

## Sorting

*David Croft*

Introduction

Bubblesort

Stable sort

In-place

Selection sort

Other  
algorithms

Quicksort

Divide & Conquer

Comparing

Recap

# Sorting algorithms

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- 1 Introduction
- 2 Bubblesort
  - Stable sort
  - In-place
- 3 Selection sort
- 4 Other algorithms
- 5 Quicksort
  - Divide & Conquer
- 6 Comparing
- 7 Recap

Sorting is one of the classic problems for learning algorithms.

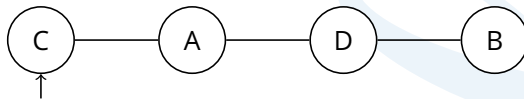
- Requirement for everything.
- Obvious applications like sorting text, statistics (median calculations).
- Less obvious, sorting objects in games for FOV (Field Of View) calculations.
- Route planning.

Very simple sort.

- Compares each item to the next in the sequence.
  - Swap items if in wrong order.

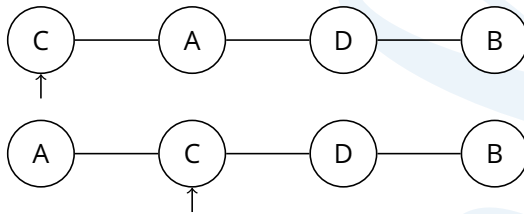
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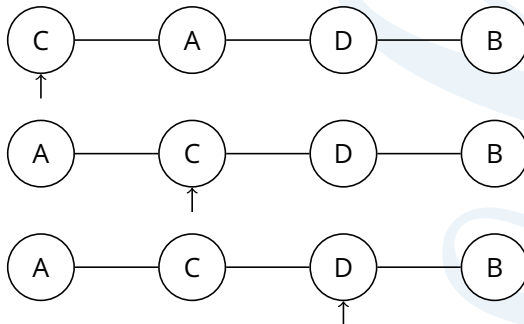
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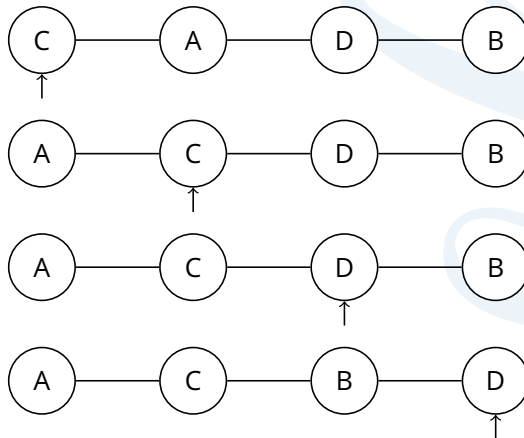
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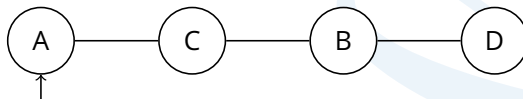
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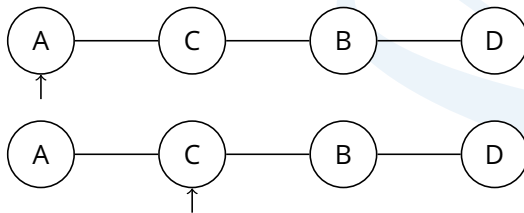
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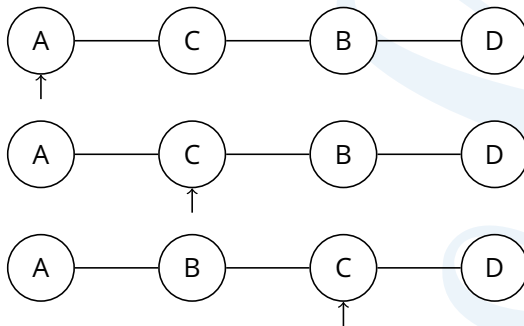
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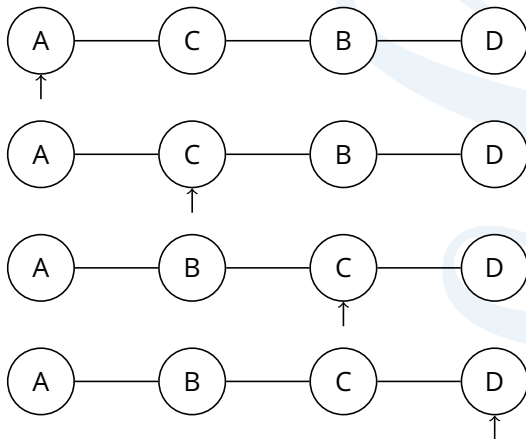
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With unstable sorting algorithm the relative orders of equivalent elements can be changed.

