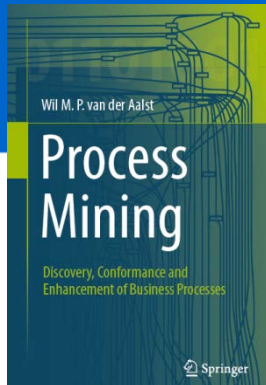


Process Mining: Data Science in Action

Aligning Observed and Modeled Behavior

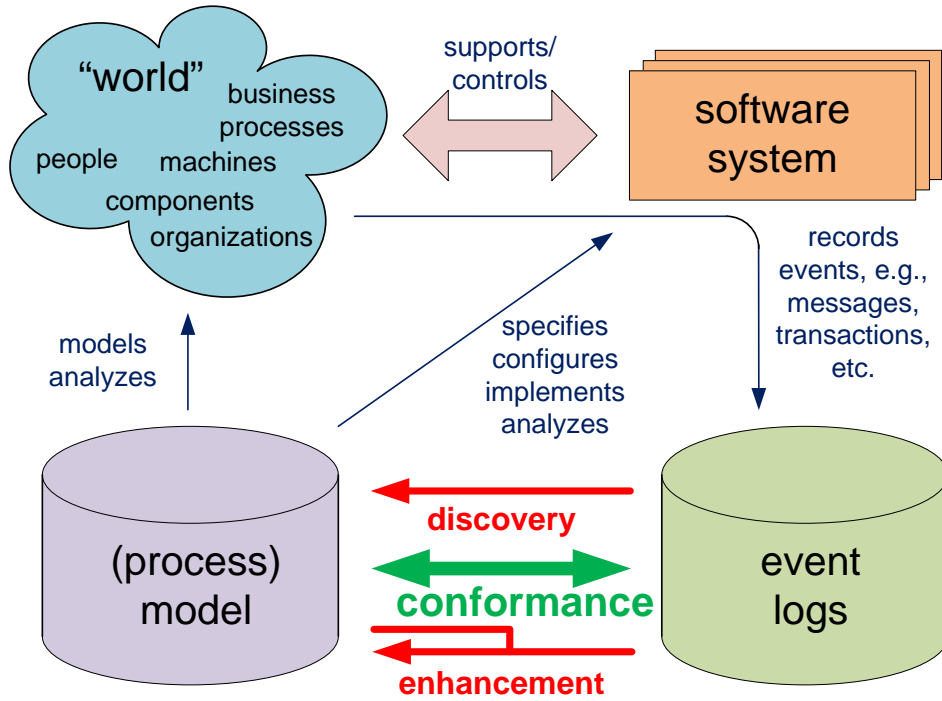
prof.dr.ir. Wil van der Aalst
www.processmining.org



TU/e Technische Universiteit
Eindhoven
University of Technology

Where innovation starts

Conformance checking



1. Conformance checking using causal footprints.
2. Conformance checking based on token-based replay.
3. **Alignment-based conformance checking.**

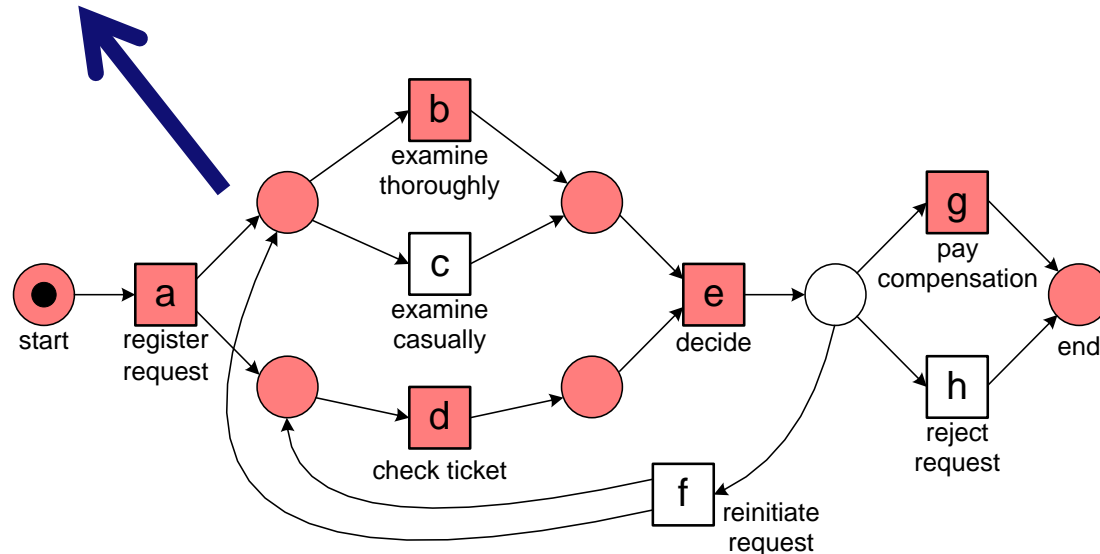
Requirements

- Conformance checking should **not** impose restrictions on the process notation (e.g., silent transitions and two transitions with the same label should be possible).
- Should provide a "**closest matching path**" through the process model for any trace in the event log.
 - Also required for **performance analysis**!
 - **Beyond** the analysis of replay fitness (advanced diagnostics, precision, generalization, etc.).

