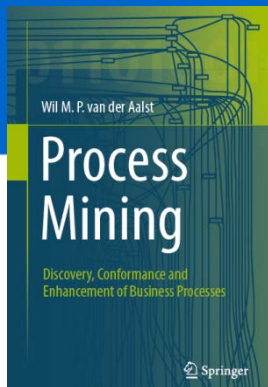


Process Mining: Data Science in Action

Alternative Process Discovery Techniques

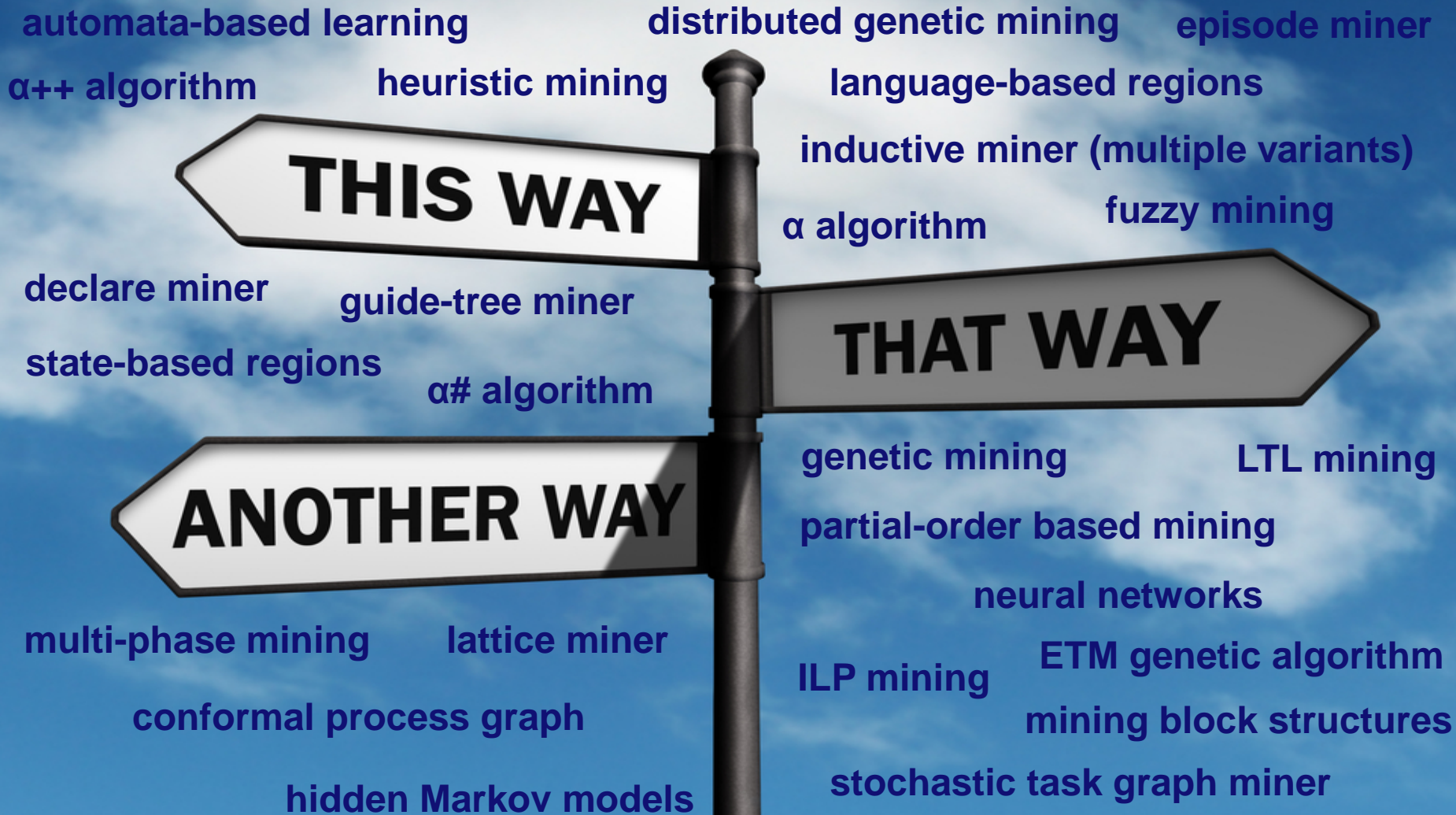
prof.dr.ir. Wil van der Aalst
www.processmining.org



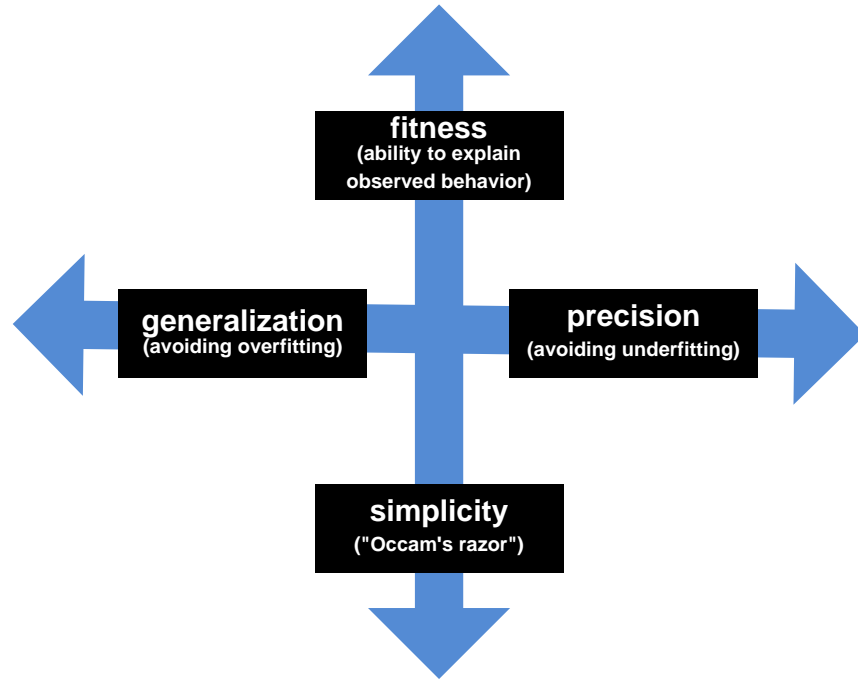
TU/e

Technische Universiteit
Eindhoven
University of Technology

Where innovation starts



Considerations

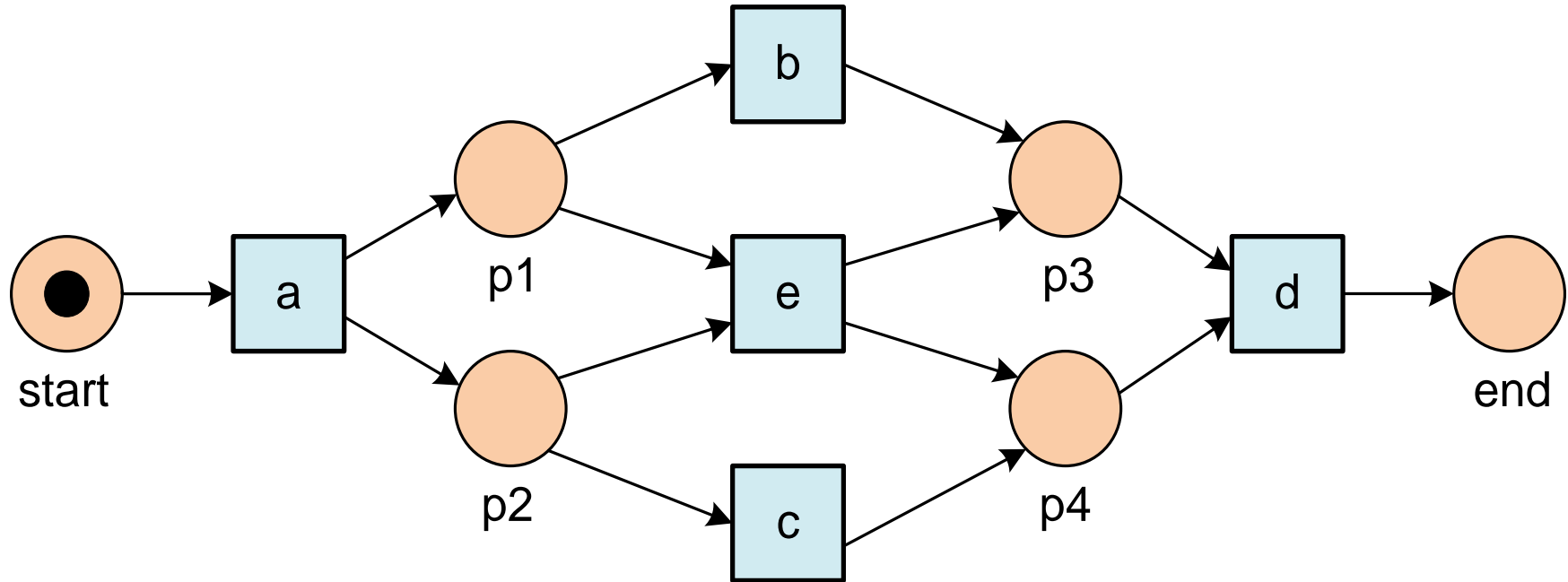


implementation versus approach

process discovery ...

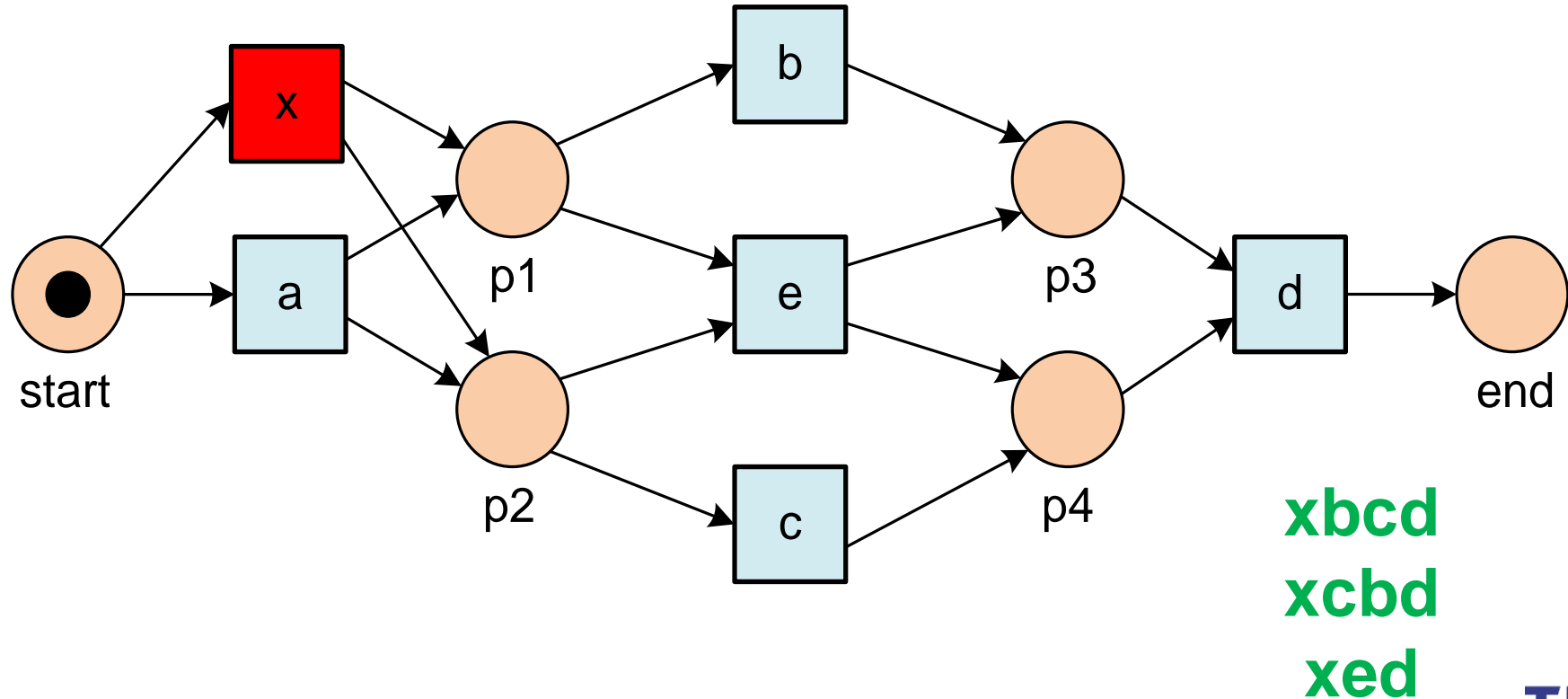
let's take a step back

Question: How to add behavior?

