The Cozo Database Manual

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CHAPTER

ONE

GETTING STARTED

Welcome to the Cozo Manual. The latest version of this manual can be read at https://cozodb.github.io/current/manual. Alternatively, you can download a PDF version for offline viewing at https://cozodb.github.io/current/manual.pdf.

We aim to make sure that this manual at least touches upon all features currently implemented in Cozo, though the coverage of some topics may be sketchy at this stage.

This manual assumes that you already know the basics of the Cozo database, at the level of the Tutorial¹.

1.1 Downloading Cozo

Cozo is distributed as a single executable. Precompiled binaries can be downloaded from the release $page^2$ on the GitHub repo, which are currently available for Linux (Intel x64), Mac (Intel x64 and Apple ARM) and Windows (Intel x64).

As the build process on Windows is internally very different from UNIX-based systems, the Windows build hasn't received as much attention as the other builds, and may suffer from inferior performance and Windows-specific bugs. For Windows users, we recommend running Cozo under WSL³ if possible, especially if your workload is heavy.

1.2 Starting Cozo

Run the cozoserver command in a terminal:

./cozoserver <PATH_TO_DATA_DIRECTORY>

If <PATH_TO_DATA_DIRECTORY> does not exist, it will be created. Cozo will then start a web server and bind to address 127.0.0.1 and port 9070. These two can be customized: run the executable with the -h option to learn how.

To stop Cozo, type CTRL-C in the terminal, or send SIGTERM to the process with e.g. kill.

¹ https://cozodb.github.io/current/tutorial.html

² https://github.com/cozodb/cozo/releases

³ https://learn.microsoft.com/en-us/windows/wsl/install

1.3 The query API

Queries are run by sending HTTP POST requests to the server. By default, the API endpoint is http://127.0.0. 1:9070/text-query. The structure of the expected JSON payload is:

```
{
    "script": "<COZOSCRIPT QUERY STRING>",
    "params": {}
}
```

params should be an object of named parameters. For example, if you have params set up to be {"num": 1}, then \$num can be used anywhere in your query string where an expression is expected. Always use params instead of constructing query strings yourself when you have parametrized queries.

As an example, the following runs a system op with the curl command line tool:

```
curl -X POST localhost:9070/text-query \
    -H 'content-type: application/json' \
    -d '{"script": "::running", "params": {}}'
```

Warning: Cozo is designed to run in a trusted environment and be used by trusted clients, therefore it does not come with elaborate authentication and security features. If you must access Cozo remotely, you are responsible for setting up firewalls, encryptions and proxies yourself.

As a guard against users carelessly binding Cozo to any address other than 127.0.0.1 and potentially exposing content to everyone on the Internet, in this case, Cozo will generate a token string and require all queries from non-loopback addresses to provide the token string in the HTTP header field x-cozo-auth. The warning printed when you start Cozo with a non-default binding will tell you how to find the token string.

Please note that this "security measure" is not considered sufficient for any purpose and is only a last defence when every other security measure that you are responsible for setting up fails.

1.4 Running queries

1.4.1 Making HTTP requests

As Cozo has a web-based API, it is accessible by all languages that are capable of making web requests. The structure of the API is also deliberately kept minimal so that no dedicated clients are necessary. The return values of requests are JSON when requests are successful, or text descriptions when errors occur, so a language only needs to be able to process JSON to use Cozo.

1.4.2 JupyterLab

JupyterLab⁴ is a web-based notebook interface in the python ecosystem heavily used by data scientists and is the recommended "IDE" of Cozo.

First, install JupyterLab by following the install instructions of the project. Then install the pycozo library by running:

```
pip install "pycozo[pandas]"
```

Now, open the JupyterLab web interface, start a Python 3 kernel, and in a cell run the following magic command⁵:

```
%load_ext pycozo.ipyext_direct
```

If you need to connect to Cozo using a non-default address or port, or you require an authentication string, you need to run the following magic commands as well:

```
%cozo_host http://<BIND_ADDRESS>:<PORT>
%cozo_auth <YOUR_AUTH_STRING>
```

Now you can execute cells as you usually do in JupyterLab, and the content of the cells will be sent to Cozo and interpreted as CozoScript. Returned relations will be formatted as Pandas dataframe⁶.

The above sets up the notebook in the Direct Cozo mode, where cells are default interpreted as CozoScript. You can still execute python code by starting the first line of a cell with the %%py. There is also an Indirect Cozo mode, started by:

```
%load_ext pycozo.ipyext
```

In this mode, only cells with the first line content **%**Cozo are interpreted as CozoScript. Other cells are interpreted in the normal way (by default, python code). Which mode you use depends on your workflow. We recommend the Indirect mode if you have lots of post-processing and visualizations.

When a query is successfully executed, the result will be bound to the python variable _ as a Pandas dataframe (this is a feature of Jupyter notebooks: the Cozo extension didn't do anything extra).

There are a few other useful magic commands:

- %cozo_run_file <PATH_TO_FILE> runs a local file as CozoScript.
- %cozo_run_string <VARIABLE> runs variable containing string as CozoScript.
- %cozo_set <KEY> <VALUE> sets a parameter with the name <KEY> to the expression <VALUE>. The set parameters will be used by subsequent queries.
- %cozo_set_params <PARAM_MAP> replace all parameters by the given expression, which must evaluate to a dictionary with string keys.
- %cozo_clear clears all set parameters.
- %cozo_params returns the parameters currently set.

⁴ https://jupyterlab.readthedocs.io/en/stable/

⁵ https://ipython.readthedocs.io/en/stable/interactive/magics.html

⁶ https://pandas.pydata.org/docs/reference/api/pandas.DataFrame.html

1.4.3 The Makeshift JavaScript Console

The Python and JupyterLab ecosystem is rather heavy-weight. If you are just testing out or running Cozo in an environment that only occasionally requires manual queries, you may be reluctant to install them. In this case, you may find the Makeshift JavaScript Console helpful.

As Cozo is running an HTTP service, we assume that the browser on your local machine can reach its network. We recommend Firefox⁷, Chrome⁸, or any Chromium-based browser for best display.

If Cozo is running under the default configuration, navigate to http://127.0.0.1:9070. You should be greeted with a mostly empty page telling you that Cozo is running. Now open the Developer Console (Firefox console⁹ or Chrome console¹⁰) and switch to the "Console" tab. Now you can execute CozoScript by running:

```
await run("<COZOSCRIPT>")
```

The returned tables will be properly formatted. If you need to pass in parameters, provide a second parameter with a JavaScript object. If you need to set an auth string, modify the global variable COZO_AUTH.

The JavaScript Console is not as nice to use as Jupyter notebooks, but we think that it provides a much better experience than hand-rolled CLI consoles, since you can use JavaScript to manipulate the results.

1.5 Building Cozo from source

If for some reason the binary distribution does not work for you, you can build Cozo from source, which is straightforward.

First, clone the Cozo git repo:

```
git clone https://github.com/cozodb/cozo.git --recursive
```

You need to pass the --recursive flag so that submodules are also cloned. Then you need to install the Rust toolchain¹¹ for your system. You also need a C++17 compiler.

After these preparations, run:

```
cargo build --release
```

in the root of the cloned repo, wait for potentially a long time, and you will find the compiled binary in target/release if everything goes well.

You can run cargo build --release -F jemalloc instead to indicate that you want to compile and use jemalloc as the memory allocator for the RocksDB storage backend, which, depending on your workload, can make a difference in performance.

⁷ https://www.mozilla.org/en-US/firefox/new/

⁸ https://www.google.com/chrome/

⁹ https://firefox-source-docs.mozilla.org/devtools-user/browser_console/index.html

¹⁰ https://developer.chrome.com/docs/devtools/console/javascript/

¹¹ https://www.rust-lang.org/tools/install

1.6 Embedded use

Here "embedded" means running in the same process as your program. As cozoserver is just a very thin wrapper around the Cozo rust library, you can use the library directly in your program.

For languages other than Rust, you will need to provide custom bindings, but again for $Python^{12}$ and $NodeJS^{13}$ this is trivial.

As Cozo uses RocksDB as its storage engine, it probably makes a lot less sense to use embedded Cozo than SQLite, since RocksDB always uses multiple threads and always has background threads running, unlike SQLite for which a connection uses only a single thread.

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¹² https://pyo3.rs/

¹³ https://neon-bindings.com/

CHAPTER

TWO

QUERIES

The Cozo database system is queried using the CozoScript language. At its core, CozoScript is a Datalog¹⁴ dialect supporting stratified negation and stratified recursive meet-aggregations. The built-in utilities and algorithms (mainly graph algorithms) further empower CozoScript for much greater ease of use and much wider applicability.

A query consists of one or many named rules. Each named rule conceptually represents a relation or a table with rows and columns. The rule named? is called the entry to the query, and its associated relation is returned as the result of the query. Each named rule has associated with it a rule head, which names the columns of the relation, and a rule body, which specifies the content of the relation, or how the content should be computed.

