David Croft

Allays

Linked lists

LL example

structures

types

Queue:

Stacks

Stacks

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Othe

Tree

Quiz

Recap

122com Data structures and types

David Croft

Coventry University david.croft@coventry.ac.uk

2017



Overview

- 1 Arrays
- 2 Linked lists
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 - LL example
- 3 Data structures
- 4 Abstract data types
- 5 Queues
- 6 Stacks
- 7 Sets
- 8 Other
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- 10 Quiz
- 11 Recap

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Quiz

Recap

A series of objects all of the same size and type.

- Stored in contiguous blocks of memory.
- Python lists are functionally closest.
 - But are not arrays.
- Can't be resized.



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Linked lists

The challenger for array's crown.

- Series of nodes, each of which points to the next element.
 - And to the previous element if it's a doubly linked list.

Doubly linked
$$\leftarrow A \leftarrow B \leftarrow C \rightarrow D$$

$$\leftarrow \mid \mathsf{A} \mid$$

$$| \rightarrow |$$
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Linked lists

Array example

Data structure

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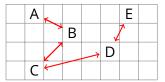
Quiz

Recap



Not in contiguous memory.

- Each node is separate.
- Scattered.
- C++ Dynamic memory (pointers!).
 - Discussed in depth later in module.



- Why would we use linked lists instead of arrays?
 - Can change size.
 - Can quickly insert and delete elements.

```
class Node:
    __prev = None
    __next = None
    value = None
```

Linked lists II

```
class Node
{
private:
    Node *prev;
    Node *next;

public:
    int value;
};
```



Arrays Linked lists

Array example

Data

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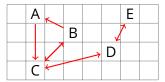
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Linked lists

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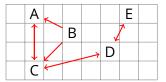
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```



Abstract da types

Queues

Stack

Sets

Othe

Tree

.