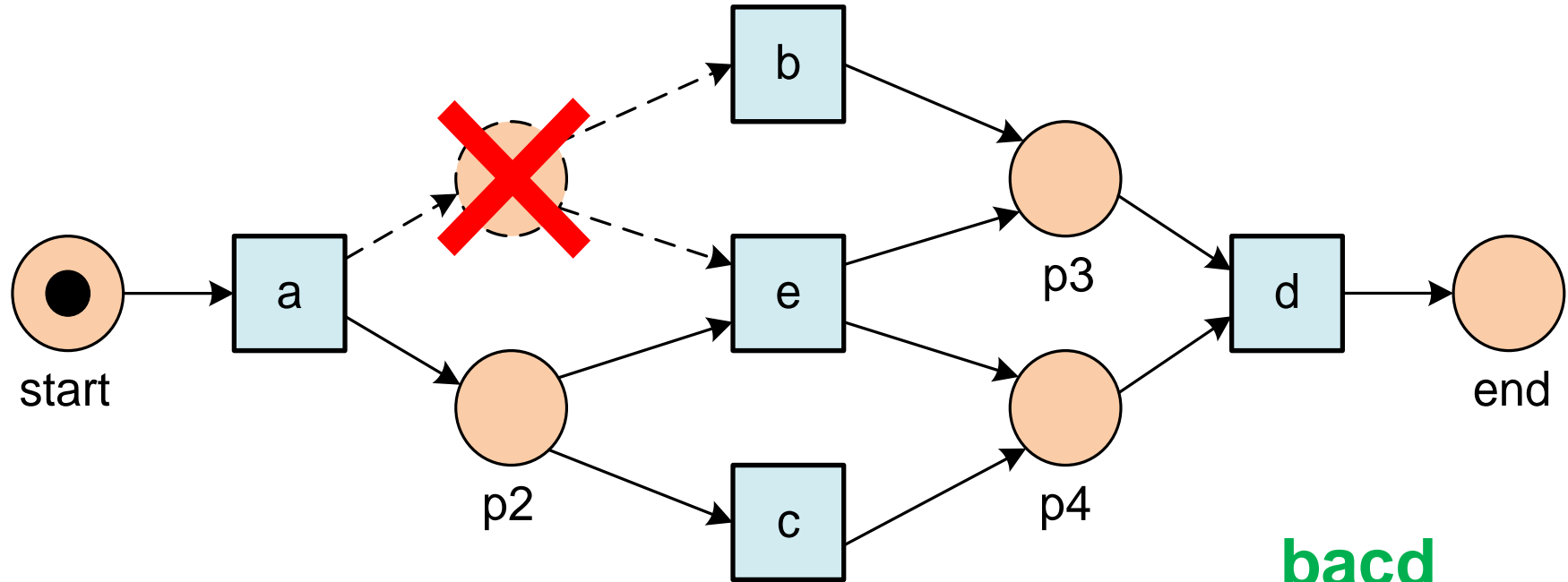


How to modify the Petri net such that it allows for **more** behavior (more traces, ignore termination)?

Answer (1/3): Adding transitions



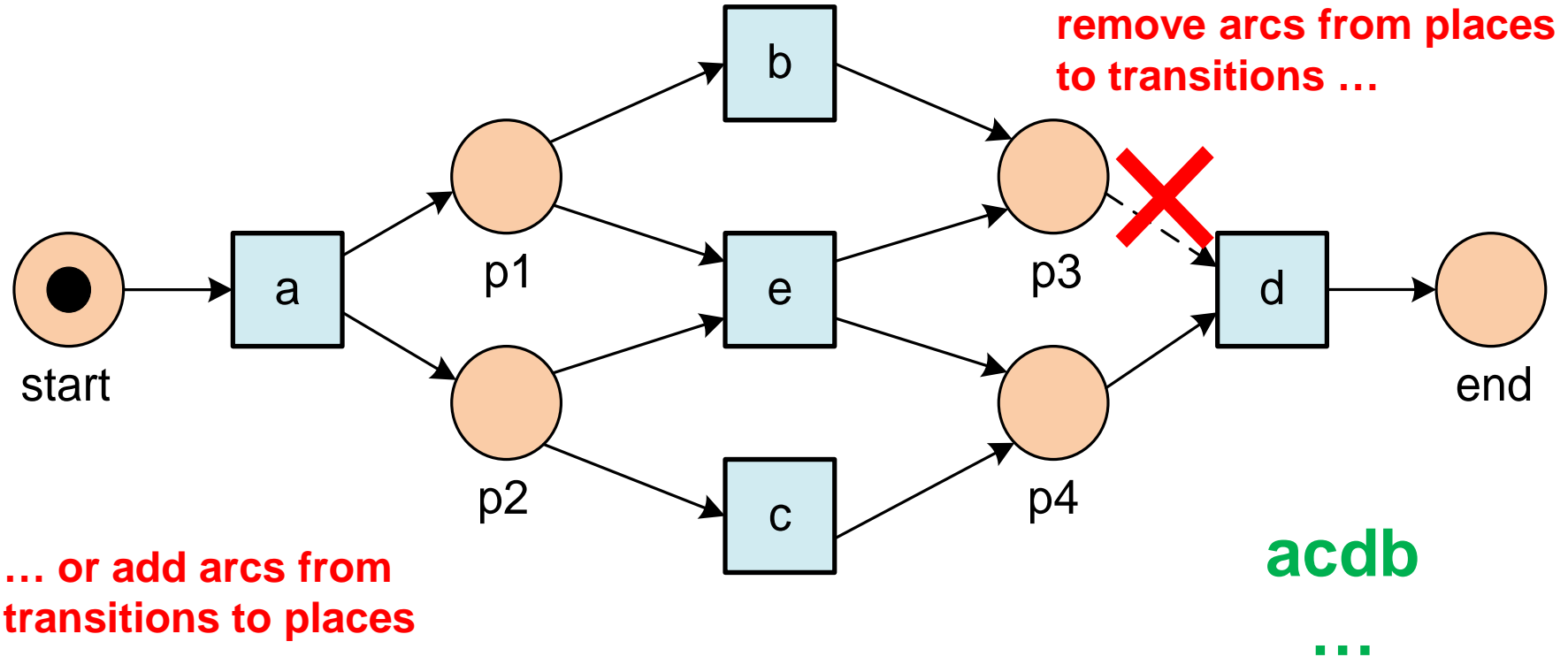
Answer (2/3): Removing places



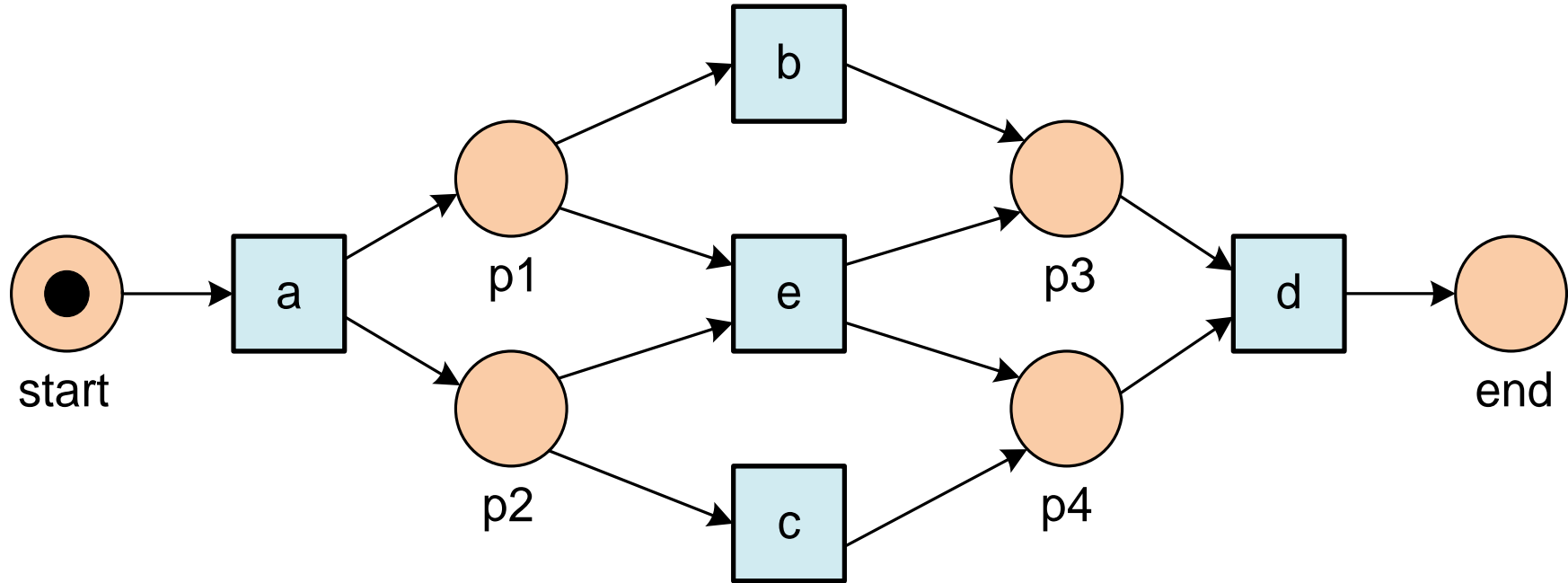
bacd

...

Answer (3/3): Removing/adding arcs

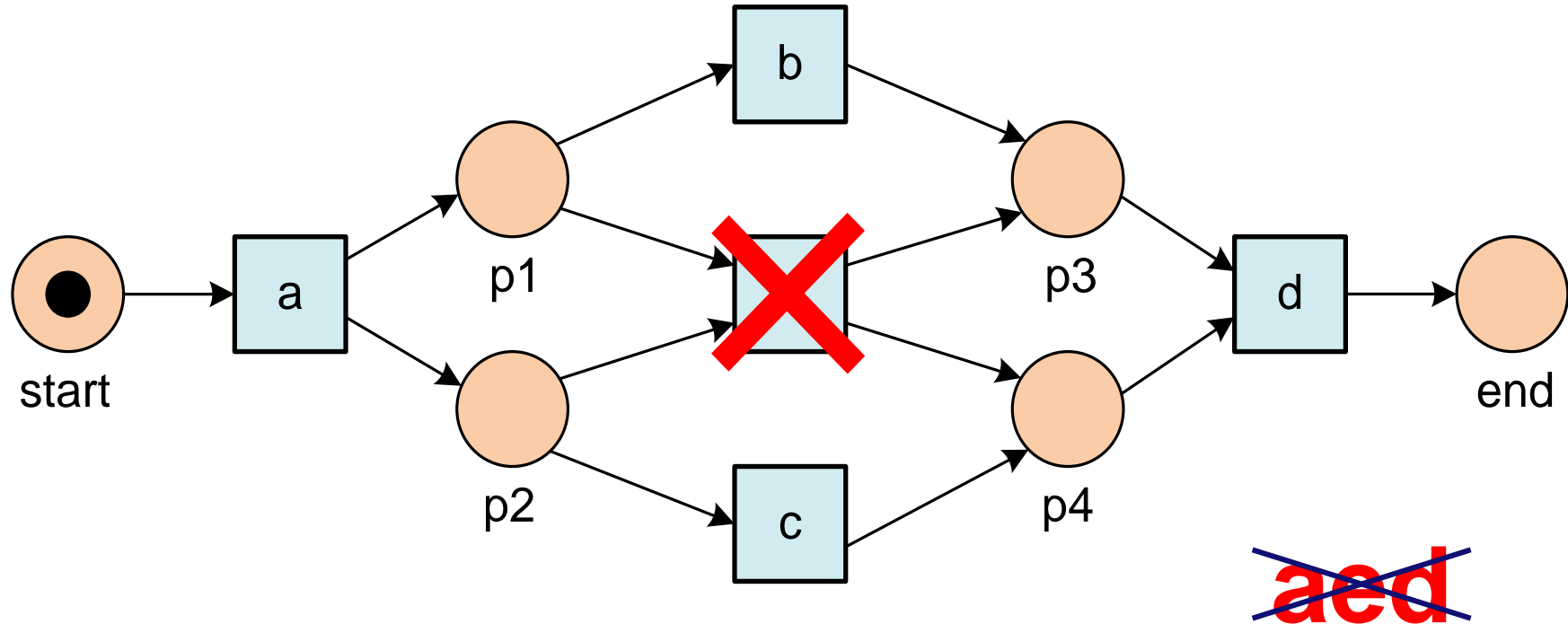


Question: How to remove behavior?

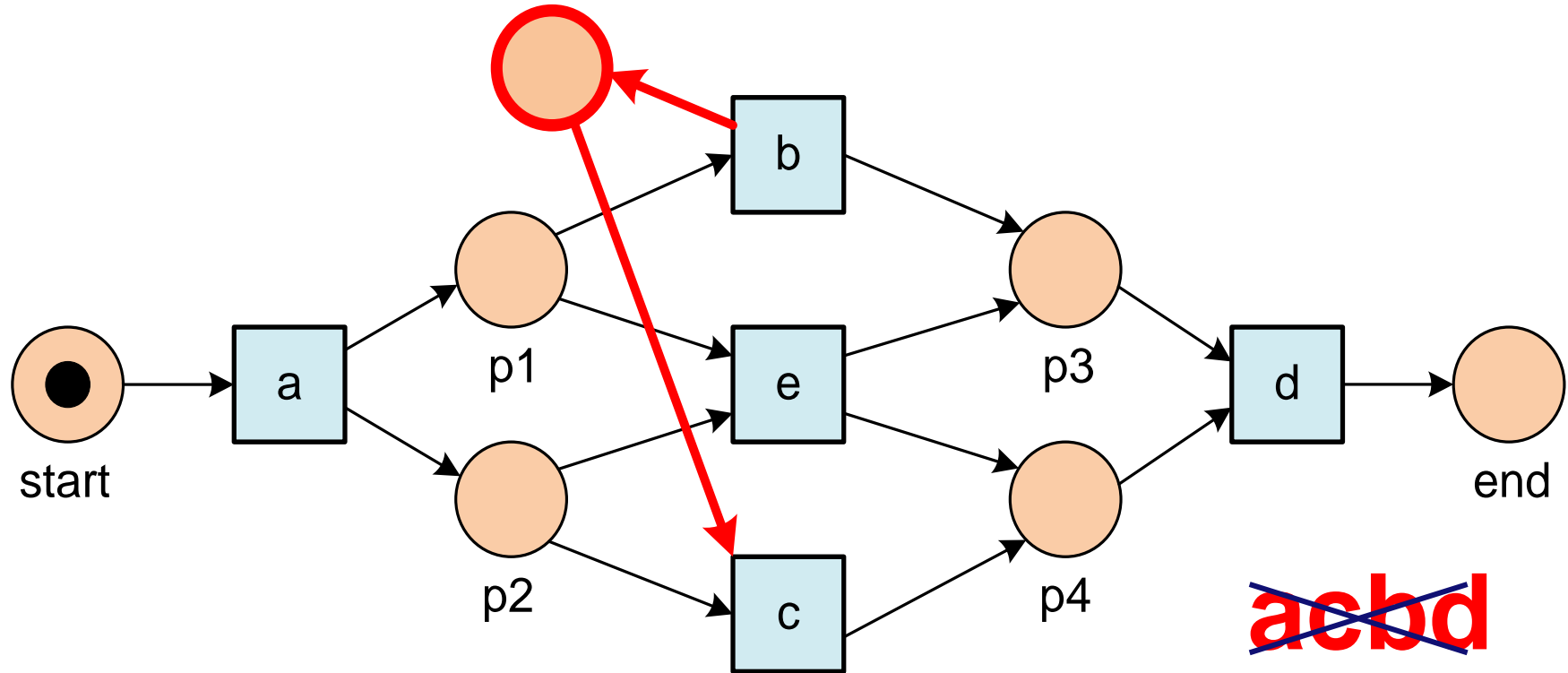


How to modify the Petri net such that it allows for **less** behavior (ignore termination)?

