### 1. Introduction

Our approach to static contract-checking is to translate source code to a first-order logic theory and then use an automated theorem prover to check the consistency of the theory.

Consider:

data List a = Nil | Cons a (List a)

notnull x = case x of
Nil -> False
Cons(x,y) -> True

head ::: (CF && {x | notnull x }) -> CF
head xs = case xs of
Nil -> BAD
Cons(x,y) -> x

First, we need to encode the List structure. We start by stating that Nil and Cons can never be equal:

$$\forall a, b. Cons(a, b) \neq Nil$$

Then, we must state that Nil never crashes (ie cannot be evaluated to an exception) and that Cons(x,y) crashes iff either x or y crashes. The statement x crashes is encoded by the term  $\mathrm{CF}(x)$ .

$$\forall a, b. \ \mathsf{CF}(a) \land \mathsf{CF}(b) \iff \mathsf{CF}(Cons(a, b))$$
 (1)

We also say some stuff about unreachibility but I can't think of a good way to explain it right now.

$$\forall y, ys. \ Cons(y, ys) \neq UNR$$

$$Nil \neq \mathtt{UNR}$$

Finally, we define projections for Cons. It is not strictly necessary, but it will be handy:

$$\forall xs, y, ys. \ sel_{1.Cons}(Cons(y, ys)) = xs \implies xs = y$$

$$\forall xs, y, ys. \ sel_{2,Cons}(Cons(y, ys)) = xs \implies xs = ys$$

Now we translate the null function. Note that the symbols true and false are the representation of the data constructors True and False in Haskell, not the boolean values  $\top$  and  $\bot$  in our logic.

$$\forall xs. \ xs = Nil \implies notnull(xs) = false$$

$$\forall xs, y, ys. \ x = Cons(y, ys) \implies notnull(xs) = true$$
 (2)

We also need to specify the translation of calls to notnull with BAD values (to encode the fact that notnull(BAD) = BAD.

$$\forall xs. \ xs = \mathtt{BAD} \rightarrow notnull(xs) = \mathtt{BAD}$$

Finally, we say that one call notnull with a an argument which is not Nil or Cons or BAD then the result is UNR.

$$\forall xs. \ xs \neq \mathtt{BAD} \land xs \neq Nil$$
 
$$\land xs \neq Cons(sel_{1,Cons}(xs), sel_{2,Cons}(xs)) \rightarrow notnull(X) = \mathtt{UNR} \tag{3}$$

The translation of *head* follows the same pattern:

$$\begin{array}{ccc} \forall xs. \ x = Nil \implies head(xs) = \mathtt{BAD} \\ \forall xs, y, ys. \ x = Cons(y, ys) \implies head(xs) = y \\ \forall xs. \ xs = \mathtt{BAD} \rightarrow head(xs) = \mathtt{BAD} \end{array} \tag{4}$$

$$\forall xs.\ xs \neq \texttt{BAD} \land xs \neq Nil \\ \land xs \neq Cons(sel_{1,Cons}(xs), sel_{2,Cons}(xs)) \rightarrow \\ head(X) = \texttt{UNR}$$

We now have translated the source code. Let us call all those formulae the theory T. We translate separatly the contract:

$$\phi := \forall xs. \ \mathsf{CF}(xs) \land not null(xs) = true \rightarrow \mathsf{CF}(head(xs))$$

Now that we translated everything to first-order logic, we can ask the theorem prover if the theory formed by those formulae is consistent, ie if  $T \vdash \phi$ .

Intuitively, T is consistent (ie  $T \not\vdash \bot$ ), because each formula serves a specific purpose. Now, assume that xs satisfies  $\mathrm{CF}(xs)$  and notnull(xs) = true. We can derive that  $xs \not= \mathrm{BAD}$  because we have  $\mathrm{CF}(xs)$  and  $\neg \mathrm{CF}(\mathrm{BAD})$ . The constraint notnull(xs) = true doesn't directly imply that xs = Cons(y, ys) for some y and ys. But notnull is totally defined, because of (3). This implies (by (2)) that there exist y and ys such that xs = Cons(y, ys). Recalling  $\mathrm{CF}(xs)$ , we can now derive  $\mathrm{CF}(y)$  and  $\mathrm{CF}(ys)$  (by (1)). But head(xs) = y because of (4), and y is crash-free, so we can finally derive  $\mathrm{CF}(head(xs))$ . QED.

