

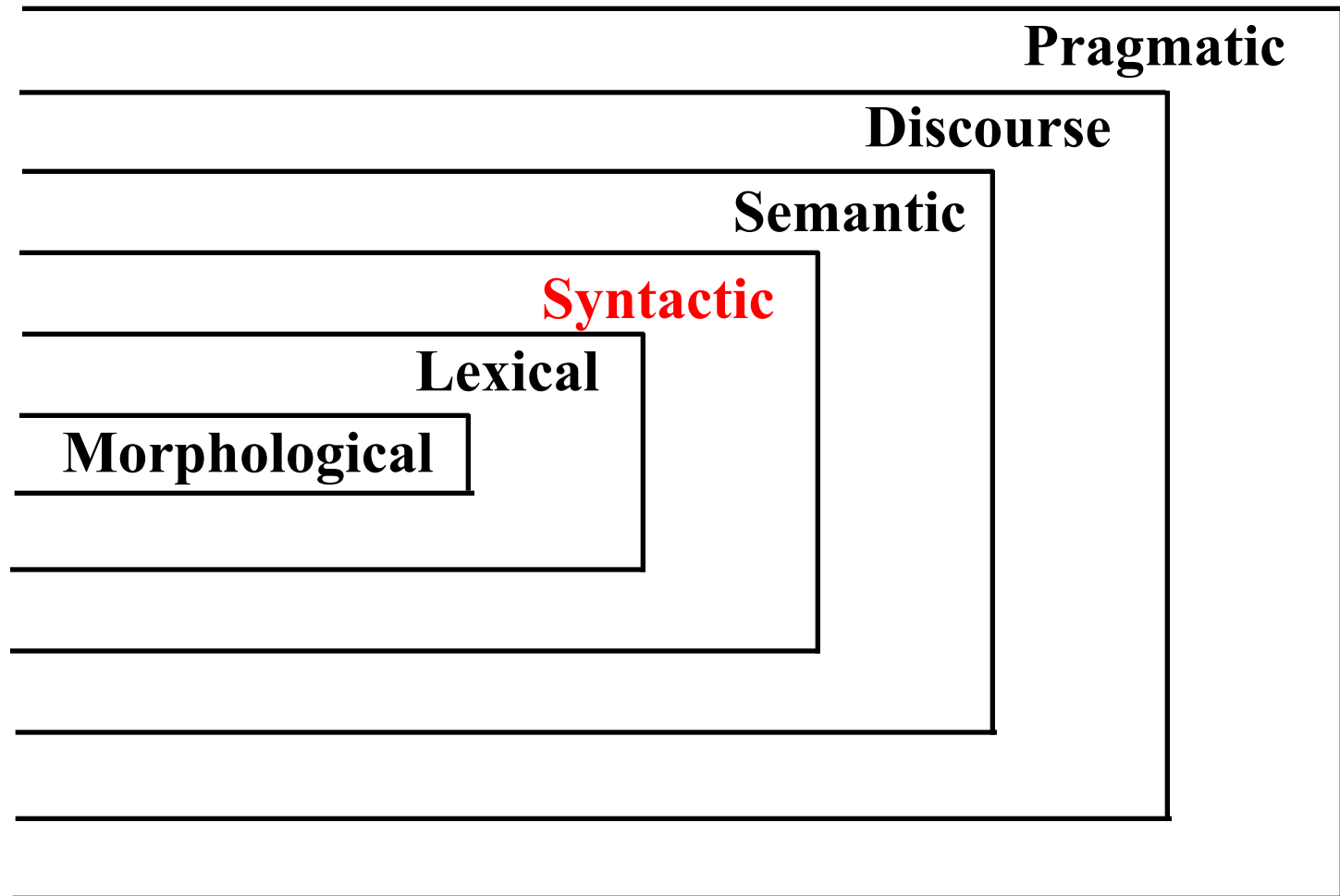
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# Introduction to Context Free Grammars



# Synchronic Model of Language

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# Syntactic Analysis

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- Syntax expresses the way in which words are arranged together.
- The kind of implicit knowledge of your native language that you had mastered by the time you were 3 or 4 years old without explicit instruction
  - Do these word sequences fit together?  
*I saw you yesterday*  
*you yesterday I year*  
  
*colorless green ideas sleep furiously*      (Chomsky)  
*furiously sleep ideas green colorless*
- NLP uses syntax to produce a structural analysis of the input sentence