Recap

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```
temp = ['A', 'B', 'C', 'D', 'E']
array<char,5> temp {'A', 'B', 'C', 'D', 'E'};
```



- Array in memory, multiple elements in a contiguous block.
- How do we remove elements from the middle?

Abstract da types

Queue

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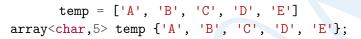
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Recap

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- Array in memory, multiple elements in a contiguous block.
- How do we remove elements from the middle?
 - Remove element from the array.

Abstract dat types

Queue

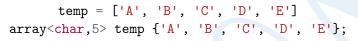
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Sets

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Tree

Recap





- Array in memory, multiple elements in a contiguous block.
- How do we remove elements from the middle?
 - Remove element from the array.
 - Move next element to occupy the empty space.



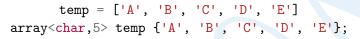
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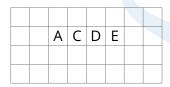




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 - Repeat.

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- Array in memory, multiple elements in a contiguous block.
- How do we remove elements from the middle?
 - Remove element from the array.
 - Move next element to occupy the empty space.
 - Repeat.
- Is very slow with large arrays.

Abstract dat

types

Queue:

Stack

Sets

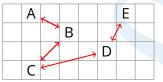
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Recap





- Linked list, separate elements scattered in memory.
- Each pointing to the next/prev element.
- How do we remove elements?

Abstract dat

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Queue

Stack

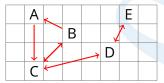
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Recap





- Linked list, separate elements scattered in memory.
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- How do we remove elements?
 - Change pointers.

Queue

Stack

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Sets

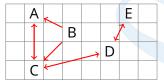
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Tree

Quiz

Recap





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- How do we remove elements?
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- Linked list, separate elements scattered in memory.
- Each pointing to the next/prev element.
- How do we remove elements?
 - Change pointers.
 - Delete old element.

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Linked lis

Data structure

Abstract dat

Queues

Stack

Sets

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Tree

1100

Recar

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Advantages

- Inserting and deleting elements is very fast.
 - O(1).
- No size limits, can keep adding new elements.
- Doesn't waste memory.

Disadvantages

- Not indexed.
 - Can't ask for the 20th element etc.
 - Have to step through the list (slow).
- Needs more memory than an array to store the same number of elements.
 - Have to keep track of where the next/prev nodes are.

Array example

Data structures

Abstract types

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Stack

Sets

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Tree

Quiz

Recap

Arrays and linked lists are data structures.

- A specific way of storing data.
- Can see how the various elements of the structure are laid out in memory.
- Direct access to the underlying memory.



Array example

Abstract data

Abstract dat types

Queues

Stack

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Quiz

Recan

As we move to storing more complex information in our software we well start to encounter Abstract Data Types (ADTs).

Software engineering principal.



Abstract data types

structures
Abstract data

types

Queue:

Stack

Sets

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Tree

Recap

- Software engineering principal.
- Keep what a data type can do...



Array example

Abstract data

types

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Tree

Recap

- Software engineering principal.
- Keep what a data type can do... ...and how it does it separate.



Linked list
Array example
LL example

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Recar

- Software engineering principal.
- Keep what a data type can do... ...and how it does it separate.
- Unlike data structure ADTs only concerned with the interface.



Linked list
Array example
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Abstract data

types

Queues

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Recan

- Software engineering principal.
- Keep what a data type can do... ...and how it does it separate.
- Unlike data structure ADTs only concerned with the interface.
- Internals of ADTs can vary widely between implementations.



122com Data

Abstract data types

Queue

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Quiz

Recap

Imagine an ADT like a car.

It has a set of supported operations, go faster, go slower, turn left, turn right.





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Arrays

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Quiz

Recap

Imagine an ADT like a car.

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- Don't care how it achieves these.



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Arrays

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Recap

Imagine an ADT like a car.

- It has a set of supported operations, go faster, go slower, turn left, turn right.
- Don't care how it achieves these.
- Don't care if, internally, it's using a combustion engine or an electric motor.



Linked lists Array example LL example

Abstract data

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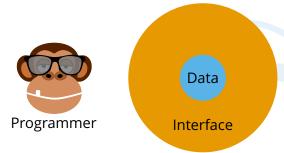
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Recap

LL example Data structures

Imagine an ADT like a car.

- It has a set of supported operations, go faster, go slower, turn left, turn right.
- Don't care how it achieves these.
- Don't care if, internally, it's using a combustion engine or an electric motor.
- Only care about the result.
- Keep people away from the internal workings/data.





Queues

Arrays

Linked lists
Array example
LL example

Abstract data

types

Queues

Stack

Sets

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Tree

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Recap

A First In First Out (FIFO) ADT.