In-place meaning that it only needs a small amount of additional memory in order to work.

- More memory efficient than the alternative.
- Can be important if...
  - ...dealing with large amounts of data.
  - ...have limited resources (i.e. embedded systems).
- Bubble sort only needs a few extra variables to swap the elements and to step through the sequence.

One of the simplest sorting algorithms.

- Explained here to introduce you to sorting concepts.
  - In-place, stable.

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  - Horrible performance, average is  $O(n^2)$ .
  - But best case is only  $O(n)$ .



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- The starting order of the sequence.

For example, Bubblesorting a 100 elements:

So sorting algorithms have 3  $O()$  values.





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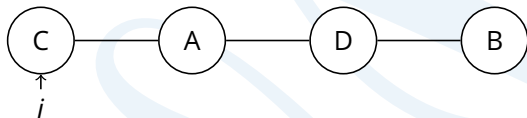
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  - Iterate over sequence once.
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  - 10,000 comparisons.
- Average case, random order.
  - Somewhere in between.

So sorting algorithms have 3  $O()$  values.

- Divides sequence into sorted and unsorted regions.
  - Not stable.
  - In place.
- 1 Iterate over sequence.
  - 2 For each element search the remaining elements on its right for the smallest value.
  - 3 Swap smallest element with current element.

## Selection sort II

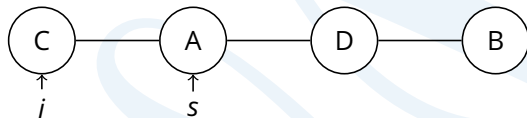
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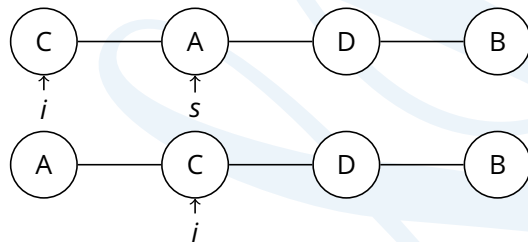


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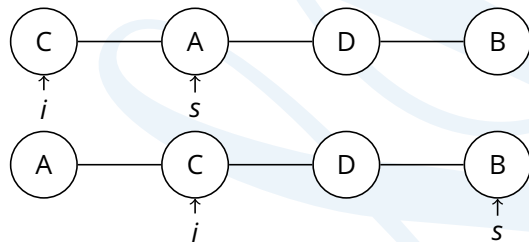
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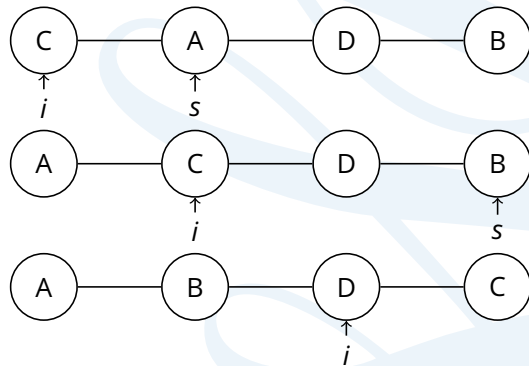




