Initial Dictionary

```
16.0
            -5.00x_1 -1.00x_2 -6.00x_3 +6.00x_4 +3.00x_5 -9.00x_6 +2.00x_7
x_8
      59.0
            -8.00x_1 -6.00x_2 +3.00x_3 +10.00x_4 +6.00x_5 +7.00x_6 -9.00x_7
x_9
     -19.0
            +3.00x_1
                             -10.00x_3 -9.00x_4 -1.00x_5
                                                                +9.00x_7
x_{10}
            -5.00x_1 +7.00x_2 -4.00x_3 -6.00x_4 -5.00x_5 +4.00x_6 -8.00x_7
x_{11}
      18.0
      59.0
            -7.00x_1 - 10.00x_2 + 1.00x_3 - 3.00x_4 - 7.00x_5 + 10.00x_6 - 5.00x_7
x_{12}
      32.0
            -9.00x_1 -2.00x_2 -1.00x_3 +8.00x_4 -6.00x_5 -2.00x_6 -2.00x_7
x_{13}
            42.0
x_{14}
z
      0.0
```

# 0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to:

$$\max \sum_{j=1}^{7} -x_j$$

Primal variable  $x_j$  corresponds to dual variable  $y_j$  for j = 1, ..., 14 Dual Dictionary (with objective changed is):

```
+5.00y_8 +8.00y_9 -3.00y_{10} +5.00y_{11} +7.00y_{12} +9.00y_{13} +9.00y_{14}
y_1
             +1.00y_8 +6.00y_9
                                                  -7.00y_{11} +10.00y_{12} +2.00y_{13} +5.00y_{14}
y_2
     1.0
            +6.00y_8 -3.00y_9 +10.00y_{10} +4.00y_{11} -1.00y_{12} +1.00y_{13} -7.00y_{14}
y_3
            -6.00y_8 \ -10.00y_9 \ +9.00y_{10} \ +6.00y_{11} \ +3.00y_{12} \ -8.00y_{13} \ -3.00y_{14}
     1.0
             -3.00y_8 \ \ -6.00y_9 \ \ +1.00y_{10} \ \ +5.00y_{11} \ \ +7.00y_{12} \ \ +6.00y_{13} \ \ +7.00y_{14}
     1.0
     1.0
            +9.00y_8 -7.00y_9
                                                   -4.00y_{11} -10.00y_{12} +2.00y_{13} +6.00y_{14}
y_6
             -2.00y_8 +9.00y_9 -9.00y_{10} +8.00y_{11} +5.00y_{12} +2.00y_{13} +5.00y_{14}
     1.0
            \overline{-16.00y_8} - \overline{59.00y_9} + \overline{19.00y_{10}} - 18.00y_{11} - 59.00y_{12} - 32.00y_{13} - 42.00y_{14}
```

Initialization succeeded in finding final dual dictionary with 2 pivots

```
0.66666666667
                           +5.67y_8 +5.00y_9 +0.33y_7 +2.33y_{11} +5.33y_{12} +8.33y_{13} +7.33y_{14}
y_1
             1.0
                           +1.00y_8 +6.00y_9
                                                           -7.00y_{11} +10.00y_{12} +2.00y_{13} +5.00y_{14}
y_2
       2.111111111111
                           +3.78y_8 +7.00y_9 -1.11y_7 +12.89y_{11} +4.56y_{12} +3.22y_{13} -1.44y_{14}
y_3
                           -8.00y_8 -1.00y_9 -1.00y_7 + 14.00y_{11} + 8.00y_{12} -6.00y_{13} +2.00y_{14}
             2.0
y_4
       1.111111111111
                           -3.22y_8 -5.00y_9 -0.11y_7 +5.89y_{11} +7.56y_{12} +6.22y_{13} +7.56y_{14}
y_5
                                                           -4.00y_{11} \ -10.00y_{12} \ +2.00y_{13} \ +6.00y_{14}
             1.0
                           +9.00y_8 -7.00y_9
y_6
                           -0.22y_8 +1.00y_9 -0.11y_7 +0.89y_{11} +0.56y_{12} +0.22y_{13} +0.56y_{14}
      0.111111111111111
y_{10}
                          -20.22y_8 - 40.00y_9 - 2.11y_7 - 1.11y_{11} - 48.44y_{12} - 27.78y_{13} - 31.44y_{14}
      2.1111111111111
```

#### Primal Dictionary is:

```
20.22222222
                         -5.67x_1 -1.00x_2 -3.78x_3 +8.00x_4 +3.22x_5 -9.00x_6 +0.22x_{10}
x_8
            40.0
                        -5.00x_1 -6.00x_2 -7.00x_3 +1.00x_4 +5.00x_5 +7.00x_6 -1.00x_{10}
x_9
x_7
      2.111111111111
                        -0.33x_1
                                            +1.11x_3 +1.00x_4 +0.11x_5
      1.111111111111
                         -2.33x_1 +7.00x_2 -12.89x_3 -14.00x_4 -5.89x_5 +4.00x_6 -0.89x_{10}
x_{11}
      48.444444444
                         -5.33x_1 - 10.00x_2 - 4.56x_3 - 8.00x_4 - 7.56x_5 + 10.00x_6 - 0.56x_{10}
x_{12}
x_{13}
      27.777777778
                        -8.33x_1 -2.00x_2 -3.22x_3 +6.00x_4 -6.22x_5 -2.00x_6 -0.22x_{10}
      31.444444444
                         -7.33x_1 -5.00x_2 +1.44x_3 -2.00x_4 -7.56x_5 -6.00x_6 -0.56x_{10}
x_{14}
                        -0.67x_1 -1.00x_2 -2.11x_3 -2.00x_4 -1.11x_5 -1.00x_6 -0.11x_{10}
      -2.1111111111111
 z
```

Primal Dictionary with original objective is:

```
20.22222222
x_8
                         -5.67x_1 -1.00x_2 -3.78x_3 +8.00x_4 +3.22x_5 -9.00x_6 +0.22x_{10}
                         -5.00x_1 -6.00x_2 -7.00x_3 +1.00x_4 +5.00x_5 +7.00x_6 -1.00x_{10}
x_9
            40.0
      2.111111111111
                                             +1.11x_3 +1.00x_4 +0.11x_5
                         -0.33x_1
x_7
      1.111111111111
                         -2.33x_1 + 7.00x_2 - 12.89x_3 - 14.00x_4 - 5.89x_5 + 4.00x_6 - 0.89x_{10}
x_{11}
      48.444444444
                         -5.33x_1 - 10.00x_2 - 4.56x_3 - 8.00x_4 - 7.56x_5 + 10.00x_6 - 0.56x_{10}
x_{12}
                         -8.33x_1 -2.00x_2 -3.22x_3 +6.00x_4 -6.22x_5 -2.00x_6 -0.22x_{10}
      27.777777778
x_{13}
      31.444444444
                         -7.33x_1 -5.00x_2 +1.44x_3 -2.00x_4 -7.56x_5 -6.00x_6 -0.56x_{10}
x_{14}
                         +3.67x_1 -4.00x_2 -7.56x_3 -10.00x_4 -3.56x_5 -4.00x_6 -0.56x_{10}
      -10.555555556
```

 $x_1$  enters and  $x_{11}$  leaves

```
17.5238095238
                          +2.43x_{11} - 18.00x_2 + 27.52x_3 + 42.00x_4 + 17.52x_5 - 18.71x_6 + 2.38x_{10}
x_8
       37.619047619
                          +2.14x_{11} - 21.00x_2 + 20.62x_3 + 31.00x_4 + 17.62x_5 - 1.57x_6 + 0.90x_{10}
x_9
x_7
       1.95238095238
                          +0.14x_{11} -1.00x_2 +2.95x_3 +3.00x_4 +0.95x_5 -0.57x_6 +0.24x_{10}
                          -0.43x_{11} +3.00x_2 -5.52x_3 -6.00x_4 -2.52x_5 +1.71x_6 -0.38x_{10}
       0.47619047619
x_1
       45.9047619048
                          +2.29x_{11} - 26.00x_2 + 24.90x_3 + 24.00x_4 + 5.90x_5 + 0.86x_6 + 1.48x_{10}
x_{12}
       23.8095238095
                          +3.57x_{11} - 27.00x_2 + 42.81x_3 + 56.00x_4 + 14.81x_5 - 16.29x_6 + 2.95x_{10}
x_{13}
       27.9523809524
                           +3.14x_{11} - 27.00x_2 + 41.95x_3 + 42.00x_4 + 10.95x_5 - 18.57x_6 + 2.24x_{10}
x_{14}
       -8.80952380952
                           -1.57x_{11} + 7.00x_2 -27.81x_3 -32.00x_4 -12.81x_5 +2.29x_6 -1.95x_{10}
```

 $x_2$  enters and  $x_{13}$  leaves

```
1.65079365079
                           +0.05x_{11} +0.67x_{13} -1.02x_3 +4.67x_4 +7.65x_5 -7.86x_6 +0.41x_{10}
x_8
                           -0.63x_{11} + 0.78x_{13} - 12.68x_3 - 12.56x_4 + 6.10x_5 + 11.10x_6 - 1.39x_{10}
       19.1005291005
x_9
                           +0.01x_{11} +0.04x_{13} +1.37x_3 +0.93x_4 +0.40x_5 +0.03x_6 +0.13x_{10}
       1.07054673721
x_7
                           -0.03x_{11} - 0.11x_{13} \ -0.77x_3 \ +0.22x_4 \ -0.88x_5 \ -0.10x_6 \ -0.05x_{10}
       3.12169312169
x_1
       22.9770723104
                           -1.15x_{11} + 0.96x_{13} - 16.32x_3 - 29.93x_4 - 8.36x_5 + 16.54x_6 - 1.37x_{10}
x_{12}
       0.881834215168
                           +0.13x_{11} -0.04x_{13} +1.59x_3 +2.07x_4 +0.55x_5 -0.60x_6 +0.11x_{10}
x_2
x_{14}
       4.14285714286
                           -0.43x_{11} + 1.00x_{13} - 0.86x_3 - 14.00x_4 - 3.86x_5 - 2.29x_6 - 0.71x_{10}
       -2.63668430335
                           -0.65x_{11} - 0.26x_{13} - 16.71x_3 - 17.48x_4 - 8.97x_5 - 1.94x_6 - 1.19x_{10}
```