- Ends of the queue called the front and back.
- New elements added to back of queue only.
 - Pushing push(value)
- Old elements removed from front of queue only.
 - Popping pop()
- No cutting in.



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Arrays

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Quiz

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Queues

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Queues

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 - Linked list.

 $front \Rightarrow$

types

Queues

Stack

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Recap



Array as a queue.

- Very similar to stacks.
 - Keep track of next free space.
 - Limited size.

Queues

Queue.

Stack

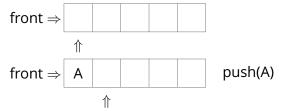
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Quiz

Recap







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Queues

Stack

sets

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Quiz

Recap

Array as a queue.

- front ⇒ ↑
- front \Rightarrow A

push(A)

 \uparrow

front \Rightarrow A B

push(B)



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Abstract data

Queues

Stacks

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Recap

Array as a queue.

I

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 \uparrow

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push(B)

 \uparrow

front \Rightarrow A B C

push(C)



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Linked list

Data structures

Abstract data types

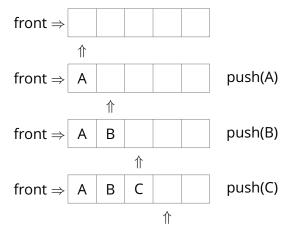
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- Very similar to stacks.
 - Keep track of next free space.
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- What happens when we pop()?
 - Have to shuffle every element forward one space.
 - Inefficient.



Linked list: Array example

Data structures

Abstract data types

Queues

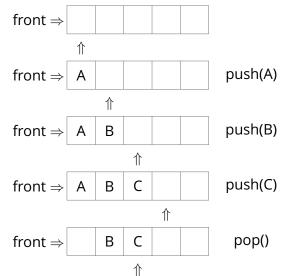
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Tree

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Array as a queue.

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Linked lists Array example

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Abstract data

Queues

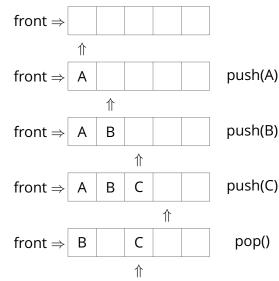
Stacks

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Abstract data

Queues

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Recap



Array as a queue.

- front \Rightarrow \uparrow
- front \Rightarrow A
 - \uparrow
- front \Rightarrow A B push(B)
- front \Rightarrow A B C push(C)
- front \Rightarrow B C \uparrow
- pop()

push(A)

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Data

Abstract dat

Queues

Stack:

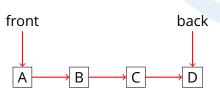
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Tree

Quiz

Recap

Linked list as a queue.





Linked list

LL example

structures

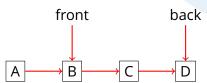
pop()

Abstract data types

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Linked list

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pop()

Abstract data types

Queues

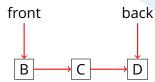
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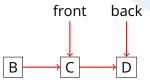
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Recap

pop(), pop()





Abstract data types

Queues

Stacks

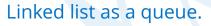
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Recap





pop(), pop()





Stack:

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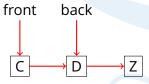
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Quiz

Recap



pop(), pop(), push(Z)





Queues

Stack

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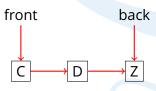
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Recap





pop(), pop(), push(Z)





Stacks

Quiz

Recap

A First In Last Out (FILO) ADT.

- Ends of the stack are called the top and bottom.
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Array

Linked list Array example LL example

Structures
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Recap

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- Which would be better for a stack? An array or a linked list?



Stacks

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- Which would be better for a stack? An array or a linked list?
 - Doesn't matter performance wise.
 - Linked list if *n* is unknown.



Abstract dat

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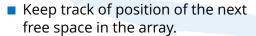
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Qui:







- Arrays have a fixed size.
 - Can't hold more values than we have space for.



structures

Abstract data types

Queues

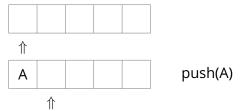
Stacks

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Tree







- Keep track of position of the next free space in the array.
- Arrays have a fixed size.
 - Can't hold more values than we have space for.



Data structure:

Abstract data

Queues

Queue.

Stacks

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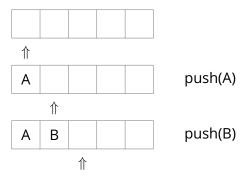
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Recan

Array as a stack.





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Arrays

Array example

Abstract dat

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Queues

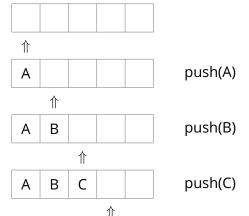
Stacks

Sets

Othe

Tree

Quiz



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Stacks



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push(A)





push(B)





push(C)



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		⇑	

pop()



Abstract da

Queue

Stack

Sets

Othe

Tree

Pocar



- An unordered ADT.
 - Items ordered by the set.
 - You have no control over it.
- Sets contain unique elements.
 - Can't contain duplicates.
- Can add items to a set.
- Can remove items from a set.
- Can see if an item is in a set.
- Can't get the *n*th element.
 - It's unordered remember.









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add(A)

Array example

structure:

Abstract data types

Queue:

Stack

Sets

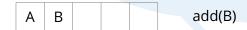
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Tree

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- \blacksquare Can't get the n^{th} element.
 - It's unordered remember.







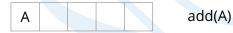


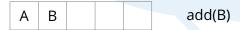
Sets

Sets

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Sets