Alignments

a	b	d	e	g
a	b	d	e	g

← $\langle a, b, d, e, g \rangle$

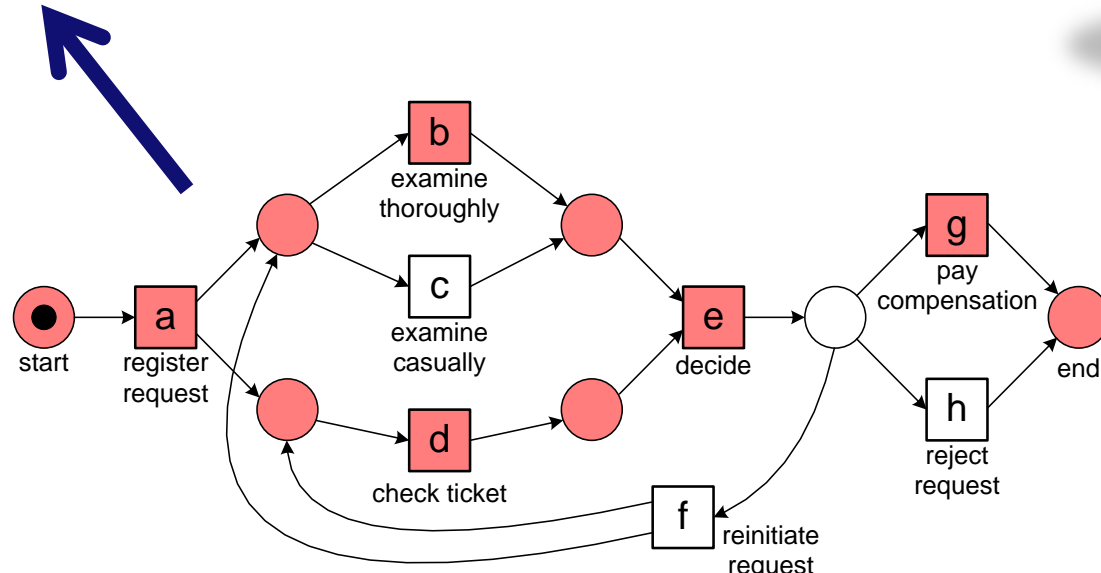


#	trace
455	acdeh
191	abdeg
177	adceh
144	abdeh
111	acdeg
82	adceg
56	adbeg
47	acdefdbeg
38	adbeg
33	acdefdbeg
14	acdefdbeg
11	acdefdbeg
9	adcefcdeh
8	adcefdbeg
5	adcefdbeg
3	acdefdbefdbeg
2	adcefdbeg
2	adcefdbefdbeg
1	adcefdbefdbeg
1	adbefdbefdbeg
1	adcefdbefcdefdbeg
1391	

Alignments

a	»	d	e	g	h
a	b	d	e	g	»

← $\langle a, d, e, g, h \rangle$



Terminology

alignment
(sequence of moves)

move in
log only

move in
model

simultaneous
move
(move in both)

a			d	e	g
		c	d	e	g

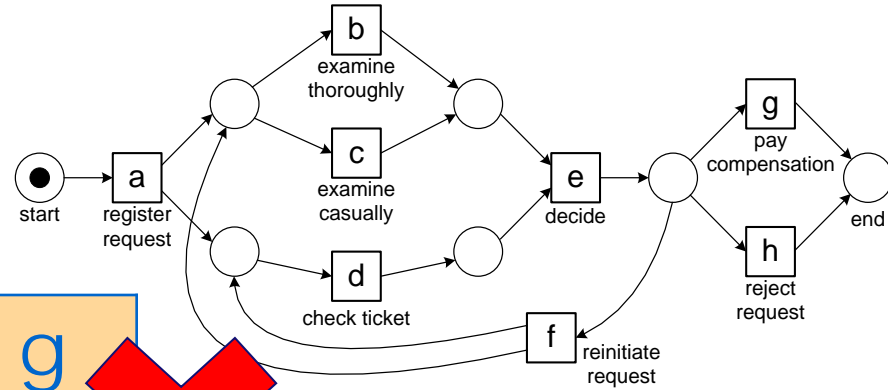
- Projection of top row (remove "no moves") corresponds to the sequence of moves in the event log.
- Projection of bottom row (remove "no moves") corresponds to a run of the model.