Answer (1/3): Removing transitions

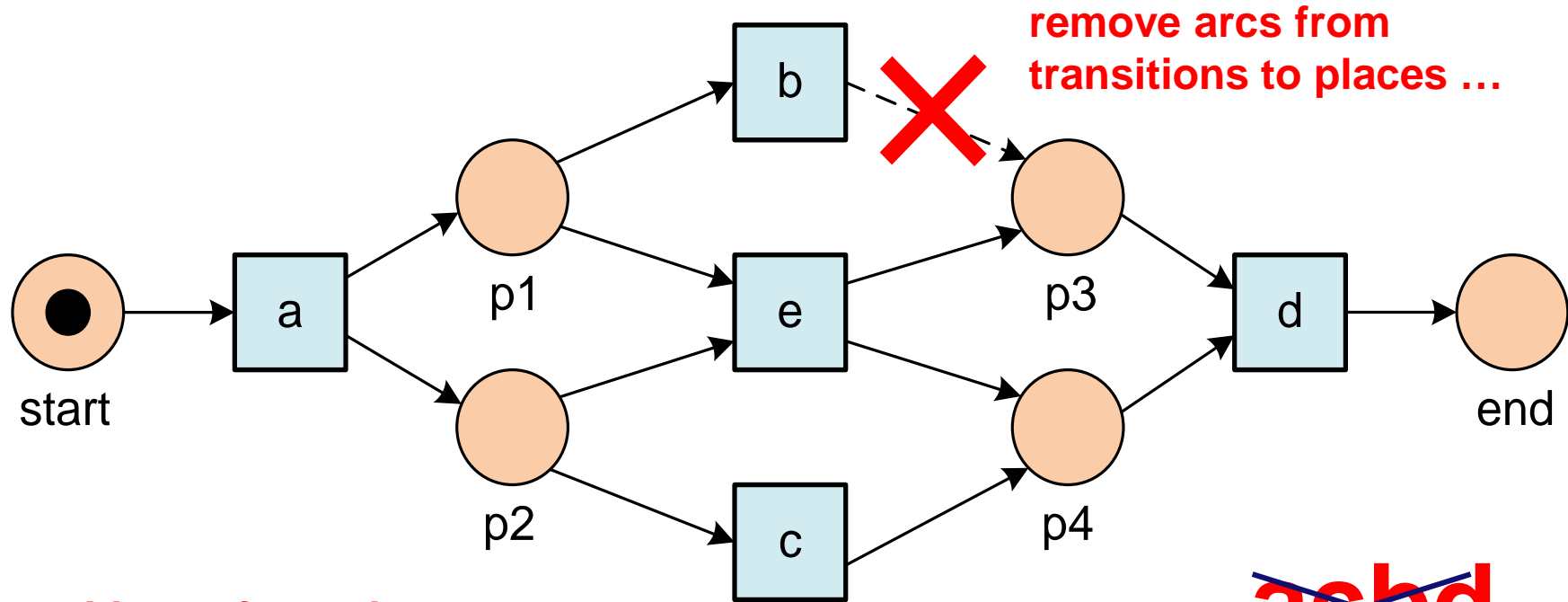


Answer (2/3): Adding places



~~acbd~~

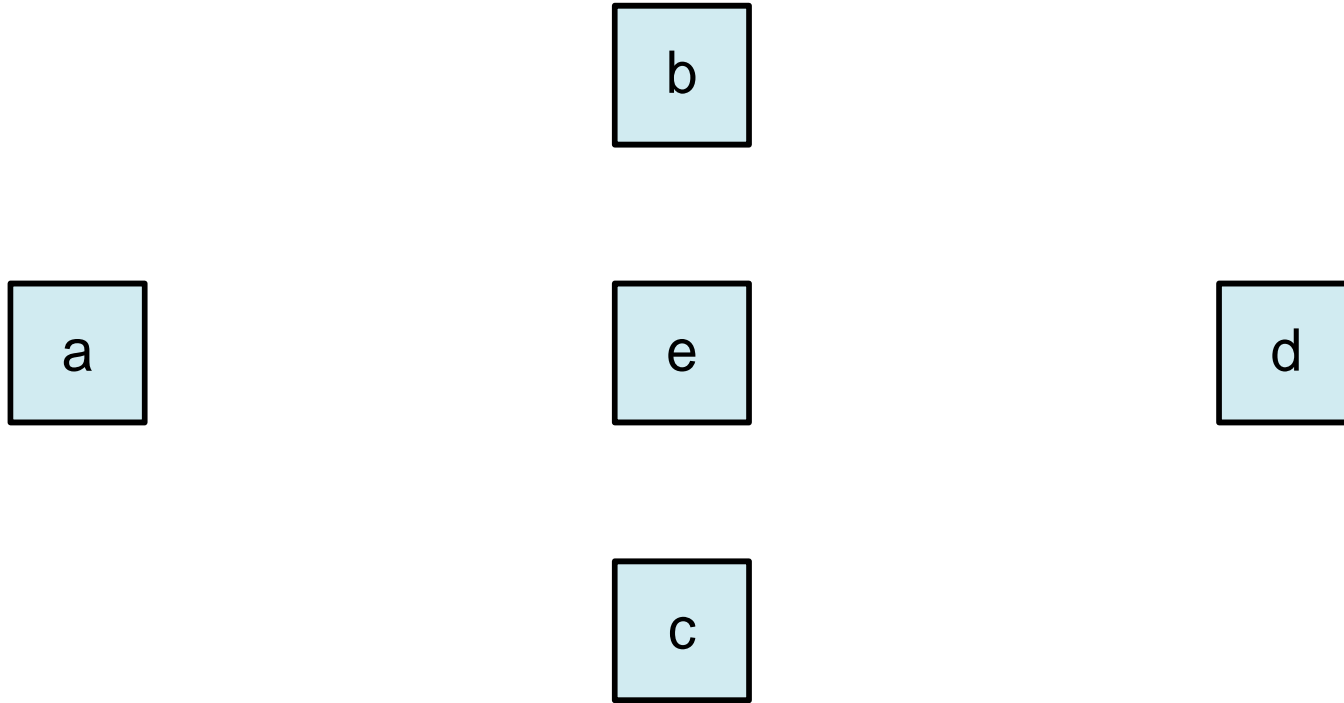
Answer (3/3): Removing/adding arcs



or add arcs from places to transitions ...

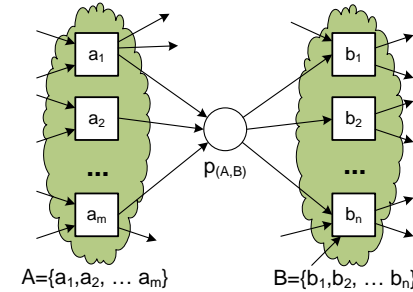
~~acbd~~

Process discovery = finding places

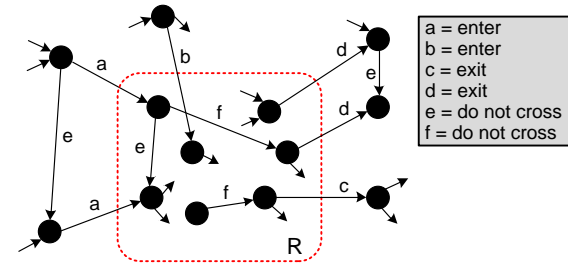


Examples of discovery techniques

- Alpha algorithm

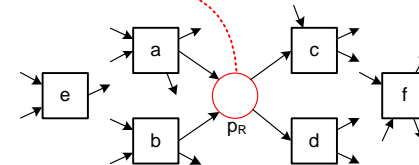


- State-based regions



- Next: language-based regions

$$c \cdot \mathbf{1} + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq 0$$





**language-
based
regions**

Looks complex, but the idea is simple ...

$$c \cdot 1 + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq 0$$

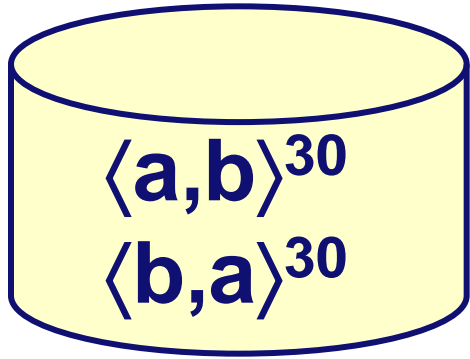
just says that places will never "go negative"

any solution (x,y,c) is a region

any region (x,y,c) is a feasible place

Defining A

$$c \cdot \mathbf{1} + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq \mathbf{0}$$

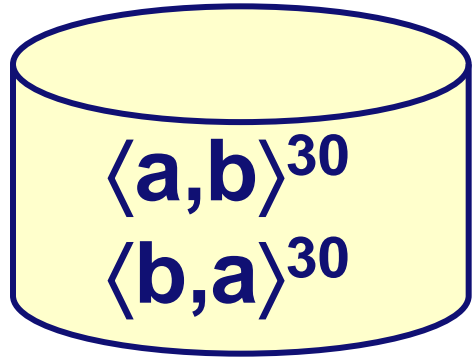


$$\mathcal{L} = \{\epsilon, \langle a \rangle, \langle b \rangle, \langle a, b \rangle, \langle b, a \rangle\}$$

$$A = \begin{matrix} & a & b \\ \begin{matrix} \langle a \rangle \\ \langle b \rangle \\ \langle a, b \rangle \\ \langle b, a \rangle \end{matrix} & \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 1 \\ 1 & 1 \end{pmatrix} \end{matrix}$$

Defining A'

$$c \cdot \mathbf{1} + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq \mathbf{0}$$

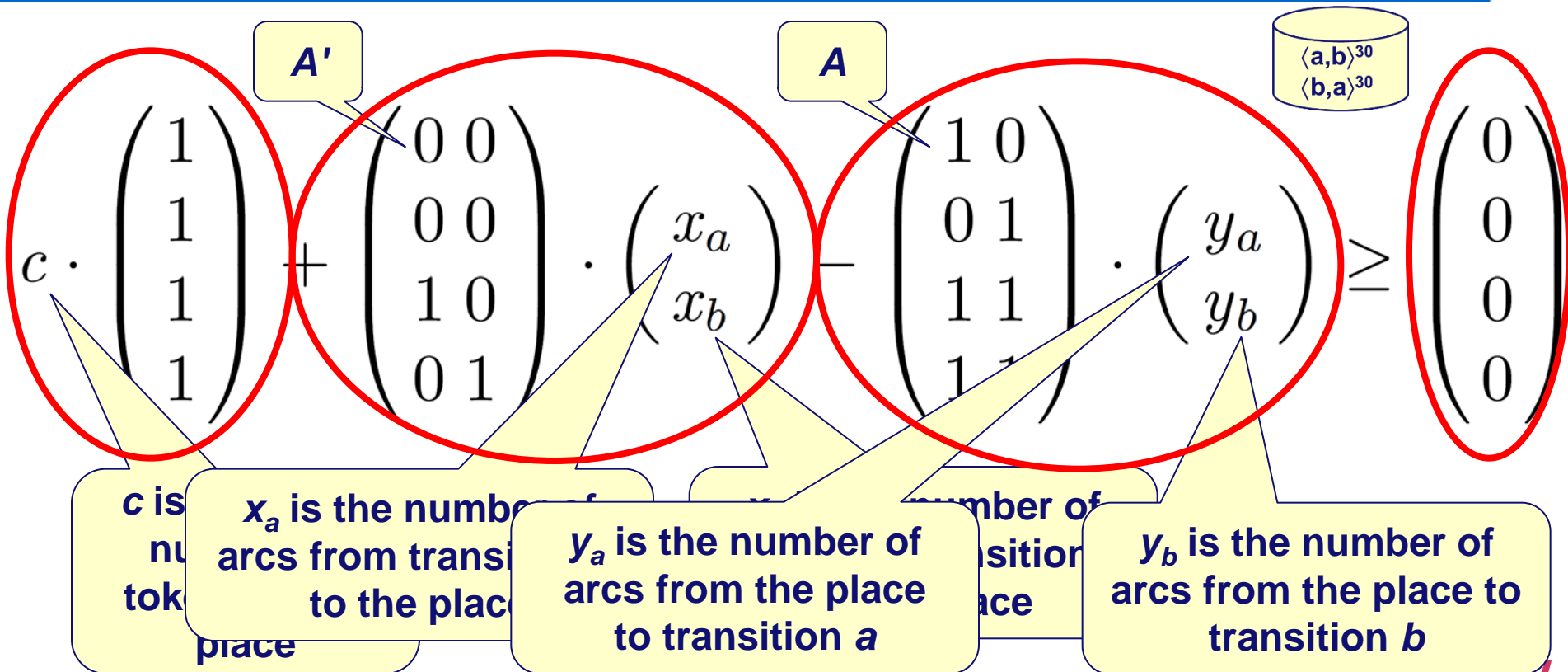


$$\mathcal{L} = \{\epsilon, \langle a \rangle, \langle b \rangle, \langle a, b \rangle, \langle b, a \rangle\}$$

$$A' = \begin{matrix} & a & b \\ \langle a \rangle & 0 & 0 \\ \langle b \rangle & 0 & 0 \\ \langle a, b \rangle & 1 & 0 \\ \langle b, a \rangle & 0 & 1 \end{matrix}$$

