

# COPENHAGEN BUSINESS ACADEMY



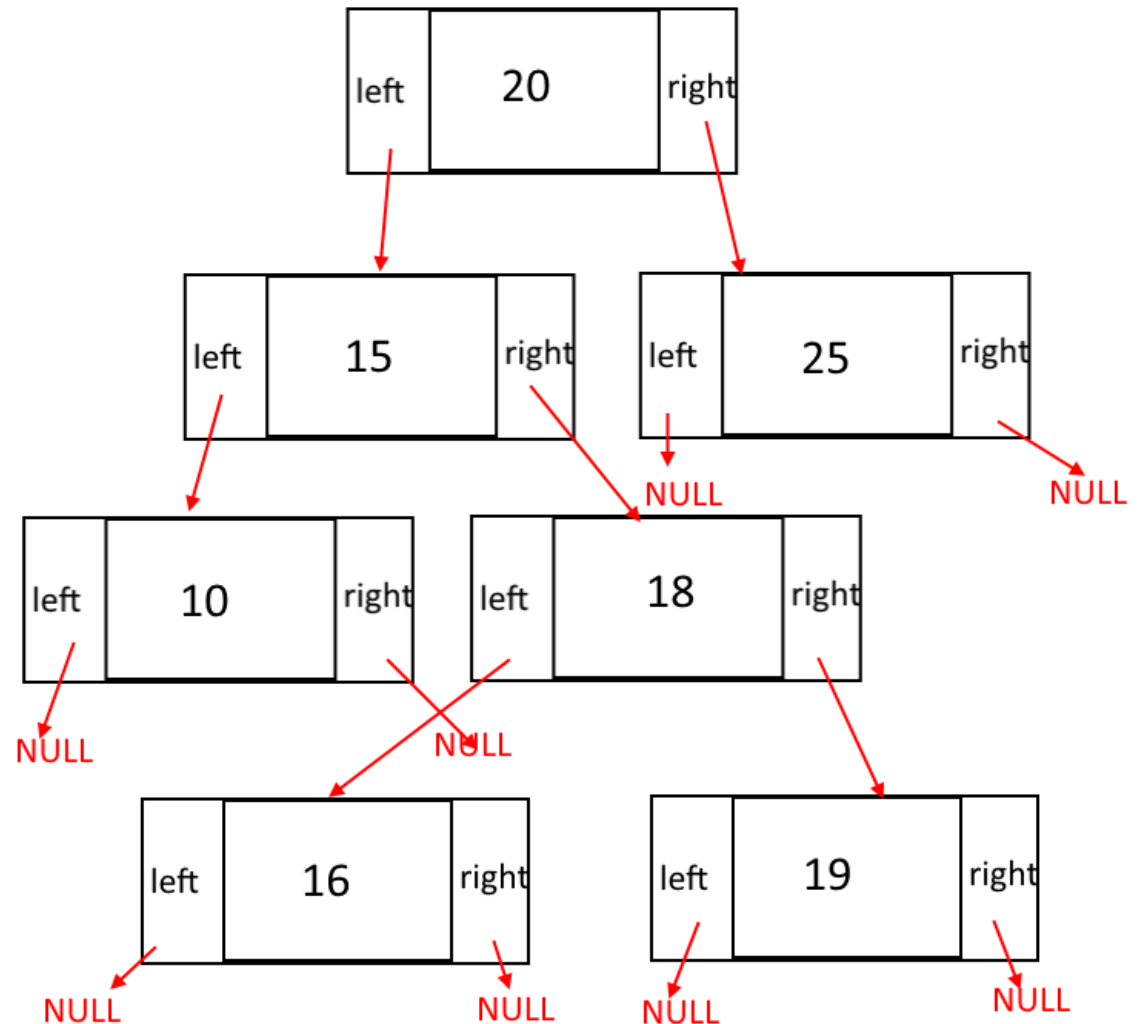
## Algorithms and Data Structure-Day3

# Today

- Classic Algorithms
  - Recursion
  - Merge sort
  - Quick sort
- Data Structures
  - Hash Table/Hash map
- Efficiency of algorithms
  - Big O