In CozoScript, relations (stored relations or relations defined by rules) abide by the *set semantics*, meaning that even if a rule may compute a row multiple times, it will occur only once in the output. This is in contradistinction to SQL.

There are two types of named rules in CozoScript: *inline rules* distinguished by using := to connect the head and the body, and *fixed rules* distinguished by using <~ to connect the head and the body. You may think that *constant rules* with <- constitute a third type, written as:

```
const_rule[a, b, c] <- [[1, 2, 3], [4, 5, 6]]
```

but this is merely syntax sugar for the fixed rule of the Constant utility:

```
const_rule[a, b, c] <~ Constant(data: [[1, 2, 3], [4, 5, 6]])
```

2.1 Inline rules

An example of an inline rule is:

```
hc_rule[a, e] := rule_a['constant_string', b], rule_b[b, d, a, e]
```

The rule body of an inline rule consists of multiple *atoms* joined by commas, and is interpreted as representing the *conjunction* of these atoms.

¹⁴ https://en.wikipedia.org/wiki/Datalog

2.1.1 Atoms

Atoms come in various flavours. In the example above:

```
rule_a['constant_string', b]
```

is an atom representing a *rule application*: a rule named rule_a must exist in the same query and have the correct arity (2 here). Each row in the named rule is then *unified* with the bindings given as parameters in the square bracket: here the first column is unified with a constant string, and unification succeeds only when the string completely matches what is given; the second column is unified with the *variable* b, and as the variable is fresh at this point (meaning that it first appears here), the unification will always succeed and the variable will become *bound*: from this point take on the value of whatever it was unified with in the named relation.

When a bound variable is used again later, for example in rule_b[b, d, a, e], the variable b was bound at this point, this unification will only succeed when the unified value is the same as the previously unified value. In other words, repeated use of the same variable in named rules corresponds to inner joins in relational algebra.

Another flavour of atoms is the *stored relation*. It may be written similarly to a rule application:

```
*stored_relation[bind1, bind2]
```

with the colon in front of the stored relation name to distinguish it from rule application. Written in this way, you must give as many bindings to the stored relation as its arity, and the bindings proceed by argument positions, which may be cumbersome and error-prone. So alternatively, you may use the fact that columns of a stored relation are always named and bind by name:

```
*stored_relation{col1: bind1, col2: bind2}
```

In this case, you only need to bind as many variables as you use. If the name you want to give the binding is the same as the name of the column, you may use the shorthand notation: *stored_relation{col1} is the same as *stored_relation{col1: col1}.

Expressions are also atoms, such as:

```
a > b + 1
```

Here a and b must be bound somewhere else in the rule, and the expression must evaluate to a boolean, and act as a *filter*: only rows where the expression evaluates to true are kept.

You can also use *unification atoms* to unify explicitly:

```
a = b + c + d
```

for such atoms, whatever appears on the left-hand side must be a single variable and is unified with the right-hand side. This is different from the equality operator ==, where both sides are merely required to be expressions. When the left-hand side is a single *bound* variable, it may be shown that the equality and the unification operators are semantically equivalent.

Another form of *unification atom* is the explicit multi-unification:

```
a in [x, y, z]
```

here the variable on the left-hand side of in is unified with each item on the right-hand side in turn, which in turn implies that the right-hand side must evaluate to a list (but may be represented by a single variable or a function call).

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2.1.2 Head and returned relation

Atoms, as explained above, corresponds to either relations (or their projections) or filters in relational algebra. Linked by commas, they, therefore, represent a joined relation, with named columns. The *head* of the rule, which in the simplest case is just a list of variables, then defines whichever columns to keep, and their order in the output relation.

Each variable in the head must be bound in the body, this is one of the *safety rules* of Datalog. Not all variables appearing in the body need to appear in the head.

2.1.3 Multiple definitions and disjunction

For inline rules only, multiple rule definitions may share the same name, with the requirement that the arity of the head in each definition must match. The returned relation is then the *disjunction* of the multiple definitions, which correspond to *union* in SQL. *Intersect* in SQL can be written in CozoScript into a single rule since commas denote conjunction. In complicated situations, you may instead write disjunctions in a single rule with the explicit or operator:

```
rule1[a, b] := rule2[a] or rule3[a], rule4[a, b]
```

For completeness, there is also an explicit and operator, but it is semantically identical to the comma, except that it has higher operator precedence than or, which in turn has higher operator precedence than the comma.

During evaluation, each rule is canonicalized into disjunction normal form¹⁵ and each clause of the outmost disjunction is treated as a separate rule. The consequence is that the safety rule may be violated even though textually every variable in the head occurs in the body. As an example:

```
rule[a, b] := rule1[a] or rule2[b]
```

is a violation of the safety rule since it is rewritten into two rules, each of which is missing a different binding.

2.1.4 Negation

Atoms in inline rules may be *negated* by putting **not** in front of them, as in:

```
not rule1[a, b]
```

When negating rule applications and stored relations, at least one binding must be bound somewhere else in the rule in a non-negated context: this is another safety rule of Datalog, and it ensures that the outputs of rules are always finite. The unbound bindings in negated rules remain unbound: negation cannot introduce bound bindings to be used in the head.

Negated expressions act as negative filters, which is semantically equivalent to putting! in front of the expression. Since negation does not introduce new bindings, unifications and multi-unifications are converted to equivalent expressions and then negated.

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¹⁵ https://en.wikipedia.org/wiki/Disjunctive normal form

2.1.5 Recursion and stratification

The body of an inline rule may contain rule applications of itself, and multiple inline rules may apply each other recursively. The only exception is the entry rule?, which cannot be referred to by other rules.

Self and mutual references allow recursion to be defined easily. To guard against semantically pathological cases, recursion cannot occur in negated positions: the Russell-style rule $r[a] := not \ r[a]$ is not allowed. This requirement creates an ordering of the rules, since negated rules must evaluate to completion before rules that apply them can start evaluation: this is called *stratification* of the rules. In cases where a total ordering cannot be defined since there exists a loop in the ordering required by negation, the query is then deemed unstratifiable and Cozo will refuse to execute it.

Note that since CozoScript allows unifying fresh variables, you can still easily write programs that produce infinite relations and hence cannot complete through recursion, but that are still accepted by the database. One of the simplest examples is:

```
r[a] := a = 0
r[a] := r[b], a = b + 1
?[a] := r[a]
```

It is up to the user to ensure that such programs are not submitted to the database, as it is not even in principle possible for the database to rule out such cases without wrongly rejecting valid queries. If you accidentally submitted one, you can refer to the system ops section for how to terminate long-running queries. Or you can give a timeout for the query when you submit.

2.1.6 Aggregation

CozoScript supports aggregations, as does SQL, which provides a very useful extension to pure relational algebra. In CozoScript, aggregations are specified for inline rules by applying aggregation operators to variables in the rule head, as in:

```
?[department, count(employee)] := *personnel{department, employee}
```

here we have used the count operator familiar to all SQL users. The semantics is that any variables in the head without aggregation operators are treated as *grouping variables*, similar to what appears in a GROUP BY clause in SQL, and the aggregation is applied using the grouping variables as keys. If you do not specify any grouping variables, then you get at most one row as the return value.

As we now understand, CozoScript follows relational algebra with set semantics. With the introduction of aggregations, the situation is a little bit more complicated, as aggregations are applied to the relation resulting from the body of the rule using bag semantics, and the resulting relation of the rule, after aggregations are applied, follows set semantics. The reason for this complication is that if aggregations are applied with set semantics, then the following query:

```
?[count(employee)] := *personnel{employee}
```

does not do what you expect: it either returns a row with a single value 1 if there are any matching rows, or it returns nothing at all if the stored relation *personnel is empty. Though semantically sound, this behaviour is not useful at all. So for aggregations, we opt for bag semantics, and the query does what one expects.

If a rule has several definitions, they must have identical aggregations applied in the same positions, otherwise, the query will be rejected. The reason is that in complicated situations the semantics is ambiguous and counter-intuitive if we do allow it.