Final Dictionary Final dictionary after first LP relaxation solve:

```
1.65079365079
                           +0.05x_{11}+0.67x_{13}-1.02x_3+4.67x_4+7.65x_5-7.86x_6+0.41x_{10}
x_8
       19.1005291005
                           -0.63x_{11} + 0.78x_{13} - 12.68x_3 - 12.56x_4 + 6.10x_5 + 11.10x_6 - 1.39x_{10}
x_9
                           +0.01x_{11} +0.04x_{13} +1.37x_3 +0.93x_4 +0.40x_5 +0.03x_6 +0.13x_{10}
       1.07054673721
x_7
       3.12169312169
                           -0.03x_{11} - 0.11x_{13} - 0.77x_3 + 0.22x_4 - 0.88x_5 - 0.10x_6 - 0.05x_{10}
x_1
       22.9770723104
                           -1.15x_{11} + 0.96x_{13} - 16.32x_3 - 29.93x_4 - 8.36x_5 + 16.54x_6 - 1.37x_{10}
x_{12}
       0.881834215168
                           +0.13x_{11} -0.04x_{13} +1.59x_3 +2.07x_4 +0.55x_5 -0.60x_6 +0.11x_{10}
x_2
x_{14}
       4.14285714286
                           -0.43x_{11} + 1.00x_{13} - 0.86x_3 - 14.00x_4 - 3.86x_5 - 2.29x_6 - 0.71x_{10}
                           -0.65x_{11} - 0.26x_{13} - 16.71x_3 - 17.48x_4 - 8.97x_5 - 1.94x_6 - 1.19x_{10}
       -2.63668430335
```

```
1.65079365079
                             +0.05x_{11} +0.67x_{13} -1.02x_3 +4.67x_4 +7.65x_5 -7.86x_6 +0.41x_{10}
x_8
        19.1005291005
                             -0.63x_{11} + 0.78x_{13} - 12.68x_3 - 12.56x_4 + 6.10x_5 + 11.10x_6 - 1.39x_{10}
x_9
                             +0.01x_{11} +0.04x_{13} +1.37x_3 +0.93x_4 +0.40x_5 +0.03x_6 +0.13x_{10}
        1.07054673721
x_7
        3.12169312169
                             -0.03x_{11} - 0.11x_{13} - 0.77x_3 + 0.22x_4 - 0.88x_5 - 0.10x_6 - 0.05x_{10}
x_1
        22.9770723104
                             -1.15x_{11} + 0.96x_{13} - 16.32x_3 - 29.93x_4 - 8.36x_5 + 16.54x_6 - 1.37x_{10}
x_{12}
                             +0.13x_{11} - 0.04x_{13} + 1.59x_3 + 2.07x_4 + 0.55x_5 - 0.60x_6 + 0.11x_{10}
       0.881834215168
x_2
        4.14285714286
                             -0.43x_{11} + 1.00x_{13} - 0.86x_3 - 14.00x_4 - 3.86x_5 - 2.29x_6 - 0.71x_{10}
x_{14}
       -0.650793650794
                             +0.95x_{11} +0.33x_{13} +0.02x_3 +0.33x_4 +0.35x_5 +0.86x_6 +0.59x_{10}
x_{15}
       -0.100529100529
                             +0.63x_{11} +0.22x_{13} +0.68x_3 +0.56x_4 +0.90x_5 +0.90x_6 +0.39x_{10}
x_{16}
      -0.0705467372134
                             +0.99x_{11}+0.96x_{13}+0.63x_3+0.07x_4+0.60x_5+0.97x_6+0.87x_{10}
x_{17}
x_{18}
       -0.121693121693
                             +0.03x_{11} +0.11x_{13} +0.77x_3 +0.78x_4 +0.88x_5 +0.10x_6 +0.05x_{10}
       -0.977072310406
                             +0.15x_{11} +0.04x_{13} +0.32x_3 +0.93x_4 +0.36x_5 +0.46x_6 +0.37x_{10}
x_{19}
                             +0.87x_{11} +0.04x_{13} +0.41x_3 +0.93x_4 +0.45x_5 +0.60x_6 +0.89x_{10}
       -0.881834215168
x_{20}
       -0.142857142857
                                                   +0.86x_3
                                                                        +0.86x_5 +0.29x_6 +0.71x_{10}
                             +0.43x_{11}
x_{21}
       -2.63668430335
                             -0.65x_{11} - 0.26x_{13} - 16.71x_3 - 17.48x_4 - 8.97x_5 - 1.94x_6 - 1.19x_{10}
```

## Forming the dual dictionary:

The Final Dual Dictionary is: Final primal dictionary obtained:

```
2.75
                            -0.13x_{11} + 0.62x_{13} -1.37x_3 +3.63x_4 +7.25x_5 -8.38x_6 +1.12x_{19}
x_8
       15.3942307692
x_9
                            -0.05x_{11} + 0.92x_{13} - 11.47x_3 - 9.04x_4 + 7.45x_5 + 12.84x_6 - 3.79x_{19}
x_7
       1.41346153846
                            -0.04x_{11} + 0.02x_{13} + 1.25x_3 + 0.60x_4 + 0.28x_5 - 0.13x_6 + 0.35x_{19}
       2.98076923077
                            -0.01x_{11} - 0.11x_{13} - 0.72x_3 + 0.36x_4 - 0.83x_5 - 0.03x_6 - 0.14x_{19}
x_1
       19.3365384615
                           -0.58x_{11} + 1.10x_{13} - 15.13x_3 - 26.48x_4 - 7.03x_5 + 18.25x_6 - 3.73x_{19}
x_{12}
       1.17307692308
                           +0.09x_{11} -0.05x_{13} +1.49x_3 +1.80x_4 +0.44x_5 -0.74x_6 +0.30x_{19}
x_2
       2.24038461538
                            -0.13x_{11} + 1.07x_{13} - 0.24x_3 - 12.20x_4 - 3.16x_5 - 1.39x_6 - 1.95x_{19}
x_{14}
       0.913461538462
                           +0.71x_{11}+0.27x_{13}-0.50x_3-1.15x_4-0.22x_5+0.12x_6+1.60x_{19}
x_{15}
                           +0.47x_{11} +0.18x_{13} +0.34x_3 -0.43x_4 +0.52x_5 +0.41x_6 +1.07x_{19}
       0.942307692308
x_{16}
                            +0.62x_{11} +0.88x_{13} -0.12x_3 -2.12x_4 -0.25x_5 -0.13x_6 +2.37x_{19}
             2.25
x_{17}
      0.0192307692308
                           +0.01x_{11} +0.11x_{13} +0.72x_3 +0.64x_4 +0.83x_5 +0.03x_6 +0.14x_{19}
x_{18}
       2.66346153846
                            -0.42x_{11} - 0.10x_{13} - 0.87x_3 - 2.52x_4 - 0.97x_5 - 1.25x_6 + 2.73x_{19}
x_{10}
       1.49038461538
                            +0.50x_{11} -0.05x_{13} -0.36x_3 -1.32x_4 -0.41x_5 -0.51x_6 +2.43x_{19}
x_{20}
       1.75961538462
                            +0.13x_{11} -0.07x_{13} +0.24x_3 -1.80x_4 +0.16x_5 -0.61x_6 +1.95x_{19}
x_{21}
       -5.79807692308
                            -0.15x_{11} - 0.14x_{13} - 15.68x_3 - 14.49x_4 - 7.82x_5 - 0.45x_6 - 3.24x_{19}
```

```
2.75
                             -0.13x_{11} + 0.62x_{13} -1.37x_3 +3.63x_4 +7.25x_5 -8.38x_6 +1.12x_{19}
x_8
        15.3942307692
                             -0.05x_{11} + 0.92x_{13} - 11.47x_3 - 9.04x_4 + 7.45x_5 + 12.84x_6 - 3.79x_{19}
x_9
x_7
        1.41346153846
                             -0.04x_{11} + 0.02x_{13} + 1.25x_3 + 0.60x_4 + 0.28x_5 - 0.13x_6 + 0.35x_{19}
        2.98076923077
                             -0.01x_{11} - 0.11x_{13} - 0.72x_3 + 0.36x_4 - 0.83x_5 - 0.03x_6 - 0.14x_{19}
x_1
                             -0.58x_{11} + 1.10x_{13} - 15.13x_3 - 26.48x_4 - 7.03x_5 + 18.25x_6 - 3.73x_{19}
x_{12}
        19.3365384615
        1.17307692308
                             +0.09x_{11} -0.05x_{13} +1.49x_3 +1.80x_4 +0.44x_5 -0.74x_6 +0.30x_{19}
x_2
        2.24038461538
                             -0.13x_{11} + 1.07x_{13} - 0.24x_3 - 12.20x_4 - 3.16x_5 - 1.39x_6 - 1.95x_{19}
x_{14}
       0.913461538462
                             +0.71x_{11}+0.27x_{13}-0.50x_3-1.15x_4-0.22x_5+0.12x_6+1.60x_{19}
x_{15}
       0.942307692308
                             +0.47x_{11} +0.18x_{13} +0.34x_3 -0.43x_4 +0.52x_5 +0.41x_6 +1.07x_{19}
x_{16}
              2.25
                             +0.62x_{11} +0.88x_{13} -0.12x_3 -2.12x_4 -0.25x_5 -0.13x_6 +2.37x_{19}
x_{17}
       0.0192307692308
                             +0.01x_{11} +0.11x_{13} +0.72x_3 +0.64x_4 +0.83x_5 +0.03x_6 +0.14x_{19}
x_{18}
        2.66346153846
                             -0.42x_{11} - 0.10x_{13} - 0.87x_3 - 2.52x_4 - 0.97x_5 - 1.25x_6 + 2.73x_{19}
x_{10}
                             +0.50x_{11} - 0.05x_{13} - 0.36x_3 - 1.32x_4 - 0.41x_5 - 0.51x_6 + 2.43x_{19}
        1.49038461538
x_{20}
        1.75961538462
                             +0.13x_{11} -0.07x_{13} +0.24x_3 -1.80x_4 +0.16x_5 -0.61x_6 +1.95x_{19}
x_{21}
             -0.75
                             +0.13x_{11} +0.38x_{13} +0.37x_3 +0.37x_4 +0.75x_5 +0.38x_6 +0.88x_{19}
x_{22}
       -0.394230769231
                             +0.05x_{11} +0.08x_{13} +0.47x_3 +0.04x_4 +0.55x_5 +0.16x_6 +0.79x_{19}
x_{23}
       -0.413461538462
                             +0.04x_{11} +0.98x_{13} +0.75x_3 +0.40x_4 +0.72x_5 +0.13x_6 +0.65x_{19}
x_{24}
       -0.980769230769
                             +0.01x_{11} +0.11x_{13} +0.72x_3 +0.64x_4 +0.83x_5 +0.03x_6 +0.14x_{19}
x_{25}
       -0.336538461538
                             +0.58x_{11} +0.90x_{13} +0.13x_3 +0.48x_4 +0.03x_5 +0.75x_6 +0.73x_{19}
x_{26}
       -0.173076923077
                             +0.91x_{11}+0.05x_{13}+0.51x_3+0.20x_4+0.56x_5+0.74x_6+0.70x_{19}
x_{27}
x_{28}
       -0.240384615385
                             +0.13x_{11} +0.93x_{13} +0.24x_3 +0.20x_4 +0.16x_5 +0.39x_6 +0.95x_{19}
       -0.913461538462
                             +0.29x_{11} +0.73x_{13} +0.50x_3 +0.15x_4 +0.22x_5 +0.88x_6 +0.40x_{19}
x_{29}
       -0.942307692308
                             +0.53x_{11} + 0.82x_{13} + 0.66x_3 + 0.43x_4 + 0.48x_5 + 0.59x_6 + 0.93x_{19}
x_{30}
                             +0.38x_{11} +0.12x_{13} +0.12x_3 +0.12x_4 +0.25x_5 +0.13x_6 +0.63x_{19}
             -0.25
x_{31}
       -0.0192307692308
                             +0.99x_{11} +0.89x_{13} +0.28x_3 +0.36x_4 +0.17x_5 +0.97x_6 +0.86x_{19}
x_{32}
       -0.663461538462
                             +0.42x_{11} +0.10x_{13} +0.87x_3 +0.52x_4 +0.97x_5 +0.25x_6 +0.27x_{19}
x_{33}
                             +0.50x_{11} +0.05x_{13} +0.36x_3 +0.32x_4 +0.41x_5 +0.51x_6 +0.57x_{19}
       -0.490384615385
x_{34}
       -0.759615384615
                             +0.87x_{11} +0.07x_{13} +0.76x_3 +0.80x_4 +0.84x_5 +0.61x_6 +0.05x_{19}
x_{35}
       -5.79807692308
                             -0.15x_{11} - 0.14x_{13} - 15.68x_3 - 14.49x_4 - 7.82x_5 - 0.45x_6 - 3.24x_{19}
```

