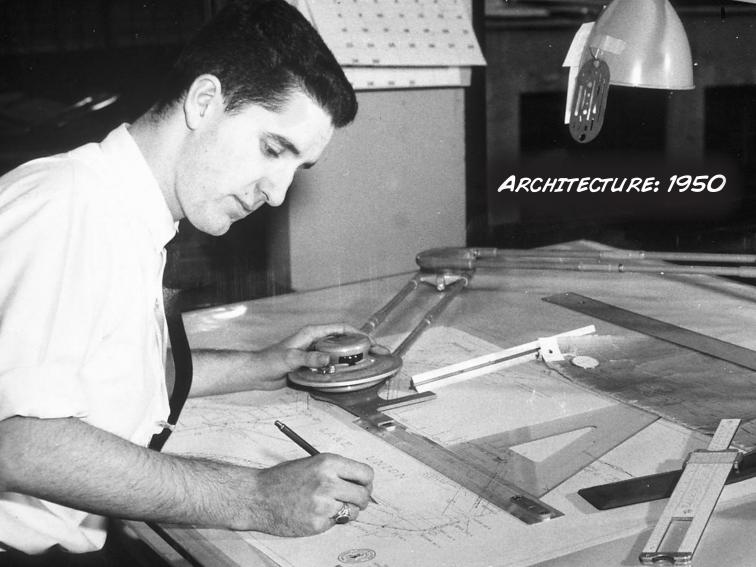
Flaviu Cipcigan Andrew Jones Jason Crain Vlad Sokhan Glenn Martyna

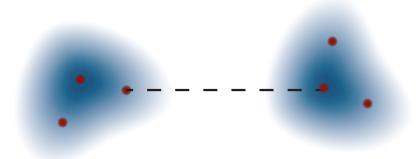
- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water
- 4. Liquid-vapour interface of QDO water





- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water
- 4. Liquid-vapour interface of QDO water

# **Challenge** efficiently model intermolecular interactions



# Challenge

efficiently model intermolecular interactions

### Solution

begin with simple building blocks



# Challenge

efficiently model intermolecular interactions

### Solution

begin with simple building blocks and assemble them into molecules



### **Electrostatics**

• •

Point charges

• •

### Electrostatics

Point charges

**Constraints** 



**Translational** 



Rotational

# Electrostatics Constraints Non-Coulomb forces Point charges Translational Rotational repulsion Pont Coulomb forces Point charges Translational repulsion

### Electrostatics

• •

**Point charges** 

### **Constraints**



**Translational** 



Rotational

### Non-Coulomb forces



van der Waals



repulsion

### Response (limited)



Fluctuating dipole



Charge transfer

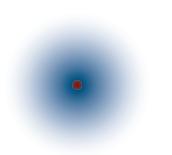
- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water
- 4. Liquid-vapour interface of QDO water

# **Quantum Drude Oscillator (QDO)**

Light negative particle tethered harmonically to a heavy positive, oppositely charged nucleus

# **Quantum Drude Oscillator (QDO)**

Light negative particle tethered harmonically to a heavy positive, oppositely charged nucleus



### Free parameters

 $\mu$  reduced mass

 $\omega$  spring frequency

q charge

# **Quantum Drude Oscillator: Response**

$$\begin{array}{ccc} \textbf{Polarisation} & \alpha_l & = & \left[\frac{q^2}{\mu\omega^2}\right] \left[\frac{(2l-1)!!}{l}\right] \left[\frac{\hbar}{2\mu\omega}\right]^{l-1} \\ \hline & \overline{\text{dipole}} \end{array}$$

# **Quantum Drude Oscillator: Response**

$$\begin{array}{ccc} \textbf{Polarisation} & \alpha_l & = & \left[\frac{q^2}{\mu\omega^2}\right] \left[\frac{(2l-1)!!}{l}\right] \left[\frac{\hbar}{2\mu\omega}\right]^{l-1} \\ \hline & \overline{\text{dipole}} \end{array}$$