# Formal Grammar

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- Rules that embody generalizations that hold for the symbols and combinations of symbols in a language for constructing acceptable sentences
  - grammar is most closely identified with syntax, but may contain elements of all levels of language
- Theoretical linguists use grammar
  - To indicate which are the well-formed sentences, defining that language
  - To show how variations of a ‘deep-structure’ are derived through ‘transformations’ on this ‘deep-structure’
  - Competence based – an ideal speaker’s internalized ability to create and understand all sentences
- Applied uses
  - To assign a structural description to the linguistic elements of which an utterance is comprised
  - “...typically not consciously modeled after any particular linguistic theory, but as descriptions of phenomena that appeared in input text.”
  - ‘Performance’ based – person’s actual use of language

# Context-Free Grammars

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- Capture **constituency and ordering**
  - Ordering is
    - What are the rules that govern the ordering of words and bigger units in the language
  - Constituency is
    - **How do words group into units and what we say about how the various kinds of units behave**
    - A constituent is a sequence of words that behave as a unit
      - John talked [to the children] [about drugs].
      - John talked [about drugs] [to the children].
      - \*John talked drugs to the children about (random reorder)
    - Constituents can be expanded or substituted for:
      - I sat [on the box/right on top of the box/there]
    - Other properties: Coordination, regular internal structure, no intrusion, fragments, semantics, ...

# Context-Free Grammar consists of:

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- **Non-terminal symbols**

S, NP, VP, etc. representing the constituents  
or categories of phrases

- **Terminal symbols**

*car, man, house*, representing words in the lexicon

- The rewrite rules will include lexical insertion rules  
(e.g.  $N \rightarrow car \mid man \mid house$ )

- **Rewrite rules / productions**

$S \rightarrow NP VP \mid VP$

(note use of  $\mid$  symbol to give alternate rhs of rules)

- A designated start symbol S
- A **derivation** is a sequence of rewrite rules applied to a string that exactly covers the items in that string

# Derivation of syntax from grammar rules

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- *Given the grammar and a sentence,  
Show top-down derivation of a parse tree.*

*the*                      *man*                      *eats*                      *the*                      *apple*

Context Free Grammar Rules (for this example):

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

$VP \rightarrow VB$

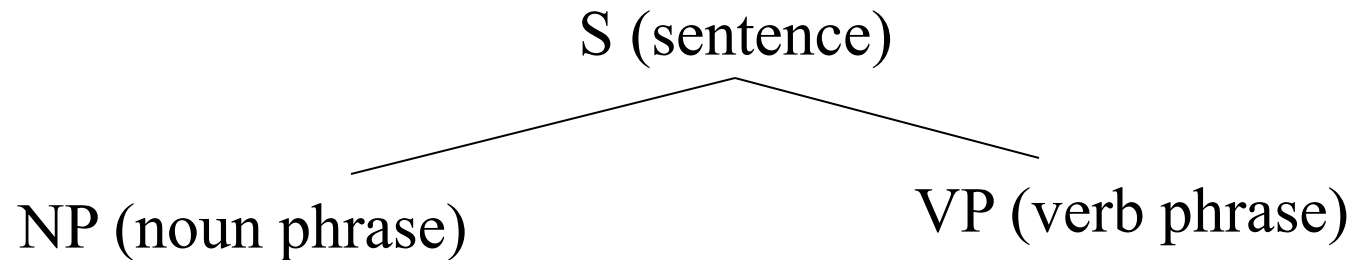
$DT \rightarrow the \mid \dots$

$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

# Top Down Derivation – starts with S

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*the*                      *man*                      *eats*                      *the*                      *apple*

Context Free Grammar Rules:

**S** → NP VP

NP → DT NN

VP → VB NP

VP → VB

DT → *the* | ...