Forming the dual dictionary:

The Final Dual Dictionary is:

```
8.52631578947
                          -0.21x_{35} +6.05x_{25} -5.58x_3 -0.11x_4 +2.42x_5 -8.42x_6 +0.26x_{19}
x_8
                          -0.16x_{35} + 8.79x_{25} - 17.68x_3 - 14.58x_4 + 0.32x_5 + 12.68x_6 - 5.05x_{19}
       23.8947368421
x_9
       1.63157894737
                          -0.05x_{35} +0.26x_{25} +1.11x_3 +0.47x_4 +0.11x_5 -0.11x_6 +0.32x_{19}
x_7
                                                            +1.00x_4
             2.0
                                     -1.00x_{25}
x_1
       29.4736842105
                          -0.79x_{35} + 10.95x_{25} - 22.42x_3 - 32.89x_4 - 15.42x_5 + 18.42x_6 - 5.26x_{19}
x_{12}
      0.736842105263
                          +0.11x_{35} -0.53x_{25} +1.79x_3 +2.05x_4 +0.79x_5 -0.79x_6 +0.37x_{19}
x_2
       12.1578947368
                          -0.26x_{35} + 10.32x_{25} - 7.47x_3 - 18.63x_4 - 11.47x_5 - 1.53x_6 - 3.42x_{19}
x_{14}
                          +0.79x_{35} +2.05x_{25} -2.58x_3 -3.11x_4 -2.58x_5 -0.42x_6 +1.26x_{19}
       3.52631578947
x_{15}
                          +0.53x_{35} +1.37x_{25} -1.05x_3 -1.74x_4 -1.05x_5 +0.05x_6 +0.84x_{19}
       2.68421052632
x_{16}
       10.4210526316
                          +0.63x_{35} +7.84x_{25} -6.26x_3 -7.68x_4 -7.26x_5 -0.74x_6 +1.21x_{19}
x_{17}
             1.0
                                     +1.00x_{25}
x_{18}
       1.68421052632
                          -0.47x_{35} -0.63x_{25} -0.05x_3 -1.74x_4 -0.05x_5 -0.95x_6 +2.84x_{19}
x_{10}
                          +0.58x_{35} -0.89x_{25} -0.16x_3 -1.21x_4 -0.16x_5 -0.84x_6 +2.53x_{19}
       1.05263157895
x_{20}
       1.10526315789
                          +0.16x_{35} -0.79x_{25} +0.68x_3 -1.42x_4 +0.68x_5 -0.68x_6 +2.05x_{19}
x_{21}
       9.26315789474
                          -0.11x_{35} + 9.53x_{25} -6.79x_3 -6.05x_4 -7.79x_5 -0.21x_6 -1.37x_{19}
x_{13}
       2.73684210526
                          +0.11x_{35} +3.47x_{25} -2.21x_3 -1.95x_4 -2.21x_5 +0.21x_6 +0.37x_{19}
x_{22}
       8.63157894737
                          -0.05x_{35} + 9.26x_{25} -5.89x_3 -5.53x_4 -6.89x_5 -0.11x_6 -0.68x_{19}
x_{24}
      0.368421052632
                          +0.05x_{35} +0.74x_{25} -0.11x_3 -0.47x_4 -0.11x_5 +0.11x_6 +0.68x_{19}
x_{23}
       8.05263157895
                          +0.58x_{35} +8.11x_{25} -6.16x_3 -5.21x_4 -7.16x_5 +0.16x_6 -0.47x_{19}
x_{26}
                          +1.05x_{35} -0.26x_{25} -0.11x_3 -0.47x_4 -0.11x_5 +0.11x_6 +0.68x_{19}
      0.368421052632
x_{27}
                          +0.05x_{35}^{35} +8.74x_{25} -6.11x_3 -5.47x_4 -7.11x_5 +0.11x_6 -0.32x_{19}
x_{28}
       8.36842105263
                          +0.26x_{35} +6.68x_{25} -4.53x_3 -4.37x_4 -5.53x_5 +0.53x_6 -0.58x_{19}
       5.84210526316
x_{29}
       6.68421052632
                          +0.53x_{35} +7.37x_{25} -5.05x_3 -4.74x_4 -6.05x_5 +0.05x_6 -0.16x_{19}
x_{30}
                          +0.42x_{35} +0.89x_{25} -0.84x_3 -0.79x_4 -0.84x_5 -0.16x_6 +0.47x_{19}
      0.947368421053
x_{31}
       8.36842105263
                          +1.05x_{35} +7.74x_{25} -6.11x_3 -5.47x_4 -7.11x_5 +0.11x_6 -0.32x_{19}
x_{32}
      0.315789473684
                          +0.47x_{35} +0.63x_{25} +0.05x_3 -0.26x_4 +0.05x_5 -0.05x_6 +0.16x_{19}
x_{33}
      0.0526315789474
                          +0.58x_{35} +0.11x_{25} -0.16x_3 -0.21x_4 -0.16x_5 +0.16x_6 +0.53x_{19}
x_{34}
                          +1.16x_{35} -0.79x_{25} -0.32x_3 -0.42x_4 -0.32x_5 -0.68x_6 +0.05x_{19}
      0.105263157895
x_{11}
                          -0.16x_{35} -1.21x_{25} -14.68x_3 -13.58x_4 -6.68x_5 -0.32x_6 -3.05x_{19}
      -7.10526315789
```

```
8.52631578947
                            -0.21x_{35} +6.05x_{25} -5.58x_3 -0.11x_4 +2.42x_5 -8.42x_6 +0.26x_{19}
x_8
        23.8947368421
                            -0.16x_{35} + 8.79x_{25} - 17.68x_3 - 14.58x_4 + 0.32x_5 + 12.68x_6 - 5.05x_{19}
x_9
        1.63157894737
                            -0.05x_{35} +0.26x_{25} +1.11x_3 +0.47x_4 +0.11x_5 -0.11x_6 +0.32x_{19}
x_7
              2.0
                                                             +1.00x_{4}
                                       -1.00x_{25}
x_1
x_{12}
        29.4736842105
                            -0.79x_{35} + 10.95x_{25} - 22.42x_3 - 32.89x_4 - 15.42x_5 + 18.42x_6 - 5.26x_{19}
       0.736842105263
                            +0.11x_{35} -0.53x_{25} +1.79x_3 +2.05x_4 +0.79x_5 -0.79x_6 +0.37x_{19}
x_2
        12.1578947368
                            -0.26x_{35} + 10.32x_{25} - 7.47x_3 - 18.63x_4 - 11.47x_5 - 1.53x_6 - 3.42x_{19}
x_{14}
        3.52631578947
                            +0.79x_{35} +2.05x_{25} -2.58x_3 -3.11x_4 -2.58x_5 -0.42x_6 +1.26x_{19}
x_{15}
x_{16}
        2.68421052632
                            +0.53x_{35} +1.37x_{25} -1.05x_3 -1.74x_4 -1.05x_5 +0.05x_6 +0.84x_{19}
        10.4210526316
                            +0.63x_{35} +7.84x_{25} -6.26x_3 -7.68x_4 -7.26x_5 -0.74x_6 +1.21x_{19}
x_{17}
              1.0
                                       +1.00x_{25}
x_{18}
        1.68421052632
                                                  -0.05x_3 -1.74x_4 -0.05x_5 -0.95x_6 +2.84x_{19}
x_{10}
                            -0.47x_{35} -0.63x_{25}
                            +0.58x_{35} -0.89x_{25} -0.16x_3 -1.21x_4 -0.16x_5 -0.84x_6 +2.53x_{19}
x_{20}
        1.05263157895
        1.10526315789
                            +0.16x_{35} -0.79x_{25} +0.68x_3 -1.42x_4 +0.68x_5 -0.68x_6 +2.05x_{19}
x_{21}
                            -0.11x_{35} + 9.53x_{25} -6.79x_3 -6.05x_4 -7.79x_5 -0.21x_6 -1.37x_{19}
        9.26315789474
x_{13}
                            +0.11x_{35} +3.47x_{25} -2.21x_3 -1.95x_4 -2.21x_5 +0.21x_6 +0.37x_{19}
        2.73684210526
x_{22}
x_{24}
        8.63157894737
                            -0.05x_{35} + 9.26x_{25} -5.89x_3 -5.53x_4 -6.89x_5 -0.11x_6 -0.68x_{19}
                            +0.05x_{35} +0.74x_{25} -0.11x_3 -0.47x_4 -0.11x_5 +0.11x_6 +0.68x_{19}
       0.368421052632
x_{23}
        8.05263157895
                            +0.58x_{35} +8.11x_{25} -6.16x_3 -5.21x_4 -7.16x_5 +0.16x_6 -0.47x_{19}
x_{26}
                            +1.05x_{35} -0.26x_{25} -0.11x_3 -0.47x_4 -0.11x_5 +0.11x_6 +0.68x_{19}
       0.368421052632
x_{27}
        8.36842105263
                            +0.05x_{35} +8.74x_{25} -6.11x_3 -5.47x_4
                                                                       -7.11x_5 +0.11x_6 -0.32x_{19}
x_{28}
        5.84210526316
                            +0.26x_{35} +6.68x_{25} -4.53x_3 -4.37x_4
                                                                      -5.53x_5 +0.53x_6 -0.58x_{19}
x_{29}
                            +0.53x_{35} +7.37x_{25} -5.05x_3 -4.74x_4 -6.05x_5 +0.05x_6 -0.16x_{19}
        6.68421052632
x_{30}
x_{31}
       0.947368421053
                            +0.42x_{35} +0.89x_{25} -0.84x_3 -0.79x_4 -0.84x_5 -0.16x_6 +0.47x_{19}
        8.36842105263
                            +1.05x_{35} +7.74x_{25} -6.11x_3 -5.47x_4 -7.11x_5 +0.11x_6 -0.32x_{19}
x_{32}
       0.315789473684
                            +0.47x_{35} +0.63x_{25} +0.05x_3 -0.26x_4 +0.05x_5 -0.05x_6 +0.16x_{19}
x_{33}
                            +0.58x_{35} +0.11x_{25} -0.16x_3 -0.21x_4 -0.16x_5 +0.16x_6 +0.53x_{19}
       0.0526315789474
x_{34}
                            +1.16x_{35} -0.79x_{25} -0.32x_3 -0.42x_4 -0.32x_5 -0.68x_6 +0.05x_{19}
x_{11}
       0.105263157895
       -0.526315789474
                            +0.21x_{35} +0.95x_{25} +0.58x_3 +0.11x_4 +0.58x_5 +0.42x_6 +0.74x_{19}
x_{36}
       -0.894736842105
                            +0.16x_{35} +0.21x_{25} +0.68x_3 +0.58x_4 +0.68x_5 +0.32x_6 +0.05x_{19}
x_{37}
      -0.631578947368
                            +0.05x_{35} +0.74x_{25} +0.89x_3 +0.53x_4 +0.89x_5 +0.11x_6 +0.68x_{19}
x_{38}
       -0.473684210526
                            +0.79x_{35} +0.05x_{25} +0.42x_3 +0.89x_4 +0.42x_5 +0.58x_6 +0.26x_{19}
x_{39}
                            +0.89x_{35} +0.53x_{25} +0.21x_3 +0.95x_4 +0.21x_5 +0.79x_6 +0.63x_{19}
       -0.736842105263
x_{40}
       -0.157894736842
                            +0.26x_{35} +0.68x_{25} +0.47x_3 +0.63x_4 +0.47x_5 +0.53x_6 +0.42x_{19}
x_{41}
                            +0.21x_{35} +0.95x_{25} +0.58x_3 +0.11x_4 +0.58x_5 +0.42x_6 +0.74x_{19}
       -0.526315789474
x_{42}
                            +0.47x_{35} +0.63x_{25} +0.05x_3 +0.74x_4 +0.05x_5 +0.95x_6 +0.16x_{19}
x_{43}
       -0.684210526316
                            +0.37x_{35} +0.16x_{25} +0.26x_3 +0.68x_4 +0.26x_5 +0.74x_6 +0.79x_{19}
       -0.421052631579
x_{44}
                            +0.47x_{35} +0.63x_{25} +0.05x_3 +0.74x_4 +0.05x_5 +0.95x_6 +0.16x_{19}
       -0.684210526316
x_{45}
      -0.0526315789474
                            +0.42x_{35} +0.89x_{25} +0.16x_3 +0.21x_4 +0.16x_5 +0.84x_6 +0.47x_{19}
x_{46}
x_{47}
       -0.105263157895
                            +0.84x_{35} +0.79x_{25} +0.32x_3 +0.42x_4 +0.32x_5 +0.68x_6 +0.95x_{19}
       -0.263157894737
                            +0.11x_{35} +0.47x_{25} +0.79x_3 +0.05x_4 +0.79x_5 +0.21x_6 +0.37x_{19}
x_{48}
       -0.736842105263
                            +0.89x_{35} +0.53x_{25} +0.21x_3 +0.95x_4 +0.21x_5 +0.79x_6 +0.63x_{19}
x_{49}
                            +0.05x_{35} +0.74x_{25} +0.89x_3 +0.53x_4 +0.89x_5 +0.11x_6 +0.68x_{19}
       -0.631578947368
x_{50}
       -0.368421052632
                            +0.95x_{35} +0.26x_{25} +0.11x_3 +0.47x_4 +0.11x_5 +0.89x_6 +0.32x_{19}
x_{51}
      -0.0526315789474
                            +0.42x_{35} +0.89x_{25} +0.16x_3 +0.21x_4 +0.16x_5 +0.84x_6 +0.47x_{19}
x_{52}
      -0.368421052632
                            +0.95x_{35} +0.26x_{25} +0.11x_3 +0.47x_4 +0.11x_5 +0.89x_6 +0.32x_{19}
x_{53}
      -0.368421052632
                            +0.95x_{35} +0.26x_{25} +0.11x_3 +0.47x_4 +0.11x_5 +0.89x_6 +0.32x_{19}
x_{54}
       -0.842105263158
                            +0.74x_{35} +0.32x_{25} +0.53x_3 +0.37x_4 +0.53x_5 +0.47x_6 +0.58x_{19}
x_{55}
       -0.684210526316
                            +0.47x_{35} +0.63x_{25} +0.05x_3 +0.74x_4 +0.05x_5 +0.95x_6 +0.16x_{19}
x_{56}
                            +0.58x_{35} +0.11x_{25} +0.84x_3 +0.79x_4 +0.84x_5 +0.16x_6 +0.53x_{19}
       -0.947368421053
x_{57}
                            +0.95x_{35} +0.26x_{25} +0.11x_3 +0.47x_4 +0.11x_5 +0.89x_6 +0.32x_{19}
x_{58}
       -0.368421052632
      -0.315789473684
                            +0.53x_{35} +0.37x_{25} +0.95x_3 +0.26x_4 +0.95x_5 +0.05x_6 +0.84x_{19}
x_{59}
      -0.0526315789474
                            +0.42x_{35} +0.89x_{25} +0.16x_3 +0.21x_4 +0.16x_5 +0.84x_6 +0.47x_{19}
x_{60}
      -0.105263157895
                            +0.84x_{35} \ +0.79x_{25} \ +0.32x_3 \ +0.42x_4 \ +0.32x_5 \ +0.68x_6 \ +0.95x_{19}
x_{61}
       -7.10526315789
                            -0.16x_{35} -1.21x_{25} -14.68x_3 -13.58x_4 -6.68x_5 -0.32x_6 -3.05x_{19}
```