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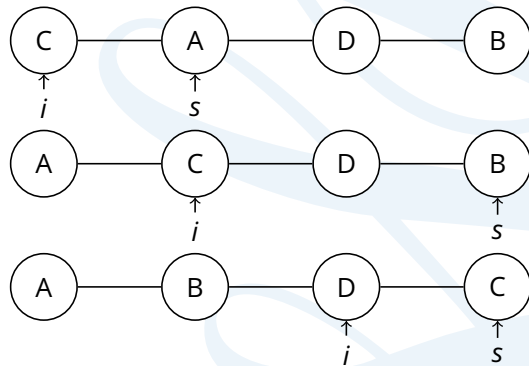
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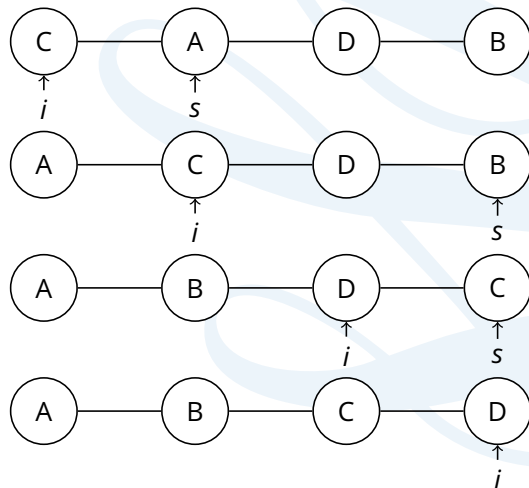
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Bubblesort is  $O(n^2)$  worst and average case .

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- Selection sort is generally faster than bubble.
  - But have same  $O()$  complexity.
  - What?

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- Selection sort is generally faster than bubble.
  - But have same  $O()$  complexity.
  - What?
- $O()$  notation describes how an algorithm will grow.
- Not good at absolute performances.
- Selection sort typically does fewer comparisons and swaps than bubblesort.
  - Therefore typically faster.
- Best case bubblesort is  $O(n)$ , selection is  $O(n^2)$ .
  - Occasionally faster.

# Sorting Algorithms

## Many sorting algorithms

- Different trade-offs, performances. <https://www.youtube.com/watch?v=ZZuD6iUe3Pc>
- Some are just jokes.

1 Bead

2 Bogo

3 Bubble

4 Circle

5 Cocktail

6 Comb

7 Counting

8 Cycle

9 Gnome

10 Heap

11 Insert

12 Merge

13 Pancake

14 Patience

15 Permutation

16 Quick

17 Radix

18 Selection

19 Shell

20 Sleep

21 Stooage

22 Strand

23 Tree

Neither bubble or selection sort are very good.

- Simple algorithms but slow.
- Not used in real life.

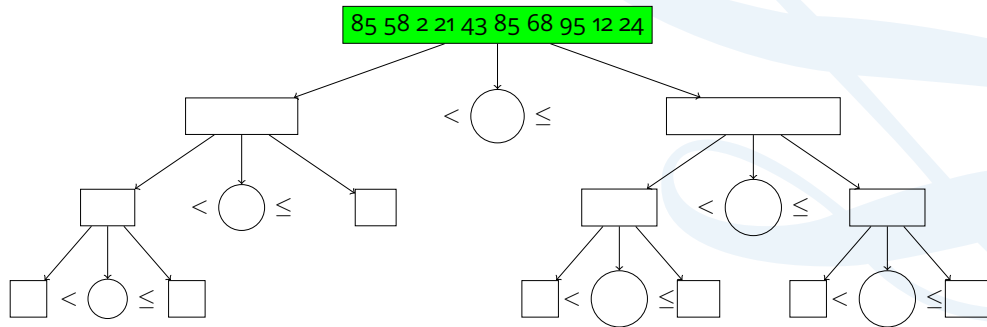
One of the fastest sorting algorithms.

- Used in real life.
- Recursively breaks the sequence in half.
  - Divide & Conquer.

