Initial Dictionary

0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to:

$$\max \sum_{i=1}^{5} -x_{i}$$

Primal variable x_j corresponds to dual variable y_j for j = 1, ..., 12 Dual Dictionary (with objective changed is):

Initialization succeeded in finding final dual dictionary with 3 pivots

```
0.0149253731343
                         +0.06y_3 +0.12y_7 -0.07y_1 +1.04y_9 +0.22y_{10} +0.99y_{11} +0.46y_{12}
y_8
     0.567164179104
                         +0.27y_3 +4.54y_7 +0.16y_1 +0.70y_9 +5.51y_{10} -4.57y_{11} -4.42y_{12}
y_2
     0.223880597015
                         -0.10y_3 -1.21y_7 -0.12y_1 +0.67y_9 +1.36y_{10} -0.22y_{11} -1.06y_{12}
y_6
     0.223880597015
                         +0.90y_3 +5.79y_7 -0.12y_1 +8.67y_9 -5.64y_{10} +1.78y_{11} +14.94y_{12}
y_4
      1.19402985075
                         -0.22y_3 -8.45y_7 +0.03y_1 +0.58y_9 -5.09y_{10} -0.19y_{11} -5.99y_{12}
y_5
                         -1.63y_3 - 11.25y_7 - 1.72y_1 - 22.97y_9 - 17.85y_{10} - 4.34y_{11} - 3.36y_{12}
      3.34328358209
```

Primal Dictionary is:

```
1.62686567164
                          -0.06x_8 - 0.27x_2 + 0.10x_6 - 0.90x_4 + 0.22x_5
x_3
      11.2537313433
x_7
                          -0.12x_8 - 4.54x_2 + 1.21x_6 - 5.79x_4 + 8.45x_5
      1.71641791045
                          +0.07x_8 -0.16x_2 +0.12x_6 +0.12x_4 -0.03x_5
x_1
      22.9701492537
                          -1.04x_8 - 0.70x_2 - 0.67x_6 - 8.67x_4 - 0.58x_5
x_9
                          -0.22x_8 - 5.51x_2 - 1.36x_6 + 5.64x_4 + 5.09x_5
      17.8507462687
x_{10}
                          -0.99x_8 + 4.57x_2 + 0.22x_6 -1.78x_4 +0.19x_5
      4.34328358209
x_{11}
      3.35820895522
                          -0.46x_8 + 4.42x_2 + 1.06x_6 - 14.94x_4 + 5.99x_5
x_{12}
      -3.34328358209
                          -0.01x_8 - 0.57x_2 - 0.22x_6 - 0.22x_4 - 1.19x_5
```

Primal Dictionary with original objective is:

```
1.62686567164
                        -0.06x_8 - 0.27x_2 + 0.10x_6 - 0.90x_4 + 0.22x_5
     11.2537313433
                        -0.12x_8 - 4.54x_2 + 1.21x_6 - 5.79x_4 + 8.45x_5
x_7
                        +0.07x_8 -0.16x_2 +0.12x_6 +0.12x_4 -0.03x_5
     1.71641791045
x_1
                        -1.04x_8 - 0.70x_2 - 0.67x_6 - 8.67x_4 - 0.58x_5
     22.9701492537
x_9
                        -0.22x_8 -5.51x_2 -1.36x_6 +5.64x_4 +5.09x_5
x_{10}
     17.8507462687
     4.34328358209
                        -0.99x_8 + 4.57x_2 + 0.22x_6 -1.78x_4 + 0.19x_5
x_{11}
     3.35820895522
                        -0.46x_8 + 4.42x_2 + 1.06x_6 - 14.94x_4 + 5.99x_5
x_{12}
                        +0.61x_8 - 1.75x_2 + 0.18x_6 + 1.18x_4 + 2.96x_5
     2.07462686567
 z
```

 x_4 enters and x_{12} leaves

```
1.42557442557
                          -0.03x_8 - 0.53x_2 + 0.04x_6 + 0.06x_{12} - 0.13x_5
x_3
                          +0.06x_8 -6.25x_2 +0.80x_6 +0.39x_{12} +6.13x_5
       9.95204795205
x_7
x_1
       1.74325674326
                          +0.07x_8 -0.13x_2 +0.13x_6 -0.01x_{12} +0.02x_5
       21.020979021
                          -0.78x_8 -3.27x_2 -1.29x_6 +0.58x_{12} -4.06x_5
x_9
                          -0.40x_8 -3.84x_2 -0.96x_6 -0.38x_{12} +7.35x_5
       19.1188811189
x_{10}
                          -0.93x_8 + 4.04x_2 + 0.10x_6 + 0.12x_{12} - 0.52x_5
       3.94405594406
x_{11}
      0.224775224775
                          -0.03x_8 + 0.30x_2 + 0.07x_6 - 0.07x_{12} + 0.40x_5
x_4
      2.33966033966
                          +0.58x_8 - 1.40x_2 + 0.26x_6 - 0.08x_{12} + 3.43x_5
```

 x_5 enters and x_9 leaves

```
x_3
     0.726600985222
                         -0.01x_8 -0.42x_2 +0.08x_6 +0.04x_{12} +0.03x_9
      41.7113300493
                         -1.11x_8 - 11.18x_2 - 1.15x_6 + 1.26x_{12} - 1.51x_9
x_7
      1.83645320197
                         +0.07x_8 -0.14x_2 +0.12x_6 -0.01x_{12} -0.00x_9
x_1
x_5
      5.18275862069
                         -0.19x_8 -0.81x_2 -0.32x_6 + 0.14x_{12} - 0.25x_9
      57.2103448276
                         -1.81x_8 -9.76x_2 -3.29x_6+0.67x_{12}-1.81x_9
x_{10}
                         -0.83x_8 +4.46x_2 +0.26x_6 +0.04x_{12} +0.13x_9
      1.26206896552
x_{11}
                         -0.11x_8 -0.03x_2 -0.06x_6 -0.01x_{12} -0.10x_9
      2.30098522167
x_4
      20.1039408867
                         -0.08x_8 -4.16x_2 -0.82x_6 + 0.41x_{12} - 0.85x_9
```

 x_{12} enters and x_4 leaves

```
10.4615384615
                        -0.46x_8 -0.54x_2 -0.15x_6 -4.23x_4 -0.38x_9
x_3
                       -15.28x_8 - 14.72x_2 - 8.54x_6 - 131.64x_4 - 14.51x_9
      344.615384615
x_7
                        +0.13x_8 -0.13x_2 +0.15x_6 +0.56x_4 +0.05x_9
     0.538461538462
x_1
                        -1.79x_8 -1.21x_2 -1.15x_6 -14.90x_4 -1.72x_9
      39.4615384615
x_5
                        -9.36x_8 -11.64x_2 -7.23x_6 -70.18x_4 -8.74x_9
x_{10}
      218.692307692
           12.0
                        -1.33x_8 +4.33x_2 +0.00x_6 -4.67x_4
x_{11}
                        -11.21x_8 -2.79x_2 -5.85x_6 -104.10x_4 -10.28x_9
      239.538461538
x_{12}
      118.692307692
                        -4.69x_8 -5.31x_2 -3.23x_6 -42.85x_4 -5.08x_9
```