Existing database systems do not usually allow aggregations through recursion, since in many cases, it is difficult to give useful semantics to such queries. In CozoScript we allow aggregations for self-recursion for a limited subset of aggregation operators, the so-called *semi-lattice aggregations*, such as the following example shows:

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```
shortest_distance[destination, min(distance)] := route{source: 'A', destination,
    distance}
shortest_distance[destination, min(distance)] :=
    shortest_distance[existing_node, prev_distance], # recursion
    route{source: existing_node, distance: route_distance},
    distance = prev_distance + route_distance
?[destination, min_distance] := shortest_distance[destination, min_distance]
```

this query computes the shortest distances from a node to all nodes using the min aggregation operator.

Concerning stratification, if a rule has aggregations in its head, then any rule that contains it in an atom must be in a higher stratum, unless that rule is the same rule (self-recursion) and all aggregations in its head are semi-lattice aggregations.

Consult the dedicated chapter for the aggregation operators available.

2.2 Fixed rules

The body of a fixed rule starts with the name of the utility or algorithm being applied, then takes a specified number of named or stored relations as its *input relations*, followed by *options* that you provide. The following query is a calculation of PageRank:

```
?[] <~ PageRank(*route[], theta: 0.5)</pre>
```

In the above example, the relation *route is the single input relation expected. Input relations may be stored relations or relations resulting from rules. Each utility/algorithm expects specific shapes of input relations, for example, PageRank expects the first two columns of the relation to denote the source and destination of links in a graph. You must consult the documentation for each utility/algorithm to understand its API. In fixed rules, bindings for input relations are usually omitted, but sometimes if they are provided they are interpreted and used in case-specific ways, for example in the DFS algorithm bindings can be used to construct an expression for testing the termination condition. In the example given above, theta is an option of the algorithm, which is required by the API to be an expression evaluating to a constant. Each utility/algorithm expects specific types for the options; some options have default values and may be omitted.

Each fixed rule has a determinate output arity, deduced from the specific utility/algorithm being applied and the options given. Usually, you omit the bindings in the rule head, as we do above, but if you do provide bindings, the arities must match.

In terms of stratification, each fixed rule lives in its own stratum: it is evaluated after all rules it depends on are completely evaluated, and all rules depending on the output relation of a fiex rule start evaluation only after complete evaluation of the fixed rule. In particular, unlike inline rules, there is no early termination even if the output relation is for the entry rule.

2.3 Query options

Each query can have query options associated with it:

```
?[name] := *personnel{name}
:limit 10
:offset 20
```

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In the example, :limit and :offset are query options, with familiar meanings from SQL. All query options start with a single colon :. Queries options can appear before or after rules, or even sandwiched between rules. Use this freedom for better readability.

Several query options deal with transactions for the database. Those will be discussed in the chapter on stored relations and transactions. Here we explain query options that exclusively affect the query itself.

:limit <N>

Limit output relation to at most <N> rows. If possible, execution will stop as soon as this number of output rows is collected.

:offset <N>

Skip the first <N> rows of the returned relation.

:timeout <N>

Abort if the query does not complete within <N> seconds. Seconds may be specified as an expression so that random timeouts are possible.

:sleep <N>

If specified, the query will wait for <N> seconds after completion, before committing or proceeding to the next query. Seconds may be specified as an expression so that random timeouts are possible. This is useful for deliberately interleaving concurrent queries to test for complex logic.

:sort <SORT_ARG> (, <SORT_ARG>)*

Sort the output relation before applying other options or returning. Specify <SORT_ARG> as they appear in the rule head of the entry, separated by commas. You can optionally specify the sort direction of each argument by prefixing them with + or -, with minus denoting descending sort. As an example, :sort -count(employee), dept_name sorts by employee count descendingly first, then break ties with department name in ascending alphabetical order. Note that your entry rule head must contain both dept_name and count(employee): aggregations must be done in inline rules, not in output sorting. :order is an alias for :sort.

:assert none

With this option, the query returns nothing if the output relation is empty, otherwise execution aborts with an error. Essential for transactions and triggers.

:assert some

With this option, the query returns nothing if the output relation contains at least one row, otherwise, execution aborts with an error. Execution of the query stops as soon as the first row is produced if possible. Essential for transactions and triggers.

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STORED RELATIONS AND TRANSACTIONS

Persistent databases store data on disk. As Cozo is a relational database, data are stored in *stored relations* on disk, which is analogous to tables in SQL databases.

3.1 Stored relations

We already know how to query stored relations: use the *relation[...] or *relation{...} atoms in inline or fixed rules. To manipulate stored relations, use one of the following query options:

:create <NAME> <SPEC>

Creates a stored relation with the given name and the given spec. The named stored relation must not exist before. If a query is specified, data from the resulting relation is put into the created stored relation. This is the only stored relation-related query option in which a query may be omitted.

:replace <NAME> <SPEC>

This is similar to :create, except that if the named stored relation exists beforehand, it is completely replaced. The schema of the replaced relation need not match the new one. You cannot omit the query for :replace.

:put <NAME> <SPEC>

Put data from the resulting relation into the named stored relation. If keys from the data exist beforehand, the rows are simply replaced with new ones.

:ensure <NAME> <SPEC>

Ensures that rows specified by the output relation and spec already exist in the database and that no other process has written to these rows at commit since the transaction starts. Useful for ensuring read-write consistency.

:rm <NAME> <SPEC>

Remove data from the resulting relation from the named stored relation. Only keys are used. If a row from the resulting relation does not match any keys, nothing happens for that row, and no error is raised.

:ensure_not <NAME> <SPEC>

Ensures that rows specified by the output relation and spec do not exist in the database and that no other process has written to these rows at commit since the transaction starts. Useful for ensuring read-write consistency.

You can rename and remove stored relations with the system ops ::relation rename and ::relation remove, described in the system op chapter.

3.1.1 Create and replace

The format of <SPEC> is identical for all four ops, whereas the semantics is a bit different.

We first describe the format and semantics for :create and :replace. A spec is a specification for columns, enclosed in curly braces {} and separated by commas:

```
?[address, company_name, department_name, head_count] <- $input_data

:create dept_info {
   company_name: String,
   department_name: String,
   =>
   head_count: Int,
   address: String,
}
```

Columns before the symbol => form the *keys* (actually, a composite key) for the stored relation, and those after it form the *values*. If all columns are keys, the symbol => may be omitted altogether. The order of columns matters in the specification, especially for keys, as data is stored in lexicographically sorted order in trees, which has implications for data access in queries. Each key corresponds to a single value.

In the above example, we explicitly specified the types for all columns. Type specification is described in its own chapter. If the types of the rows do not match the specified types, the system will first try to coerce the values, and if that fails, the query is aborted. You can selectively omit types for columns, and columns with types omitted will have the type Any?, which is valid for any value. As an example, if you do not care about type validation, the above query can be written as:

```
?[address, company_name, department_name, head_count] <- $input_data
:create dept_info { company_name, department_name => head_count, address }
```

In the example, the bindings for the output match the columns exactly (though not in the same order). You can also explicitly specify the correspondence:

```
?[a, b, count(c)] <- $input_data

:create dept_info {
   company_name = a,
   department_name = b,
   =>
   head_count = count(c),
   address: String = b
}
```

You *must* use explicit correspondence if the entry head contains aggregation. The address field shows how to specify both a type and a correspondence.

Instead of specifying bindings, you can specify an expression to generate values:

```
?[a, b] <- $input_data

:create dept_info {
   company_name = a,
   department_name = b,</pre>
```

(continues on next page)

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```
=>
  head_count default 0,
  address default ''
}
```

The expression is evaluated once for each row, so for example if you specified one of the UUID-generating functions, you will get a different UUID for each row.

3.1.2 Put, remove, ensure and ensure-not

For :put, :remove, :ensure and :ensure_not, you do not need to specify all existing columns in the spec if the omitted columns have a default generator, in which case the generator will be used to generate a value, or the type of the column is nullable, in which case the value is null. The spec specified when the relation was created will be consulted to know how to store data correctly. Specifying default values does not have any effect and will not replace existing ones.

For :put and :ensure, the spec needs to contain enough bindings to generate all keys and values. For :rm and :ensure_not, it only needs to generate all keys.

3.2 Chaining queries

Each script you send to Cozo is executed in its own transaction. To ensure consistency of multiple operations on data, You can define multiple queries in a single script, by wrapping each query in curly braces {}. Each query can have its independent query options. Execution proceeds for each query serially, and aborts at the first error encountered. The returned relation is that of the last query. Within a transaction, execution of queries adheres to multi-version concurrency control: only data that are already committed, or written within the same transaction, are read, and at the end of the transaction, any changes to stored relations are only committed if there are no conflicts and no errors are raised.

The :assert, :ensure and :ensure_not query options allow you to express complicated constraints that must be satisfied for your transaction to commit.

3.3 Triggers and indices

Cozo does not have traditional indices on stored relations. You must define your indices as separate stored relations yourself, for example by having a relation containing identical data but in different column order. More complicated and exotic "indices" are also possible and used in practice. At query time, you explicitly query the index instead of the original stored relation.

You synchronize your indices and the original by ensuring that any mutations you do on the database write the correct data to the "canonical" relation and its indices in the same transaction. As doing this by hand for every mutation in your business logic leads to lots of repetitions, is error-prone and a maintenance nightmare, Cozo also supports *triggers* to do it automatically for you.

You attach triggers to a stored relation by running the system op ::relation set_triggers:

```
::relation set_triggers relation_name

on put { <QUERY> }
on put { <QUERY> } # you can specify as many triggers as you need
```

(continues on next page)

(continued from previous page)

```
on rm { <QUERY> }
on replace { <QUERY> }
```

You can have anything valid query for <QUERY>.

The on put queries will run when any data is inserted into the relation, which can be triggered by :put, :create and :replace query options. The implicitly defined rules _new[] and _old[] can be used in the queries, and contain the added rows, and the replaced rows (if any).

The on rm queries will run when deletion is triggered by the :rm query option. The implicitly defined rules _new[] and _old[] can be used in the queries, the first rule contains the keys of the rows for deletion, and the second rule contains the rows actually deleted, with both keys and non-keys.