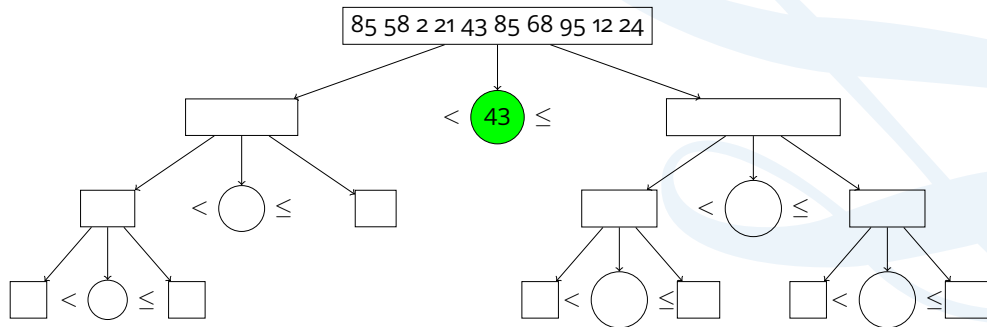
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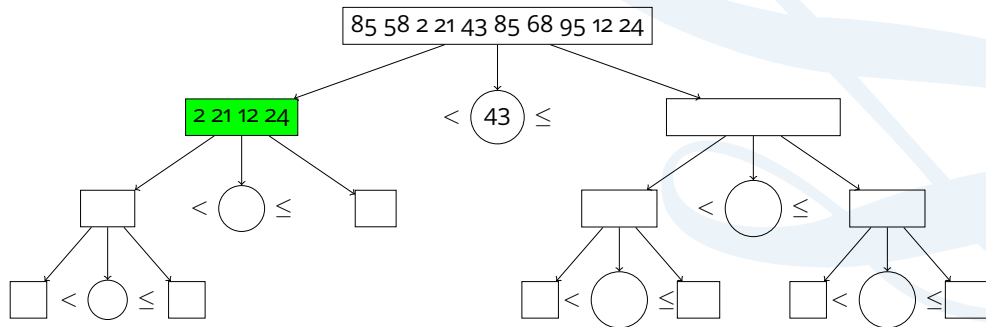
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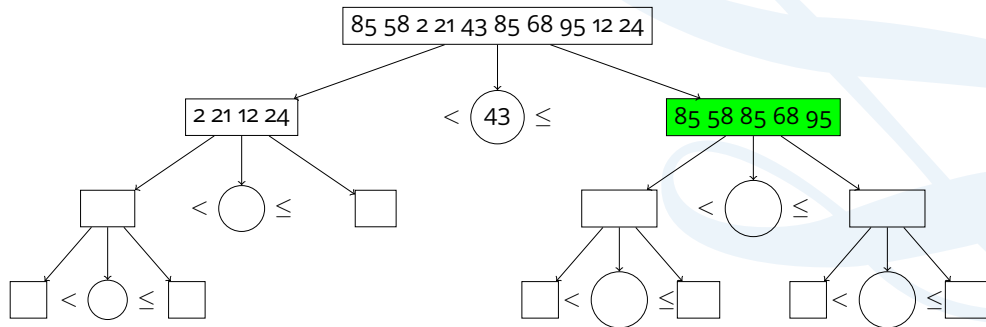
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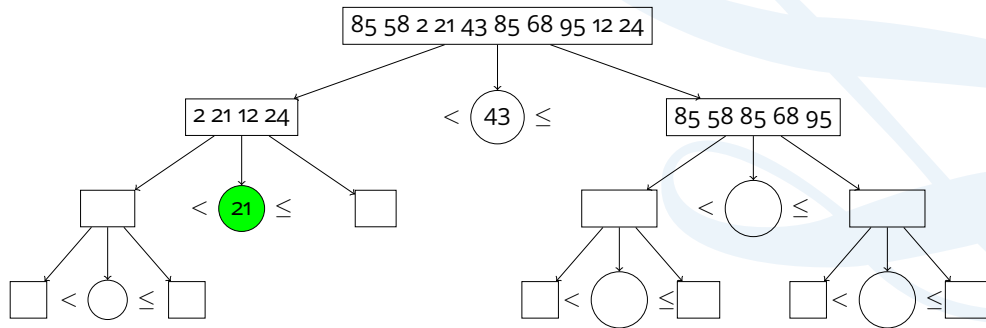
