

SUPPORT VECTOR MACHINES-ML METHOD

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Introduction to Support Vector Machines

- Support Vector Machines (SVM's) are a relatively new learning method generally used for classification problem.
- Although the first paper dates way back to early 1960's it is only in 1992-1995 that this powerful method was universally adopted as a mainstream machine learning paradigm

The basic idea is to find a hyper plane which separates the d-dimensional data perfectly into its classes.

What is a Hyper Plane

In two dimensions, a hyper plane is defined by the equation:

$$W_1 X_1 + W_2 X_2 + b = 0$$

This is nothing but equation of line.

The above equation can be easily extended to the p-dimensional setting:

$$W_1 X_1 + W_2 X_2 + \dots + W_p X_p + b = 0$$

In short,

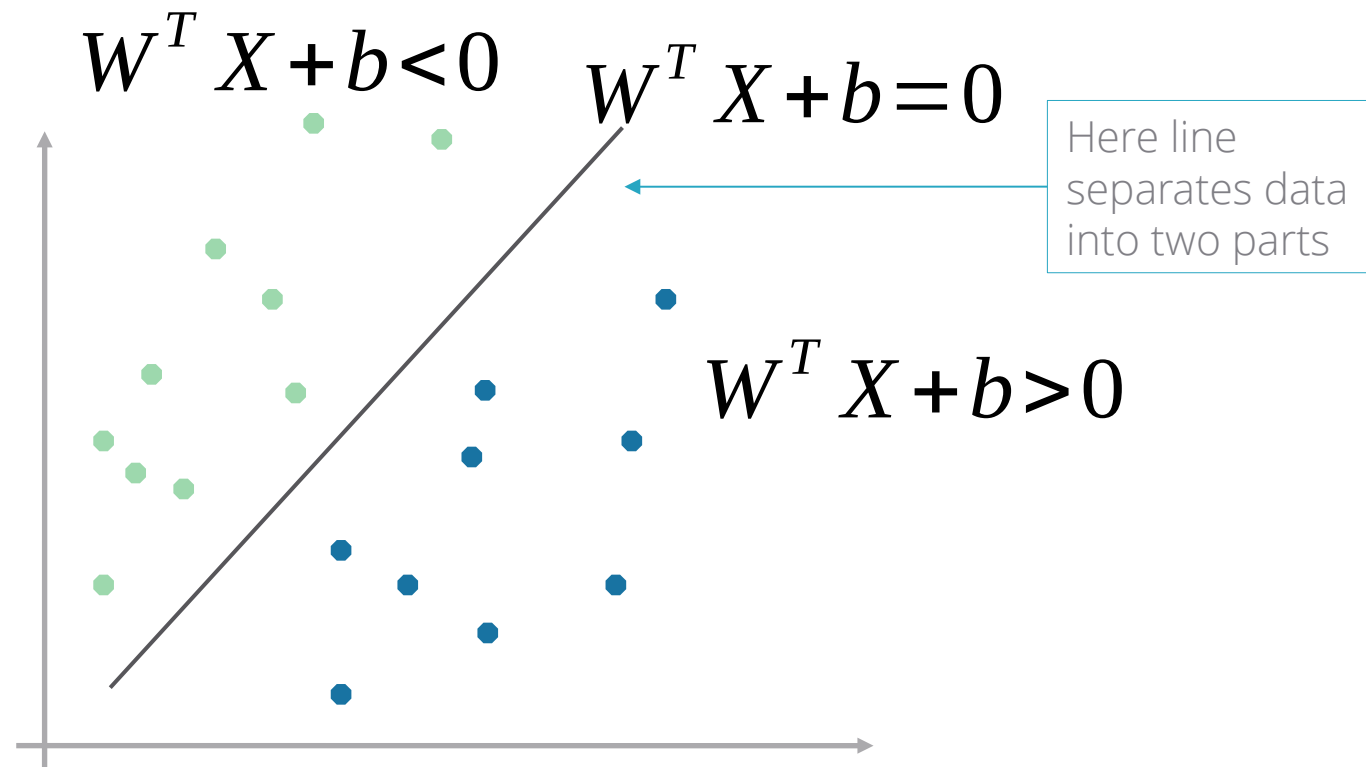
$$W^T X + b = 0$$

In $p > 3$ dimensions, it can be hard to visualize a hyper planes.