Inequation system

$$c \cdot \mathbf{1} + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq \mathbf{0}$$



Inequation system

$$c \cdot \mathbf{1} + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq \mathbf{0}$$

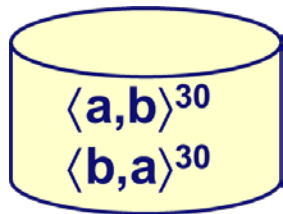
$$c \cdot \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_a \\ x_b \end{pmatrix} - \begin{pmatrix} 1 & 0 \\ 0 & 1 \\ 1 & 1 \\ 1 & 1 \end{pmatrix} \cdot \begin{pmatrix} y_a \\ y_b \end{pmatrix} \geq \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$c - y_a \geq 0$$

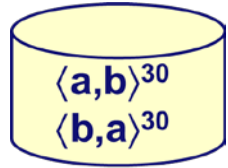
$$c - y_b \geq 0$$

$$c + x_a - y_a - y_b \geq 0$$

$$c + x_b - y_a - y_b \geq 0$$



Example solutions



$$c - y_a \geq 0$$

$$c - y_b \geq 0$$

$$c + x_a - y_a - y_b \geq 0$$

$$c + x_b - y_a - y_b \geq 0$$

$$c = 1$$

$$x_a = 0$$

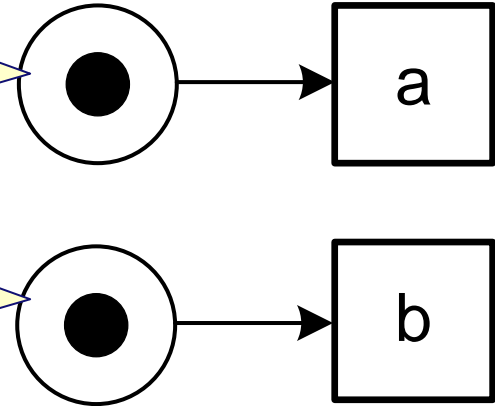
$$c = 1$$

$$x_a = 0$$

$$x_b = 0$$

$$y_a = 0$$

$$y_b = 1$$



Language-based regions

$$c \cdot \mathbf{1} + A' \cdot \mathbf{x} - A \cdot \mathbf{y} \geq 0$$

- Any solution is a feasible place.
- Additional constraints can be added easily (empty at end, limited fan-in or fan-out, etc.).
- **Goal function** can be used to select the most interesting places.
- **Optimization problem (e.g. ILP)!**
(ILP = Integer Linear Programming)

ProM's ILP miner

Constructs a Petri net with the selected search strategy.

ILP Variant Settings

Number of places:

Per Causal Dependency

Basic Representation

Per Causal Dependency

Before & After Transition

Before Transition

After Transition

ILP Extensions

Marked Graph

☐ T. van der Wier

All places have at most one incoming and at most one outgoing arc.

Pure Net

☐ T. van der Wier

No self loops are allowed.

Elementary Net

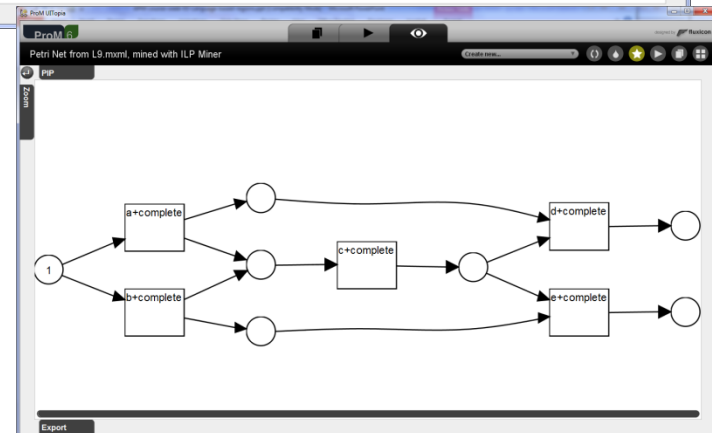
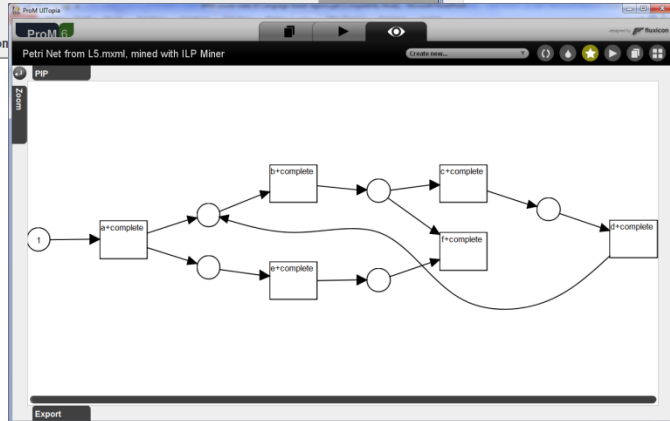
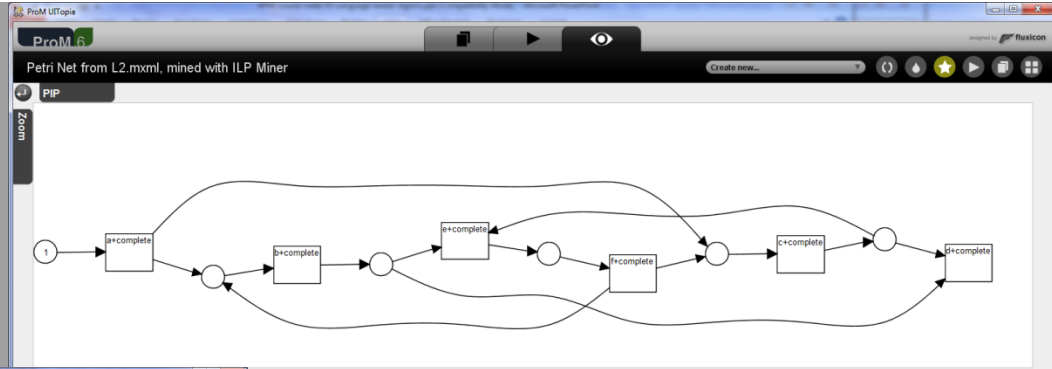
☐ T. van der Wier

Guarantees that a place can never contain more than one token.

State Machine

☐ T. van der Wier

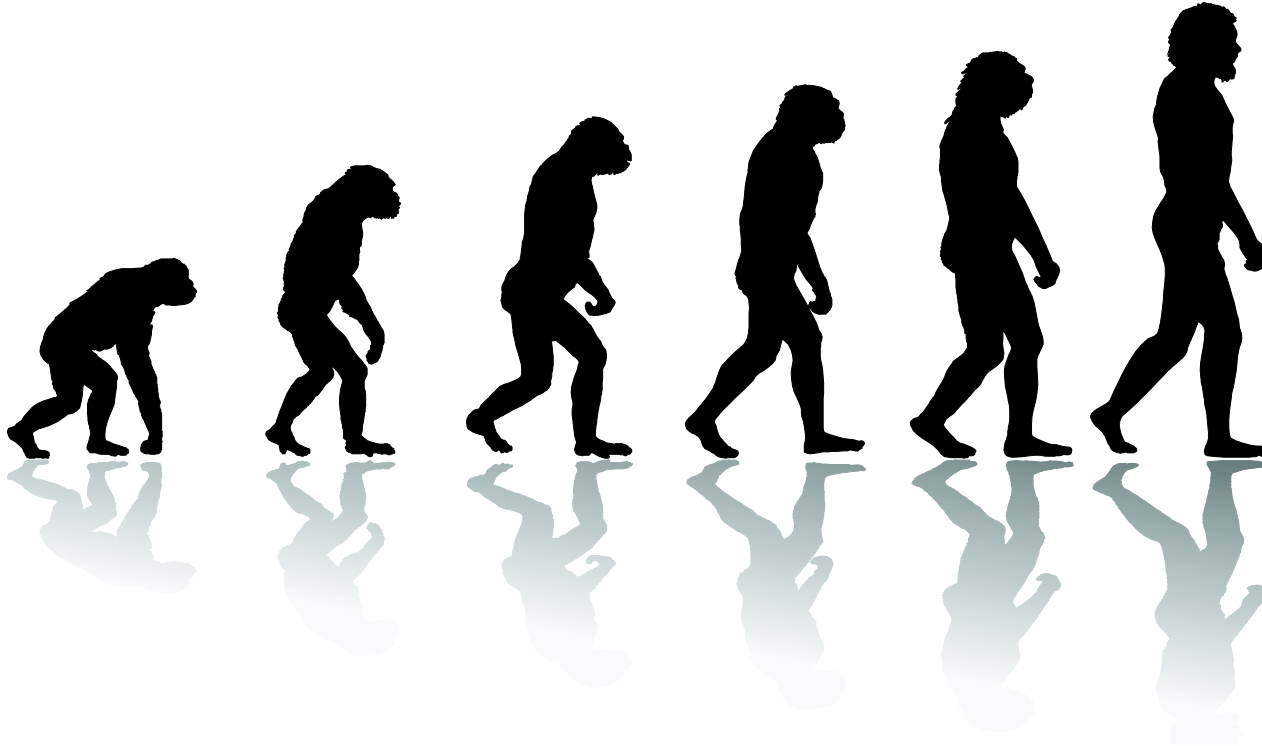
All transitions have at most one



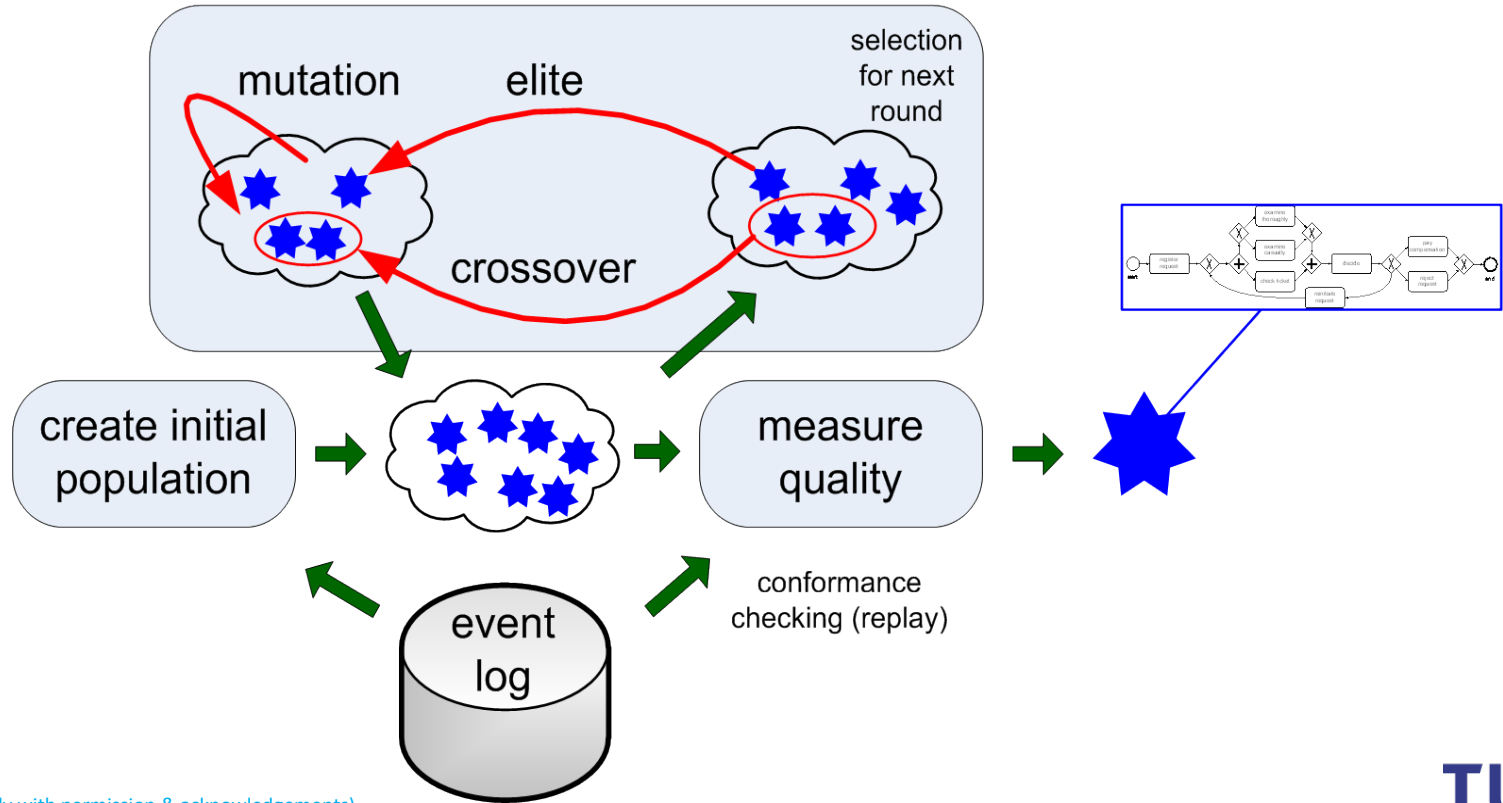


**genetic
process
mining**

Let evolution do its work ...

