

SUPPLEMENTARY MATERIAL

Low field depolarization of electronic spins through dipole-dipole coupling

C. Pellet-Mary¹, M. Perdriat¹, G. Hétet¹

*Laboratoire De Physique de l'École Normale Supérieure,
École Normale Supérieure, PSL Research University,
CNRS, Sorbonne Université, Université Paris Cité ,
24 rue Lhomond, 75231 Paris Cedex 05, France.*

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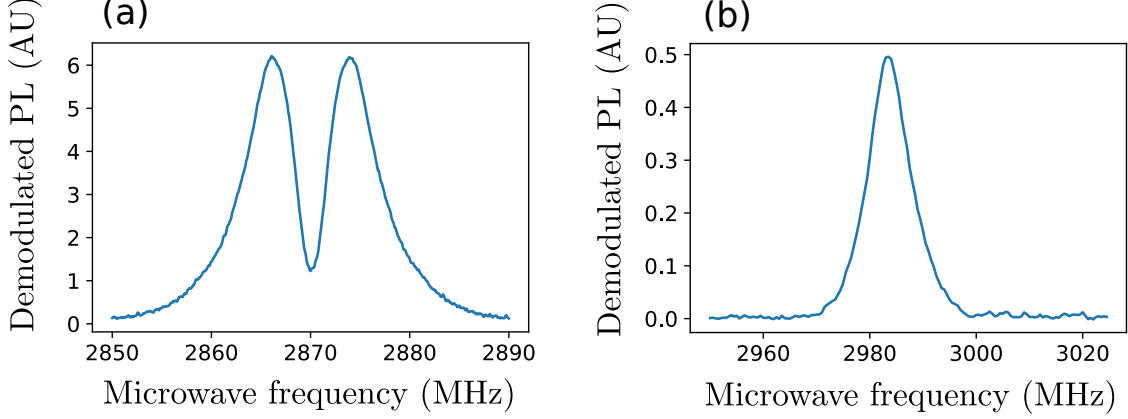


FIG. 1. ODMR measurement (a) in zero magnetic field, (b) in non-zero magnetic field when zooming on a single class transition

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I. NV^- GROUND STATE HAMILTONIAN IN LOW MAGNETIC FIELD

With zero external magnetic field, there are three possible sources of splitting of the $\{|+1\rangle, |-1\rangle\}$ manifold : local electric field, crystal strain and local magnetic field. Of these three causes, only the electric field can explain the shape of the ODMR line that we observe in zero external magnetic field (Fig. 1a) [4].

Indeed, random local magnetic field would produce a single broadened line, and crystal strain would produce a shifting of the zero field splitting (ZFS) comparable its splitting, which would also blur the two transitions into a single line. On the other hand, due to the large difference between the longitudinal and transverse electric field susceptibilities ($d_{\parallel} = 0.35 \text{ Hz cm/V}$ and $d_{\perp} = 17 \text{ Hz cm/V}$ [5]), random local electric field will, on average, cause a splitting much stronger than its ZFS shifting and result in a two peak spectrum.

In our low magnetic field dipole-dipole coupling model, we will therefore neglect the contribution of the strain, local magnetic field and longitudinal electric field. We also don't take into account the hyper-fine structure of the NV center due of the large inhomogeneous broadening of the transitions (Fig. 1b). We will then consider the following spin Hamiltonian for the NV^- ground state :

$$\mathcal{H}_s = DS_z^2 + \gamma_e \vec{B}_{\text{ext}} \cdot \vec{S} + d_{\perp} [E_x(S_y^2 - S_x^2) + E_y(S_x S_y + S_y S_x)] \quad (1)$$