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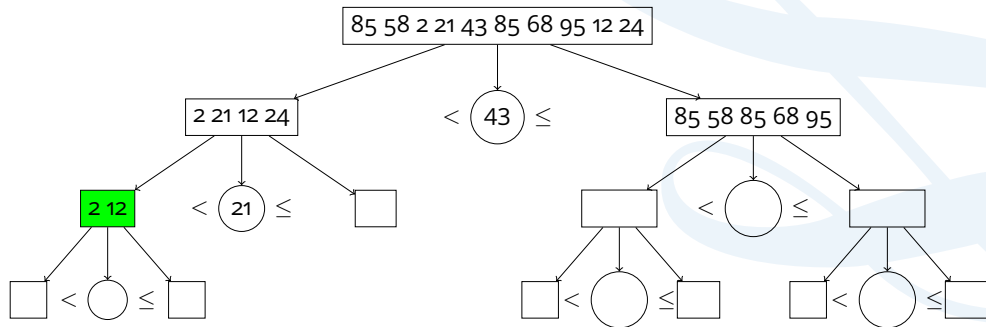
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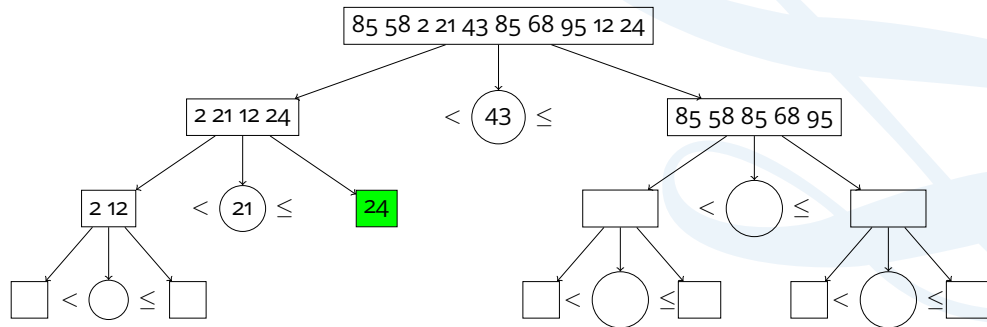
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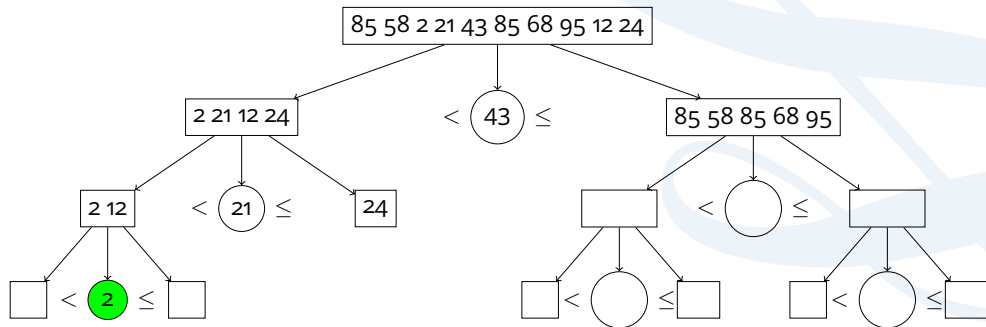
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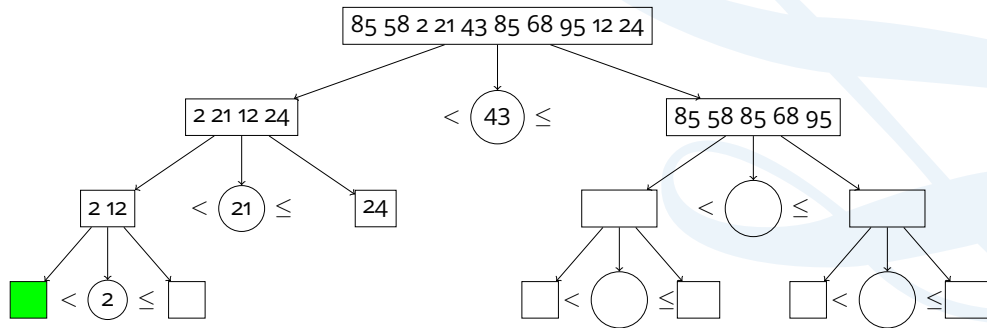