# Binary Search Tree (BST)

- All nodes smaller than root is on the left
- All nodes greater than root is on the right
- $O(\log(n))$  for a search



# Heapsort

- Ordered binary tree
- Max heap – parent  $>$  child
- Array of values
- Sort the array in location
- Left child =  $2*i + 1$
- Right child =  $2*i + 2$

# Binary Search Tree

- Balances and not Balanced binary tree
- Complete binary tree if all levels except possibly the last are completely filled with exception to the last level
- Divide and conquer
- Balanced binary tree makes the search quicker

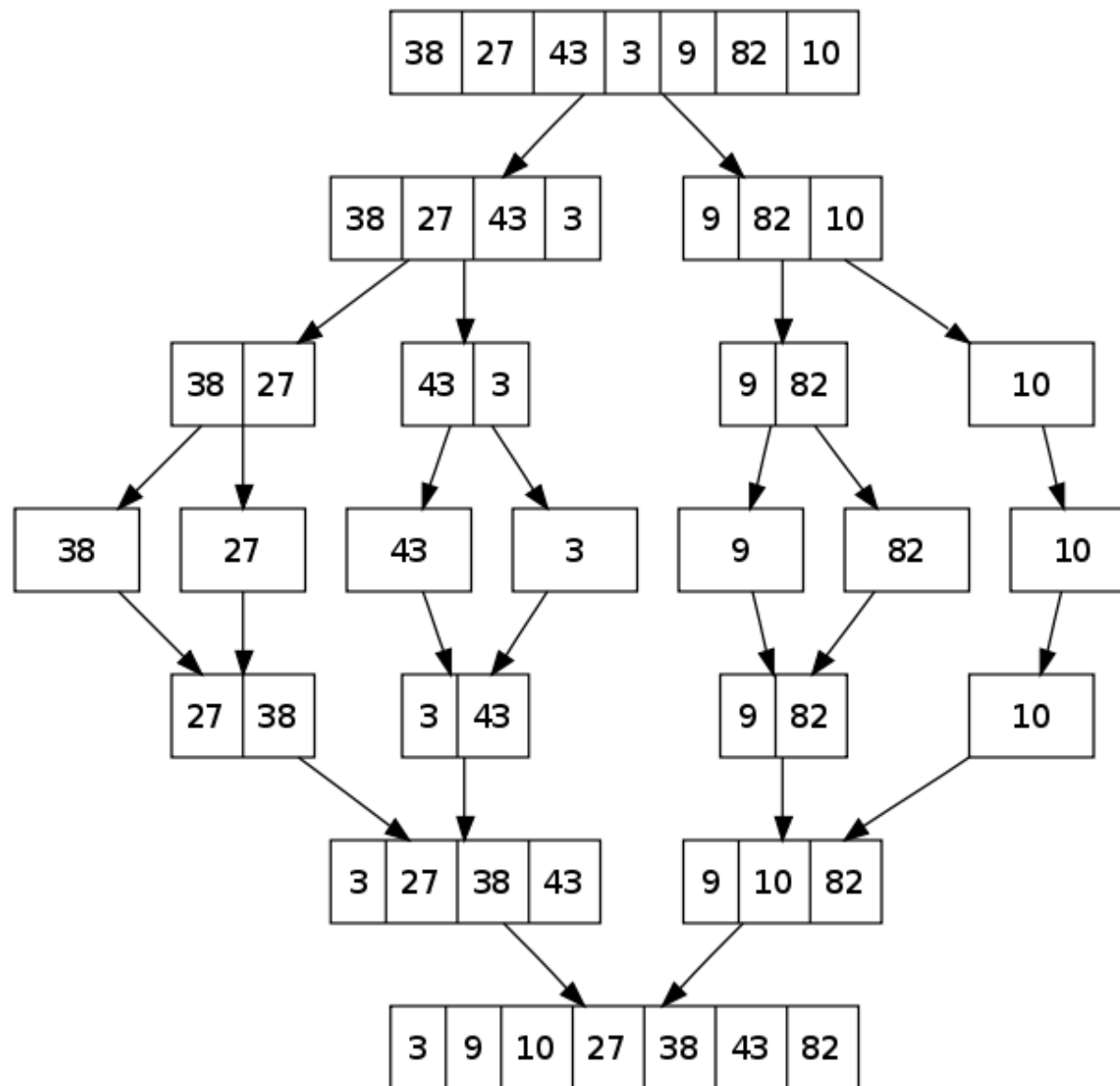
# Recursive Sorting

- Divide and Conquer
- Merge Sort
- Quick Sort

# Divide and Conquer

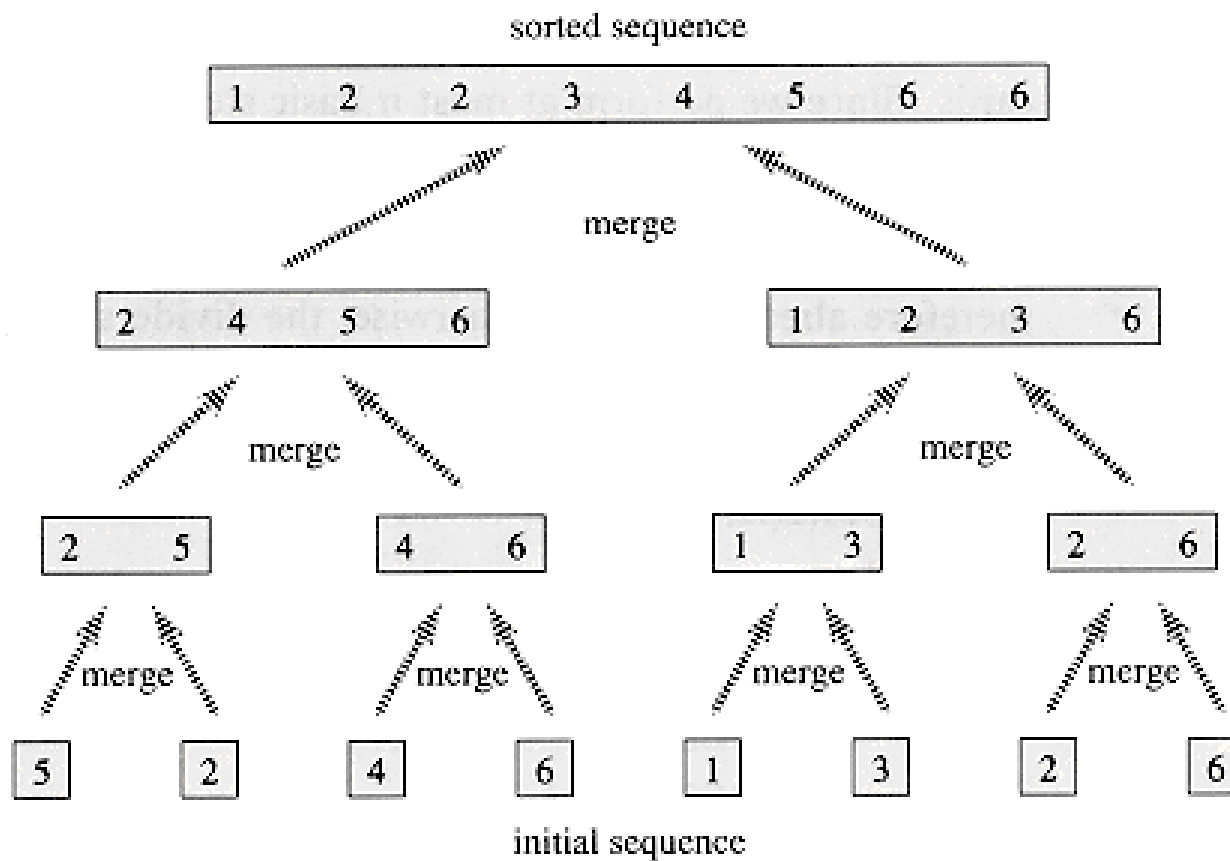
- Divide and break
  - Break the problem in to smaller sub-problem recursively
  - Sub-problem should represent a part of the original problem
  - Keep on dividing until no more division is possible
- Conquer/Solve
  - Smallest sub-problem are solved
  - Solutions of all the sub-problems are merged
- Merge/Combine
  - Recursively combines small solutions to the big solutions

