

Read in the following dictionary:

$x_6$	38.0	$-9.00x_1$	$-3.00x_3 + 4.00x_4 - 5.00x_5$
$x_7$	18.0	$-10.00x_1 - 9.00x_2 - 6.00x_3 - 2.00x_4 + 3.00x_5$	
$x_8$	1.0	$+6.00x_1 + 7.00x_2 - 2.00x_3 + 8.00x_4 + 6.00x_5$	
$x_9$	13.0	$-2.00x_1 - 1.00x_2 - 3.00x_5$	
$x_{10}$	-11.0	$+9.00x_1 - 4.00x_2 + 8.00x_3 + 1.00x_4 - 3.00x_5$	
$z$	0.0	$-1.00x_1 + 5.00x_2 - 5.00x_3 - 4.00x_4 - 3.00x_5$	

## 0.1 Initialization Phase: Dual Problem Solving

New Objective in primal was changed to :

$$\max \sum_{j=1}^5 -x_j$$

Primal variable  $x_j$  corresponds to dual variable  $y_j$  for  $j = 1, \dots, 10$  Dual Dictionary (with objective changed is):

$y_1$	1.0	$+9.00y_6 + 10.00y_7 - 6.00y_8 + 2.00y_9 - 9.00y_{10}$
$y_2$	1.0	$+9.00y_7 - 7.00y_8 + 1.00y_9 + 4.00y_{10}$
$y_3$	1.0	$+3.00y_6 + 6.00y_7 + 2.00y_8 - 8.00y_{10}$
$y_4$	1.0	$-4.00y_6 + 2.00y_7 - 8.00y_8 - 1.00y_{10}$
$y_5$	1.0	$+5.00y_6 - 3.00y_7 - 6.00y_8 + 3.00y_9 + 3.00y_{10}$
$z$	-0	$-38.00y_6 - 18.00y_7 - 1.00y_8 - 13.00y_9 + 11.00y_{10}$

Initialization succeeded in finding final dual dictionary with 2 pivots

$y_{10}$	0.111111111111	$+1.00y_6 + 1.11y_7 - 0.67y_8 + 0.22y_9 - 0.11y_1$
$y_2$	1.444444444444	$+4.00y_6 + 13.44y_7 - 9.67y_8 + 1.89y_9 - 0.44y_1$
$y_3$	0.111111111111	$-5.00y_6 - 2.89y_7 + 7.33y_8 - 1.78y_9 + 0.89y_1$
$y_4$	0.888888888889	$-5.00y_6 + 0.89y_7 - 7.33y_8 - 0.22y_9 + 0.11y_1$
$y_5$	1.333333333333	$+8.00y_6 + 0.33y_7 - 8.00y_8 + 3.67y_9 - 0.33y_1$
$z$	1.222222222222	$-27.00y_6 - 5.78y_7 - 8.33y_8 - 10.56y_9 - 1.22y_1$

Primal Dictionary is:

$x_6$	27.0	$-1.00x_{10} - 4.00x_2 + 5.00x_3 + 5.00x_4 - 8.00x_5$
$x_7$	5.777777777778	$-1.11x_{10} - 13.44x_2 + 2.89x_3 - 0.89x_4 - 0.33x_5$
$x_8$	8.333333333333	$+0.67x_{10} + 9.67x_2 - 7.33x_3 + 7.33x_4 + 8.00x_5$
$x_9$	10.555555555556	$-0.22x_{10} - 1.89x_2 + 1.78x_3 + 0.22x_4 - 3.67x_5$
$x_1$	1.222222222222	$+0.11x_{10} + 0.44x_2 - 0.89x_3 - 0.11x_4 + 0.33x_5$
$z$	-1.222222222222	$-0.11x_{10} - 1.44x_2 - 0.11x_3 - 0.89x_4 - 1.33x_5$

Primal Dictionary with original objective is:

$x_6$	27.0	$-1.00x_{10}$	$-4.00x_2$	$+5.00x_3$	$+5.00x_4$	$-8.00x_5$
$x_7$	5.77777777778	$-1.11x_{10}$	$-13.44x_2$	$+2.89x_3$	$-0.89x_4$	$-0.33x_5$
$x_8$	8.33333333333	$+0.67x_{10}$	$+9.67x_2$	$-7.33x_3$	$+7.33x_4$	$+8.00x_5$
$x_9$	10.5555555556	$-0.22x_{10}$	$-1.89x_2$	$+1.78x_3$	$+0.22x_4$	$-3.67x_5$
$x_1$	1.22222222222	$+0.11x_{10}$	$+0.44x_2$	$-0.89x_3$	$-0.11x_4$	$+0.33x_5$
$z$	$-1.22222222222$	$-0.11x_{10}$	$+4.56x_2$	$-4.11x_3$	$-3.89x_4$	$-3.33x_5$

## 1 Optimization Phase Simplex

Starting Dictionary is:

$x_6$	27.0	$-1.00x_{10}$	$-4.00x_2$	$+5.00x_3$	$+5.00x_4$	$-8.00x_5$
$x_7$	5.77777777778	$-1.11x_{10}$	$-13.44x_2$	$+2.89x_3$	$-0.89x_4$	$-0.33x_5$
$x_8$	8.33333333333	$+0.67x_{10}$	$+9.67x_2$	$-7.33x_3$	$+7.33x_4$	$+8.00x_5$
$x_9$	10.5555555556	$-0.22x_{10}$	$-1.89x_2$	$+1.78x_3$	$+0.22x_4$	$-3.67x_5$
$x_1$	1.22222222222	$+0.11x_{10}$	$+0.44x_2$	$-0.89x_3$	$-0.11x_4$	$+0.33x_5$
$z$	$-1.22222222222$	$-0.11x_{10}$	$+4.56x_2$	$-4.11x_3$	$-3.89x_4$	$-3.33x_5$

$x_2$  enters and  $x_7$  leaves

$x_6$	25.2809917355	$-0.67x_{10}$	$+0.30x_7$	$+4.14x_3$	$+5.26x_4$	$-7.90x_5$
$x_2$	0.429752066116	$-0.08x_{10}$	$-0.07x_7$	$+0.21x_3$	$-0.07x_4$	$-0.02x_5$
$x_8$	12.4876033058	$-0.13x_{10}$	$-0.72x_7$	$-5.26x_3$	$+6.69x_4$	$+7.76x_5$
$x_9$	9.74380165289	$-0.07x_{10}$	$+0.14x_7$	$+1.37x_3$	$+0.35x_4$	$-3.62x_5$
$x_1$	1.4132231405	$+0.07x_{10}$	$-0.03x_7$	$-0.79x_3$	$-0.14x_4$	$+0.32x_5$
$z$	0.735537190083	$-0.49x_{10}$	$-0.34x_7$	$-3.13x_3$	$-4.19x_4$	$-3.45x_5$

Final Dictionary Solution: 0.735537190083 Num Pivots: 2