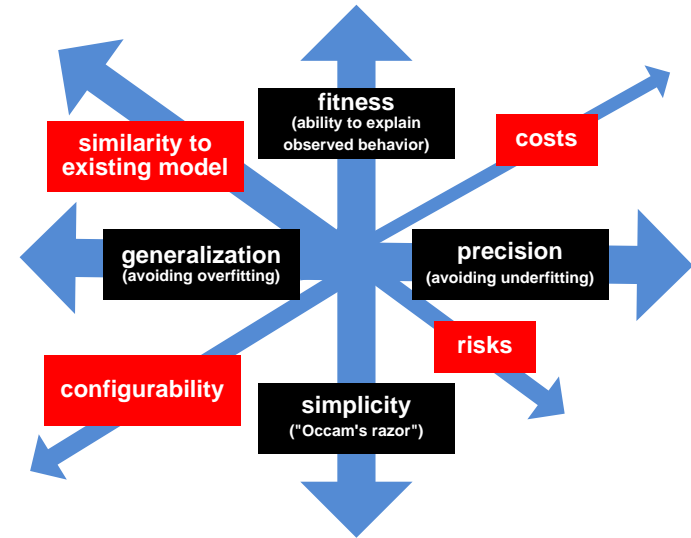


Approach



Properties of genetic mining

- For larger processes or event logs: very, very slow.
- Very flexible: easy to add new forces (add quality measures).
- Often used when confronted with a new question, followed by more efficient approaches.





**inductive
mining**

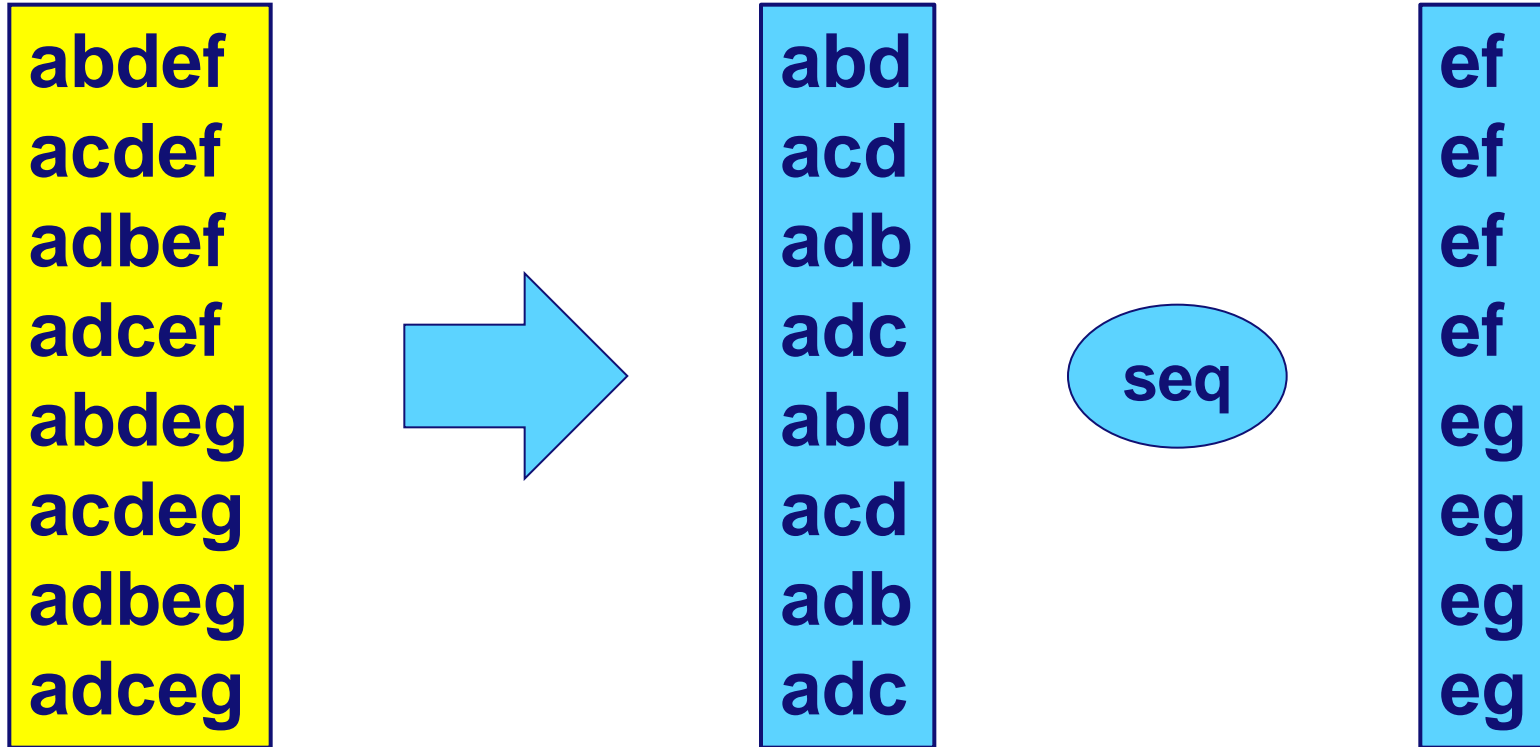
Split event logs based on activity labels

abdef
acdef
adbef
adcef
abdeg
acdeg
adbeg
adceg

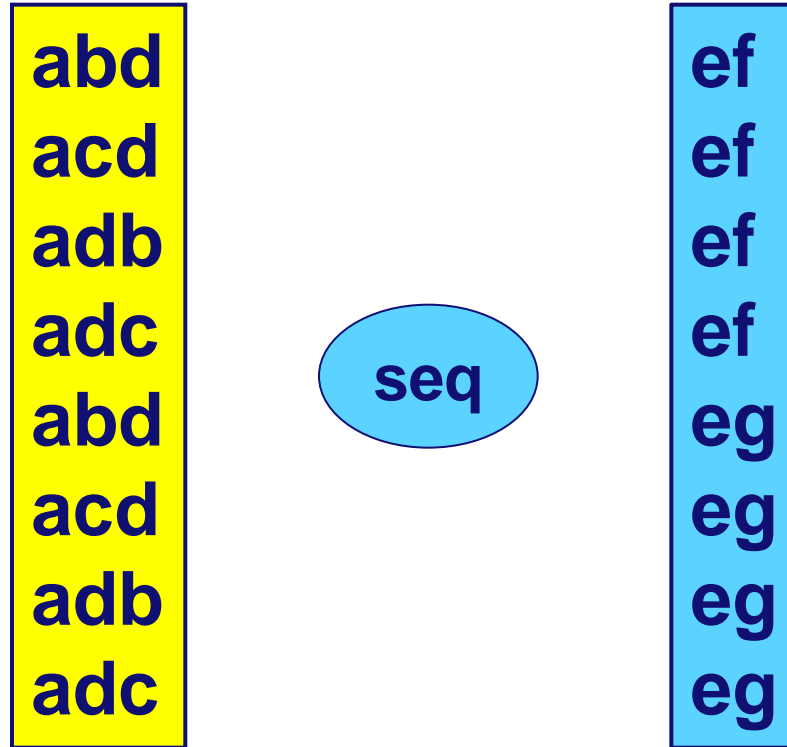
Split $\{a,b,c,d,e,f,g,h\}$ into $\{a,b,c,d\}$ and $\{e,f,g\}$ using sequence decomposition

**abdef
acdef
adbef
adcef
abdeg
acdeg
adbeg
adceg**

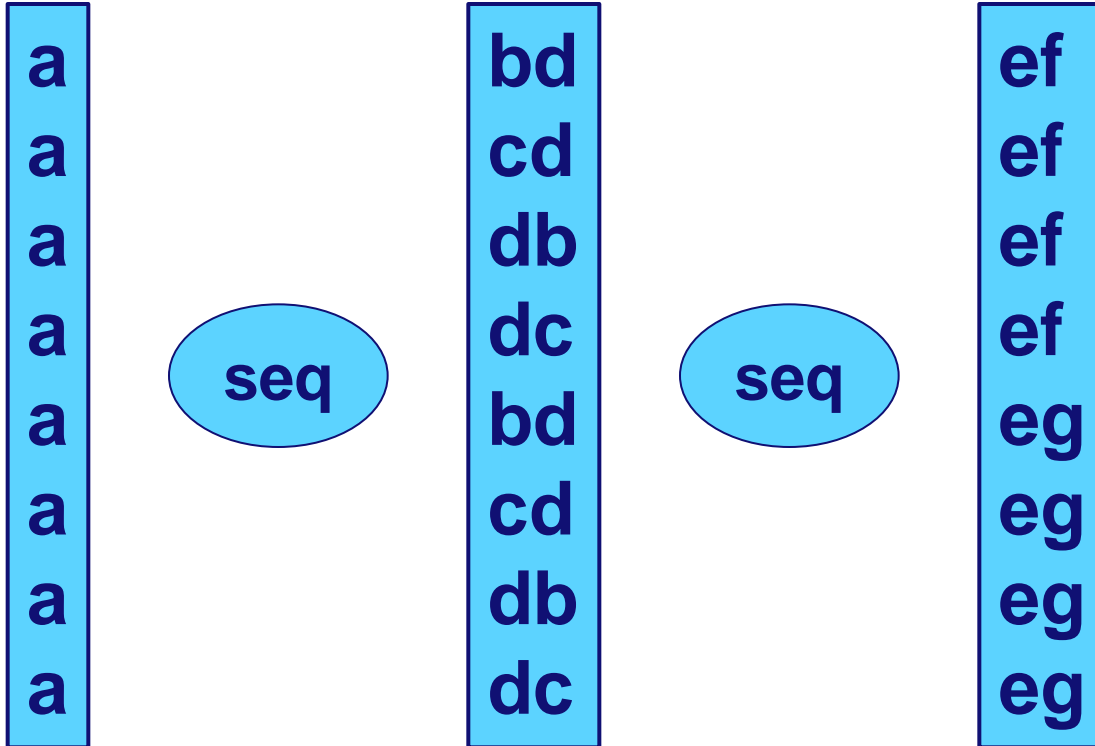
Result



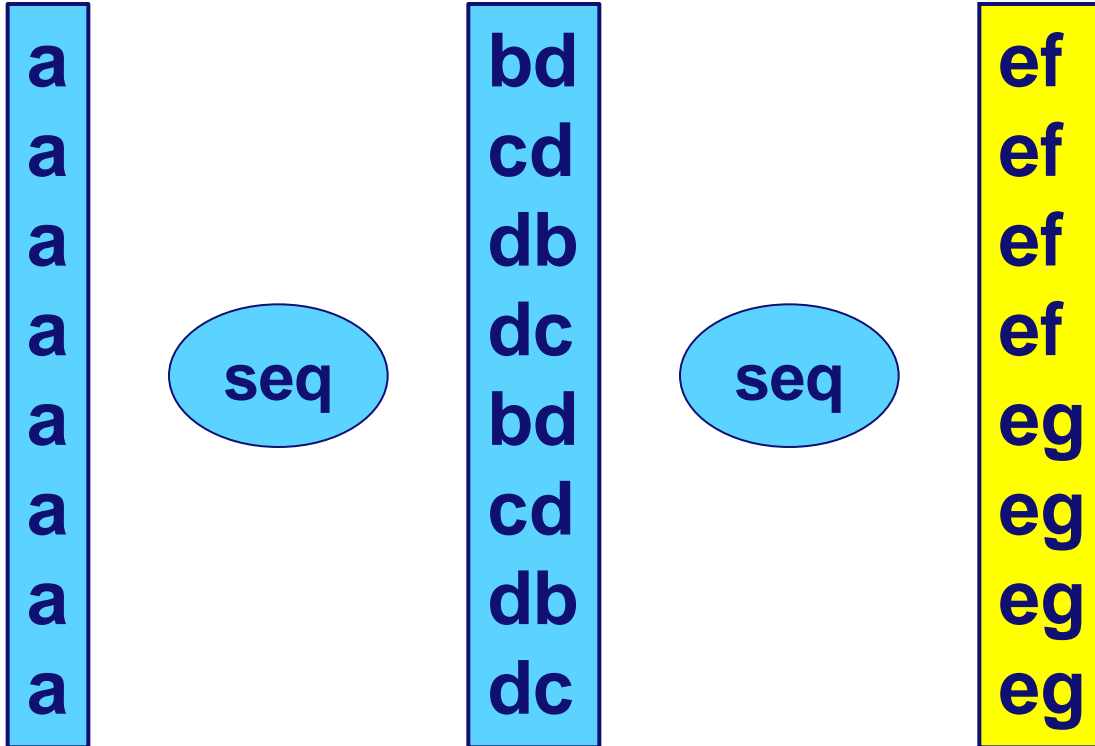
Split $\{a,b,c,d\}$ into $\{a\}$ and $\{b,c,d\}$ using sequence decomposition