# 2. Languages

#### 2.1 $\mathcal{H}'$ : $\lambda$ -calculus variant

The syntax of  ${\mathcal H}$  is defined in figure 1. A module is a list of toplevel definitions, claims that functions statisfy contracts and data definitions.

- There's no  $\lambda$ -abstraction, because we can always lift them to toplevel declaration.
- We do not allow nested case expressions, because once again, we can always lift them to the toplevel.
- Until section 6 we will only consider full application of functions (f(x,y)), in order to remove clutter. Dealing with partial application is not hard but a bit cumbersome.

$$\begin{array}{rcll} mod & := & def_1, \dots, def_n \\ def & \in & \mathrm{Definition} \\ def & := & \mathrm{data} \ T = K_1 \mid \dots \mid K_n & \mathrm{Data} \ \mathrm{definition} \\ & \mid & f \in c & \mathrm{Contract} \ \mathrm{claim} \\ & \mid & f \vec{x} = e \\ & \mid & f \vec{x} = e \\ & \mid & f \vec{x} = \mathrm{case} \ e \ \mathrm{of} \\ & & K_1(\vec{x_1}) \to e_1 \mid \dots \mid K_n(\vec{x_n}) \to e_n \\ \\ & x, y, f, g, a, b & \in \mathrm{Variables} \\ & T & \in \mathrm{Type} \ \mathrm{Constructors} \\ & K & \in \mathrm{Data} \ \mathrm{Constructors} \\ & e \in \mathrm{Expressions} \\ & e := & x \\ & \mid & \mathrm{BAD} \\ & \mid & e \ e \\ & \mid & f(e, \dots, e) \\ & \mid & K(e, \dots, e) \end{array}$$

Figure 1. Syntax of the language  $\mathcal{H}'$ 

### 2.2 Contracts

Contract syntax is described in figure 2. The predicates we use in our contracts can be any boolean  $\mathcal{H}'$  expression. We only consider

pairs of contract for simplicity, although there is no issue with generalisation to arbitrary tuples.



Figure 2. Contract syntax

We give the semantics of contract by defining "e satisfies t", written  $e \in t$  in figure 3. Note that this definition doesn't yield any operative way to check that an expression actually meets the specification given by its contract.

```
\begin{array}{ccccc} e \in \{x \mid p\} & \Longleftrightarrow & e \text{ diverges or } p[e/x] \not \to^{\star} \{\mathtt{BAD}, False\} \\ e \in x : c_1 \to c_2 & \Longleftrightarrow & \forall e_1 \in c_1, (e \ e_1) \in c_2[e_1/x] \\ e \in (c_1, c_2) & \Longleftrightarrow & e \text{ diverges or } \\ & & (e \to^{\star} (e_1, e_2) \text{ and } e_1 \in c_1, e_2 \in c_2) \\ e \in c_1 \land c_2 & \Longleftrightarrow & e \in c_1 \text{ and } e \in c_2 \\ e \in c_1 \lor c_2 & \Longleftrightarrow & e \in c_1 \text{ or } e \in c_2 \\ e \in \mathtt{CF} & \Longleftrightarrow & e \text{ is crash-free} \end{array}
```

Figure 3. Semantics of contract satisfaction

#### 2.3 Crash-freeness

Note that CF represents two things: it can be a contract, as in  $f \in CF$  or a special formula in first-order logic CF(f).

We use BAD to signal that something has gone wrong in the program: it has crashed.