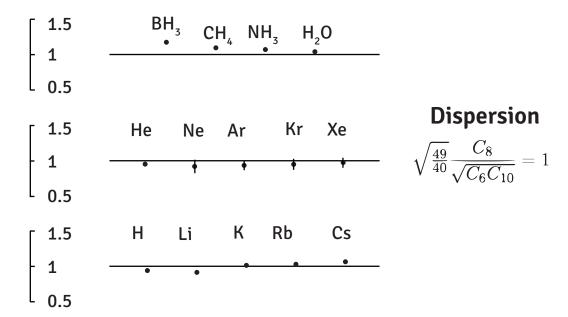
Dispersion 
$$C_6=rac{3}{4}lpha_1lpha_1\hbar\omega$$
 dipole-dipole  $C_8=5lpha_1lpha_2\hbar\omega$  dipole-quadrupole

# **Quantum Drude Oscillator: Invariants**

$$\begin{bmatrix} 1.5 & CH_4 & H_2O \\ 1 & & & \\ 0.5 & & & \\ \end{bmatrix}$$
He Ne Ar Kr Xe
$$\begin{bmatrix} 1.5 & He & Ne & Ar & Kr & Xe \\ 1 & & & & \\ 0.5 & & & & \\ \end{bmatrix}$$

$$\begin{bmatrix} 1.5 & H & Li & K & Rb & Cs \\ 1 & & & & \\ \end{bmatrix}$$

## **Quantum Drude Oscillator: Invariants**



# Electrostatics Constraints Non-Coulomb forces Point charges Translational Rotational Rotational repulsion

### Response



Fluctuating dipole



Quantum Drude Oscillator



Charge transfer

- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water
- 4. Liquid-vapour interface of QDO water

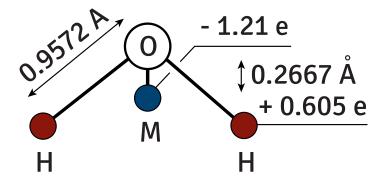
- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water

Frame QDO Repulsion Damping Sampling

4. Liquid-vapour interface of QDO water

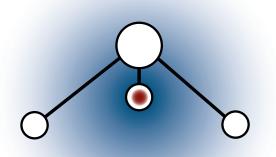
### 1. Frame

ground state moments



# 2. QDO

molecular response



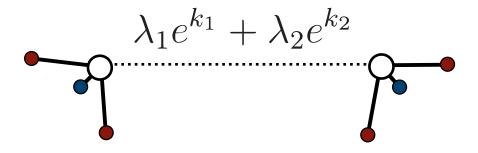
$$\mu$$
 = 0.3656 amu

$$\omega$$
 = 0.6287  $\omega_h$ 

$$q$$
 =-1.1973 e

# 3. Repulsion

**Short range correction** 



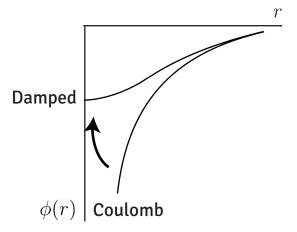
# 4. Electrostatic Damping

**Short range correction** 

Gaussian charges
$$-rac{\mathrm{erf}(\gamma r)}{r}$$

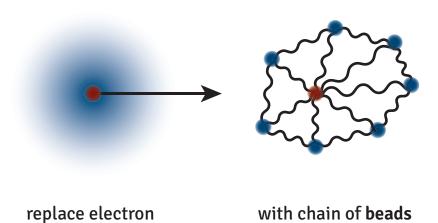
# 4. Electrostatic Damping

**Short range correction** 



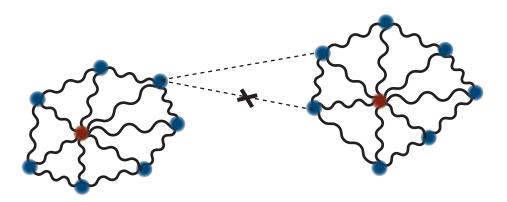
# 5. Efficient Sampling

Path Integral Molecular Dynamics



# 5. Efficient Sampling

Path Integral Molecular Dynamics



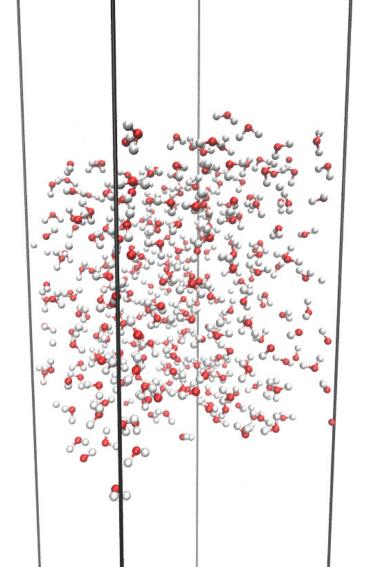
no cross interactions between beads

- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water
- 4. Liquid-vapour interface of QDO water