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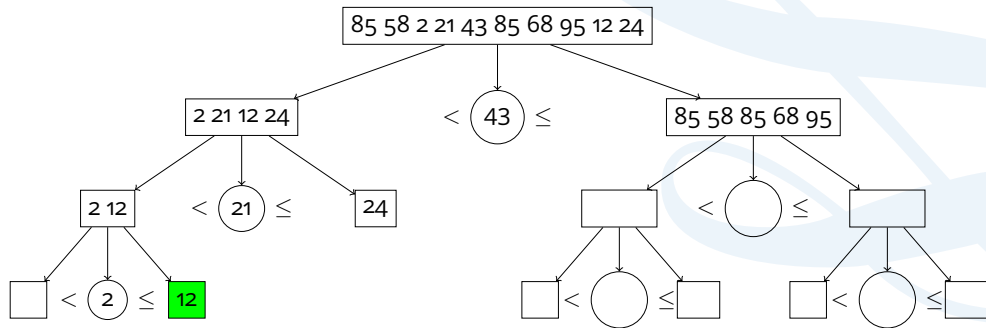




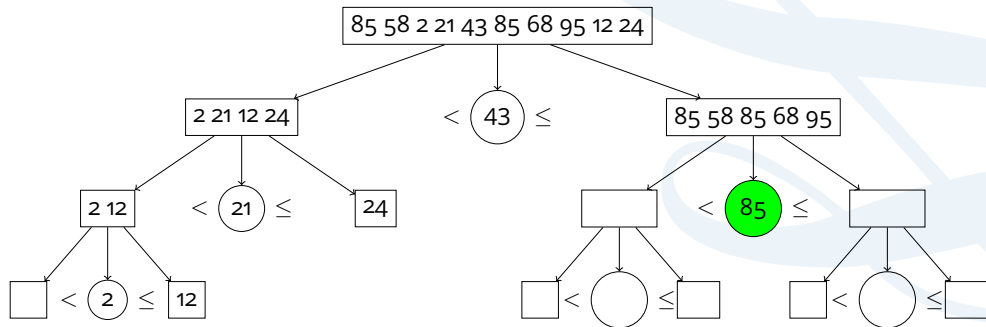
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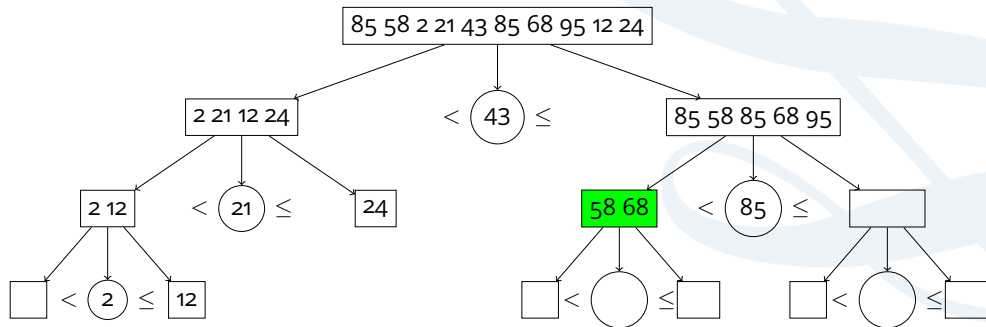
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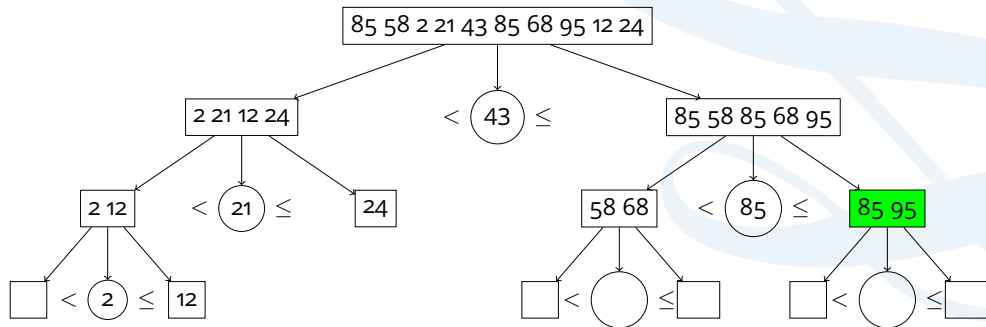