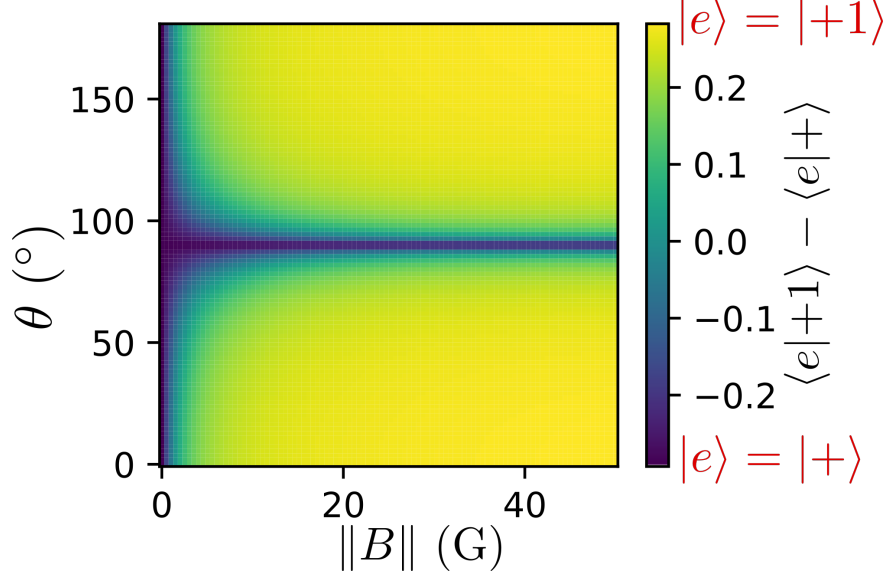


FIG. 2. Numerical simulations of the closeness of the Hamiltonian most excited state $|e\rangle$ with the states $|+1\rangle$ and $|+\rangle$, as a function of the magnetic field amplitude and angle θ with respect to the NV axis.

Where $D = 2.87$ GHz is the zero field splitting and $\gamma_e = 2.8$ MHz/G the gyromagnetic ratio of the electron.

In the absence of an external magnetic field, the symmetry in the (xy) plane allows us to chose the x direction along the electric field. The eigenstates of \mathcal{H}_s then become $\{|0\rangle, |+\rangle = \frac{|+1\rangle + |-1\rangle}{\sqrt{2}}, |-\rangle = \frac{|+1\rangle - |-1\rangle}{\sqrt{2}}\}$.

In the presence of non-zero magnetic field, let us call the Hamiltonian eigenstates $\{|g\rangle, |d\rangle, |e\rangle\}$. Fig. 2 shows how close the $|e\rangle$ state is to the $|+1\rangle$ and $|+\rangle$ states as a function of the external magnetic field. Looking at the closeness of $|d\rangle$ to $|-1\rangle$ and $|-\rangle$ would show similar results, while $|g\rangle$ is pretty much equals to $|0\rangle$ for $B < 100$ G.

This tells us that in most cases, the $\{|0\rangle, |+\rangle, |-\rangle\}$ basis is only the good Hamiltonian basis for magnetic field smaller than a few Gauss, except in the case of pure transverse magnetic field where the $\{|0\rangle, |+\rangle, |-\rangle\}$ basis remains a good basis even for sizable magnetic fields.

II. SAMPLES

A faire à la fin pour être sur des figures du main text.

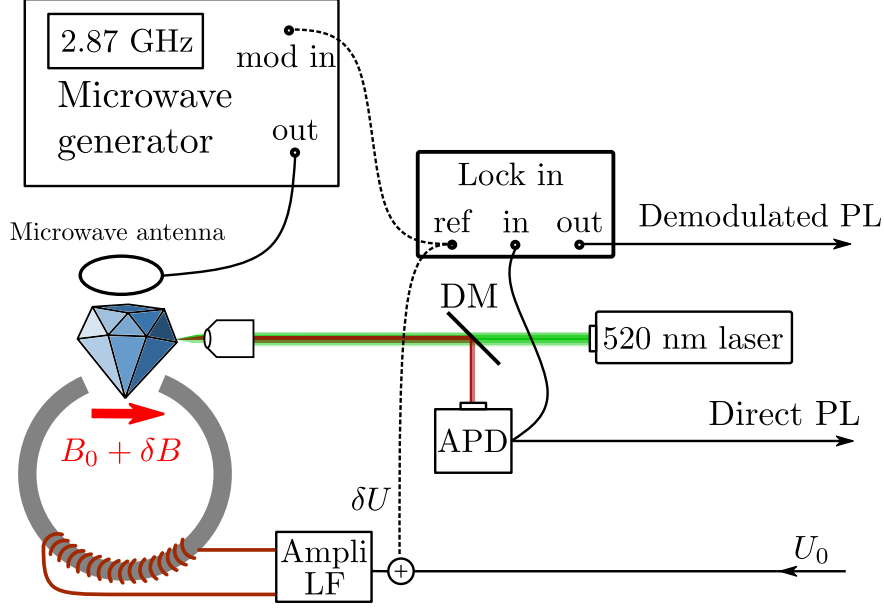


FIG. 3. Experimental Setup

III. EXPERIMENTAL SETUP

Fig. 3 shows the general purpose experimental setup used for all the experiments presented in this article.