Optimal alignment for ⟨a,b,d,e,g⟩

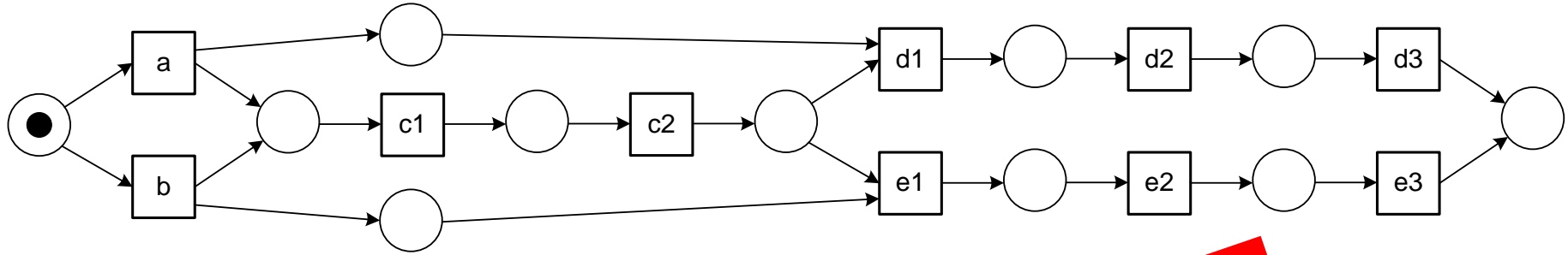
a	b	d	e	g
a	b	d	e	g

a	b	»	d	e	g
a	»	c	d	e	g

a	b	d	e	g	»	»	»	»	»
»	»	»	»	»	a	c	d	e	g



Optimal alignment for $\langle a, c1, c2, e1, e2, e3 \rangle$?



a	»	c1	c2	e1	e2	e3
»	b	c1	c2	e1		

a	c1	c2	»	e1	e2	e3	
a	c	d1	d2	d3	»	»	»

Depends on cost function!

Standard cost function

count »'s in alignment

...	a	...
...	»	...

...	»	...
...	a	...

...	a	...
...	a	...

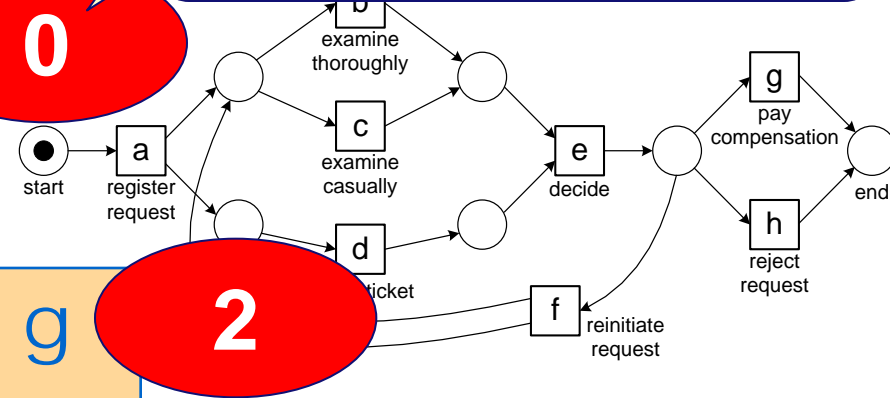
...	a	...
...	b	...