Forming the dual dictionary: The Final Dual Dictionary is:

```
0.2708333333333
                                              +0.12x_8 -2.19x_{38} +2.21x_3 +2.31x_4 +0.21x_5 +3.31x_{37} +0.58x_{10}
x_2
              36.6458333333
                                              -1.62x_8 + 28.94x_{38} - 28.04x_3 - 22.56x_4 + 2.96x_5 - 36.56x_{37} - 7.92x_{10}
x_9
                       1.5
                                              +0.00x_8 +0.50x_{38} +1.00x_3 +0.50x_4 +0.00x_5 -0.50x_{37} -0.00x_{10}
x_7
                                              -0.00x_8 -1.50x_{38} +0.33x_3 +1.50x_4 +0.33x_5 +1.50x_{37} +0.33x_{10}
              1.83333333333
x_1
                                              -2.50x_8 + 41.75x_{38} - 37.17x_3 - 42.25x_4 - 10.17x_5 - 54.25x_{37} - 10.67x_{10} + 10.07x_{10} - 10.07x_{10} 
x_{12}
              46.5833333333
              3.20833333333
                                              +0.25x_8 -4.38x_{38} -1.92x_3 -2.38x_4 -3.92x_5 +10.63x_{37} +0.83x_{10}
x_{35}
              10.2708333333
                                              +0.13x_8+14.81x_{38} -6.79x_3 -22.69x_4-11.79x_5-19.69x_{37} -4.42x_{10}
x_{14}
                                              +0.25x_8 -0.88x_{38} -5.25x_3 -5.88x_4 -7.25x_5 +7.13x_{37} +0.50x_{10}
                     6.375
x_{15}
x_{16}
                    4.9375
                                              +0.12x_8 -0.19x_{38} -3.13x_3 -3.69x_4 -4.13x_5 +4.31x_{37} +0.25x_{10}
                    13.375
                                              +0.25x_8 +8.13x_{38} -10.25x_3 -12.87x_4 -13.25x_5 -2.88x_{37} -1.50x_{10}
x_{17}
                                              +0.00x_8 +1.50x_{38} -0.33x_3 -0.50x_4 -0.33x_5 -1.50x_{37} -0.33x_{10}
              1.16666666667
x_{18}
                                              -0.00x_8 -0.00x_{38} -0.67x_3 -0.00x_4 -0.67x_5 +1.00x_{37} +0.33x_{10}
x_{19}
             0.33333333333333
x_{20}
              2.70833333333
                                              +0.25x_{8} -4.88x_{38} -1.92x_{3} -1.88x_{4} -3.92x_{5} +11.13x_{37} +1.83x_{10}
                    1.4375
                                              +0.12x_8 -2.69x_{38} -0.13x_3 -1.19x_4 -1.13x_5 +5.81x_{37} +1.25x_{10}
x_{21}
                                              +0.00x_8+14.50x_{38} -8.67x_3 -10.50x_4 -9.67x_5 -16.50x_{37} -3.67x_{10}
              9.83333333333
x_{13}
                                              +0.00x_8 +5.00x_{38} -4.00x_3 -4.00x_4 -4.00x_5 -4.00x_{37} -1.00x_{10}
                       4.0
x_{22}
x_{24}
              9.66666666667
                                              +0.00x_8 + 14.00x_{38} - 8.33x_3 - 10.00x_4 - 9.33x_5 - 15.00x_{37} - 3.33x_{10}
                                              +0.00x_8 +1.00x_{38} -1.00x_3 -1.00x_4 -1.00x_5 -0.00x_{37} -0.00x_{10}
                       1.0
x_{23}
              11.2708333333
                                              +0.13x_8 +9.81x_{38} -9.79x_3 -10.69x_4 -11.79x_5 -6.69x_{37} -2.42x_{10}
x_{26}
              4.04166666667
                                              +0.25x_8 -4.88x_{38} -2.58x_3 -2.88x_4 -4.58x_5 +12.13x_{37} +1.17x_{10}
x_{27}
                                              +0.00x_8+13.00x_{38}-9.00x_3-10.00x_4-10.00x_5-13.00x_{37}-3.00x_{10}
                      10.0
x_{28}
              8.1666666667
                                              +0.00x_8 + 9.50x_{38} -7.33x_3 -8.50x_4 -8.33x_5 -8.50x_{37} -2.33x_{10}
x_{29}
                                              +0.13x_8 +8.81x_{38} -8.46x_3 -9.69x_4 -10.46x_5 -5.69x_{37} -2.08x_{10}
              9.60416666667
x_{30}
x_{31}
                    2.4375
                                              +0.12x_8 -0.69x_{38} -2.13x_3 -2.19x_4 -3.13x_5 +3.81x_{37} +0.25x_{10}
              13.0416666667
                                              +0.25x_{8} +7.13x_{38} -10.58x_{3} -11.87x_{4} -13.58x_{5} -0.88x_{37} -1.83x_{10}
x_{32}
                    1.9375
                                              +0.12x_8 -1.19x_{38} -1.13x_3 -1.69x_4 -2.13x_5 +4.31x_{37} +0.25x_{10}
x_{33}
                                              +0.12x_8 -2.19x_{38} -1.79x_3 -1.69x_4 -2.79x_5 +6.31x_{37} +0.58x_{10}
              2.27083333333
x_{34}
                                                                           -1.71x_3 -2.56x_4 -4.71x_5 +14.44x_{37} +1.42x_{10}
x_{11}
              2.97916666667
                                              +0.37x_8 -7.06x_{38}
                    1.0625
                                              -0.12x_8 + 1.19x_{38} -0.87x_3 -0.31x_4 +0.13x_5 -1.31x_{37} -0.25x_{10}
x_6
                                              -0.00x_8 + 1.00x_{38} - 1.00x_3 - 1.00x_4 - 1.00x_5 + 1.00x_{37} + 0.00x_{10}
                       1.0
x_{36}
             0.166666666667
                                              +0.00x_8 +1.50x_{38} -0.33x_3 -0.50x_4 -0.33x_5 -1.50x_{37} -0.33x_{10}
x_{25}
              2.770833333333
                                              +0.12x_8 -2.69x_{38} -1.79x_3 -1.19x_4 -2.79x_5 +7.81x_{37} +0.58x_{10}
x_{39}
                                              +0.12x_8 -2.19x_{38} -2.79x_3 -1.69x_4 -3.79x_5 +8.31x_{37} +0.58x_{10}
              3.27083333333
x_{40}
                                              +0.00x_8 +0.50x_{38} -1.00x_3 -0.50x_4 -1.00x_5 +1.50x_{37} +0.00x_{10}
                       1.5
x_{41}
                                              -0.00x_8 + 1.00x_{38} - 1.00x_3 - 1.00x_4 - 1.00x_5 + 1.00x_{37} + 0.00x_{10}
                       1.0
x_{42}
                                                                           -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{10}
x_{43}
                       2.0
                                              -0.00x_8 -0.00x_{38}
                                                                           -1.67x_3 -0.50x_4 -1.67x_5 +3.50x_{37} +0.33x_{10}
              1.83333333333
                                              -0.00x_8 -0.50x_{38}
x_{44}
                                                                          -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{10}
                                              -0.00x_8 -0.00x_{38}
                       2.0
x_{45}
                       2.5
                                              -0.00x_8 +0.50x_{38}
                                                                           -2.00x_3 -1.50x_4 -2.00x_5 +2.50x_{37} +0.00x_{10}
x_{46}
x_{47}
              3.77083333333
                                                                           -2.79x_3 -2.19x_4 -3.79x_5 +7.81x_{37} +0.58x_{10}
                                              +0.12x_8 -1.69x_{38}
                       0.5
                                              -0.00x_8 + 0.50x_{38} + 0.00x_3 -0.50x_4 + 0.00x_5 + 0.50x_{37} + 0.00x_{10}
x_{48}
              3.27083333333
                                                                           -2.79x_3 -1.69x_4 -3.79x_5 +8.31x_{37} +0.58x_{10}
                                              +0.12x_8 -2.19x_{38}
x_{49}
                                              +0.00x_8 +1.00x_{38} +0.00x_3 +0.00x_4 +0.00x_5 -0.00x_{37}
             .12687636999e
                                                                                                                                        -0.00x_{10}
x_{50}
              3.77083333333
                                              +0.12x_8 -2.69x_{38}
                                                                           -2.79x_3 -2.19x_4 -3.79x_5 +8.81x_{37} +0.58x_{10}
x_{51}
                       2.5
                                              -0.00x_8 + 0.50x_{38} -2.00x_3 -1.50x_4 -2.00x_5 +2.50x_{37} +0.00x_{10}
x_{52}
              3.770833333333
                                              +0.12x_8 -2.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +8.81x_{37} +0.58x_{10}
x_{53}
                                              +0.12x_{8}-2.69x_{38} -2.79x_{3} -2.19x_{4} -3.79x_{5} +8.81x_{37} +0.58x_{10}
              3.77083333333
x_{54}
              2.27083333333
                                              +0.12x_8 -2.19x_{38} -1.79x_3 -1.69x_4 -2.79x_5 +7.31x_{37} +0.58x_{10}
x_{55}
                                              -0.00x_8 -0.00x_{38} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{10}
                       2.0
x_{56}
                                              +0.12x_8 -2.19x_{38} -0.79x_3 -0.69x_4 -1.79x_5 +6.31x_{37} +0.58x_{10}
              1.27083333333
x_{57}
                                                                           -2.79x_3 -2.19x_4 -3.79x_5 +8.81x_{37} +0.58x_{10}
x_{58}
              3.77083333333
                                              +0.12x_8 -2.69x_{38}
                                              +0.12x_8 -1.69x_{38} -0.79x_3 -1.19x_4 -1.79x_5 +5.81x_{37}
              1.77083333333
                                                                                                                                        +0.58x_{10}
x_{59}
                       2.5
                                              -0.00x_8 +0.50x_{38} -2.00x_3 -1.50x_4 -2.00x_5 +2.50x_{37} +0.00x_{10}
x_{60}
              3.770833333333
                                              +0.12x_8 -1.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +7.81x_{37} +0.58x_{10}
x_{61}
             -9.16666666667
                                              +0.00x_8 -1.50x_{38} -11.67x_3 -12.50x_4 -3.67x_5 -2.50x_{37} -0.67x_{10}
```