**Definition 1** (Crash). A closed term e crashed iff  $e \rightarrow^* BAD$ .

**Definition 2** (Diverges). A closed expression e diverges iff either  $e \rightarrow^* UNR$  or there is no value val such that  $e \rightarrow^* val$ 

**Definition 3** (Syntactic safety). *A (possibly open) expression e is syntactically safe iff BAD*  $\not\in_s e$ . *Similarly a context C is syntactically safe iff BAD*  $\not\in_s C$ .

The notation BAD  $\not\in e$  means that BAD does not appear anywhere in e, similarly for BAD  $\not\in_s \mathcal{C}$ . For example, Just3 is syntactically safe whereas JustBAD is not.

**Definition 4** (Crash-free). *An expression e is said to be crash-free iff* 

$$\forall \mathcal{C}. \ \textit{BAD} \not\in_s \mathcal{C} \ \textit{and} \ \vdash \mathcal{C}\llbracket e \rrbracket :: ()\mathcal{C} \not\to^* \textit{BAD}$$

The notation  $\mathcal{C}[\![e]\!]$  :: () means that  $\mathcal{C}[\![e]\!]$  is closed and well-typed. Note that there are crash-free expression that are not syntactically safe, for example fst (1, BAD).

### 2.4 BAD and UNR

Consider the following piece of code:

```
a = 0 + True
b ::: CF
b = undefined
c = error "foo"
```

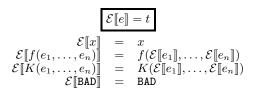
- ullet a is ill-typed
- b's implementation is not correct wrt its contract

$$\begin{array}{rcl} v,w,s,t &:= & x \mid K(t,\ldots,t) \mid f(t,\ldots,t) \mid app(t,t) \\ & \mid \mathsf{BAD} \mid \mathsf{UNR} \\ \phi &:= & \forall x.\phi \mid \neg \phi \mid \phi \lor \phi \mid \top \mid \bot \mid t=t \mid \mathsf{CF}(t) \\ & \mid \phi \land \phi \mid \phi \to \phi \mid \phi \leftrightarrow \phi \\ \Phi &:= & \epsilon \mid \phi \mid \Phi \cup \Phi \end{array}$$

Figure 4. First-order logic syntax

```
 \begin{array}{cccc} \mathcal{E} \llbracket \text{expression} \rrbracket & \to & t \text{ (Term)} \\ \mathcal{D} \llbracket def \rrbracket & \to & \Phi \text{ (Set of formulae)} \\ \mathcal{K} \llbracket \text{data } T = \dots \rrbracket & \to & \Phi \text{ (Set of formulae)} \\ \mathcal{C} \llbracket f \in c \rrbracket & \to & \Phi \text{ (Set of formulae)} \\ \end{array}
```

Figure 5. Translations



**Figure 6.**  $\mathcal{E}[]$  – Expression translation

 c goes through the whole toolchain (compiler, typechecker, contractchecker)

One thing to notice is that a and b are things that "sould not happen" but are caught statically whereas c should not happen but can only be dealt with dynamically.

We can now define two types of problematic expressions: those that cannot happen during a run of the program and those that can. Expressions of the first type are called unreachable (and equated to the special value UNR in our first-order theory), whilst expressions of the latter type are called bad (and equated to the special value BAD).

We said earlier that we only considered syntactically correct and well-typed programs as input. That implies that the "a" case cannot happen. But given that our first-order logic is not typed, the theorem prover may decide to instanciate a variable with an ill-typed value! In order to prevent this, we will need to encode some basic type-checking mecanism directly in our first-order theory.

### 2.5 First-order logic with equality

We use first-order logic with equality, defined in figure 4.

### 3. Translations

For an overview of the different translations we define, see figure 5

## 3.1 $\mathcal{E}[[]]$ – Expressions

Our most basic translation is from expressions in  $\mathcal{H}'$  to terms in first-order logic. Given this translation we will be able to translate definitions, data types and contracts to first-order formulae. It is described in figure 6.

# 3.2 $\mathcal{D}[[]]$ – Definitions

We give in figure 7 the two translations of function definitions.

figure ?? gives the translation of function not defined by pattern matching, which is really easy: we just have to state the equality between le left-hand side and the right-hand side.