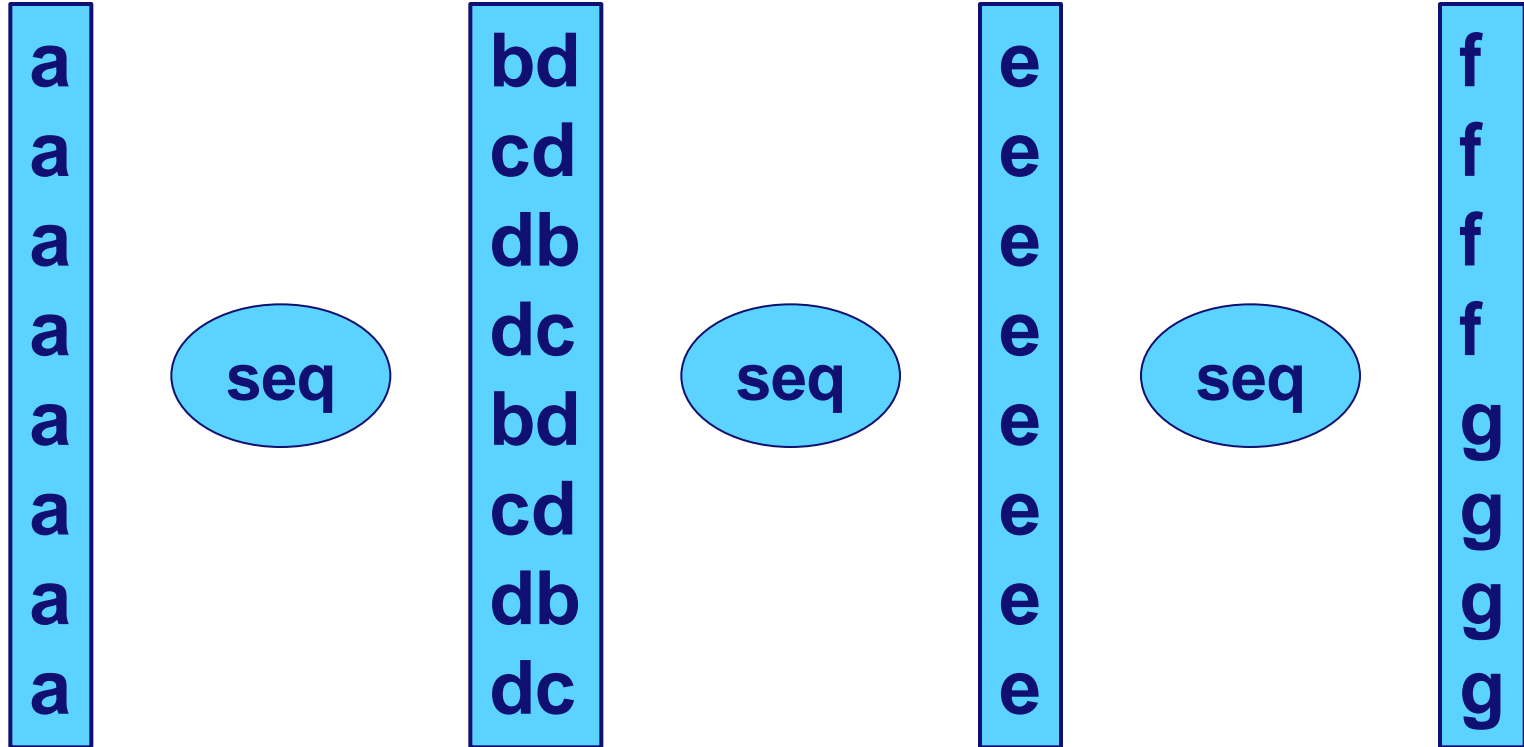
Result



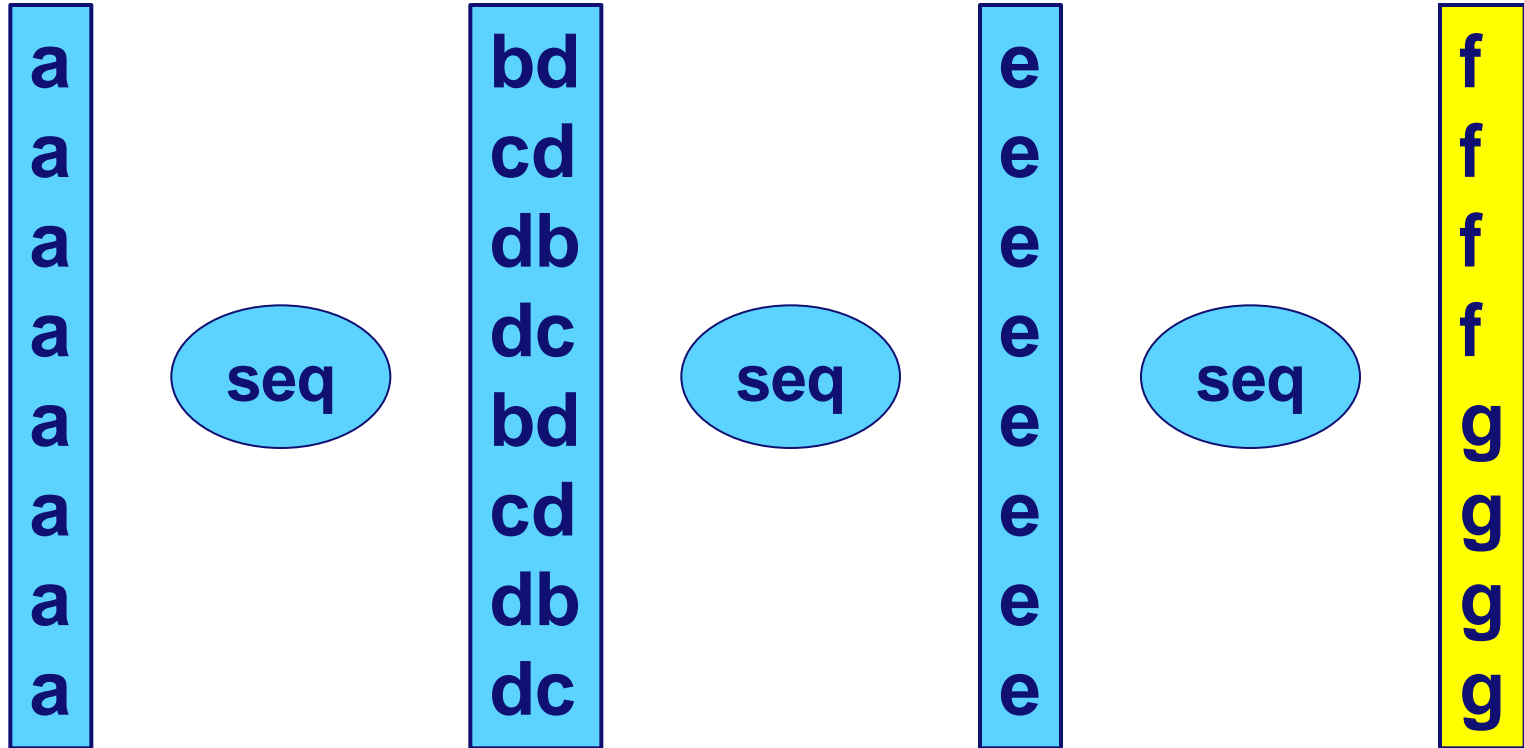
Split $\{e,f,g\}$ into $\{e\}$ and $\{f,g\}$ using sequence decomposition



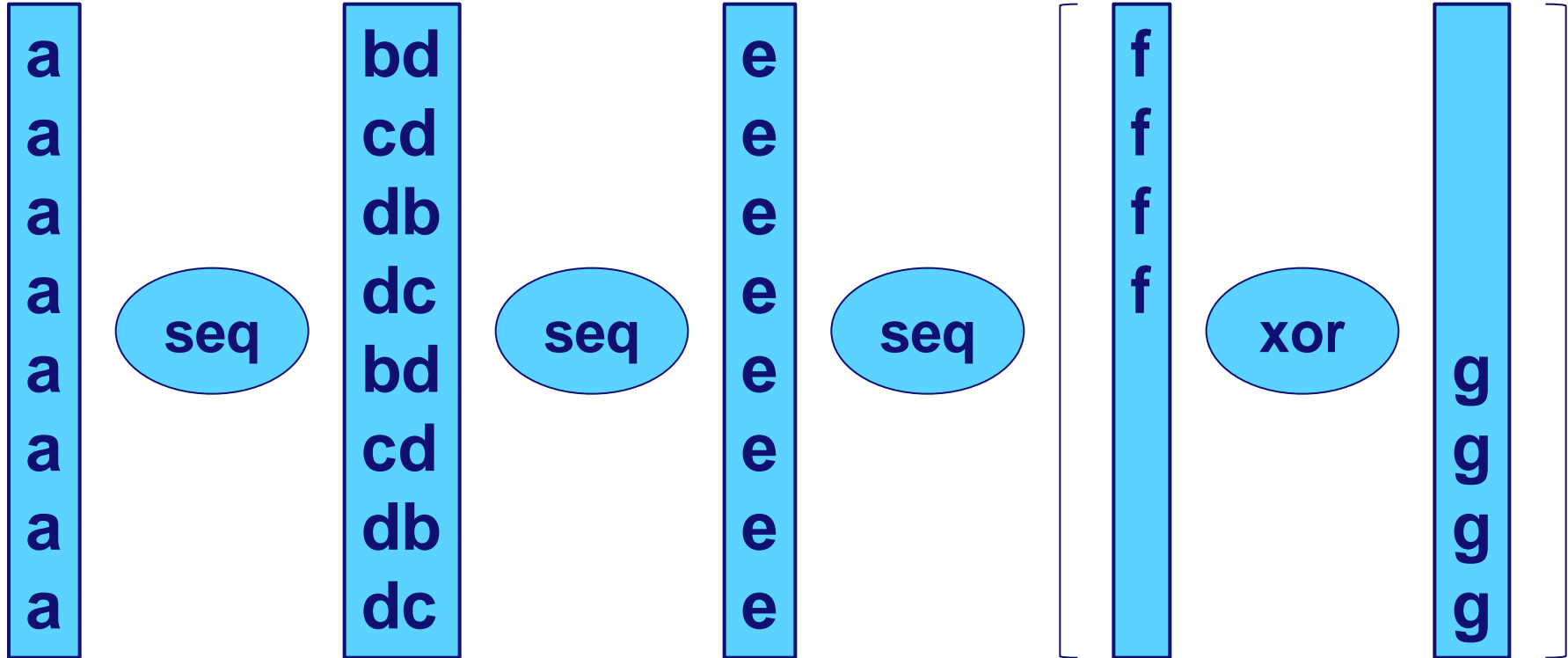
Result



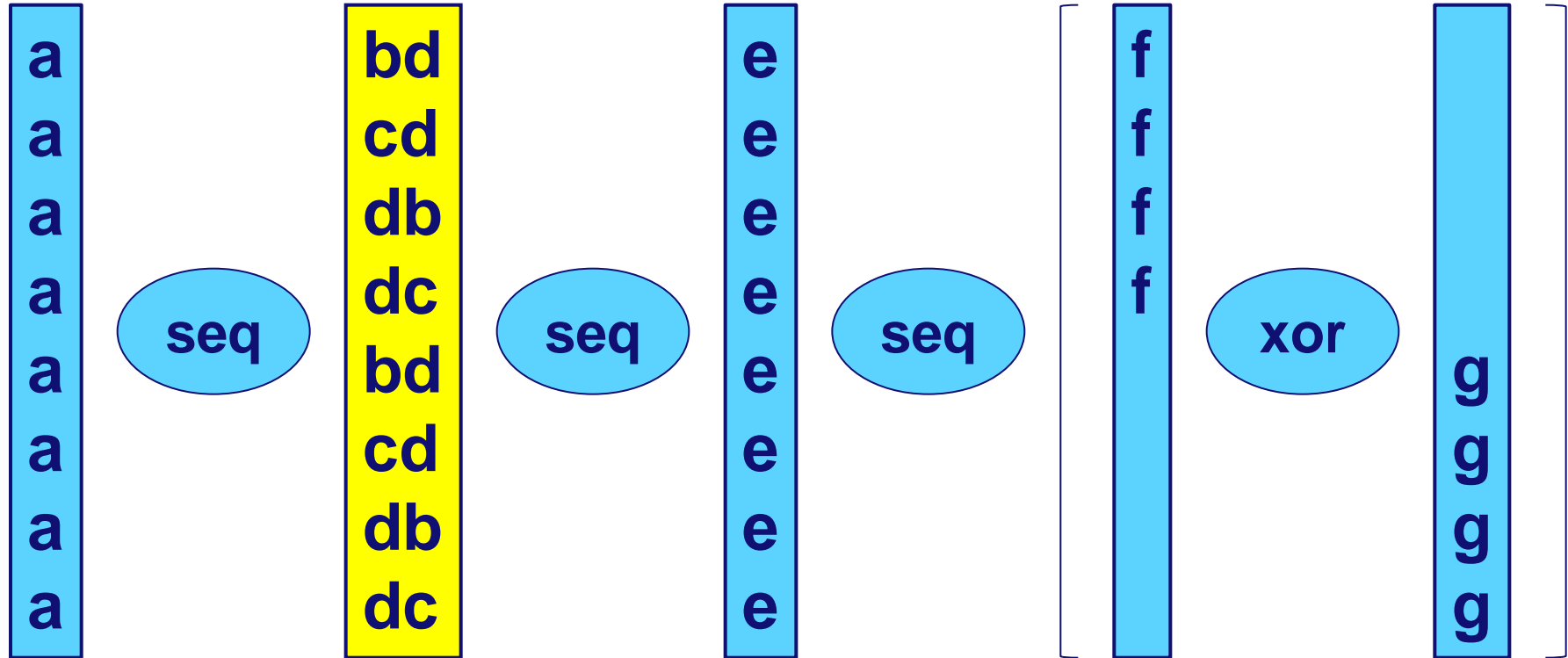
Split $\{f,g\}$ into $\{f\}$ and $\{g\}$ using XOR decomposition