Using the standard cost function

optimal
there is no other alignment
that has lower costs

a	b	d	e	g
a	b	d	e	g

0



a	b	»	d	e	g
a	»	c	d	e	g

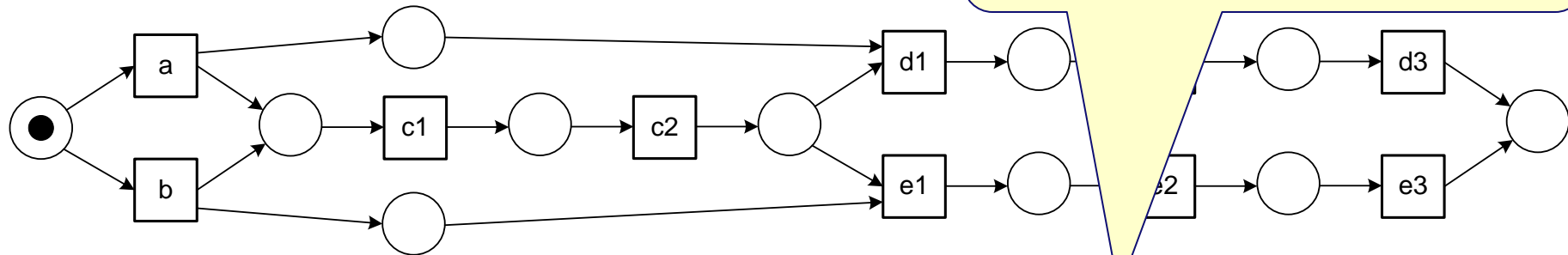
2

a	b	d	e	g	»	»	»	»	»
»	»	»	»	»	a	c	d	e	g

10

Using the standard cost function

trace in log: $\langle a, c1, c2, e1, e2, e3 \rangle$



optimal
there is no other alignment
that has lower costs

a	»	c1	c2	e1	e2	e3
»	b	c1	c2	e1	e2	e3

2

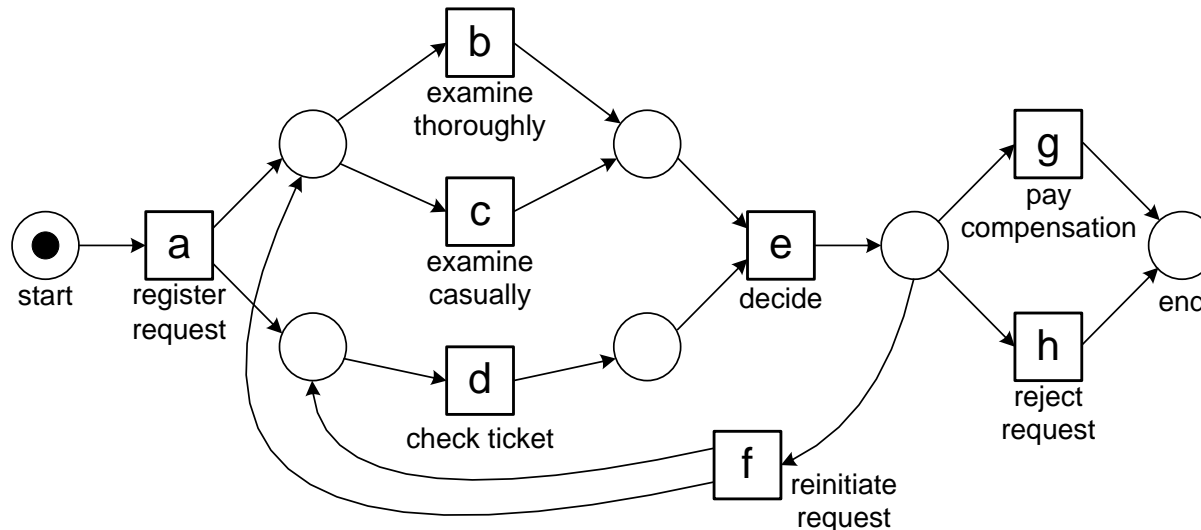
a	c1	c2	»	»	»	e1	e2	e3
a	c1	c2	d1	d2	d3	»	»	»

6

Optimal alignment for $\langle a, b, e, f, d, e, g \rangle$ (1/2)

a	b	e	f	d	e	g
a	b	»	»	d	e	g

2

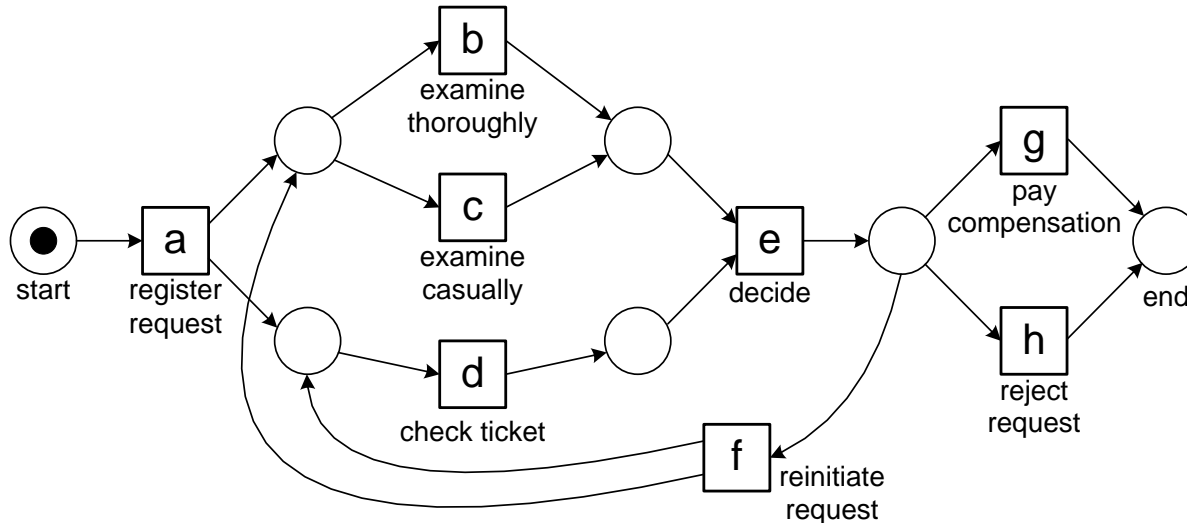


**loop is not
taken: e and f in
event log are
discarded**

Optimal alignment for $\langle a, b, e, f, d, e, g \rangle$ (2/2)