The on replace queries will run when :replace query options are run. They are run before any on put triggers are run for the same stored relation.

All triggers for a relation must be specified together, in the same system op. In other words, ::relation set_triggers simply replaces all the triggers associated with a stored relation. To remove all triggers from a stored relation, simply pass no queries for the system op.

As a very simple example of using triggers to make index, let's say we have the following relation:

```
:create rel {a => b}
```

However, we often want to use *rel[a, b] with b bound but a unbound. This will cause a full scan, which can be expensive. So we really need an index:

```
:create rel.rev {b, a}
```

In the generate case, we cannot assume a functional dependency $b \Rightarrow a$, so here both fields appear as keys.

To manage the index automatically, simply do:

```
::relation set_triggers rel

on put {
    ?[a, b] := _new[a, b]
    :put rel.rev{ b, a }
}
on rm {
    ?[a, b] := _old[a, b]
    :rm rel.rev{ b, a }
}
```

With the index set up, you can use *rel.rev{..} in place of *rel{..} in your queries.

Indices in Cozo are manual, but extremely flexible, since you need not conform to any predetermined patterns in your use of <code>_old[]</code> and <code>_new[]</code>. You also need to explicitly use the indices in your query: there is no "query optimization" for them. For simple queries, this can seem cumbersome, but for complex ones, the deterministic evaluation entailed can be a huge blessing.

Besides indices, creative use of triggers abounds, but you must consider the maintenance burden they introduce.

Warning: Do not introduce loops in your triggers. A loop occurs when a relation has triggers which affect other relations, which in turn have other triggers that ultimately affect the starting relation.

CHAPTER

FOUR

SYSTEM OPS

System ops start with a double-colon :: and must appear alone in a script. In the following, we explain what each system op does, and the arguments they expect.

4.1 Explain

::explain { <query> }

A single query is enclosed in curly braces. Query options are allowed but ignored. The query is not executed, but its query plan is returned instead. Currently, there is no specification for the return format, but if you are familiar with the semi-naïve evaluation of stratified Datalog programs subject to magic-set rewrites, the returned data is pretty self-explanatory.

4.2 Ops on stored relations

::relations

List all stored relations currently in the database

::columns <REL_NAME>

List all columns for the stored relation <REL_NAME>.

::remove <REL_NAME> (, <REL_NAME>)*

Remove stored relations. Several can be specified, joined by commas.

```
::rename <OLD_NAME> -> <NEW_NAME> (, <OLD_NAME> -> <NEW_NAME>)*
```

Rename stored relation <OLD_NAME> into <NEW_NAME>. Several may be specified, joined by commas.

::show_triggers <REL_NAME>

Display triggers associated with the stored relation <REL_NAME>.

::set_triggers <REL_NAME> <TRIGGERS>

Set triggers for the stored relation <REL_NAME>. This is explained in more detail in the transactions chapter.

::access_level <REL_NAME> <ACCESS_LEVEL>

Sets the access level of <REL_NAME> to the given level. The levels are:

- normal allows everything,
- protected disallows ::remove and :replace,
- read_only additionally disallows any mutations and setting triggers,
- hidden additionally disallows any data access (metadata access via ::relations, etc., are still allowed).

It is recommended to give the appropriate access levels to tables to prevent data loss from programming mistakes.

4.3 Monitor and kill

::running

Display currently running queries and their IDs.

::kill <ID>

Kill a running query specified by <ID>. The ID may be obtained by ::running.

4.4 Maintenance

::compact

Run compaction on the database. Running this may make the database smaller on disk and faster for queries, but running the op itself may take some time in the background.

CHAPTER

FIVE

DATATYPES

5.1 Value types

A runtime value in Cozo can be of the following *value-types*:

- Null
- Bool
- Number
- String
- Bytes
- Uuid
- List

Number can be Float (double precision) or Int (signed, 64 bits). Cozo will auto-promote Int to Float when necessary.

List can contain any number of mixed-type values, including other lists.

Cozo sorts values according to the above order, e.g. null is smaller than true, which is in turn smaller than the list [].

Within each type values are *compared* according to logic custom to each type:

- false < true;
- -1 == -1.0 < 0 == 0.0 < 0.5 == 0.5 < 1 == 1.0 (however, see the caveat below);
- Lists are ordered lexicographically by their elements;
- Bytes are compared lexicographically;
- Strings are ordered lexicographically by their UTF-8 byte representations.
- UUIDs are sorted in a way that UUIDv1 with similar timestamps are near each other. This is to improve data locality and should be considered an implementation detail. Depending on the order of UUID in your application is not recommended.

Warning: Because there are two internal number types Int and Float under the umbrella type Number, sorting numbers can be more complex than anticipated.

When sorting, the integer always comes before the equivalent float. For example, 1.0 = 1, 1.0 > 1 and 1.0 < 1 all evaluate to true, but when sorting 1 and 1.0 are two _different_ values and 1 is placed before 1.0.

This may create problems when applying aggregations since if a grouping key contains both 1.0 and 1, they are treated as separate group headings. In such cases, it may help to use explicit coercion to_float or round to coerce all sorted values to the same type.

5.2 Value literals

The standard notations null for the type Null, false and true for the type Bool are followed.

Besides the usual decimal notation for signed integers, you can prefix a number with 0x or -0x for hexadecimal notation, with 0x or -0x for octal notation, or with 0x or -0x for binary notation. Floating point numbers include the decimal dot, which may be trailing, and may be in scientific notation. All numbers may include underscores _ in their representation for clarity. For example, 299_792_458 is the speed of light in meters per second.

Strings can be typed in the same way as they do in JSON between double quotes "", with the same escape rules. You can also use single quotes ' ' in which case the roles of the double quote and single quote are switched. In addition, there is a raw string notation:

```
r___"I'm a raw string with "quotes"!"___
```

A raw string starts with the letter \mathbf{r} followed by an arbitrary number of underscores, and then a double quote. It terminates when followed by a double quote and the same number of underscores. Everything in between is interpreted exactly as typed, including any newlines.

There is no literal representation for Bytes or Uuid due to restrictions placed by JSON. You must pass in its Base64 encoding for bytes, or hyphened strings for UUIDs, and use the appropriate functions to decode it. If you are just inserting data into a stored relation with a column specified to contain bytes or UUIDs, auto-coercion will kick in.

Lists are items enclosed between square brackets [], separated by commas. A trailing comma is allowed after the last item.

5.3 Column types

The following *atomic types* can be specified for columns in stored relations:

- Int
- Float
- Bool
- String
- Bytes
- Uuid

There is no Null type. Instead, if you put a question mark after a type, it is treated as *nullable*, meaning that it either takes value in the type or is null.

Two composite types are available. A *homogeneous list* is specified by square brackets, with the inner type in between, like this: [Int]. You may optionally specify how many elements are expected, like this: [Int; 10]. A *heterogeneous list*, or a *tuple*, is specified by round brackets, with the element types listed by position, like this: (Int, Float, String). Tuples always have fixed lengths.

A special type Any can be specified, allowing all values except null. If you want to allow null as well, use Any?. Composite types may contain other composite types or Any types as their inner types.

CHAPTER

SIX

QUERY EXECUTION

Usually, in a database, how queries are executed is usually considered an implementation detail hidden behind an abstraction barrier, which normal users need not care about. The idea is that databases will take advantage of this abstraction barrier by using query optimizers to choose the best query plan, regardless of how the query was originally written. As everyone knows, however, this abstraction barrier is leaky, since bad query execution plans invariably occur and hurt performance. The problem is especially severe when dealing with graphs, since graph traversals generally use a lot more joins than non-graph queries, and the reliability of even the best query optimizer decreases exponentially with the number of joins.

In Cozo we take the pragmatic approach and assume that the user eventually knows (or should know) what is the best way to query their data. This is certainly true for those developers who spend hours "coercing" the query optimizers to use a query plan that the user intends, sometimes in rather convoluted ways. In Cozo, no coercion is necessary since the query execution is completely determined by how the query is written: there is no stats-based query planning involved. In our experience, this saves quite a lot of developer time, since developers eventually learn how to write efficient queries naturally, and after they do, they no longer have to deal with endless "query de-optimizations".

6.1 Stratification

As discussed in the chapter on queries, Cozo sees a query as a set of named rules. Fixed rules are left as they are, and inline rules are converted into disjunctive normal forms. After conversion, all inline rules consist of conjunction of atoms only, and negation only occurs for the leaf atoms.

The next step towards executing the query is *stratifying* the rules. Stratification begins by making a graph of the named rules, with the rules themselves as nodes, and a link is added between two nodes when one of the rules applies the other. This application is through atoms for inline rules, and input relations for fixed rules. Now some of the links are labelled *stratifying*: when an inline rule applies another rule through negation, when an inline rule applies another inline rule that contains aggregations, when an inline rule applies itself and it has non-semi-lattice, when an inline rule applies another rule which is a fixed rule, or when a fixed rule has another rule as an input relation. The strongly connected components of this graph are then determined and tested, and if it found that some strongly connected component contains a stratifying link, the graph is deemed *unstratifiable*, and the execution aborts. Otherwise, Cozo will topologically sort the strongly connected components to determine a *stratification* of the rules: rules within the same stratum are logically executed together, and no two rules within the same stratum can have a stratifying link between them. In this process, Cozo will merge the strongly connected components into as few supernodes as possible while still maintaining the restriction on stratifying links. The resulting strata are then passed on to be processed in the next step.