The optical polarization and readout of the spins is done by focusing a green laser on the diamond sample with an objective lens([ref]), and collecting the back-scattered red fluorescence from the NV center on an avalanche photo-diode (APD, REF). The laser is filtered out using a dichroic mirror (DM, ref) and a notch filter. The NV⁰ fluorescence is filtered using an additional 645 nm longpass filter.

The laser used here is a [REF], providing pulses of X ns at a rate of 20 MHz, with an average power of 0.5 ~ 5 mW. The trigger of the pulses is generated externally in order to achieve fast gating of the laser for the T_1 measurement. We previously did similar experiment using a continuous 532 nm laser and observed no difference in the behavior of the spins.

The magnetic field is provided by a homemade electromagnet composed of a c-shape iron core and copper wires. The magnet is mounted on two mechanical rotation stages, allowing a control on the polar and azimuthal angle of the magnetic field within a fraction of a degree and is alimented through a low frequency amplifier (REF)

The microwave field is generated by a Rhode & Shwarz SMB 100A and is emitted with a handmade loop antenna. The field is gated by a [REF minicircuit] switch controlled

externally.

A lock-in amplifier is used either to modulate the microwave amplitude for ODMR measurement, or to add an oscillatory magnetic field for the magnetometry protocol. In both case we use a modulation frequency ~ 1 kHz and demodulate the APD signal.

IV. EXPERIMENTAL DETAILS

A. T_1 fitting Protocol

The T_1 profile that we observe with our samples is neither purely exponential, nor purely stretched exponential, which is to be expected when the dipole-dipole spin decay is comparable to the phonon decay.

Fig. 4 shows the result of a lifetime measurement, measured with the subtraction protocol described in the main text, for zero and non-zero magnetic field. The result is fitted with exponential and stretched-exponential (with a stretch factor $\beta = 0.5$) functions. We can see that for the shorter lifetime (zero field), the measurement follows more closely the stretched-exponential profile, while the longer lifetime is closer to the exponential one (except at very short times).

In order to directly compare the results from different magnetic fields, we therefore decided to fit each T_1 measurement with both a stretched and exponential decay : $S(\tau) = A \exp\left(-\frac{\tau}{T_1^{\text{ph}}} - \sqrt{\frac{\tau}{T_1^{\text{dd}}}}\right)$. To add consistency to the measurement of T_1^{dd} , we decided to fix T_1^{ph} for each sample, leaving T_1^{dd} and the signal amplitude as the only free parameters in the fitting procedure. The value chosen for samples [REF] and [REF] was $T_1^{\text{ph}} = 3.62$ ms. Fig. 1 of the main text shows the result of fitting the same two measurement with this formula.

An other possibility would be to use an arbitrary stretched factor in the fitting function : $S(\tau) = A \exp\left(-(\frac{\tau}{T_1^{\text{ph}}})^\beta\right)$. Fig. 5 shows the optimal β parameter as a function of the external magnetic field, which confirms that the T_1 profile gets closer to a pure stretched-exponential in zero magnetic field.