Sets

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- Can add items to a set.
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- Can't get the *n*th element.
 - It's unordered remember.















remove(A)

add(A)



...and the others

Arrays

Array example

Data structures

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Sets

Other

Tree:

Quiz

Recap

Lots of other ADTs.

- Different names in different languages.
- Lists.
- Circular lists.
- Associative arrays.
 - Dictionaries/Maps.
- Double-ended queues.
- Trees.
- Graphs.



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Arrays

Linked lists

Data

Abstract data types

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Trees







Trees

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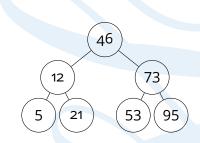
Trees

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Recap

Variation on linked lists.

- Made of nodes and relationships.
- Root node at top.
- Each node can have > o children.
- Binary search tree.
 - Very common type.
 - Ordered.
 - Max two children.
 - Binary searching.
 - Very good for sets.





Balance

Queues

Stack

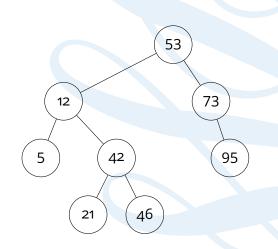
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Trees

....

- Trees can be balanced or unbalanced.
- Not required for all trees.
- Going to be talking about BSTs from here on.
- Unbalanced because more than a one node difference between the two halves.





Balance

Data structures

Abstract data types

Queue:

Stacks

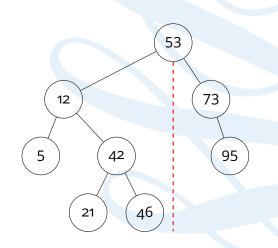
Sets

Othe

Trees

....

- Trees can be balanced or unbalanced.
- Not required for all trees.
- Going to be talking about BSTs from here on.
- Unbalanced because more than a one node difference between the two halves.
 - For the whole tree...





Balance

Data structures

Abstract data types

Queue:

Stack

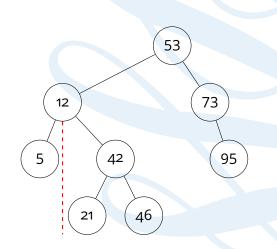
C - 4 -

Otho

Trees

1100

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- Not required for all trees.
- Going to be talking about BSTs from here on.
- Unbalanced because more than a one node difference between the two halves.
 - For the whole tree...
 - ...and one of the subtrees.



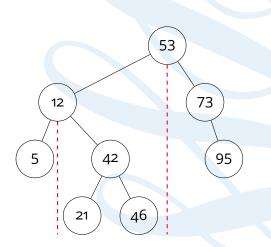


Coventr

Balance



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 - For the whole tree...
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David Croft

Arrays

Linked lists
Array example

Data structures

Abstract dat types

Queues

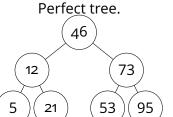
Jeuc.

Trees

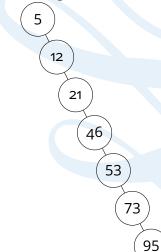
Recap

Coventry University

Important that you keep your BSTs balanced.



Degenerate tree.



122com Data structs & types

David Croft

Arrays

Linked lists

Data

Abstract d

Queuc

Stack:

Sets

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Quiz

David Croft

Arrays

Array example

structures

Abstract data types

Queues

Stacks

Stack:

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Troo

Quiz

Recap

Stacks and queues are examples of _____

- Data structures.
- Linked lists.
- Arrays.
- Abstract Data Types.



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Arrays

Array example

Data structure

Abstract data types

Stacks

Sets

Othe

Tree

Quiz

Recap

Stacks and queues are examples of _____

- Data structures.
- Linked lists.
- Arrays.
- Abstract Data Types.



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Linked list

Array example LL example

structures

Abstract dat types

Oueues

Stacks

Sets

Othe

Tree

Quiz

Recap

Coventry University

One advantage of linked lists over arrays is that _____

- They use less memory.
- They don't waste memory.
- They can be used for queues.
- They are faster to search though.

Array example

Data structure

Abstract dat

Queues

_ _ _

Stacks

Sets

Othe

Tree

Quiz

Recap

One advantage of linked lists over arrays is that _____

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- They don't waste memory.
- They can be used for queues.
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Arrays

Array example

Data structure

Abstract data

types

Queue

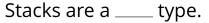
Stack

Soto

Other

Tree

Quiz



- FIFO.
- FOFI.
- FILO.
- FIDO.



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Allays

Array example

LL example

Structures
Abstract dat

Abstract data types

Queues

Charles

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....

Recap

Stacks are a ____ type.

- FIFO.
- FOFI.
- FILO.
- FIDO.



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Arrays

Array example

Data structure

Abstract dat

0.....

Queue

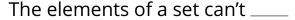
Stack

Sets

Othe

Tree

Quiz



- Contain duplicates.
- Be sequences, ie. lists, strings.
- Be out of order.
- Be removed.



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Arrays

Array example

Data structur

Abstract data types

Ougues

Queue.

Stack:

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Quiz

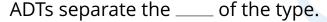
Recap

The elements of a set can't ____

- Contain duplicates.
- Be sequences, ie. lists, strings.
- Be out of order.
- Be removed.



Quiz



- Input and output.
- Attributes and methods.
- Implementation and interface.
- Code and software.



Quiz

ADTs separate the ____ of the type.

- Input and output.
- Attributes and methods.
- Implementation and interface.
- Code and software.



types

Queues

Stack

Jeaci

Otho

....

rree

Quiz

Recap



Everyone

- Need to understand the structures before we can pick the right one.
- Different data structures have very different characteristics.
- Huge effect on efficiency of your code.
- If you pick the right ADT it can save you a lot of code.
 - E.g. why write code to check for duplicates? Use a set and they can't exist.
 - **E**.g. why write code to find the most recent addition to a list, use a stack.



Arrays

Linked list Array example LL example

Abstract dat

Abstract dat types

Queue

Stack

Sets

_

Tree

- Arrays.
 - Advantages/disadvantages.
- Linked lists .
 - Advantages/disadvantages.
 - How to insert/delete.
- Difference between data structure and ADTs.
- Stack.
 - FILO.
 - Using an array as one.
 - Using a LL as one.

- Queue.
 - FIFO.
 - Using an array as one.
 - Using a LL as one.
- Sets.
 - No duplicates.
 - Unordered.
- Trees.
 - Balanced/unbalanced.



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Arrays

Linked lists

Data

Abstract data types

Queue:

Stacks

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Othe

O...:-

Recap



The End