U E000000000000

```
0.2708333333333
                                 +0.12x_8 -2.19x_{38} +2.21x_3 +2.31x_4 +0.21x_5 +3.31x_{37} +0.58x_{10}
x_2
                                 -1.62x_8 + 28.94x_{38} - 28.04x_3 - 22.56x_4 + 2.96x_5 - 36.56x_{37} - 7.92x_{10}
          36.6458333333
x_9
                                 +0.00x_8 +0.50x_{38} +1.00x_3 +0.50x_4 +0.00x_5 -0.50x_{37} -0.00x_{10}
                 1.5
x_7
                                 -0.00x_8 -1.50x_{38} +0.33x_3 +1.50x_4 +0.33x_5 +1.50x_{37} +0.33x_{10}
           1.83333333333
x_1
                                 -2.50x_8 + 41.75x_{38} - 37.17x_3 - 42.25x_4 - 10.17x_5 - 54.25x_{37} - 10.67x_{10}
x_{12}
           46.5833333333
                                 +0.25x_8 -4.38x_{38} -1.92x_3 -2.38x_4 -3.92x_5 +10.63x_{37} +0.83x_{10}
          3.20833333333
x_{35}
                                 +0.13x_8 + 14.81x_{38} -6.79x_3 -22.69x_4 -11.79x_5 -19.69x_{37} -4.42x_{10}
           10.2708333333
x_{14}
                                 +0.25x_8 -0.88x_{38} -5.25x_3 -5.88x_4 -7.25x_5 +7.13x_{37} +0.50x_{10}
               6.375
x_{15}
x_{16}
               4.9375
                                 +0.12x_8 -0.19x_{38} -3.13x_3 -3.69x_4 -4.13x_5 +4.31x_{37} +0.25x_{10}
               13.375
                                 +0.25x_8 +8.13x_{38} -10.25x_3 -12.87x_4 -13.25x_5 -2.88x_{37}
x_{17}
                                 +0.00x_8 +1.50x_{38} -0.33x_3 -0.50x_4 -0.33x_5 -1.50x_{37} -0.33x_{10}
          1.16666666667
x_{18}
                                 -0.00x_8 -0.00x_{38} -0.67x_3 -0.00x_4 -0.67x_5 +1.00x_{37} +0.33x_{10}
x_{19}
          0.33333333333333
                                 +0.25x_8 -4.88x_{38} -1.92x_3 -1.88x_4 -3.92x_5 +11.13x_{37} +1.83x_{10}
          2.70833333333
x_{20}
               1.4375
                                 +0.12x_8 -2.69x_{38} -0.13x_3 -1.19x_4 -1.13x_5 +5.81x_{37} +1.25x_{10}
x_{21}
          9.83333333333
                                 +0.00x_8+14.50x_{38} -8.67x_3 -10.50x_4 -9.67x_5 -16.50x_{37} -3.67x_{10}
x_{13}
                                 +0.00x_8 +5.00x_{38} -4.00x_3 -4.00x_4 -4.00x_5 -4.00x_{37} -1.00x_{10}
                 4.0
x_{22}
          9.6666666667
                                 +0.00x_8 + 14.00x_{38} - 8.33x_3 - 10.00x_4 - 9.33x_5 - 15.00x_{37} - 3.33x_{10}
x_{24}
                                 +0.00x_8 +1.00x_{38} -1.00x_3 -1.00x_4 -1.00x_5 -0.00x_{37} -0.00x_{10}
                 1.0
x_{23}
           11.2708333333
                                 +0.13x_8 +9.81x_{38} -9.79x_3 -10.69x_4 -11.79x_5 -6.69x_{37} -2.42x_{10}
x_{26}
                                 +0.25x_8 -4.88x_{38} -2.58x_3 -2.88x_4 -4.58x_5 +12.13x_{37} +1.17x_{10}
           4.04166666667
x_{27}
                                 +0.00x_8+13.00x_{38}-9.00x_3-10.00x_4-10.00x_5-13.00x_{37}-3.00x_{10}
                10.0
x_{28}
          8.1666666667
                                 +0.00x_8 +9.50x_{38} -7.33x_3 -8.50x_4 -8.33x_5 -8.50x_{37} -2.33x_{10}
x_{29}
                                 +0.13x_8 +8.81x_{38} -8.46x_3 -9.69x_4 -10.46x_5 -5.69x_{37} -2.08x_{10}
          9.60416666667
x_{30}
               2.4375
                                 +0.12x_8 -0.69x_{38} -2.13x_3 -2.19x_4 -3.13x_5 +3.81x_{37} +0.25x_{10}
x_{31}
                                 +0.25x_8 +7.13x_{38} -10.58x_3 -11.87x_4 -13.58x_5 -0.88x_{37}
           13.0416666667
x_{32}
                                 +0.12x_8 -1.19x_{38} -1.13x_3 -1.69x_4 -2.13x_5 +4.31x_{37} +0.25x_{10}
               1.9375
x_{33}
                                 +0.12x_8 -2.19x_{38} -1.79x_3 -1.69x_4 -2.79x_5 +6.31x_{37} +0.58x_{10}
           2.270833333333
x_{34}
                                 +0.37x_{8} -7.06x_{38} -1.71x_{3} -2.56x_{4} -4.71x_{5} +14.44x_{37} +1.42x_{10}
           2.97916666667
x_{11}
               1.0625
                                 -0.12x_8 +1.19x_{38} -0.87x_3 -0.31x_4 +0.13x_5 -1.31x_{37} -0.25x_{10}
x_6
                                 -0.00x_8 + 1.00x_{38} - 1.00x_3 - 1.00x_4 - 1.00x_5 + 1.00x_{37} + 0.00x_{10}
                 1.0
x_{36}
          0.166666666667
                                 +0.00x_8 +1.50x_{38} -0.33x_3 -0.50x_4 -0.33x_5 -1.50x_{37} -0.33x_{10}
x_{25}
          2.77083333333
                                 +0.12x_8 -2.69x_{38} -1.79x_3 -1.19x_4 -2.79x_5 +7.81x_{37} +0.58x_{10}
x_{39}
                                 +0.12x_8 -2.19x_{38} -2.79x_3 -1.69x_4 -3.79x_5 +8.31x_{37} +0.58x_{10}
          3.27083333333
x_{40}
                                 +0.00x_8 +0.50x_{38} -1.00x_3 -0.50x_4 -1.00x_5 +1.50x_{37} +0.00x_{10}
                 1.5
x_{41}
                                 -0.00x_8 + 1.00x_{38} - 1.00x_3 - 1.00x_4 - 1.00x_5 + 1.00x_{37}
                 1.0
                                                                                                  +0.00x_{10}
x_{42}
                                                      -2.00x_3 -1.00x_4 -2.00x_5
                 2.0
                                 -0.00x_8 -0.00x_{38}
                                                                                      +3.00x_{37}
                                                                                                  +0.00x_{10}
x_{43}
                                 -0.00x_8 -0.50x_{38} -1.67x_3 -0.50x_4 -1.67x_5
                                                                                                  +0.33x_{10}
           1.83333333333
                                                                                      +3.50x_{37}
x_{44}
                 2.0
                                 -0.00x_8 -0.00x_{38} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{10}
x_{45}
                 2.5
                                 -0.00x_8 + 0.50x_{38} -2.00x_3 -1.50x_4 -2.00x_5 +2.50x_{37}
                                                                                                  +0.00x_{10}
x_{46}
x_{47}
           3.77083333333
                                 +0.12x_8 -1.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +7.81x_{37}
                 0.5
                                 -0.00x_8 + 0.50x_{38} + 0.00x_3 -0.50x_4 + 0.00x_5 + 0.50x_{37} + 0.00x_{10}
x_{48}
          3.270833333333
                                 +0.12x_8 -2.19x_{38} -2.79x_3 -1.69x_4 -3.79x_5 +8.31x_{37} +0.58x_{10}
x_{49}
                                 +0.00x_8 +1.00x_{38} +0.00x_3 +0.00x_4 +0.00x_5 -0.00x_{37}
x_{50}
          .12687636999e -
                                                                                                  -0.00x_{10}
                                 +0.12x_8 -2.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +8.81x_{37}
           3.77083333333
x_{51}
                 2.5
                                 -0.00x_8 + 0.50x_{38} -2.00x_3 -1.50x_4 -2.00x_5 +2.50x_{37} +0.00x_{10}
x_{52}
          3.770833333333
                                 +0.12x_8 -2.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +8.81x_{37} +0.58x_{10}
x_{53}
                                 +0.12x_{9} -2.69x_{38} -2.79x_{3} -2.19x_{4} -3.79x_{5} +8.81x_{37} +0.58x_{10}
x_{54}
          3.77083333333
          2.27083333333
                                 +0.12x_8 -2.19x_{38} -1.79x_3 -1.69x_4 -2.79x_5 +7.31x_{37} +0.58x_{10}
x_{55}
                                 -0.00x_8 -0.00x_{38} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{10}
                 2.0
x_{56}
                                 +0.12x_8 -2.19x_{38} -0.79x_3 -0.69x_4 -1.79x_5 +6.31x_{37}
           1.27083333333
                                                                                                  +0.58x_{10}
x_{57}
                                 +0.12x_8 -2.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +8.81x_{37}
          3.77083333333
                                                                                                  +0.58x_{10}
x_{58}
                                 +0.12x_8 -1.69x_{38} -0.79x_3 -1.19x_4 -1.79x_5
           1.77083333333
                                                                                      +5.81x_{37}
                                                                                                  +0.58x_{10}
x_{59}
                                 -0.00x_8 + 0.50x_{38} -2.00x_3 -1.50x_4 -2.00x_5 +2.50x_{37} +0.00x_{10}
                 2.5
x_{60}
                                 +0.12x_8 -1.69x_{38} -2.79x_3 -2.19x_4 -3.79x_5 +7.81x_{37} +0.58x_{10}
          3.770833333333
x_{61}
         -0.2708333333333
                                 +0.88x_8 +0.19x_{38} +0.79x_3 +0.69x_4 +0.79x_5 +0.69x_{37} +0.42x_{10}
x_{62}
         -0.6458333333332
                                 +0.62x_8 +0.06x_{38} +0.04x_3 +0.56x_4 +0.04x_5 +0.56x_{37} +0.92x_{10}
x_{63}
                                 +1.00x_8 +0.50x_{38} +1.00x_3 +0.50x_4 +1.00x_5 +0.50x_{37} +0.00x_{10}
                -0.5
x_{64}
         -0.8333333333333
                                 +0.00x_8 +0.50x_{38} +0.67x_3 +0.50x_4 +0.67x_5 +0.50x_{37} +0.67x_{10}
x_{65}
```