# 1. Setup

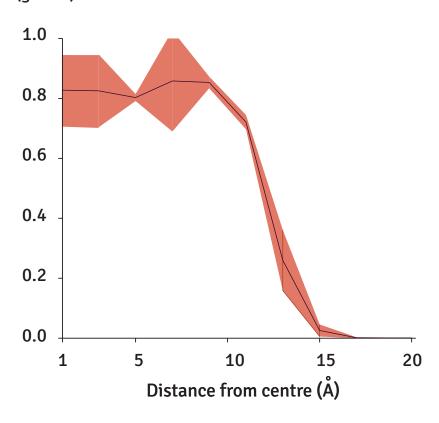
300 QDO-water molecules Periodic boundaries

Unit cell 20.80126 × 20.80126 × 80 Å<sup>3</sup>

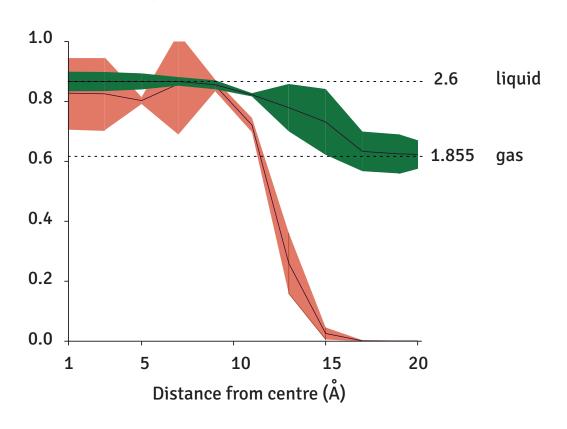


# 2. Density

(g·cm<sup>-3</sup>)

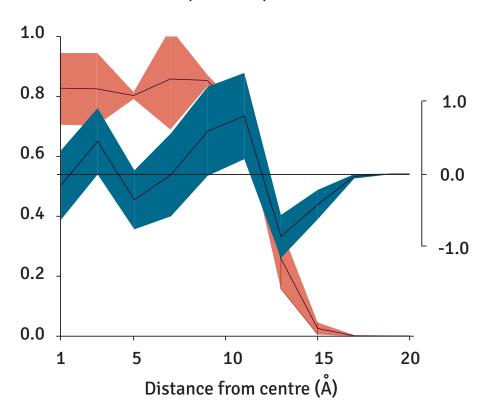


# 3. Dipole moment (Debye)



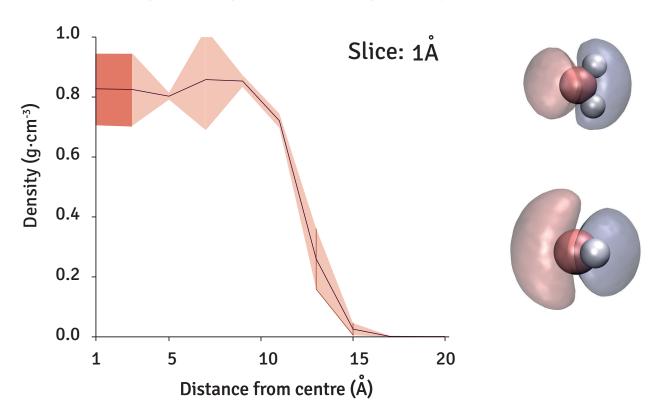
# 3. Surface charge density

(e·A-3·10-3)



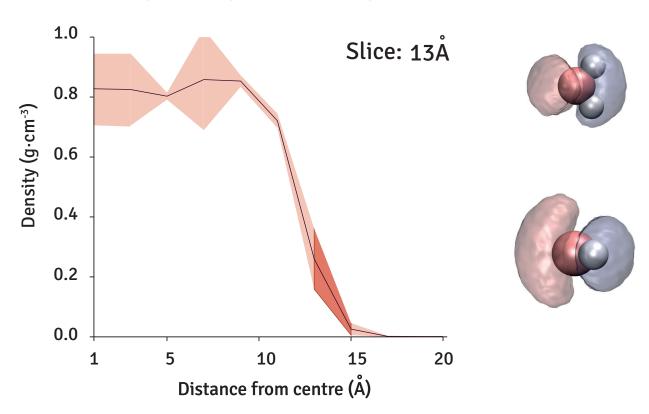
### 4. Electronic distribution

(minus gas phase ground state charge density)