Translating definitions that use pattern-matching is more challenging and is described in figure 7.

The first line says that when applied to an argument that matches a pattern of the case expression, we should equate the function call to the corresponding expression.

The second line states that if the pattern-matching failed or if we pattern-matched on BAD then the result should be UNR.

### 3.3 $\mathcal{K}[]$ – Datatypes

We break down the translation for datatypes in four parts, described in figure 8

$$\mathcal{K}\llbracket \text{data } T = K_1, \dots, K_n \rrbracket = \Phi_1 \cup \Phi_2 \cup \Phi_3 \cup \Phi_4$$

- $(\Phi_1)$  For each  $K_i$  of arity  $a_i$  we introduce selectors  $sel_{k,K_i}$ , which are the projection of  $K_i(x_1,\ldots,x_{n_i})$  on its k-th component.
- $(\Phi_2)$  For each pair of constructors  $K_i, K_j$ , we state that they can never map to the same value.
- (Φ<sub>3</sub>) Then, we have to give crash-freeness conditions for each K<sub>i</sub>: Notice that we have a equivalence.
  - ←: if we pack crash-free values in a data constructor, the resulting value is crash-free.
  - →: a value t of type T is crash-free implies that every value packed in it is crash-free. Recall that one can define projection on any argument of a value of type t. So if the k-th argument of t is not crash-free, then the k-th projection is a crash-free context that throws an expression that is not crash-free.

Note that this is not true for functions: a function is not required to use all of its arguments. fst is crash-free if and only if the first argument of the pair is crash-free. The second argument being crash-free or not doesn't matter.

- $(\Phi_4)$  None of the  $K_i$  is unreachable.
- One may want to also state that if  $\vec{x} \neq \text{BAD}$  then  $K_i(\vec{x}) \neq \text{BAD}$ . It is already implied by the fact that  $\text{CF}(\vec{x}) \to \text{CF}(K_i(\vec{x}))$ .

### 3.4 C $\square$ – Contracts

We give in figure 9 the translation of contract satisfaction. true refers to the translation to a term of the data constructor True in  $\mathcal{H}'$ , not to the actual true value.

Note that we define the translation of  $f \in c$  and of  $f \notin c$ . We have to do that because one is not the negation of the other, even though  $\neg (f \notin c)$  implies  $f \in c$ .

## 

#### 4.1 Prelude

There are some formulae that should always be included in our FO theory.

We need to state that BAD is not crash-free with the formula:  $\neg CF(BAD)$ .

Plus we need to give formulae for the boolean datatype and for unreachability. Strictly speaking, we can omit them and just add the following lines to source files:

But given that those datatypes are used by our translation, we can just directly include their translation every time we translate a module.

### 4.2 Contract checking – Non-recursive case

Input: a module M that consists of a list of definitions, datatypes, contracts and a contract c for a non-recursive function f this is defined in M.

We say that the function implementation is correct wrt to its contract iff

$$[\![M]\!] \vdash \mathcal{C}[\![f \in c]\!]$$

### 4.3 Contract checking – Recursive case

If the function f=e is recursive, then we ask the theorem prover the following:

$$[M - f], \mathcal{D}[f = e[f/f_p]], \mathcal{C}[f_p \in c] \vdash \mathcal{C}[f \in c]$$

Where M-f means the content of the module M without f's definition and f's contract. TODO Stress that it's not always enough and that we may have to unroll several times!

#### 4.4 Module checking

A module is a collection of function definitions, data definitions and contracts. What we want to do is to check that functions satisfy their contract(s).

### 4.4.1 Naive example

Here is a little example showing that we should be careful about which formulae should belong to a theory.

Assume that we have a module that contains two functions defintion f and g and two contracts :  $f \in CF$  and  $g \in CF$ . We assume that those contracts do not hold, for example if f is head and g is last.