You can see the stratum number assigned to rules by using the ::explain system op.

6.2 Magic set rewrites

Within each stratum, the input rules are rewritten using a technique called magic sets. In intuitive terms, this rewriting is to ensure that the query execution does not waste time calculating results that are then simply discarded. As an example, consider:

```
reachable[a, b] := link[a, n]
reachable[a, b] := reachable[a, c], link[c, b]
?[r] := reachable['A', r]
```

Without magic set rewrites, the whole reachable relation is generated first, then most of them are thrown away, keeping only those starting from 'A'. Magic set avoids this problem. How the rewrite proceeds is rather technical, but you can see the results in the output of ::explain.

The rewritten query is guaranteed to yield the same relation for ?, and will in general yield fewer intermediate rows.

Currently, the rewrite applies only to inline rules without aggregations. So for the moment being, you may need to manually constrain some of your rules.

6.3 Semi-naïve evaluation

Now each stratum contains either a single fixed rule or a set of inline rules. The single fixed rule case is easy: just run the specific implementation of the rule. In the case of the inline rules, each of the rules is assigned an output relation. Assuming we know how to evaluate each rule given all the relations it depends on, the semi-naïve algorithm can now be applied to the rules to yield all output rows.

The semi-naïve algorithm is a bottom-up evaluation strategy, meaning that it tries to deduce all facts from a set of given facts. By contrast, top-down strategies start with stated goals and try to find proof for the goals. Bottom-up strategies have many advantages over top-down ones when the whole output of each rule is needed, but may waste time generating unused facts if only some of the output is kept. Magic set rewrites are introduced to eliminate precisely this weakness.

6.4 Ordering of atoms

Now we discuss how a single definition of an inline rule is evaluated. We know from the query chapter that the body of the rule contains atoms, and after conversion to disjunctive normal forms, all atoms are linked by conjunction, and each atom can only be one of the following:

- an explicit unification,
- applying a rule or a stored relation,
- an expression, which should evaluate to a boolean,
- a negation of an application.

The first two cases may introduce fresh bindings, whereas the last two cannot. The atoms are then reordered: all atoms that introduce new bindings stay where they are, whereas all atoms that do not introduce new bindings are moved to the earliest possible place where all their bindings are bound. In fact, all atoms that introduce bindings correspond to joining with a pre-existing relation followed by projections in relational algebra, and all atoms that do not correspond to filters. The idea is to apply filters as early as possible to minimize the number of rows before joining with the next relation.

This procedure is completely deterministic. When writing the body of rules, we therefore should aim to minimize the total number of rows generated. A strategy that works almost in all cases is to put the most restrictive atoms which generate new bindings first, as this can make the left relation in each join small.

6.5 Relations as indices

Next, we need to understand how a single atom which generates new bindings is processed.

For the case of unification, it is simple: the right-hand side of the unification, which is an expression with all variables bound, is simply evaluated, and the result is joined to the current relation (as in a map-cat operation in functional languages).

For the case of the application of relations, the first thing to understand is that all relations in Cozo are conceptually trees. All the bindings of relations generated by inline or fixed rules, and the keys of stored relations, act as a composite key for the tree. The access complexity is therefore determined by whether a key component is bound. For example, the following application:

```
a_rule['A', 'B', c]
```

with c unbound is very efficient, since this corresponds to a prefix scan in the tree with the key prefix ['A', 'B'], whereas the following application:

```
a_rule[a, 'B', 'C']
```

where a is unbound is very expensive, since we must do a full relation scan. On the other hand, if a is bound, then this is only a logarithmic-time check.

For stored relations, you need to check its schema for the order of keys to deduce the complexity. The system op ::explain may also give you some information.

6.6 Early stopping

Within each stratum, rows are generated in a streaming fashion. For the entry rule ?, if :limit is specified as a query option, a counter is used to monitor how many valid rows are already generated. If enough rows are generated, the query stops. Note that this only works when the entry rule is inline, and when you are *not* specifying :order.

FUNCTIONS

Functions can be used in expressions in Cozo. All function arguments in Cozo are immutable. All functions except those having names starting with rand_ are deterministic.

Internally, all function arguments are partially evaluated before binding variables to input tuples. For example, the regular expression in regex_matches(var, '[a-zA-Z]+') will only be compiled once during the execution of the query, instead of being repeatedly compiled for every input tuple.

7.1 Equality and Comparisons

```
eq(x, y)
```

Equality comparison. The operator form is x == y or x = y. The two arguments of the equality can be of different types, in which case the result is false.

neq(x, y)

Inequality comparison. The operator form is x != y. The two arguments of the equality can be of different types, in which case the result is true.

```
gt(x, y)
```

Equivalent to x > y

ge(x, y)

Equivalent to x >= y

lt(x, y)

Equivalent to x < y

le(x, y)

Equivalent to $x \ll y$

Note: The four comparison operators can only compare values of the same value type. Integers and floats are of the same type Number.

```
\max(x,...)
```

Returns the maximum of the arguments. Can only be applied to numbers.

min(x,...)

Returns the minimum of the arguments. Can only be applied to numbers.

7.2 Boolean functions

```
and(...)
      Variadic conjunction. For binary arguments it is equivalent to x && y.
or(...)
      Variadic disjunction. For binary arguments it is equivalent to x \mid \mid y.
negate(x)
      Negation. Equivalent to !x.
assert(x,...)
      Returns true if x is true, otherwise will raise an error containing all its arguments as the error message.
7.3 Mathematics
add(...)
      Variadic addition. The binary version is the same as x + y.
sub(x, y)
      Equivalent to x - y.
mul(...)
      Variadic multiplication. The binary version is the same as x * y.
div(x, y)
      Equivalent to x / y.
minus(x)
      Equivalent to -x.
pow(x, y)
      Raises x to the power of y. Equivalent to x ^ y. Always returns floating number.
mod(x, y)
      Returns the remainder when x is divided by y. Arguments can be floats. The returned value has the same sign
      as x. Equivalent to x % y.
abs(x)
      Returns the absolute value.
signum(x)
      Returns 1, 0 or -1, whichever has the same sign as the argument, e.g. signum(to_float('NEG_INFINITY'))
      ==-1, signum(0.0) == 0, but signum(-0.0) ==-1. Returns NAN when applied to NAN.
floor(x)
      Returns the floor of x.
ceil(x)
      Returns the ceiling of x.
round(x)
      Returns the nearest integer to the argument (represented as Float if the argument itself is a Float). Round halfway
      cases away from zero. E.g. round(0.5) == 1.0, round(-0.5) == -1.0, round(1.4) == 1.0.
```

```
exp(x)
      Returns the exponential of the argument, natural base.
exp2(x)
      Returns the exponential base 2 of the argument. Always returns a float.
ln(x)
      Returns the natual logarithm.
log2(x)
      Returns the logarithm base 2.
log10(x)
      Returns the logarithm base 10.
sin(x)
      The sine trigonometric Func.
\cos(x)
      The cosine trigonometric Func.
tan(x)
     The tangent trigonometric Func.
asin(x)
      The inverse sine.
acos(x)
      The inverse cosine.
atan(x)
      The inverse tangent.
atan2(x, y)
      The inverse tangent atan2^{16} by passing x and y separately.
sinh(x)
      The hyperbolic sine.
cosh(x)
      The hyperbolic cosine.
tanh(x)
      The hyperbolic tangent.
asinh(x)
     The inverse hyperbolic sine.
acosh(x)
      The inverse hyperbolic cosine.
atanh(x)
      The inverse hyperbolic tangent.
deg_to_rad(x)
     Converts degrees to radians.
```

16 https://en.wikipedia.org/wiki/Atan2

^{7.3.} Mathematics 29

rad_to_deg(x)

Converts radians to degrees.

$haversine(a_lat, a_lon, b_lat, b_lon)$

Computes with the haversine formula¹⁷ the angle measured in radians between two points a and b on a sphere specified by their latitudes and longitudes. The inputs are in radians. You probably want the next function since most maps measure angles in radians.

haversine_deg_input(a_lat, a_lon, b_lat, b_lon)

Same as the previous function, but the inputs are in degrees instead of radians. The return value is still in radians. If you want the approximate distance measured on the surface of the earth instead of the angle between two points, multiply the result by the radius of the earth, which is about 6371 kilometres, 3959 miles, or 3440 nautical miles.

Warning: The haversine formula, when applied to the surface of the earth, which is not a perfect sphere, can result in an error of less than one percent.

7.4 String functions

length(str)

Returns the number of Unicode characters in the string.

Can also be applied to a list or a byte array.

Warning: length(str) does not return the number of bytes of the string representation. Also, what is returned depends on the normalization of the string. So if such details are important, apply unicode_normalize before length.

concat(x, ...)