B. Spectral range of the dipole-dipole cross-relaxations

In the absence of other

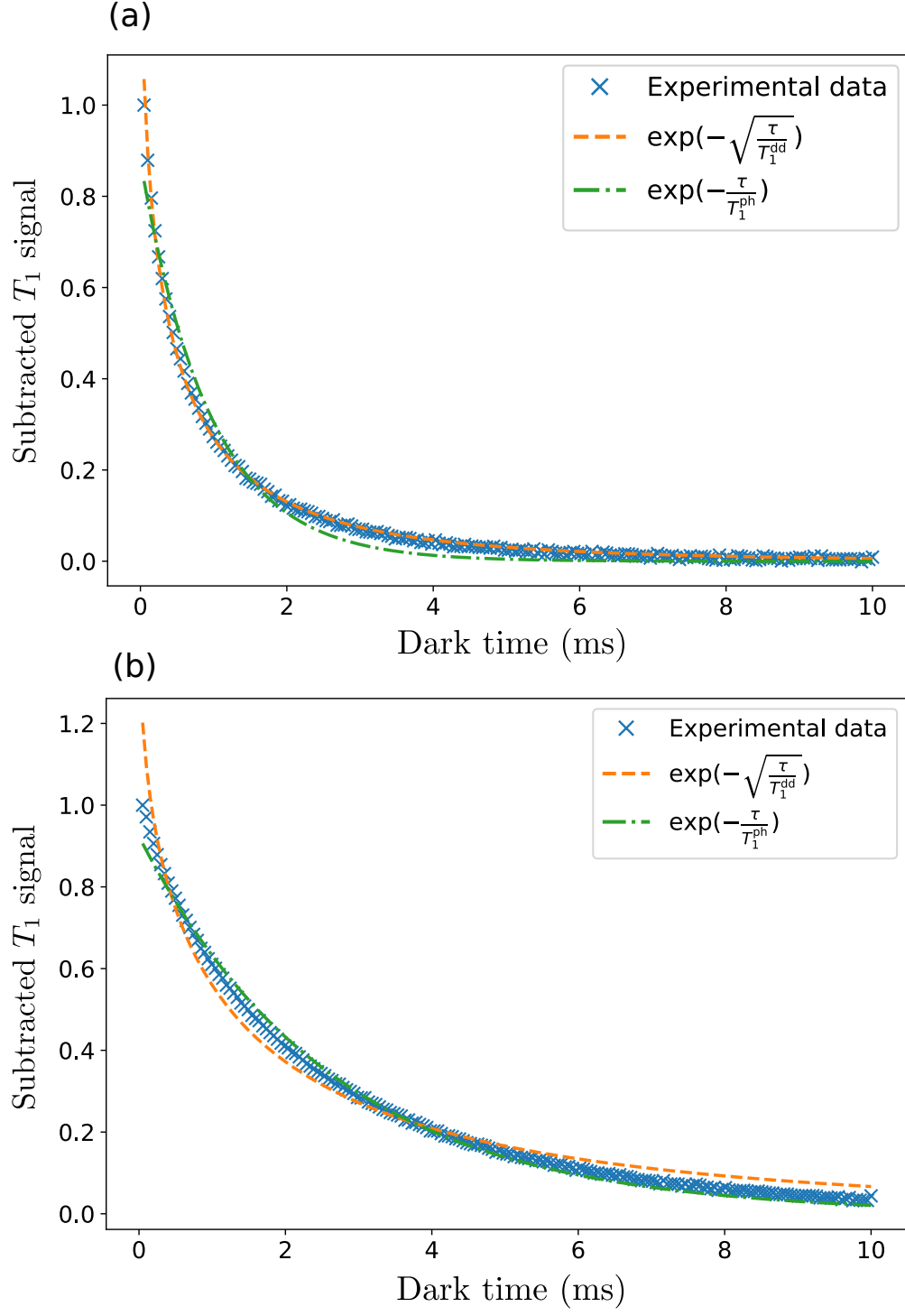


FIG. 4. T_1 measurement with purely exponential and purely stretched exponential fits (a) in zero magnetic field (b) in non-zero magnetic field

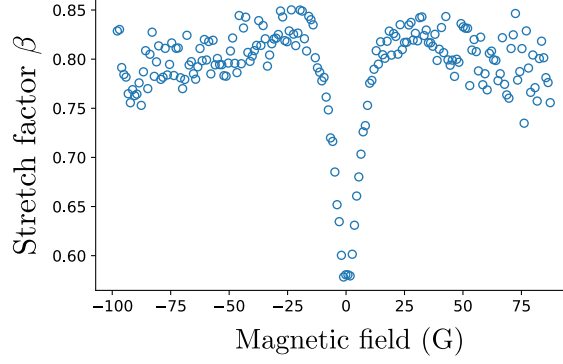


FIG. 5. Best stretch factor β for a T_1 fit of the form $f(\tau) = A \exp\left(-(\frac{\tau}{T_1})^\beta\right)$ as a function of a randomly oriented magnetic field amplitude

An experimental signature of the fluctuator hypothesis developed in [2] is to measure the depolarization rate for two near-resonant classes : if there are indeed very fast decaying NV centers (fluctuators with lifetime $T_1^f < 100ns$), then the spectral width of the fluctuator would be increased beyond $1/T_2^*$ (which we assume to be homogeneous among all spins in the crystal), which means that they would be able to exchange spin quanta (flip-flop) with non-resonant NV detuned by $\Delta\nu$ such that $2\pi/T_1^f > \Delta\nu > 2\pi/T_2^*$

In order to verify this claim, we have to measure the spectral overlap between two classes, which in the absence of fluctuator should be proportional to the flip-flop rate, and compare it to the actual flip-flop rate which we can measure through the depolarization rate of the spins.