Final Dictionary Final dictionary after first LP relaxation solve:

```
x_3
      10.4615384615
                        -0.46x_8 -0.54x_2 -0.15x_6 -4.23x_4
     344.615384615
                        -15.28x_8 - 14.72x_2 - 8.54x_6 - 131.64x_4 - 14.51x_9
x_7
     0.538461538462
                        +0.13x_8 -0.13x_2 +0.15x_6 +0.56x_4 +0.05x_9
x_1
                        -1.79x_8 -1.21x_2 -1.15x_6 -14.90x_4 -1.72x_9
     39.4615384615
x_5
      218.692307692
                        -9.36x_8 -11.64x_2 -7.23x_6 -70.18x_4 -8.74x_9
x_{10}
           12.0
                        -1.33x_8 +4.33x_2 +0.00x_6 -4.67x_4
                                                               -0.33x_9
x_{11}
      239.538461538
                        -11.21x_8 -2.79x_2 -5.85x_6 -104.10x_4 -10.28x_9
x_{12}
                        -4.69x_8 -5.31x_2 -3.23x_6 -42.85x_4 -5.08x_9
      118.692307692
```

```
10.4615384615
                          -0.46x_8 -0.54x_2 -0.15x_6 -4.23x_4 -0.38x_9
x_3
       344.615384615
                          -15.28x_8 - 14.72x_2 - 8.54x_6 - 131.64x_4 - 14.51x_9
x_7
                          +0.13x_8 -0.13x_2 +0.15x_6 +0.56x_4 +0.05x_9
      0.538461538462
x_1
       39.4615384615
                          -1.79x_8 -1.21x_2 -1.15x_6 -14.90x_4
x_5
       218.692307692
                          -9.36x_8 -11.64x_2 -7.23x_6 -70.18x_4
                                                                  -8.74x_9
x_{10}
                          -1.33x_8 +4.33x_2 +0.00x_6 -4.67x_4
                                                                  -0.33x_9
            12.0
x_{11}
       239.538461538
                          -11.21x_8 -2.79x_2 -5.85x_6 -104.10x_4 -10.28x_9
x_{12}
     -0.461538461538
                          +0.46x_8 +0.54x_2 +0.15x_6 +0.23x_4
x_{13}
     -0.615384615384
                          +0.28x_8 +0.72x_2 +0.54x_6 +0.64x_4
                                                                  +0.51x_9
x_{14}
     -0.538461538462
                          +0.87x_8 +0.13x_2 +0.85x_6 +0.44x_4
                                                                  +0.95x_9
x_{15}
     -0.461538461538
                          +0.79x_8 +0.21x_2 +0.15x_6 +0.90x_4
                                                                  +0.72x_9
x_{16}
      -0.692307692307
                          +0.36x_8 +0.64x_2 +0.23x_6 +0.18x_4
                                                                  +0.74x_9
x_{17}
     -0.538461538461
                          +0.21x_8 +0.79x_2 +0.85x_6 +0.10x_4
                                                                  +0.28x_9
x_{18}
       118.692307692
                          -4.69x_8 -5.31x_2 -3.23x_6 -42.85x_4
```

Forming the dual dictionary:

The Final Dual Dictionary is:

```
-4.00x_4
                 10.0
                                               -1.00x_{13}
x_3
                330.0
                                   -4.00x_{15} - 22.00x_{13} - 3.00x_{14} - 122.00x_4 - 1.00x_{16}
x_7
                 0.5
                                   +0.50x_{15} +0.50x_{13} -0.50x_{14} +1.00x_{4} -0.50x_{16}
x_1
                 38.0
                                   -1.00x_{15} -2.00x_{13} -0.00x_{14} -14.00x_4 -0.00x_{16}
x_5
                208.5
                                   -5.50x_{15} - 22.50x_{13} - 0.50x_{14} - 69.00x_4 + 7.50x_{16}
x_{10}
                                   -4.00x_{15} +1.00x_{13} +6.00x_{14} -7.00x_{4} +0.00x_{16}
x_{11}
                 14.0
x_{12}
                233.0
                                   -7.00x_{15} -6.00x_{13} +3.00x_{14} -98.00x_4 -4.00x_{16}
                 0.5
                                   -0.50x_{15} +1.50x_{13} +0.50x_{14} +0.00x_{4} -0.50x_{16}
x_2
       4.87554441264e - 13
                                   +2.00x_{15} +2.00x_{13} -1.00x_{14} +2.00x_{4} -3.00x_{16}
x_6
       1.51517687286e - 12
                                   +2.00x_{15} +6.00x_{13} -4.00x_{14} +3.00x_{4} -3.00x_{16}
x_8
          0.499999999998
                                   -2.50x_{15} -7.50x_{13} +4.50x_{14} -5.00x_4 +5.50x_{16}
x_9
       -5.60662627436e - 13
                                   -1.00x_{15} -2.00x_{13} +2.00x_{14} -2.00x_4 +2.00x_{16}
x_{17}
       4.00457444982e - 13
                                   +1.00x_{15} +2.00x_{13} +0.00x_{14} +1.00x_{4} -2.00x_{16}
x_{18}
                113.5
                                   -0.50x_{15} -4.50x_{13} -3.50x_{14} -38.00x_4 -1.50x_{16}
 z
```

```
-1.00x_{13}
                 10.0
                                                                        -4.00x_4
x_3
                330.0
                                   -4.00x_{15} - 22.00x_{13} - 3.00x_{14} - 122.00x_4 - 1.00x_{16}
x_7
x_1
                 0.5
                                   +0.50x_{15} +0.50x_{13} -0.50x_{14} +1.00x_{4} -0.50x_{16}
                 38.0
                                   -1.00x_{15} -2.00x_{13} -0.00x_{14} -14.00x_4 -0.00x_{16}
x_5
                208.5
                                   -5.50x_{15} - 22.50x_{13} - 0.50x_{14} - 69.00x_4 + 7.50x_{16}
x_{10}
                 14.0
                                   -4.00x_{15} +1.00x_{13} +6.00x_{14} -7.00x_{4} +0.00x_{16}
x_{11}
                233.0
                                   -7.00x_{15} -6.00x_{13} +3.00x_{14} -98.00x_4 -4.00x_{16}
x_{12}
                 0.5
                                   -0.50x_{15} +1.50x_{13} +0.50x_{14} +0.00x_{4} -0.50x_{16}
x_2
       4.87554441264e - 13
                                   +2.00x_{15} +2.00x_{13} -1.00x_{14} +2.00x_{4} -3.00x_{16}
x_6
x_8
       1.51517687286e - 12
                                   +2.00x_{15} +6.00x_{13} -4.00x_{14} +3.00x_{4} -3.00x_{16}
          0.499999999998
                                   -2.50x_{15} -7.50x_{13} +4.50x_{14} -5.00x_4 +5.50x_{16}
x_9
       -5.60662627436e - 13
                                   -1.00x_{15} -2.00x_{13} +2.00x_{14} -2.00x_{4} +2.00x_{16}
x_{17}
       4.00457444982e - 13
                                   +1.00x_{15} +2.00x_{13} +0.00x_{14} +1.00x_{4} -2.00x_{16}
x_{18}
                                   +0.50x_{15} +0.50x_{13} +0.50x_{14} +0.00x_{4} +0.50x_{16}
x_{19}
                 -0.5
                 -0.5
                                   +0.50x_{15} +0.50x_{13} +0.50x_{14} +1.00x_{4} +0.50x_{16}
x_{20}
                 -0.5
                                   +0.50x_{15} +0.50x_{13} +0.50x_{14} +1.00x_{4} +0.50x_{16}
x_{21}
         -0.499999999998
                                   +0.50x_{15} +0.50x_{13} +0.50x_{14} +1.00x_{4} +0.50x_{16}
x_{22}
                                   -0.50x_{15} -4.50x_{13} -3.50x_{14} -38.00x_4 -1.50x_{16}
                113.5
```