# Merge Sort – top down

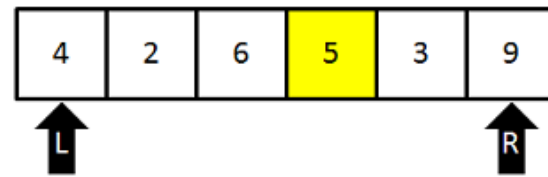




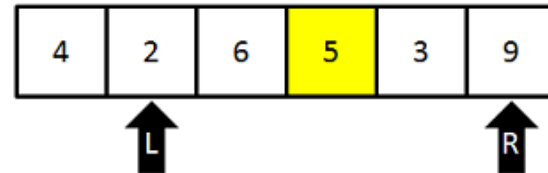
# Merge Sort – Bottom up



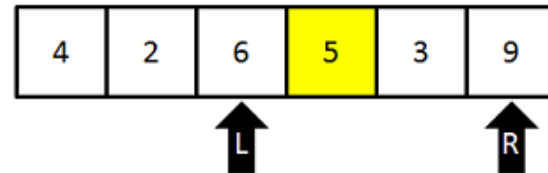
**Step 2**  
Start pointers at left and right



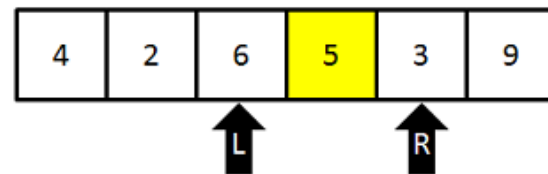
**Step 3**  
Since  $4 < 5$ , shift left pointer



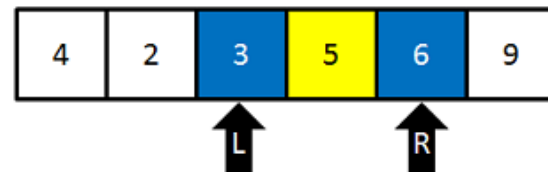
**Step 4**  
Since  $2 < 5$ , shift left pointer  
Since  $6 > 5$ , stop



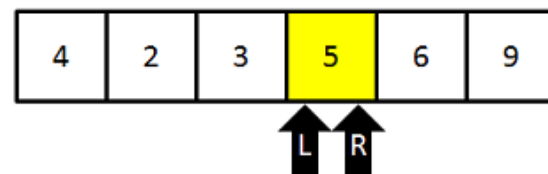
**Step 5**  
Since  $9 > 5$ , shift right pointer  
Since  $3 < 5$ , stop



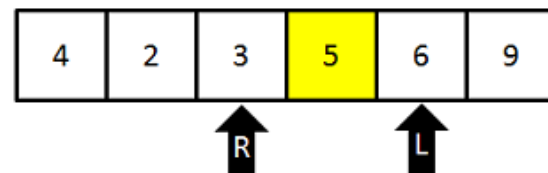
**Step 6**  
Swap values at pointers



**Step 7**  
Move pointers one more step



**Step 8**  
Since  $5 == 5$ ,  
move pointers one more step  
Stop



# Choice of data structure

|                    | Access                 | Search                 | Insert                 | Delete                 |
|--------------------|------------------------|------------------------|------------------------|------------------------|
| Array              | $O(1)$                 | $O(n)$                 | $O(n)$                 | $O(n)$                 |
| Linked List        | $O(n)$                 | $O(n)$                 | $O(1)$                 | $O(1)$                 |
| Binary Search Tree | $O(n)$<br>$O(\log(n))$ | $O(n)$<br>$O(\log(n))$ | $O(n)$<br>$O(\log(n))$ | $O(n)$<br>$O(\log(n))$ |
| HashTable          | ??                     | ??                     | ??                     | ??                     |

# Efficiency of algorithms

| Algorithm            | Time Complexity |
|----------------------|-----------------|
| Quicksort            | $O(n^2)$        |
| Merge sort           | $O(n \log(n))$  |
| Balanced binary tree | $O(\log n)$     |
| Heapsort             | $O(n \log(n))$  |
| Bubble sort          | $O(n^2)$        |
| Insertion sort       | $O(n^2)$        |
| Selectio sort        | $O(n^2)$        |