10.17

10.25~

Forming the dual dictionary: The Final Dual Dictionary is:

1 49070E019960

```
0.69387755102
                                  +0.14x_{81} -1.51x_{25} +1.57x_3 +1.41x_4 -0.43x_5 +0.90x_{37} +0.10x_{65}
x_2
                                  -1.86x_{81} + 20.06x_{25} - 19.43x_3 - 10.45x_4 + 11.57x_5 - 4.39x_{37} - 1.61x_{65}
           30.8367346939
x_9
           1.57142857143
                                  -0.00x_{81} +0.29x_{25} +1.00x_3 +0.57x_4 -0.00x_5 -0.14x_{37} +0.14x_{65}
x_7
                                                                    +1.00x_4
                 2.0
                                              -1.00x_{25}
x_1
           38.9795918367
                                  -2.86x_{81} + 28.63x_{25} - 25.43x_3 - 25.31x_4 + 1.57x_5 - 8.67x_{37} - 1.33x_{65}
x_{12}
                                  +0.29x_{81} -2.88x_{25} -2.86x_3 -3.90x_4 -4.86x_5 +6.22x_{37} -0.22x_{65}
           3.67346938776
x_{35}
                                  +0.14x_{81}+10.35x_{25}-2.43x_3-16.88x_4-7.43x_5-3.53x_{37}-1.47x_{65}
           7.40816326531
x_{14}
                                  +0.29x_{81} -0.73x_{25} -5.86x_3 -6.61x_4 -7.86x_5 +5.65x_{37} +0.35x_{65}
           6.95918367347
x_{15}
x_{16}
           5.26530612245
                                  +0.14x_{81} -0.22x_{25}
                                                         -3.43x_3 -4.02x_4 -4.43x_5 +3.76x_{37} +0.24x_{65}
           12.9591836735
                                  +0.29x_{81} +5.27x_{25}
                                                         -8.86x_3 -10.61x_4 -11.86x_5 +4.65x_{37} +0.35x_{65}
x_{17}
                                             +1.00x_{25}
                 1.0
x_{18}
x_{19}
          0.714285714286
                                  -0.00x_{81} -0.14x_{25}
                                                         -1.00x_3 -0.29x_4 -1.00x_5 +0.57x_{37} +0.43x_{65}
           4.24489795918
                                  +0.29x_{81} -3.59x_{25}
                                                         -3.86x_3 -4.33x_4 -5.86x_5 +5.08x_{37} +0.92x_{65}
x_{20}
           2.55102040816
                                                         -1.43x_3 -2.73x_4 -2.43x_5 +2.18x_{37} +0.82x_{65}
                                  +0.14x_{81} -2.08x_{25}
x_{21}
           7.71428571429
                                  +0.00x_{81} +9.86x_{25} -5.00x_3 -5.29x_4 -6.00x_5 -1.43x_{37} -0.57x_{65}
x_{13}
           3.57142857143
                                  -0.00x_{81} + 3.29x_{25} -3.00x_3 -2.43x_4 -3.00x_5 +0.86x_{37} +0.14x_{65}
x_{22}
           7.85714285714
                                  +0.00x_{81} +9.43x_{25} -5.00x_3 -5.14x_4 -6.00x_5 -0.71x_{37} -0.29x_{65}
x_{24}
           1.14285714286
                                  -0.00x_{81} +0.57x_{25} -1.00x_3 -0.86x_4 -1.00x_5 +0.71x_{37} +0.29x_{65}
x_{23}
                                                         -7.43x_3 -7.31x_4 -9.43x_5 +3.33x_{37} -0.33x_{65}
           9.97959183673
                                  +0.14x_{81} +6.63x_{25}
x_{26}
                                                         -3.86x_3 -4.76x_4 -5.86x_5 +6.94x_{37} +0.06x_{65}
           4.81632653061
                                  +0.29x_{81} -3.31x_{25}
x_{27}
                                                         -6.00x_3 -5.57x_4 -7.00x_5 +0.14x_{37} -0.14x_{65}
           8.42857142857
                                  +0.00x_{81} +8.71x_{25}
x_{28}
           6.85714285714
                                                        -5.00x_3 -5.14x_4 -6.00x_5 +1.29x_{37} -0.29x_{65}
                                  -0.00x_{81} +6.43x_{25}
x_{29}
           8.55102040816
                                  +0.14x_{81} +5.92x_{25} -6.43x_3 -6.73x_4 -8.43x_5 +3.18x_{37} -0.18x_{65}
x_{30}
           2.69387755102
                                  +0.14x_{81} -0.51x_{25}
                                                         -2.43x_3 -2.59x_4 -3.43x_5 +2.90x_{37} +0.10x_{65}
x_{31}
                                                         -8.86x_3 -9.47x_4 -11.86x_5 +6.37x_{37} -0.37x_{65}
           12.1020408163
                                  +0.29x_{81} +4.84x_{25}
x_{32}
           2.12244897959
                                                         -1.43x_3 -2.16x_4 -2.43x_5 +3.04x_{37} -0.04x_{65}
                                  +0.14x_{81} -0.80x_{25}
x_{33}
                                                         -2.43x_3 -2.59x_4 -3.43x_5 +3.90x_{37} +0.10x_{65}
           2.69387755102
x_{34}
                                  +0.14x_{81} -1.51x_{25}
                                                         -3.29x_3 -5.06x_4 -6.29x_5 +7.27x_{37} -0.27x_{65}
                                  +0.43x_{81} -4.67x_{25}
x_{11}
           3.79591836735
          0.877551020408
                                  -0.14x_{81} +0.80x_{25}
                                                        -0.57x_3 +0.16x_4 +0.43x_5 -0.04x_{37} +0.04x_{65}
x_6
                                  -0.00x_{81} +0.57x_{25} -1.00x_3 -0.86x_4 -1.00x_5 +1.71x_{37} +0.29x_{65}
           1.14285714286
x_{36}
                                  -0.00x_{81} +0.57x_{25} -0.00x_3 +0.14x_4 -0.00x_5 +0.71x_{37} +0.29x_{65}
          0.142857142857
x_{38}
           3.12244897959
                                  +0.14x_{81} -1.80x_{25} -2.43x_3 -2.16x_4 -3.43x_5 +5.04x_{37} -0.04x_{65}
x_{39}
           3.69387755102
                                  +0.14x_{81} -1.51x_{25} -3.43x_3 -2.59x_4 -4.43x_5 +5.90x_{37} +0.10x_{65}
x_{40}
                                  +0.00x_{81} +0.29x_{25} -1.00x_3 -0.43x_4 -1.00x_5 +1.86x_{37} +0.14x_{65}
           1.57142857143
x_{41}
           1.14285714286
                                                         -1.00x_3 -0.86x_4 -1.00x_5 +1.71x_{37} +0.29x_{65}
                                  -0.00x_{81} +0.57x_{25}
x_{42}
                                                         -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{65}
                                  -0.00x_{81} -0.00x_{25}
x_{43}
                 2.0
                                  -0.00x_{81} -0.43x_{25}
           2.14285714286
                                                         -2.00x_3 -0.86x_4 -2.00x_5 +2.71x_{37} +0.29x_{65}
x_{44}
                 2.0
                                  -0.00x_{81} -0.00x_{25} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{65}
x_{45}
x_{46}
           2.57142857143
                                  -0.00x_{81} +0.29x_{25}
                                                         -2.00x_3 -1.43x_4 -2.00x_5 +2.86x_{37} +0.14x_{65}
           4.26530612245
                                                         -3.43x_3 -3.02x_4 -4.43x_5 +5.76x_{37} +0.24x_{65}
x_{47}
                                  +0.14x_{81} -1.22x_{25}
          0.571428571429
                                                         -0.00x_3 -0.43x_4 -0.00x_5 +0.86x_{37} +0.14x_{65}
                                  -0.00x_{81} +0.29x_{25}
x_{48}
                                                         -3.43x_3 -2.59x_4 -4.43x_5 +5.90x_{37} +0.10x_{65}
           3.69387755102
                                  +0.14x_{81} -1.51x_{25}
x_{49}
          0.142857142857
                                  -0.00x_{81} +0.57x_{25}
                                                         -0.00x_3 +0.14x_4 -0.00x_5 +0.71x_{37} +0.29x_{65}
x_{50}
                                                         -3.43x_3 -3.16x_4 -4.43x_5 +6.04x_{37} -0.04x_{65}
           4.12244897959
x_{51}
                                  +0.14x_{81} -1.80x_{25}
           2.57142857143
                                  -0.00x_{81} +0.29x_{25} -2.00x_3 -1.43x_4 -2.00x_5 +2.86x_{37} +0.14x_{65}
x_{52}
                                  +0.14x_{81} -1.80x_{25} -3.43x_3 -3.16x_4 -4.43x_5 +6.04x_{37} -0.04x_{65}
           4.12244897959
x_{53}
x_{54}
           4.12244897959
                                  +0.14x_{61} -1.80x_{25} -3.43x_{3} -3.16x_{4} -4.43x_{5} +6.04x_{37} -0.04x_{65}
           2.69387755102
                                  +0.14x_{81} -1.51x_{25} -2.43x_3 -2.59x_4 -3.43x_5 +4.90x_{37} +0.10x_{65}
x_{55}
                                  -0.00x_{81} -0.00x_{25} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{65}
                 2.0
x_{56}
                                  +0.14x_{81} -1.51x_{25} -1.43x_3 -1.59x_4 -2.43x_5 +3.90x_{37} +0.10x_{65}
           1.69387755102
x_{57}
                                  +0.14x_{81} -1.80x_{25}
                                                         -3.43x_3 -3.16x_4 -4.43x_5 +6.04x_{37} -0.04x_{65}
           4.12244897959
x_{58}
           2.26530612245
                                  +0.14x_{81} -1.22x_{25}
                                                         -1.43x_3 -2.02x_4 -2.43x_5 +3.76x_{37} +0.24x_{65}
x_{59}
           2.57142857143
                                  -0.00x_{81} +0.29x_{25}
                                                        -2.00x_3 -1.43x_4 -2.00x_5 +2.86x_{37} +0.14x_{65}
x_{60}
                                  +0.14x_{81} -1.22x_{25} -3.43x_3 -3.02x_4 -4.43x_5 +5.76x_{37} +0.24x_{65}
x_{61}
           4.26530612245
          0.755102040817
                                  +0.71x_{81} -0.41x_{25} -1.14x_3 -0.67x_4 -1.14x_5 -1.08x_{37} +1.08x_{65}
x_{63}
          0.714285714285
                                  +1.00x_{81} -0.14x_{25} +0.00x_3 -0.29x_4 +0.00x_5 -0.43x_{37} +0.43x_{65}
x_{62}
                                  +1.14x_{81} -0.08x_{25} -0.43x_3 -0.73x_4 -0.43x_5 -0.82x_{37} -0.18x_{65}
          0.551020408163
x_8
                                  -0.00x_{81} \ -0.43x_{25} \ -1.00x_3 \ -0.86x_4 \ -1.00x_5 \ -1.29x_{37} +1.29x_{65}
           1.14285714286
x_{10}
```