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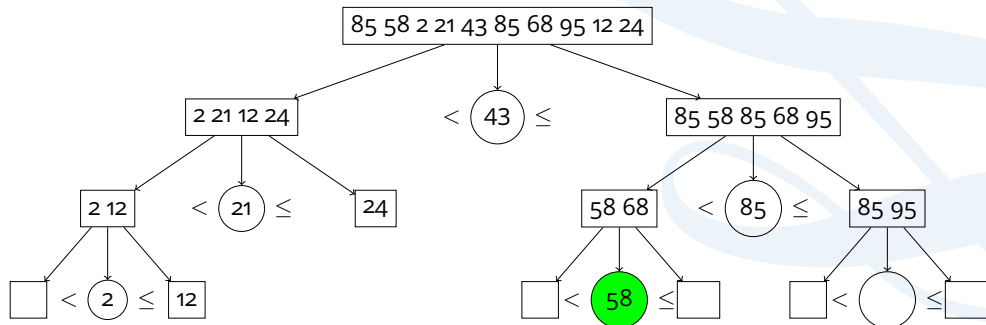
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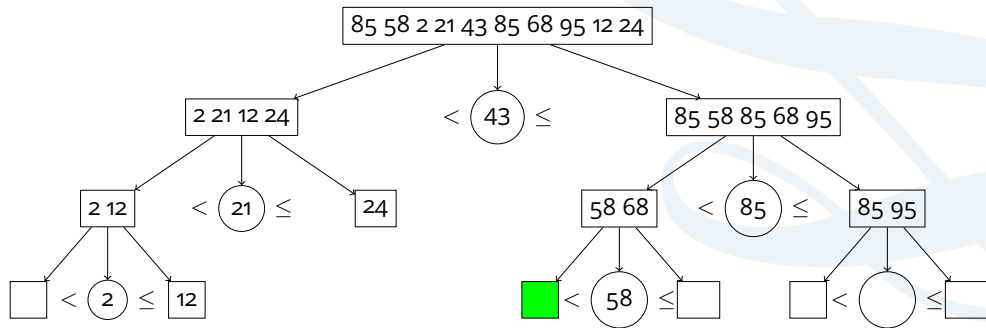
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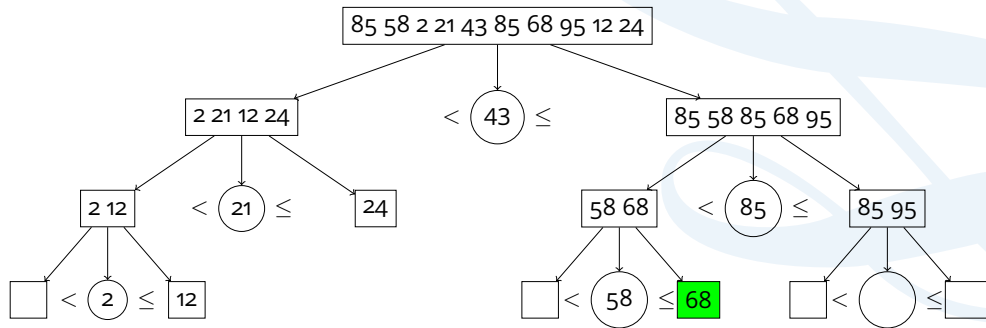
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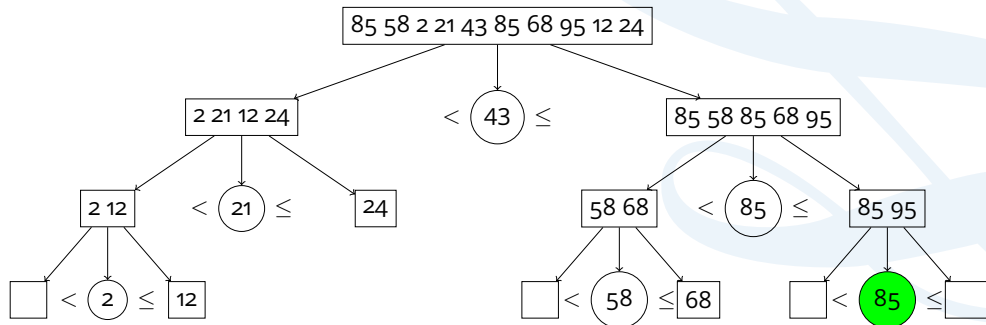