Concatenates strings. Equivalent to x ++ y in the binary case.

Can also be applied to lists.

$str_includes(x, y)$

Returns true if x contains the substring y, false otherwise.

lowercase(x)

Convert to lowercase. Supports Unicode.

uppercase(x)

Converts to uppercase. Supports Unicode.

trim(x)

Removes whitespace¹⁸ from both ends of the string.

trim_start(x)

Removes whitespace¹⁹ from the start of the string.

¹⁷ https://en.wikipedia.org/wiki/Haversine_formula

¹⁸ https://en.wikipedia.org/wiki/Whitespace_character

¹⁹ https://en.wikipedia.org/wiki/Whitespace_character

trim_end(x)

Removes whitespace²⁰ from the end of the string.

$starts_with(x, y)$

Tests if x starts with y.

Tip: starts_with(var, str) is prefered over equivalent (e.g. regex) conditions, since the compiler may more easily compile the clause into a range scan.

$ends_with(x, y)$

tests if x ends with y.

unicode_normalize(str, norm)

Converts str to the normalization²¹ specified by norm. The valid values of norm are 'nfc', 'nfd', 'nfkc' and 'nfkd'.

chars(str)

Returns Unicode characters of the string as a list of substrings.

from_substrings(list)

Combines the strings in list into a big string. In a sense, it is the inverse function of chars.

Warning: If you want substring slices, indexing strings, etc., first convert the string to a list with chars, do the manipulation on the list, and then recombine with from_substring. Hopefully, the omission of functions doing such things directly can make people more aware of the complexities involved in manipulating strings (and getting the *correct* result).

7.5 List functions

list(*x*,...)

Constructs a list from its argument, e.g. list(1, 2, 3). Equivalent to the literal form [1, 2, 3].

is_in(el, list)

Tests the membership of an element in a list.

first(l)

Extracts the first element of the list. Returns null if given an empty list.

last(l)

Extracts the last element of the list. Returns null if given an empty list.

get(l, n)

Returns the element at index n in the list 1. This function will raise an error if the access is out of bounds. Indices start with 0.

$maybe_get(l, n)$

Returns the element at index n in the list 1. This function will return null if the access is out of bounds. Indices start with 0.

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 $^{^{20}\} https://en.wikipedia.org/wiki/Whitespace_character$

²¹ https://en.wikipedia.org/wiki/Unicode_equivalence

```
length(list)
     Returns the length of the list.
     Can also be applied to a string or a byte array.
slice(l, start, end)
     Returns the slice of list between the index start (inclusive) and end (exclusive). Negative numbers may be
     used, which is interpreted as counting from the end of the list. E.g. slice([1, 2, 3, 4], 1, 3) == [2, 3]
     3], slice([1, 2, 3, 4], 1, -1) == [2, 3].
concat(x, ...)
     Concatenates lists. The binary case is equivalent to x ++ y.
     Can also be applied to strings.
prepend(l, x)
     Prepends x to 1.
append(l, x)
     Appends x to 1.
reverse(l)
     Reverses the list.
sorted(l)
     Sorts the list and returns the sorted copy.
chunks(l, n)
     Splits the list 1 into chunks of n, e.g. chunks ([1, 2, 3, 4, 5], 2) == [[1, 2], [3, 4], [5]].
chunks_exact(l, n)
     Splits the list 1 into chunks of n, discarding any trailing elements, e.g. chunks ([1, 2, 3, 4, 5], 2) ==
      [[1, 2], [3, 4]].
windows(l, n)
     Splits the list 1 into overlapping windows of length n. e.g. windows ([1, 2, 3, 4, 5], 3) == [[1, 2,
      3], [2, 3, 4], [3, 4, 5]].
union(x, y, ...)
     Computes the set-theoretic union of all the list arguments.
intersection(x, y, ...)
     Computes the set-theoretic intersection of all the list arguments.
difference(x, y, ...)
     Computes the set-theoretic difference of the first argument with respect to the rest.
```

7.6 Binary functions

```
length(bytes)
```

Returns the length of the byte array.

Can also be applied to a list or a string.

```
bit_and(x, y)
```

Calculate the bitwise and. The two bytes must have the same lengths.

$bit_or(x, y)$

Calculate the bitwise or. The two bytes must have the same lengths.

bit_not(x)

Calculate the bitwise not.

$bit_xor(x, y)$

Calculate the bitwise xor. The two bytes must have the same lengths.

pack_bits([...])

packs a list of booleans into a byte array; if the list is not divisible by 8, it is padded with false.

unpack_bits(x)

Unpacks a byte array into a list of booleans.

encode_base64(b)

Encodes the byte array b into the Base64²²-encoded string.

Note: encode_base64 is automatically applied when output to JSON since JSON cannot represent bytes natively.

decode_base64(str)

Tries to decode the str as a Base64²³-encoded byte array.

7.7 Type checking and conversions

to_string(x)

Convert \mathbf{x} to a string: the argument is unchanged if it is already a string, otherwise its JSON string representation will be returned.

to_float(x)

Tries to convert x to a float. Conversion from numbers always succeeds. Conversion from strings has the following special cases in addition to the usual string representation:

- INF is converted to infinity;
- NEG_INF is converted to negative infinity;
- NAN is converted to NAN (but don't compare NAN by equality, use is_nan instead);
- PI is converted to pi (3.14159...);
- E is converted to the base of natural logarithms, or Euler's constant (2.71828...).

$to_uuid(x)$

Tries to convert **x** to a UUID. The input must either be a hyphenated UUID string representation or already a UUID for it to succeed.

uuid_timestamp(x)

Extracts the timestamp from a UUID version 1, as seconds since the UNIX epoch. If the UUID is not of version 1, null is returned. If x is not a UUID, an error is raised.

$is_null(x)$

Checks for null.

²² https://en.wikipedia.org/wiki/Base64

²³ https://en.wikipedia.org/wiki/Base64

$is_int(x)$

Checks for integers.

is_float(x)

Checks for floats.

is_finite(x)

Returns true if x is an integer or a finite float.

is_infinite(x)

Returns true if x is infinity or negative infinity.

$is_nan(x)$

Returns true if x is the special float NAN. Returns false when the argument is not of number type.

$is_num(x)$

Checks for numbers.

is_bytes(x)

Checks for bytes.

is_list(x)

Checks for lists.

is_string(x)

Checks for strings.

is_uuid(x)

Checks for UUIDs.

7.8 Random functions

rand_float()

Generates a float in the interval [0, 1], sampled uniformly.

rand_bernoulli(p)

Generates a boolean with probability p of being true.

rand_int(lower, upper)

Generates an integer within the given bounds, both bounds are inclusive.

rand_choose(list)

Randomly chooses an element from list and returns it. If the list is empty, it returns null.

rand_uuid_v1()

Generate a random UUID, version 1 (random bits plus timestamp).

rand_uuid_v4()

Generate a random UUID, version 4 (completely random bits).

7.9 Regex functions

```
regex_matches(x, reg)
```

Tests if x matches the regular expression reg.

```
regex_replace(x, reg, y)
```

Replaces the first occurrence of the pattern reg in x with y.

```
regex_replace_all(x, reg, y)
```

Replaces all occurrences of the pattern reg in x with y.

```
regex_extract(x, reg)
```

Extracts all occurrences of the pattern reg in x and returns them in a list.

```
regex_extract_first(x, reg)
```

Extracts the first occurrence of the pattern reg in x and returns it. If none is found, returns null.

7.9.1 Regex syntax

Matching one character:

```
. any character except new line
\d digit (\p{Nd})
\D not digit
\pN One-letter name Unicode character class
\p{Greek} Unicode character class (general category or script)
\PN Negated one-letter name Unicode character class
\P{Greek} negated Unicode character class (general category or script)
```

Character classes:

```
[xyz]
              A character class matching either x, y or z (union).
[^xyz]
              A character class matching any character except x, y and z.
[a-z]
              A character class matching any character in range a-z.
[[:alpha:]]
              ASCII character class ([A-Za-z])
[[:^alpha:]] Negated ASCII character class ([^A-Za-z])
[x[^xyz]]
              Nested/grouping character class (matching any character except y and z)
[a-y&&xyz]
              Intersection (matching x or y)
[0-9&&[^4]]
              Subtraction using intersection and negation (matching 0-9 except 4)
              Direct subtraction (matching 0-9 except 4)
[0-9--4]
[a-g\sim b-h]
              Symmetric difference (matching `a` and `h` only)
[/[/]]
              Escaping in character classes (matching [ or ])
```

Composites:

```
xy concatenation (x followed by y)
x|y alternation (x or y, prefer x)
```

Repetitions:

```
x* zero or more of x (greedy)
x+ one or more of x (greedy)
x? zero or one of x (greedy)
```

(continues on next page)

(continued from previous page)

```
x*?
          zero or more of x (ungreedy/lazy)
          one or more of x (ungreedy/lazy)
x+?
x??
          zero or one of x (ungreedy/lazy)
          at least n x and at most m x (greedy)
x\{n,m\}
          at least n x (greedy)
x\{n,\}
x\{n\}
          exactly n x
          at least n x and at most m x (ungreedy/lazy)
x{n,m}?
x\{n,\}?
          at least n x (ungreedy/lazy)
x\{n\}?
          exactly n x
```

Empty matches:

```
the beginning of the text
the end of the text
A only the beginning of the text
c only the end of the text
b a Unicode word boundary (\w on one side and \W, \A, or \z on the other)
not a Unicode word boundary
```

7.10 Timestamp functions

now()

Returns the current timestamp as seconds since the UNIX epoch.

format_timestamp(ts, tz?)