0.71 ~

0.65~

0.71  $\infty$ 

1 49070E019960

```
0.69387755102
                                  +0.14x_{81} -1.51x_{25} +1.57x_3 +1.41x_4 -0.43x_5 +0.90x_{37} +0.10x_{65}
x_2
                                  -1.86x_{81} + 20.06x_{25} - 19.43x_3 - 10.45x_4 + 11.57x_5 - 4.39x_{37} - 1.61x_{65}
           30.8367346939
x_9
           1.57142857143
                                  -0.00x_{81} +0.29x_{25} +1.00x_3 +0.57x_4 -0.00x_5 -0.14x_{37} +0.14x_{65}
x_7
                                                                    +1.00x_4
                 2.0
                                              -1.00x_{25}
x_1
x_{12}
           38.9795918367
                                  -2.86x_{81} + 28.63x_{25} - 25.43x_3 - 25.31x_4 + 1.57x_5 - 8.67x_{37} - 1.33x_{65}
                                  +0.29x_{81} -2.88x_{25} -2.86x_3 -3.90x_4 -4.86x_5 +6.22x_{37} -0.22x_{65}
           3.67346938776
x_{35}
                                  +0.14x_{81}+10.35x_{25}-2.43x_3-16.88x_4-7.43x_5-3.53x_{37}-1.47x_{65}
           7.40816326531
x_{14}
                                  +0.29x_{81} -0.73x_{25} -5.86x_3 -6.61x_4 -7.86x_5 +5.65x_{37} +0.35x_{65}
           6.95918367347
x_{15}
x_{16}
           5.26530612245
                                  +0.14x_{81} -0.22x_{25}
                                                         -3.43x_3 -4.02x_4 -4.43x_5 +3.76x_{37} +0.24x_{65}
           12.9591836735
                                  +0.29x_{81} +5.27x_{25}
                                                         -8.86x_3 -10.61x_4 -11.86x_5 +4.65x_{37} +0.35x_{65}
x_{17}
                                             +1.00x_{25}
                 1.0
x_{18}
x_{19}
          0.714285714286
                                  -0.00x_{81} -0.14x_{25}
                                                         -1.00x_3 -0.29x_4 -1.00x_5 +0.57x_{37} +0.43x_{65}
           4.24489795918
                                  +0.29x_{81} -3.59x_{25}
                                                         -3.86x_3 -4.33x_4 -5.86x_5 +5.08x_{37} +0.92x_{65}
x_{20}
           2.55102040816
                                  +0.14x_{81} -2.08x_{25}
                                                         -1.43x_3 -2.73x_4 -2.43x_5 +2.18x_{37} +0.82x_{65}
x_{21}
           7.71428571429
                                  +0.00x_{81} +9.86x_{25} -5.00x_3 -5.29x_4 -6.00x_5 -1.43x_{37} -0.57x_{65}
x_{13}
           3.57142857143
                                  -0.00x_{81} + 3.29x_{25} -3.00x_3 -2.43x_4 -3.00x_5 +0.86x_{37} +0.14x_{65}
x_{22}
           7.85714285714
                                  +0.00x_{81} +9.43x_{25} -5.00x_3 -5.14x_4 -6.00x_5 -0.71x_{37} -0.29x_{65}
x_{24}
           1.14285714286
                                  -0.00x_{81} +0.57x_{25} -1.00x_3 -0.86x_4 -1.00x_5 +0.71x_{37} +0.29x_{65}
x_{23}
                                                         -7.43x_3 -7.31x_4 -9.43x_5 +3.33x_{37} -0.33x_{65}
           9.97959183673
                                  +0.14x_{81} +6.63x_{25}
x_{26}
                                                         -3.86x_3 -4.76x_4 -5.86x_5 +6.94x_{37} +0.06x_{65}
           4.81632653061
                                  +0.29x_{81} -3.31x_{25}
x_{27}
                                                         -6.00x_3 -5.57x_4 -7.00x_5 +0.14x_{37} -0.14x_{65}
           8.42857142857
                                  +0.00x_{81} +8.71x_{25}
x_{28}
           6.85714285714
                                                        -5.00x_3 -5.14x_4 -6.00x_5 +1.29x_{37} -0.29x_{65}
                                  -0.00x_{81} +6.43x_{25}
x_{29}
           8.55102040816
                                  +0.14x_{81} +5.92x_{25} -6.43x_3 -6.73x_4 -8.43x_5 +3.18x_{37} -0.18x_{65}
x_{30}
           2.69387755102
                                  +0.14x_{81} -0.51x_{25}
                                                         -2.43x_3 -2.59x_4 -3.43x_5 +2.90x_{37} +0.10x_{65}
x_{31}
                                                         -8.86x_3 -9.47x_4 -11.86x_5 + 6.37x_{37} - 0.37x_{65}
           12.1020408163
                                  +0.29x_{81} +4.84x_{25}
x_{32}
           2.12244897959
                                                         -1.43x_3 -2.16x_4 -2.43x_5 +3.04x_{37} -0.04x_{65}
                                  +0.14x_{81} -0.80x_{25}
x_{33}
                                                         -2.43x_3 -2.59x_4 -3.43x_5 +3.90x_{37} +0.10x_{65}
           2.69387755102
                                  +0.14x_{81} -1.51x_{25}
x_{34}
                                                         -3.29x_3 -5.06x_4 -6.29x_5 +7.27x_{37} -0.27x_{65}
                                  +0.43x_{81} -4.67x_{25}
x_{11}
           3.79591836735
          0.877551020408
                                  -0.14x_{81} +0.80x_{25}
                                                        -0.57x_3 +0.16x_4 +0.43x_5 -0.04x_{37} +0.04x_{65}
x_6
                                  -0.00x_{81} +0.57x_{25} -1.00x_3 -0.86x_4 -1.00x_5 +1.71x_{37} +0.29x_{65}
           1.14285714286
x_{36}
                                  -0.00x_{81} +0.57x_{25} -0.00x_3 +0.14x_4 -0.00x_5 +0.71x_{37} +0.29x_{65}
          0.142857142857
x_{38}
           3.12244897959
                                  +0.14x_{81} -1.80x_{25} -2.43x_3 -2.16x_4 -3.43x_5 +5.04x_{37} -0.04x_{65}
x_{39}
           3.69387755102
                                  +0.14x_{81} -1.51x_{25} -3.43x_3 -2.59x_4 -4.43x_5 +5.90x_{37} +0.10x_{65}
x_{40}
                                  +0.00x_{81} +0.29x_{25} -1.00x_3 -0.43x_4 -1.00x_5 +1.86x_{37} +0.14x_{65}
           1.57142857143
x_{41}
           1.14285714286
                                                         -1.00x_3 -0.86x_4 -1.00x_5 +1.71x_{37} +0.29x_{65}
                                  -0.00x_{81} +0.57x_{25}
x_{42}
                                                         -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{65}
                                  -0.00x_{81} -0.00x_{25}
x_{43}
                 2.0
                                  -0.00x_{81} -0.43x_{25}
           2.14285714286
                                                         -2.00x_3 -0.86x_4 -2.00x_5 +2.71x_{37} +0.29x_{65}
x_{44}
                 2.0
                                                        -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{65}
x_{45}
                                  -0.00x_{81} -0.00x_{25}
           2.57142857143
                                  -0.00x_{81} +0.29x_{25}
                                                         -2.00x_3 -1.43x_4 -2.00x_5 +2.86x_{37} +0.14x_{65}
x_{46}
           4.26530612245
                                                         -3.43x_3 -3.02x_4 -4.43x_5 +5.76x_{37} +0.24x_{65}
                                  +0.14x_{81} -1.22x_{25}
x_{47}
          0.571428571429
                                                         -0.00x_3 -0.43x_4 -0.00x_5 +0.86x_{37} +0.14x_{65}
                                  -0.00x_{81} +0.29x_{25}
x_{48}
                                                         -3.43x_3 -2.59x_4 -4.43x_5 +5.90x_{37} +0.10x_{65}
           3.69387755102
                                  +0.14x_{81} -1.51x_{25}
x_{49}
          0.142857142857
                                  -0.00x_{81} +0.57x_{25}
                                                         -0.00x_3 +0.14x_4 -0.00x_5 +0.71x_{37} +0.29x_{65}
x_{50}
                                                         -3.43x_3 -3.16x_4 -4.43x_5 +6.04x_{37} -0.04x_{65}
           4.12244897959
x_{51}
                                  +0.14x_{81} -1.80x_{25}
           2.57142857143
                                  -0.00x_{81} +0.29x_{25} -2.00x_3 -1.43x_4 -2.00x_5 +2.86x_{37} +0.14x_{65}
x_{52}
                                  +0.14x_{81} -1.80x_{25} -3.43x_3 -3.16x_4 -4.43x_5 +6.04x_{37} -0.04x_{65}
           4.12244897959
x_{53}
x_{54}
           4.12244897959
                                  +0.14x_{21} -1.80x_{25} -3.43x_{3} -3.16x_{4} -4.43x_{5} +6.04x_{37} -0.04x_{65}
           2.69387755102
                                  +0.14x_{81} -1.51x_{25} -2.43x_3 -2.59x_4 -3.43x_5 +4.90x_{37} +0.10x_{65}
x_{55}
                                  -0.00x_{81} -0.00x_{25} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{65}
                 2.0
x_{56}
                                  +0.14x_{81} -1.51x_{25} -1.43x_3 -1.59x_4 -2.43x_5 +3.90x_{37}+0.10x_{65}
           1.69387755102
x_{57}
                                  +0.14x_{81} -1.80x_{25}
                                                         -3.43x_3 -3.16x_4 -4.43x_5 +6.04x_{37} -0.04x_{65}
           4.12244897959
x_{58}
           2.26530612245
                                  +0.14x_{81} -1.22x_{25}
                                                         -1.43x_3 -2.02x_4 -2.43x_5 +3.76x_{37} +0.24x_{65}
x_{59}
           2.57142857143
                                  -0.00x_{81} +0.29x_{25}
                                                        -2.00x_3 -1.43x_4 -2.00x_5 +2.86x_{37} +0.14x_{65}
x_{60}
                                  +0.14x_{81} -1.22x_{25} -3.43x_3 -3.02x_4 -4.43x_5 +5.76x_{37} +0.24x_{65}
x_{61}
           4.26530612245
          0.755102040817
                                  +0.71x_{81} -0.41x_{25} -1.14x_3 -0.67x_4 -1.14x_5 -1.08x_{37} +1.08x_{65}
x_{63}
          0.714285714285
                                  +1.00x_{81} -0.14x_{25} +0.00x_3 -0.29x_4 +0.00x_5 -0.43x_{37} +0.43x_{65}
x_{62}
                                  +1.14x_{81} -0.08x_{25} -0.43x_3 -0.73x_4 -0.43x_5 -0.82x_{37} -0.18x_{65}
          0.551020408163
x_8
                                  -0.00x_{81} \ -0.43x_{25} \ -1.00x_3 \ -0.86x_4 \ -1.00x_5 \ -1.29x_{37} +1.29x_{65}
           1.14285714286
x_{10}
```