a	b	»	e	f	d	»	e	g
a	b	d	e	f	d	b	e	g

2



**loop is taken:
d and b are
missing in
event log**

Not one unique optimal alignment

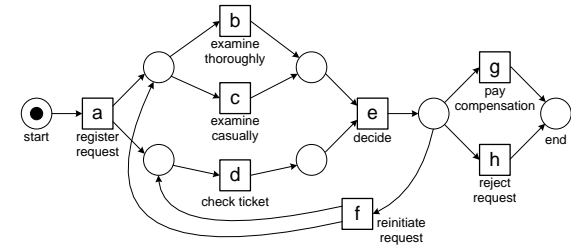
a	b	»	e	f	d	»	e	g
a	b	d	e	f	d	b	e	g

2

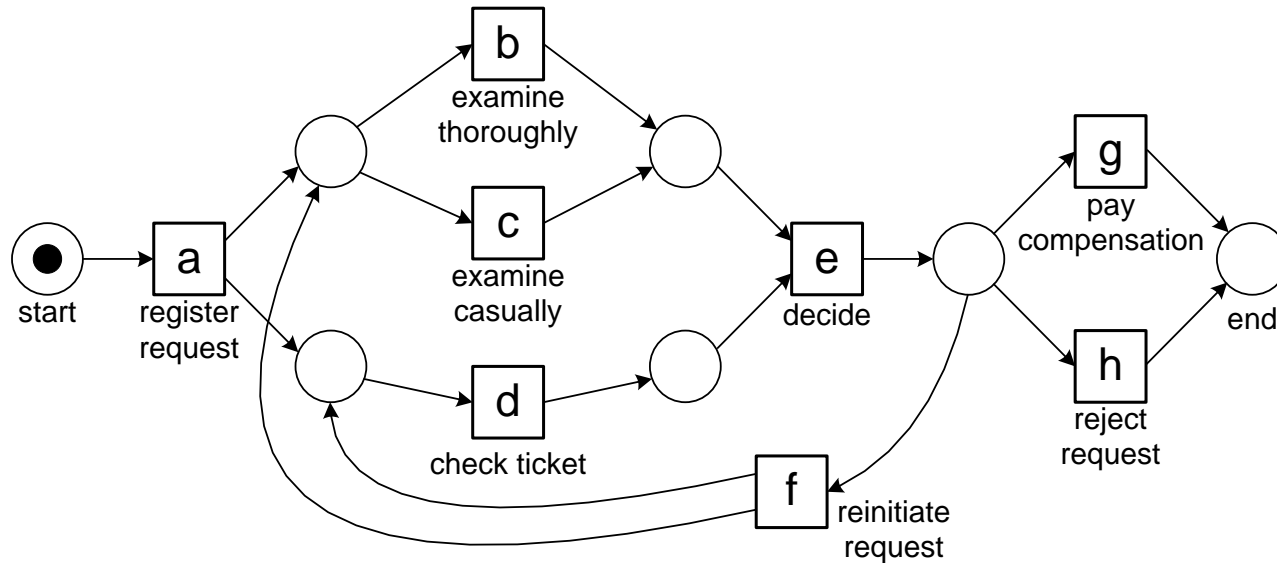
a	b	e	f	d	e	g
a	b	»	»	d	e	g

2

■ ■ ■



Question: How many optimal alignments are there for $\langle a, b, e, f, d, e, g \rangle$?



$\langle a, b, e, f, d, e, g \rangle$

Answer: 9

$1+(2 \times 2)+(2 \times 2)=9$ optimal alignments having cost 2

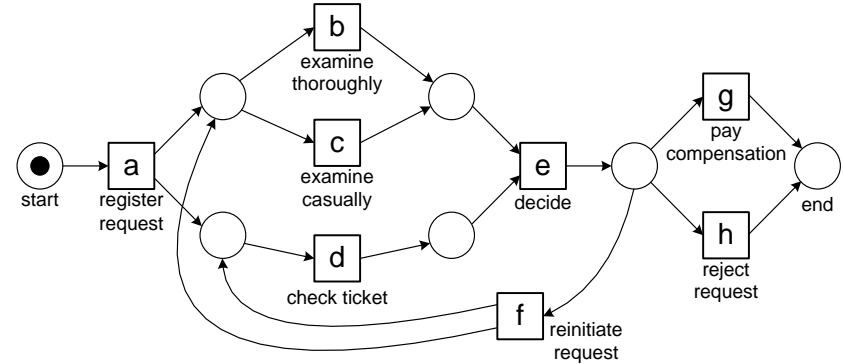
a	b	e	f	d	e	g
a	b	»	»	d	e	g

1x

move in model can be
reordered in concurrent part

a	b	»	e	f	d	»	e	g
a	b	d	e	f	d	b	e	g

4x



a	b	»	e	f	d	»	e	g
a	b	d	e	f	d	c	e	g

4x

Any cost structure is possible

...	send-letter(John,4 weeks, \$400)	...
...	send-email(Sue,3 weeks,\$500)	...

Any cost structure is possible

...	send-letter(John, 4 weeks, \$400)	...
...	send-email(Sue, 3 weeks, \$500)	...