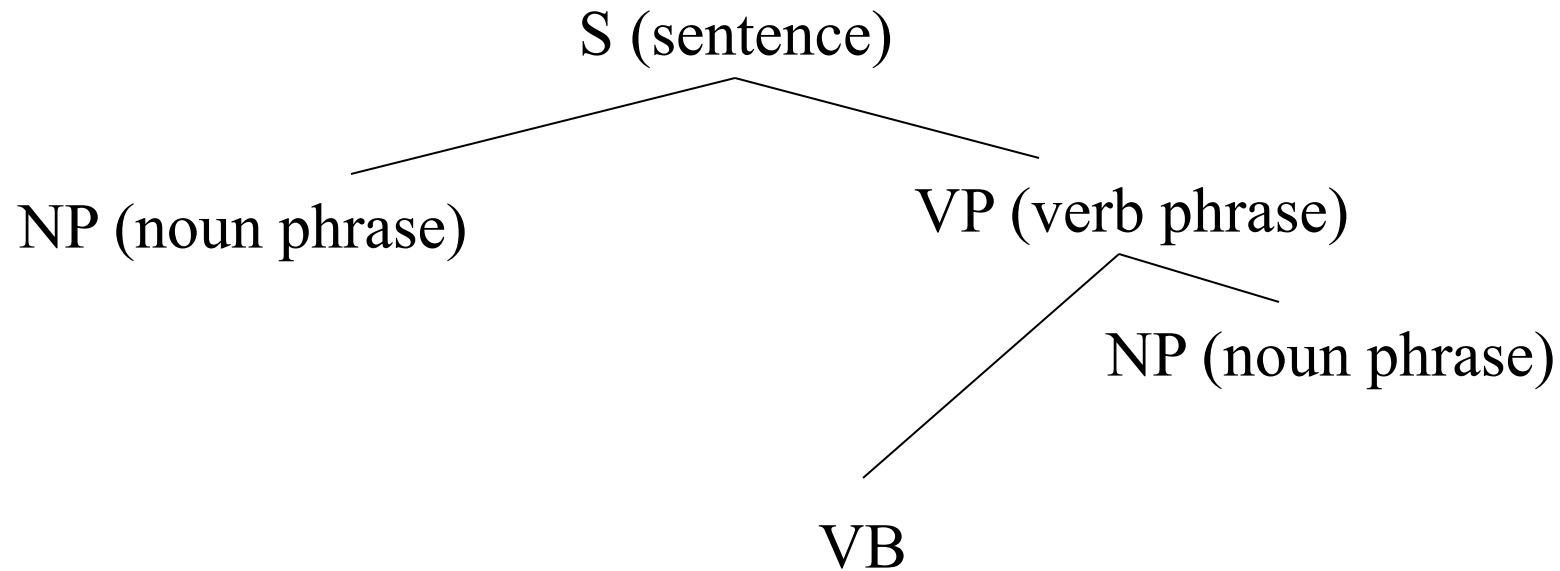
NN → *man* | *apple* | ... (add words)

VB → *eats* | ...



# Top Down Derivation – add rule for VP

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*the*

*man*

*eats*

*the*

*apple*

Context Free Grammar Rules:

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

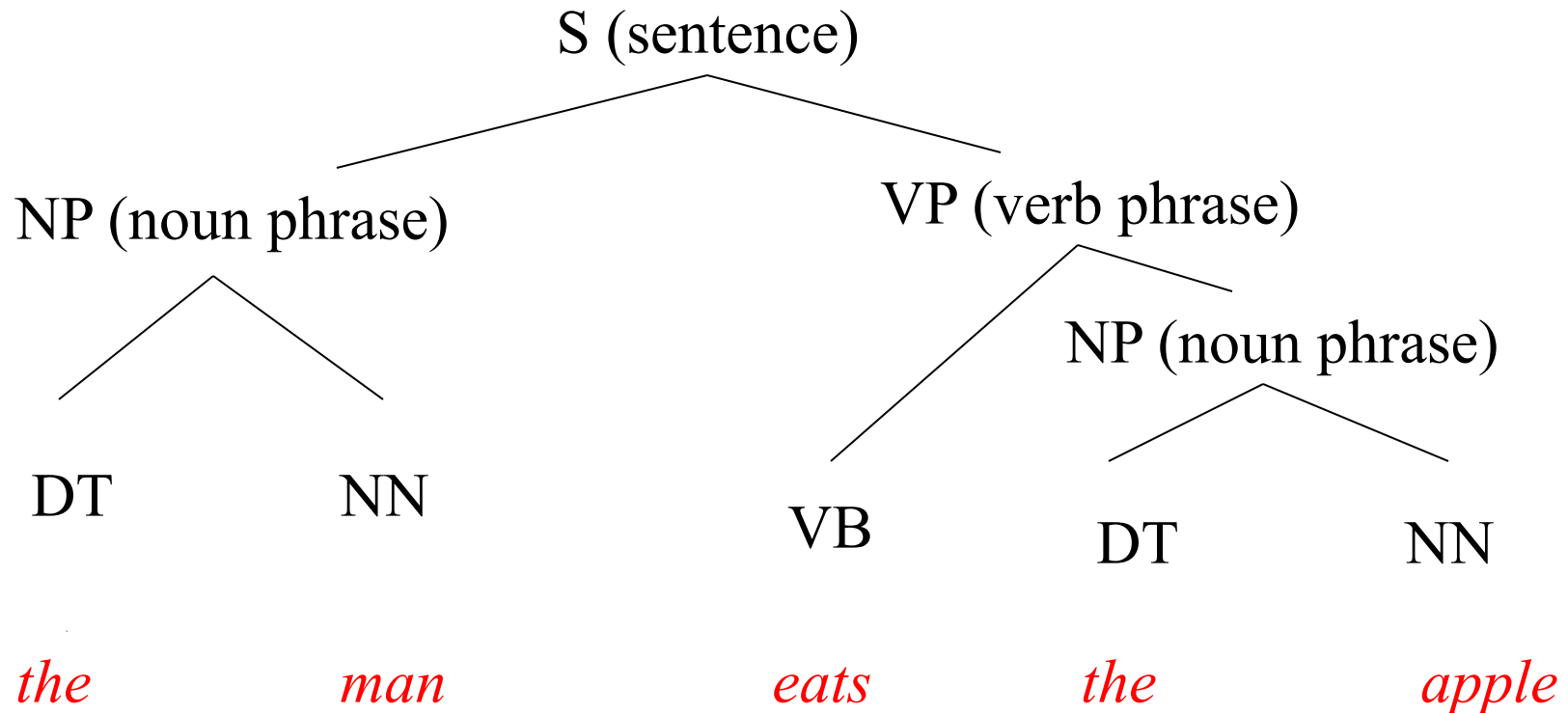
$VP \rightarrow VB$

$DT \rightarrow the \mid \dots$

$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

# Top Down Derivation – add rules for NP



Context Free Grammar Rules:

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

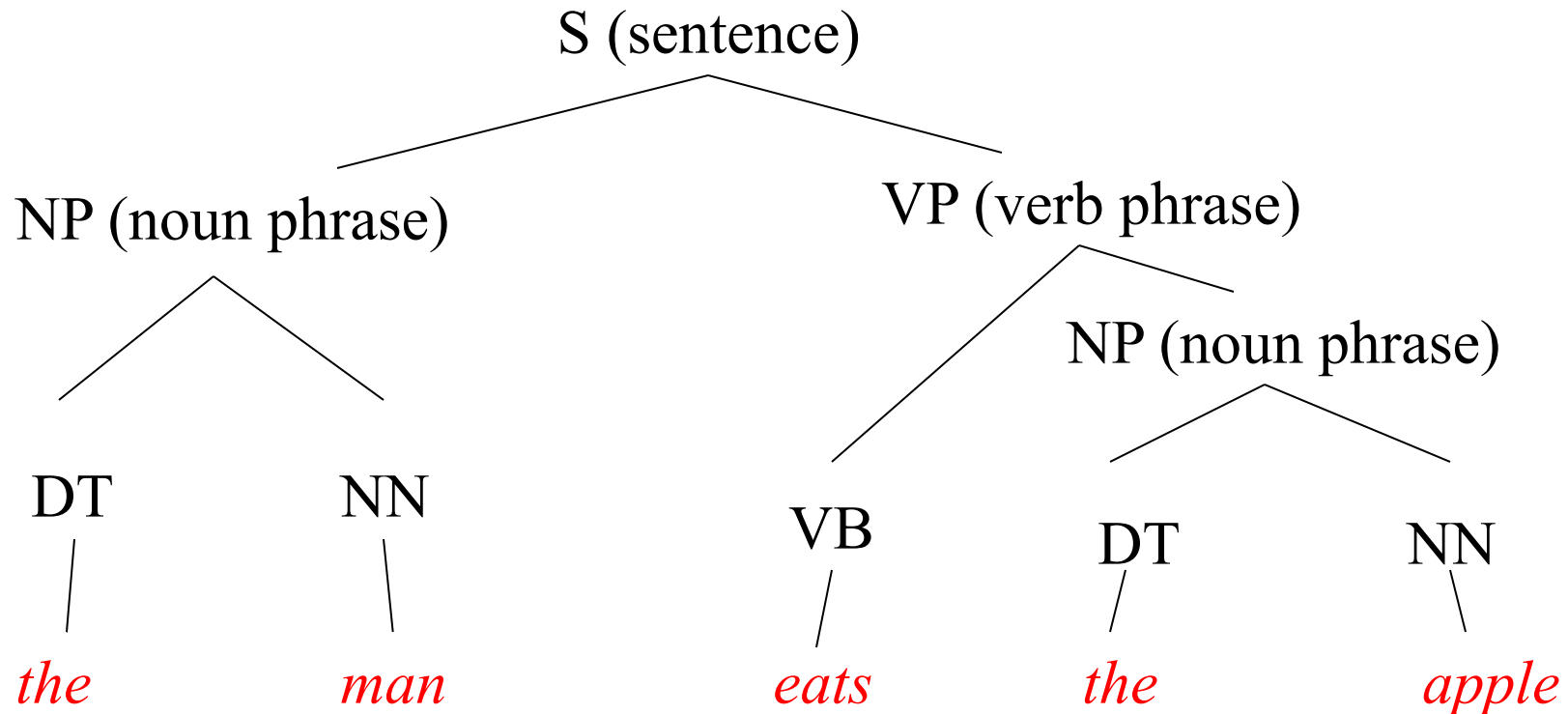
$VP \rightarrow VB$

$DT \rightarrow the \mid \dots$

$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

# Top Down Derivation – add POS/lexical rules



Context Free Grammar Rules:

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

$VP \rightarrow VB$

$DT \rightarrow the \mid \dots$

$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

# Derivation of syntax from grammar rules

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- *Given the grammar and a sentence,  
Show bottom-up derivation of a parse tree.*

*the*                      *man*                      *eats*                      *the*                      *apple*

Context Free Grammar Rules (for this example):

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

$VP \rightarrow VB$

$DT \rightarrow the \mid \dots$

$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

# Bottom Up Derivation – start with POS/lexical rules

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DT

|

*the*

NN

|

*man*

VB

|

*eats*

DT

|

*the*

NN

|

*apple*

Context Free Grammar Rules:

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

$VP \rightarrow VB$

$DT \rightarrow the \mid \dots$

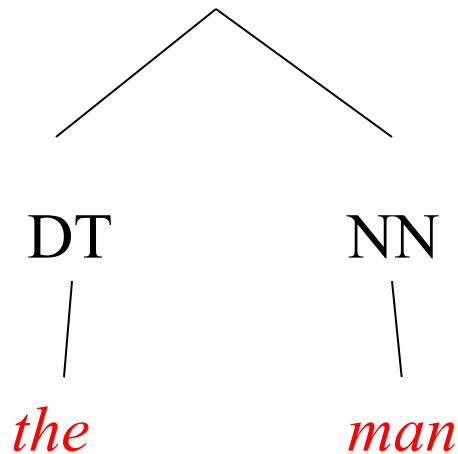
$NN \rightarrow man \mid apple \mid \dots \text{ (add words)}$

$VB \rightarrow eats \mid \dots$

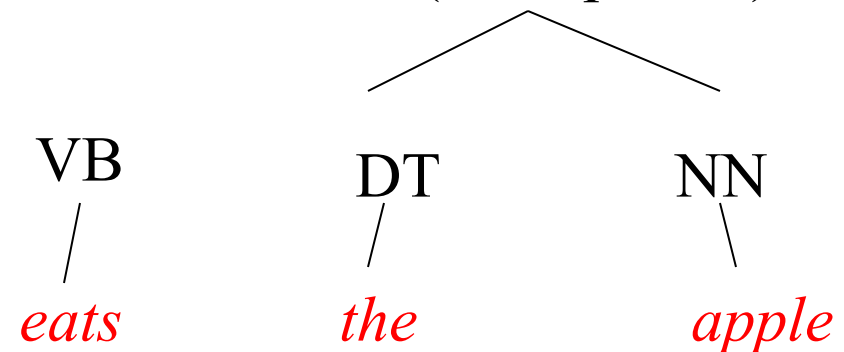
# Bottom Up Derivation – add NP rules

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NP (noun phrase)



NP (noun phrase)



Context Free Grammar Rules:

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

$VP \rightarrow VB$

$DT \rightarrow the \mid \dots$

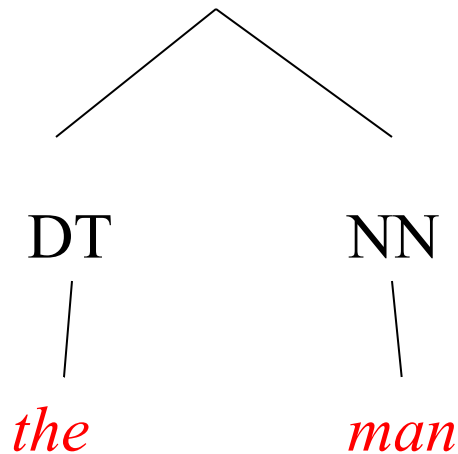
$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