Forming the dual dictionary:

The Final Dual Dictionary is:

```
10.0
                                                                       -4.00x_4
x_3
                                   -6.00x_{19} -17.00x_{13} -2.00x_{14} -120.00x_4 +1.00x_{17}
                327.0
x_7
          0.66666666667
                                   +0.33x_{19} -0.33x_{13} -0.00x_{14} +0.33x_4 -0.33x_{17}
x_1
                                   -1.33x_{19} -0.67x_{13} +0.00x_{14} -13.33x_4 +0.33x_{17}
x_5
          37.3333333333
x_{10}
           207.333333333
                                   -2.33x_{19} -12.67x_{13} -8.00x_{14} -60.33x_4 +4.33x_{17}
           11.3333333333
                                   -5.33x_{19} +6.33x_{13} +6.00x_{14} -4.33x_4 +1.33x_{17}
x_{11}
                                  -12.00x_{19} +2.00x_{13} +7.00x_{14} -96.00x_{4} +1.00x_{17}
                227.0
x_{12}
        3.61137046193e - 13
                                  -1.00x_{19} +2.00x_{13} +1.00x_{14} +0.00x_{4} -0.00x_{17}
x_2
          0.3333333333333
                                   +0.67x_{19} -1.67x_{13} +2.00x_{14} -1.33x_{4} -1.67x_{17}
x_6
          0.3333333333334
                                  +0.67x_{19} +2.33x_{13} -1.00x_{14} -0.33x_{4} -1.67x_{17}
x_8
                                  +0.67x_{19} +0.33x_{13} -1.00x_{14} +0.67x_{4} +0.33x_{17}
          0.3333333333334
x_{16}
                                  +0.33x_{19} -2.33x_{13} -1.00x_{14} +0.33x_{4} +2.67x_{17}
          0.666666666666
x_9
       -1.57623913921e - 13
                                  +0.00x_{19} -0.00x_{13} +2.00x_{14} -1.00x_{4} -1.00x_{17}
x_{18}
          0.666666666667
                                   +1.33x_{19} -1.33x_{13} -0.00x_{14} -0.67x_4 -0.33x_{17}
x_{15}
       4.17739916732e - 13
                                   +1.00x_{19} -0.00x_{13} +0.00x_{14} +1.00x_4 +0.00x_{17}
x_{20}
       3.61137046193e - 13
                                   +1.00x_{19} +0.00x_{13} -0.00x_{14} +1.00x_{4} +0.00x_{17}
x_{21}
       1.95486219804e - 12
                                   +1.00x_{19} +0.00x_{13} -0.00x_{14} +1.00x_{4} +0.00x_{17}
x_{22}
                                   -1.67x_{19} -4.33x_{13} -2.00x_{14} -38.67x_4 -0.33x_{17}
           112.666666667
 z
```

```
10.0
                                               -1.00x_{13}
                                                                       -4.00x_4
x_3
                                   -6.00x_{19} -17.00x_{13} -2.00x_{14} -120.00x_4 +1.00x_{17}
                327.0
x_7
          0.666666666667
                                   +0.33x_{19} -0.33x_{13} -0.00x_{14} +0.33x_4 -0.33x_{17}
x_1
          37.3333333333
                                   -1.33x_{19} -0.67x_{13} +0.00x_{14} -13.33x_4 +0.33x_{17}
x_5
                                   -2.33x_{19} -12.67x_{13} -8.00x_{14} -60.33x_{4} +4.33x_{17}
x_{10}
           207.333333333
x_{11}
           11.33333333333
                                   -5.33x_{19} +6.33x_{13} +6.00x_{14} -4.33x_{4} +1.33x_{17}
                227.0
                                  -12.00x_{19} +2.00x_{13} +7.00x_{14} -96.00x_{4} +1.00x_{17}
x_{12}
                                   -1.00x_{19} +2.00x_{13} +1.00x_{14} +0.00x_{4} -0.00x_{17}
       -3.61137046193e - 13
x_2
          0.3333333333333
                                   +0.67x_{19} -1.67x_{13} +2.00x_{14} -1.33x_{4} -1.67x_{17}
x_6
          0.3333333333334
                                   +0.67x_{19} +2.33x_{13} -1.00x_{14} -0.33x_{4} -1.67x_{17}
x_8
          0.3333333333334
                                   +0.67x_{19} +0.33x_{13} -1.00x_{14} +0.67x_{4} +0.33x_{17}
x_{16}
                                   +0.33x_{19} -2.33x_{13} -1.00x_{14} +0.33x_4 +2.67x_{17}
          0.66666666666
x_9
       -1.57623913921e - 13
                                   +0.00x_{19} -0.00x_{13} +2.00x_{14} -1.00x_{4} -1.00x_{17}
x_{18}
          0.666666666667
                                   +1.33x_{19} -1.33x_{13} -0.00x_{14} -0.67x_4 -0.33x_{17}
x_{15}
       4.17739916732e - 13
                                   +1.00x_{19} -0.00x_{13} +0.00x_{14} +1.00x_4 +0.00x_{17}
x_{20}
                                   +1.00x_{19} +0.00x_{13} -0.00x_{14} +1.00x_{4} +0.00x_{17}
       3.61137046193e - 13
x_{21}
       1.95486219804e - 12
                                   +1.00x_{19} +0.00x_{13} -0.00x_{14} +1.00x_{4} +0.00x_{17}
x_{22}
         -0.666666666667
                                   +0.67x_{19} +0.33x_{13} +0.00x_{14} +0.67x_{4} +0.33x_{17}
x_{23}
         -0.3333333333333
                                   +0.33x_{19} +0.67x_{13} +1.00x_{14} +0.33x_{4} +0.67x_{17}
x_{24}
         -0.3333333333335
                                   +0.33x_{19} +0.67x_{13} +0.00x_{14} +0.33x_{4} +0.67x_{17}
x_{25}
                                   +0.33x_{19} +0.67x_{13} +1.00x_{14} +0.33x_{4} +0.67x_{17}
         -0.3333333333331
x_{26}
                                   +0.33x_{19} \ +0.67x_{13} \ +1.00x_{14} \ +0.33x_{4} \ +0.67x_{17}
         -0.3333333333333
x_{27}
         -0.3333333333334
                                   +0.33x_{19} +0.67x_{13} +0.00x_{14} +0.33x_{4} +0.67x_{17}
x_{28}
         -0.3333333333334
                                   +0.33x_{19} +0.67x_{13} +0.00x_{14} +0.33x_{4} +0.67x_{17}
x_{29}
         -0.666666666666
                                   +0.67x_{19} +0.33x_{13} +0.00x_{14} +0.67x_{4} +0.33x_{17}
x_{30}
         -0.666666666667
                                   +0.67x_{19} +0.33x_{13} +0.00x_{14} +0.67x_{4} +0.33x_{17}
x_{31}
                                   -1.67x_{19} -4.33x_{13} -2.00x_{14} -38.67x_4 -0.33x_{17}
           112.666666667
```

Forming the dual dictionary:

The Final Dual Dictionary is:

```
9.81818181818
                                  +0.09x_{18} - 0.12x_8 - 0.30x_2 - 3.73x_4 - 0.33x_{23}
x_3
          320.090909091
                                  -0.55x_{18} - 2.61x_8 - 3.52x_2 - 113.64x_4 - 11.67x_{23}
x_7
          0.636363636364
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4 +0.00x_{23}
x_1
                                  -0.27x_{18} - 0.30x_8 + 0.24x_2 - 12.82x_4 - 1.33x_{23}
          36.5454545455
x_5
                                  -3.36x_{18} - 1.85x_8 - 3.12x_2 - 60.09x_4
          203.727272727
                                                                            -6.33x_{23}
x_{10}
          11.4545454545
                                  +0.27x_{18} - 1.03x_8 + 4.42x_2 - 4.18x_4
                                                                             -0.33x_{23}
x_{11}
          222.181818182
                                  -0.09x_{18} - 2.21x_8 + 4.97x_2 - 91.27x_4
                                                                             -8.33x_{23}
x_{12}
                                  +0.36x_{18} -0.15x_8 +0.12x_2 +0.09x_4
                                                                             +0.33x_{23}
          0.272727272727
x_{14}
         0.636363636364
                                  +0.18x_{18} +0.09x_8 -0.27x_2 -0.45x_4
                                                                             +1.00x_{23}
x_{19}
         0.181818181818
                                  -0.09x_{18} + 0.12x_8 + 0.30x_2 -0.27x_4
                                                                             +0.33x_{23}
x_{13}
                                  -0.36x_{18} + 0.15x_8 - 0.12x_2 - 0.09x_4
         0.727272727273
                                                                             +0.67x_{23}
x_{16}
          1.63636363636
                                  -0.82x_{18} - 0.91x_8 - 0.27x_2 - 1.45x_4
                                                                             +1.00x_{23}
x_9
                                  +1.45x_{18} +0.06x_8 -0.85x_2 +0.36x_4
                                                                             -0.33x_{23}
         0.0909090909086
x_6
x_{15}
          1.09090909091
                                  +0.45x_{18} +0.06x_8 -0.85x_2 -0.64x_4
                                                                             +0.67x_{23}
         0.636363636364
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +1.00x_{23}
x_{20}
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +1.00x_{23}
         0.636363636364
x_{21}
          0.636363636365
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +1.00x_{23}
x_{22}
         0.545454545455
                                  -0.27x_{18} - 0.30x_8 + 0.24x_2 - 0.82x_4
                                                                             +0.67x_{23}
x_{17}
                                  +0.18x_{18} -0.24x_8 +0.39x_2 -0.45x_4
         0.636363636364
                                                                             +1.33x_{23}
x_{24}
                                  -0.18x_{18} - 0.09x_8 + 0.27x_2 - 0.55x_4
         0.363636363635
                                                                             +1.00x_{23}
x_{25}
                                  +0.18x_{18} -0.24x_8 +0.39x_2 -0.45x_4
x_{26}
         0.636363636366
                                                                             +1.33x_{23}
         0.636363636364
                                  +0.18x_{18} -0.24x_8 +0.39x_2 -0.45x_4
                                                                             +1.33x_{23}
x_{27}
         0.363636363636
                                  -0.18x_{18} - 0.09x_8 + 0.27x_2 - 0.55x_4
                                                                             +1.00x_{23}
x_{28}
         0.363636363636
                                  -0.18x_{18} - 0.09x_8 + 0.27x_2 - 0.55x_4
                                                                             +1.00x_{23}
x_{29}
x_{30}
       3.06695325701e - 13
                                  -0.00x_{18} - 0.00x_8 + 0.00x_2 - 0.00x_4
       -3.02788097625e - 17
                                  +0.00x_{18} -0.00x_8 -0.00x_2 +0.00x_4 +1.00x_{23}
x_{31}
                                  -0.55x_{18} - 0.27x_8 - 1.18x_2 - 36.64x_4 - 4.00x_{23}
           110.090909091
```

```
9.81818181818
                                  +0.09x_{18} -0.12x_8 -0.30x_2 -3.73x_4
                                                                            -0.33x_{23}
x_3
          320.090909091
                                  -0.55x_{18} - 2.61x_8 - 3.52x_2 - 113.64x_4 - 11.67x_{23}
x_7
          0.636363636364
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +0.00x_{23}
x_1
                                  -0.27x_{18} - 0.30x_8 + 0.24x_2 - 12.82x_4
                                                                             -1.33x_{23}
          36.5454545455
x_5
                                  -3.36x_{18} - 1.85x_8 - 3.12x_2 - 60.09x_4
                                                                             -6.33x_{23}
x_{10}
           203.727272727
          11.4545454545
                                  +0.27x_{18} - 1.03x_8 + 4.42x_2 - 4.18x_4
                                                                             -0.33x_{23}
x_{11}
                                  -0.09x_{18} - 2.21x_8 + 4.97x_2 - 91.27x_4
                                                                             -8.33x_{23}
          222.181818182
x_{12}
          0.272727272727
                                  +0.36x_{18} -0.15x_8 +0.12x_2 +0.09x_4
                                                                             +0.33x_{23}
x_{14}
                                  +0.18x_{18} +0.09x_8 -0.27x_2 -0.45x_4
          0.636363636364
                                                                             +1.00x_{23}
x_{19}
          0.181818181818
                                  -0.09x_{18} + 0.12x_8 + 0.30x_2 -0.27x_4
                                                                             +0.33x_{23}
x_{13}
          0.727272727273
                                  -0.36x_{18} + 0.15x_8 - 0.12x_2 - 0.09x_4
                                                                             +0.67x_{23}
x_{16}
                                  -0.82x_{18} - 0.91x_8 - 0.27x_2 - 1.45x_4
                                                                             +1.00x_{23}
x_9
           1.63636363636
         0.0909090909086
                                  +1.45x_{18} +0.06x_8 -0.85x_2 +0.36x_4
                                                                             -0.33x_{23}
x_6
                                  +0.45x_{18} +0.06x_8 -0.85x_2 -0.64x_4
          1.09090909091
                                                                             +0.67x_{23}