Fig. 6 shows the results of such an experiment where we measured the stretched part of the NV's decay rate, which is very well fitted by a Lorentzian of width $\sigma = 8.04MHz$, and compare it to an ODMR line of a single class of NV centers, stretched by a factor of $\sqrt{2}$ and 2 to simulate the spectral overlap of the two classes (discussed bellow). One should notice that, not only is $1/T_1^{dd}$ significantly larger than the ODMR profile, it also doesn't have the same shape.

We should note that this broadening can not be explained by the dipole-dipole interaction strength : for a sample with 3 ppm of NV centers, the average dipole-dipole interaction strength between two nearest NV centers $J_0/r^3 \sim 27$ kHz which is several order of magnitude lower than the broadening we observe.

As illustrated on Fig. 7, we define the spectral overlap $S(\Delta\nu)$ between two spins of spectral response $S_1(\nu)$ and $S_2(\nu)$, centered respectively on the frequencies ν_1 and ν_2 where

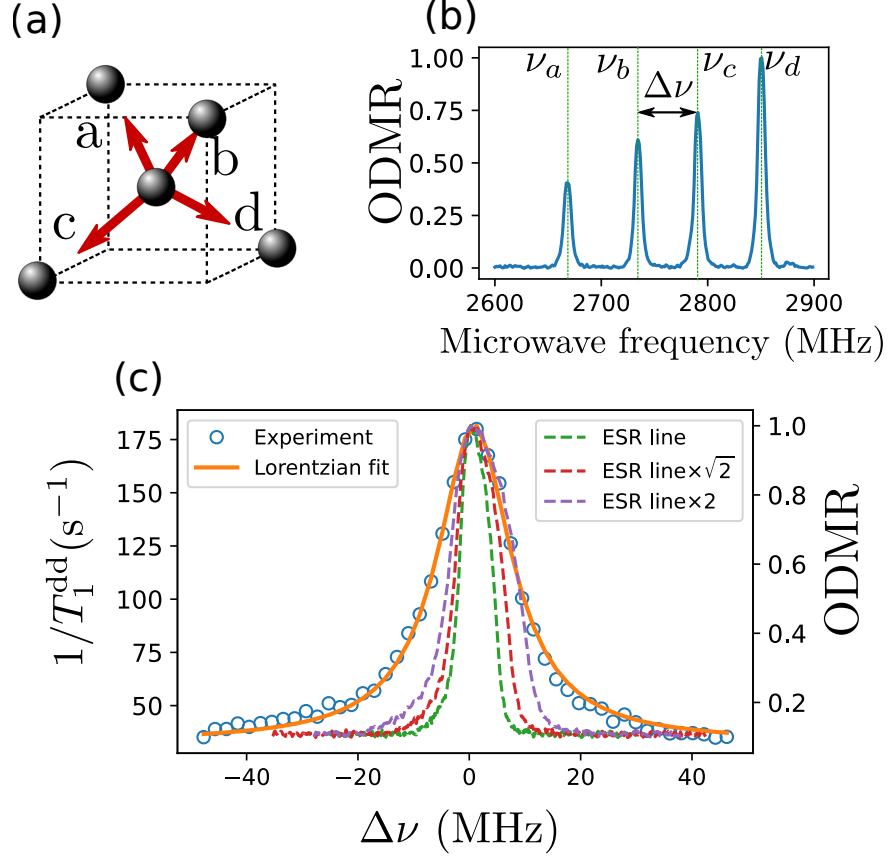


FIG. 6. Dipole-dipole depolarization for two near-resonant classes. (a) Sketch of the four possible orientations ("classes") in a single crystal diamond lattice. (b) ODMR spectrum showing four $|0\rangle \rightarrow |-1\rangle$ resonances corresponding to the four spin classes. The detuning $\Delta\nu$ between the classes b and c was controlled by changing the orientation of the external magnetic field. (c) Stretch part of the lifetime decay for the spins resonant with ν_c as a function of the detuning $\Delta\nu$ (blue circles), fitted by a Lorentzian with half width at half maximum 8.04 MHz. Single class ESR line stretched by a factor of 1, $\sqrt{2}$ and 2 are added for comparison