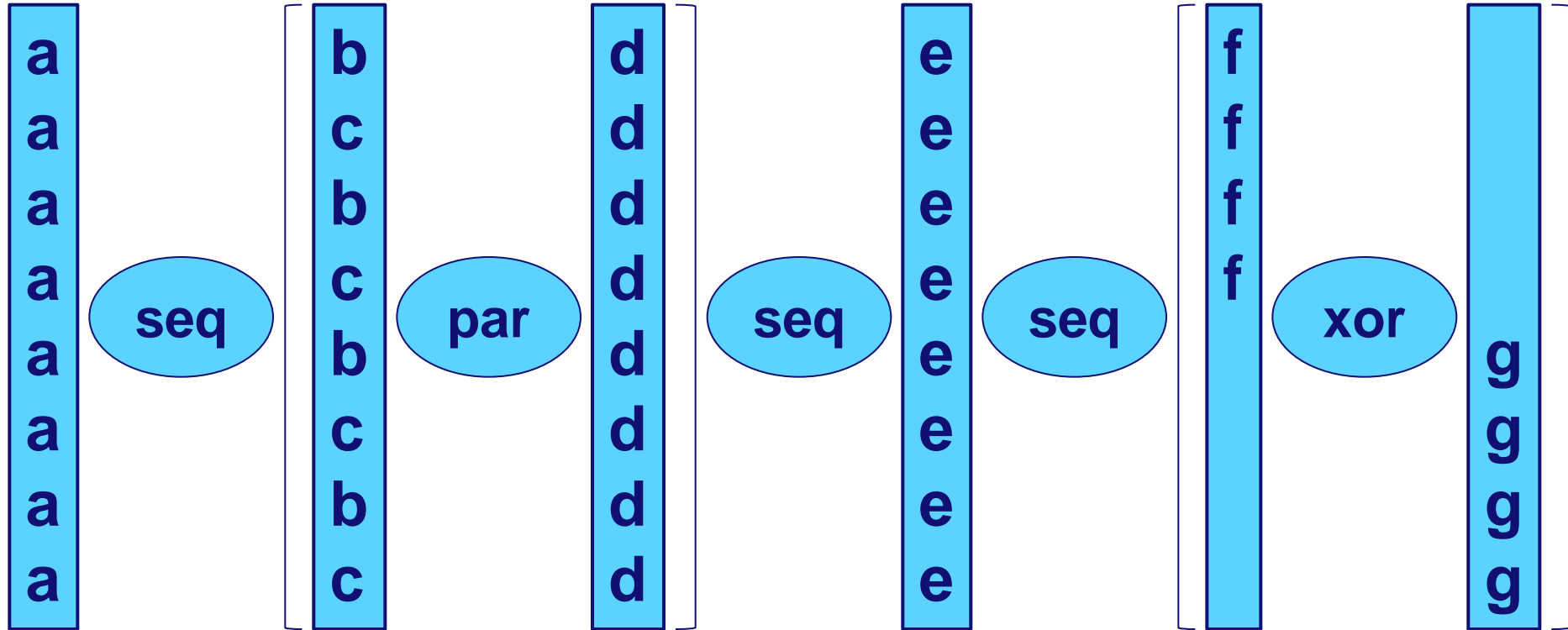
Result



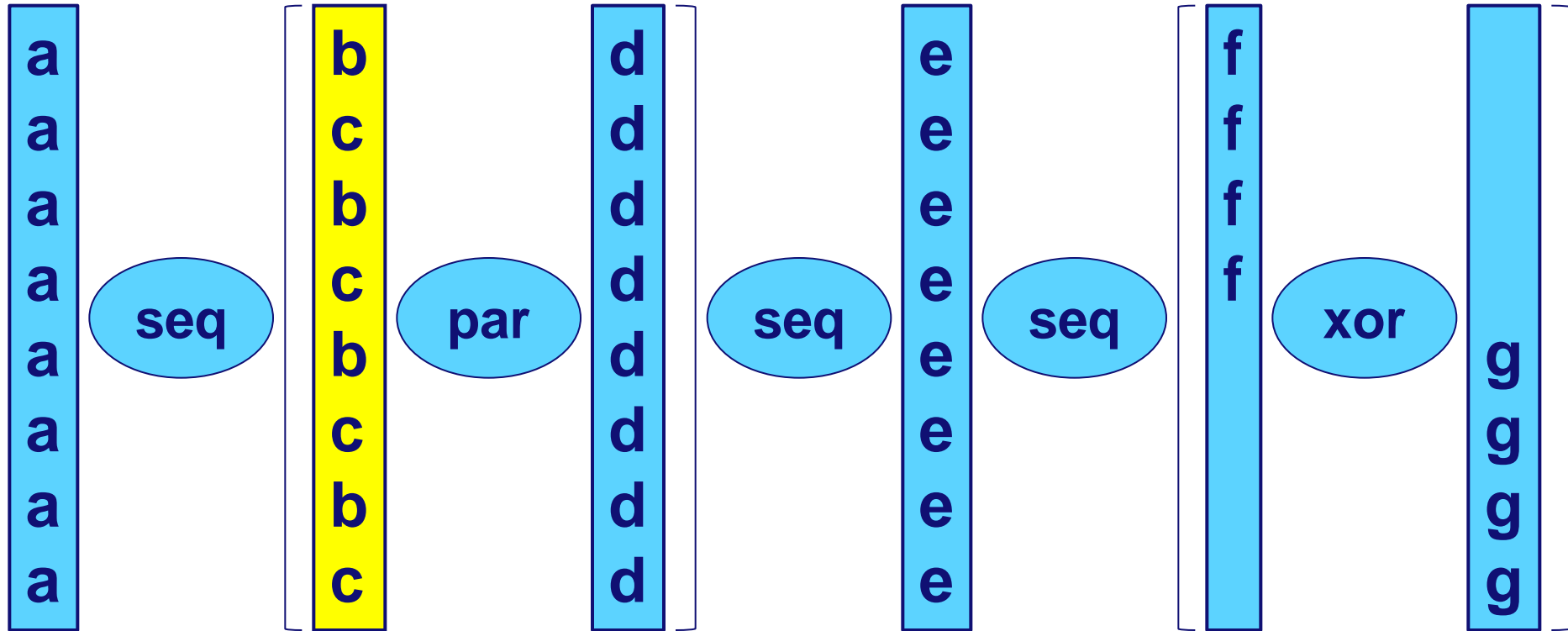
Split $\{b,c,d\}$ into $\{b,c\}$ and $\{d\}$ using AND decomposition



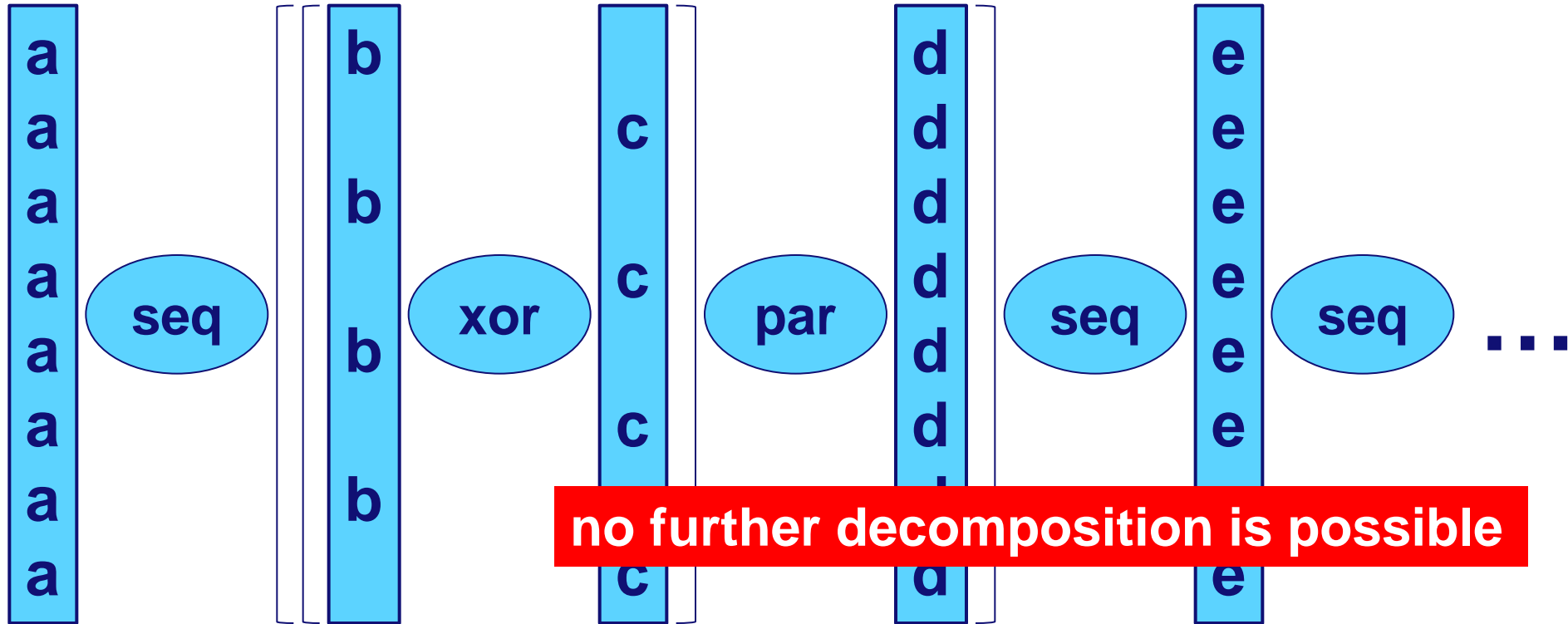
Result



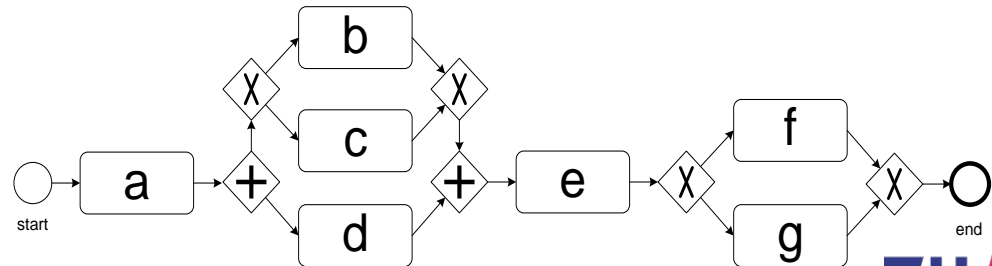
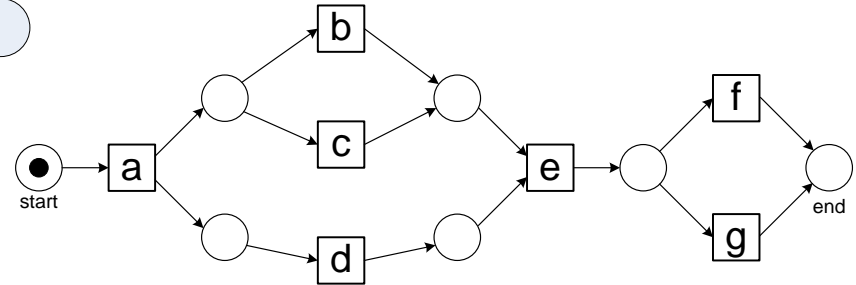
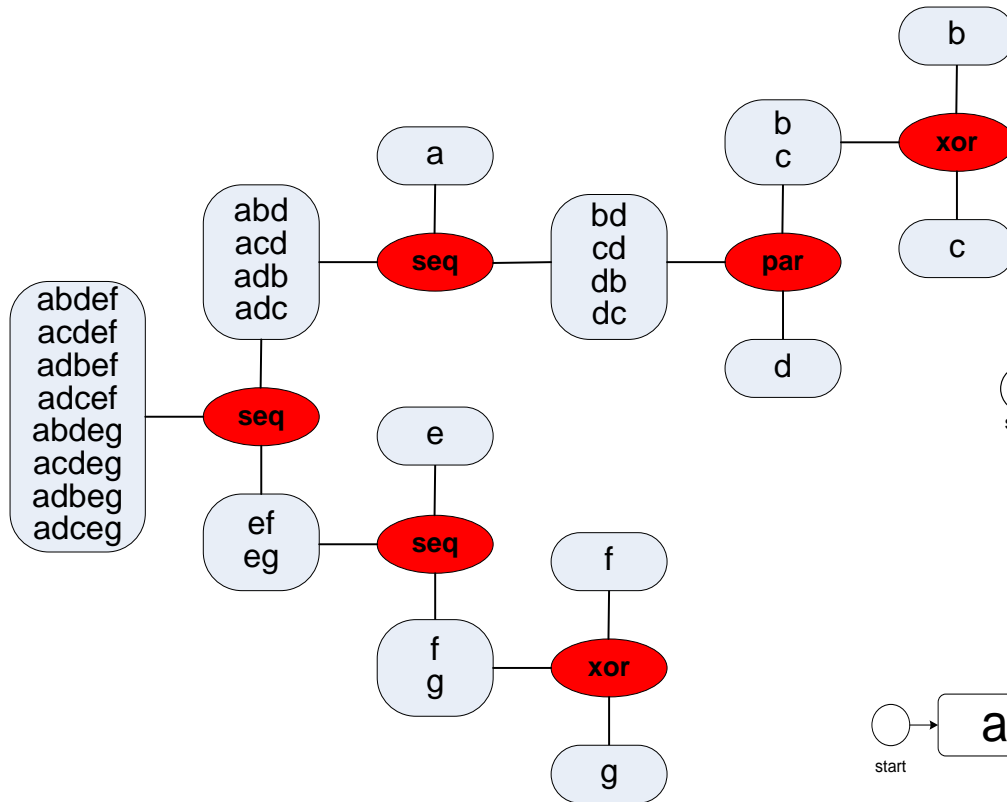
Split {b,c} into {b} and {c} using XOR decomposition