Separating a Hyper Plane

- Binary classification can be viewed as the task of separating classes in feature space:

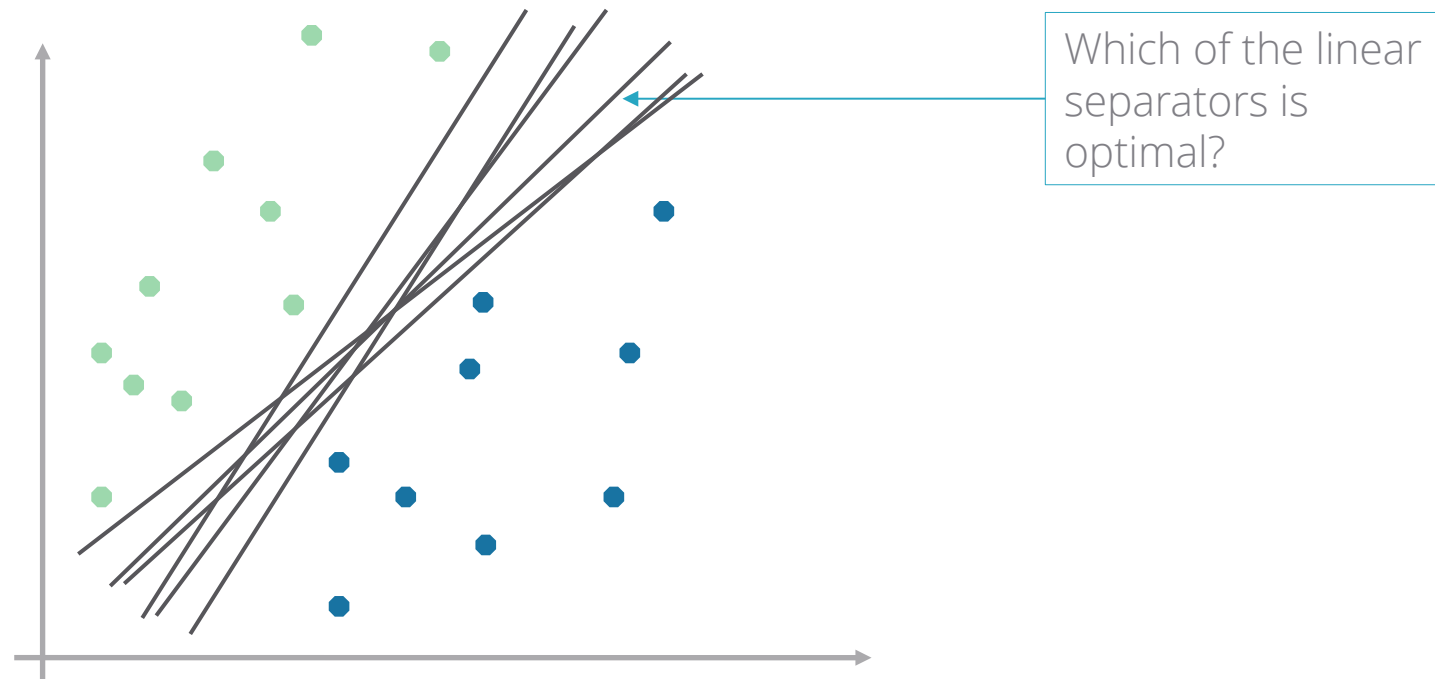
Fig. 01: Binary Classification



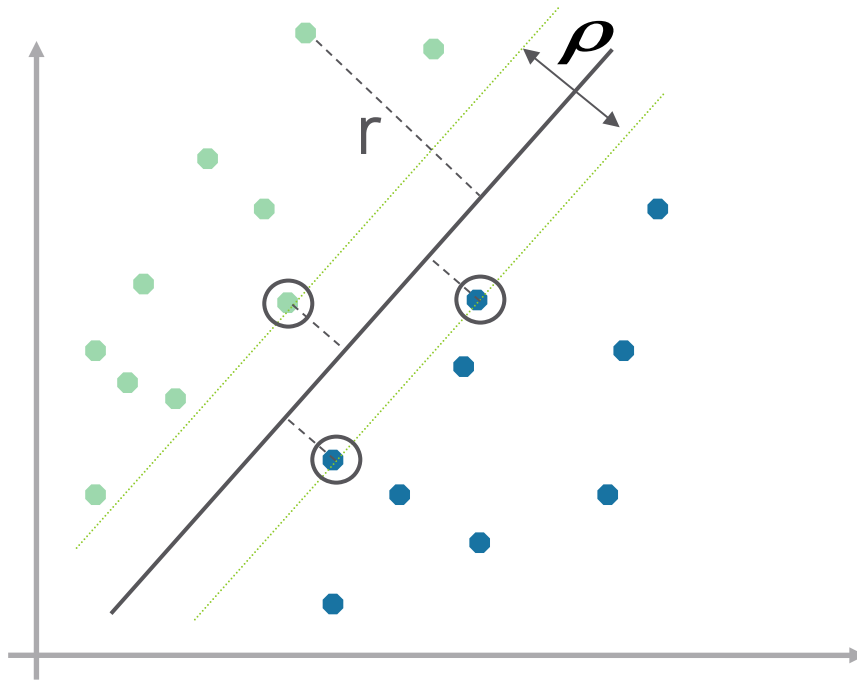
Linear Separators

The objective in SVM is to find optimum separator

Fig. 02: Linear Separators



Classification Margin



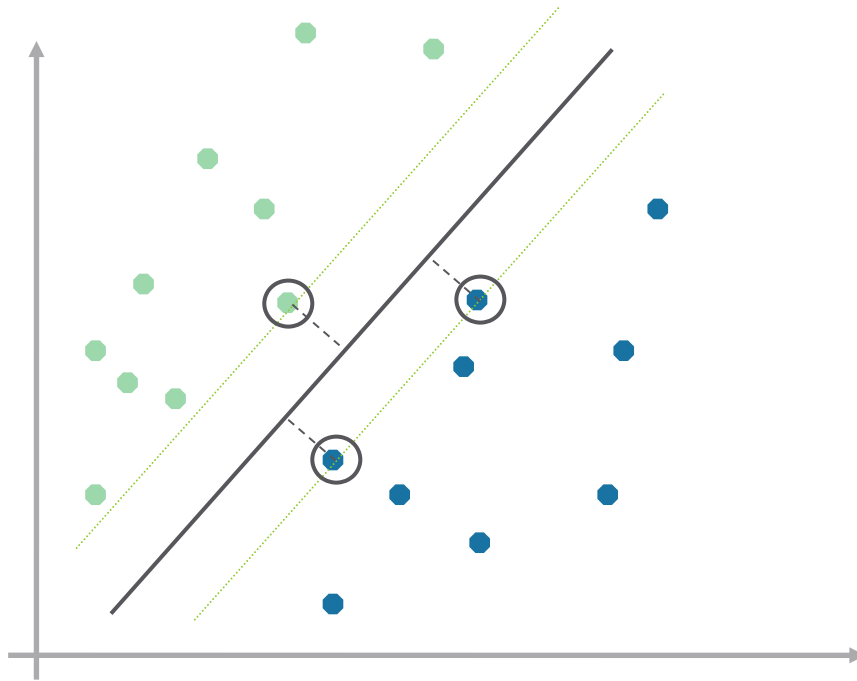
- Distance from case x_i to the separator is

$$r = \frac{w^T x_i + b}{\|w\|}$$

Here is length of a vector given by $\sqrt{\sum(W^2)}$

- Cases closest to the hyper plane are Support Vectors
- Margin ρ of the separator is the distance between support vectors

Maximum Margin Classification



- The objective is now to maximize the margin p of the separator
- The focus is on 'Support Vectors'
- Other cases are not considered in the algorithm

Mathematical Approach to Linear SVM

Let training set be separated by a hyper plane with margin ρ . Then for each training observation

$$\leftrightarrow y_i (w^T x_i + b) \geq \rho/2$$

For every support vector the above inequality is an equality

After rescaling w and b in the equality, we obtain that distance between each x_i and the hyper plane is

$$r = \frac{y_i (w^T x_i + b)}{\|w\|} = \frac{1}{\|w\|}$$

Margin can be expressed through ρ

$$\rho = 2r = \frac{2}{\|w\|}$$

Mathematical Approach to Linear SVM

Quadratic Optimisation problem is:

Find w and b such that
is maximised
and

which can be reformulated as:

Find w and b such that
is minimised
and

Case Study – Predicting Loan Defaulters

Background

- The bank possesses demographic and transactional data of its loan customers. If the bank has a robust model to predict defaulters it can undertake better resource allocation.

