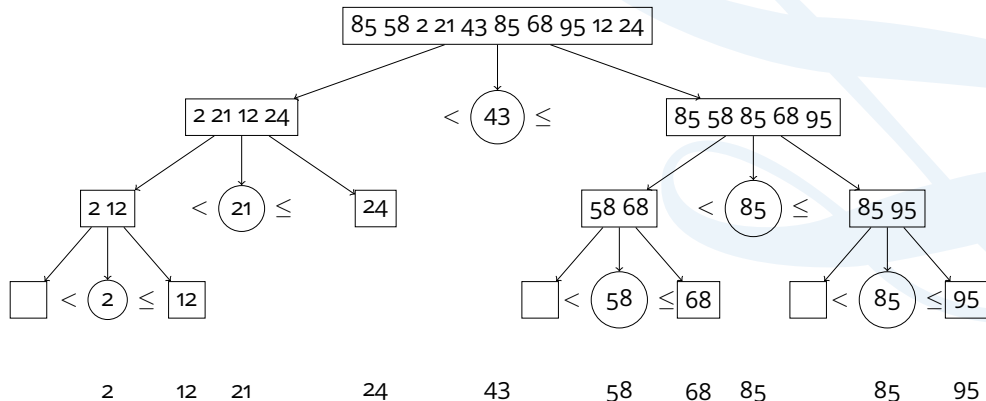
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Quicksort is...

- ...sometimes in-place.
 - Depends on implementation.
- ...sometimes stable.
 - Depends on implementation.

Some issues with the original algorithms (1959).

- Choosing the pivot.
 - First element.
 - Middle element.
 - Average of first, middle and last.
- Repeated elements.
 - Fat partition.

Quicksort is a divide and conquer algorithm.

- Too hard to sort the whole sequence?
- Divide the problem.
 - Still too hard?
 - Divide the problem.
 - Still too hard?
 - Divide the problem.
 - Etc, etc, etc.

Naturally suited for parallelism.



Have seen there are many ways to sort.

- Best sorting algorithm depends on multiple factors.
- Good in one situation is bad in another.



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 - Sequential memory (arrays)?

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 - Selection sort.

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Bubblesort

Stable sort

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Other
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Quicksort

Divide & Conquer

Comparing

Recap

Quiz

- Many sorting algorithms.
- Bubblesort.
- Selection sort.
- Quicksort
- Advantages/disadvantages.
 - In place.
 - In order.
 - Divide and Conquer.
- Performance
 - $O()$
 - Sequence type.
 - Read/writes.
 - Size of n .

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The End