**similar activities (lower costs
for related activities)**

Any cost structure is possible

...	send-letter(John , 4 weeks, \$400)	...
...	send-email(Sue , 3 weeks, \$50)	...

**resource-related conformance costs
(done by someone that does or does not have
the specified role)**

Any cost structure is possible

...	send-letter(John, 4 weeks, \$400)	...
...	send-email(Sue, 3 weeks, \$500)	...

**time-related conformance costs
(activity should happen within a preset
deadline)**

Any cost structure is possible

...	send-letter(John, 4 weeks, \$400)	...
...	send-email(Sue, 3 weeks, \$500)	...

**data-related conformance costs
(routing condition is violated, e.g., path
only for more valuable orders)**

Any cost structure is possible

...	send-letter(John, 4 weeks, \$400)	...
...	send-email(Sue, 3 weeks, \$500)	...

risk-related conformance costs, context-dependent conformance costs, ...

Computing fitness

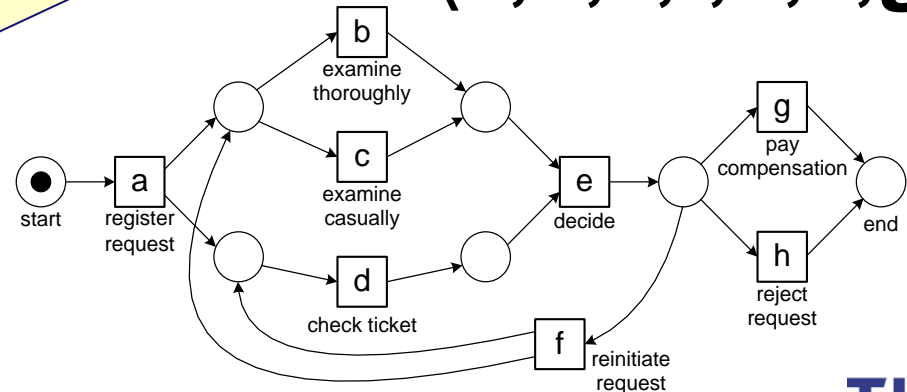
all events cause a move in log only

model.

$$1 - \frac{2}{7+5} = 0.833$$

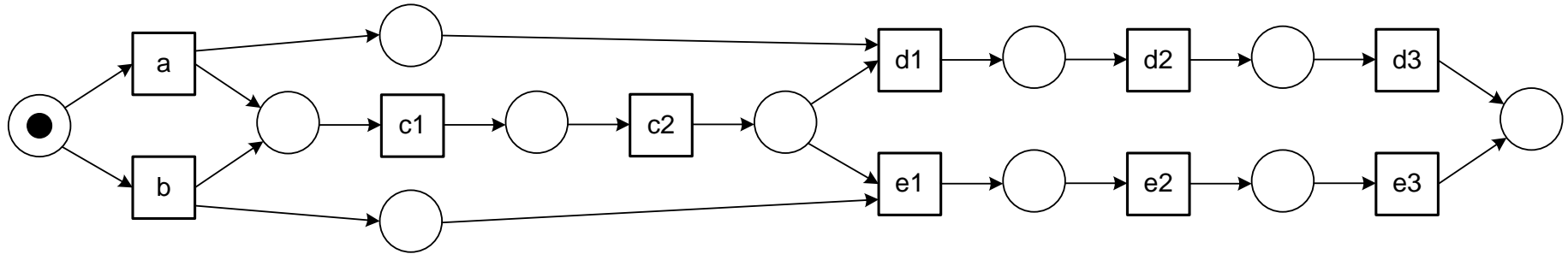
an optimal alignment with a
shortest path from initial
state to final state