x_{15}
         0.636363636364
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +1.00x_{23}
x_{20}
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +1.00x_{23}
         0.636363636364
x_{21}
         0.636363636365
                                  +0.18x_{18} +0.09x_8 -0.27x_2 +0.55x_4
                                                                             +1.00x_{23}
x_{22}
         0.545454545455
                                  -0.27x_{18} - 0.30x_8 + 0.24x_2 - 0.82x_4
                                                                             +0.67x_{23}
x_{17}
                                  +0.18x_{18} -0.24x_8 +0.39x_2 -0.45x_4
                                                                             +1.33x_{23}
         0.636363636364
x_{24}
                                  -0.18x_{18} - 0.09x_8 + 0.27x_2 - 0.55x_4
         0.363636363635
                                                                             +1.00x_{23}
x_{25}
                                  +0.18x_{18} - 0.24x_8 + 0.39x_2 -0.45x_4
                                                                             +1.33x_{23}
          0.636363636366
x_{26}
         0.636363636364
                                  +0.18x_{18} -0.24x_8 +0.39x_2 -0.45x_4
                                                                             +1.33x_{23}
x_{27}
                                  -0.18x_{18} - 0.09x_8 + 0.27x_2 - 0.55x_4
                                                                             +1.00x_{23}
         0.363636363636
x_{28}
          0.363636363636
                                  -0.18x_{18} - 0.09x_8 + 0.27x_2 - 0.55x_4
                                                                             +1.00x_{23}
x_{29}
       3.06695325701e - 13
                                  -0.00x_{18} -0.00x_8 +0.00x_2 -0.00x_4
                                                                             +1.00x_{23}
x_{30}
        -3.02788097625e - 17
                                  +0.00x_{18} -0.00x_8 -0.00x_2 +0.00x_4
                                                                             +1.00x_{23}
x_{31}
                                  +0.91x_{18} +0.12x_8 +0.30x_2 +0.73x_4
                                                                             +0.33x_{23}
         -0.818181818182
x_{32}
                                  +0.55x_{18} +0.61x_8 +0.52x_2 +0.64x_4
         -0.090909090909
                                                                             +0.67x_{23}
x_{33}
         -0.636363636364
                                  +0.82x_{18} +0.91x_8 +0.27x_2 +0.45x_4
                                                                             +1.00x_{23}
x_{34}
                                  +0.27x_{18} +0.30x_8 +0.76x_2 +0.82x_4
                                                                             +0.33x_{23}
         -0.54545454545455
x_{35}
                                                                             +0.33x_{23}
         -0.727272727273
                                  +0.36x_{18} +0.85x_8 +0.12x_2 +0.09x_4
x_{36}
         -0.45454545454545
                                  +0.73x_{18} +0.03x_8 +0.58x_2 +0.18x_4
                                                                             +0.33x_{23}
x_{37}
         -0.181818181818
                                  +0.09x_{18} +0.21x_8 +0.03x_2 +0.27x_4
                                                                             +0.33x_{23}
x_{38}
                                  +0.64x_{18} +0.15x_8 +0.88x_2 +0.91x_4
                                                                             +0.67x_{23}
         -0.272727272727
x_{39}
         -0.636363636364
                                  +0.82x_{18} +0.91x_8 +0.27x_2 +0.45x_4
                                                                             +1.00x_{23}
x_{40}
         -0.181818181818
                                  +0.09x_{18} +0.88x_8 +0.70x_2 +0.27x_4
                                                                             +0.67x_{23}
x_{41}
                                  +0.36x_{18} +0.85x_8 +0.12x_2 +0.09x_4
                                                                             +0.33x_{23}
         -0.727272727273
x_{42}
                                  +0.82x_{18} +0.91x_8 +0.27x_2 +0.45x_4
                                                                             +0.00x_{23}
         -0.636363636364
x_{43}
        -0.0909090909086
                                  +0.55x_{18} +0.94x_8 +0.85x_2 +0.64x_4
                                                                             +0.33x_{23}
x_{44}
x_{45}
        -0.0909090909089
                                  +0.55x_{18} +0.94x_8 +0.85x_2 +0.64x_4
                                                                             +0.33x_{23}
         -0.636363636364
                                  +0.82x_{18}+0.91x_{8}+0.27x_{2}+0.45x_{4}
                                                                             +0.00x_{23}
x_{46}
                                  +0.82x_{18} +0.91x_8 +0.27x_2 +0.45x_4
                                                                             +0.00x_{23}
         -0.636363636364
x_{47}
                                  +0.82x_{18} +0.91x_8 +0.27x_2 +0.45x_4
                                                                             +0.00x_{23}
         -0.636363636365
x_{48}
         -0.54545454545455
                                  +0.27x_{18} +0.30x_8 +0.76x_2 +0.82x_4
                                                                             +0.33x_{23}
x_{49}
         -0.636363636364
                                  +0.82x_{18}+0.24x_{8}+0.61x_{2}+0.45x_{4}
                                                                             +0.67x_{23}
x_{50}
         -0.363636363635
                                  +0.18x_{18} +0.09x_8 +0.73x_2 +0.55x_4
                                                                             +1.00x_{23}
x_{51}
                                  +0.82x_{18} +0.24x_{8} +0.61x_{2} +0.45x_{4}
                                                                             +0.67x_{23}
         -0.636363636366
x_{52}
         -0.636363636364
                                  +0.82x_{18}+0.24x_{8}+0.61x_{2}+0.45x_{4}
                                                                             +0.67x_{23}
x_{53}
                                                                             +1.00x_{23}
         -0.363636363636
                                  +0.18x_{18} +0.09x_8 +0.73x_2 +0.55x_4
x_{54}
                                  +0.18x_{18} +0.09x_8 +0.73x_2 +0.55x_4
                                                                             +1.00x_{23}
         -0.363636363636
x_{55}
           110.090909091
                                  -0.55x_{18} - 0.27x_8 - 1.18x_2 - 36.64x_4
```