Objective

- To predict whether the customer applying for the loan will be a defaulter

Available Information

- Sample size is 700
- Age group, Years at current address, Years at current employer, Debt to Income Ratio, Credit Card Debts, Other Debts are the independent variables
- **Defaulter** (=1 if defaulter, 0 otherwise) is the dependent variable



Independent Variables

Dependent Variable



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SVM in R

Importing and Readyng the Data

```
bankloan<-read.csv("BANK LOAN.csv",header=T)
```

```
bankloan$AGE<-as.factor(bankloan$AGE)
```

as.factor() changes age from an integer to a factor variable.

```
str(bankloan)
```

str() is used to check if the conversion to factor has taken place and if all other variable formats are appropriate, before moving to SVM modeling.

Output

```
'data.frame': 700 obs. of 8 variables:
 $ SN      : int  1 2 3 4 5 6 7 8 9 10 ...
 $ AGE     : Factor w/ 3 levels "1","2","3": 3 1 2 3 1 3 2 3 1 2 ...
 $ EMPLOY  : int  17 10 15 15 2 5 20 12 3 0 ...
 $ ADDRESS : int  12 6 14 14 0 5 9 11 4 13 ...
 $ DEBTINC : num  9.3 17.3 5.5 2.9 17.3 10.2 30.6 3.6 24.4 19.7 ...
 $ CREDDEBT: num  11.36 1.36 0.86 2.66 1.79 ...
 $ OTHDEBT : num  5.01 4 2.17 0.82 3.06 ...
 $ DEFAULTER: int  1 0 0 0 1 0 0 0 1 0 ...
```



SVM in R

SVM Using Package "e1071"

```
install.packages("e1071")
library(e1071)

model<-svm(formula=DEFAULTER~AGE+EMPLOY+ADDRESS+
            DEBTINC+CREDDEBT+OTHDEBT,data=bankloan,
            type="C",probability=TRUE,kernel="linear")
```

Model
coef(model)

- ❑ **svm()** trains a support vector machine.
- ❑ **formula=** gives the model to be fit.
- ❑ **data=** specifies the data object.
- ❑ **type=** specifies whether SVM is used for classification or regression or novelty detection. Default for **type=** is "C".
- ❑ **probability=** logical for indicating whether model should allow for probability predictions.
- ❑ **kernel=** specifies the kernel used in training and predicting. Here, we have kept kernel as linear.

SVM in R

Output

```
> model  
  
Call:  
svm(formula = DEFAULTER ~ AGE + EMPLOY + ADDRESS + DEBTINC + CREDDEBT + OTHDEBT,  
     data = bankloan, type = "C", probability = TRUE,  
     kernel = "linear")  
  
Parameters:  
  SVM-Type:  C-classification  
 SVM-Kernel:  linear  
       cost:  1  
  
Number of Support Vectors:  312
```

Predictions Based on SVM

Predictions

```
pred1<-predict(model,bankloan,probability=TRUE)
```

- ❑ **predict()** returns predicted probabilities based on the model results and historical data.
- ❑ First argument is the **svm()** model object while the second argument is original dataset.
- ❑ **probability=TRUE** returns raw probabilities. This argument is valid only when **type="probability"** is specified in **svm()**.
- ❑ ***pred1<-predict(model,bankloan,decision.values =TRUE) gives scores***

```
pred2<-attr(pred1,"probability")
```

- ❑ **attr()**, from base R, is used get or set specific attributes of an object. Here, we want to get the predicted probabilities obtained by the **svm()** model.
- ❑ First argument is the name of the object whose attributes we want to extract.
- ❑ Second argument is the character string specifying which attribute is to be accessed. Check **pred1** to know the exact name, which is