$\langle a, b, e, f, d, e, g \rangle$



Question: Compute alignment-based fitness

$\langle a, c1, c2, e1, e2, e3 \rangle$



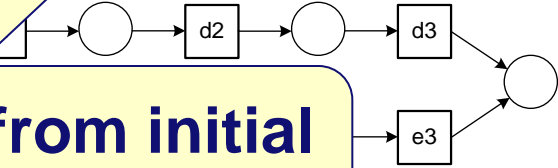
Answer

cost of optimal alignment = 2

$\langle a, c1, c2, e1, e2, e3 \rangle$

all ev
move in log only
worst-case scenario

shortest path from initial
state to final state



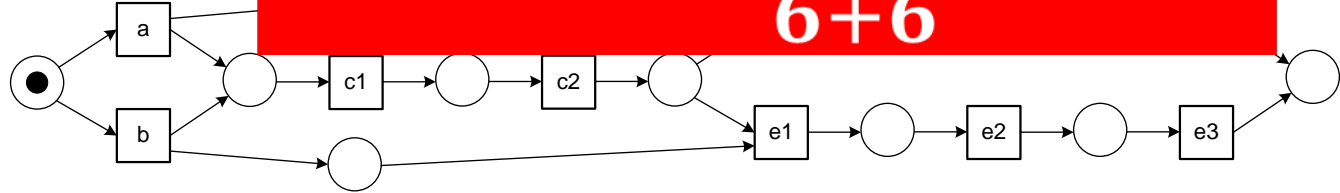
a	c1	c2	e1	e2	e3
»	c1	c2	e1	e2	e3

a	c1	c2	e1	e2	e3	»	»	»	»	»	»
»	»	»	»	»	»	a	c1	c2	d1	d2	d3

Answer

$\langle a, c1, c2, e1, e2, e3 \rangle$

$$\text{fitness} = 1 - \frac{2}{6+6} = 0.833$$



2

a	»	c1	c2	e1	e2	e3
»	b	c1	c2	e1	e2	e3

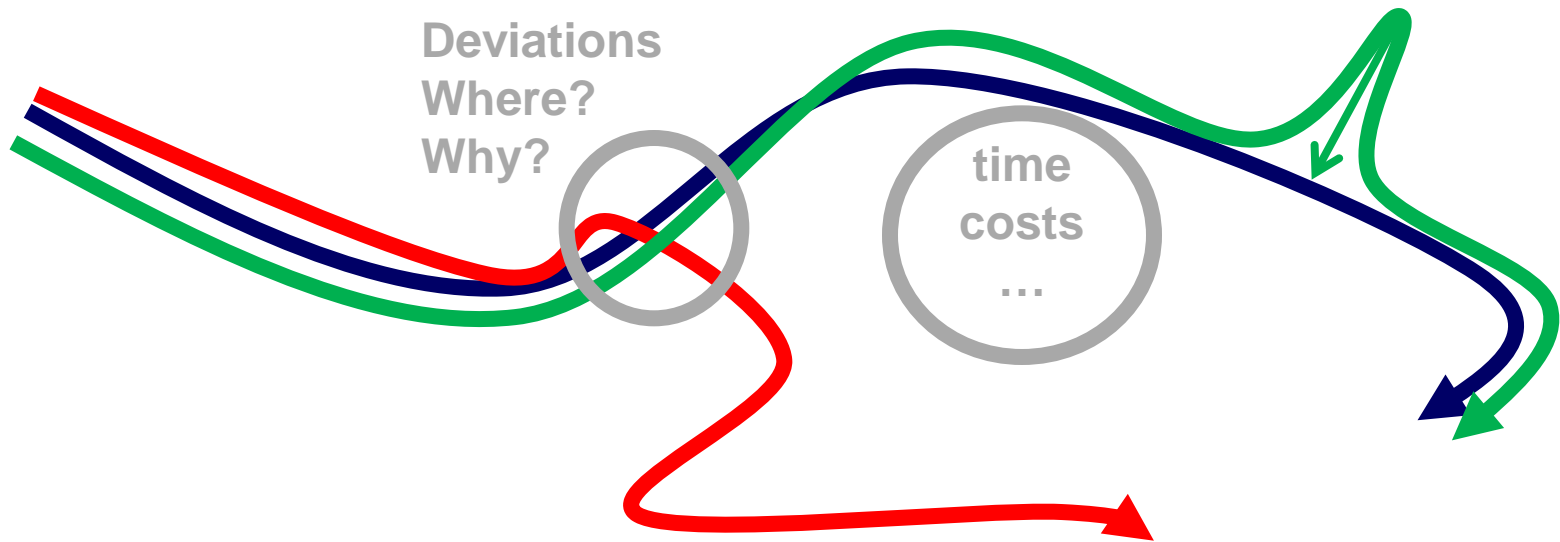
6

a	c1	c2	e1	e2	e3	»	»	»	»	»	»
»	»	»	»	»	»	a	c1	c2	d1	d2	d3

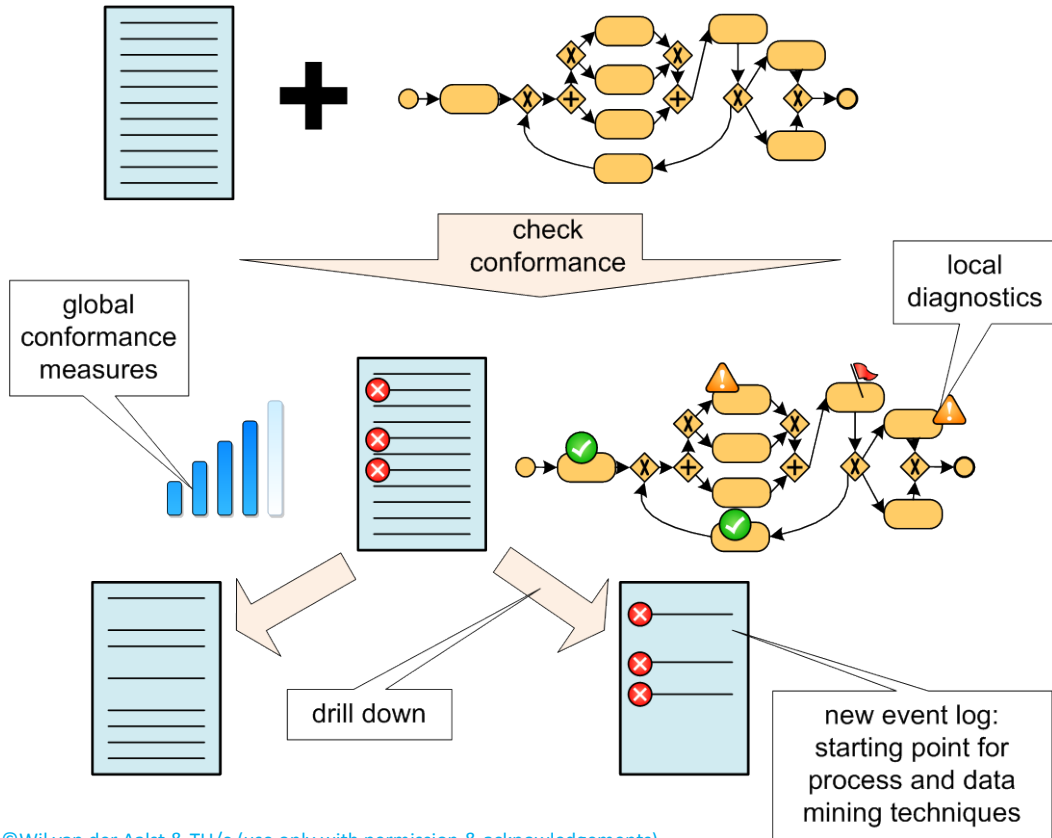
6

Advantages of aligning log and model

- Observed behavior is **directly related** to modeled behavior.
- Very **flexible** (any cost structure).
- Detailed **diagnostics**.
- After aligning log and model, other quality dimensions can be investigated (**separation of concerns**).



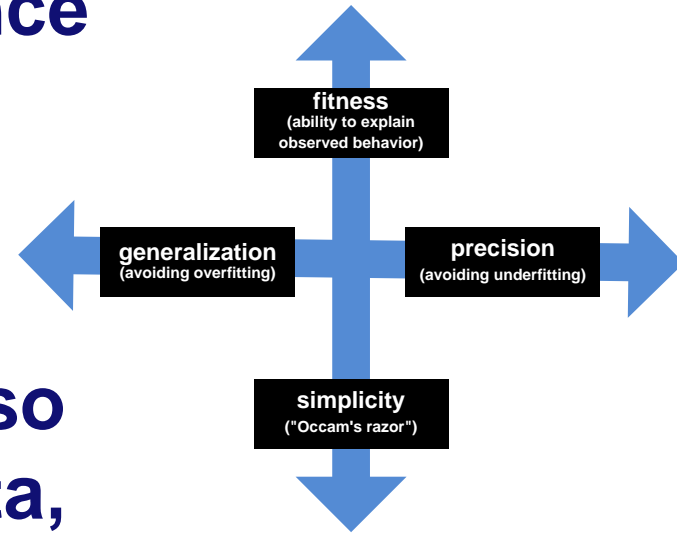
Drilling down



- Create event log containing deviating (or non-deviating) cases.
- Apply process mining to new log.
- Comparative process mining.

Beyond fitness and control-flow