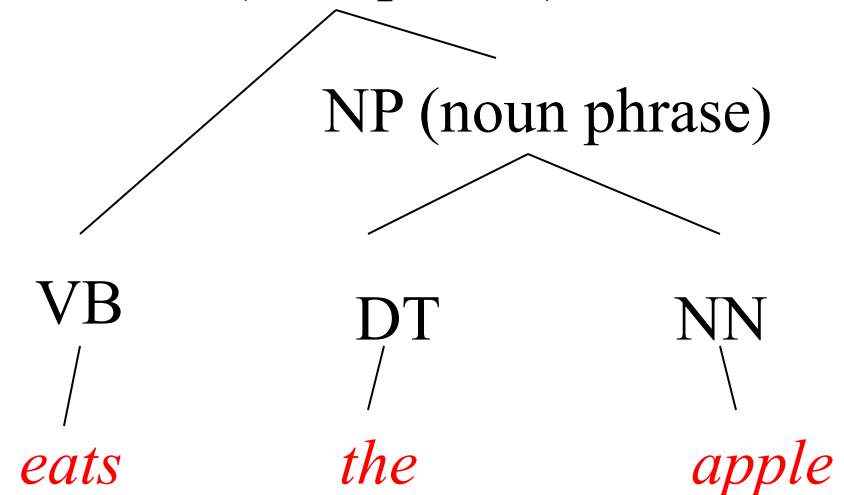
# Bottom Up Derivation – add VP rule

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NP (noun phrase)



VP (verb phrase)



Context Free Grammar Rules:

$S \rightarrow NP VP$

$NP \rightarrow DT NN$

$VP \rightarrow VB NP$

$VP \rightarrow VB$

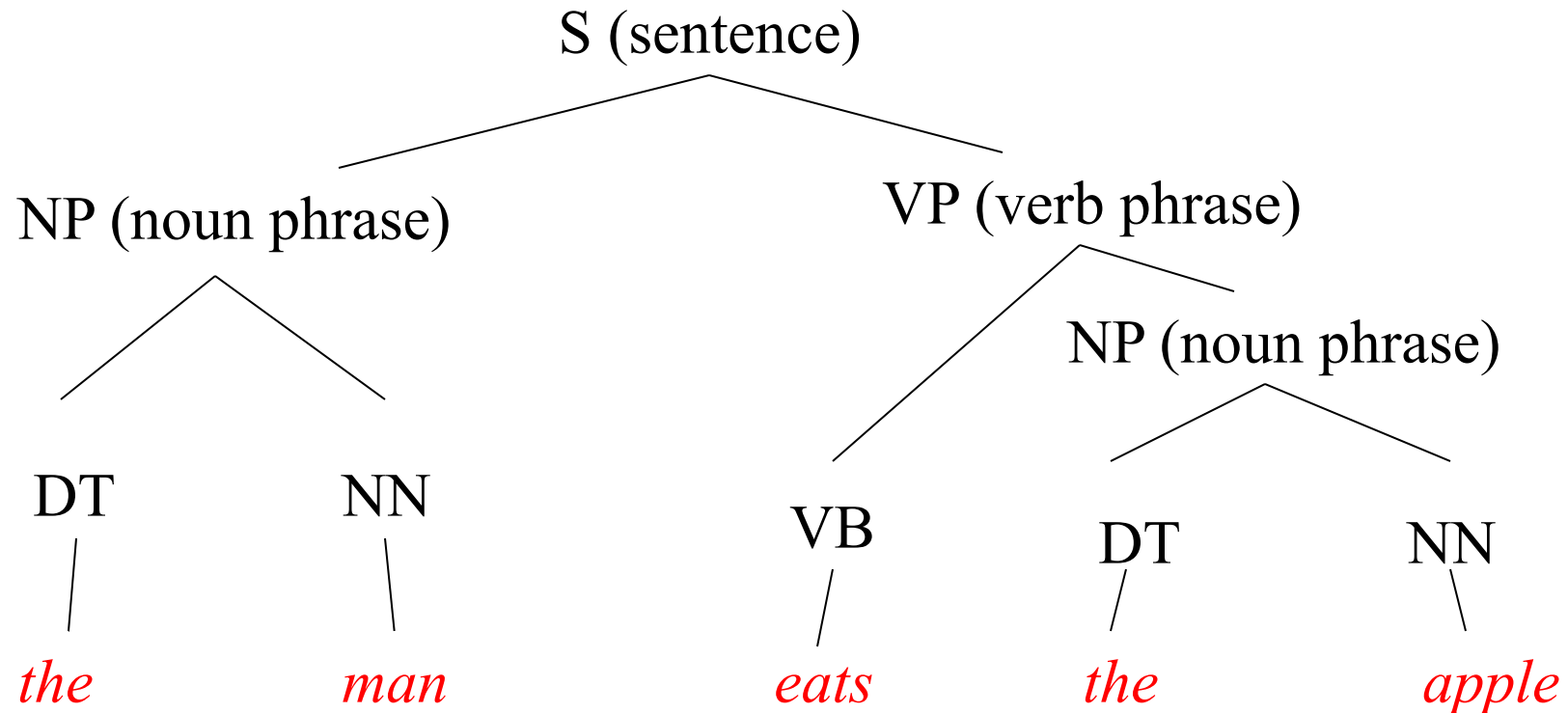
$DT \rightarrow the \mid \dots$

$NN \rightarrow man \mid apple \mid \dots$  (add words)

