

# Statistical Inference Using Bootstrapping



# BOOTSTRAPPING

- Bootstrapping is a method for estimating the **sampling distribution** of an estimator by **resampling with replacement from the original sample**.
- The method is especially useful when sampling distribution of estimator is not standard distribution.
- The method can be used in any statistical inference problem.
- The use of the term 'bootstrap' comes from the phrase “To pull oneself up by one's bootstraps ” - generally interpreted as succeeding inspite of limited resources.

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- Many conventional statistical methods of analysis make assumptions about normality, including correlation, regression,  $t$  tests, and analysis of variance. When these assumptions are violated, such methods may fail.
- Bootstrapping method is used when assumptions of parametric tests are not satisfied and/or the parameter of interest does not have standard sampling distribution. (example- median or difference between 2 medians)

# BOOTSTRAPPING

- Bootstrapping, a data-based simulation method, is steadily becoming more popular as a statistical methodology. It is intended to simplify the calculation of statistical inferences, sometimes in situations where no analytical answer can be obtained.
- As computer processors become faster and more powerful, the time and effort required for bootstrapping decreases to levels where it becomes a viable alternative to standard parametric techniques.

# BOOTSTRAPPING

In following scenarios bootstrapping can be used:

- Small sample sizes with unknown population distribution
- When assumption of normality does not hold
- Skewed data
- A non-linear combination of variables (e.g. a ratio)
- A location statistic other than the mean(median,difference in median)

# BOOTSTRAPPING

Original Sample  
12,23,11,29,34, 38,41,45,6

Median=29.00

	Sample 1	Sample 2	Sample 3			Sample B
	23	11	6			41
	23	29	45			45
	29	11	11			11
	29	29	29			34
	34	34	11			34
	38	34	38			38
	41	41	41			41
	45	45	41			45
	41	11	6			6
Median	34.00	29.00	29.00			38.00

Here sampling distribution of sample median is Generated.  
Assuming B=1000,  
25<sup>th</sup> value and 975<sup>th</sup> value  
Will provide 95% confidence  
Interval for median.

**Sample size of original and each bootstrap sample is 9**



# BOOTSTRAPPING IN R

```
#Import csv data set "bootdata"
```

```
bootdata<-read.csv(file.choose(),header=T)
```

```
#Install and call package "boot"
```

```
install.packages("boot")
```

```
library(boot)
```

# BOOTSTRAPPING IN R

```
#Create function to find median. The function boot calls this function  
R=1000 times.
```

```
f<-function(data,i){  
  d<-data[i,]  
  med<-median(d)  
  return(med)  
}
```

```
#The function boot sends data and random number vector to function f  
1000 times.Each time random number vector is different.
```

```
bootobject <- boot(data=bootdata,statistic=f,R=1000)
```



# BOOTSTRAPPING IN R 95% CI

```
#calculate 95% confidence interval
```

```
boot.ci(bootobject,type="perc")
```

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Intervals :

Level	Percentile
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95%	( 0.90, 1.85 )
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Calculations and Intervals on Original Scale

**THANK YOU!!**