Forming the dual dictionary: The Final Dual Dictionary is:

```
9.75
                                   +0.25x_{32} -0.50x_{35} -0.00x_{51} -3.50x_4 -0.25x_{23}
x_3
                                   +1.50x_{32} - 11.00x_{35} +6.00x_{51} -109.00x_4 -14.50x_{23}
x_7
                317.5
          0.750000000001
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51} +0.50x_4 +0.75x_{23}
x_1
                                   -0.25x_{32} -1.50x_{35} +2.00x_{51} -12.50x_4 -2.75x_{23}
                36.25
x_5
                                   -2.50x_{32} -6.00x_{35} +3.00x_{51} -55.00x_4 -6.50x_{23}
x_{10}
                199.5
                                   -0.25x_{32} -7.50x_{35} +14.00x_{51} -5.50x_4 -11.75x_{23}
                12.25
x_{11}
                                   -0.25x_{32} - 13.50x_{35} + 21.00x_{51} - 91.50x_4 - 24.75x_{23}
               222.25
x_{12}
                                   +0.50x_{32} -1.00x_{35} +1.00x_{51}
                                                                       +0.00x_4
                                                                                    -0.50x_{23}
          0.4999999999999
x_{14}
x_{19}
          0.7500000000001
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        -0.50x_4
                                                                                    +1.75x_{23}
                 0.25
                                   -0.25x_{32} +0.50x_{35} +0.00x_{51}
                                                                        -0.50x_4
                                                                                    +0.25x_{23}
x_{13}
          0.5000000000002
                                   -0.50x_{32} +1.00x_{35} -1.00x_{51}
                                                                        -0.00x_4
                                                                                    +1.50x_{23}
x_{16}
          0.499999999994
                                   -0.50x_{32} -4.00x_{35} +4.00x_{51}
                                                                        +0.00x_4
                                                                                    -1.50x_{23}
x_9
                 1.0
                                   +2.00x_{32} +0.00x_{35} -2.00x_{51}
                                                                        -0.00x_{4}
                                                                                    +1.00x_{23}
x_6
                                                                        -0.50x_{4}
                 1.25
                                   +0.75x_{32} +0.50x_{35} -2.00x_{51}
                                                                                    +2.25x_{23}
x_{15}
          0.7500000000002
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        +0.50x_4
                                                                                    +1.75x_{23}
x_{20}
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        +0.50x_4
                                                                                    +1.75x_{23}
          0.7500000000002
x_{21}
                                                                                    +1.75x_{23}
          0.7500000000003
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        +0.50x_4
x_{22}
                                                                                    -0.75x_{23}
          0.249999999997
                                   -0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
x_{17}
                                                                        -0.50x_4
                                   +0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                                    -0.25x_{23}
          0.749999999998
x_{24}
                                   -0.25x_{32} -0.50x_{35} +1.00x_{51}
          0.249999999997
                                                                        -0.50x_4
                                                                                    +0.25x_{23}
x_{25}
                                   +0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
                                                                                    -0.25x_{23}
                 0.75
x_{26}
          0.749999999998
                                   +0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
                                                                                    -0.25x_{23}
x_{27}
                                                                        -0.50x_4
                                                                                    +0.25x_{23}
          0.249999999998
                                   -0.25x_{32} -0.50x_{35} +1.00x_{51}
x_{28}
          0.249999999998
                                   -0.25x_{32} -0.50x_{35} +1.00x_{51}
                                                                        -0.50x_4
                                                                                    +0.25x_{23}
x_{29}
       2.97796509674e - 13
                                   -0.00x_{32} -0.00x_{35} +0.00x_{51}
                                                                        -0.00x_4
                                                                                    +1.00x_{23}
x_{30}
                                                                                    +1.00x_{23}
       -4.16333634235e - 17
                                   +0.00x_{32} -0.00x_{35} -0.00x_{51}
                                                                        +0.00x_4
x_{31}
                                   +1.25x_{32} -0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
                                                                                    -0.25x_{23}
                 0.75
x_{18}
                                   +0.25x_{32} +2.50x_{35} -2.00x_{51}
                                                                        -0.50x_4
          0.7500000000003
                                                                                    +1.75x_{23}
x_{33}
          0.500000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                    +3.50x_{23}
x_{34}
          0.500000000007
                                   -0.50x_{32} +5.00x_{35} -5.00x_{51}
                                                                        -1.00x_4
                                                                                    +3.50x_{23}
x_8
       5.17502707353e - 12
                                   -0.00x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                    +3.00x_{23}
x_{36}
          0.249999999999
                                   +0.75x_{32} -0.50x_{35} +1.00x_{51}
                                                                        -0.50x_4
                                                                                    -0.75x_{23}
x_{37}
       1.70138902966e - 12
                                   -0.00x_{32} +1.00x_{35} -1.00x_{51}
                                                                        -0.00x_4
                                                                                    +1.00x_{23}
x_{38}
          0.499999999998
                                   +0.50x_{32} -0.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
                                                                                    -0.50x_{23}
x_{39}
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                    +3.50x_{23}
          0.5000000000006
x_{40}
                                   -0.50x_{32} +4.00x_{35} -3.00x_{51}
          0.5000000000004
                                                                        -1.00x_4
                                                                                    +2.50x_{23}
x_{41}
       5.77193848272e - 12
                                   -0.00x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                    +3.00x_{23}
x_{42}
          0.500000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                    +2.50x_{23}
x_{43}
                 1.0
                                   -0.00x_{32} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                    +2.00x_{23}
x_{44}
x_{45}
                 1.0
                                   -0.00x_{32} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                    +2.00x_{23}
                                                                                    +2.50x_{23}
          0.5000000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
x_{46}
          0.500000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                    +2.50x_{23}
x_{47}
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
          0.5000000000004
                                                                                    +2.50x_{23}
x_{48}
        2.38836728172e -
                                   +0.00x_{32} +1.00x_{35} -0.00x_{51}
                                                                        +0.00x_4
                                                                                    +0.00x_{23}
x_{49}
          0.249999999999
                                   +0.75x_{32} +0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
                                                                                    +0.25x_{23}
x_{50}
          0.24999999997
                                   -0.25x_{32} -0.50x_{35} +2.00x_{51}
                                                                       -0.50x_4
                                                                                    -1.75x_{23}
x_2
                                   +0.75x_{30} +0.50x_{35} -0.00x_{51}
                                                                       -0.50x_4
                                                                                    +0.25x_{23}
          0.249999999997
x_{52}
          0.249999999999
                                   +0.75x_{32} +0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
x_{53}
                                                                                    +0.00x_{23}
       -9.57164902893e - 13
                                   +0.00x_{32} -0.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
x_{54}
      -1.32507893547e - 12
                                                                                    +0.00x_{23}
                                   +0.00x_{32} -0.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
x_{55}
                109.25
                                   -0.25x_{32} -0.50x_{35} -1.00x_{51}
                                                                       -35.50x_4
 z
```

