

## REVIEW

1) Normal DISTRIBUTION of population

2) Now, sample ~~test~~ should be a proportionally normal

3) Either find area from  $[0, 3.3]$  and subtract from 1 or  $(8 - 3.3) \times 0.125 = 0.5875$

4)  $P(n < 6.1) = 6.1 \times 0.125 = 0.7625$

5) The amount is a  $z$  score so using the table  $z$  score of 1.13  $\Rightarrow$  area of 0.8708

6)  $z$  score of Area 0.9559 (use table) = 1.75

7)  $P(-2.41 \leq z \leq 0)$

Use table find  $P(0)$  &  $P(-2.4)$

Subtract  $P(0) - P(-2.4) = 0.5 - 0.0080 = 0.4920$

8) The temperatures are normally distributed. Look at the  $z$  score for an area of 0.40 -0.25 is the score.

9)  $z_{0.36} = z$  score with area of 0.36 to the right  
 Look at chart find area of  $1 - 0.36$   
 $0.64 \Rightarrow z = 0.36$   
 area to right

10) Since mean = 100 &  $\sigma = 15$  find  $z$  scores for  
 $85 \pm 125$  they are  $-15/15 = -1$  and  $25/15 = 1.667$

Corresponding to areas of 0.9525 & 0.1587

$$0.9525 - 0.1587 = 0.7938$$

11)  $\mu = 15.2, \sigma = 0.9, P(x > 15.2) = 0.50$

This is "obvious" because in a normal distribution half the values are above the mean and half below

12) Using Central Limit theorem, we calculate a standard deviation of  $\frac{\sigma}{\sqrt{n}} = \frac{14}{\sqrt{49}} = 2$ . We calculate a  $z$  score of  $\frac{96.8 - 89}{2} = 1.4$ . This gives an area

of 0.9192 to the LEFT. Therefore the area  
Desired is  $1 - 0.9192 = 0.0808$

13)  $Z_{\alpha/2} \Rightarrow 91\%$  confidence

91% confidence implies  $\alpha/2 = 0.045$   
 $1 - 0.045 = 0.9550$

corresponds to Z-score 1.70

14)  $0.62 < p < 0.72 = p \pm E$   
 $E = (0.72 - 0.62)/2 = 0.05$   
 $0.62 \pm E = 0.67$   
 $0.67 \pm 0.05$

15)  $0.686 < p < 0.712$  find  $\hat{p}$   
 $\hat{p} - E < p < \hat{p} + E$   
 $E = (0.712 - 0.686)/2 = 0.013$   
 $\hat{p} = 0.686 + 0.013 = 0.699$

16) 90% confidence,  $n = 430$ ,  $x = 80$ , find  $E$   
\* Round to 5 decimal places, I lost 30 min by not  
rounding my calculations \*

$$E = Z_{\alpha/2} \sqrt{\frac{\hat{p}\hat{q}}{n}} \quad \hat{p} = \frac{80}{430} \quad \hat{q} = 1 - \hat{p} \quad \alpha = 10$$

$$Z_{0.10/2} = Z_{0.05} = 1.645$$

$$\hat{p} = \frac{80}{430} = 0.18605 \quad \hat{q} = 0.81395$$

$$E = 0.03087$$

17) 99% confidence,  $n = 1180$   $\hat{p} = 45$

$$\hat{q} = 55 \quad \alpha = 0.05$$

$$Z_{0.005} = 2.575$$

$$E = Z_{0.01/2} \sqrt{\frac{(45)(55)}{1180}} = 0.0373$$

$$18) n=96, x=43 \quad 98\%$$

$$\hat{p} = \frac{43}{96}$$

$$Z_{0.02/2} = 2.33$$

$$E = Z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = 2.33 \sqrt{\frac{(0.4479)(0.5521)}{96}} = 0.11826$$

$$p - E < p < p + E$$

$$0.330 < p < 0.566$$

$$19) E = 0.018 \quad \text{confidence } 99\% \quad p \text{ is UNKNOWN}$$

$$n = \frac{[Z_{\alpha/2}]^2 \cdot 0.25}{E^2}$$

$$n = \frac{[2.575]^2 \cdot 0.25}{[0.018]^2} = 5116.222994$$

$$n = 5117$$

$$20) E = 0.04, \text{ conf } 99\%, \hat{p} = 0.14, \hat{q} = 1 - \hat{p} = 0.86$$

$$\text{USING } n = \frac{[Z_{\alpha/2}]^2 \hat{p} \hat{q}}{E^2} = \frac{[2.575]^2 (0.14)(0.86)}{[0.018]^2} = 498.95$$

$$n = 497$$

$$21) 91\%, n=45, \sigma \text{ IS KNOWN, Skewed}$$

$$Z_{0.09/2} = 1.70$$

$$22) H_0: p = \frac{2}{1000} \quad H_1: p < \frac{2}{1000}$$

$$23) H_0: \mu = 63500$$

$$H_1: \mu > 63500$$

$$24) \alpha = 0.09 \text{ for Right-tailed test}$$

$$\text{USE Chart } Z_{0.9100} = 1.34$$

find area of 0.9100

$$25) \alpha = 0.05 \text{ for Left-tailed test}$$

$$Z_{0.05} = -1.645$$

$$26) \alpha = 0.1 \text{ for Two-tailed test}$$

$$Z_{0.05} = \pm 1.645$$

27) Statistic Right tailed test  $z = 1.43$   
Significance 0.05 implies  $z = 1.645$

$1.43 < 1.645$  fail to Reject  $H_0$

28) Asks for type 2 - Reject CLAIM when true

$H_0$  - 3% of adults suffer from shyness

Fail to reject CLAIM that 3% of adults  
suffer from shyness when  $> 3\%$   
suffer

29)  $H_0$  mileage = 21 mpg

Type I - reject claim mileage = 21 when it is 21