Interpret ts as seconds since the epoch and format as a string according to RFC3339²⁴.

If a second string argument is provided, it is interpreted as a timezone²⁵ and used to format the timestamp.

parse_timestamp(str)

Parse str into seconds since the epoch according to RFC3339.

²⁴ https://www.rfc-editor.org/rfc/rfc3339

²⁵ https://en.wikipedia.org/wiki/Tz_database

AGGREGATIONS

Aggregations in Cozo can be thought of as a function that acts on a string of values and produces a single value (the aggregate). Due to Datalog semantics, the stream is never empty.

There are two kinds of aggregations in Cozo, *ordinary aggregations* and *meet aggregations*. They are implemented differently in Cozo, with meet aggregations generally faster and more powerful (e.g. only meet aggregations can be recursive).

The power of meet aggregations derive from the additional properties they satisfy by forming a semilattice²⁶:

idempotency

the aggregate of a single value a is a itself,

commutativity

the aggregate of a then b is equal to the aggregate of b then a,

associativity

it is immaterial where we put the parentheses in an aggregate application.

Meet aggregations can be used as ordinary ones, but the reverse is impossible.

8.1 Meet aggregations

min(x)

Aggregate the minimum value of all x.

max(x)

Aggregate the maximum value of all x.

and(var)

Aggregate the logical conjunction of the variable passed in.

or(var)

Aggregate the logical disjunction of the variable passed in.

union(var)

Aggregate the unions of var, which must be a list.

intersection(var)

Aggregate the intersections of var, which must be a list.

 $^{^{26}}$ https://en.wikipedia.org/wiki/Semilattice

choice(var)

Non-deterministically chooses one of the values of var as the aggregate. It simply chooses the first value it meets (the order that it meets values should be considered non-deterministic).

choice_last(var)

Non-deterministically chooses one of the values of var as the aggregate. It simply chooses the last value it meets.

min_cost([data, cost])

The argument should be a list of two elements and this aggregation chooses the list of the minimum cost.

shortest(var)

var must be a list. Returns the shortest list among all values. Ties will be broken non-deterministically.

coalesce(var)

Returns the first non-null value it meets. The order is non-deterministic.

bit_and(var)

var must be bytes. Returns the bitwise 'and' of the values.

bit_or(var)

var must be bytes. Returns the bitwise 'or' of the values.

8.2 Ordinary aggregations

count(var)

Count how many values are generated for var (using bag instead of set semantics).

count_unique(var)

Count how many unique values there are for var.

collect(var)

Collect all values for var into a list.

unique(var)

Collect var into a list, keeping each unique value only once.

group_count(var)

Count the occurrence of unique values of var, putting the result into a list of lists, e.g. when applied to 'a', 'b', 'c', 'c', 'a', 'c', the results is [['a', 2], ['b', 1], ['c', 3]].

bit_xor(var)

var must be bytes. Returns the bitwise 'xor' of the values.

latest_by([data, time])

The argument should be a list of two elements and this aggregation returns the data of the maximum cost. This is very similar to min_cost, the differences being that maximum instead of minimum is used, only the data itself is returned, and the aggregation is deliberately note a meet aggregation. Intended to be used in timestamped audit trails.

choice_rand(var)

Non-deterministically chooses one of the values of var as the aggregate. Each value the aggregation encounters has the same probability of being chosen. This version of choice is not a meet aggregation since it is impossible to satisfy the uniform sampling requirement while maintaining no state, which is an implementation restriction unlikely to be lifted.

8.2.1 Statistical aggregations

mean(x)

The mean value of x.

sum(x)

The sum of x.

product(x)

The product of x.

variance(x)

The sample variance of \mathbf{x} .

$std_dev(x)$

The sample standard deviation of \mathbf{x} .

UTILITIES AND ALGORITHMS

Fixed rules in CozoScript apply utilities and/or algorithms. The purpose of the native, built-in utilities and algorithms in Cozo is to enable easy computation of results that would require either queries too awkward to express in pure Datalog, or time or space requirements that are unreasonable if implemented in the interpreted queries framework.

9.1 Utilities

Constant(data: [...])

Returns a constant relation containing the data passed in. The constant rule ?[] <- ... is actually syntax sugar for $?[] <\sim Constant(data: ...)$.

Parameters

data – A list of lists, representing the rows of the returned relation.

ReorderSort(rel[...], out: [...], sort_by: [...], descending: false, break_ties: false, skip: 0, take: 0) Sort and then extract new columns of the passed in relation rel.

Parameters

- **out** (*required*) A list of expressions which will be used to produce the output relation. Any bindings in the expressions will be bound to the named positions in rel.
- **sort_by** A list of expressions which will be used to produce the sort keys. Any bindings in the expressions will be bound to the named positions in rel.
- descending Whether the sorting process should be done in descending order. Defaults to false.
- **break_ties** Whether ties should be broken, e.g. whether the first two rows with *identical* sort keys should be given ordering numbers 1 and 2 instead of 1 and 1. Defaults to false.
- **skip** How many rows to skip before producing rows. Defaults to zero.
- take How many rows at most to produce. Zero means no limit. Defaults to zero.

Returns

The returned relation, in addition to the rows specified in the parameter out, will have the ordering prepended. The ordering starts at 1.

Tip: This algorithm serves a similar purpose to the global :order, :limit and :offset options, but can be applied to intermediate results. Prefer the global options if it is applied to the final output.

CsvReader(url: ..., types: [...], delimiter: ',', prepend_index: false, has_headers: true)

Read a CSV file from disk or an HTTP GET request and convert the result to a relation.

Parameters

- url (required) URL for the CSV file. For local file, use file://<PATH_TO_FILE>.
- **types** (*required*) A list of strings interpreted as types for the columns of the output relation. If any type is specified as nullable and conversion to the specified type fails, null will be the result. This is more lenient than other functions since CSVs tend to contain lots of bad values.
- **delimiter** The delimiter to use when parsing the CSV file.
- prepend_index If true, row index will be prepended to the columns.
- has_headers Whether the CSV file has headers. The reader will not interpret the header in any way but will instead simply ignore it.

JsonReader(url: ..., fields: [...], json_lines: true, null_if_absent: false, prepend_index: false)

Read a JSON file for disk or an HTTP GET request and convert the result to a relation.

Parameters

- url (required) URL for the JSON file. For local file, use file://<PATH_TO_FILE>.
- **fields** (*required*) A list of field names, for extracting fields from JSON arrays into the relation.
- **json_lines** If true, parse the file as lines of JSON objects, each line containing a single object; if false, parse the file as a JSON array containing many objects.
- null_if_absent If a true and a requested field is absent, will output null in its place. If false and the requested field is absent, will throw an error.
- **prepend_index** If true, row index will be prepended to the columns.

9.2 Connectedness algorithms

ConnectedComponents(edges[from, to])

Computes the connected components²⁷ of a graph with the provided edges.

Returns

Pairs containing the node index, and its component index.

StronglyConnectedComponent(edges[from, to])

Computes the strongly connected components²⁸ of a graph with the provided edges.

Returns

Pairs containing the node index, and its component index.

SCC(...)

See Algo. StronglyConnectedComponent.

MinimumSpanningForestKruskal(edges[from, to, weight?])

Runs Kruskal's algorithm²⁹ on the provided edges to compute a minimum spanning forest³⁰. Negative weights are fine.

²⁷ https://en.wikipedia.org/wiki/Connected_component_(graph_theory)

²⁸ https://en.wikipedia.org/wiki/Strongly_connected_component

Returns

Triples containing the from-node, the to-node, and the cost from the tree root to the to-node. Which nodes are chosen to be the roots are non-deterministic. Multiple roots imply the graph is disconnected.

MinimumSpanningTreePrim(edges[from, to, weight?], starting?[idx])

Runs Prim's algorithm³¹ on the provided edges to compute a minimum spanning tree³². starting should be a relation producing exactly one node index as the starting node. Only the connected component of the starting node is returned. If starting is omitted, which component is returned is arbitrary.

Returns

Triples containing the from-node, the to-node, and the cost from the tree root to the to-node.

TopSort(edges[from, to])

Performs topological sorting³³ on the graph with the provided edges. The graph is required to be connected in the first place.

Returns

Pairs containing the sort order and the node index.