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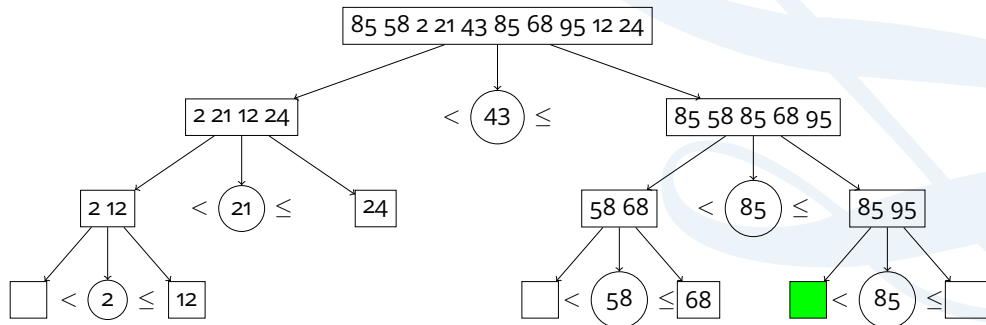




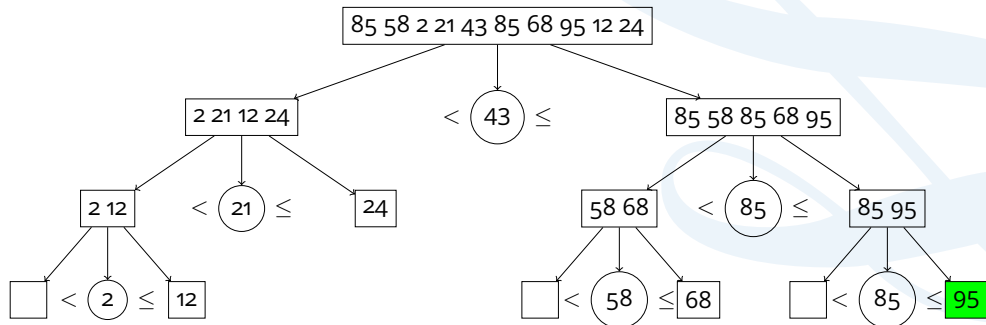
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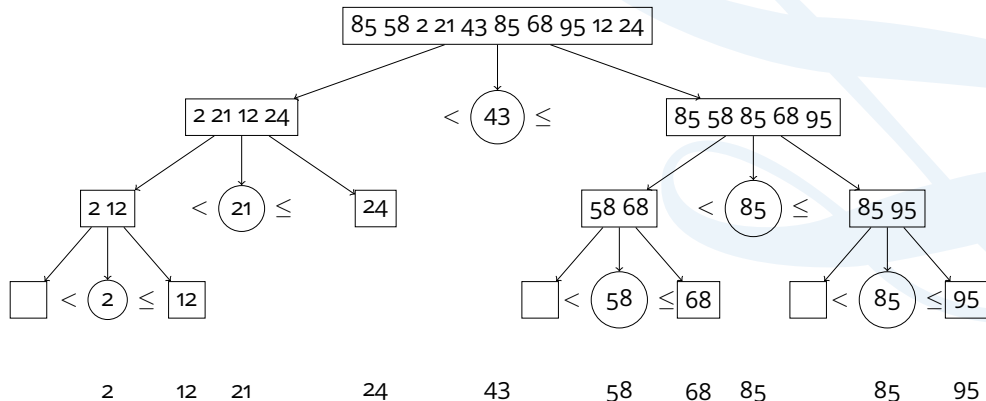
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## Quicksort is...

- ...sometimes in-place.
  - Depends on implementation.
- ...sometimes stable.
  - Depends on implementation.

## Some issues with the original algorithms (1959).

- Choosing the pivot.
  - First element.
  - Middle element.
  - Average of first, middle and last.
- Repeated elements.
  - Fat partition.

Quicksort is a divide and conquer algorithm.

- Too hard to sort the whole sequence?
- Divide the problem.
  - Still too hard?
  - Divide the problem.
    - Still too hard?
    - Divide the problem.
    - Etc, etc, etc.

Naturally suited for parallelism.

# Comparing algorithms



Have seen there are many ways to sort.

- Best sorting algorithm depends on multiple factors.
- Good in one situation is bad in another.



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  - Selection sort.

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# Quiz

- Many sorting algorithms.
- Bubblesort.
- Selection sort.
- Quicksort
- Advantages/disadvantages.
  - In place.
  - In order.
  - Divide and Conquer.
- Performance
  - $O()$
  - Sequence type.
  - Read/writes.
  - Size of  $n$ .

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