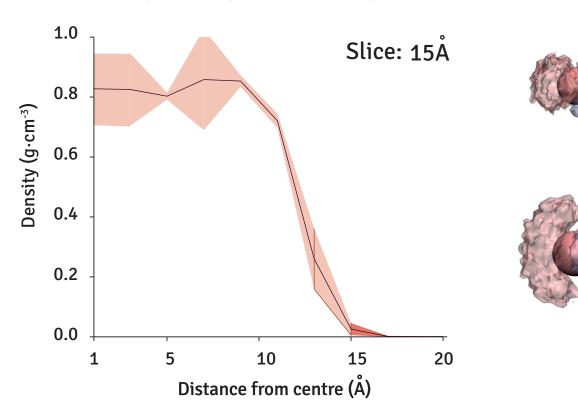
### 4. Electronic distribution

(minus gas phase ground state charge density)

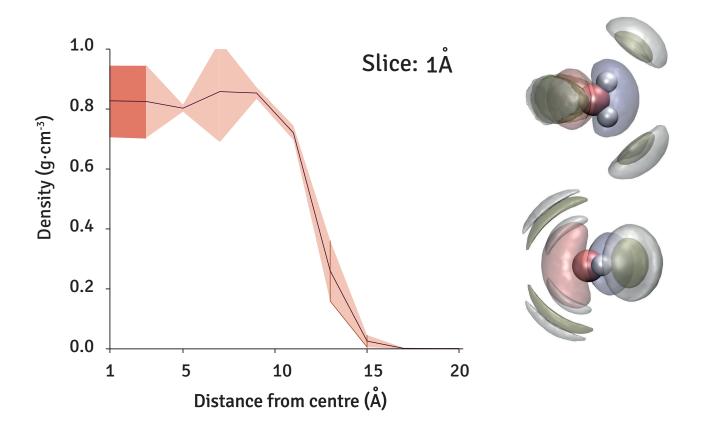


### 4. Electronic distribution

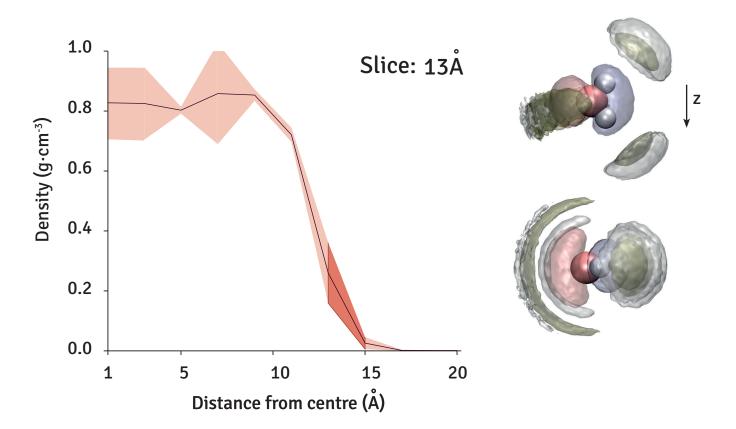
(minus gas phase ground state charge density)



# 5. Nearest neighbour distribution



# 5. Nearest neighbour distribution



- 1. Molecular models
- 2. The Quantum Drude Oscillator (QDO)
- 3. Introducing QDO water
- 4. Liquid-vapour interface of QDO water

### **Conclusions**

QDOs are an accurate model for long range forces QDO water has a physical liquid-vapour interface

# **Next steps**

Exploration of the interface's structure and the effects of dispersion and polarisation on physical properties

### References

A. Jones, Quantum drude oscillators for accurate many-body intermolecular forces, PhD thesis, The University of Edinburgh

A. Jones, F. Cipcigan, V. Sokhan, J. Crain, G. Martyna, Electronically coarse grained water, PRL (under review)



# THE UNIVERSITY of EDINBURGH





# Liquid radial distribution function