$\Delta\nu = \nu_2 - \nu_1$ as :

$$S(\Delta\nu) = \int S_1(\nu, \nu_1) S_2(\nu, \nu_2) d\nu \quad (2)$$

In order to approximate the spectral overlap in our experiment, we will consider the analytical solution in the Gaussian and Lorentzian case :

- For two gaussians of standard deviation σ , the spectral overlap as a function of the

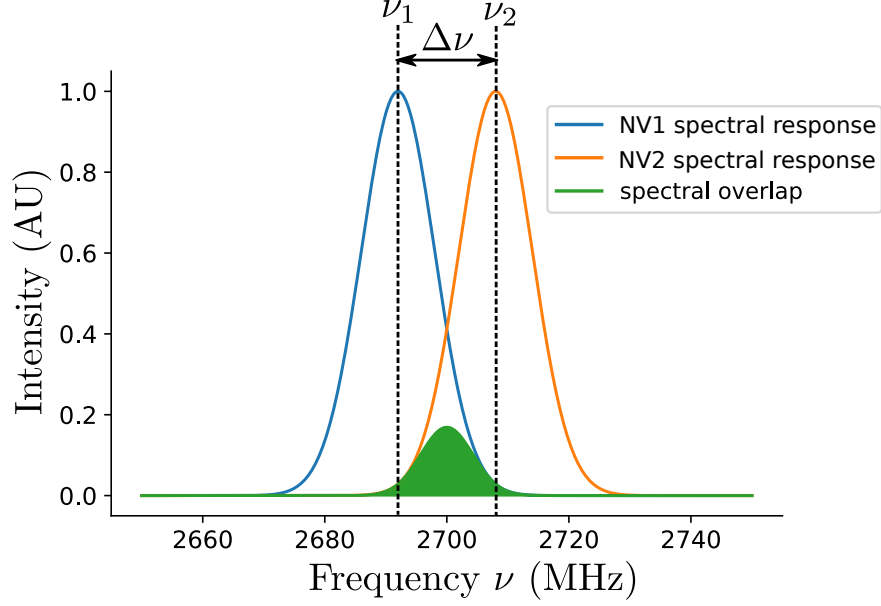


FIG. 7. Illustration of the spectral overlap for two gaussian spectra

detuning $\Delta\nu = \nu_1 - \nu_2$ is itself a gaussian of standard deviation $\sigma' = \sqrt{2}\sigma$. :

$$\begin{aligned}
 S(\Delta\nu) &\propto \int \exp\left(-\frac{(\nu - \nu_1)^2}{2\sigma^2}\right) \exp\left(-\frac{(\nu - \nu_2)^2}{2\sigma^2}\right) d\nu \\
 &\propto \exp\left(-\frac{(\Delta\nu)^2}{4\sigma^2}\right)
 \end{aligned}$$

- For two Lorentzian profile with width σ , the overlap function is itself a Lorentzian with width $\sigma' = 2\sigma$:

$$\begin{aligned}
 S(\Delta\nu) &\propto \int \frac{1}{1 + \frac{(\nu - \nu_1)^2}{\sigma^2}} \cdot \frac{1}{1 + \frac{(\nu - \nu_2)^2}{\sigma^2}} d\nu \\
 &\propto \frac{1}{1 + \frac{(\Delta\nu)^2}{4\sigma^2}}
 \end{aligned}$$

The ODMR lines that we measure are neither Lorentzian nor Gaussian (although they tend to be closer to Gaussians), and can even be asymmetric. Nevertheless, the overlap between two classes can most likely be approximated by a single class ODMR profile stretched by a factor between $\sqrt{2}$ and 2.