- There are also solid conformance measures for **precision**, **generalization**, and **simplicity**.
- Multiple definitions possible.
- Conformance checking may also include **other perspectives** (data, resources, time, cost, etc.).
- Example: **data-aware alignments**.



Part I: Preliminaries

Chapter 1
Introduction

Chapter 2
Process Modeling and
Analysis

Chapter 3
Data Mining

Part III: Beyond Process Discovery

Chapter 7
Conformance
Checking

Chapter 8
Mining Additional
Perspectives

Chapter 9
Operational Support

Part II: From Event Logs to Process Models

Chapter 4
Getting the Data

Chapter 5
Process Discovery: An
Introduction

Chapter 6
Advanced Process
Discovery Techniques

Part IV: Putting Process Mining to Work

Chapter 10
Tool Support

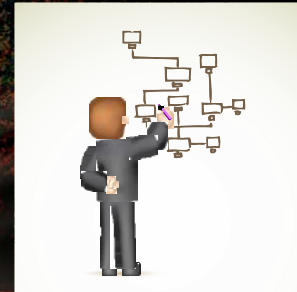
Chapter 11
Analyzing “Lasagna
Processes”

Chapter 12
Analyzing “Spaghetti
Processes”

Part V: Reflection

Chapter 13
Cartography and
Navigation

Chapter 14
Epilogue



Wil M. P. van der Aalst

Process Mining

Discovery, Conformance and
Enhancement of Business Processes

Springer

For more details see:
***W.M.P. van der Aalst, A. Adriansyah, and B. van Dongen.
Replaying History on Process Models for Conformance
Checking and Performance Analysis. WIREs Data Mining
and Knowledge Discovery, 2(2):182-192, 2012.***