

```
setwd("~/Workspace/College/DIT/MATH9952/Data")

# read in the data
retention = read.csv("retention.csv", header = T)
```

```
# remove unnecessary columns
retention$X = NULL
retention$lc_points.1 = NULL
```

```
# convert columns to factors
retention$mathgrd = as.factor(retention$mathgrd)
retention$address = as.factor(retention$address)
```

```
# remove rows where NULLs or NAs are present
retention = retention[complete.cases(retention),]
```

```
# have a look at the data
head(retention)
```

```
attach(retention)
```

```
# list the column names
colnames(retention)
```

Question 1

```
# fit a model with all interactions
fit1 = glm(passed ~ .*, family = binomial(link = "logit"), data = retention)
summary(fit1)
```

```
# prune unnecessary predictors
step(fit1, scope = list(lower = ~ 1, upper = ~ .*), direction = "backward", trace = 1)
```

```
# fit the final model
fitf = glm(passed ~ gender + mathgrd + CAO_choice + lc_points + gender:CAO_choice, family = binomial(link = "logit"), data = retention)
summary(fitf)
```

Question 3

```
nd = data.frame(gender = 1, lc_points = 300, mathgrd = "50-60", CAO_choice = "3")
p = predict(fitf, newdata = nd, se = T)
```

```
prob = exp(p$fit) / (1 + exp(p$fit))
ciu = exp(p$fit + 1.96 * p$se.fit) / (1 + exp(p$fit + 1.96 * p$se.fit))
cil = exp(p$fit - 1.96 * p$se.fit) / (1 + exp(p$fit - 1.96 * p$se.fit))
```

```
data.frame(prob = prob, upperCI = ciu, lowerCI = cil)
#      prob  upperCI  lowerCI
# 1 0.6629496 0.8398823 0.4244774
```

Question 4

```
fitz = glm(passed ~ gender + lc_points, family = binomial(link = "logit"), data = retention)
summary(fitz)
```

```
# NR Method
```

```
x1 = gender
x2 = lc_points
y = passed
```

```
beta0 = 1
beta1 = 0
beta2 = 0
beta = matrix(c(beta0, beta1, beta2), nrow = 3)
```

```

# iterations start...

eta      = (beta[1, 1] + beta[2, 1] * x1 + beta[3, 1] * x2)

score1   = sum(y          - ((1 * exp(eta)) / (1 + exp(eta))))
score2   = sum((y * x1) - ((1 * x1 * exp(eta)) / (1 + exp(eta))))
score3   = sum((y * x2) - ((1 * x2 * exp(eta)) / (1 + exp(eta))))

h11      = sum( (1 * exp(eta)^2)          / (1 + exp(eta))^2 - ((1 * exp(eta)) / (1 + exp(eta))))
h12      = sum( (1 * x1 * exp(eta)^2)      / (1 + exp(eta))^2 - ((1 * x1 * exp(eta)) / (1 + exp(eta))))
h13      = sum( (1 * x2 * exp(eta)^2)      / (1 + exp(eta))^2 - ((1 * x2 * exp(eta)) / (1 + exp(eta))))
h22      = sum( (1 * x1^2 * exp(eta)^2)    / (1 + exp(eta))^2 - ((1 * x1^2 * exp(eta)) / (1 + exp(eta))))
h23      = sum( (1 * x1 * x2 * exp(eta)^2) / (1 + exp(eta))^2 - ((1 * x1 * x2 * exp(eta)) / (1 + exp(eta))))
h33      = sum( (1 * x2^2 * exp(eta)^2)    / (1 + exp(eta))^2 - ((1 * x2^2 * exp(eta)) / (1 + exp(eta))))

u        = matrix(c(score1, score2, score3), nrow = 3)
h        = matrix(c(h11, h12, h13, h12, h22, h23, h13, h23, h33), nrow = 3, byrow = T)

betanew  = beta - solve(h) %*% u
beta     = betanew

result   = data.frame(beta = beta, score = u, hessian = h)
result
# iterations end...

```

Appendix

```

# fit a model without interactions - simpler!

# fit1 = glm(passed ~ ., family = binomial(link = "logit"), data = retention)
# formula(fit1)
# summary(fit1)

# use the step function to help you find the predictors to drop...

# step(fit1, scope = list(lower = ~ 1, upper = ~ .), direction = "backward", trace = 1)

# or use the drop1 function to manually drop predictors...

# drop1(fit1, test = 'LRT')
# fit2 = update(fit1, ~. - CAO_choice)
# summary(fit2)
#
# drop1(fit2, test = 'LRT')
# fit3 = update(fit2, ~. - address)
# summary(fit3)
#
# drop1(fit3, test = 'LRT')

```