$VB \rightarrow eats \mid \dots$

# Bottom Up Derivation – add S rule

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Context Free Grammar Rules:

**S** → NP VP

NP → DT NN

VP → VB NP

VP → VB

DT → *the* | ...

NN → *man* | *apple* | ... (add words)

VB → *eats* | ...



# Notations for (constituent) syntactic structure

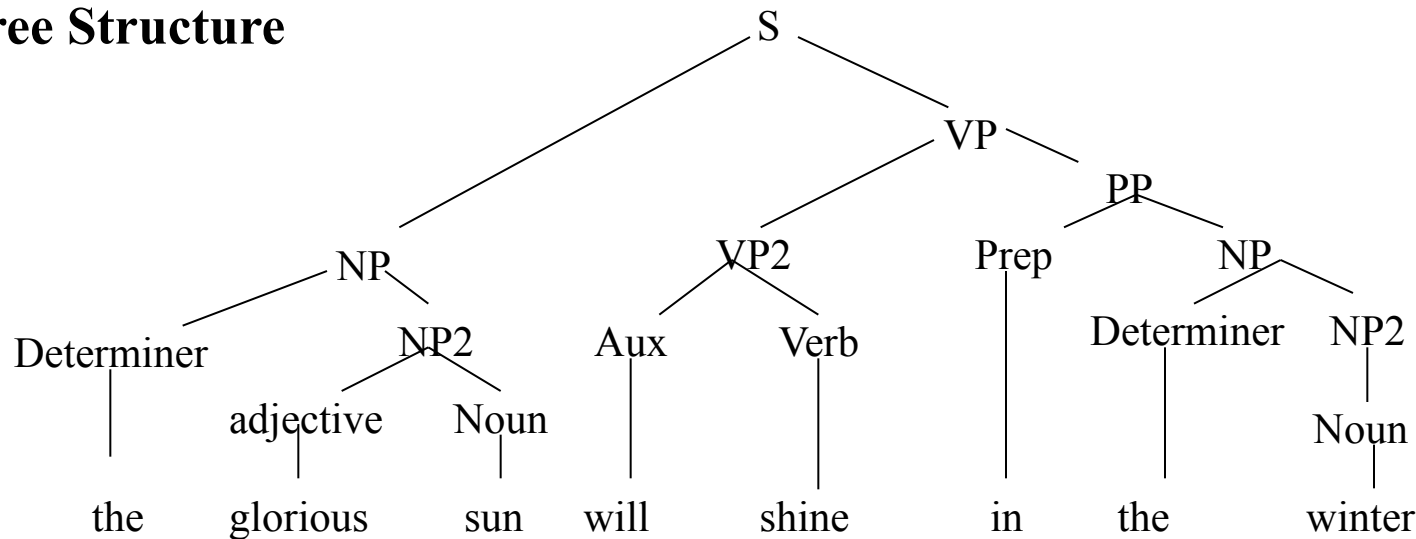
## Bracketed text

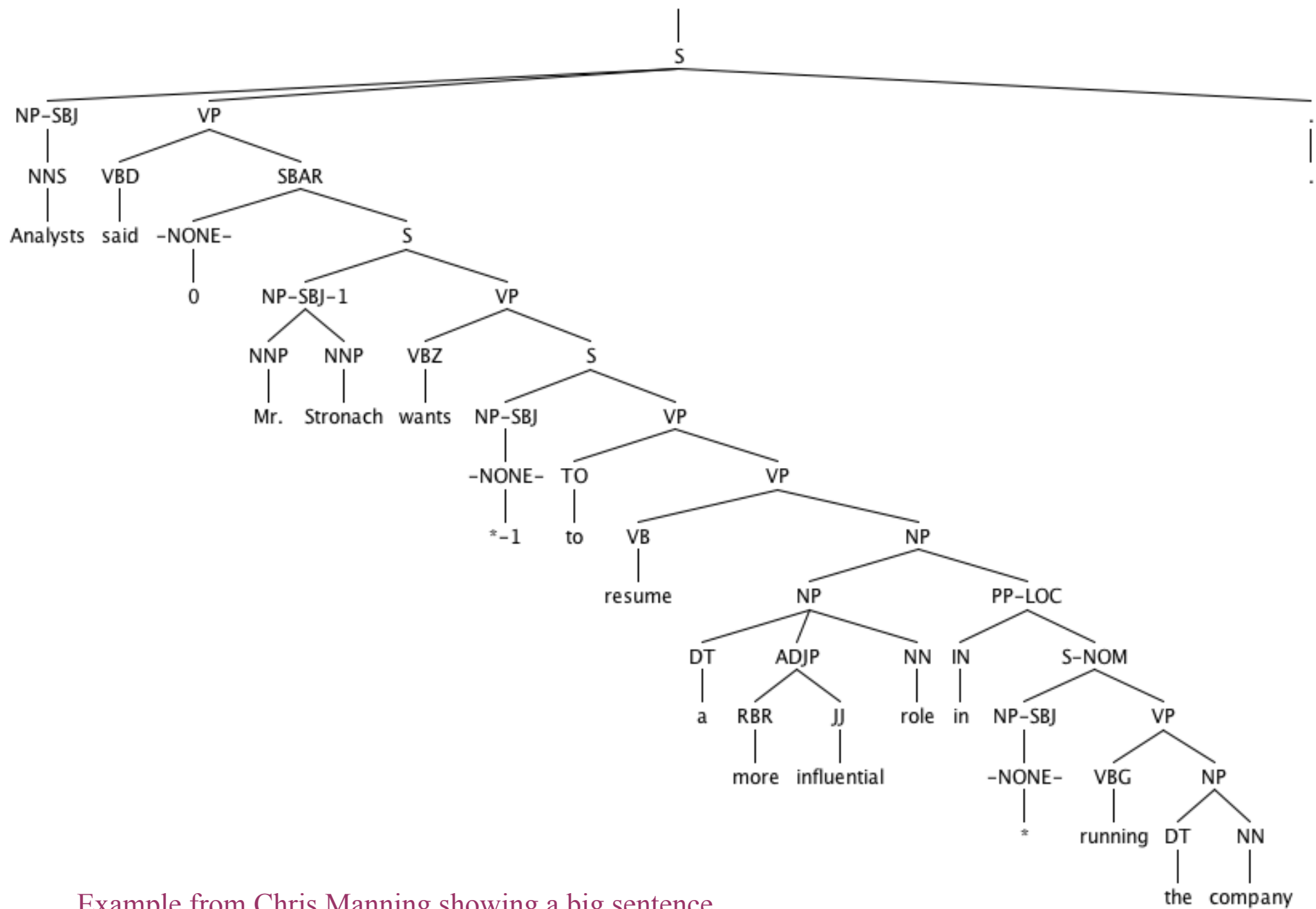
[<sub>S</sub> [<sub>NP</sub> the [<sub>NP2</sub> glorious sun]] [<sub>VP</sub> [<sub>VP2</sub> will shine] [<sub>PP</sub> in [<sub>NP</sub> the [<sub>NP2</sub> winter]]]]]

## Indented bracketed text

(S  
  (NP (DT The) (JJ glorious) (NN sun))  
  (VP (MD will)  
    (VP (VB shine)  
      (PP (IN in)  
        (NP (DT the) (NN winter))))))

## Tree Structure





Example from Chris Manning showing a big sentence with nested constituents and empty elements.

# Generativity vs. Parsing

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- You can view these rules as either synthesis or analysis machines
  - Generate strings in the language
  - Reject strings not in the language
  - Impose structures (trees) on strings in the language
- The latter two are the analysis tasks of parsing
  - Parsing is the process of finding a derivation (i. e. sequence of productions) leading from the START symbol to a TERMINAL symbol (or TERMINALS to START symbol)
  - Shows how **a particular sentence *could be* generated by the rules of the grammar**
  - If sentence is structurally ambiguous, **more than one possible derivation is produced**

# Context-Free Grammars

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- Why Context-Free?
  - The notion of **context** in CFGs has nothing to do with the ordinary meaning of the word context in language.
  - All it really means is that the non-terminal on the left-hand side of a rule can be replaced regardless of context
    - Context-sensitive grammars allow context to be placed on the left-hand side of the rewrite rule
- In programming languages, and other uses of CFGs in Computer Science, notably XML, CFGS are
  - Unambiguous
    - Assign at most, 1 structural description to a string
  - Parsable in time linearly proportional to the length of the string