First, we want to check f's contract. So we ask the theorem prover if

$$\mathcal{D}\llbracket f \rrbracket, \mathcal{D}\llbracket g \rrbracket, \mathcal{C}\llbracket g \rrbracket \vdash \mathcal{C}\llbracket f \rrbracket$$

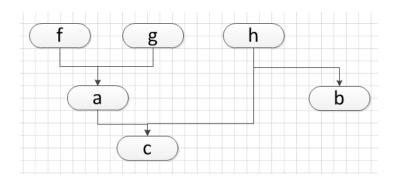
But, given that g's contract does not hold, we can derive  $\bot$  and then prove that f's contract hold.

For the same reason, we can prove that g contract's holds, when in fact it doesn't.

Finally, the user thinks he's done, but in fact he has proven nothing.

### 4.4.2 The proper way to check a module

Consider the following situation, where a's definition relies on f and g.



We should only include formulae that belongs to functions that are actually used. For example, to prove a's contract, we should only include f and g translations, and we would ask equinox:

$$\mathcal{D}[\![f]\!], \mathcal{D}[\![g]\!], \mathcal{D}[\![a]\!], \mathcal{C}[\![f]\!], \mathcal{C}[\![g]\!] \vdash \mathcal{C}[\![a]\!]$$

**Figure 7.**  $\mathcal{D}[\![]\!]$  – Defintions translation

```
\mathcal{K}[\![data\ def]\!] = \Phi
\mathcal{K}[\![data\ T = K_1, \dots, K_n]\!] = \Phi_1 \cup \Phi_2 \cup \Phi_3 \cup \Phi_4
where
\Phi_1 = \bigcup_{1 \leq i \leq n} \forall \vec{x}, a. \ (\min(a) \land K_i(\vec{x}) = a) \to \bigwedge_{1 \leq j \leq k} x_j = sel_{j,K_i}(a)
\Phi_2 = \bigcup_{1 \leq i < j \leq n} \forall \vec{x}, \vec{y}, a. \ \neg(\min(a) \land K_i(\vec{x}) = a \land K_j(\vec{x}) = a)
\Phi_3 = \bigcup_{1 \leq i \leq n} \forall \vec{x}, a. \ \min(a) \land a = K_i(\vec{x}) \to ((\bigwedge_{1 \leq j \leq k} \operatorname{CF}(x_j)) \leftrightarrow \operatorname{CF}(K_i(\vec{x})))
\Phi_4 = \bigcup_{1 \leq i \leq n} \forall \vec{x}, a. \ (\min(a) \land a = K_i(\vec{x})) \to a \neq \operatorname{UNR} \land a \neq \operatorname{BAD}
```

**Figure 8.**  $\mathcal{K}[\![]\!]$  – Data type translation

```
\begin{split} \mathcal{C}[\![contract]\!] &= \Phi \\ \mathcal{C}[\![e \in \{x \mid b\}]\!] &= \min(\mathcal{E}[\![b[e/x]]\!]) \wedge (\mathcal{E}[\![b[e/x]]\!] = true \vee \mathcal{E}[\![e]\!] = \text{UNR}) \\ \mathcal{C}[\![e \in x : c_1 \to c_2]\!] &= \forall x. \min(\mathcal{E}[\![e x]\!]) \to (\mathcal{C}[\![x \not\in c_1]\!] \vee \mathcal{C}[\![e x \in c_2]\!]) \\ \mathcal{C}[\![e \in \text{CF}]\!] &= \min(\mathcal{E}[\![e]\!]) \wedge \text{CF}(\mathcal{E}[\![e]\!]) \\ \\ \mathcal{C}[\![e \notin \text{CF}]\!] &= \min(\mathcal{E}[\![b[e/x]]\!]) \wedge (\mathcal{E}[\![b[e/x]]\!] = false \vee \mathcal{E}[\![e]\!] = \text{BAD}) \\ \mathcal{C}[\![e \notin x : c_1 \to c_2]\!] &= \exists x. \, \mathcal{C}[\![x \in c_1]\!] \wedge \mathcal{C}[\![e x \not\in c_2]\!] \\ \mathcal{C}[\![e \notin \text{CF}]\!] &= \min(\mathcal{E}[\![e]\!]) \wedge \neg \text{CF}(\mathcal{E}[\![e]\!]) \\ \\ \\ \mathcal{C}[\![e \notin \text{CT}]\!] &= \min(\mathcal{E}[\![e]\!]) \wedge \neg \text{CF}(\mathcal{E}[\![e]\!]) \\ \\ \mathcal{C}[\![e \notin c_1]\!] &= \mathcal{C}[\![e \notin c_1]\!] \wedge \mathcal{C}[\![e \notin c_2]\!] \\ \mathcal{C}[\![e \notin c_1||c_2]\!] &= \mathcal{C}[\![e \notin c_1]\!] \wedge \mathcal{C}[\![e \notin c_2]\!] \\ \mathcal{C}[\![a,b) \in (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \wedge \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a,b) \notin (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \wedge \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a,b) \notin (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \wedge \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a,b) \notin (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a,b) \notin (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a,b) \notin (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a,b) \notin (c_1,c_2)\!] &= \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![b \notin c_2]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_2]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]\!] \\ \mathcal{C}[\![a \notin c_1]\!] \vee \mathcal{C}[\![a \notin c_1]
```