ROC Curve and Area Under ROC Curve

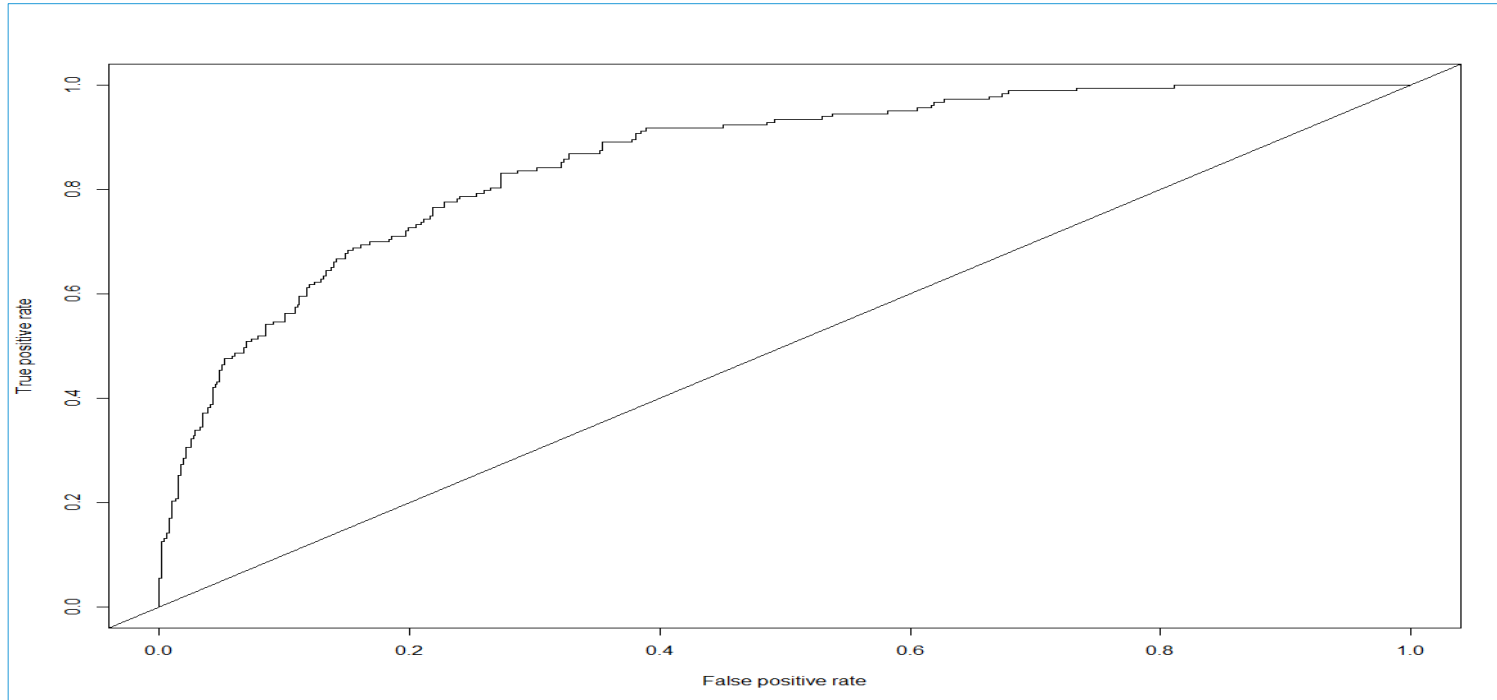
#ROC Curve

```
install.packages("ROCR")  
library(ROCR)  
  
pred<-prediction(pred2,bankloan$DEFAULTER)  
perf<-performance(pred,"tpr","fpr")  
  
plot(perf)  
  
abline(0,1)
```

- **prediction()** creates object of class prediction, required for ROC curve.
- **performance()** calculates predictor evaluations.
- Using **measure="tpr"**, **measure="fpr"** we can plot an ROC Curve.
- **abline()** adds a straight line to the plot.

ROC Curve and Area Under ROC Curve

Output



Area Under ROC Curve

```
auc<-performance(pred,"auc")  
auc@y.values  
[[1]]  
[1] 0.855577
```

← **"auc"** in performance()
calculates Area Under ROC
Curve.

Quick Recap

Support Vector Machines

- SVMs find a hyper plane which separates the d-dimensional data perfectly into its classes

SVM in R

- Package "**e1071**" has **svm()** that trains a support vector machine
- The function takes arguments to specify whether **svm()** is to be used for classification or regression; if probabilities are to be returned and which kernel to use for training and predicting



THANK YOU!!