

Advanced Sorting Algorithms and Datastructures

Marjahan Begum and Anders Kalhauge



Spring 2017

Sorting

- Divide and Conquer

- Merge Sort

- Quick Sort

Sorting

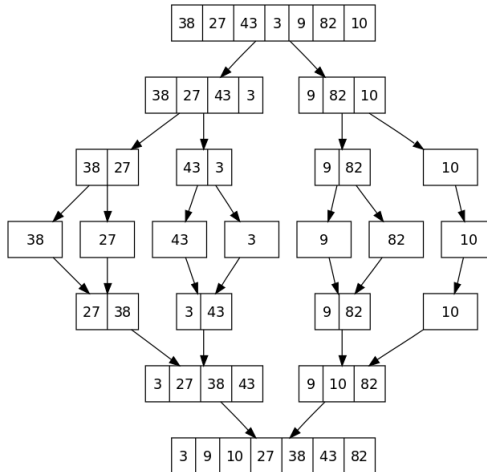
Divide and Conquer

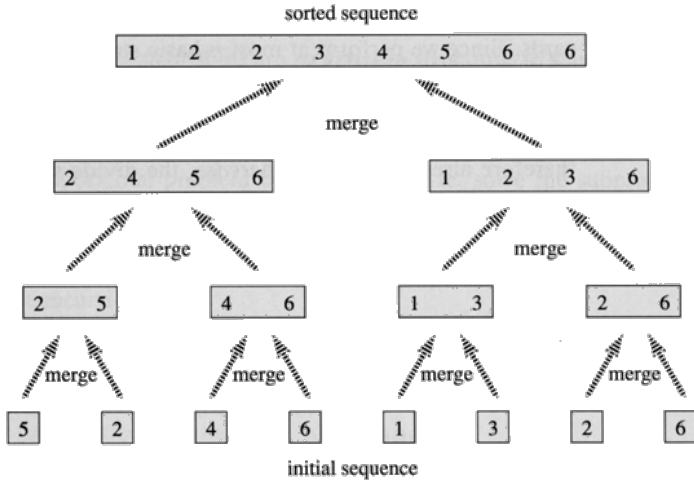
Merge Sort

Quick Sort

- Divide and break
 - Break the problem in to smaller sub-problem recursively
 - Sub-problem should represent a part of the original problem
 - Keep on dividing until no more division is possible
- Conquer/Solve
 - Smaller sub-problem are solved
 - Solutions of all the sub-problems are merged
- Merge/Combine
 - Recursively combines small solutions to the big solutions

Divide and Conquer





Quick sort doesn't use auxiliary space

1. Choose a pivot p , e.g: first element of array
2. Bring all element less than the pivot to one end of the array and all elements greater to the other.
3. Place the pivot in between.
4. Sort items left of the pivot
5. Sort items right of the pivot

		v	a[]															
	i	j	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Initial values	0	16	K	R	A	T	E	L	E	P	U	I	M	Q	C	X	O	S
scan left, scan right	1	12	K	R	A	T	E	L	E	P	U	I	M	Q	C	X	O	S
exchange	1	12	K	C	A	T	E	L	E	P	U	I	M	Q	R	X	O	S
scan left, scan right	3	9	K	C	A	T	E	L	E	P	U	I	M	Q	R	X	O	S
exchange	3	9	K	C	A	I	E	L	E	P	U	T	M	Q	R	X	O	S
scan left, scan right	5	6	K	C	A	I	E	L	E	P	U	T	M	Q	R	X	O	S
exchange	5	6	K	C	A	I	E	E	L	P	U	T	M	Q	R	X	O	S
scan left, scan right	6	5	K	C	A	I	E	E	L	P	U	T	M	Q	R	X	O	S
final exchange	6	5	E	C	A	I	E	K	L	P	U	T	M	Q	R	X	O	S
result		5	E	C	A	I	E	K	L	P	U	T	M	Q	R	X	O	S

Partitioning trace (array contents before and after each exchange)

- Show using pen and paper trace of sorting the string “EASYQUESTION” with top-down and bottom up merge sort.
- Re-design your `SortingAlgorithms` class. This time do the following:
 1. Implement a method for merge sort
 - 1.1 Create another method that checks if small arrays are already sorted
 - 1.2 Implement if possible, a merge sort without using an auxiliary array
 - 1.3 Implement a bottom up merge sort
 2. Implement one method for quick sort

Identify Big-O for all the above