0.750000000001

```
9.75
                                   +0.25x_{32} -0.50x_{35} -0.00x_{51}
                                                                       -3.50x_4
                                   +1.50x_{32} - 11.00x_{35} + 6.00x_{51} - 109.00x_4 - 14.50x_{23}
x_7
                317.5
          0.750000000001
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                       +0.50x_4 +0.75x_{23}
x_1
                                   -0.25x_{32} -1.50x_{35} +2.00x_{51} -12.50x_4 -2.75x_{23}
                36.25
x_5
x_{10}
                199.5
                                   -2.50x_{32} -6.00x_{35} +3.00x_{51} -55.00x_4 -6.50x_{23}
                                   -0.25x_{32} -7.50x_{35} +14.00x_{51} -5.50x_4 -11.75x_{23}
                12.25
x_{11}
                                   -0.25x_{32} - 13.50x_{35} + 21.00x_{51} - 91.50x_4 - 24.75x_{23}
                222.25
x_{12}
                                   +0.50x_{32} -1.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
                                                                                     -0.50x_{23}
          0.4999999999999
x_{14}
x_{19}
          0.7500000000001
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        -0.50x_4
                 0.25
                                   -0.25x_{32} +0.50x_{35} +0.00x_{51}
                                                                        -0.50x_4
                                                                                     +0.25x_{23}
x_{13}
          0.5000000000002
                                   -0.50x_{32} +1.00x_{35} -1.00x_{51}
                                                                        -0.00x_4
                                                                                     +1.50x_{23}
x_{16}
                                   -0.50x_{32} -4.00x_{35} +4.00x_{51}
          0.499999999994
x_9
                                                                        +0.00x_4
                                                                                     -1.50x_{23}
                 1.0
                                   +2.00x_{32} +0.00x_{35} -2.00x_{51}
                                                                        -0.00x_4
                                                                                     +1.00x_{23}
x_6
                 1.25
                                   +0.75x_{32} +0.50x_{35} -2.00x_{51}
                                                                        -0.50x_4
                                                                                     +2.25x_{23}
x_{15}
          0.7500000000002
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        +0.50x_4
                                                                                     +1.75x_{23}
x_{20}
                                                                        +0.50x_4
          0.7500000000002
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                                     +1.75x_{23}
x_{21}
x_{22}
          0.7500000000003
                                   +0.25x_{32} +0.50x_{35} -1.00x_{51}
                                                                        +0.50x_4
                                                                                     +1.75x_{23}
                                                                                     -0.75x_{23}
          0.249999999997
                                   -0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
x_{17}
                                   +0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
                                                                                     -0.25x_{23}
          0.749999999998
x_{24}
          0.249999999997
                                   -0.25x_{32} -0.50x_{35} +1.00x_{51}
                                                                        -0.50x_4
                                                                                     +0.25x_{23}
x_{25}
                                   +0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                         -0.50x_4
                 0.75
                                                                                     -0.25x_{23}
x_{26}
          0.749999999998
                                   +0.25x_{32} -1.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
                                                                                     -0.25x_{23}
x_{27}
          0.249999999998
                                   -0.25x_{32} -0.50x_{35} +1.00x_{51}
                                                                        -0.50x_4
                                                                                     +0.25x_{23}
x_{28}
x_{29}
          0.249999999998
                                   -0.25x_{32} -0.50x_{35} +1.00x_{51}
                                                                        -0.50x_4
                                                                                     +0.25x_{23}
x_{30}
       2.97796509674e - 13
                                   -0.00x_{32} -0.00x_{35} +0.00x_{51}
                                                                        -0.00x_4
                                                                                     +1.00x_{23}
        -4.16333634235e - 17
                                   +0.00x_{32} -0.00x_{35} -0.00x_{51}
                                                                        +0.00x_4
                                                                                     +1.00x_{23}
x_{31}
                                   +1.25x_{32} -0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
                 0.75
                                                                                     -0.25x_{23}
x_{18}
x_{33}
          0.7500000000003
                                   +0.25x_{32} +2.50x_{35} -2.00x_{51}
                                                                        -0.50x_4
                                                                                     +1.75x_{23}
          0.500000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                     +3.50x_{23}
x_{34}
          0.500000000007
                                                                        -1.00x_4
                                                                                     +3.50x_{23}
                                   -0.50x_{32} +5.00x_{35} -5.00x_{51}
x_8
                                   -0.00x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
       5.17502707353e - 12
                                                                                     +3.00x_{23}
x_{36}
          0.249999999999
                                   +0.75x_{32} -0.50x_{35} +1.00x_{51}
                                                                        -0.50x_4
                                                                                     -0.75x_{23}
x_{37}
       1.70138902966e - 12
                                   -0.00x_{32} +1.00x_{35} -1.00x_{51}
                                                                        -0.00x_4
                                                                                     +1.00x_{23}
x_{38}
                                   +0.50x_{32} -0.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
          0.499999999998
                                                                                     -0.50x_{23}
x_{39}
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                     +3.50x_{23}
          0.5000000000006
x_{40}
x_{41}
          0.5000000000004
                                   -0.50x_{32} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.50x_{23}
                                                                                     +3.00x_{23}
       5.77193848272e - 12
                                   -0.00x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
x_{42}
          0.500000000006
                                                                        -1.00x_4
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                                     +2.50x_{23}
x_{43}
                 1.0
                                   -0.00x_{32} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.00x_{23}
x_{44}
x_{45}
                 1.0
                                   -0.00x_{32} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.00x_{23}
          0.500000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.50x_{23}
x_{46}
          0.500000000006
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.50x_{23}
x_{47}
                                                                        -1.00x_4
          0.5000000000004
                                   +0.50x_{32} +4.00x_{35} -4.00x_{51}
                                                                                     +2.50x_{23}
x_{48}
        2.38836728172e -
                                   +0.00x_{32} +1.00x_{35} -0.00x_{51}
                                                                        +0.00x_4
x_{49}
                                                                                     +0.00x_{23}
          0.249999999999
                                   +0.75x_{32} +0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
                                                                                     +0.25x_{23}
x_{50}
          0.249999999997
                                   -0.25x_{32} -0.50x_{35} +2.00x_{51}
                                                                        -0.50x_4
                                                                                     -1.75x_{23}
x_2
          0.249999999997
                                   +0.75x_{30} +0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
                                                                                     +0.25x_{23}
x_{52}
          0.249999999999
                                   +0.75x_{32} +0.50x_{35} -0.00x_{51}
                                                                        -0.50x_4
x_{53}
                                                                                     +0.25x_{23}
        -9.57164902893e - 13
                                   +0.00x_{32} -0.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
                                                                                     +0.00x_{23}
x_{54}
       -1.32507893547e - 12
                                   +0.00x_{32} -0.00x_{35} +1.00x_{51}
                                                                         +0.00x_4
                                                                                     +0.00x_{23}
x_{55}
x_{56}
                -0.75
                                   +0.75x_{32} +0.50x_{35} +0.00x_{51}
                                                                        +0.50x_4
                                                                                     +0.25x_{23}
         -0.499999999991
                                   +0.50x_{32} +0.00x_{35} +0.00x_{51}
                                                                        +1.00x_4
                                                                                     +0.50x_{23}
x_{57}
         -0.7500000000001
                                   +0.75x_{32} +0.50x_{35} +0.00x_{51}
                                                                        +0.50x_4
                                                                                     +0.25x_{23}
x_{58}
         -0.249999999997
                                   +0.25x_{32} +0.50x_{35} +1.00x_{51}
                                                                        +0.50x_4
                                                                                     +0.75x_{23}
x_{59}
x_{60}
         -0.499999999996
                                   +0.50x_{32} +0.00x_{35} +1.00x_{51}
                                                                        +1.00x_4
                                                                                     +0.50x_{23}
          -0.24999999998
                                   +0.25x_{32} +0.50x_{35} +1.00x_{51}
                                                                        +0.50x_4
                                                                                     +0.75x_{23}
x_{61}
         -0.2499999999969
                                   +0.25x_{32} +0.50x_{35} +1.00x_{51}
                                                                        +0.50x_4
                                                                                     +0.75x_{23}
x_{62}
x_{63}
         -0.4999999999999
                                   +0.50x_{32} +0.00x_{35} +1.00x_{51}
                                                                        +1.00x_4
                                                                                    +0.50x_{23}
```