0.71 ~

0.65~

0.71  $\infty$ 

Forming the dual dictionary: The Final Dual Dictionary is:

2.0

 $x_{10}$ 

```
5.0
                                   +7.00x_2 +21.50x_{126} -11.00x_3 -9.50x_4 +3.00x_5 -16.50x_{37} -12.00x_{116}
x_{81}
                 40.0
                                   -13.00x_2 +1.00x_{126} +1.00x_3 +8.00x_4 +6.00x_5 +7.00x_{37} -1.00x_{116}
x_9
                                   -0.00x_2 \ +0.50x_{126} \ +1.00x_3 \ +0.50x_4 \ -0.00x_5 \ -0.50x_{37} \ +0.00x_{116}
                  2.0
x_7
                                   -0.00x_2 \quad -2.00x_{126} \quad -0.00x_3 \quad +1.00x_4 \quad -0.00x_5 \quad +1.00x_{37} \quad +1.00x_{116}
                  1.0
x_1
                 52.0
                                   -20.00x_2 -3.50x_{126} +6.00x_3 +2.50x_4 -7.00x_5 +10.50x_{37} +3.00x_{116}
x_{12}
                  2.0
                                   +2.00x_2 +0.50x_{126} -6.00x_3 -6.50x_4 -4.00x_5 +4.50x_{37} -1.00x_{116}
x_{35}
                                   +6.00x_2 +19.00x_{126} -9.00x_3 -8.00x_4 +3.00x_5 -14.00x_{37} -10.00x_{116}
                  4.0
x_{110}
                  8.0
                                   +2.00x_2 +4.50x_{126} -9.00x_3 -9.50x_4 -7.00x_5 +1.50x_{37} -2.00x_{116}
x_{15}
x_{16}
                  6.0
                                   +1.00x_2 +2.50x_{126} -5.00x_3 -5.50x_4 -4.00x_5 +1.50x_{37} -1.00x_{116}
                 20.0
                                   +2.00x_2 +16.50x_{126} -12.00x_3 -13.50x_4 -11.00x_5 -5.50x_{37} -8.00x_{116}
x_{17}
                                   +0.00x_2 +2.00x_{126} +0.00x_3 -0.00x_4 +0.00x_5 -1.00x_{37} -1.00x_{116}
                  2.0
x_{18}
                                   -0.00x_2 \quad -0.50x_{126} \quad -1.00x_3 \quad -0.50x_4 \quad -1.00x_5 \quad +0.50x_{37} \quad +1.00x_{116}
x_{19}
                  1.0
                  3.0
                                   +2.00x_2 -1.50x_{126} -7.00x_3 -7.50x_4 -5.00x_5 +3.50x_{37} +2.00x_{116}
x_{20}
                  2.0
                                   +1.00x_2 -1.50x_{126} -3.00x_3 -4.50x_4 -2.00x_5 +1.50x_{37} +2.00x_{116}
x_{21}
                                   -0.00x_2 +1.00x_{126} -0.00x_3 -0.00x_4 -0.00x_5 -1.00x_{37} +1.00x_{116}
                  1.0
x_{109}
                  7.0
                                   -0.00x_2 +6.50x_{126} -3.00x_3 -2.50x_4 -3.00x_5 -2.50x_{37} -3.00x_{116}
x_{22}
                                   +0.00x_2 +19.00x_{126} -5.00x_3 -5.00x_4 -6.00x_5 -10.00x_{37} -10.00x_{116}
                 17.0
x_{24}
                  2.0
                                   -0.00x_2 +1.00x_{126} -1.00x_3 -1.00x_4 -1.00x_5 +0.00x_{37} +0.00x_{116}
x_{23}
                                   +1.00x_2 +16.50x_{126} -9.00x_3 -8.50x_4 -9.00x_5 -5.50x_{37} -9.00x_{116}
                 17.0
x_{26}
                  3.0
                                   +2.00x_2 -0.50x_{126} -7.00x_3 -7.50x_4 -5.00x_5 +5.50x_{37} +0.00x_{116}
x_{27}
                                   +0.00x_2 +17.50x_{126} -6.00x_3 -5.50x_4 -7.00x_5 -8.50x_{37} -9.00x_{116}
                 17.0
x_{28}
                 13.0
                                   +0.00x_2 +13.00x_{126} -5.00x_3 -5.00x_4 -6.00x_5 -5.00x_{37} -7.00x_{116}
x_{29}
                 15.0
                                   +1.00x_2 +15.00x_{126} -8.00x_3 -8.00x_4 -8.00x_5 -5.00x_{37} -8.00x_{116}
x_{30}
                  3.0
                                   +1.00x_2 +2.00x_{126} -4.00x_3 -4.00x_4 -3.00x_5 +1.00x_{37} -1.00x_{116}
x_{31}
                 18.0
                                   +2.00x_2 +16.00x_{126} -12.00x_3 -12.00x_4 -11.00x_5 -3.00x_{37} -9.00x_{116}
x_{32}
                                   +1.00x_2 \ +1.50x_{126} \ -3.00x_3 \ -3.50x_4 \ -2.00x_5 \ +1.50x_{37} \ -1.00x_{116}
                  2.0
x_{33}
                 2.0
                                   +1.00x_2 -0.00x_{126} -4.00x_3 -4.00x_4 -3.00x_5 +3.00x_{37} +0.00x_{116}
x_{34}
x_{11}
                  1.0
                                   +3.00x_2 -0.00x_{126} -8.00x_3 -9.00x_4 -5.00x_5 +5.00x_{37} -1.00x_{116}
                 17.0
                                   +0.00x_2 +20.00x_{126} -5.00x_3 -5.00x_4 -6.00x_5 -11.00x_{37} -11.00x_{116}
x_{13}
                                   -0.00x_2 +1.00x_{126} -1.00x_3 -1.00x_4 -1.00x_5 +1.00x_{37} +0.00x_{116}
                  2.0
x_{36}
                                   -0.00x_2 +1.00x_{126} -0.00x_3 -0.00x_4 -0.00x_5 +0.00x_{37} +0.00x_{116}
                  1.0
x_{38}
                  2.0
                                   +1.00x_2 -0.50x_{126} -4.00x_3 -3.50x_4 -3.00x_5 +4.50x_{37} +0.00x_{116}
x_{39}
                  3.0
                                   +1.00x_2 -0.00x_{126} -5.00x_3 -4.00x_4 -4.00x_5 +5.00x_{37} +0.00x_{116}
x_{40}
                                   +0.00x_2 +0.50x_{126} -1.00x_3 -0.50x_4 -1.00x_5 +1.50x_{37} +0.00x_{116}
                  2.0
x_{41}
                                   -0.00x_2 \ +1.00x_{126} \ -1.00x_3 \ -1.00x_4 \ -1.00x_5 \ +1.00x_{37} \ +0.00x_{116}
                  2.0
x_{42}
                                   -0.00x_2 \ \ -0.00x_{126} \ \ -2.00x_3 \ \ -1.00x_4 \ \ -2.00x_5 \ \ +3.00x_{37} \ \ +0.00x_{116}
                  2.0
x_{43}
                  2.0
                                   -0.00x_2 -1.00x_{126} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +1.00x_{116}
x_{44}
                  2.0
                                   -0.00x_2 -0.00x_{126} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{116}
x_{45}
                                   -0.00x_2 \ +0.50x_{126} \ -2.00x_3 \ -1.50x_4 \ -2.00x_5 \ +2.50x_{37} \ +0.00x_{116}
x_{46}
                  3.0
                  4.0
                                   +1.00x_2 +0.50x_{126} -5.00x_3 -4.50x_4 -4.00x_5 +4.50x_{37} +0.00x_{116}
x_{47}
                  1.0
                                   -0.00x_2 +0.50x_{126} -0.00x_3 -0.50x_4 -0.00x_5 +0.50x_{37} +0.00x_{116}
x_{48}
                                   +1.00x_2 -0.00x_{126} -5.00x_3 -4.00x_4 -4.00x_5 +5.00x_{37} +0.00x_{116}
                  3.0
x_{49}
                                   -0.00x_2 +1.00x_{126} -0.00x_3 -0.00x_4 -0.00x_5 +0.00x_{37}
                  1.0
x_{50}
                                                                                                        +0.00x_{116}
                  3.0
                                   +1.00x_2 -0.50x_{126} -5.00x_3 -4.50x_4 -4.00x_5 +5.50x_{37} +0.00x_{116}
x_{51}
                                   -0.00x_2 \ +0.50x_{126} \ -2.00x_3 \ -1.50x_4 \ -2.00x_5 \ +2.50x_{37} \ +0.00x_{116}
                  3.0
x_{52}
                                   +1.00x_2 -0.50x_{126} -5.00x_3 -4.50x_4 -4.00x_5 +5.50x_{37} +0.00x_{116}
                  3.0
x_{53}
x_{54}
                  3.0
                                   +1.00 x_{126} -0.50x_{126} -5.00x_{3} -4.50x_{4} -4.00x_{5} +5.50x_{37} +0.00x_{116}
                                   +1.00x_2 -0.00x_{126} -4.00x_3 -4.00x_4 -3.00x_5 +4.00x_{37} +0.00x_{116}
                  2.0
x_{55}
                  2.0
                                   -0.00x_2 -0.00x_{126} -2.00x_3 -1.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{116}
x_{56}
                                   +1.00x_2 -0.00x_{126} -3.00x_3 -3.00x_4 -2.00x_5 +3.00x_{37} +0.00x_{116}
                  1.0
x_{57}
                                   +1.00x_2 \quad -0.50x_{126} \quad -5.00x_3 \quad -4.50x_4 \quad -4.00x_5 \quad +5.50x_{37}
                  3.0
                                                                                                        +0.00x_{116}
x_{58}
                  2.0
                                   +1.00x_2 +0.50x_{126} -3.00x_3 -3.50x_4 -2.00x_5 +2.50x_{37} +0.00x_{116}
x_{59}
                  3.0
                                   -0.00x_2 \ +0.50x_{126} \ -2.00x_3 \ -1.50x_4 \ -2.00x_5 \ +2.50x_{37} \ +0.00x_{116}
x_{60}
                  4.0
                                   +1.00x_2 +0.50x_{126} -5.00x_3 -4.50x_4 -4.00x_5 +4.50x_{37} +0.00x_{116}
x_{61}
                  5.0
                                   +5.00x_2 +14.00x_{126} -9.00x_3 -8.00x_4 +1.00x_5 -13.00x_{37} -6.00x_{116}
x_{63}
                  6.0
                                   +7.00x_2 +21.00x_{126} -11.00x_3 -10.00x_4 +3.00x_5 -17.00x_{37} -11.00x_{116}
x_{62}
                                   +1.00x_2 +24.50x_{126} -4.00x_3 -17.50x_4 -7.00x_5 -15.50x_{37} -15.00x_{116}
                 17.0
x_{14}
```

 $-0.00x_2$   $-1.50x_{126}$   $-1.00x_3$   $-1.50x_4$   $-1.00x_5$   $-1.50x_{37}$   $+3.00x_{116}$ 

6 500

L 1 00 m

7.00~

Final answer: -12.000000 Done. Added 183 cuts