9.3 Pathfinding algorithms

 $\textbf{ShortestPathDijkstra} (edges[from,\ to,\ weight?],\ starting[idx],\ goals[idx],\ undirected:\ false,\ keep_ties:\ false)$

Runs Dijkstra's algorithm³⁴ to determine the shortest paths between the starting nodes and the goals. Weights, if given, must be non-negative.

Parameters

- undirected Whether the graph should be interpreted as undirected. Defaults to false.
- **keep_ties** Whether to return all paths with the same lowest cost. Defaults to false, in which any one path of the lowest cost could be returned.

Returns

4-tuples containing the starting node, the goal, the lowest cost, and a path with the lowest cost.

KShortestPathYen(edges[from, to, weight?], starting[idx], goals[idx], k: expr, undirected: false)

Runs Yen's algorithm³⁵ (backed by Dijkstra's algorithm) to find the k-shortest paths between nodes in starting and nodes in goals.

Parameters

- **k** (required) How many routes to return for each start-goal pair.
- undirected Whether the graph should be interpreted as undirected. Defaults to false.

Returns

4-tuples containing the starting node, the goal, the cost, and a path with the cost.

²⁹ https://en.wikipedia.org/wiki/Kruskal%27s_algorithm

³⁰ https://en.wikipedia.org/wiki/Minimum_spanning_tree

³¹ https://en.wikipedia.org/wiki/Prim%27s_algorithm

³² https://en.wikipedia.org/wiki/Minimum_spanning_tree

³³ https://en.wikipedia.org/wiki/Topological_sorting

³⁴ https://en.wikipedia.org/wiki/Dijkstra%27s_algorithm

³⁵ https://en.wikipedia.org/wiki/Yen%27s_algorithm

BreadthFirstSearch(edges[from, to], nodes[idx, ...], starting?[idx], condition: expr, limit: 1)

Runs breadth first search on the directed graph with the given edges and nodes, starting at the nodes in starting. If starting is not given, it will default to all of nodes, which may be quite a lot to calculate.

Parameters

- condition (required) The stopping condition, will be evaluated with the bindings given to nodes. Should evaluate to a boolean, with true indicating an acceptable answer was found
- limit How many answers to produce for each starting nodes. Defaults to 1.

Returns

Triples containing the starting node, the answer node, and the found path connecting them.

BFS(...)

See Algo.BreadthFirstSearch.

DepthFirstSearch(edges[from, to], nodes[idx, ...], starting?[idx], condition: expr, limit: 1)

Runs depth first search on the directed graph with the given edges and nodes, starting at the nodes in starting. If starting is not given, it will default to all of nodes, which may be quite a lot to calculate.

Parameters

- **condition** (*required*) The stopping condition, will be evaluated with the bindings given to nodes. Should evaluate to a boolean, with true indicating an acceptable answer was found.
- limit How many answers to produce for each starting nodes. Defaults to 1.

Returns

Triples containing the starting node, the answer node, and the found path connecting them.

Tip: You probably don't want to use depth first search for path finding unless you have a really niche use case.

DFS(...)

See Algo.DepthFirstSearch.

ShortestPathAStar(edges[from, to, weight], nodes[idx, ...], starting[idx], goals[idx], heuristic: expr)

Computes the shortest path from every node in starting to every node in goals by the A^* algorithm³⁶.

edges are interpreted as directed, weighted edges with non-negative weights.

Parameters

heuristic (*required*) – The search heuristic expression. It will be evaluated with the bindings from goals and nodes. It should return a number which is a lower bound of the true shortest distance from a node to the goal node. If the estimate is not a valid lower-bound, i.e. it overestimates, the results returned may not be correct.

Returns

4-tuples containing the starting node index, the goal node index, the lowest cost, and a path with the lowest cost.

Tip: The performance of A^* star algorithm heavily depends on how good your heuristic function is. Passing in $\mathbf{0}$ as the estimate is always valid, but then you really should be using Dijkstra's algorithm.

³⁶ https://en.wikipedia.org/wiki/A*_search_algorithm

Good heuristics usually come about from a metric in the ambient space in which your data live, e.g. spherical distance on the surface of a sphere, or Manhattan distance on a grid. Func.Math.haversine_deg_input could be helpful for the spherical case. Note that you must use the correct units for the distance.

Providing a heuristic that is not guaranteed to be a lower-bound *might* be acceptable if you are fine with inaccuracies. The errors in the answers are bound by the sum of the margins of your over-estimates.

9.4 Community detection algorithms

ClusteringCoefficients(edges[from, to, weight?])

Computes the clustering coefficients³⁷ of the graph with the provided edges.

Returns

4-tuples containing the node index, the clustering coefficient, the number of triangles attached to the node, and the total degree of the node.

CommunityDetectionLouvain(edges[from, to, weight?], undirected: false, max_iter: 10, delta: 0.0001, keep depth?: depth)

Runs the Louvain algorithm³⁸ on the graph with the provided edges, optionally non-negatively weighted.

Parameters

- undirected Whether the graph should be interpreted as undirected. Defaults to false.
- max_iter The maximum number of iterations to run within each epoch of the algorithm. Defaults to 10.
- **delta** How much the modularity³⁹ has to change before a step in the algorithm is considered to be an improvement.
- **keep_depth** How many levels in the hierarchy of communities to keep in the final result. If omitted, all levels are kept.

Returns

Pairs containing the label for a community, and a node index belonging to the community. Each label is a list of integers with maximum length constrained by the parameter keep_depth. This list represents the hierarchy of sub-communities containing the list.

LabelPropagation(edges[from, to, weight?], undirected: false, max_iter: 10)

Runs the label propagation algorithm⁴⁰ on the graph with the provided edges, optionally weighted.

Parameters

- undirected Whether the graph should be interpreted as undirected. Defaults to false.
- max_iter The maximum number of iterations to run. Defaults to 10.

Returns

Pairs containing the integer label for a community, and a node index belonging to the community.

³⁷ https://en.wikipedia.org/wiki/Clustering_coefficient

³⁸ https://en.wikipedia.org/wiki/Louvain_method

³⁹ https://en.wikipedia.org/wiki/Modularity_(networks)

⁴⁰ https://en.wikipedia.org/wiki/Label_propagation_algorithm

9.5 Centrality measures

DegreeCentrality(edges[from, to])

Computes the degree centrality of the nodes in the graph with the given edges. The computation is trivial, so this should be your first thing to try when exploring new data.

Returns

4-tuples containing the node index, the total degree (how many edges involve this node), the out-degree (how many edges point away from this node), and the in-degree (how many edges point to this node).

PageRank(edges[from, to, weight?], undirected: false, theta: 0.8, epsilon: 0.05, iterations: 20)

Computes the PageRank⁴¹ from the given graph with the provided edges, optionally weighted.

Parameters

- undirected Whether the graph should be interpreted as undirected. Defaults to false.
- **theta** A number between 0 and 1 indicating how much weight in the PageRank matrix is due to the explicit edges. A number of 1 indicates no random restarts. Defaults to 0.8.
- **epsilon** Minimum PageRank change in any node for an iteration to be considered an improvement. Defaults to 0.05.
- **iterations** How many iterations to run. Fewer iterations are run if convergence is reached. Defaults to 20.

Returns

Pairs containing the node label and its PageRank. For a graph with uniform edges, the PageRank of every node is 1. The L2-norm⁴² of the results is forced to be invariant, i.e. in the results those nodes with a PageRank greater than 1 is "more central" than the average node in a certain sense.

ClosenessCentrality(edges[from, to, weight?], undirected: false)

Computes the closeness centrality⁴³ of the graph. The input relation represent edges connecting node indices which are optionally weighted.

Parameters

undirected – Whether the edges should be interpreted as undirected. Defaults to false.

Returns

Node index together with its centrality.

BetweennessCentrality(edges[from, to, weight?], undirected: false)

Computes the betweenness centrality⁴⁴ of the graph. The input relation represent edges connecting node indices which are optionally weighted.

Parameters

undirected – Whether the edges should be interpreted as undirected. Defaults to false.

Returns

Node index together with its centrality.

Warning: BetweennessCentrality is very expensive to compute for medium to large graphs. Plan resources accordingly.

⁴¹ https://en.wikipedia.org/wiki/PageRank

⁴² https://en.wikipedia.org/wiki/Norm_(mathematics)

⁴³ https://en.wikipedia.org/wiki/Closeness_centrality

⁴⁴ https://en.wikipedia.org/wiki/Betweenness_centrality

9.6 Miscellaneous

RandomWalk(edges[from, to, ...], nodes[idx, ...], starting[idx], steps: 10, weight?: expr, iterations: 1)

Performs random walk on the graph with the provided edges and nodes, starting at the nodes in starting.

Parameters

- **steps** (*required*) How many steps to walk for each node in starting. Produced paths may be shorter if dead ends are reached.
- weight An expression evaluated against bindings of nodes and bindings of edges, at a time when the walk is at a node and choosing between multiple edges to follow. It should evaluate to a non-negative number indicating the weight of the given choice of edge to follow. If omitted, which edge to follow is chosen uniformly.
- iterations How many times walking is repeated for each starting node.

Returns

Triples containing a numerical index for the walk, the starting node, and the path followed.

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