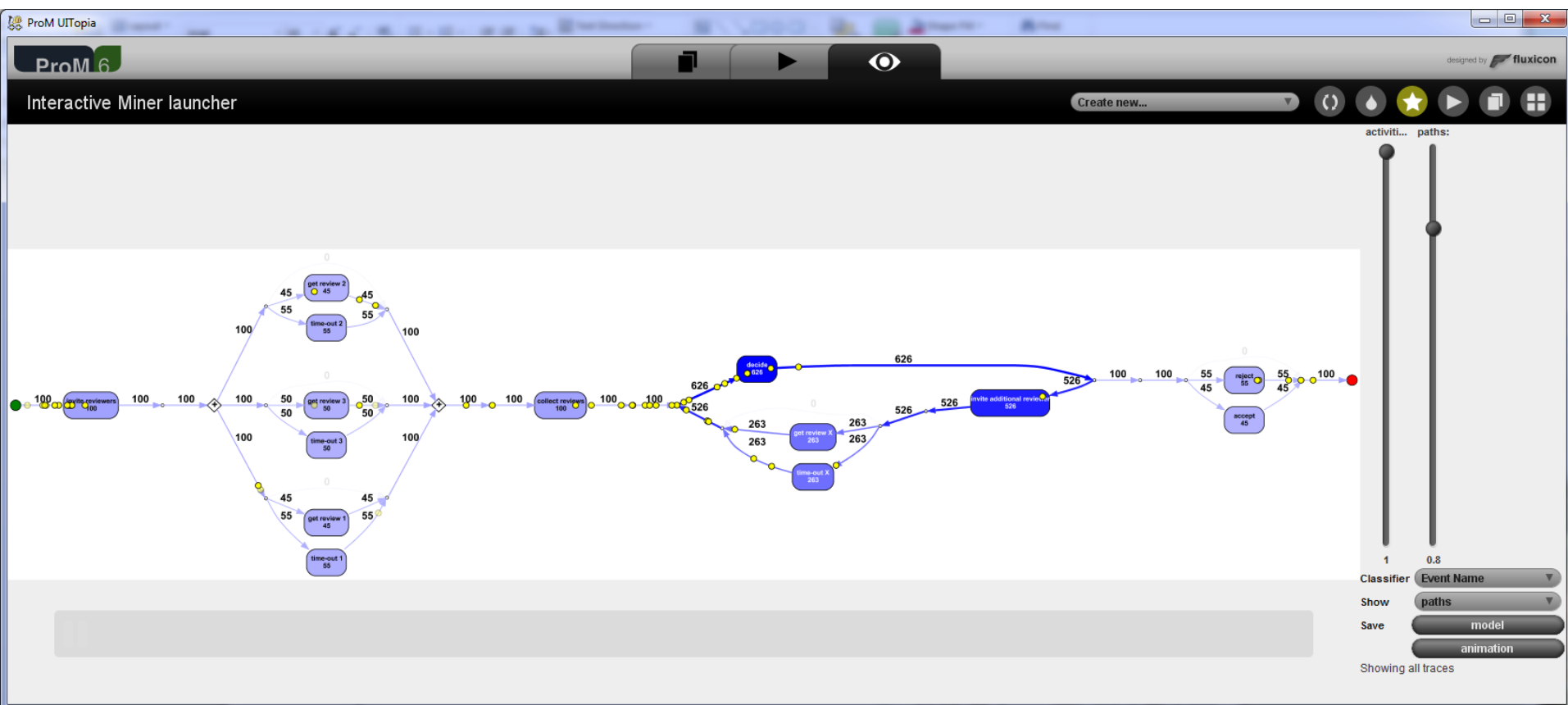
Result



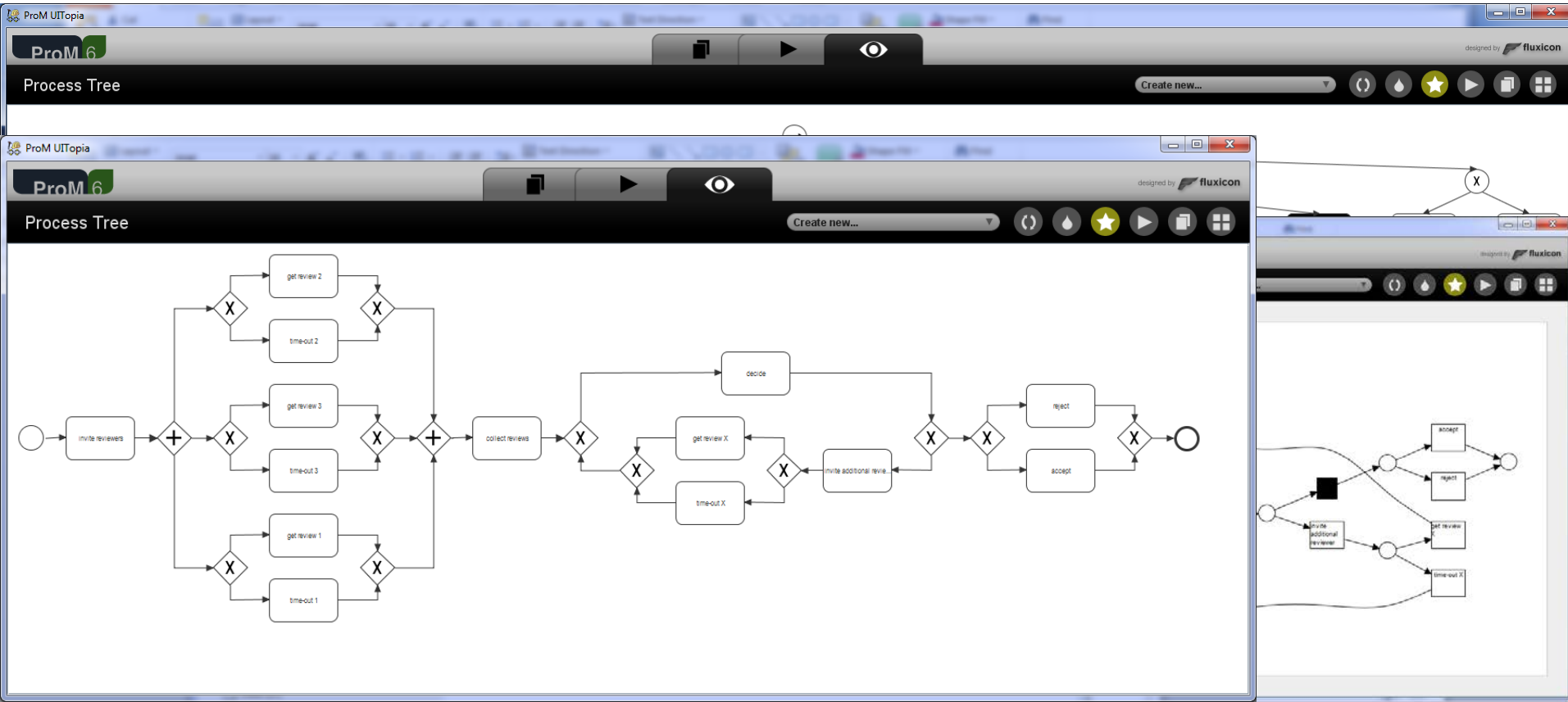
Process tree



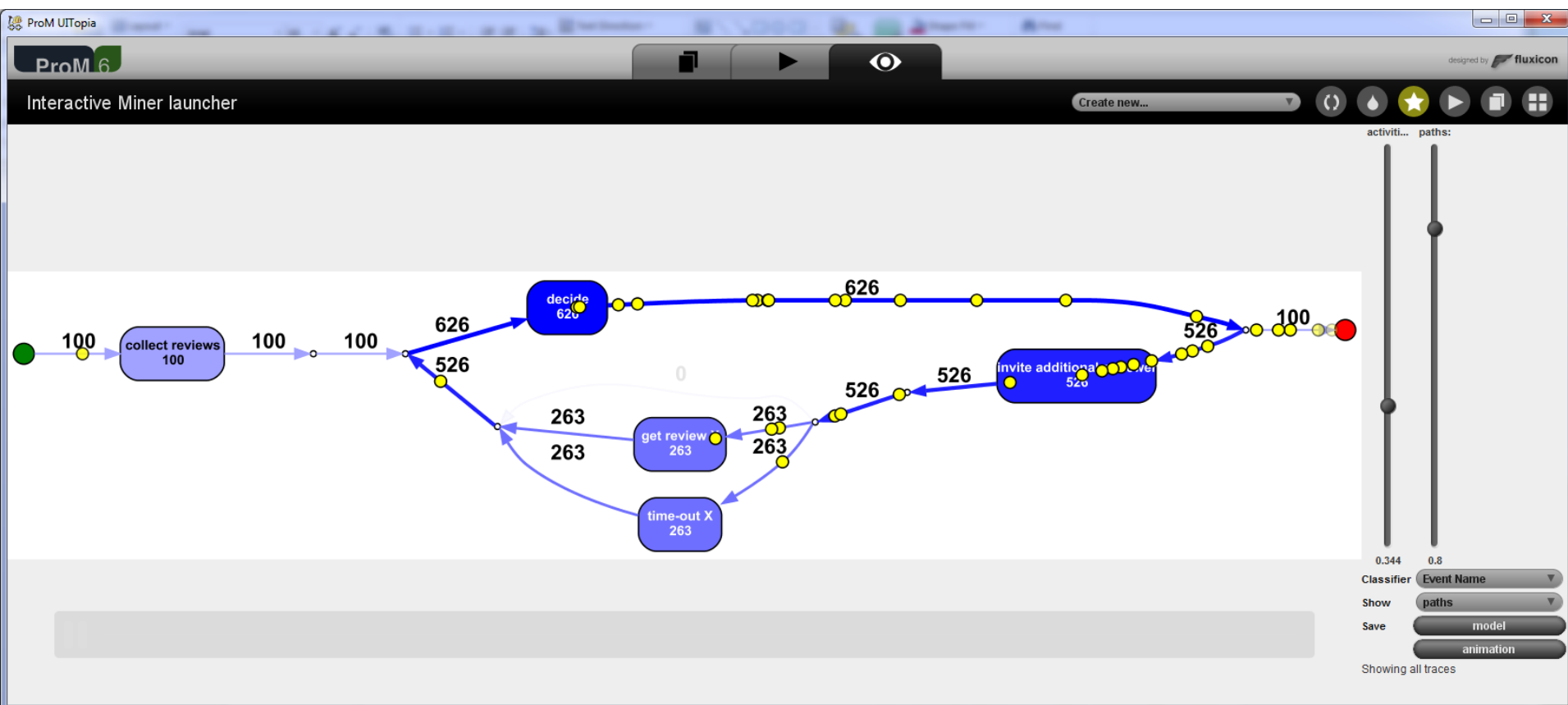
ProM's inductive miner



Result can be visualized using different notations



Seamless simplification of models



automata-based learning

distributed genetic mining

episode miner

$\alpha++$ algorithm

heuristic mining

language-based regions

THIS WAY

inductive miner (multiple variants)

α algorithm

fuzzy mining

declare miner

guide-tree miner

THAT WAY

state-based regions

$\alpha\#$ algorithm

ANOTHER WAY

genetic mining

LTL mining

partial-order based mining

neural networks

multi-phase mining

lattice miner

ILP mining

ETM genetic algorithm

conformal process graph

mining block structures

hidden Markov models

stochastic task graph miner

Part I: Preliminaries

Chapter 1
Introduction

Chapter 2
Process Modeling and
Analysis

Chapter 3
Data Mining

Part III: Beyond Process Discovery

Chapter 7
Conformance
Checking

Chapter 8
Mining Additional
Perspectives

Chapter 9
Operational Support

Part II: From Event Logs to Process Models

Chapter 4
Getting the Data

Chapter 5
Process Discovery: An
Introduction

Chapter 6
Advanced Process
Discovery Techniques

Part IV: Putting Process Mining to Work

Chapter 10
Tool Support

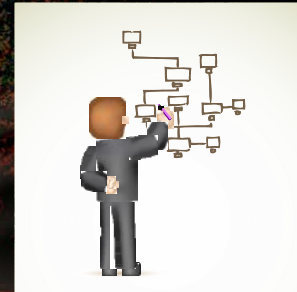
Chapter 11
Analyzing “Lasagna
Processes”

Chapter 12
Analyzing “Spaghetti
Processes”

Part V: Reflection

Chapter 13
Cartography and
Navigation

Chapter 14
Epilogue



Wil M. P. van der Aalst

Process Mining

Discovery, Conformance and
Enhancement of Business Processes

 Springer