Figure 9. C[] – Contract translation

## 5. Correctness of the translation

For the translation to be useful,  $[\![M]\!] \vdash \mathcal{C}[\![f \in c]\!]$  should imply that  $f \in c.$ 

# 6. Higher-orderness

Our current translation only considers fully applied functions and first-order functions. For example, so far, we cannot give any contract to map because it would involve quantifying over a function, a thing that is not first-order.

There is a possible workaround, which involves the "app" function defined in our first-order logic. Assume we have a function f that is not fully applied somewhere in a module. We create the term f-ptr which relates to f by the equations given in figure 10

This way, we can emulate quantification over function by quantifying on their ptr counterpart.

# 7. Experiments

That's how we roll.

$$\begin{split} \mathcal{E}[\![e_1\ e_2]\!] &= app(e_1,e_2) \\ \forall x_1,\ldots,x_n.\ f(x_1,\ldots,x_n) &= app(app(\ldots app(f\_ptr,x_1),x_2),\ldots,x_n) \\ \mathsf{CF}(f\_ptr) &\leftrightarrow \forall x_1,\ldots,x_n.\ \mathsf{CF}(x_1) \wedge \cdots \wedge \mathsf{CF}(x_n) \to \mathsf{CF}(f(x_1,\ldots,x_n)) \\ \forall f\_ptr,x.\ \mathsf{CF}(f\_ptr) \wedge \mathsf{CF}(x) \to \mathsf{CF}(app(f\_ptr,x)) \end{split}$$

Figure 10. Encoding of higher-orderness

Problem	Equinox	Equinox (+ weak)	SPASS	Vampire	E
Add.hs	0.25	0.08	0.04	0.12	0.05
BinaryTree.hs	0.45	0.2	0.04	0.01	0.04
Branch.hs	0.27	0.40	0.04	0.01	0.03
Copy.hs	0.86	0.09	0.03	0.01	184.3
Head.hs	0.32	0.29	0.03	0.03	4.2
Implies.hs	3.24	0.32	0.06	0.02	0.11
Map.hs	2.47	0.14	0.92	1.02	>300
Mult.hs	>300	0.41	0.05	0.22	11.71
Multgt.hs	>300	1.24	0.62	1.31	>300
NatEq.hs	203.12	0.33	0.02	0.03	0.343
Odd.hs	0.42	1.17	0.06	0.03	>300
Reverse.hs	72.32	0.12	0.05	0.02	0.038
Simple.hs	0.07	0.04	0.01	0.01	0.022
Test.hs	7.76	2.86	0.08	0.05	>300
Test2.hs	5.63	0.09	0.07	0.01	1.02

Figure 11. Comparison (in seconds) with other theorem provers