10.50~

Forming the dual dictionary: The Final Dual Dictionary is: Final primal dictionary obtained:

44106049506

```
10.0
                                   +0.33x_{56} -0.67x_{35} -0.00x_{51}
                                                                       -3.67x_4
                319.0
                                   +2.00x_{56} - 12.00x_{35} +6.00x_{51} -110.00x_4 -15.00x_{23}
x_7
                 1.0
                                   +0.33x_{56} +0.33x_{35} -1.00x_{51}
                                                                       +0.33x_4 +0.67x_{23}
x_1
                                   -0.33x_{56} -1.33x_{35} +2.00x_{51} -12.33x_4 -2.67x_{23}
                 36.0
x_5
x_{10}
                197.0
                                   -3.33x_{56} -4.33x_{35} +3.00x_{51} -53.33x_4 -5.67x_{23}
                                   -0.33x_{56} -7.33x_{35} +14.00x_{51} -5.33x_4 -11.67x_{23}
                 12.0
x_{11}
                                   -0.33x_{56} - 13.33x_{35} + 21.00x_{51} - 91.33x_4 - 24.67x_{23}
                222.0
x_{12}
          0.999999999999
                                   +0.67x_{56} -1.33x_{35} +1.00x_{51}
                                                                        -0.33x_4
                                                                                     -0.67x_{23}
x_{14}
x_{19}
                 1.0
                                   +0.33x_{56} +0.33x_{35} -1.00x_{51}
                                                                        -0.67x_4
       9.67559365961e - 14
                                   -0.33x_{56} +0.67x_{35} +0.00x_{51}
                                                                        -0.33x_4
                                                                                     +0.33x_{23}
x_{13}
                                   -0.67x_{56} +1.33x_{35} -1.00x_{51}
        1.6748269438e - 12
                                                                        +0.33x_4
                                                                                     +1.67x_{23}
x_{16}
       -5.52352608096e - 12
                                   -0.67x_{56} -3.67x_{35} +4.00x_{51}
x_9
                                                                        +0.33x_4
                                                                                     -1.33x_{23}
x_6
                 3.0
                                   +2.67x_{56} -1.33x_{35} -2.00x_{51}
                                                                        -1.33x_4
                                                                                     +0.33x_{23}
                 2.0
                                   +1.00x_{56} +0.00x_{35} -2.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.00x_{23}
x_{15}
                 1.0
                                   +0.33x_{56} +0.33x_{35} -1.00x_{51}
                                                                        +0.33x_4
                                                                                     +1.67x_{23}
x_{20}
                                                                        +0.33x_4
                 1.0
                                   +0.33x_{56} +0.33x_{35} -1.00x_{51}
                                                                                     +1.67x_{23}
x_{21}
x_{22}
                 1.0
                                   +0.33x_{56} +0.33x_{35} -1.00x_{51}
                                                                        +0.33x_4
                                                                                     -0.67x_{23}
        -2.56270005217e - 12
                                   -0.33x_{56} -1.33x_{35} +2.00x_{51}
                                                                        -0.33x_4
x_{17}
          0.99999999998
                                   +0.33x_{56} -1.67x_{35} +2.00x_{51}
                                                                        -0.67x_4
                                                                                     -0.33x_{23}
x_{24}
        -2.79568035388e - 12
                                   -0.33x_{56} -0.33x_{35} +1.00x_{51}
                                                                        -0.33x_4
                                                                                     +0.33x_{23}
x_{25}
                                   +0.33x_{56} -1.67x_{35} +2.00x_{51}
                                                                        -0.67x_4
x_{26}
                 1.0
                                                                                     -0.33x_{23}
          0.99999999998
                                   +0.33x_{56} -1.67x_{35} +2.00x_{51}
                                                                        -0.67x_4
                                                                                     -0.33x_{23}
x_{27}
                                                                                     +0.33x_{23}
x_{28}
       -1.85232384986e - 12
                                   -0.33x_{56} -0.33x_{35} +1.00x_{51}
                                                                        -0.33x_4
x_{29}
       -1.49333323485e - 12
                                   -0.33x_{56} -0.33x_{35} +1.00x_{51}
                                                                        -0.33x_4
                                                                                     +0.33x_{23}
       2.88588597463e - 13
x_{30}
                                   -0.00x_{56} -0.00x_{35} +0.00x_{51}
                                                                        -0.00x_4
                                                                                     +1.00x_{23}
       -1.61161817746e - 29
                                   +0.00x_{56} -0.00x_{35} -0.00x_{51}
                                                                        +0.00x_4
                                                                                     +1.00x_{23}
x_{31}
                                   +1.67x_{56} -1.33x_{35} -0.00x_{51}
                                                                        -1.33x_4
                 2.0
                                                                                     -0.67x_{23}
x_{18}
x_{33}
                 1.0
                                   +0.33x_{56} +2.33x_{35} -2.00x_{51}
                                                                        -0.67x_4
                                                                                     +1.67x_{23}
           1.00000000001
                                   +0.67x_{56} +3.67x_{35} -4.00x_{51}
                                                                        -1.33x_4
                                                                                     +3.33x_{23}
x_{34}
                                                                        -0.67x_4
         7.353340159e - 12
                                                                                     +3.67x_{23}
                                   -0.67x_{56} +5.33x_{35} -5.00x_{51}
x_8
       5.09214892475e - 12
                                   -0.00x_{56} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
                                                                                     +3.00x_{23}
x_{36}
                                                                        -1.00x_4
          0.999999999999
                                   +1.00x_{56} -1.00x_{35} +1.00x_{51}
x_{37}
       1.67331426493e - 12
                                   -0.00x_{56} +1.00x_{35} -1.00x_{51}
                                                                        -0.00x_4
                                                                                     +1.00x_{23}
x_{38}
          0.99999999998
                                   +0.67x_{56} -0.33x_{35} +1.00x_{51}
                                                                        -0.33x_4
                                                                                     -0.67x_{23}
x_{39}
                                   +0.67x_{56} +3.67x_{35} -4.00x_{51}
                                                                        -1.33x_4
                                                                                     +3.33x_{23}
           1.000000000001
x_{40}
x_{41}
       4.46087611294e - 12
                                   -0.67x_{56} +4.33x_{35} -3.00x_{51}
                                                                        -0.67x_4
                                                                                     +2.67x_{23}
                                                                                     +3.00x_{23}
       5.67867974866e - 12
                                   -0.00x_{56} +4.00x_{35} -4.00x_{51}
                                                                        -1.00x_4
x_{42}
           1.00000000001
                                   +0.67x_{56} +3.67x_{35} -4.00x_{51}
                                                                        -1.33x_4
                                                                                     +2.33x_{23}
x_{43}
x_{44}
                 1.0
                                   -0.00x_{56} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.00x_{23}
x_{45}
                 1.0
                                   -0.00x_{56} +4.00x_{35} -3.00x_{51}
                                                                        -1.00x_4
                                                                                     +2.00x_{23}
           1.000000000001
                                   +0.67x_{56} +3.67x_{35} -4.00x_{51}
                                                                        -1.33x_4
                                                                                     +2.33x_{23}
x_{46}
           1.00000000001
                                   +0.67x_{56} +3.67x_{35} -4.00x_{51}
                                                                        -1.33x_4
                                                                                     +2.33x_{23}
x_{47}
                                                                        -1.33x_4
                 1.0
                                   +0.67x_{56} +3.67x_{35}
                                                           -4.00x_{51}
                                                                                     +2.33x_{23}
x_{48}
        2.32980301718e -
                                   +0.00x_{56} +1.00x_{35} -0.00x_{51}
                                                                        +0.00x_4
x_{49}
                                                                                     +0.00x_{23}
          0.999999999999
                                   +1.00x_{56} +0.00x_{35} -0.00x_{51}
                                                                        -1.00x_4
                                                                                     +0.00x_{23}
x_{50}
                                   -0.33x_{56} -0.33x_{35} +2.00x_{51}
                                                                        -0.33x_4
        -2.79568035388e - 12
                                                                                     -1.67x_{23}
x_2
                                                                        -1.00x_4
          0.99999999997
                                   +1.00x_{12} +0.00x_{35} -0.00x_{51}
                                                                                     +0.00x_{23}
x_{52}
          0.999999999999
                                   +1.00x_{56} -0.00x_{35} -0.00x_{51}
                                                                        -1.00x_4
x_{53}
                                                                                     +0.00x_{23}
        -9.433842596e - 13
                                   +0.00x_{56} -0.00x_{35} +1.00x_{51}
                                                                        +0.00x_4
                                                                                     +0.00x_{23}
x_{54}
       -1.30237487461e - 12
                                   +0.00x_{56} -0.00x_{35} +1.00x_{51}
                                                                         +0.00x_4
                                                                                     +0.00x_{23}
x_{55}
x_{32}
                  1.0
                                   +1.33x_{56} -0.67x_{35}
                                                           -0.00x_{51}
                                                                         -0.67x_4
                                                                                     -0.33x_{23}
       9.11987152463e - 12
                                   +0.67x_{56} -0.33x_{35} +0.00x_{51}
                                                                        +0.67x_4
                                                                                     +0.33x_{23}
x_{57}
       -1.44106948596e - 12
                                   +1.00x_{56} -0.00x_{35} +0.00x_{51}
                                                                        +0.00x_4
                                                                                     +0.00x_{23}
x_{58}
                                                                                     +0.67x_{23}
       2.79917755641e - 12
                                   +0.33x_{56} +0.33x_{35} +1.00x_{51}
                                                                        +0.33x_4
x_{59}
x_{60}
       3.64419605603e - 12
                                   +0.67x_{56} -0.33x_{35} +1.00x_{51}
                                                                        +0.67x_4
                                                                                     +0.33x_{23}
       2.00837402264e - 11
                                   +0.33x_{56} +0.33x_{35} +1.00x_{51}
                                                                        +0.33x_4
                                                                                     +0.67x_{23}
x_{61}
       3.03370939481e - 11
                                   +0.33x_{56} +0.33x_{35} +1.00x_{51}
                                                                        +0.33x_4
                                                                                     +0.67x_{23}
x_{62}
                                   +0.67x_{56} -0.33x_{35} +1.00x_{51}
       1.20653487201e - 12
x_{63}
                                                                        +0.67x_4
                                                                                    +0.33x_{23}
```

0.00

Final answer: 109.000000 Done. Added cuts