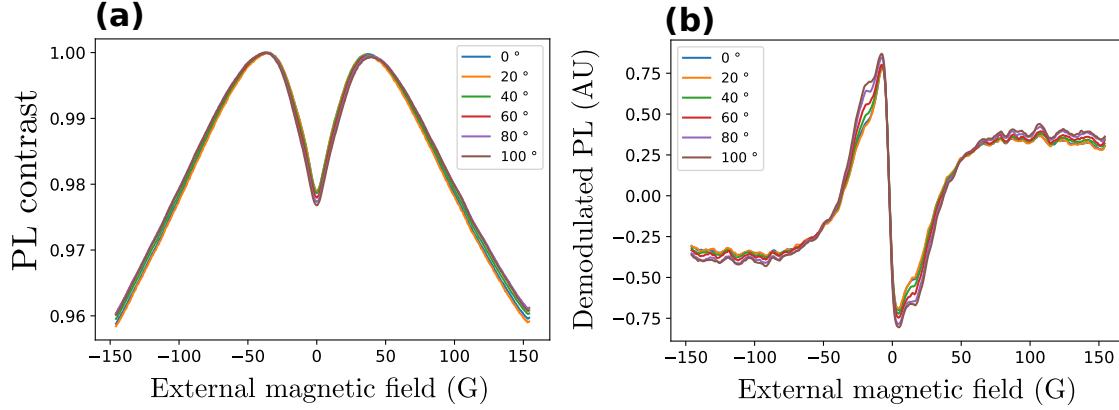


FIG. 8. Effect of the polarization of the incident laser. (a) Photoluminescence as a function of randomly oriented magnetic field amplitude for various polarization angle. (b) Demodulated PL in the same conditions

V. LES DÉTAILS QUI TUENT

A. Effect of laser polarization

Previous studies [1, 3] reported the presence of a photoluminescence dip in zero magnetic field which was heavily dependent on the laser polarization angle with respect to the diamond axes and the magnetic field.

We did not observe a strong dependence on the laser polarization with the samples used in this study. Fig.8 shows the photoluminescence from one of our sample as a function of the magnetic field, either directly or with a modulation of the magnetic field, for 6 randomly chosen polarization angle and saw no major difference.

In particular, we did not observe the apparition of an anti-line inside the main dip, unlike what was observed in the two previously cited work. We expect that the main reason behind the different behaviors is that we seem to observe far grater spin depolarization in zero-field, which we attribute to dipole-dipole coupling, and that this effect could hide smaller effects such as the one related to the laser polarization.

B. Alignment of B

La faudrait p-e montrer ce qu'il se passe pour un décalage de quelques degrés. A voir si j'ai déjà les plots

VI. EXTENSION OF THE FLUCTUATOR MODEL TO LOW MAGNETIC FIELDS

A. Summary of the NV-fluctuator model

As mentioned in the main text, we base our analysis on the NV-fluctuator model developed in [2] whose main hypothesis and conclusions we will summarize here :

The NV^- centers in the crystal are divided between two categories : "normal" NV centers (simply called NV) which, in the absence of dipole-dipole coupling would have a phonon-limited T_1 ($T_1^{\text{NV}} \sim \text{ms}$), and fluctuators who are NV centers with an additional, fast, depolarization mechanism, such that their lifetime $T_1^f < 100 \text{ ns}$. Having such a short lifetime, the fluctuators are pretty much unpolarized by the green laser, making them invisible in standard optical NV measurement protocol (T_1 , ODMR, etc.).

Assuming a homogeneous distribution of the fluctuators in the bulk of the crystal, the authors conclude that the fluctuators create an additionnal decay channel for the NV population, through dipole-dipole interaction, characterized by a decay rate γ which follows the probability distribution :

$$\rho(\gamma) = \frac{e^{-1/(4\gamma T)}}{\sqrt{4\pi\gamma^3 T}} \quad (3)$$

Where the timescale T is defined as

$$\frac{1}{T} = \left(\frac{4\pi n_f J_0 \bar{\eta}}{3} \right)^2 \frac{\pi}{\gamma_f} \quad (4)$$

Where n_f is the fluctuator density in the crystal in nm^{-3} , $J_0 = 52 \text{ MHz} \cdot \text{nm}^3$ is the characteristic dipole-dipole strength between two spins, γ_f is the fluctuator intrinsic decay rate and $\bar{\eta}$ is a dimension-less number which characterizes the average dipole-dipole interaction between the NV centers and the fluctuators (resonance conditions, relative orientations etc. Further details are given below).

The polarization dynamics of the averaged ensemble of NV centers then follows :

$$P(t) = \int_0^\infty \rho(\gamma) e^{-\gamma t} d\gamma = e^{-\sqrt{t/T}} \quad (5)$$

B. Dipole-Dipole Hamiltonian between two NV^- centers

C. 121 VS 22

D. 100 vs 0B

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